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# In Situ Characterization of Mixtures of Linear and Branched Hydrocarbons Confined within Porous Media Using 2D DQF-COSY NMR Spectroscopy 

Qingyuan Zheng, Mick D. Mantle, Andrew J. Sederman, Timothy A. Baart, Constant M. Guédon, and Lynn F. Gladden*



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#### Abstract

The analysis of 1D anti-diagonal spectra from the projections of 2D double-quantum filtered correlation spectroscopy NMR spectra is presented for the determination of the compositions of liquid mixtures of linear and branched alkanes confined within porous media. These projected spectra do not include the effects of line broadening and therefore retain high-resolution information even in the presence of inhomogeneous magnetic fields as are commonly found in porous media. A partial least-square regression analysis is used to characterize the mixture compositions. Two case studies are considered. First, mixtures of 2 -methyl alkanes and $n$-alkanes are investigated. It is shown that estimation of the $\mathrm{mol} \%$ of branched species present was mixture of linear and branched alkanes confined in a porous titania   achieved with a root-mean-square error of prediction (RMSEP) of 1.4 $\mathrm{mol} \%$. Second, the quantification of multicomponent mixtures consisting of linear alkanes and 2-, 3-, and 4-monomethyl alkanes was considered. Discrimination of 2-methyl and linear alkanes from other branched isomers in the mixture was achieved, although discrimination between 3- and 4- monomethyl alkanes was not possible. Compositions of the linear alkane, 2-methyl alkane, and the total composition of 3- and 4-methyl alkanes were estimated with a RMSEP $<3 \mathrm{~mol} \%$. The approach was then used to estimate the composition of the mixtures in terms of submolecular groups of $\mathrm{CH}_{3} \mathrm{CH}_{2},\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}$, and $\mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right) \mathrm{CH}_{2}$ present in the mixtures; a RMSEP $<1 \mathrm{~mol} \%$ was achieved for all groups. The ability to characterize the mixture compositions in terms of molecular subgroups allows the application of the method to characterize mixtures containing multimethyl alkanes. The motivation for this work is to develop a method for determining the mixture composition inside the catalyst pores during Fischer-Tropsch synthesis. However, the method reported is generic and can be applied to any system in which there is a need to characterize mixture compositions of linear and branched alkanes.


## INTRODUCTION

The ability to characterize the composition of a reaction mixture inside the pore space of a catalyst provides a powerful tool to probe how the catalyst formulation and pore structure and reactor operating conditions influence the product composition and hence provides insight into catalyst performance. This work reports an experimental methodology for characterizing the hydrocarbon mixtures forming inside catalyst pores with a particular focus on discriminating linear and branched hydrocarbons. This is of particular interest with regard to gaining insight into the catalytic mechanism and the resulting product composition.
Analytical techniques such as gas chromatography, ${ }^{1,2}$ mass spectroscopy, ${ }^{3,4}$ and nuclear magnetic resonance (NMR) ${ }^{5-10}$ spectroscopy are routinely used to characterize hydrocarbon mixtures in the bulk liquid phase; in the context of catalysts and catalytic processes, such mixtures might be the liquid product of the catalytic reaction or the liquid mixture extracted from the pore space. With regard to NMR, $1 \mathrm{D}{ }^{13} \mathrm{C} \mathrm{NMR}^{5-8}$
and ${ }^{1} \mathrm{H}$ 2D correlation spectroscopy (COSY) ${ }^{10}$ have been applied to characterize the types and compositions of branched alkanes in bulk liquid mixtures of hydrocarbons. More generally, 2D NMR spectroscopy is established as a powerful tool in identifying the molecular structure and thus discriminating chemical species in complex mixtures. ${ }^{11-13}$ However, the application of NMR to characterize such mixtures inside the pores of heterogeneous catalysts is significantly hindered by line broadening of the NMR signal due to the enhanced field inhomogeneity characteristic of porous media. Application to the characterization of liquid

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Table 1. Estimation of the Compositions of Chemicals and Submolecular Groups in the Samples TM1-TM19 Using the PLSR Models ${ }^{a}$

| samples | chemical composition [mol \%] |  |  | group composition [mol \%] |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | linear | 2-methyl | 3- + 4-methyl | group 1 | group 2 | group 3 |
| TM1 | 95.2 (94.4) | 4.8 (5.6) | 0 | 97.6 (97.2) | 2.4 (2.8) | 0 |
| TM2 | 92.0 (90.2) | 8.0 (9.8) | 0 | 96.0 (95.1) | 4.0 (4.9) | 0 |
| TM3 | 86.2 (84.6) | 13.8 (15.4) | 0 | 93.1 (92.3) | 6.9 (7.7) | 0 |
| TM4 | 81.7 (80.0) | 18.3 (20.0) | 0 | 90.8 (90.0) | 9.2 (10.0) | 0 |
| TM5 | 58.5 (60.0) | 41.5 (40.0) | 0 | 79.2 (80.0) | 20.8 (20.0) | 0 |
| TM6 | 38.1 (40.0) | 61.9 (60.0) | 0 | 69.1 (70.0) | 31.0 (30.0) | 0 |
| TM7 | -0.5 (0) | 100.5 (100.0) | 0 | 49.8 (50.0) | 50.3 (50.0) | 0 |
| TM8 | 89.7 (89.2) | 10.3 (10.8) | 0 | 94.8 (94.6) | 5.2 (5.4) | 0 |
| TM9 | 88.6 (89.6) | 11.4 (10.4) | 0 | 94.3 (94.8) | 5.7 (5.2) | 0 |
| TM10 | 30.9 (32.9) | 30.3 (33.4) | 38.8 (33.7) | 67.1 (66.4) | 14.4 (16.7) | 18.5 (16.9) |
| TM11 | 29.1 (24.5) | 24.6 (25.2) | 46.3 (50.2) | 67.7 (66.5) | 11.0 (11.2) | 21.3 (22.3) |
| TM12 | 60.7 (60.0) | 7.4 (8.6) | 32.0 (31.5) | 81.2 (81.1) | 3.7 (4.0) | 15.1 (14.8) |
| TM13 | 70.3 (70.1) | 8.9 (9.4) | 20.8 (20.4) | 86.5 (85.7) | 4.0 (4.5) | 9.5 (9.8) |
| TM14 | 79.2 (78.0) | 3.5 (3.8) | 17.3 (18.2) | 90.6 (89.4) | 1.6 (1.8) | 7.8 (8.8) |
| TM15 | 82.7 (87.8) | 4.8 (3.7) | 12.4 (8.4) | 92.1 (94.0) | 2.2 (1.8) | 5.7 (4.2) |
| TM16 | 63.4 (59.9) | 8.9 (7.9) | 27.7 (32.2) | 81.7 (81.1) | 4.5 (3.7) | 13.9 (15.2) |
| TM17 | 70.0 (69.6) | 10.0 (8.9) | 20.0 (21.5) | 85.1 (85.4) | 4.9 (4.3) | 9.9 (10.3) |
| TM18 | 79.8 (79.4) | 4.7 (4.1) | 15.6 (16.4) | 89.9 (90.0) | 2.4 (2.0) | 7.8 (8.0) |
| TM19 | 86.6 (90.0) | 3.6 (2.8) | 9.8 (7.2) | 93.3 (95.1) | 1.8 (1.4) | 4.9 (3.6) |

${ }^{a}$ The $\mathrm{CH}_{3} \mathrm{CH}_{2},\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}$, and $\mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right) \mathrm{CH}_{2}$ groups are denoted as groups 1,2, and 3, respectively, in the table. The estimated chemical and group compositions have standard errors of $\pm 0.4$ and $\pm 0.2 \mathrm{~mol} \%$, respectively. The values in brackets are the compositions measured gravimetrically. Samples TM10-TM15 are prepared as bulk liquid mixtures. Samples TM1-TM9 and TM16-TM19 are prepared as liquid mixtures confined within the porous titania.
mixtures and, in particular, the identification of branched hydrocarbon species while inside catalyst pores has been reported. One such example is the measurement of iso-butane composition during $n$-butane isomerization. ${ }^{9}$ However, to achieve this measurement, ${ }^{13} \mathrm{C}$ magic-angle spinning solid-state NMR was employed, which cannot be used in studying catalysts working inside a packed-bed reactor operating under industrially relevant conditions. Recently, Terenzi et al. ${ }^{14}$ applied COSY to determine the carbon number of pure $n$ alkanes and $n$-alkane mixtures confined within a porous titania. The 2D COSY spectra were projected along the diagonal direction to form anti-diagonal projected spectra. It was reported that while line broadening was observed along the main diagonal direction of the 2D spectra, the line-broadening effect was not observed in the anti-diagonal direction and therefore in the anti-diagonal projected spectra. ${ }^{14}$ This absence of line broadening is explained by the fact that spectral properties perpendicular to the diagonal are determined by intramolecular properties, such as the chemical shift difference $\Delta \delta$ between coupled ${ }^{1} \mathrm{H}$ nuclei and the corresponding $J$ coupling constants, which remain unchanged in the presence of magnetic field inhomogeneity. Therefore, high spectral resolution is retained in the 1 D projection along the main diagonal direction; herein, we refer to the 1D projection of the main diagonal as the anti-diagonal spectrum. As a result, the 1D anti-diagonal spectrum of a 2D COSY experiment can be used for the quantitative analysis of mixtures confined within porous media.
While the 2D COSY pulse sequence should, in principle, enable acquisition of the information required for the characterization of the liquid mixtures inside the pore space, the standard COSY pulse sequence is limited in its application because of the intense diagonal signal which suffers from significant $t_{1}$ noise. ${ }^{11,15}$ As a result, the analysis of cross-peaks,
which contain the information on the molecular structure needed to discriminate branched and linear alkanes, can be significantly obscured. To overcome this problem, the ${ }^{1} \mathrm{H}$ double-quantum filtered (DQF) COSY technique ${ }^{11,16}$ is used. The DQF-COSY pulse sequence yields an anti-phase multiplet signal along the main diagonal; ${ }^{11}$ the positive and negative parts of these anti-phase multiplets act to cancel out each other and result in the suppression of the signal along the main diagonal and the associated $t_{1}$ noise. Apart from reduced signal intensities due to the application of the double-quantum filter, ${ }^{11}$ the characteristics of DQF-COSY cross-peaks, and hence the associated analysis of the spectra, are the same as those acquired with COSY.

In this work, $2 \mathrm{D}{ }^{1} \mathrm{H}$ DQF-COSY spectroscopy is used to enable the discrimination and quantification of the chemical species in mixtures confined in porous media. Such measurement would be impossible to achieve by 1D NMR spectroscopy because of the line-broadening effect. The method is demonstrated in application to the characterization of mixtures of branched and linear alkanes. The measurement is of immediate relevance to Fischer-Tropsch (FT) synthesis, although the characterization of branched alkanes within $n$ alkane mixtures is also of relevance to catalytic hydrocracking and isomerization of alkanes. ${ }^{17,18}$ FT synthesis converts hydrogen and carbon monoxide to hydrocarbon mixtures which are subsequently used to produce synthetic fuels and lubrication oils. ${ }^{19}$ In conventional FT synthesis, while the majority of products are linear $n$-alkanes, branched alkanes are produced in small amounts, typically $<20 \%$, in product mixtures. Monomethyl branched alkanes have been reported as the predominant branching products, and different branched isomers can coexist with the branching methyl group distributed along the alkyl chains. ${ }^{1,7,20,21}$ Recent studies using bifunctional catalysts ${ }^{22,23}$ have reported product compositions


Figure 1. $2 \mathrm{D}{ }^{1} \mathrm{H}$ DQF-COSY spectra of bulk liquids of (a) $n-\mathrm{C}_{12}$, (b) $2-\mathrm{C}_{7}$, (c) $3-\mathrm{C}_{7}$, (d) 4- $\mathrm{C}_{9}$, and of (e) $n-\mathrm{C}_{12}$ and (f) 2 - $\mathrm{C}_{7}$ confined in the titania. The contour level for each 2D spectrum is different to allow clear visualization. The arrow at the top-right corner of (a) indicates the direction of the main diagonal projection that is used to obtain the 1D anti-diagonal spectra.
containing as much as $>60 \mathrm{~mol} \%$ branched alkanes. Being able to control the amount and nature of branched alkanes enables control over the properties and quality of fuels. ${ }^{22,24,25}$ Furthermore, the branching compositions in product mixtures have been reported to reflect the reaction mechanism of FT synthesis. ${ }^{20,21}$

The present study reports the first in situ quantification of branched alkanes from within the pores of a catalyst support. The extent to which DQF-COSY can characterize the nature and extent of branching of alkanes within the pores of a real catalyst support is studied. A partial least-square regression (PLSR) analysis was applied to estimate the mixture compositions from the DQF-COSY spectral data. First, a simple case of mixtures of 2-methyl alkanes and $n$-alkanes is considered, in which the molecular components are identified unambiguously from their spectral signatures. Second, the approach is applied to mixtures comprising linear alkanes and monomethyl alkanes, in particular, 2-methyl alkanes, 3-methyl alkanes, and 4-methyl alkanes. In this second case, the PLSR approach was further extended to characterize the mixtures in terms of the composition of the submolecular groups $\left[\mathrm{CH}_{3} \mathrm{CH}_{2},\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}\right.$, and $\left.\mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right) \mathrm{CH}_{2}\right]$ present in the mixtures.

## - EXPERIMENTAL SECTION

Materials. The liquid alkanes 2 -methylheptane ( $2-\mathrm{C}_{7}$, purity $\geq 99 \%$ ), 3-methylheptane ( $3-\mathrm{C}_{7}$, purity $\geq 97 \%$ ), 2methylnonane ( $2-\mathrm{C}_{9}$, purity $\geq 98 \%$ ), $n$-decane ( $n-\mathrm{C}_{10}$, purity $\geq 99 \%$ ), and $n$-dodecane ( $n-C_{12}$, purity $\geq 99 \%$ ) were purchased
from Fisher Scientific. 4-Methylnonane (4-C ${ }_{9}$, purity $\geq 98 \%$ ) and $n$-hexadecane ( $n$ - $\mathrm{C}_{16}$, purity $\geq 99 \%$ ) were purchased from Sigma-Aldrich. Measurements were made on the liquids confined within porous titania $\left(\mathrm{TiO}_{2}\right)$ pellets, provided by Evonik Industries AG, in the form of cylindrical extrudates of a length and a diameter of 5 and 1.8 mm , respectively. The surface area, pore diameter, and pore volume of the titania were measured by nitrogen sorption analysis as $54.4 \mathrm{~m}^{2} \mathrm{~g}^{-1}$, 25.0 nm , and $0.34 \mathrm{~cm}^{3} \mathrm{~g}^{-1}$, respectively. The titania had a porosity of 0.58 , as measured by mercury porosimetry.

Experiments on the Mixtures of Branched and Linear Alkanes. The PLSR models were calibrated to estimate the mixture compositions using linear combinations of the spectral data of single-component $2-\mathrm{C}_{7}, 3-\mathrm{C}_{7}, 4-\mathrm{C}_{9}$, and $n-\mathrm{C}_{12}$ liquid samples. The samples were prepared by filling a 5 mm NMR tube to a height of 10 mm ; this height ensured that the entire sample sat within the length of the signal detection region of the radio frequency (r.f.) coil; hence, the liquid volume of the sample can be estimated from the acquired NMR signal (Supporting Information, section S1).

Test mixtures (TM1-19) were prepared with the compositions as reported in Tables 1 and S1. For samples TM12-TM19, the relative compositions between branched alkanes were consistent with those reported for the FT reaction on cobalt catalysts. ${ }^{21}$ The preparation of the samples of bulk liquid mixtures was the same as for pure bulk liquids. To prepare samples of liquid mixtures confined in the titania, the liquid mixture was imbibed in $3.6-4 \mathrm{~g}$ of the as-received titania pellets. To minimize the change of mixture composition


Figure 2. 1D anti-diagonal spectra obtained from the data shown in Figure 1. The anti-diagonal spectra for bulk liquids of $n-\mathrm{C}_{12}, 2-\mathrm{C}_{7}, 3-\mathrm{C}_{7}$, and 4 $\mathrm{C}_{9}$ and confined liquid of $n-\mathrm{C}_{12}$ and $2-\mathrm{C}_{7}$ are shown in (a-f), respectively. Each spectrum was normalized to the intensity of the peak located at $\Delta \delta$ $\sim 0.40 \mathrm{ppm}$.
due to competitive adsorption, a liquid mixture of the same volume as the total pore volume of the titania pellets was used to saturate the pellets so that all the liquid was imbibed within the pores. Therefore, the compositions of confined mixtures were considered the same as those of the prepared bulk liquid mixtures. The amounts of hydrocarbons required to prepare each liquid mixture were determined gravimetrically using a Precisa 125 A balance, measured to an accuracy of $\pm 0.0001 \mathrm{~g}$. The saturated titania pellets were packed into a glass tube of an inner diameter of 11 mm to a height of 38 mm .

NMR Experiments. The NMR measurements were performed on a Bruker AV 300 spectrometer which had a vertical superwide-bore 7.1 T superconducting magnet and a three-axis gradient set with a maximum gradient strength of $81 \mathrm{G} \mathrm{cm}^{-1}$ in each direction. The signal was detected using a r.f. coil of 66 mm inner diameter, which was tuned to the ${ }^{1} \mathrm{H}$ resonance frequencies of the chemicals used. The typical $90^{\circ}$ pulse length was $95 \mu$ s.

The 2D ${ }^{1} \mathrm{H}$ DQF-COSY measurements were performed using a gradient-selective pulse sequence (cosygpmfqf in Topspin, Bruker). In this sequence, the selective acquisition of signals associated with double-quantum coherence was achieved by applying three sine-shaped gradient pulses of a duration of 1 ms and a gradient stabilization time of $200 \mu \mathrm{~s}$ along the vertical $z$ direction. The relative gradient strength of the three gradient pulses in the order in which they were applied was 16:12:40. The acquisition was carried out with $8-$ 16 scans with a recycle time of 10 s . Given that the $T_{1}$ values of all the species studied were $\leq 2.5 \mathrm{~s}$, the effect of $T_{1}$ relaxation on the measurement is negligible. The time domain dataset consisted of $1024 \times 256$ complex points in the direct and
indirect dimensions, and a sweep width of 4000 Hz was used in both dimensions. The dataset for each sample was acquired 23 times to estimate the experimental error.

Data Analysis. Processing of DQF-COSY Data. The timedomain dataset was first multiplied by the sine window functions in both dimensions, and the indirect dimension was then zero-filled to 1024 points. The 2D dataset was Fouriertransformed to obtain the 2D spectrum which was then modulus-corrected. The modulus-corrected spectrum was symmetrized against the diagonal of the spectrum, and baseline correction was then applied. The quantitative analysis of the data was performed on the 1D anti-diagonal spectra. The direction of the projection is indicated by the arrow at the topright corner of Figure 1a.

Analysis of DQF-COSY Spectra. In a 2D DQF-COSY spectrum, the peaks located on the diagonal (dashed lines in Figure 1) are conventionally referred to as diagonal peaks and the peaks off the diagonal are known as cross-peaks. Crosspeaks are associated with pairs of ${ }^{1} \mathrm{H}$ nuclei interacting by $J$ coupling and therefore contain the structural information characterizing a molecule. The intensity of a given cross-peak is associated with the number of nuclei involved in the coupling and the strength of $J$-coupling. The analysis focused on the cross-peaks. Only the cross-peaks associated with J-coupling between ${ }^{1} \mathrm{H}$ nuclei within a distance of three chemical bonds were considered, as the $J$-coupling constants and the corresponding cross-peaks for coupling more than three bonds are negligible. ${ }^{26}$

Figure 1a-d shows the 2D DQF-COSY spectra of the bulk liquids of $n-\mathrm{C}_{12}, 2-\mathrm{C}_{7}, 3-\mathrm{C}_{7}$, and $4-\mathrm{C}_{9}$, respectively, along with the standard 1 D spectral projections of the 2 D data onto the
vertical and horizontal chemical shift axes. All the chemical shifts in this work are relative to the ${ }^{1} \mathrm{H}$ resonance frequency of tetramethylsilane. The chemical shifts of ${ }^{1} \mathrm{H}$ nuclei involved in $J$-coupling and the coordinates of the resulting cross-peaks in the 2D spectra in Figure 1 are summarized in Table S2. Figure 1a-d and Table S2 confirm that different types of branching lead to different cross-peaks, which discriminate linear and branched alkanes and different branched isomers. Figure 1e,f presents the DQF-COSY spectra, along with the standard 1D spectral projections on the vertical and horizontal axes, of $n$ $\mathrm{C}_{12}$ and $2-\mathrm{C}_{7}$, respectively, confined within the porous titania. The cross-peaks observed in Figure 1a,b for bulk liquid species are again observed in Figure 1e,f, but the broadening along the main diagonal due to magnetic field inhomogeneity is also clearly seen. Figure $1 \mathrm{e}, \mathrm{f}$ also confirms that it is impossible to discriminate the two species from their 1D spectra, as seen from the projected spectra.

Figure 2 presents the 1D anti-diagonal spectra of the 2D data shown in Figure 1. The horizontal axis of the 1D antidiagonal spectra shows the chemical shift difference $\Delta \delta=\delta_{x}-$ $\delta_{y}$, where $\delta_{x}$ and $\delta_{y}$ denote the coordinates of the 2D spectrum. For the signal located at the position $\left[\delta_{x}, \delta_{y}\right]$ on the 2 D spectrum, the anti-diagonal spectrum of the signal appears at $\Delta \delta=\delta_{x}-\delta_{y}$, which is proportional to the distance of the signal away from the main diagonal of the 2D data $\left(\left|\delta_{x}-\delta_{y}\right| / \sqrt{2}\right)$. Therefore, for the 1 D anti-diagonal spectra, the peaks located at $\Delta \delta=0 \mathrm{ppm}$ correspond to the 2 D main diagonal peaks while those located at $\Delta \delta \neq 0 \mathrm{ppm}$ correspond to 2 D crosspeaks. The values of $\Delta \delta$ for cross-peaks are listed in Table S2. In Figure 2, the cross-peaks observed at $\Delta \delta \sim \pm 0.40 \mathrm{ppm}$ for all the species correspond to the $\mathrm{CH}_{3} \mathrm{CH}_{2}$ group at the linear terminus of an alkyl chain. The cross-peaks that allow discrimination of $2-\mathrm{C}_{7}$ are located at $\Delta \delta= \pm 0.65 \mathrm{ppm}$ (Figure $2 b)$, which are associated with the $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}$ group. $3-\mathrm{C}_{7}$ and $4-\mathrm{C}_{9}$ can be discriminated from $n-\mathrm{C}_{12}$ and $2-\mathrm{C}_{7}$ by the crosspeaks at $\Delta \delta= \pm 0.22 \mathrm{ppm}$ and $\Delta \delta= \pm 0.47-0.56 \mathrm{ppm}$ (Figure $2 \mathrm{c}, \mathrm{d})$, which are associated with the $\mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right) \mathrm{CH}_{2}$ groups. Discrimination between $3-\mathrm{C}_{7}$ and $4-\mathrm{C}_{9}$ is achieved in the bulk liquid state (Figure 1), for example, by the cross-peak associated with carbon [1, $2^{\prime}$ ] for $3-\mathrm{C}_{7}$ (Table S2). However, this discrimination is impossible when these species are confined within the pore space of the titania because of line broadening along the main diagonal. The anti-diagonal spectra for $n-\mathrm{C}_{12}$ and $2-\mathrm{C}_{7}$ confined in the titania are shown in Figure 2e,f, respectively. It is observed in these cases that the high chemical resolution is retained in the anti-diagonal spectra, consistent with the data acquired for those liquids in the bulk liquid state shown in Figure 2a,b. These anti-diagonal spectra are used to quantify the composition of the liquid mixtures.

PLSR Analysis. PLSR is well established as a multivariate calibration method that has been widely applied to the analysis of spectroscopy data. ${ }^{27-29}$ In this work, PLSR was applied to obtain calibration relationships between the DQF-COSY spectral data and mixture compositions. Given the complexity of the liquid mixtures that this approach will be used for when studying real catalytic data, the spectra upon which the PLSR models were calibrated were produced by linear combination of the spectra of the pure bulk-liquid species from which the mixtures were derived. For the initial analysis of mixtures of $n$ $\mathrm{C}_{12}$ and $2-\mathrm{C}_{7}, 11$ calibration spectra were simulated based on the spectra of the two pure single-component species. For the four-component mixtures of $n-\mathrm{C}_{12}, 2-\mathrm{C}_{7}, 3-\mathrm{C}_{7}$, and $4-\mathrm{C}_{9}$, the spectral data of the pure species were employed to simulate

1111 spectra for PLSR calibration. The details of the simulation of spectra for the calibration mixtures and the details of the PLSR calibration are given in the Supporting Information (sections S1 and S2, respectively).

The performance of the calibration models, and hence the error quoted for the resulting compositions, was evaluated using root-mean-square error (RMSE) and absolute error. The RMSEs calculated for the calibration and test samples are referred to as RMSEC and RMSEP, respectively. The details of the error analysis are reported in the Supporting Information (section S3).

## - RESULTS AND DISCUSSION

Composition Analysis of the Mixtures of Linear and 2-Methyl Alkanes (TM1-TM9). The results of the PLSR analysis are reported in Table 1. The RMSEPs of 2-methyl and linear alkanes were both calculated as $1.4 \mathrm{~mol} \%$, indicating accurate estimation. The RMSEC of the PLSR model was calculated as $0.8 \mathrm{~mol} \%$. It is noted that this approach is designed to characterize the extent and nature of branching in mixtures of alkanes and does not characterize the alkane chain length. In earlier work, the use of COSY to characterize the chain length of $n$-alkanes has been addressed, the analysis being based on the relative intensity between cross- and diagonal peaks of COSY spectra. ${ }^{14}$

For the relatively simple application to the characterization of the amount of 2-methyl alkane species present in a mixture with $n$-alkanes, it is also possible to identify a simple theoretical relationship from which the 2-methyl alkane composition can be estimated from a single measurement of the ratio of the intensities of the cross-peaks characterizing the $\mathrm{CH}_{3} \mathrm{CH}_{2}$ and $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}$ groups present in the mixture. Figure 3a shows the


Figure 3. (a) Anti-diagonal spectra of mixtures TM1-TM7 with the 2-methyl alkane composition $x_{2 \text { methyl }}=5.6-100 \mathrm{~mol} \%$. Each spectrum was normalized to the intensity at $\Delta \delta=0 \mathrm{ppm}$. (b) Ratios of cross-peak intensities $R_{\mathrm{X}}$ against $x_{2 \text { methyl }}$. The $R_{\mathrm{X}}$ values have a standard error of $\pm 0.001$.
anti-diagonal spectra obtained from the binary mixtures of 2$\mathrm{C}_{7}$ and $n-\mathrm{C}_{12}$ (TM1-TM7) in which the $2-\mathrm{C}_{7}$ composition, $x_{2 \text { methyl }}$, lies in the range $5.6-100 \mathrm{~mol} \%$. Each spectrum in Figure 3a was normalized to its own maximum at $\Delta \delta=0 \mathrm{ppm}$. It is observed that the cross-peaks at $\Delta \delta= \pm 0.40 \mathrm{ppm}$ and $\Delta \delta$ $= \pm 0.65 \mathrm{ppm}$ associated with the $\mathrm{CH}_{3} \mathrm{CH}_{2}$ and $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}$ groups, respectively, are well separated with their intensities identified unambiguously. Denoting the cross-peaks at $\Delta \delta=$ $\pm 0.40 \mathrm{ppm}$ and $\Delta \delta= \pm 0.65 \mathrm{ppm}$ as cross-peak 1 (X1) and cross-peak 2 (X2), respectively, it is observed in Figure 3a that as $x_{2 \text { methyl }}$ increases, the intensities of X1 decrease, while the intensities of X 2 increase. Given that one $n-\mathrm{C}_{12}$ molecule has two $\mathrm{CH}_{3} \mathrm{CH}_{2}$ groups and that one $2-\mathrm{C}_{7}$ molecule has one $\mathrm{CH}_{3} \mathrm{CH}_{2}$ group and one $\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}$ group, a theoretical


Figure 4. Distributions of the absolute errors for the PLSR estimation of the compositions of (a) $n-\mathrm{C}_{12}$, (b) $2-\mathrm{C}_{7}$, and (c) $3-\mathrm{C}_{7}+4-\mathrm{C}_{9}$ in the calibration mixtures.
relationship between $x_{2 \text { methyl }}$ and the relative cross-peak intensity $R_{\mathrm{X}}=I_{\mathrm{X} 2} / I_{\mathrm{X} 1}$ is obtained

$$
\begin{equation*}
R_{\mathrm{X}}=\frac{R_{0} x_{2 \text { methyl }}}{2-x_{2 \text { methyl }}} \tag{1}
\end{equation*}
$$

where $R_{0}=I_{\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}} / I_{\mathrm{CH}_{3} \mathrm{CH}_{2}}$ is the intensity ratio of equal moles of the two groups. The $R_{0}$ value was estimated from the pure-component spectrum $\left(x_{2 \text { methyl }}=1\right)$, consistent with the PLSR approach, resulting in $R_{0}=0.829 \pm 0.001$. Figure 3b shows the $R_{\mathrm{X}}$ values calculated for samples TM1-TM9 plotted against $x_{2 \text { methyl }}$. Equation 1 is plotted as the solid line in Figure 3 b , and it is observed that eq 1 estimates $x_{2 \text { methyl }}$ accurately with the RMSEP calculated as $1.1 \mathrm{~mol} \%$, similar to that for PLSR analysis.

Characterization of the Mixtures of Linear and 2-, 3-, 4-Monomethyl Alkanes (TM10-TM19). As discussed previously, discrimination between $3-\mathrm{C}_{7}$ and $4-\mathrm{C}_{9}$ in porous titania was not possible, and hence, the mixtures of these four isomers in samples TM10-TM19 are considered as a ternary system, with $3-\mathrm{C}_{7}$ and $4-\mathrm{C}_{9}$ being treated as a singlecomponent and the total composition of these two isomers being estimated in the PLSR analysis. The results of PLSR model calibration for this system are first presented. For each calibration mixture, the composition of the mixture estimated by the PLSR models has been compared with the known calibration composition, and the absolute error for each component of each calibration mixture is plotted in Figure 4. Figure $4 a-c$ shows the components of $n-\mathrm{C}_{12}, 2-\mathrm{C}_{7}$, and $3-\mathrm{C}_{7}+$ $4-\mathrm{C}_{9}$, respectively. It is seen that for $>90 \%$ of the composition space, the absolute errors are $<5 \mathrm{~mol} \%$ for all three components, suggesting accurate estimation of the PLSR models. However, larger errors are observed in estimating the $n-\mathrm{C}_{12}$ and $3-\mathrm{C}_{7}+4-\mathrm{C}_{9}$ compositions at low $n-\mathrm{C}_{12}$ and high 3-$\mathrm{C}_{7}+4-\mathrm{C}_{9}$ compositions. This arises because $n-\mathrm{C}_{12}$ has only one cross-peak position at $\Delta \delta= \pm 0.40 \mathrm{ppm}$, which overlaps within the experimental error with the cross-peaks associated with the ${ }^{1} \mathrm{H}$ attached to carbons [1,2], [4,5], and [9, 10] of 4$C_{9}$ and carbons [1, 2], [3, 4], and [7, 8] of 3-C (see Table $^{2}$ S2). The RMSEC values for calibration mixtures were calculated as $2.4,1.8$, and $2.7 \mathrm{~mol} \%$ for $n-\mathrm{C}_{12}, 2-\mathrm{C}_{7}$, and 3-$\mathrm{C}_{7}+4-\mathrm{C}_{9}$, respectively.

The results of PLSR estimation of the compositions of samples TM10-TM19 are listed in Table 1. It is seen that there is good agreement between the estimated and true
compositions for all the bulk liquid and confined mixtures. The RMSEP values were calculated using the data presented in Table 1, and the values for $n-\mathrm{C}_{12}, 2-\mathrm{C}_{7}$, and $3-\mathrm{C}_{7}+4-\mathrm{C}_{9}$ were obtained as $2.8,1.3$, and $3.0 \mathrm{~mol} \%$, respectively.

The analysis presented can be generalized to any mixtures of linear and monomethyl branched alkanes, with all monomethyl alkanes branched at carbon indices $>3$ treated as equivalent. For isomers with branching at carbon indices $>3$, it is assumed that the positions and intensities of cross-peaks do not change with the branching positions. Confirmation of the assumption was achieved using simulated spectra predicted by the open web-based software packages nmrshiftdb $2^{30}$ and SPINUS. ${ }^{\text {31 }}$

The PLSR analysis presented so far uses the calibration spectra based on the single-component spectra of monomethyl alkanes and $n$-alkanes and is therefore not applicable to multimethyl branched alkanes because the analysis assumes that one branched alkane molecule contains a single branching methyl group. However, it is now shown that the calibration spectra do allow the characterization of such mixtures in terms of the submolecular groups $\left[\mathrm{CH}_{3} \mathrm{CH}_{2},\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}\right.$, and $\mathrm{CH}_{2} \mathrm{CH}\left(\mathrm{CH}_{3}\right) \mathrm{CH}_{2}$ ] they contain. The PLSR models were calibrated to estimate the composition of submolecular groups, as detailed in the Supporting Information (section S2), where the calculation of the group compositions based on the molecular compositions is also presented. The absolute errors of the PLSR estimation of the group compositions of calibration mixtures are presented in Figure S3. The RMSEC values were calculated for each group in the calibration mixtures, yielding values of $0.9 \mathrm{~mol} \%$ for all three groups. The results of the PLSR estimation of the group compositions of samples TM10-TM19 are listed in Table 1, based on which the RMSEPs were calculated as $<1 \mathrm{~mol} \%$ for all the three groups.

## - CONCLUSIONS

In this work, $2 \mathrm{D}{ }^{1} \mathrm{H}$ DQF-COSY spectroscopy was applied to discriminate branched and linear alkanes. The main diagonal projection of the 2 D data was used to characterize the compositions of mixtures of branched and linear alkanes confined within a porous titania catalyst support with the application of PLSR analysis. Two case studies are reported. First, mixtures of 2-methyl and linear alkanes were considered. Accurate PLSR estimation was achieved with an RMSEP of 1.4 $\mathrm{mol} \%$ for 2-methyl alkane compositions. The 2-methyl alkane composition was also shown to be well predicted by a
theoretical relationship which considered the relative intensity between the cross-peaks. In the second case, the method was applied to a more complicated system comprising $n-\mathrm{C}_{12}, 2-\mathrm{C}_{7}$, $3-\mathrm{C}_{7}$, and $4-\mathrm{C}_{9}$. The results showed that discrimination of $2-$ methyl and linear alkanes from other isomers in the mixtures was achieved. However, discrimination between monomethyl alkanes with the branching groups located at relatively central positions of alkyl chains was not achieved. PLSR models were applied to estimate the compositions of $n-\mathrm{C}_{12}, 2-\mathrm{C}_{7}$, and the total composition of $3-\mathrm{C}_{7}$ and $4-\mathrm{C}_{9}$ in the test mixtures, yielding RMSEP $\leq 3 \mathrm{~mol} \%$ for all the components. The PLSR analysis was further extended to estimate the compositions of the submolecular groups $\mathrm{CH}_{3} \mathrm{CH}_{2},\left(\mathrm{CH}_{3}\right)_{2} \mathrm{CH}$, and $\mathrm{CH}_{2} \mathrm{CH}$ $\left(\mathrm{CH}_{3}\right) \mathrm{CH}_{2}$ in the mixtures, resulting in RMSEP $<1 \mathrm{~mol} \%$ for all groups. The extended PLSR models calibrated for group compositions can be applied to determine the branching level in mixtures containing multimethyl branched alkanes. While the mixtures and their compositions considered in this work are of interest in FT synthesis, the method is considered generic and not limited to specific systems.

## ■ ASSOCIATED CONTENT

## si Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.analchem.1c04295.

Details of the simulation of the spectra of calibration mixtures, of the implementation of PLSR calibration, and of error analysis; compositions of the test mixtures, and chemical shifts of coupled ${ }^{1} \mathrm{H}$ nuclei that give rise to cross-peaks in the DQF-COSY spectra (PDF)

## - AUTHOR INFORMATION

## Corresponding Author

Lynn F. Gladden - Department of Chemical Engineering and Biotechnology, University of Cambridge, Cambridge CB3 OAS, U.K.; © orcid.org/0000-0001-9519-0406; Email: 1fg1@cam.ac.uk

## Authors

Qingyuan Zheng - Department of Chemical Engineering and Biotechnology, University of Cambridge, Cambridge CB3 OAS, U.K.; © orcid.org/0000-0003-3902-1848
Mick D. Mantle - Department of Chemical Engineering and Biotechnology, University of Cambridge, Cambridge CB3 OAS, U.K.; © orcid.org/0000-0001-7977-3812
Andrew J. Sederman - Department of Chemical Engineering and Biotechnology, University of Cambridge, Cambridge CB3 OAS, U.K.; © orcid.org/0000-0002-7866-5550
Timothy A. Baart - Shell Global Solutions International B.V., Amsterdam 1031 HW, The Netherlands
Constant M. Guédon - Shell Global Solutions International B.V., Amsterdam 1031 HW, The Netherlands

Complete contact information is available at:
https://pubs.acs.org/10.1021/acs.analchem.1c04295

## Notes

The authors declare no competing financial interest.

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