

## Research Article

# Accurate Adiabatic and Diabatic Potential Energy Surfaces for the Reaction of He + H<sub>2</sub>

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The accurate adiabatic and diabatic potential energy surfaces, which are for the two lowest states of He + H<sub>2</sub>, are presented in this study. The Molpro 2012 software package is used, and the large basis sets (aug-cc-pV5Z) are selected. The high-level MCSCF/MRCI method is employed to calculate the adiabatic potential energy points of the title reaction system. The triatomic reaction system is described by Jacobi coordinates, and the adiabatic potential energy surfaces are fitted accurately using the B-spline method. The equilibrium structures and electronic energies for the H<sub>2</sub> are provided, and the corresponding different levels of vibrational energies of the ground state are deduced. To better express the diabatic process of the whole reaction, avoid crossing points being calculated and conical intersection also being optimized. Meanwhile, the diabatic potential energy surfaces of the reaction process are constructed. This study will be helpful for the analysis of histopathology and for the study in biological and medical mechanisms.

## 1. Introduction

Helium and hydrogen atoms were the most abundant substances in the universe [1]. The heating led to the rotation and vibration of the H<sub>2</sub> molecule in the universe when helium collided with H<sub>2</sub> in the molecular cloud. In the interstellar medium, the formation of stars was quite closely linked to their interactions, which suggested that the interactions between helium and hydrogen atoms were of particular interest. Therefore, the reaction between He and H<sub>2</sub> was necessary to know the star formation in physics and chemistry, which was essential to understand the properties of many astrophysical objects. In addition, many researchers had constructed diabatic potential energy surfaces [2–16], so the construction of the global potential energy surfaces was an essential prerequisite for the title reaction. Which was an essential prerequisite for the study of molecular reaction kinetics.

Many years ago, the He + H<sub>2</sub> reaction system was studied by experimental [17–21] and theoretical [1, 22–35] researchers. In 1963, Roberts [36] obtained the interaction energy of the HeH<sub>2</sub> system at a relatively large center of charge separation. Subsequently, the interaction potential between He and H<sub>2</sub> was studied by Krauss and Mies [23], who got conclusion that the forces are comparable for collisions along the centerline and along the molecular parallels. Henry and co-workers [37] constructed and calculated each atom in the HeH<sub>2</sub> system separately using Gaussian basis functions. The calculated 416 configurations were used to predict the van der Waals interaction between the lowest state of the helium atom and the hydrogen molecule. At the same time, Gengenbach and Hahn [20] constructed the earliest empirical potential energy surface for He-H<sub>2</sub>. Wilson's work [26] proposed a universal expression for the HeH<sub>2</sub> potential energy surfaces with a straightforward function. Soon after that, Dove and Raynor [38] improved and

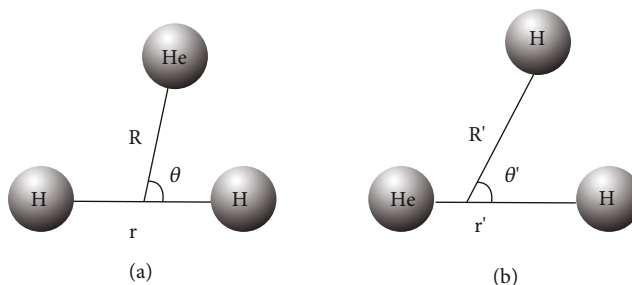


FIGURE 1: (a) Reactant Jacobi coordinate. (b) Product Jacobi coordinate.

TABLE 1: Calculation range of reactant part.

Calculation range of reactant part	
$R$ (He-HH, Å)	0.4, 0.6, 0.8, 1.0, 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9, 2.0, 2.1, 2.2, 2.3, 2.4, 2.6, 2.8, 3.0, 3.2, 3.4, 3.6, 3.8, 4.0, 4.2, 4.4, 4.6, 4.8, 5.0, 5.2, 5.4, 5.6, 5.8, 6.0
$r$ (HH, Å)	0.4, 0.6, 0.7, 0.72, 0.74, 0.75, 0.76, 0.8, 1.0, 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9, 2.0, 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8, 2.9, 3.0, 3.2, 3.4, 3.6, 3.8, 4.0
$\theta$ (degree)	0, 10, 20, 30, 40, 50, 60, 70, 80, 90

$R$  (He-HH, Å): bond length from helium to the center of mass between two hydrogens, the unit is Å.  $r$  (HH, Å): bond length between two hydrogen atoms, the unit is Å.  $\theta$  (degree): the angle between  $R$  and  $r$ , the unit is degree.

TABLE 2: Calculation range of products part.

Calculation range of products part	
$R'$ (H-HeH, Å)	0.4, 0.6, 0.8, 1.0, 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9, 2.0, 2.1, 2.2, 2.3, 2.4, 2.6, 2.8, 3.0, 3.2, 3.4, 3.6, 3.8, 4.0, 4.2, 4.4, 4.6, 4.8, 5.0, 5.2, 5.4, 5.6, 5.8, 6.0
$r'$ (HeH, Å)	0.4, 0.6, 0.7, 0.8, 1.0, 1.1, 1.2, 1.3, 1.4, 1.5, 1.6, 1.7, 1.8, 1.9, 2.0, 2.1, 2.2, 2.3, 2.4, 2.5, 2.6, 2.7, 2.8, 2.9, 3.0, 3.2, 3.4, 3.6, 3.8, 4.0
$\theta'$ (degree)	0, 10, 20, 30, 40, 50, 60, 70, 80, 90, 100, 110, 120, 130, 140, 150, 160, 170, 180

$R'$  (H-HeH, Å): bond length from the hydrogen atom to the center of mass between helium and hydrogen, the unit is Å.  $r'$  (HeH, Å): bond length between helium and hydrogen atoms, the unit is Å.  $\theta'$  (degree): the angle between  $R'$  and  $r'$ , the unit is degree.

optimized these potential energy surfaces. Meanwhile, they studied the collisional dissociation of He to H<sub>2</sub>. The ground and excited state potential energy surfaces were constructed for the HeH<sub>2</sub> system by Stavros [36], who used the *ab initio* MRD CI calculation method. Up to 2003, Arnold and Peter [1] employed the *ab initio* method and calculated 20203 energy points in the interaction region of HeH<sub>2</sub>, which had an improvement and enhancement compared with previous scholars. Cavity-enhanced spectra of He-H<sub>2</sub> were discussed by Słowiński et al. [39], and the results also showed that *ab initio* calculations could provide reference data for atmospheric spectroscopy studies. In the laboratory, the collision of hydrogen molecular and helium atoms would create ultracold molecules. Hence, the interaction between He and H<sub>2</sub> was also an essential factor in determining the properties of hydrogen clusters within helium.

In order to getting the precisely potential energy surfaces, the large range is used to scan. the large basis sets (aug-cc-pV5Z) were selected, and the three energy states of the He + H<sub>2</sub> system were calculated, using high-level MCSCF/MRCI. Secondly, the energy points were fitted using the B-spline method. Finally, as electrons would transfer near the interaction area, the conical intersection was opti-

mized, and the avoided crossing points were studied. Meanwhile, the adiabatic and diabatic potential energy surfaces were constructed for this reaction system.

The study was organized as follows: in the next section, a brief overview of the theoretical calculation method; the adiabatic and diabatic potential energy surfaces of He + H<sub>2</sub> were presented in the third chapter. And the simple summary and the conclusion would be shown in the fourth chapter.

## 2. Computational Methods

**2.1. Ab Initio Calculations.** The MOLPRO 2012 [40] package was used to perform all *ab initio* single-point energies at the high-level method (MCSCF/MRCI) with large basis sets (aug-cc-pV5Z) [41]. The three lowest state adiabatic potential energies were calculated in the He + H<sub>2</sub> reaction system. There were 4 electrons in the orbital, including 15 active orbitals and 229 external orbitals (141A'+88A''). The Jacobi ( $r, R, \theta$ ) coordinates were selected for this triatomic system, which was widely used in our former studies [42–49]. The configuration coordinates (Figure 1) were illustrated to describe the reaction of the triatomic molecules.

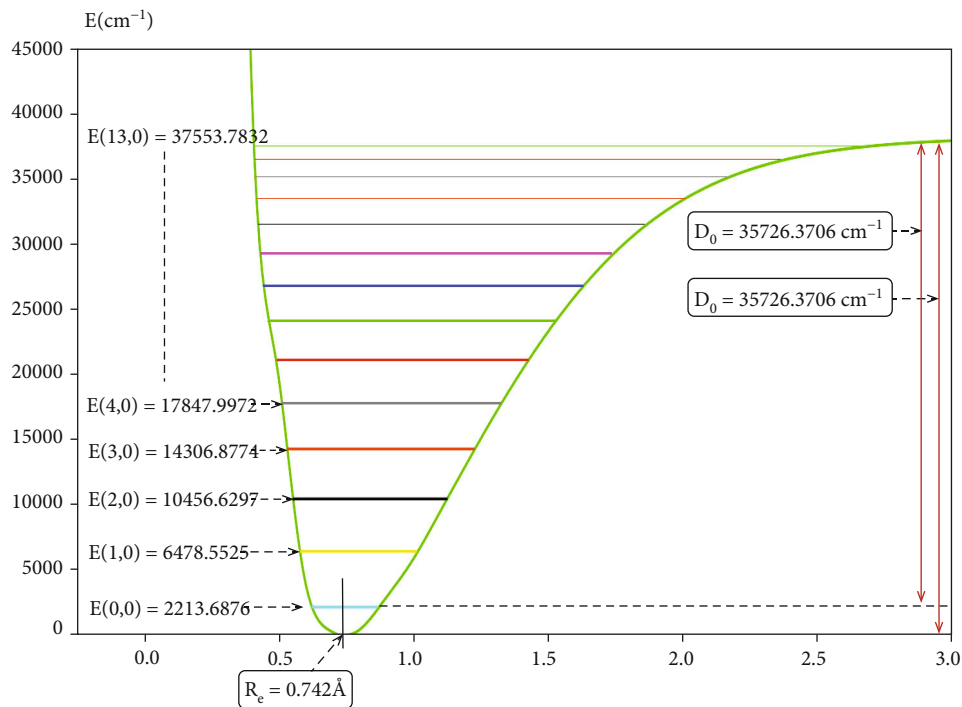


FIGURE 2: The one-dimensional potential energy surfaces for  $H_2$  molecule as a function of distances  $r_{H-H}$  (in Å) and its different vibrational state energies  $E(v, j=0)$  (in  $cm^{-1}$ ).

TABLE 3: Spectroscopic constants for  $H_2$ .

$H_2 (X^1\Sigma_g^+)$	$R_e$ (Å)	$D_0$ ( $cm^{-1}$ )	$D_e$ ( $cm^{-1}$ )
This work	0.742	35726.3706	37940.0582
Lee's work [49]	0.743	35687	37868
Yuan's work [50]	0.7414		38313.2
He's work [51]	0.7418		38186.2
Expt.	0.742 [52]	36118.06 [53]	38288 [52]

$R_e$  (Å): the equilibrium bond length of the  $H_2$ , the unit is Å.  $D_0$  ( $cm^{-1}$ ): the experimental dissociation energy of the  $H_2$ , the unit is  $cm^{-1}$ .  $D_e$  ( $cm^{-1}$ ): the equilibrium dissociation energy of the  $H_2$ , the unit is  $cm^{-1}$ .

The angle was determined from  $0^\circ$  to  $90^\circ$  with the grids at  $10^\circ$  for the reactants and field, and 12960 adiabatic potential energy points were calculated independently for each electronic state energy. For the products region, 21888 points were scanned at an angle of  $0^\circ$  to  $180^\circ$ . For each electronic state energy in the reactants and products, 34848 adiabatic potential energy points were measured, which guaranteed that the adiabatic potential energy surfaces were reliable. Tables 1 and 2 indicate the scan ranges of reactants and products, respectively. The B-spline method was used to fit the potential energy surface for this process. This method may be useful for the analysis of histopathology and for the study in biological and medical mechanisms.

**2.2. Mixing Angle ( $\alpha$ ) Calculation.** The wave functions of the three lowest states were  $\psi_1^a$ ,  $\psi_2^a$ , and  $\psi_3^a$  respectively, and the

adiabatic wave functions for the two lowest states were expressed as:

$$\begin{pmatrix} \Psi_1^d \\ \Psi_2^d \end{pmatrix} = \begin{pmatrix} \cos a & \sin a \\ -\sin a & \cos a \end{pmatrix} \begin{pmatrix} \varphi_1^a \\ \varphi_2^a \end{pmatrix}, \quad (1)$$

where  $\alpha$  was denoted as the mixing angles, and the energy of the diabatic potential energy ( $H_{ii}^d$ ) was obtained by fitting the adiabatic potential energy ( $E_i^a$ ):

$$H_{11}^d = \cos^2 a E_1^a + \sin^2 a E_2^a, \quad (2)$$

$$H_{22}^d = \sin^2 a E_1^a + \cos^2 a E_2^a, \quad (3)$$

$$H_{12}^d = H_{21}^d = \sin a \cos a (E_2^a - E_1^a), \quad (4)$$

$$H_{12}^d = H_{21}^d. \quad (5)$$

$H_{11}^d$  and  $H_{21}^d$  were the coupling energy between the two states. The  $\hat{P}_z$  was the Z component of the dipole moment operator. The following equation was obtained:

$$\langle \Psi_3^a | \hat{P}_z | \Psi_1^a \rangle = \sin a \langle \Psi_3^a | \hat{P}_z | \varphi_2^d \rangle + \cos a \langle \Psi_3^a | \hat{P}_z | \varphi_1^d \rangle, \quad (6)$$

$$\langle \Psi_3^a | \hat{P}_z | \Psi_2^a \rangle = -\sin a \langle \Psi_3^a | \hat{P}_z | \varphi_1^d \rangle + \cos a \langle \Psi_3^a | \hat{P}_z | \varphi_2^d \rangle. \quad (7)$$

$\langle \Psi_3^a | \hat{P}_z | \varphi_1^d \rangle$  and  $\langle \Psi_3^a | \hat{P}_z | \varphi_2^d \rangle$  were both highly symmetric

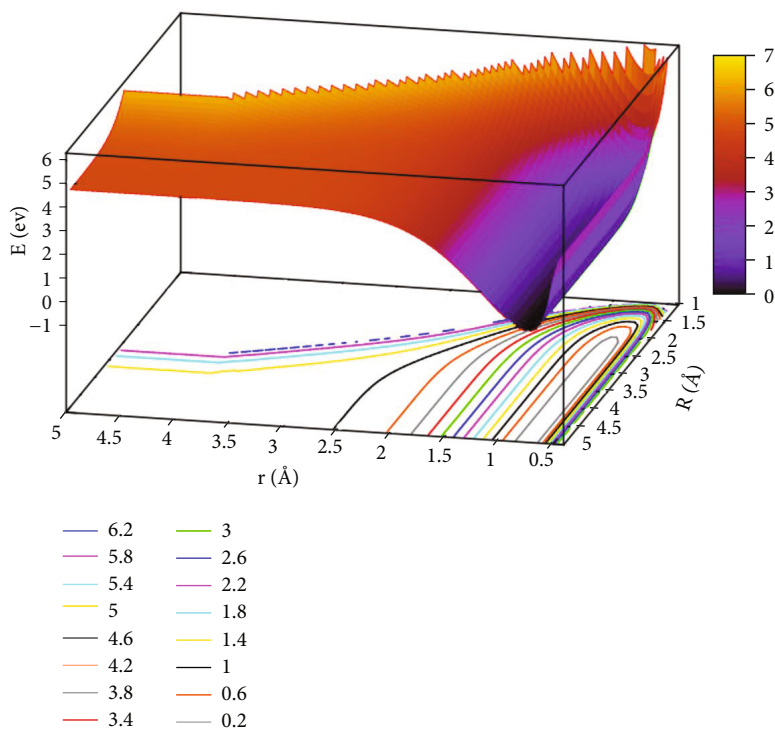


FIGURE 3: The lowest state potential energy surface (in eV) for the reaction of He + H<sub>2</sub> at  $\theta=0.0^\circ$  in Jacobi coordinate.

matrices:

$$\langle \Psi_3^a | \hat{P}_z | \varphi_1^a \rangle = 0, \quad (8)$$

$$\langle \Psi_3^a | \hat{P}_z | \varphi_2^a \rangle = 1. \quad (9)$$

Thus, the mixing angles were obtained as:

$$a = \arctan \left( \left| \frac{\langle \Psi_3^a | \hat{P}_z | \Psi_1^a \rangle}{\langle \Psi_3^a | \hat{P}_z | \Psi_2^a \rangle} \right| \right). \quad (10)$$

The main idea of the method for the mixing angle calculation can be used for histopathology after optimizing.

### 3. Results and Discussion

The lowest ground state and the first excited state potential energy surfaces were constructed in this reaction system with angles (including  $0^\circ$ ,  $30^\circ$ ,  $50^\circ$ ,  $60^\circ$ , and  $90^\circ$ ), sequentially. To more clearly and specifically display the potential energy surfaces, the lowest state energy of the He + H<sub>2</sub> was shifted at 0.00 eV, and the results were analyzed as follows.

**3.1. One-Dimensional Diatomic Adiabatic Potential Surface.** Figure 2 shows the equilibrium bond length ( $R_e$ ) of the H<sub>2</sub> molecule was  $0.742 \text{ \AA}$ , and the dissociation energy ( $D_e$ ) was  $37940.0582 \text{ cm}^{-1}$ . From the image, it was clearly found that a total of 13 vibrational states in the one-dimensional potential energy surface, and the zero point energy of the diatomic molecule was  $E(0,0) = 2213.6876 \text{ cm}^{-1}$ , and the highest vibrational energy was  $E(13,0) = 37553.7832 \text{ cm}^{-1}$ .

The spectroscopic constants for H<sub>2</sub> are presented in Table 3. The data were found to be in good agreement with the theoretical and experimental researchers, such as Lee, Yuan, and He, which indicated that the calculations were more specific in this study.

### 3.2. Two-Dimensional Adiabatic Potential Energy Surfaces.

The lowest potential energy for the He + H<sub>2</sub> reaction system at  $\theta=0.0^\circ$  is seen in Figure 3. All the potential energy surface curves were very smooth. The self-variable for  $x$ ,  $y$ , and  $z$  were represented by  $r$  (in  $\text{\AA}$ ),  $R$  (in  $\text{\AA}$ ), and  $E$  (in eV). The contour intervals of the potential energy surface were  $0.40 \text{ eV}$ . When  $r > 2.0 \text{ \AA}$  and  $R > 3.0 \text{ \AA}$ , the distance between contours was relatively sparse, which implies that the energy was comparable. When  $1.0 \text{ \AA} > r > 0.5 \text{ \AA}$  and  $R > 2.5 \text{ \AA}$  was the entrance area in the reaction. The entrance part of the reaction had no reaction barrier, the potential energy surface had no minimum geometries, and there was no stable configuration. To more intuitively reflect the lowest ground state and the first excited state potential energy surfaces, we plotted the first excited state potential energy surfaces.

Figure 4 depicts the first excited state potential energy surface at  $\theta=0.0^\circ$ . When the He atom collision with H<sub>2</sub> along a straight line, the geometry crossing a transition state TS<sub>1</sub> (Panel B) would form the M<sub>1</sub> (Panel A). The M<sub>1</sub> configuration was  $r=1.15 \text{ \AA}$  and  $R=1.44 \text{ \AA}$ , and the energy was  $11.870 \text{ eV}$ . The energy of the TS<sub>1</sub> (Panel B) was about  $12.037 \text{ eV}$ , when the distance was  $R=1.85 \text{ \AA}$ ,  $r=1.06$ . It indicated that when He attacked with H<sub>2</sub>, it possibly generated a stable configuration (M<sub>1</sub>). Similarly, the complex (M<sub>1</sub>) overcame the TS<sub>2</sub> (Panel C) which would form the M<sub>2</sub>, the complex (M<sub>2</sub>) with  $r=2.66 \text{ \AA}$  and  $R=2.21 \text{ \AA}$ , and the energy value

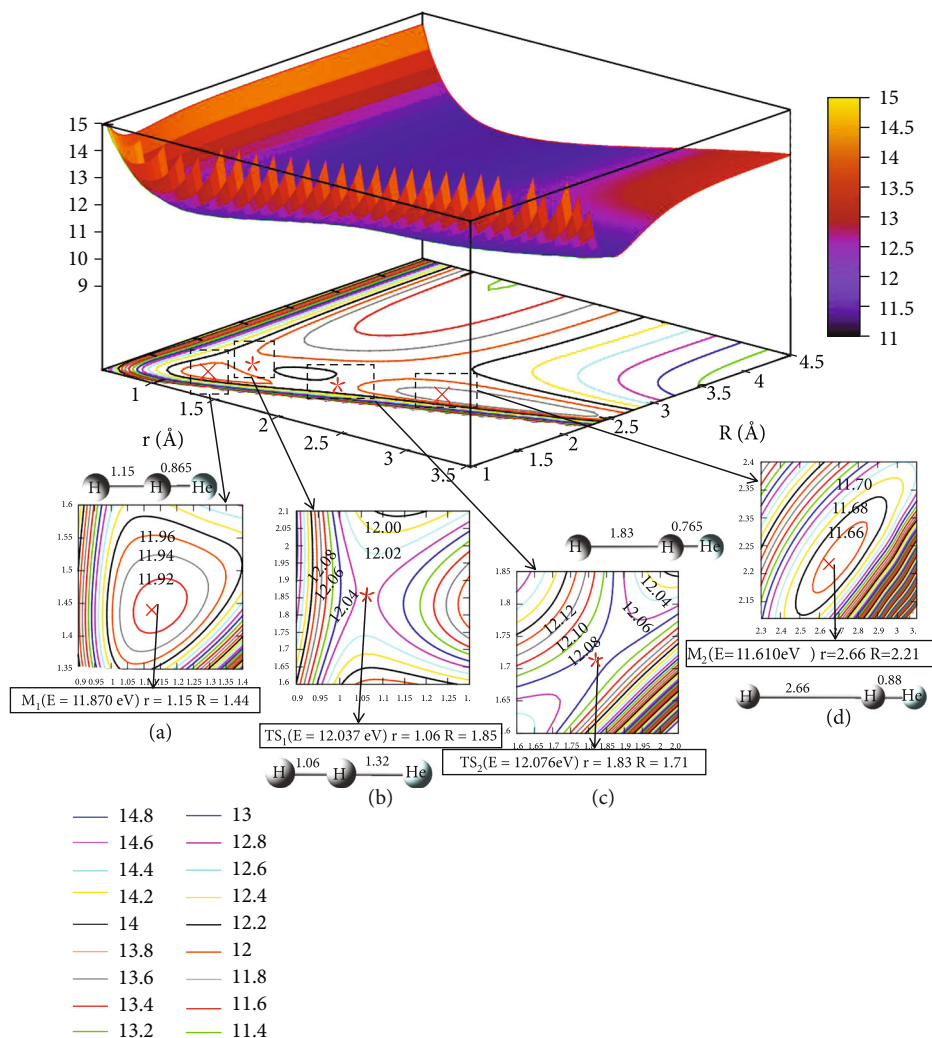


FIGURE 4: The first excited state potential energy surface (in eV) for the reaction of He + H<sub>2</sub> at  $\theta = 0.0^\circ$  in Jacobi coordinate.

was 11.610 eV. To sum up, the energy of M<sub>2</sub> was 11.610 eV, which was slightly lower than the M<sub>1</sub>.

The character of Figure 5 exhibited the lowest state for potential energy surfaces when the angle was 30.0°. From the figure, the energy between adjacent contours was 0.40 eV in the contours plot, and the potential energy values became smaller as the value of  $r$  and  $R$  decreased. When  $R > 2.5 \text{ \AA}$  and  $0.5 \text{ \AA} < r < 1.0 \text{ \AA}$ , which was the entrance part of the reactants. There were no obvious minimum at the lowest potential energy surface and no stable configuration in this region. In order to express this process more clearly and distinctly, we also plotted the first excited state potential energy surface. As shown in Figure 6, when  $r$  was in the range of 1.0 Å to 1.5 Å and  $R > 3.0 \text{ \AA}$ , which was the entrance region for the reactants. As  $R$  gradually became smaller and  $r$  became larger, the potential energy surface appeared at a saddle point (TS<sub>3</sub>) at  $r=1.25 \text{ \AA}$  and  $R=1.73 \text{ \AA}$ , and the energy was 11.776 eV. Crossing the saddle point, a minimum (M<sub>3</sub>) would form gradually. The configuration of M<sub>3</sub> was  $r$  equal to 2.65 Å and  $R$  equal to 0.88 Å, and the minimum energy was 10.147 eV.

When the angle was 50.0°, Figure 7 depicts the image of the potential energy surfaces of the ground state. In the region of  $0.5 \text{ \AA} < r < 1.0 \text{ \AA}$  and  $R > 4.0 \text{ \AA}$ , which was the reaction entrance of the lowest state potential energy surface, and there was no obvious minimum and stable configuration. To better illustrate this process, we also showed the potential energy surfaces of excited state for the He + H<sub>2</sub> reaction system, which was described in Figure 8. It is clear that for  $1.0 \text{ \AA} < r < 1.5 \text{ \AA}$  and  $R > 2.5 \text{ \AA}$ , the energy hardly changes with  $R$ , which indicated the entrance part of the reactant. As the helium atom gradually approached the center of mass of the two hydrogen atoms, the minimum (M<sub>4</sub>) was formed, where at  $r=1.90 \text{ \AA}$  and  $R=0.84 \text{ \AA}$ , and the energy was 9.616 eV, which was the global minimum of the first excited state.

The lowest state potential energy surface and contour plot at  $\theta=60.0^\circ$  are shown in Figure 9. There was no minimum in the lowest state potential energy surface. In the range of  $0.5 \text{ \AA} < r < 1.0 \text{ \AA}$  and  $R > 4.0 \text{ \AA}$ , the potential energy hardly changes with increasing  $R$ , so the region was the entrance region of the reactant. Similarly, we plotted the first excited state potential energy surface and contours plot in Figure 10.

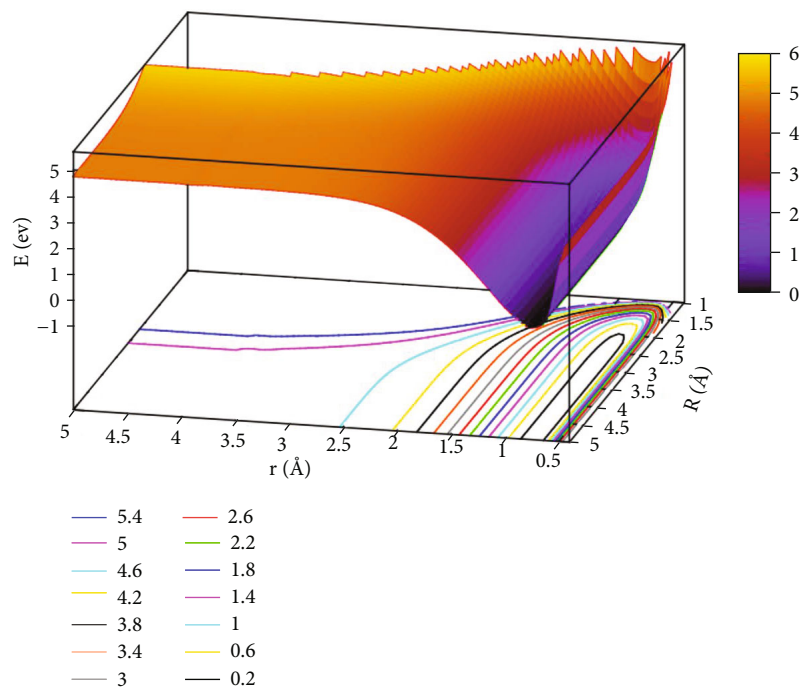


FIGURE 5: The lowest state potential energy surface (in eV) for the reaction of He + H<sub>2</sub> at  $\theta=30.0^\circ$  in Jacobi coordinate.

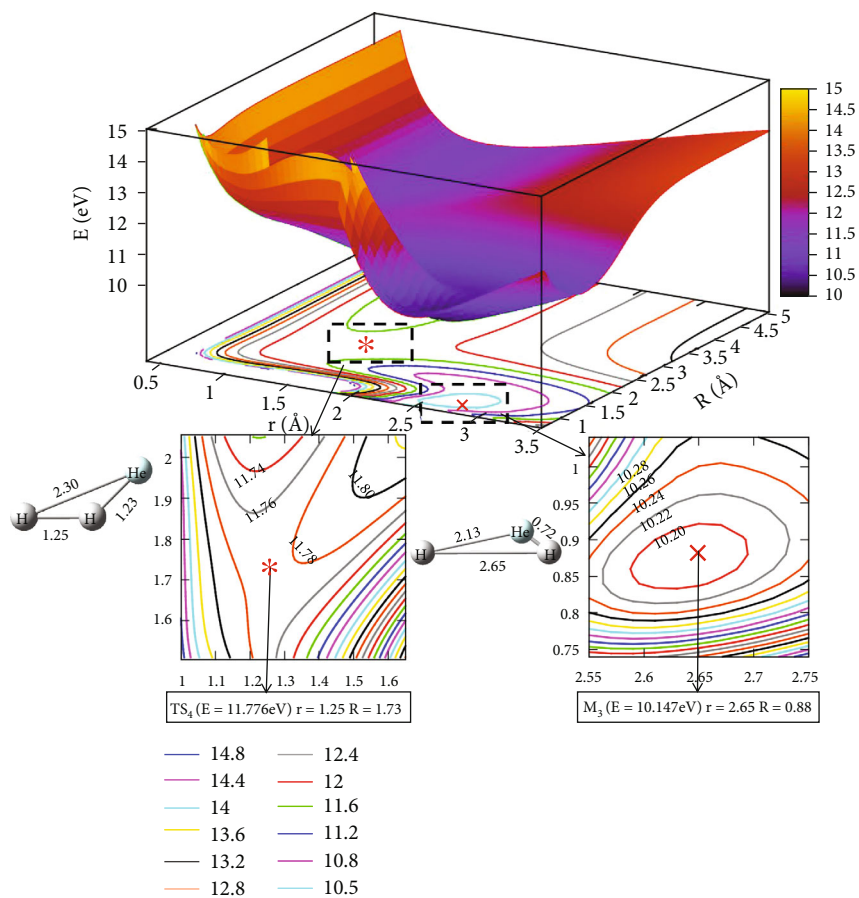


FIGURE 6: The first excited state potential energy surface (in eV) for the reaction of He + H<sub>2</sub> at  $\theta=30.0^\circ$  in Jacobi coordinate.

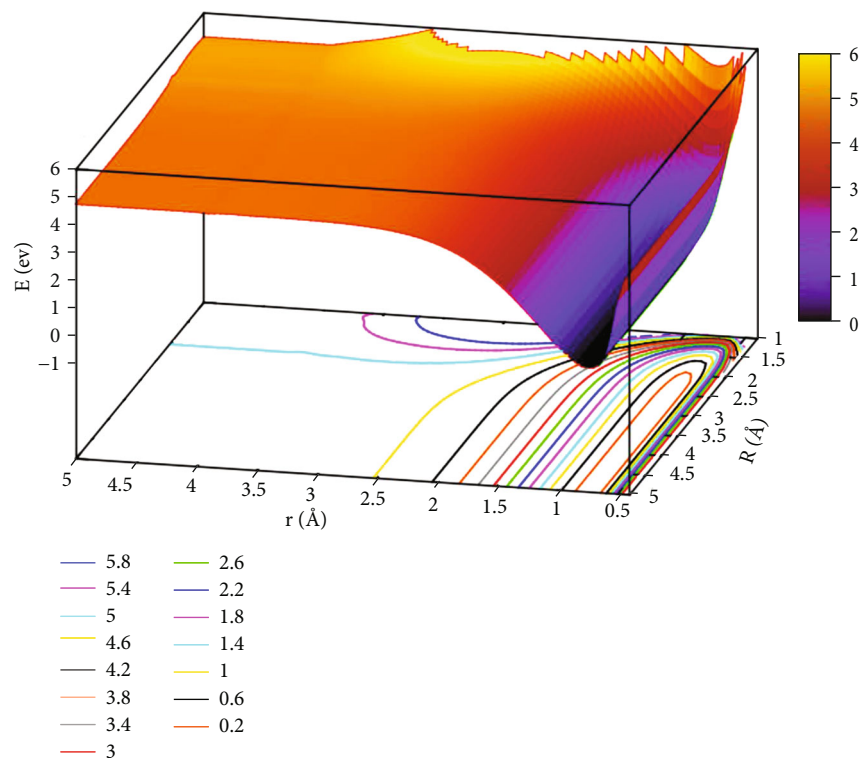


FIGURE 7: The lowest state potential energy surface (in eV) for the reaction of He + H<sub>2</sub> at  $\theta=50.0^\circ$  in Jacobi coordinate.

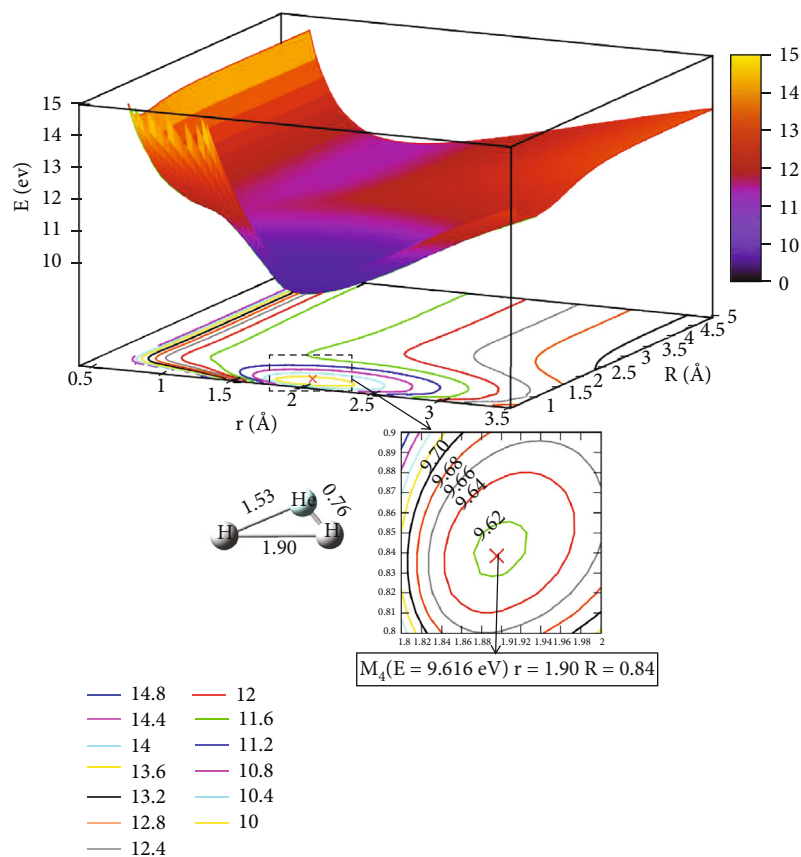


FIGURE 8: The first excited state potential energy surface (in eV) for the reaction of He + H<sub>2</sub> at  $\theta = 50.0^\circ$  in Jacobi coordinate.

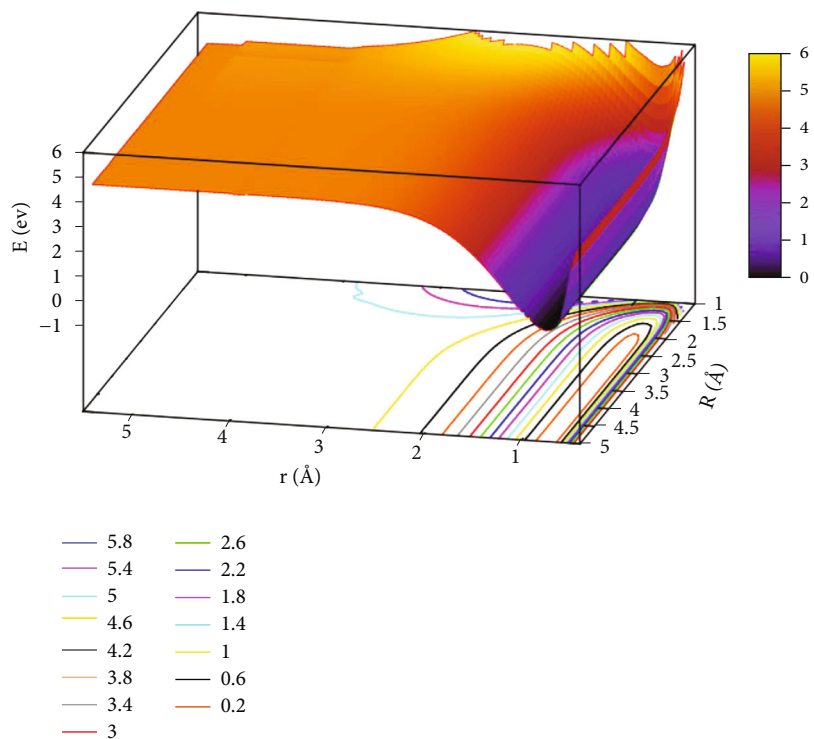


FIGURE 9: The lowest state potential energy surface (in eV) for He + H<sub>2</sub> at  $\theta = 60.0^\circ$  in Jacobi coordinate.

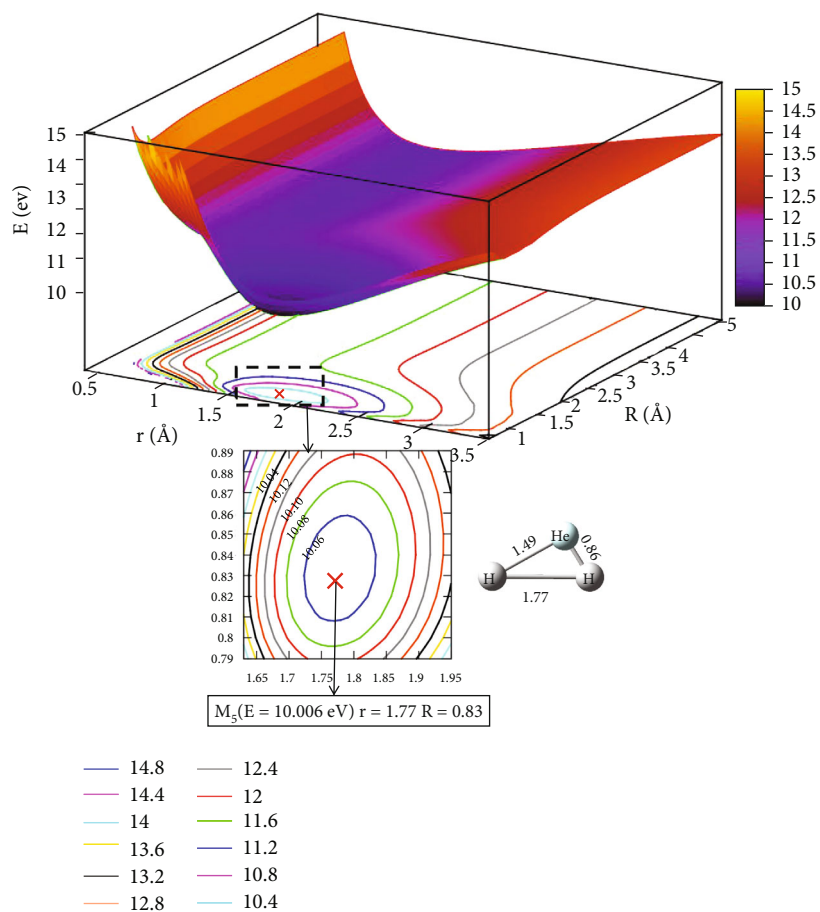


FIGURE 10: The first excited state potential energy surface (in eV) for the reaction of the He + H<sub>2</sub> at  $\theta=60.0^\circ$  in Jacobi coordinate.



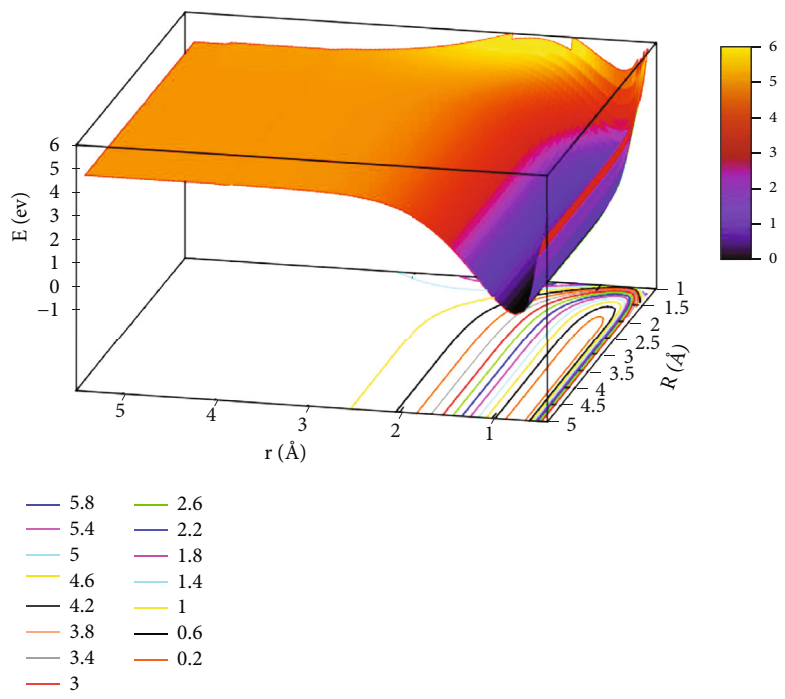


FIGURE 11: The lowest state potential energy surface (in eV) for He + H<sub>2</sub> at  $\theta = 90.0^\circ$  in Jacobi coordinate.

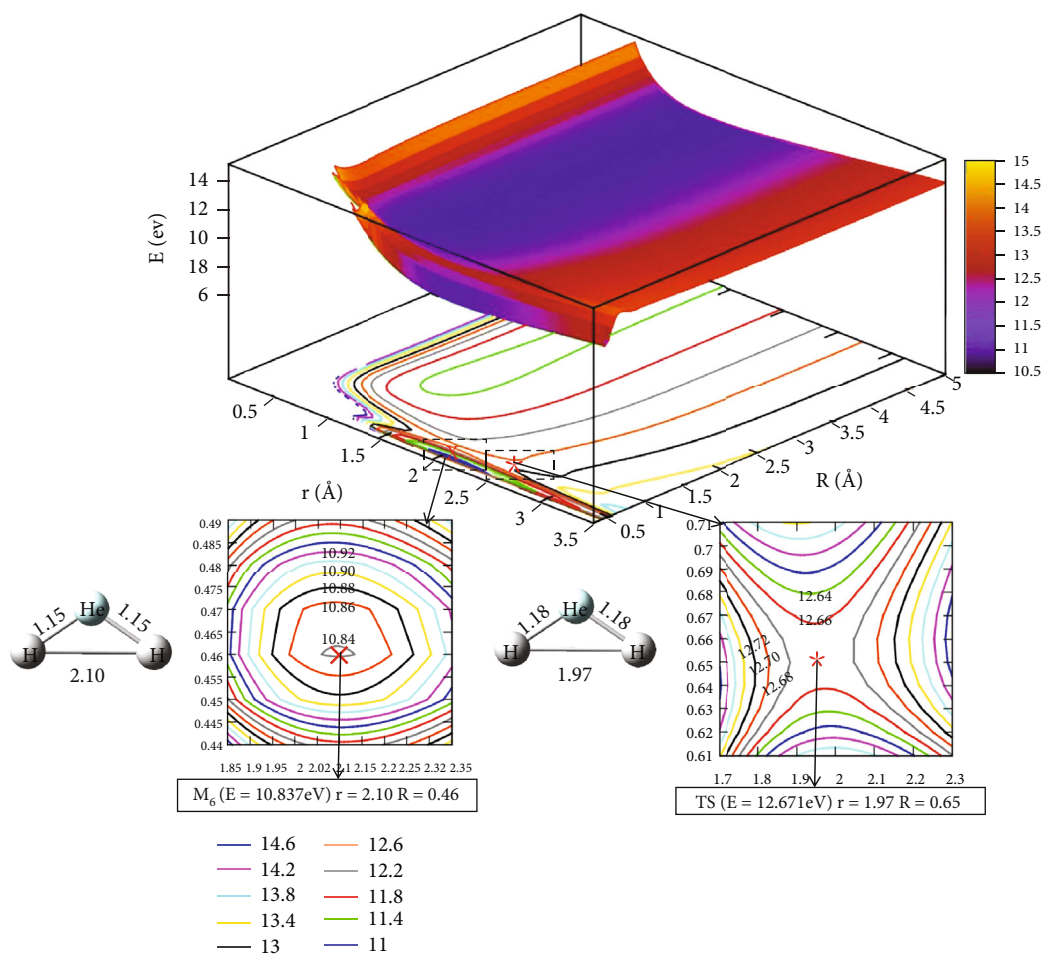


FIGURE 12: The first excited state potential energy surface (in eV) for the reaction of He + H<sub>2</sub> at  $\theta = 90.0^\circ$  in Jacobi coordinate.

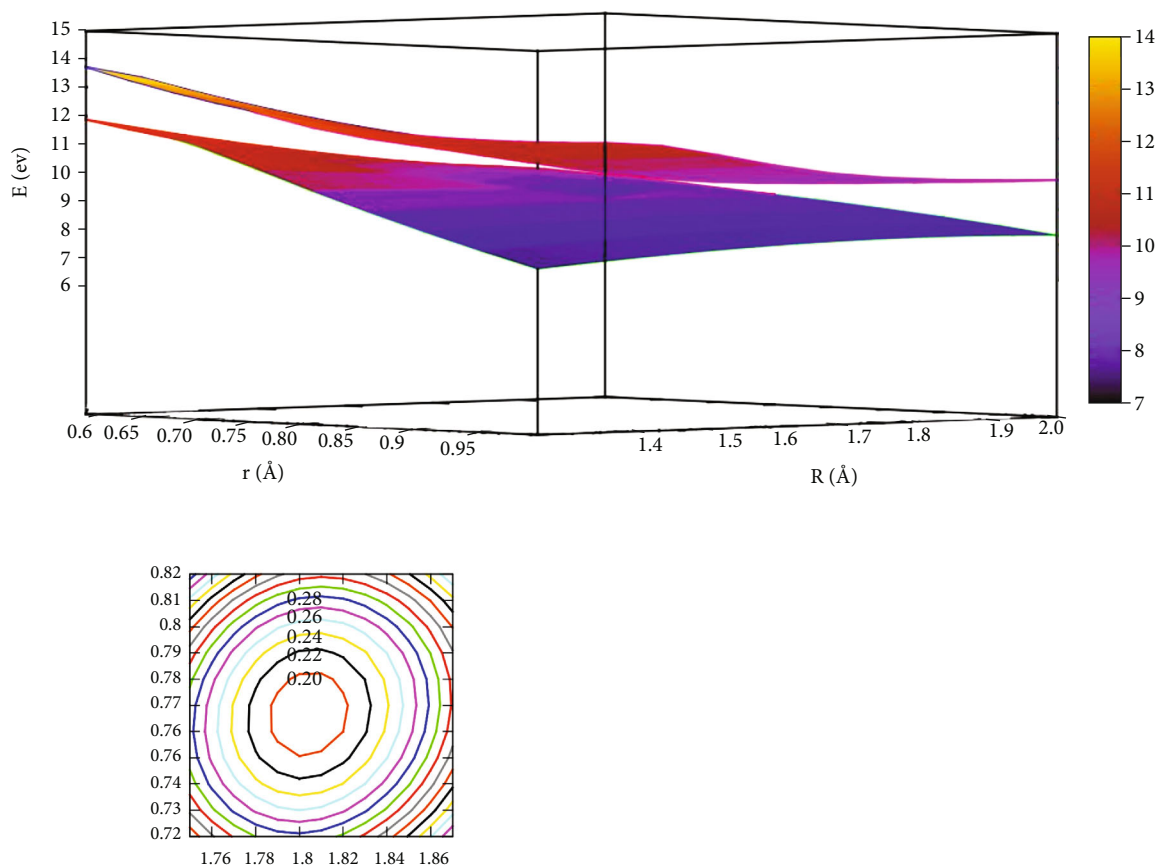


FIGURE 13: Avoid crossing point for the lowest state and the first excited state of He + H<sub>2</sub> reaction.

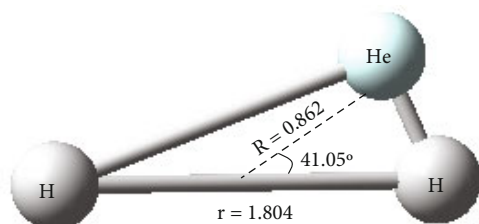


FIGURE 14: The conical intersection structure for He + H<sub>2</sub>.

There was a complex ( $M_5$ ) formed, which had an energy value of 10.006 eV when  $r=1.77$  Å and  $R=0.83$  Å. It was different from the energy value of  $\theta=50^\circ$ . It can be seen that  $M_5$  was not the global minimum of the whole reaction system.

Figure 11 presents the lowest state potential energy surface of the He + H<sub>2</sub> reaction system when  $\theta=90.0^\circ$ . It was seen that for  $r>2.0$  Å and  $R>2.5$  Å, there was no minimum. At the  $0.5$  Å  $< r < 1.0$  Å and at  $R>4.5$  Å, which was entrance region for the reaction. Figure 12 represents the first excited state potential energy. When the helium atom attacks the hydrogen atom along the angle of  $90.0^\circ$ , the entrance region was  $R>1.5$  Å,  $1.0$  Å  $< r < 1.5$  Å. As the helium atoms close H<sub>2</sub>, they passed a transition state  $TS_4$ , at  $R=0.65$  Å and  $r=1.97$  Å. Crossing this transition state, the minimum ( $M_6$ ) was formed, and it was at  $r=2.10$  Å,  $R=0.46$  Å. The minimum energy was 10.837 eV.

### 3.3. Two-Dimensional Diabatic Potential Energy Surfaces

**3.3.1. Avoid Crossing Point.** As seen in Figure 13, it described the difference energy between the lowest state and the first excited state. At  $r=1.80$  Å and  $R=0.77$  Å, the energy interval between the two lowest states was the smallest, and the energy difference was 0.186 eV. It indicated that the diabatic reaction happens easily in this area.

**3.3.2. Conical Intersection Structure.** The configuration of the conical intersection point was optimized and obtained with MOLPRO 2012 software, and the distance between two hydrogen atoms was 1.804 Å. The distance from the helium atom to the center of mass between the two hydrogen molecules was 0.862 Å, as shown in Figure 14.

The mixing angle formula was used to calculate the diabatic potential energies of the He + H<sub>2</sub> reaction system. The kinetic characteristics of the entire reaction system were modified by the interaction zone. The adiabatic and diabatic potential energy surfaces with fixed  $\theta=50.0^\circ$  are shown in Figure 15. These panels (a), (b), (c), and (d) correspond to the potential energy curves, when the distance between two hydrogen atoms was equal to 1.1 Å, 1.2 Å, 1.3 Å, and 1.4 Å, respectively. When mix angle is equal to  $0.0^\circ$ ,  $E_1=H_{22}$  and  $E_2=H_{11}$ , and when the mixing angle is equal to  $90.0^\circ$ , adiabatic energy and diabatic energy were  $E_1=H_{11}$  and  $E_2=H_{22}$ . The cross point appeared when the mixing angle was

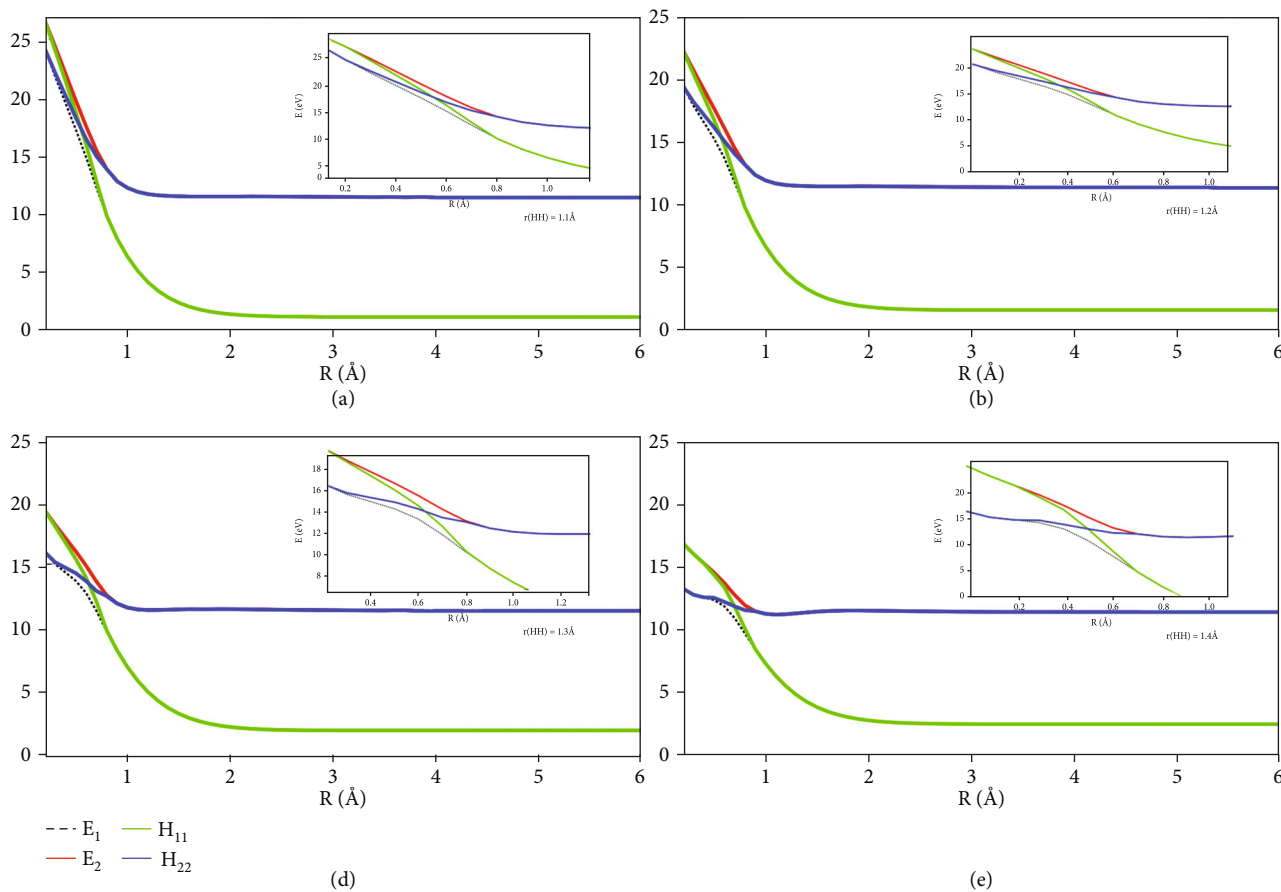


FIGURE 15: Adiabatic and diabatic potential energy surface at (a)  $r_{\text{H-H}}=1.1 \text{ \AA}$ , (b)  $r_{\text{H-H}}= 1.2 \text{ \AA}$ , (c)  $r_{\text{H-H}}=1.3 \text{ \AA}$ , (d)  $r_{\text{H-H}}=1.4 \text{ \AA}$  at  $\theta= 50.0^\circ$ .

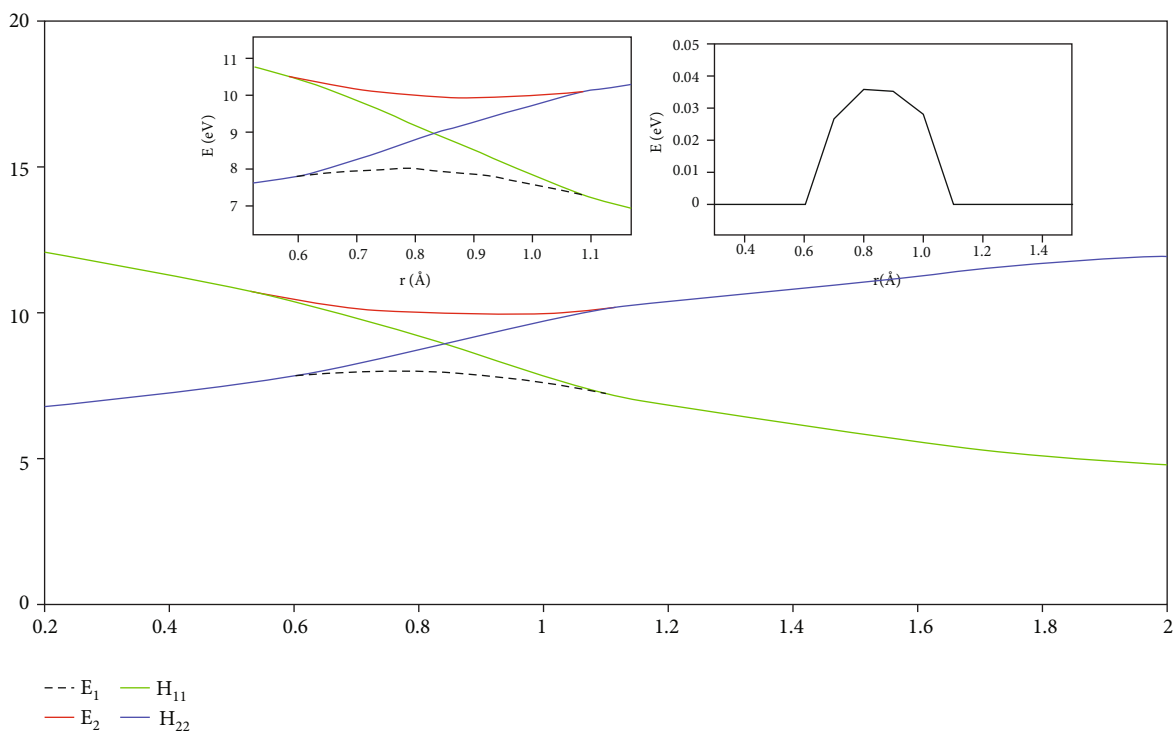


FIGURE 16: Cut-out plot of the diabatic potential energy surface (in eV) as a function of distance  $r$  (in Å)

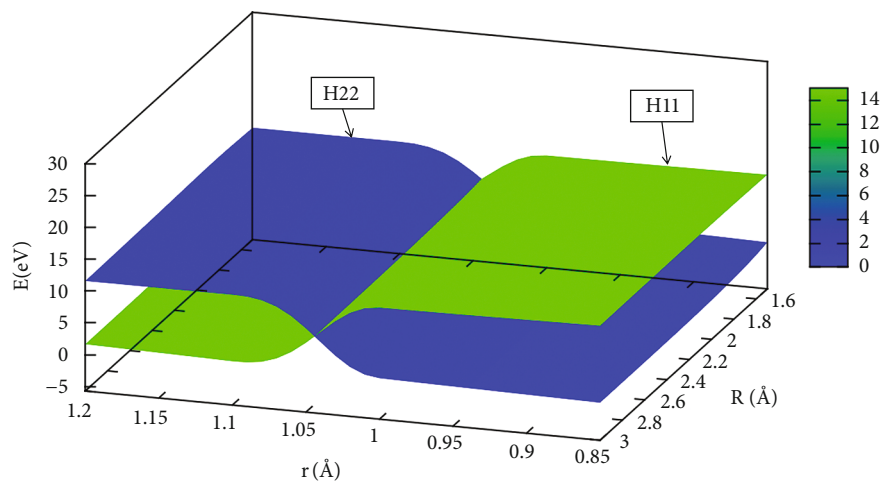


FIGURE 17: When  $\theta=0.0^\circ$ , diabatic potential energy surfaces (in eV) as a function of distances  $r$  (in Å) and  $R$  (in Å).

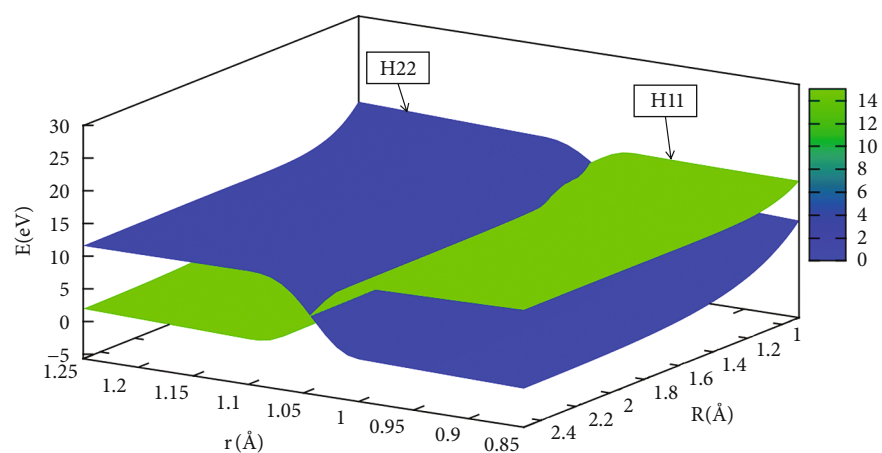


FIGURE 18: When  $\theta=30.0^\circ$ , Diabatic potential energy surfaces (in eV) as the function of  $r$  and  $R$  (in Å) for  $\theta=30.0^\circ$   $r$  (in Å) and  $R$  (in Å).

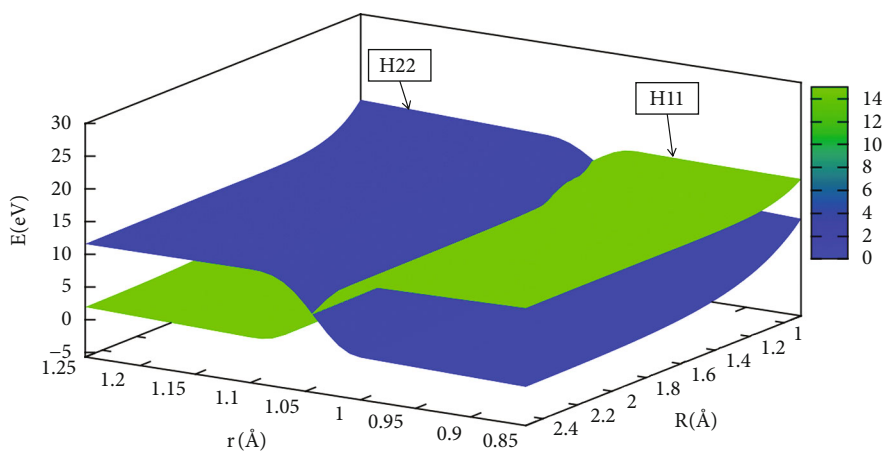


FIGURE 19: When  $\theta=60.0^\circ$ , diabatic potential energy surfaces (in eV) as a function of distances  $r$  (in Å) and  $R$  (in Å).

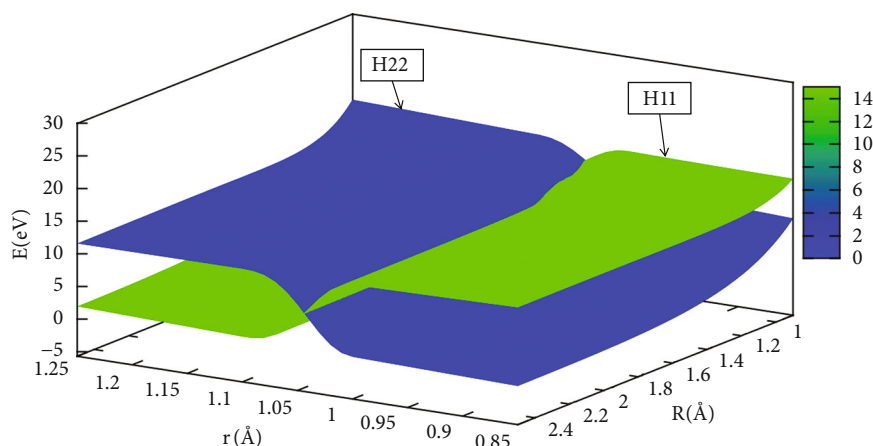


FIGURE 20: When  $\theta=90.0^\circ$ , diabatic potential energy surfaces (in eV) as a function of distances  $r$  (in Å) and  $R$  (in Å).

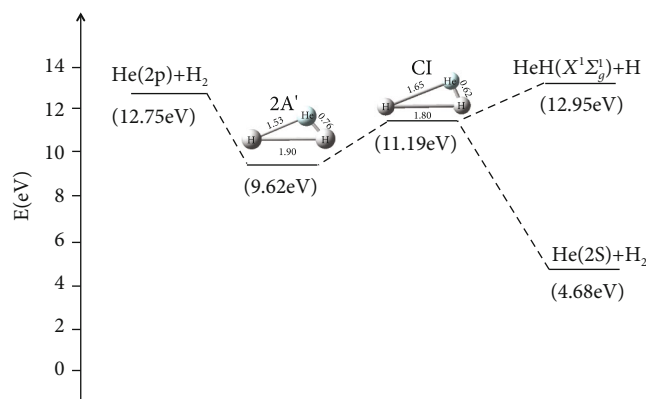


FIGURE 21: The possible reaction path in the He + H<sub>2</sub> reaction system.

equal to  $45.0^\circ$ . It was seen that the  $R$  of the crossing point increased with  $r$ .

While  $r$  was equal to 2.20 and the angle at  $50.0^\circ$ , Figure 16 is the enlarged view of the conical intersection area. The path of the transition from energy H<sub>11</sub> to energy H<sub>22</sub> in this range was clearly visible.

**3.3.3. Two-Dimensional Diabatic Potential Energy Surfaces.** In order to better understand the reaction process, the diabatic potential energy surfaces are expressed by Figures 17–20 for angles set as  $0.0^\circ, 30.0^\circ, 60.0^\circ, 90.0^\circ$ , respectively. The H<sub>11</sub> and H<sub>22</sub> represented the diabatic potential energy surfaces for the He + H<sub>2</sub> reaction system at angles (including  $0.0^\circ, 30.0^\circ, 60.0^\circ$ , and  $90.0^\circ$ ), respectively.

The diabatic potential energy surfaces in the He + H<sub>2</sub> system were displayed at  $0.0^\circ, 30.0^\circ, 60.0^\circ$ , and  $90.0^\circ$ , where the blue part represented the H<sub>22</sub> and the green part represented the H<sub>11</sub>. As the distance between two hydrogens ( $r$ ) atoms increased, the cross point appeared, and the H<sub>11</sub> of the reaction was transformed into H<sub>22</sub>. All the points on these crossing regions were almost located on the same straight line, which also meant that the diabatic potential

energy surfaces constructed by the mixing angle formula were accurate and reliable.

The most likely reaction path for the He + H<sub>2</sub> reaction system was predicted, which is illustrated in Figure 21. Firstly, the first excited helium atom attacked the ground state H<sub>2</sub> molecule, which formed the intermediate with bond lengths of 1.53 Å, 1.90 Å, and 0.76 Å, respectively, and the energy was 9.62 eV. Secondly, the intermediate crossed the conical intersection, and the conical intersection bond lengths of 1.65 Å, 1.80 Å, and 0.62 Å. The configuration of conical intersection was very similar to the intermediate configuration in the first excited state for the reaction. Finally, the product is gradually produced. For this reaction, it was seen that the product of HeH ( $X^1\Sigma_g^1$ ) + H was the most probable reaction path to reach the product.

## 4. Conclusion

In this paper, the potential energy points of the He + H<sub>2</sub> reaction system were calculated using the MOLPRO 2012 software package, which selected the aug-cc-pV5Z basis sets, and applied the *ab initio* calculation method at the MCSCF and MRCI levels. The study calculated the region of  $0^\circ$ – $90^\circ$  for the reactants and  $0^\circ$ – $180^\circ$  for the products. A total of three lowest electronic states with 34848 potential energy points were calculated, and these energy points were fitted precisely using the B-Spline method.

First of all, based on the accurate potential energies, the diatomic potential energy curves of the H<sub>2</sub> molecule were constructed. We found a total of 13 vibrational states and studied the equilibrium bond distance of H<sub>2</sub> was 0.742 Å. The potential energy surface features were analyzed, which deduced that the global minimum energy of the first excited state was 9.616 eV. Meanwhile, the energy difference of two lowest states was 0.186 eV in interaction area, which was consistent with the conical intersection. Finally, the diabatic potential energy surfaces were constructed in the present work.

It was worth performing the full dynamical study with this global potential energy surface. We would continue this work in the following study [54].

## Data Availability

The authors can supply the study data.

## Conflicts of Interest

The authors declare that they have no conflicts of interest.

## Authors' Contributions

Jing Cao and Nan Gao contributed equally to this work.

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