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Journal Pre-proofs

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Analysis of Serological Surveys of Antibodies to SARS-CoV-2 in the United States to Estimate Parameters Needed for Transmission Modeling and to Evaluate and Improve the Accuracy of Predictions

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The findings and conclusions in this report are those of the authors and do not necessarily represent the official positions of the Centers for Disease Control and Prevention, National Science Foundation, or Purdue University.

Abstract

Seroprevalence studies can estimate proportions of the population that have been infected or vaccinated, including infections that were not reported because of the lack of symptoms or testing. Based on information from studies in the United States from mid-summer 2020 through the end of 2021, we describe proportions of the population with antibodies to SARS-CoV-2 as functions of age and time. Slices through these surfaces at arbitrary times provide initial and target conditions for simulation modeling. They also provide the information needed to calculate age-specific forces of infection, attack rates, and – together with contact rates – age-specific probabilities of infection on contact between susceptible and infectious people.

We modified the familiar Susceptible-Exposed-Infectious-Removed (SEIR) model to include features of the biology of COVID-19 that might affect transmission of SARS-CoV-2 and stratified by age and location. We consulted the primary literature or subject matter experts for contact rates and other parameter values. Using time-varying Oxford COVID-19 Government Response Tracker assessments of US state and DC efforts to mitigate the pandemic and compliance with non-pharmaceutical interventions (NPIs) from a YouGov survey fielded in the US during 2020, we estimate that the efficacy of social-distancing when possible and mask-wearing otherwise at reducing susceptibility or infectiousness was 31% during the fall of 2020. Initialized from seroprevalence among people having commercial laboratory tests for purposes other than SARS-CoV-2 infection assessments on 7 September 2020, our age- and location-stratified SEIR population model reproduces seroprevalence among members of the same population on 25 December 2020 quite well.

Introducing vaccination mid-December 2020, first of healthcare and other essential workers, followed by older adults, people who were otherwise immunocompromised, and then progressively younger people, our metapopulation model reproduces seroprevalence among blood donors on 4 April 2021 less well, but we believe that the discrepancy is due to vaccinations being under-reported or blood donors being disproportionately vaccinated, if not both. As experimenting with reliable transmission models is the best way to assess the indirect effects of mitigation measures, we determined the impact of vaccination, conditional on NPIs. Results indicate that, during this period, vaccination substantially reduced infections, hospitalizations and deaths.

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Keywords: COVID-19 pandemic; Serial, cross-sectional serosurveys; SEIR metapopulation modeling; SARS-CoV-2 transmission; Impact of mitigation measures; Vaccination strategies

Highlights

- Metapopulation SEIR model of SARS-CoV-2 transmission in the US
- All parameters save efficacy of NPIs estimated independently
- Initialized on 7 September, reproduces seroprevalence on 25 December 2020
- Evaluated vaccination, conditional on NPIs, through 4 April 2021
- Symptomatic infections, hospitalizations, and deaths reduced by 30-40%

1. Introduction

Mitigating outbreaks with pandemic potential has been compared to building ships while sailing or planes while flying, metaphors that emphasize the uncertainties associated with newly emerging human pathogens. While each pathogen is unique, historical pandemics share many characteristics. Most have resulted from respiratory diseases caused by airborne pathogens (Wang, et al. 2021), the substance of much mathematical epidemiology. While model evaluations of possible strategies can inform public policymaking, unless forecasts are accurate, the utility of simulated scenarios is questionable (loannidis, et al. 2020).

Early in the COVID-19 pandemic, we built a framework (superstructure in the airplane or shipbuilding analogy) that we could use, together with local information, to answer urgent public health questions. We chose the Susceptible-Exposed-Infectious-Removed (SEIR) epidemiological structure, but included biological features of COVID-19 that might affect the transmission and control of SARS-CoV-2, including asymptomatic, pre-symptomatic and hospitalized states, disease-induced mortality, and vaccination (figure 1).

In earlier work, we modeled SARS-CoV-2 transmission in host populations stratified by age or location to assess the impact of various non-pharmaceutical interventions (NPIs). Here we model transmission in the United States' population stratified by both age and location (the 50 states plus Washington, DC, but neither Puerto Rico nor other territories) considering infection- and vaccination-acquired immunity equivalent. As susceptibility to SARS-CoV-2 reinfection may depend on the variant with which previously infected (Rössler, et al. 2022) and waning of immunity from that infection or vaccination, we have stratified hosts by exposure to more or less related variants and by infection, vaccination, or both (in preparation).

Here we determine the simpler model's ability to reproduce transmission in the United States during the last quarter of 2020, when the ancestral strain was circulating and NPIs were in effect, and first few of 2021, when vaccination began and the alpha variant became dominant (Lambrou, et al. 2022). After demonstrating the accuracy of this particular metapopulation (a term coined by Levins in 1969 for a population composed of sub-populations) framework, we evaluate the impact of vaccinating healthcare and other essential workers, then elderly, otherwise immunocompromised, and finally, healthy younger people, conditional on NPIs. And we discuss an alternative strategy, results of whose evaluation we report elsewhere (Vo, et al. submitted).

2. Methods

2.1 Model Equations

The model diagrammed in figure 1 can be represented as a system of ordinary differential equations, where S_i is the number who are susceptible in group *i* (here *i* indexes ages, locations, or combinations; there are *n* such groups), E_i is the number who have been infected, but are not yet infectious, V_i is the number who have received one dose of vaccine (\geq 14 days ago), I_{iw} (w = a, p, s, h) are the numbers infectious in group *i* who are asymptomatic, pre-symptomatic, symptomatic, or hospitalized, R_i is the number who have recovered or been vaccinated a second time (\geq 14 days ago), and are temporarily immune, B_i is the number whose immunity has waned, but can be boosted by revaccination, and M_i is the number in group *i* who have died:

$$\begin{split} S_{i}' &= q_{i}\omega B_{i} + \omega_{v}V_{i} - \left[\lambda_{i}(t) + \chi_{1i}\right]S_{i}, \\ B_{i}' &= \omega R_{i} - \left[q_{i}\omega + (1 - q_{i})\epsilon_{3}\chi_{3i} + (1 - \epsilon_{3})\lambda_{i}(t)\right]B_{i} \\ E_{i}' &= \lambda_{i}(t)S_{i} + (1 - \epsilon_{1})\lambda_{i}(t)V_{i} + (1 - \epsilon_{3})\lambda_{i}(t)B_{i} - kE_{i}, \\ V_{i}' &= \chi_{1i}S_{i} - \left[(1 - \epsilon_{1})\lambda_{i}(t) + \omega_{v} + \epsilon_{2}\chi_{2i}\right]V_{i}, \\ I_{ia}' &= kp_{i}E_{i} - \gamma_{ia}I_{ia}, \\ I_{ip}' &= k(1 - p_{i})E_{i} - \xi I_{ip}, \\ I_{is}' &= \xi I_{ip} - \left[\gamma_{is} + \delta_{i}\gamma_{is \to h}\right]I_{is}, \\ I_{ih}' &= \delta_{i}\gamma_{is \to h}I_{is} - \gamma_{ih}I_{ih}, \\ R_{i}' &= \gamma_{ia}I_{ia} + \theta_{is}\gamma_{is}I_{is} + \theta_{ih}\gamma_{ih}I_{ih} + \epsilon_{2}\chi_{2i}V_{i} + (1 - q_{i})\epsilon_{3}\chi_{3i}B_{i} - \omega R_{i}, \\ M_{i}' &= (1 - \theta_{is})\gamma_{is}I_{is} + (1 - \theta_{ih})\gamma_{ih}I_{ih}, \quad i = 1, 2, ..., n, \end{split}$$

where the force or hazard rate of infection among susceptible people in group *i* (and those receiving one vaccine dose, whose susceptibility to infection is $1 - \epsilon_1$, where ϵ_1 is the efficacy of a single dose) is

$$\lambda_{i}(t) = \psi_{iS} a_{i} \beta_{i} \sum_{j=1}^{n} c_{ij} \psi_{jI} \frac{\eta_{ja} I_{ja}(t) + \eta_{jp} I_{jp}(t) + I_{js}(t) + \eta_{jh} I_{jh}(t)}{N_{j}}, \text{ where}$$

$$N_{j} = S_{j} + B_{j} + E_{j} + V_{j} + I_{ja} + I_{jp} + I_{js} + I_{jh} + R_{j} + M_{j} \text{ and } N = \sum_{j=1}^{n} N_{j}.$$

In this expression, $\psi_{is} = 1 - c_i b_{is}$ and $\psi_{ii} = 1 - c_i b_{ii}$ represent reductions in susceptibility and infectiousness, respectively, due to physical-distancing if possible and mask-wearing otherwise, c_i is the proportion of group ithat comply with such recommendations and b_{is} and b_{ii} are their respective efficacies. Here the parameter a_i is the *per capita* contact rate, β_i is the probability of transmission per contact between susceptible and infectious people ($a_i \times \beta_i$ is the effective contact rate), and c_{ij} is the proportion of their contacts that members of group ihave with those of group j. As we are interested in relatively short periods during which M_j is small relative to N_j , we maintain N constant by including M_j in the equation for N_j .

Values for most transmission model parameters can be found by carefully reviewing the primary literature or consulting subject-matter experts (tables 1 and 2). But the probabilities of infection upon contact must be obtained from populations of interest. In the following sections, we describe seroprevalence – the humoral (versus cell-mediated) component of the adaptive immune response – as a function of age and time from a study involving assays of residual sera from commercial laboratory tests for purposes other than SARS-CoV-2 infection assessments, then estimate forces of infection and attack rates for n discrete age groups. Finally, given age-specific contact rates and proportions with each of those groups from the literature, we calculate the requisite probabilities by solving n equations, each with one unknown.

2.2 Forces of Infection

First, we model national and location-specific proportions seropositive from studies of commercial laboratory tests, described by Bajema, et al. (2021), or blood donors, described by Jones, et al. (2021), as functions of both age and time via bivariate logistic regressions in which the independent variables are represented via third-order polynomials and, because subjects aged a at time t are aged a+1 at time t+1, all interactions (figure 2a). Where

observations were lacking, we used adjacent ones (e.g., DC is a composite of MD and VA). While we used linelistings, public-use summaries of these and other data described later are available on the CDC's COVID Data Tracker: <u>https://covid.cdc.gov/covid-data-tracker/#datatracker-home</u>.

Then we discretize these proportions (i.e., assume that they are constant within intervals, Feng and Glasser 2019a). Ages and times were recorded in conventional units, but such surfaces are continuous, so we can choose any intervals. Information needed for transmission modeling typically is available in 5-year age groups, so we chose age unit years. Time is continuous in most of our models, so we chose time unit days. We number these discrete periods $a_0 = 0$, $a_1 = 1$, $a_2 = 2$, ...; $t_0 = 0$, $t_1 = 1$, $t_2 = 2$, and so on. Here we use the indices *a* and *t* to denote continuous age and time and *i* and *j* to denote their discrete analogs.

Because all SARS-CoV-2 vaccines used in the United States target the spike protein, most vaccinated people have anti-spike (anti-S) antibodies. Most infected people also have antibodies to a nucleocapsid protein (anti-N antibodies). The national commercial laboratory seroprevalence study includes all ages, but measures only anti-N. The blood-donor study measures antigens to both spike and nucleocapsid proteins, but does not include children. While neither study population is a random sample, their anti-N seroprevalences are comparable (results not shown). We use results from both studies in this work.

Post-vaccination onset, we let $S(i, j) = 1 - I_B(i, j)$ denote the proportion susceptible among those aged $a_{i-1} \le a < a_i$ at time $t_{j-1} \le t < t_j$, where the proportion immune, $I_B = I_I + I_V$, with I_I by virtue of infection and I_V vaccination (i.e., $1 - I_B$ is the probability of having escaped both). Further, we let $\lambda(i, j)$ and $\chi(i, j)$ denote the specific rates of infection and immunization in the appropriate intervals of age and time.

Because neither $I_I(i,j)$ nor $I_V(i,j)$ increases monotonically with age, but both increase monotonically with time (figure 2b), and forces of infection and vaccination can be calculated using either (Hens, et al. 2010), we write $S(i,j) = S(i,j-1)exp\left\{-\left[\lambda(i,j) + \chi(i,j)\right]\right\}$, which leads, first by rearrangement and then by substitution, to $\lambda(i,j) + \chi(i,j) = -ln\left[S(i,j)/S(i,j-1)\right] = -ln\left\{\left[1-I_B(i,j)\right]/\left[1-I_B(i,j-1)\right]\right\}$. Similarly, writing $\chi(i,j) = -ln\left\{\left[1-I_V(i,j)\right]/\left[1-I_V(i,j-1)\right]\right\}$, we obtain the forces or hazard rates of infection, $\lambda(i,j)$ as the difference. Pre-vaccination, $S(i,j) = 1 - I_I(i,j)$, whereupon $\lambda(i,j) = -ln\left\{\left[1-I_I(i,j)\right]/\left[1-I_I(i,j-1)\right]\right\}$.

2.3 Attack Rates

We calculate age-specific attack rates as products of probabilities of remaining susceptible at time t and the corresponding forces of infection. Because for any age, $P_S(t) = exp\left[-\int_{\tau=0}^t \lambda(\tau) + \chi(\tau)d\tau\right]$, where $P_S(t)$ denotes the probability of remaining susceptible at time t (i.e., neither infected nor immunized), and $1 - P_S(t)$ the cumulative probability of being immune (i.e., either or both), $-dP_S(t)/dt = -P_S'(t) = [\lambda(t) + \chi(t)] \times P_S(t)$. Further, $\lambda(t) \times P_S(t)$ are rates of new infections at time t, commonly called attack rates, and $\chi(t) \times P_S(t)$ are rates of new immunizations.

As explained earlier, given contact rates, a_i and proportions with each age group, c_{ik} from a contact study (those illustrated in figure 3 are from Prem, et al. 2017), we calculate the age-specific probabilities of infection on contact, β_i by solving n equations, $\lambda_i = a_i \beta_i \sum_{k=1}^n c_{ik} (I_k / N_k)$, each with one unknown (figure 4). The quantity I_k / N_k represents the probability that an individual aged k is infectious and $-P_s'(t)$ is the rate at which individuals

are removed (from the susceptible state) at exactly time *t*. Thus, integrating the derivative over time intervals yields probability density functions. Because vaccination moves individuals from the *S* to *V*, not *I* state, however, equating those probabilities and I_k/N_k , as we do here, is safest pre-vaccination.

As vaccination began on 14 December 2020 and the β_i had declined slightly among older people having commercial laboratory testing by 17 February 2021 (figure 4), the probabilities of infection on contact used in our transmission modeling were derived from the forces of infection and attack rates on 26 November 2020.

2.4 Mixing

In the simplest models, host populations are constant in size and homogeneous. In more complex models, they may be stratified, generally by age, a proxy for conditions (e.g., co-morbidities) that may increase the risk of serious disease. Age stratification also permits demographic dynamics (e.g., ageing, births by age of mother, deaths by age) that may be needed for long-term simulations. Model populations also may be spatially stratified, permitting locations to differ in population density (e.g., urban and rural) and other characteristics affecting transmission. Stratification also permits non-random mixing.

Age-specific observations usually are contacts per participant aged x with people aged y together with the numbers of participants aged x. One calculates average numbers of contacts per participant aged x with people aged y, C_{ij} if x and y are grouped. Contacts should balance (i.e., $N_i \times C_{ij} = N_j \times C_{ji}$), but rarely do, so we calculate means of corresponding elements (e.g., square roots of products of empirical matrices and their transposes). Then $c_{ij} = C_{ij}/a_{i}$, where $a_i = \sum_k C_{ik}$. Matrices of the proportions, c_{ij} , are referred to as mixing matrices and marginal sums of the contact matrix, a_i as activities. In our age-structured models, we create mixing matrices from local contact studies where possible or use synthetic ones (figure 3).

In the spirit of Hethcote and van Ark (1987), we model contacts within locations as a saturating function of population density (e.g., natural logarithms increase with density at decreasing rates, figure 4a). Consequently, the average *per capita* contact rate, $a_i = \ln(\rho_i)$, where ρ_i is the quotient of the population size and land area of location *i*, and decay exponentially with distance between locations, d_{ip} at rates, *b*. Thus,

$$\begin{split} C_{i,p} &= a_i \exp(-b \times d_{ip}) / \sum_k \exp(-b \times d_{ik}), \\ c_{i,p} &= C_{i,p} / \sum_k C_{i,k}, \end{split}$$

where $C_{i,p}$ is the contact matrix (e.g., contacts per person per day) and $c_{i,p}$ is the mixing matrix (i.e., proportions of contacts between members of group *i* and all groups *k*, including *i*).

In our age- and location-stratified models, we combine these approaches, multiplying age-specific contacts within locations by ratios of the natural logs of location-specific and overall population densities (figure 5b). Consequently, marginal contacts within more (less) densely populated locations are greater (less) than the average (figure 3a). The District of Columbia, for example, is almost 12K times as densely populated as Alaska (figure 5a), but their respective log ratios differ from average only by a factor of 2 (figure 5b). Between locations, contacts decline exponentially with distance at age-specific rates (figure 6) whose calculation Feng, et al. (2017) describe. Here distances are "as the crow flies" between population centers, but other measures may be indicated (e.g., in a mountainous Argentine province, distances were shortest routes by car).

Thus, in our age- and location-stratified models, mixing matrix elements are

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$$c_{l_i a_j l_p a_q} = \frac{c_{a_j a_q}^{(p)} e^{-b_{a_q} d_{l_i l_p}}}{\sum_{r=1}^n \sum_{s=1}^m c_{a_j a_r}^{(s)} e^{-b_{a_r} d_{l_i l_s}}},$$

where

$$c_{a_{j}a_{q}}^{(p)} = c_{a_{j}a_{q}} \times \frac{\ln(\rho^{(p)})}{\ln(\rho)}, \ 1 \le i, p \le m; 1 \le j, q \le n$$

In these expressions, ρ is population density, with the indices *i* and *p* denoting locations, of which in the model described here there are m = 51 (50 states plus Washington, DC), and *j* and *q* denoting age groups, of which there are n = 16, ages 0-4, 5-9, ..., 75+ years. Thus, the *m* matrices $C_{a_ja_q}^{(p)}$ and one matrix $C_{l_ia_jl_pa_q}$ have $n^2 = 256$ and $(m \times n)^2 = 665,856$ elements, respectively. We drop the compound notation in future equations. For more about our mixing models, please see Feng and Glasser (2019b).

3. Other Parameter Values and Initial Conditions

Other parameter values were gleaned from the primary literature or subject-matter experts (tables 1 and 2). Our proportions asymptomatic are US proportions without co-morbidities from Clark, et al. (2020), which vary inversely with age (table 2). Dichotomizing what likely is a spectrum of illness is bound to lead to a range, but our weighted average exceeds most estimates of the proportion asymptomatic.

Clark, et al. also provide proportions requiring hospitalization if infected, but – as people with asymptomatic infections don't require hospitalization – we applied their proportions (table 2) to symptomatic infections. We assumed that hospitalized people sought care within two days of symptom onset, but – as only about 70% of deaths were among inpatients (<u>https://www.cdc.gov/nchs/nvss/vsrr/covid_weekly/index.htm#PlaceDeath</u>) – some people who needed hospital-based care may not have received it. Similarly, we converted the infection fatality ratios (IFRs) of Levin, et al. (2020) into symptomatic infection fatality ratios (i.e., so-called case fatality rates). Sojourns (residence times) in our various states are largely from He, et al. (2021).

We initialized our age- and location-stratified model of the transmission of SARS-CoV-2 in the United States from location-specific surfaces like that illustrated for the entire United States in figure 2a on 7 September 2020 (t = 251 days from 31 December 2019) and incidence on the preceding x days:

$$\begin{split} S_{i,j}(t) &= 1 - R_{i,j}(t), \\ E_{i,j}(t) &= \sum_{x=0}^{-12} \lambda_{i,j}(t-x) \times S_{i,j}(t-x) \times e^{-x/k}, \\ I_{i,j}(t) &= \sum_{x=0}^{-12} \lambda_{i,j}(t-x) \times S_{i,j}(t-x) \times (1 - e^{-x/k}), \\ I_{a(i,j)}(t) &= \gamma_a^{-1} \times I_{i,j}(t) \times (1 - \Pr[CM+])_j, \\ I_{p(i,j)}(t) &= \xi^{-1} \times I_{i,j}(t) \times \Pr[CM+]_j, \\ I_{s(i,j)}(t) &= \gamma_s^{-1} \times I_{i,j}(t) \times \Pr[CM+]_j, \\ R_{i,j}(t) &= \Pr[S+]_{i,j}(t). \end{split}$$

In these approximations, *i* and *j* denote location and age, *t* denotes time, $e^{-x/k}$ the exponential survival probability for an epidemiological state with a mean sojourn of k^{-1} days, $\Pr[CM+]$ proportions with any comorbidity that increases the risk of severe disease or hospitalization (table 2), which vary only with age in our US model, $\Pr[S+]$ proportions with antibodies to nucleocapsid (with or without antibodies to spike), and the respective mean sojourns in *E*, I_p and I_s are 1/k, $1/\xi$, and $1/\gamma_s$ days (table 1).

4. Interventions

In prior work with populations subject to national regulations, officials in ministries of health and education helped us to model imposing and relaxing NPIs (e.g., closing schools and non-essential businesses, restricting meeting sizes, imposing curfews, requiring physical-distancing or mask-wearing in public places, and recommending outdoor or adequately-ventilated indoor activities) mechanistically for impact assessments, but – because their nature and timing was spatially heterogeneous in the United States – that is impractical.

4.1 Non-Pharmaceutical

In our model of the transmission of SARS-CoV-2 in the United States, we multiplied contact rates within locations by time-varying complements of Oxford Stringency Indices (Hale, et al. 2021) expressed as proportions (figure 7). For compliance, we scored responses (always = 1, frequently = 0.75, sometimes = 0.5, rarely = 0.25, never = 0) to "How often have you worn a face mask outside your home (e.g., when on public transport, going to a supermarket, going to a main road)?" by n = 33,940 US YouGov survey participants aged 18 to 99 years surveyed from March to December of 2020 (Jones 2020). Our parameter values are age-group averages from logistic regressions of scored responses as a cubic function of age (table 2).

4.2 Vaccination

In the United States, vaccination began on 14 December 2020 with healthcare and other essential workers, followed by those at risk of serious illness, hospitalization, or death (i.e., older adults and people who were immunocompromised), and then progressively younger people. Booster doses were not reported before 4 April 2021. Federal eligibility recommendations were generally followed, but jurisdictions differed in the levels of vaccine coverage or disease incidence at which NPIs were relaxed and re-imposed.

We have modeled vaccination using either 1) age-, time-, and location-specific immunization rates from the serological survey of blood donors (calculated as described in section 2.3) or 2) age-, time-, location-, and dose-specific reports to the CDC of vaccines administered.

In the first, susceptible people move directly to the removed class at weekly immunization rates. In the second, employed in the work described here, we determined age- and location-specific numbers of people eligible for vaccination (i.e., susceptible and vaccinated with one dose) at the beginning of each week by simulation, calculated the proportions vaccinated from the reported first and second doses administered that week, simulated with the corresponding rates, $\chi_1(i,j)$ and $\chi_2(i,j)$, and repeated the next week. We would calculate $\chi_3(i,j)$ similarly, but no booster doses were reported during the periods studied.

5. Simulation Results

Adjusting only the efficacy of physical-distancing when possible and mask-wearing otherwise at reducing susceptibility or infectiousness, $b_I = b_S = 0.31$, our model fits the prevalence of anti-N among those having commercial laboratory testing on 25 December 2020 quite well (figure 8a). Using the second method described above, doses administered reports to the CDC and efficacies of vaccination at preventing infections, $\epsilon_1 = \epsilon_2 =$

0.93 from El Sahly, et al. (2021), the lower of the two mRNA vaccines authorized for use at the time (Polack, et al. 2020), it fits the prevalence of anti-N or anti-S among blood donors on 4 April 2021 less well (figure 8b).

We compare reported and simulated symptomatic infections and deaths during the last quarter of 2020 and first few of 2021 (table 3). Case and death reports are from information summarized on the CDC's COVID Data Tracker, cited above. Our model predicts more infections, but fewer symptomatic ones than reported, and more deaths than reported between 6 September and 25 December 2020 and fewer between 25 December 2020 and 4 April 2021. The age-specific hospitalization rates of Clark, et al. (2020) are comparable to those from COVID-NET (https://www.cdc.gov/coronavirus/2019-ncov/covid-data/covid-net), which are based on surveillance of about 10% of the US population.

Predicted 4 April infections without vaccination resemble serology among commercial laboratory clients (figure 8d), suggesting that the discrepancy with vaccination (figure 8b) may be attributable to blood donors being disproportionately vaccinated (Busch, et al. 2022), including those previously infected. The discrepancy also may be explicable by vaccine doses administered being under-reported. Similarly, the above-mentioned comparison of reported and simulated cases and deaths suggests that infections were under-reported too.

5.1 Impact of Vaccination

Rather than comparing disparate simulations and reports, we compare simulated infections, hospitalizations, and deaths with and without vaccination (table 4). As one would expect, given that vaccination began mid-December in the United States, impact was modest during the last quarter of 2020 (7 September to 25 December). In contrast, impact during the period from 25 December 2020 to 4 April 2021 was substantial, particularly on symptomatic infections and hospitalizations.

We could also compare actual and hypothetical vaccination strategies the same way. The purpose of the initial strategy was to protect healthcare and other essential workers, then elderly and others at risk of serious disease, hospitalization, and death. Younger and healthier people were vaccinated subsequently.

Unquestionably, the optimal strategy for protecting healthcare and other essential workers is to vaccinate them. This direct approach also might be best for people at risk of serious disease, hospitalization, and death for reasons other than age, but the immune responses of older adults may be less effective than those of younger people. Accordingly, for example, higher dose influenza vaccines are recommended (https://www.cdc.gov/flu/highrisk/65over.htm).

6. Discussion

Early in the COVID-19 pandemic, we developed an SEIR-based framework for modeling the transmission of SARS-CoV-2 that we could use, together with locally-available information, to answer policy questions. In one instance, we used information from cell phone transmissions to determine which restrictions affected movements and then a location-stratified version of this model to determine the impact of movement restriction on transmission. In another, we used an age-stratified version to determine the impact of closing schools and otherwise limiting inter-personal contacts.

For this more recent US work, we estimated some parameters of an age- and location-stratified version of our model from nationwide seroprevalence studies and others from the literature. Initialized via seroprevalence on and incidence shortly before 7 September 2020, this model predicts seroprevalence well on 25 December 2020 and less well on 4 April 2021. The first evaluation compared seroprevalence from the same survey, among

people having commercial laboratory tests, from which it was initialized and the probabilities of infection on contact were estimated. The second compared seroprevalence among blood donors, who may be unusually wellness-oriented and hence disproportionately vaccinated. Also, results not reported here using immunization rates estimated from the survey of blood-donations (via the first approach described in section 4.2) are more concordant with observations from that survey, suggesting that vaccine doses administered may have been under-reported to the CDC.

Our model predicts more than twice as many infections as reported, most presumably asymptomatic or mildly symptomatic infections among people who were not tested, but the factor by which infections exceed reports declines over time (cf. Jones, et al. 2021). It also predicts more deaths than attributed to COVID-19 during the last quarter of 2020, most among older adults (because of the IFRs in table 2), and fewer afterwards.

Ability to experiment (i.e., to deduce the effects of phenomena by altering them individually) underlies the scientific method. While withholding measures of proven efficacy is unethical, we can experiment with models of pathogen transmission among the members of host populations. Because such models account for infections not caused by ones that are averted (i.e., indirect as well as direct effects of mitigation measures), these experiments assess the total impact of public health interventions, be they actual or hypothetical.

All models are imperfect, but alternative approaches also have shortcomings. Because it is impossible to control statistically for the extent to which the vaccination of others reduces the forces of infection to which unvaccinated people are subjected, natural experiments (e.g., Loeb, et al. 2010) under-estimate indirect effects. Similarly, all else never is equal, even in the best matched community intervention trials. In models, however, the impact of vaccination is the difference between infections, hospitalizations, and deaths with and without vaccination, but all other conditions identical (e.g., the same NPIs).

6.1 An Alternative Strategy

Vaccination policymakers generally envision protecting vulnerable people for whom vaccination is contraindicated by attaining a population immunity above which infectious people contact, on average, fewer than one susceptible person intimately enough to infect them. However, as Morens, et al. (2022) explain, waning immunity and pathogen evolution make attaining an effective reproduction number equal to one difficult for COVID-19. Moreover, in heterogeneous population models (e.g., with age or spatial structure), if not the real world, that condition could be attained via an infinite number of combinations of sub-population immunities (Feng, et al. 2015). The gradient (multivariate partial derivative) answers the question, "Which is optimal?"

Besides simulating our model with and without the actual vaccination strategy, we could also compare the actual strategy with a hypothetical alternative derived via the gradient of the effective reproduction number with respect to possible immunization rates. Fewer elderly people might be infected if those who otherwise might infect them were vaccinated instead. Feng, et al. (2015) advocated, and have since used (Feng, et al. 2017; Hao, et al. 2019; Feng, et al. 2020; Su, et al. 2021), the gradient of the effective reproduction number with respect to possible vaccination rates to identify strategies that would reduce the average number of secondary infections per primary most expeditiously. This is tantamount to determining which groups contribute most.

6.2 Limitations

We began modeling the transmission of SARS-CoV-2 long before effective vaccines were developed, much less approved for use, but – to keep pace with vaccination policy – added one, then two doses, and finally boosting of infection- or vaccine-induced immunity. However, we have since learned that the duration and possibly other

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characteristics of immunity may depend on whether an individual was infected, vaccinated or both, and possibly even the sequence of those events (Goldberg, et al. 2022). These developments and the evolution of variants, several successively dominant, motivated us to develop different models for later pandemic periods.

We have derived the reproduction numbers from our models and quantities, such as the gradient and population-immunity threshold, that can be derived from the effective number. We have written about this analytical work, including simulations comparing the actual and this alternative strategy (i.e., direct with indirect protection), and about the development and analysis of other models elsewhere (Vo, et al. submitted).

7. Summary

All models are imperfect, but – because measures to mitigate infectious diseases have indirect effects that are difficult to estimate via field studies – reliable transmission modeling arguably is the best way to assess their impact. Observations from cross-sectional serological surveys conducted in the United States from mid-summer 2020 through the end of 2021 provided the wherewithal for us to demonstrate that accurate transmission modeling is possible during pandemics. We modified the familiar SEIR model to include features of the biology of COVID-19 that might affect transmission of SARS-CoV-2 and consulted the primary literature or subject matter experts for contact rates and most other parameter values. We assessed the impact of vaccination, conditional on NPIs, in an age- and location-stratified model US population during the first quarter of 2021. Vaccination substantially reduced symptomatic infections, hospitalizations, and deaths.

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The vaccine doses administered from which, together with the numbers eligible for vaccination, we derived the age- and location-specific rates used in our simulations were compiled by Allison DeSantis and Arthur Presnetsov of the Vaccine Task Force's Data Monitoring and Reporting team. The seroprevalence studies were supported by the Centers for Disease Control and Prevention [via multiple contracts] and our modeling in part by the National Science Foundation [via DMS-1814545 to ZF].

Public-use summaries of these data are available via the CDC's COVID Data Tracker: <u>https://covid.cdc.gov/covid-data-tracker/#datatracker-home</u>. We used Mathematica 13.1 (Wolfram Research, Champaign, IL).

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Figures

Figure 1. Diagram of a modified SEIR Model. This metapopulation model includes asymptomatic and presymptomatic stages, disease-induced mortality, vaccination, and the waning and boosting of immunity, features of COVID-19 that affect SARS-CoV-2 transmission. It is cross-classified by age and location.



Figure 2. Seroprevalence in the United States. a) Bivariate logistic regression of observations from analyses of surplus sera from commercial laboratory testing for purposes other than evaluation of possible exposures to SARS-CoV-2. b) Slices through the surface at arbitrary times.







Figure 4. Probabilities of Infection upon Contact. We estimated other parameters of the *n* equations, $\lambda_i = a_i \beta_i \sum_{k=1}^{n} c_{ik} (I_k / N_k)$, from the information illustrated in figure 2a and synthetic US contact matrix (figure 3) and then solved them simultaneously for these unknown probabilities, β_i .



Figure 5. Contacts are a Function of Population Density. Multiplying contacts within locations (figure 3a) by ratios of natural logs of population density, a) saturating functions of density, and that of the entire country, b) reduces to twofold the difference in activities between the most and least densely populated locations.



Figure 6. Rates at which Contacts Decline with Distance. Proximity to others affects the probability of contacting them. Feng, et al. (2017) assumed an exponential function. Distances are between population centers (<u>https://www.census.gov/geographies/reference-files/2010/geo/2010-centers-population.html</u>).







Figure 8. Observed numbers with antibodies to SARS-CoV-2, from the national commercial laboratory (Anti-N) or blood donor (Anti-S or Anti-N) seroprevalence study, and predicted numbers temporarily immune (Removed) from simulations with (A and B) and without (C and D) vaccination on 25 December 2020 (A and C) and 4 April 2021 (B and D). Vaccination had no discernible impact on 25 December 2020 serology.



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Tables

Table 1. Symbol definitions, approximate values, and sources.

Symbol	Meaning	Values	Source
p_i	Proportions of Infectious people who are Asymptomatic (or	Tbl 2	Clark,
	Symptomatic, $1 - p_i$)		et al.
<i>a</i> .	Proportions not receiving booster doses when eligible	+	2020
q_i	Proportions not receiving booster doses when engible Per capita rate of progression from Exposed E to Asymptomatic I or	+	Ho ot
Γ.	Pre-symptomatic L_{a} (1/3 to 1/5 days depending on variant)	dvs	al
	The symptomatic, T_p (1/5 to 1/5 days depending on variancy	uys	2020
$\xi, \gamma_{s \to h}$	<i>Per capita</i> rates of progression from Pre-symptomatic, I_p to	1/2	He, et
2773 M	Symptomatic, I_s and Symptomatic to Hospitalized, I_h	dys	al.
			2020
Ya	<i>Per capita</i> rate at which people with Asymptomatic infections recover (become no longer infectious)	1/7	
γs	Per capita rate at which people with Symptomatic infections who are	1/5	He, et
	not hospitalized recover (again, become no longer infectious)	dys	al.
			2020
γh	Per capita rate at which Hospitalized people recover (NB: may well	1/10	
	differ from the discharge rate)	dys	
θ_w	Proportions of Symptomatic people who Recover (or Die, $1 - \theta_w$),	1012	Levin,
	which may differ among those Hospitalized ($w = s, h$)		et al.
δ	Proportions of Symptomatic people who are Hospitalized	Thl 2	Clark
	(proportions with 2+ co-morbidities)	1012	et al.
	ur print i i i i i i i i i i i i i i i i i i		2020
$\chi_{1i}, \chi_{2i},$	<i>Per capita</i> immunization rates $\chi = -\ln[1-v]/\delta t$, where v is the	‡	
X3i,	coverage attained during period δt		
E1 E2 E2	Probabilities of protection upon contact with infectious people 14 or	0.93	FI
-1, -2, -3	more days after first, second, and booster doses		Sahlv.
			et al.
			2021
ω, ω _ν	Per capita rates at which infection- and vaccine-induced immunity is	1/365	
	lost	dys	
c_i	Proportion of people complying with social distancing or mask	Tbl 2	Jones
	wearing recommendations (compliance)		2020
b_S, b_I	Reduced susceptibility or infectivity (efficacy) by virtue of complying	0.31	Estima
	with physical-distancing where possible and mask-wearing otherwise	0.5	ted
η_w	scaling constants ($w = a, p, h$) representing the infectivity of I_{ia} , I_{ip} , I_{ih}	0.5,	
		1.25,	
		0.1	1

Notes: We assume that people with asymptomatic infections are less infectious than those with symptomatic ones, but that their sojourns are the same. ‡Calculated from reports summarized on <u>https://data.cdc.gov/</u>.

Age	Population	Population	Pr(asymp inf)	Pr(hosp inf)	IFR	Compliance
	numbers	proportions			(percentages)	
0-4	19,676,332	0.059444636	0.981400373	1.0435E-05	0.0008	0.706360069
5-9	20,045,152	0.060558887	0.972064267	0.000143099	0.001312163	0.715211185
10-14	21,089,487	0.063713953	0.969763501	0.00027027	0.002400084	0.71952257
15-19	21,242,908	0.064177457	0.960291933	0.003637205	0.004390005	0.720175768
20-24	22,258,745	0.067246426	0.941577238	0.006854725	0.00802978	0.71795013
25-29	23,835,330	0.072009485	0.913456364	0.017709616	0.014687309	0.713574937
30-34	23,052,479	0.069644395	0.880594618	0.025217824	0.026864628	0.707771036
35-39	21,615,791	0.065303982	0.839642887	0.035166793	0.049138219	0.701279533
40-44	20,294,599	0.061312498	0.775783537	0.037368978	0.08987895	0.694876881
45-49	20,053,798	0.060585008	0.708076043	0.051520404	0.164398026	0.689376822
50-54	20,577,807	0.062168104	0.623043155	0.062486388	0.300701205	0.685620487
55-59	21,542,270	0.065081866	0.521907521	0.083247801	0.550014019	0.684456022
60-64	20,669,143	0.062444041	0.421531351	0.090697794	1.006033295	0.686708224
65-69	17,819,027	0.053833488	0.328351424	0.110144916	1.8 <mark>4</mark> 0140307	0.693136453
70-74	14,354,863	0.043367819	0.2503706	0.118491978	3.365809369	0.704376296
75+	22,874,916	0.069107955	0.163464241	0.139755917	14.30030403	0.744380002
Wtd			0.715196	0.047154	1.373312	0.705841
Avg						

Table 2. Parameter values for age-stratified transmission modeling in the United States

Notes: Populations, proportions without co-morbidities (assumed asymptomatic) and requiring hospitalization if infected are from Clarke, et al. (2020), the infection-fatality ratios (IFRs) are from Levin, et al. (2020), and the compliances are our estimates, obtained from Jones (2020) as described in the text.

Table 3. Reported infections and deaths (<u>https://covid.cdc.gov/covid-data-tracker/#datatracker-home</u>) and simulated infections, hospitalizations, and deaths during the periods from 6 September to 25 December 2020 and from 25 December 2020 to 4 April 2021.

	6 Sep to 25	5 Dec 2020	25 Dec to 4 Apr 2021		
Outcomes	Reported	Simulated	Reported	Simulated	
Cases or Infections	12,545,671	45,075,200	11,603,565	23,635,060	
Hospitalizations		1,766,850		974,486	
Deaths	147,776	176,342	214,902	120,978	

Notes: Cases are reported, infections are simulated, of which roughly 75% are asymptomatic. Consequently, fewer symptomatic infections are predicted than cases reported. More deaths were simulated than reported during the first period, but fewer during the second. Hospitalizations are not compiled, but rates from surveillance of about 10% of the US population are available (https://gis.cdc.gov/grasp/COVIDNet/COVID19_3.html).

	6 Sep to 25 Dec 2020			25 Dec 2020 to 4 Apr 2021		
Outcomes	Without	With	Averted	Without	With	Averted
Asymptomatic	34,739,600	33,911,200	828,400	26,721,000	17,958,500	8,762,500
Infections			(2.38%)			(32.79%)
Symptomatic	11,447,400	11,164,000	283,400	9,389,030	5,676,560	3,712,470
Infections			(2.48%)			(39.54%)
Hospitalizations	1,813,190	1,766,850	46,340	1,608,080	974,486	633,594
			(2.56%)			(39.4%)
Deaths	176,349	176,342	7	172,549	120,978	51,571
			(<0.01%)			(29.89%)

Table 4. Results of simulations with and without vaccination to deduce by difference its impact during the periods from 6 September to 25 December 2020 and from 25 December 2020 to 4 April 2021.

Notes: As vaccination began mid-December 2020 in the United States, one would not expect much impact during the first period.

Highlights

- Metapopulation SEIR model of SARS-CoV-2 transmission in the US
- All parameters save efficacy of NPIs estimated independently
- Initialized on 7 September, reproduces seroprevalence on 25 December 2020
- Evaluated vaccination, conditional on NPIs, through 4 April 2021
- Symptomatic infections, hospitalizations, and deaths reduced by 30-40%

JG, ZF – Conceptualization;

- JJ, KC Data curation;
- ZF, MV Formal analysis;
- JJ, KC, ZF Funding acquisition;
- JG, ZF, MV Methodology;
- JJ, KC Supervision;
- JG, ZF, MV Visualization;
- JG Writing original draft;
- ZF, MV, KC, JJ Writing review & editing