# Chimp optimization algorithm in multilevel image thresholding and image clustering 

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#### Abstract

Multilevel image thresholding and image clustering, two extensively used image processing techniques, have sparked renewed interest in recent years due to their wide range of applications. The approach of yielding multiple threshold values for each color channel to generate clustered and segmented images appears to be quite efficient and it provides significant performance, although this method is computationally heavy. To ease this complicated process, nature inspired optimization algorithms are quite handy tools. In this paper, the performance of Chimp Optimization Algorithm (ChOA) in image clustering and segmentation has been analyzed, based on multilevel thresholding for each color channel. To evaluate the performance of ChOA in this regard, several performance metrics have been used, namely, Segment evolution function, peak signal-to-noise ratio, Variation of information, Probability Rand Index, global consistency error, Feature Similarity Index and Structural Similarity Index, Blind/Referenceless Image Spatial Quality Evaluatoe, Perception based Image Quality Evaluator, Naturalness Image Quality Evaluator. This performance has been compared with eight other well known metaheuristic algorithms: Particle Swarm Optimization Algorithm, Whale Optimization Algorithm, Salp Swarm Algorithm, Harris Hawks Optimization Algorithm, Moth Flame Optimization Algorithm, Grey Wolf Optimization Algorithm, Archimedes Optimization Algorithm, African Vulture Optimization Algorithm using two popular thresholding techniques-Kapur's entropy method and Otsu's class variance method. The results demonstrate the effectiveness and competitive performance of Chimp Optimization Algorithm.


Keywords Thresholding • Clustering • Optimization algorithm $\cdot$ Metaheuristic $\cdot \mathrm{ChOA}$

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## 1 Introduction

For the past few years, image processing has been a rapidly expanding discipline with a wide range of applications. Newer and more efficient techniques are gradually being introduced and applied to various image processing application usage scenarios. Image thresholding and image clustering are two key studies in this field. Both of these studies hold significant impact in different fields such as medicine (Gao et al. 2011), agriculture (Lanthier et al. 2008), computer vision (Jolion et al. 1991), pattern recognition (Haralick and Kelly 1969), object identification (Barik and Mondal 2010), image synthesis (Reed et al. 2016), animation (Lu and Zhang 2010) and so on. These versatile range of use case scenarios and impact of these applications necessitate some organized, efficient and optimized methods.

Thresholding-based techniques have gained a lot of popularity among image segmentation methods due to their efficacy and ease of use. In these types of approaches, image

Segmentation requires thresholding measures to isolate different objects or specific parts of the image or to extract specific image information. In Bi-level thresholding, the image is divided into two classes where pixel values less than a specific threshold value are classified under one class and pixel values above the specific threshold are classified under another class. Multilevel thresholding is generally used in RGB images where the whole image is subdivided into multiple classes based on multiple threshold values. This multilevel thresholding technique is the baby step for image clustering where the image is first segmented using multiple threshold values and later on, these thresholds are used to generate different clusters. Clustering can also be done using a single threshold value for each color channel (Red, Green and Blue) but multilevel thresholding for each color channel results in more efficient clustering of images. The image pixels are classified in such a way that the pixels with similar spatial coordinates fall under the same cluster, and pixels assigned in the same cluster vary with pixels assigned to other clusters, which is achieved by using the threshold values for each color channel.

Kapur's maximum entropy method (Kapur et al. 1985) and Otsu's class variance method (Otsu Jan. 1979) are two the most popular methods for image segmentation and clustering purposes. Both of these methods require optimized values of respective objective functions which itself is a cumbersome process, also the computational complexity of these techniques arises significantly as the number of threshold increases. This is where metaheuristic optimization algorithms come into play. These optimization algorithms not only deal with the computational accuracy of above mentioned multilevel thresholding techniques, also they are capable of reducing the complexity and computational time of the problem.

Chimp Optimization Algorithm (ChOA) is a novel metaheuristic optimization algorithm proposed by M. Khishe and M.R. Mosavi in 2020 (Khishe and Mosavi 2020), where they mimicked the sexual motivation and diverse intelligence of chimps in group hunting. ChOA provides a mathematical modeling of hunting mechanisms of 4 types of chimps along with their respective hunting strategies. This algorithm has been proven to be worth solving many complex engineering problems for its excellent balance between exploration and exploitation (Nagadurga et al. 2021; Pedram Haeri Boroujeni and Pashaei 2021). In this paper, we have used ChOA for image clustering using multilevel image thresholding technique. Kapur's entropy method and Otsu's thresholding method were used for evaluating the performance of ChOA and the performance has been compared with other well known metaheuristic algorithms, namely Particle Swarm Optimization Algorithm (PSO), Whale Optimization Algorithm (WOA), Salp Swarm Optimization Algorithm, Harris Hawks Optimization Algorithm
(HHO), Moth Flame Optimization Algorithm (MFO), Grey Wolf Optimization Algorithm (GWO), Archimedes Optimization Algorithm (AOA) and African Vulture Optimization Algorithm (AVOA).

## 2 Related works

Image segmentation has always been a challenging task for the researchers. A good number of methods have been found in the literature for image segmentation such as- edge based method (Muthukrishnan and Radha 2011), wavelet transform based method (Demirhan et al. 2015), neural network based method (Wang et al. 2010), clustering based method (Chuang et al. 2006), threshold based method (Ouadfel and Taleb-Ahmed 2016) etc. Threshold-based techniques, more specifically multilevel threshold-based techniques have been highly adapted for image segmentation applications that can extensively be found in the literature. In 1985, Kapur et al. proposed one of the most popular thresholding based image segmentation methods, named as maximum entropy method, where they optimized the maximum entropy of the image histogram to measure the homogeneity of different classes and find the optimal threshold values (Kapur et al. 1985). In Otsu (Jan. 1979) the author presented a new thresholding technique known as Otsu's method where the target image is similarly sub divided into various classes based on multiple threshold values which are found by maximizing the interclass variance.

Image clustering approaches based on thresholding techniques appear to be more effective than other approaches that can be found in the literature namely, K-means data classification method (MacQueen 1967), Fuzzy c-means (FCM) method (Bezdek et al. 1984) etc. Thresholding based approaches overcome the drawbacks of other clustering methods such as, reliance on the number of clusters, computational complexities, repetitive natures and so on. For grayscale images, this process of clustering is relatively easier by means of binarization and thresholding. In such instances, the quality of clusters improves as the number of thresholds increases in multilevel thresholding. When multilevel thresholding is used on color photos, however, the technique gets more complicated. Demirci et al. (2014) proposed an idea where they determined a single threshold value separately for each color channel (Red, Green, and Blue) using Kapur's entropy method and Otsu's method for image clustering. Authors in Rahkar Farshi et al. (2018) extended this idea of multilevel thresholding for each color channel separately using Kapur's entropy method. They showed that their approach resulted in better clustering than the work in Demirci et al. (2014) as they could increase the number of clusters by increasing the number of sub-cubes generated by means of multilevel thresholding for each color channel.

The rising problem complexity in multilevel thresholding highly motivated the use of optimization algorithms in this context for quite a long time. Authors in Sharma et al. (2018) used Firefly Algorithm (FA) in grayscale image segmentation using multiple thresholds. Similar works can be found in Pei et al. (2009) where the authors used Otsu's method by using Differential Evolution algorithm.

For RGB images, the application of optimization algorithms can be found extensively in the literature for multilevel thresholding purposes. Cuckoo Search Algorithm (CSO) were used for multilevel thresholding as a means of image segmentation using Kapur's entropy method (Brajevic et al. 2012). Authors in [22] used Crow Search Algorithm in the similar context for optimal multilevel image segmentation. Whale optimization Algorithm (WOA) has been used in underwater multilevel image segmentation using Kapur's maximum entropy technique (Yan et al. 2021). Authors in Jia et al. (2019) applied a modified Moth Flame Optimization Algorithm in multilevel color segmentation purpose on 10 test images to yield more optimal and accurate results comparing to other algorithms in this regard. In [42], authors developed an improved Biogeography-Based Optimization Algorithm for the applications of clustering optimization and applied it in medical image segmentation. Authors in Wong et al. (2011) used Particle Swarm Optimization Algorithm for image clustering using two distinct fitness functions and showed that PSO works better than conventional K-means method because of its ability to generate more compact clusters. A hybrid Firefly and Particle Swarm Optimization Algorithm was used in the similiar purpose in the works of Rahkar Farshi and Ardabili (2021) which resulted in comparatively superior performance than 4 other metaheuristic algorithms that they compared with. In Rahkar Farshi et al. (2018), the authors evaluated the performance of Particle Swarm Optimization (PSO) and Forest Optimization Algorithm (FOA) in image clustering based on multilevel thresholding for each color channel, following by the work of Demirci et al. (2014) in the similar context who did the clustering using a single threshold for each color channel.

The Chimp Optimization algorithm has gained much popularity in recent days in several fields of engineering and complex applications. The innate strategic strengths of this algorithm of not getting trapped in local minima for multi dimensional problems and avoiding slow convergence speed due to its proper balance between exploration and exploitation phase, this algorithm tends to provide better performance in most of the engineering applications as compared to other existing algorithms (Kharrich et al. 2021). In the image processing genre, where the optimization problems become compact due to their high computational complexity, specially in multilevel thresholding and threshold based clustering, ChOA can provide extensive performance in this regard. Authors in Houssein et al. (2021) used ChOA in
a similar context for segmentation of thermography based breast cancer imaging. In Tianqing et al. (2021), authors used a novel two-phase approach for classifying chest X-ray images, for real time detection of COVID-19 cases. They used deep CNN in first phase and extreme learning machines in second phase, stabilized by Chimp Optimization algorithm for better result.

Some more advances and applications of Chimp Optimization Algorithm can be found in recent literatures. Authors in Kaur et al. (2021) applied sin- cosine functions to update the equations of Chimp and thus developed a novel fusion algorithm named SChoA for HLS of datapaths in digital filters and engineering applications. In Wang et al. (2021), authors developed a binary version of Chimp optimization algorithm (BChOA) to solve optimization problems. Authors in Khishe et al. (2021) proposed a weighted Chimp Optimization algorithm by demonstrating that the proposed algorithm generates better results in terms of convergence speed and avoidance of local minima as compared to other metaheuristic algorithms. In Dhiman (2021), authors proposed a hybrid algorithm named SSC (Spotted Hyena-based Chimp Optimization Algorithm) for solving engineering problems, which is a combination of sine-cosine function and attacking strategy of Spotted Hyena Optimizer (SHO). Authors in Kaidi et al. (2022) proposed a Dynamic Levy Flight Chimp optimization algorithm to mitigate the problem of local optima stagnation of Chimp Optimization algorithm. In the works of (Khishe and Mosavi 2020), authors trained an Artificial Neural Network (ANN) using Chimp Optimization algorithm for the purpose of classification of underwater acoustical dataset.

This study focuses on carrying out an comprehensive investigation on the performances of different optimization algorithms, based on image thresholding. Hence, the performances are compared in an extensive fashion with a view to executing how Chimp optimization algorihm can play a significant role in terms of optimizing the fitness function using Kapur and OTSU's method for image clustering using multilevel thresholding. Therefore, the paper at hand provides a wide-ranging perspective in terms studying the applicability and compatibility of Chimp optimization algorithm pertaining to image thresholding and image clustering which will open new windows in the domain of image processing.

## 3 Methodology

Thresholding can be thought of a statistical-decision theory problem, and the goal of the problem is to minimize the average error resulting from assigning pixels to two or more groups. The probability density function (PDF) of each group's intensity level and the probability that each group's occurrence in a given application are the two fundamental pillars of the
solution to the thresholding problem, but predicting the nature of the PDF is difficult. Otsu's method and Kapur's method are some of the alternative of this problem, and applying these alternative solutions to multilevel thresholding and determining the the threshold value with stochastic algorithm is one of the way to achieve the threshold values.

Gray scale images, also RGB images, have intensities in the range of $\{0,1,2, \ldots, L-1\}$; thus the probability of the $i$ th gray level is given by the equation that follows.
$c_{i}=\frac{h_{i}}{M \times N}$
In (1), $M$ and $N$ signifies the size of an image and $h_{i}$ points to pixel number of the level $i, 0 \leq i \leq(L-1)$. In the case of multi-level thresholds $T h_{i}, T h_{2}$ are used for clarification, and number of pixels clustered will be incremented by one. In the case of gray picture threshold, value of the pixels between two thresholds will be rounded up to the immediate highest threshold i.e. pixel value between $T h_{i}<t_{1}, t_{2}, \ldots, T h_{i+1}-1 \leq T h_{i}$ will be rounded up to $T h_{i+1}$.

In the case of RGB image, the same concept of rounding up is applied to each color histogram.

### 3.1 Kapur's method

Kapr's method (Mirjalili et al. 2017) was devised from the theory of entropy, and though it was, at first, proposed for binary thresholding, however, the technique can also be applied to multilevel thresholding.
$\operatorname{Fitness}\left(T h_{1}, T h_{2}, \ldots, T h_{n}\right)=H i s_{0}+H i s_{1}+\cdots+H i s_{n}$
In (2), $T h_{i}$ values are thresholds value for multilevel segmentation, and $H i s_{i}$ values denotes histogram entropy value up to the particular threshold. Each of the entropy is given by the following equations.
$H i s_{0}=-\sum_{i=0}^{T h_{1}-1} \frac{c_{i}}{w_{0}} \ln \frac{c_{i}}{w_{0}}, w_{0}=\sum_{i=0}^{T h_{1}-1} c_{i}$
$H i s_{1}=-\sum_{i=T h_{1}}^{T h_{2}-1} \frac{c_{i}}{w_{1}} \ln \frac{c_{i}}{w_{1}}, w_{1}=\sum_{i=T h_{1}}^{T h_{2}-1} c_{i}$
$H i s_{n}=-\sum_{i=T h_{n}}^{L-1} \frac{c_{i}}{w_{n}} \ln \frac{c_{i}}{w_{n}}, w_{n}=\sum_{i=T h}^{L-1} c_{i}$

### 3.2 Otsu's method

Otsu's method (Heidari et al. 2019) was devised from class variance algorithm. In terms of optimization algorithm, the objective functions is stated below.
$\operatorname{Fitness}\left(T h_{1}, T h_{2}, \ldots, T h_{n}\right)=\sigma_{0}+\sigma_{1}+\cdots+\sigma_{n}$
In (6), $\sigma_{i}$ values are between-class variance values, and they are given by the next sets of equations.
$\sigma_{0}=w_{0}\left(\mu_{0}-\mu_{t}\right)^{2}$
$w_{0}=\sum_{i=0}^{T h_{1}-1} c_{i}, \mu_{0}=\sum_{i=0}^{T h_{1}-1} \frac{i c_{i}}{w_{0}}$
$w_{1}=\sum_{i=T h_{1}-1}^{T h_{2}-1} c_{i}, \mu_{1}=\sum_{T h_{1}-1}^{T h_{2}-1} \frac{i c_{i}}{w_{1}}$
$\sigma_{n}=w_{n}\left(\mu_{n}-\mu_{t}\right)^{2}$
$w_{1}=\sum_{i=L-1}^{T h_{n}-1} c_{i}, \mu_{n}=\sum_{T h_{n}}^{L-1} \frac{i c_{i}}{w_{n}}$
In (7)(8)(9), $\mu_{t}$ is defined as follow.
$\mu_{t}=\sum_{i=0}^{L-1} c_{i}$
In (7)(8)(9) and (10), $\mu_{i}$ denotes the mean of groups where $0 \leq i \leq n$ and the overall image average value is denoted by $\mu_{T}$

## 4 Image clustering

After achieving the best set of threshold values, where number of threshold value depends on the application (i.e. particular image), the set of values can be used to cluster the image. In RGB image, three sets of thresholds are used to cluster each dimension of color (i.e. RGB image where there is a dimension for each color histogram). The integration of thresholds values to color partition was done by the techniques in Demirci et al. (2014). Though the technique in (Demirci et al. 2014) was designed for single value threshold, the authors in (Rahkar Farshi et al. 2018) enhanced the technique for application in


Fig. 1 3D color space with assigned clusters (Rahkar Farshi et al. 2018)
multi-level thresholds. Even after the criteria for each color channel are determined, establishing meaningful clusters with information from each color channel is a key issue. Subsets of color space are created using the threshold values computed for each channel. As a result, in Fig. 1, there are cubes instead of discreet values of the pixels. Figure 1 was taken from (Rahkar Farshi et al. 2018). This is due to the rounding up of pixel values to the nearest highest threshold(i.e. pixel value between $T h_{i}<t_{1}, t_{2}, \ldots, T h_{i+1}-1 \leq T h_{i}$ will be rounded up to $T h_{i+1}$ ), hence creating cubes in RGB color space. The distribution of cubes differs from image to image, and by increasing the number of thresholds, larger cubes can be divided into smaller cubes and the maximum number of cubes is given by (11). Clusters may appear to be far apart to be related. However, image clustering with the technique above creates meaningful clusters as shown in Rahkar Farshi et al. (2018). The size of the cubes in RGB space is related to individual pixel intensity distribution of an image, thus creating unique positions of cubes in RGB color space for particular image, and considering the homogeneity of an image, though large size of cube enhances the homogeneity, smaller size of cubes can also maintain the homogeneity if the number of thresholds are increased; the reason is pixel value are limited to the range [0,255]. So, increasing the number of thresholds will create such distribution where the clustered image will have more similar distribution to the original image, hence increasing homogeneity.
max. number of clusters $=(\text { number of threshold }+1)^{3}$

## 5 Necessary parameters

### 5.1 Segment evolution function

To quantitatively judge the achieved thresholds values for RGB image, evolution function is used which was first proposed in Liu and Yang (1994b) and the technique is elaborated in Liu and Yang (1994a) and Borsotti et al. (1998).
$F=\frac{1}{1000(M \times N)} \sqrt{R} \sum_{i=L-1}^{R} \frac{e_{i}^{2}}{\sqrt{A_{i}}}$
In (12), $M \times N$ gives the number of pixels; $R$ denotes the number of obtained regions. $A_{i}$ gives the pixel number in the $i$ )th region. Average of color error in the $i$ th region is signified by $e_{i}$, and it is defined as the sum of the Euclidean distances between pixels of the $i$ th region in the original color image and the attributed pixel values of the $i$ th region in the segmented image. The $F$-value shrinks excessively, and to prevent that $\sqrt{R}$ term is multiplied. The number of region is inversely proportional to $F$, and lower the $F$, the better.

Related to this there are two other widely used quantitative assessment function termed as $F^{\prime}$ and $Q$, proposed in Borsotti et al. (1998). $F^{\prime}$ is defined as below.
$F^{\prime}(I)=\frac{1}{1000(M \times N)} \sqrt{\sum_{A=1}^{M A X}[R(A)]^{1+\frac{1}{A}}} \times \sum_{i=L-1}^{R} \frac{e_{i}^{2}}{\sqrt{A_{i}}}$
$Q$ is further reinforced by $F^{\prime}$.
$Q(I)=\frac{1}{1000(M \times N)} \sqrt{R} \sum_{i=1}^{R}\left[\frac{e_{i}^{2}}{1+\log A_{i}}+\left(\frac{R\left(A_{i}\right)}{A_{i}}\right)^{2}\right]$
$R$ is the number of regions marked, and $A_{i}$ represents pixel numbers in the $i t h$ region, and $e_{i}$ denotes the $i t h$ color region. Lower values of $F^{\prime}$ and $Q$ are desired for better clustering performance.

In Farshi et al. (2020) the authors represented these 3 quantitative assessment functions in an organized manner.

### 5.2 Structure Similarity Index (SSIM)

SSIM is given by the following equation (Wang et al. 2004).
$\operatorname{SSIM}(x, y)=\frac{\left(2 \mu_{x} \mu_{y}+c_{1}\right)\left(2 \sigma_{x y}+c_{2}\right)}{\left(\mu_{x}^{2}+\mu_{y}^{2}+c_{1}\right)\left(\sigma_{x}^{2}+\sigma_{y}^{2}+c_{2}\right)}$
where $\mu_{x}$ and $\mu_{y}$ denote the mean intensity of the original image and that of the segmented image, respectively. $\sigma_{x}^{2}$ and $\sigma_{y}^{2}$ denote the standard deviation of the original image and that of the segmented image, respectively. $\sigma_{x y}$ denotes the
co-variance between the original image and the segmented image. $c_{1}$ and $c_{2}$ are constants.

According to brightness, contrast, and structural similarity, the SSIM is utilized to detect the similarity between the segmented image and the original image.The image segmentation impact improves as the SSIM value approaches one.

### 5.3 Peak signal-to-noise ratio (PSNR)

PSNR is given by the following equations (Aldahdooh et al. 2018).
$P S N R=10 \log _{10}\left(\frac{255^{2}}{M S E^{2}}\right)$
$M S E=\frac{1}{M N} \sum_{i=1}^{M} \sum_{j=1}^{N}[I(i, j)-k(i, j)]^{2}$
Based on the intensity value of the image, the PSNR is used to detect the difference between the segmented image and the original image. The better the image segmentation effect, the higher the PSNR value. A segmented image with a greater PSNR value may be worse than a segmented image with a lower PSNR value due to differences in human visual acuity.

### 5.4 Variation of information (VOI)

VOI refers to the unrelated randomness property between different image segments, that is, how much the distribution of randomness varies from one segment to another. A lower value of VOI denotes better performance.

### 5.5 Probability Rand Index (PRI)

PRI denotes a connection between the segmented image and the main image. Higher value of this parameter is desired.

### 5.6 Global consistency error (GCE)

GCE denotes the extent to which one segmented image can be viewed or considered as a refinement of another segmented image. Lower result of this parameter is desired as it indicates better performance.

### 5.7 Feature Similarity Index (FSIM)

This is one of the important image segmentation parameters for image quality assessment that measures how much dependency the segmented image has with the original image. FSIM value always ranges between -1 to 1 . A higher value of FSIM signifies better performance.
$\operatorname{FSIM}(x, y)=\frac{\sum_{x \in \Omega} S_{L}(X) P C_{m}(x)}{\sum_{x \in \Omega} P C_{m}(x)}$
Original image. FSIM value always ranges between -1 and 1. A higher value of FSIM signifies better performance.

### 5.8 Blind/referenceless image spatial quality evaluatoe (BRISQUE)

BRISQUE uses statistical method of local normal luminance coefficients is used by BRISQUE to measure probable losses of "naturalness" in the image due to distortions. It does not compute ringing, blur, blocking, or anyother distortion specific parameters. Lower score signifies greater quality of an image (Mittal et al. Dec. 2012; MATLAB 2021).

### 5.9 Perception based image quality evaluator (PIQE)

PIQE is an unbiased paramter for image quality assessment without relying on subjective view. This paremeter measures distortions based on local features from visibly important spatial regions, and smaller PIQE score signifes better quality (Venkatanath et al. 2015; MATLAB 2021).

### 5.10 Naturalness image quality evaluator (NIQE)

Based on space domain natural scene statistic (NSS) model, NIQE measures the quality with the construction of some quality indicative statistical features, and similarly better quality is indicated by lower NIQE score. Mittal et al. (2013) MATLAB (2021)

## 6 Chimp Optimization Algorithm

Chimp optimization algorithm (ChOA) is a stochastic algorithm. In recent years, there has been a paradigm shift in algorithms in solving multidimensional problems. The major reason is deterministic algorithms are quite computationally expensive when it comes to finding global optimum value. Due to the randomness as an innate property of these algorithms, stochastic algorithms have high probability of convergence to global optimum in finite number of iterations, thus lessening the computational burden.

ChOA is one such algorithm, and it is a nature inspired swarm intelligence algorithm. Most of the stochastic algorithms have two fundamental phases: exploration and exploitation. In the exploration phase, search agents, initiated by the algorithm, roam around the search space (i.e. the variable space) for the best fitness value (output of the multi-dimensional function) of the objective function (multidimensional function). The exploration and the exploitation
phase are divided in terms of iteration, and an outside function based on the iteration values determine the transition from exploration to exploitation. In the exploitation phase, the search agents circles around the best solution obtained so far in quest of finding more better solution. Search agents have cognitive abilities modeled and governed by few mathematical equations, and it is this cognitive ability along with the transition from exploration to exploitation phase makes stochastic algorithm appropriate in image thresholding application.

### 6.1 Inspiration Of ChOA

ChOA was inspired from the group behavior of chimps in hunting prey (Khishe and Mosavi 2020). There are four types of chimps when it comes to hunting: driver, barrier, chaser and attacker. Driver keeps track of prey's movement; while barriers try to impede the progression of the prey; meanwhile chaser move swiftly to catch the prey, and finally it's the attacker that launches the attack based on anticipating prey's movement. It's a group hunting, and role of each member is crucial in order to catch the prey. Attacker chimps are usually the ones who do the hunting. Driver, barrier, and chaser chimps are all involved in the hunting procedure on occasion. Unfortunately, there is no information regarding the best position in an abstract search space (prey). It is assumed that the first attacker (best solution available), driver, barrier, and chaser are better informed about the location of possible prey in order to mathematically imitate the chimps' behavior. As a result, four of the greatest answers so far are saved, and other chimps are pushed to update their places based on the best chimps' placements.

### 6.2 Mathematical modeling Of ChOA

The four individual groups search the issue space locally and globally using their unique patterns. Driving and chasing are given by the following equations.
$\mathbf{d}=\left|\mathbf{c} \cdot \mathbf{x}_{\text {prey }}(t)-\mathbf{m} \cdot \mathbf{x}_{\text {chimp }}(t)\right|$
$\mathbf{x}_{\text {chimp }}(t+1)=\mathbf{x}_{\text {prey }}(t)-\mathbf{a . d}$
Current iteration number is defined with the symbol $t$, and $\mathbf{a}, \mathbf{m}$ and $\mathbf{c}$ are the coefficient vectors, $\mathbf{x}_{\text {prey }}$ is prey's vector position and $\mathbf{x}_{\text {chimp }}$ gives the chimp's vector position. a,m and $\mathbf{c}$ are defined by the equation that follows.
$\mathbf{a}=2 . \mathbf{f} \cdot \mathbf{a}_{1}-\mathbf{f}$
$\mathbf{c}=2 . \mathbf{r}_{2}$
$\mathbf{m}=$ Choatic_value
Non-linear reduction of $\mathbf{f}$ is done, from 2.5 to 0 , in both the phases. Random vectors are generated in each iteration and two random sets are assigned to $\mathbf{r}_{1}$ and $\mathbf{r}_{2}$, and $\mathbf{m}$ value is generated from various chaotic map.

In exploitation phase, the chimps behavior are modeled by the equations as follows.
$\mathbf{d}_{\text {attacker }}=\left|\mathbf{c}_{1} \cdot \mathbf{x}_{\text {attacker }}-\mathbf{m}_{1} \cdot \mathbf{x}\right|$
$\mathbf{d}_{\text {barrierr }}=\left|\mathbf{c}_{2} \cdot \mathbf{x}_{\text {barrier }}-\mathbf{m}_{2} \cdot \mathbf{x}\right|$
$\mathbf{d}_{\text {chaser }}=\left|\mathbf{c}_{3} \cdot \mathbf{x}_{\text {chaser }}-\mathbf{m}_{3} \cdot \mathbf{x}\right|$
$\mathbf{d}_{\text {driver }}=\left|\mathbf{c}_{4} \cdot \mathbf{x}_{\text {driver }}-\mathbf{m}_{4} \cdot \mathbf{x}\right|$
$\mathbf{x}_{1}=\mathbf{x}_{\text {attacker }}-\mathbf{d}_{\text {attacker }} \cdot \mathbf{a}_{1}$
$\mathbf{x}_{2}=\mathbf{x}_{\text {barrier }}-\mathbf{d}_{\text {barrier }} . \mathbf{a}_{2}$
$\mathbf{x}_{3}=\mathbf{x}_{\text {chaser }}-\mathbf{d}_{\text {chaser }} . \mathbf{a}_{3}$
$\mathbf{x}_{4}=\mathbf{x}_{\text {drivere }}-\mathbf{d}_{\text {driver }} . \mathbf{a}_{4}$
$\mathbf{x}(t+1)=\frac{\mathbf{x}_{1}+\mathbf{x}_{2}+\mathbf{x}_{3}+\mathbf{x}_{4}}{4}$
$\mathbf{x}_{\text {chimp }}(t+1)=\left\{\begin{array}{l}\mathbf{x}_{\text {prey }}(t)-\text { a.d if } \mu<0.5 \\ \text { Chaotic_value if } \mu \geq 0.5\end{array}\right.$
In the above equations $\mathbf{c}$ is a random vector ranging from 0 to 2 (i.e. $[0,2]$ ), and $\mathbf{a}$ is random variable ranging from $[-2 \mathbf{f}, 2 \mathbf{f}]$. In case of chaotic map (Saremi et al. 2014), the initial value was set to 0.7 in image thresholding optimization problem.

The original ChOA algorithm incorporate six different chaos map and two different sets of equations to update dynamic strategies. The dynamic strategy is used for determining the coefficients $\mathbf{c}_{1}, \mathbf{c}_{2}, \mathbf{c}_{3}$, and $\mathbf{c}_{4}$.

For the sake of the simplicity of this work, only one set of dynamic strategy and one chaos map were used. This particular version of ChOA is labelled as ChOA12. The chaos map is known as Gauss or Mouse. It's defined as follows.
$x_{i+1}=\left\{\begin{array}{lc}1 & x_{i}=0 \\ \frac{1}{\bmod \left(x_{i}, 1\right)} & \text { otherwise }\end{array}\right.$
In the final stage, chimps relinquish their hunting responsibilities after acquiring meet and subsequent social drive
(sex and grooming). As a result, they strive to gather meat in a chaotic manner.In tackling high-dimensional problems, ChOA is aimed to address the two issues of sluggish convergence speed and entrapment in local optima. This chaotic behavior in the last step aids chimps in overcoming the two issues of entrapment in local optima and sluggish convergence rate in high-dimensional problem solving.

ChOA allows the chimps to update their locations based on the positions of the attacker, barrier, chaser, and driving
chimps and assault the prey, according to the operators who have already been provided. However, ChOA may still be at risk of becoming trapped in local minima, necessitating the use of other operators to overcome this problem. Despite the fact that the proposed driving, blocking, and chasing mechanisms appear to depict the exploration process, ChOA requires additional operators to focus on the exploration phase.

### 6.3 Pseducode

```
Algorithm 1 Algorithm for Chimp Optimization Algorithm
Input: Number of iteration, Objective Function, Chimp number
Output: Objective Value
    InitialisationChimp Population, f,m, a
    Calculate the initial position of each chimp
    Divide chimps randomly into independent groups
    This is repeated before stopping conditions are met
    Calculate the fitness of each chimp
    Determine \(\mathbf{x}_{\text {attacker }}, \mathbf{x}_{\text {chaser }}, \mathbf{x}_{\text {barrier }}, \mathbf{x}_{\text {diver }}\)
    While current iteration \(<\) Maximum Number of iteration
        for loop each chimp
        Extract the chimp's group
        Use its mathematical model to update \(\mathrm{f}, \mathrm{m}, \mathrm{c}\)
        Use \(\mathbf{f}, \mathbf{m}\) and \(\mathbf{c}\) to calculate \(\mathbf{a}\) and then \(\mathbf{d}\)
        end for loop
        for each search chimp
            if \((\mu<0.5)\)
                    if \((|a|<1)\)
                    Update the position of the current search agent by the models
            else if \((|a|>1)\)
            Select a random search agent
            end if
            else if ( \(\mu>0.5\) )
                Update the position of the current search
                    end if
            end for loop
        Update f, m, a and c
        Update \(x_{\text {Attacker }}, x_{\text {Driver }}, x_{\text {Barrier }}, x_{\text {Chaser }}\)
        \(\mathrm{t}=\mathrm{t}+1\)
    end while
    return \(x_{\text {Attacker }}\)
```


### 6.4 Flowchart

See Fig. 2.

## 7 Result and analysis

See Figs. 3, 4, 5 and 6


Fig. 2 Flowchart of Chimp Optimization Algorithm


Fig. 3 Original image 1

(a) Image 2

(b) Histogram of image 2

Fig. 4 Original image 2

### 7.1 Overall method

In this work, Chimp optimization algorithm has been applied in multilevel image thresholding and image clustering problem using Kapur's entropy method and Otsu's method. The performance of the proposed algorithm is evaluated based on multiple performance metrics. Later on, the overall performance has been compared with 8 other existing metaheuristic algorithms in the similar context to depict a conclusion on the efficiency of ChOA in this problem.

However, due to the stochastic nature of the algorithms and pixel distribution of images, it is hard to evaluate
algorithms analytically. The performance of ChOA can be evaluated in terms of two broad applications, image clustering and image segmentation. The tables shows the average value after 30 tries and in each tries there were 100 iterations and in each iteration number of particles were 100. Chimp Optimization Algorithm was applied for each color channel (Red, Green and Blue) separately. Maximum entropy was evaluated for each color channel using Kapur's entropy method, similarly that has been done for Otsu's class variance method. The objective functions were maximized to generate k number of thresholds for each channel individually $(k=2,5,8,10)$. These thresholds in 3 dimensional

(a) Image 3

(b) Histogram of image 3

Fig. 5 Original image 3

(a) Image 4

(b) Histogram of image 4

Fig. 6 Original image 4
plane were used to further generate small sub-cubes, or clusters.

Tables 1 and 2 contain the fitness values measured for each color channel separately by applying both Kapur's
entropy method and Otsu's class variance method for the four test images.

From Figs. 7, 8, 9, 10, 11 and Figs. 14, 15, 16 are the clustered Images after applying all algorithms for different


Fig. 7 Kapur's thresholding of image 1
threshold values, for both Kapur's and Otsu's method. The results signify the effectiveness of ChOA in successful multilevel thresholding and image clustering. It is also evident as expected that the clustered image quality gradually improves as the number of thresholds (k) increases. Similar strategy was repeated for 8 other metaheuristic optimization algorithms: Particle Swarm Optimization Algorithm (PSO) (Kennedy and Eberhart 1995), Whale Optimization Algorithm (WOA) (Mirjalili and Lewis 2016), Salp Swarm Algorithm (Mirjalili et al. 2017), Harris Hawks Optimization Algorithm (HHO) (Heidari et al. 2019), Moth Flame


Fig. 8 Otsu's thresholding of image 1

Optimization Algorithm (MFO) (Mirjalili 2015), Grey Wolf Optimization Algorithm (GWO) (Mirjalili 2014), Archimedes Optimization Algorithm (AOA) (Hashim et al. 2021), African Vulture Optimization Algorithm (AVOA) (Abdollahzadeh et al. 2021).

Figures 12 and 13 represent the whole research flow. In Fig. 13, randomly initialized search agents in ascending order is a crucial part of the MATLAB code. Kapur's threshold values are mathematically defined in ascending order and the lower values of pixel below a particular threshold are rounded up to that threshold. The optimization algorithm doesn't inherently generate search solution set in an

Fig. 9 Kapur's thresholding of image 2

ascending order. So, without this particular part of code the algorithm, doesn't converge to any meaningful solution, but with this part, the optimization algorithm stores the fitness value of ascending ordered threshold before first iteration; any fitness value that doesn't maintain this ascending order will give Zero fitness value. Since the optimization algorithm stores the fitness value of ascending ordered threshold, the algorithm will see any descending order threshold value as a solution set as unworthy and update the next set of solution set so that it doesn't generate other than ascending order solution set.

### 7.2 Benchmark images

Four test images were taken from Berkeley Segmentation Data Set 500 (BSDS500). Chimp Optimization Algorithm was applied on these images to generate clustered images by means of both Kapur's entropy method and Otsu's class variance method for different number of thresholds. The performance of ChOA was evaluated by computing some of the performance parameters. From Figs. 3, 4 and 5 represent the test RGB images.

Fig. 10 Otsu's thresholding of Image 2
$\square$


### 7.3 Experimental environment

For conducting our experiments, we used MATLAB r2020a. These were carried out in Windows 10-64 bit environment and Core i5 2.20 GHz CPU was used with 8GB RAM. Each experiment was run 30 times for each single case of threshold value and the average value of those 30 values was taken for every parameter calculation.

### 7.4 Image clustering

The primary parameters in image clustering are $\mathrm{F}, \mathrm{F}, \mathrm{Q}$. Table 3 covers F values, and it is apparent that ChOA performed no less than other algorithms. Moreover, F values from using Kapur's method is better than F values from using Otsu's method. Nonetheless, in both of the method ChOA performance have significance in overall application.

Fig. 11 Kapur's thresholding of Image 3


In Table 3, using Kapur's method for image 1, in case of $k=5$, it performed the best.

Using Otsu's method, ChOA performed relatively better when $k=5$ and $k=8$, and ChOA was in second best position when $k=10$. In case of F ' value, apparent from Table 4, ChOA gave the best and the second best when $k=8$ and $k=5$ respectively by Kapur's method, and ChOA performed best when $k=8$ and performed second best when $k=5$ using Otsu's method. In case of other $k$ values, ChOA gave competitive results.

When it comes to Q value in image 1, ChOA gave the best and the second best for $k=8,10$ respectively for Kapur's method; and by using Otsu's method, for $k=5,8,10$, ChOA
gave best result for the first two $k$ values and third best result for the last $k$ value. The values of the parameter Q can be found from Table 5.

Similarly, for F value in image 2, ChOA performed best when $k=5$ using Kapur's method, and when $k=5$ and $k=8$ using Otsu's method. ChOA gave the best F ' value when $k=5$ using Kapur's method, and gave the best and second best F ' value when $k=5,8$ respectively using Otsu's method. Performance in Q values were similar to that of F ' values with slight exceptions: ChOA gave best when $k=5,8$ using Otsu's method.

In case of image 3, ChOA gave the best F value using Otsu's method when $k=2,8,10$ and gave the third best

Fig. 12 Program workflow


Fig. 13 Image thresholding workflow


Fig. 14 Otsu's thresholding of Image 3

result when $k=5$, 10 using Kapur's method. For F' Value, ChOA gave the third best result when $k=5$ by using Kapur's method, and gave the best result using Otsu's method when $k=2,8,10$. As for Q value using Kapur's method, ChOA gave the best value when number of threshold were 2,10 and the second best result when the number of threshold was 5. Additionally, using Otsu's method, ChOA gave the best values for $k=2,8,10$.

In case of image $4, \mathrm{ChOA}$ gave the best F value when $k=5,8,10$ using Kapur's method and gave the best result when $k=2,8,10$ using Otsu's method. For F' Value, ChOA gave the second and third best result using Kapur's method when $k=5,10$ respectively, and gave the best result using

Otsu's method when $k=2,8$ and the second best results when $k=5,10$. As for Q value using Kapur's method, ChOA gave the best value when number of threshold was 5 and the third best result when the number of threshold were 8,10 . Additionally, using Otsu's method, ChOA gave the best when $k=2,8$, and second best when $k=10$.

Table 6 represents the number of clusters generated by each algorithm for each of the threshold values, both for Kapur's entropy method. It is to be mentioned that the maximum number of generated sub-cubes or clusters is determined by (11). But generally the generated clusters are lower in number since some spaces in the 3D plane are kept vacant and some are filled. ChOA tends to generate lower number


Fig. 15 Kapur's thresholding of Image 4


Fig. 17 Converge curve solving Kapur's method for image 1


Fig. 18 Converge curve solving Otsu's method for image 1


Fig. 19 Converge curve solving Kapur's method for image 2


Fig. 20 Converge curve solving Otsu's method for image 2


Fig. 21 Converge curve solving Kapur's method for image 3


Fig. 22 Converge curve solving Otsu's method for image 3


Fig. 23 Converge curve solving Kapur's method for image 4


Fig. 24 Converge curve solving Otsu's method for image 4
Table 1 Fitness Values of Image 1 and Image 2

|  |  | K | Color | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | kapur | 2 | R | 12.372857 | 12.372857 | 12.372857 | 12.372857 | 12.372857 | 12.372857 | 12.372857 | 12.372857 | 12.372754 |
|  |  |  | G | 12.421712 | 12.421712 | 12.421712 | 12.421712 | 12.421712 | 12.421712 | 12.421712 | 12.421712 | 12.421395 |
|  |  |  | B | 12.593963 | 12.593963 | 12.593963 | 12.593963 | 12.593963 | 12.593963 | 12.593963 | 12.593963 | 12.593887 |
|  |  | 5 | R | 20.666193 | 20.666160 | 20.666193 | 20.666193 | 20.666193 | 20.666162 | 20.666193 | 20.666193 | 20.643232 |
|  |  |  | G | 20.934369 | 20.938162 | 20.927835 | 20.928681 | 20.935612 | 20.939279 | 20.928788 | 20.9289432 | 20.911856 |
|  |  |  | B | 21.176528 | 21.176385 | 21.176410 | 21.176196 | 21.176597 | 21.176538 | 21.176597 | 21.172512 | 21.117204 |
|  |  | 8 | R | 27.474067 | 27.486959 | 27.465192 | 27.484303 | 27.467813 | 27.481512 | 27.481728 | 27.461675 | 27.288891 |
|  |  |  | G | 27.969456 | 27.9666203 | 27.970492 | 27.964796 | 27.973122 | 27.966387 | 27.968874 | 27.963489 | 27.678408 |
|  |  |  | B | 28.276833 | 28.289863 | 28.259285 | 28.289836 | 28.278877 | 28.287689 | 28.277100 | 28.290128 | 28.096257 |
|  |  | 10 | R | 31.503162 | 31.524930 | 31.465783 | 31.521176 | 31.487059 | 31.509512 | 31.523769 | 31.505456 | 30.938372 |
|  |  |  | G | 32.095035 | 32.111117 | 32.097204 | 32.112612 | 32.085780 | 32.085206 | 32.085769 | 32.0910865 | 31.382341 |
|  |  |  | B | 32.419176 | 32.447299 | 32.393470 | 32.447251 | 32.416763 | 32.433842 | 32.441883 | 32.445479 | 31.876969 |
|  | otsu | 2 | R | 1688.6068 | 1688.6068 | 1688.6068 | 1688.6068 | 1688.6068 | 1688.6068 | 1688.6068 | 1688.6068 | 1688.6040 |
|  |  |  | G | 1564.1468 | 1564.1468 | 1564.1468 | 1564.14686 | 1564.14686 | 1564.1468 | 1564.1468 | 1564.1468 | 1564.1431 |
|  |  |  | B | 5163.0786 | 5163.0786 | 5163.0786 | 5163.0786 | 5163.0786 | 5163.0786 | 5163.0786 | 5163.0786 | 5163.0724 |
|  |  | 5 | R | 1886.0937 | 1886.0975 | 1886.0976 | 1886.0976 | 1886.0976 | 1886.0915 | 1886.0915 | 1886.0976 | 1877.6782 |
|  |  |  | G | 1778.9139 | 1778.9164 | 1778.9157 | 1778.9164 | 1778.8789 | 1778.9164 | 1778.9164 | 1778.9164 | 1775.4114 |
|  |  |  | B | 5478.3788 | 5478.3747 | 5478.3788 | 5478.3788 | 5478.3788 | 5478.3781 | 5478.3788 | 5478.3788 | 5474.7757 |
|  |  | 8 | R | 1921.2703 | 1921.4733 | 1921.3843 | 1921.4792 | 1920.5207 | 1921.3944 | 1921.4604 | 1921.4810 | 1913.1397 |
|  |  |  | G | 1817.5782 | 1819.7774 | 1818.7684 | 1820.0816 | 1816.9701 | 1819.3842 | 1818.6199 | 1818.2624 | 1800.7978 |
|  |  |  | B | 5534.9632 | 5535.0690 | 5534.8814 | 5535.0774 | 5535.0317 | 5535.0397 | 5535.0472 | 5535.0773 | 5516.3147 |
|  |  | 10 | R | 1930.8586 | 1932.6789 | 1931.0013 | 1932.6754 | 1928.8831 | 1930.4847 | 1932.0463 | NaN | 1922.1757 |
|  |  |  | G | 21830.3434 | 1831.9524 | 1830.2871 | 1831.9658 | 1826.2210 | 1831.7611 | 1829.9380 | NaN | 1809.3954 |
|  |  |  | B | 5548.7543 | 5549.3642 | 5549.0851 | 5549.1045 | 5548.5593 | 5548.9177 | 5548.7225 | NaN | 5525.2978 |
| Image 2 | kapur | 2 | R | 12.769517 | 12.769517 | 12.769517 | 12.769517 | 12.769517 | 12.769517 | 12.769517 | 12.769517 | 12.769115 |
|  |  |  | G | 13.056162 | 13.056162 | 13.056162 | 13.056162 | 13.056162 | 13.056162 | 13.056162 | 13.056162 | 13.056034 |
|  |  |  | B | 12.813901 | 12.813901 | 12.813901 | 12.813901 | 12.813901 | 12.813901 | 12.813901 | 12.813901 | 12.813655 |
|  |  | 5 | R | 21.545681 | 21.545115 | 21.545476 | 21.545342 | 21.545681 | 21.545162 | 21.545550 | 21.545448 | 21.508079 |
|  |  |  | G | 21.979204 | 21.980376 | 21.973448 | 21.980349 | 21.980200 | 21.980315 | 21.979435 | 21.980036 | 21.954498 |
|  |  |  | B | 21.615313 | 21.614305 | 21.6120875 | 21.613021 | 21.615179 | 21.613390 | 21.614106 | 21.612996 | 21.588597 |
|  |  | 8 | R | 28.790121 | 28.797747 | 28.772019 | 28.795719 | 28.800917 | 28.791314 | 28.777562 | 28.778000 | 28.616082 |
|  |  |  | G | 29.477244 | 29.477643 | 29.478742 | 29.478411 | 29.479473 | 29.475401 | 29.479927 | 29.479973 | 29.274375 |
|  |  |  | B | 29.000661 | 28.998212 | 29.001691 | 29.001747 | 29.003544 | 28.997842 | 29.002927 | 29.001982 | 28.825251 |

Table 1 (continued)

|  | K | Color | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| otsu | 10 | R | 33.215121 | 33.158651 | 33.185556 | 33.189398 | 33.212201 | 33.109765 | 33.182616 | 33.191660 | 32.596906 |
|  |  | G | 33.810679 | 33.829308 | 33.816052 | 33.832864 | 33.807115 | 33.798933 | 33.808557 | 33.834285 | 33.350285 |
|  |  | B | 33.324712 | 33.336083 | 33.332417 | 33.341131 | 33.329619 | 33.272821 | 33.301099 | 33.311236 | 32.908248 |
|  | 2 | R | 2125.9467 | 2125.9467 | 2125.9467 | 2125.9467 | 2125.9467 | 2125.9467 | 2125.9467 | 2125.9467 | 2125.9326 |
|  |  | G | 4872.6117 | 4872.6117 | 4872.6117 | 4872.6117 | 4872.6117 | 4872.6117 | 4872.6117 | 4872.6117 | 4872.6083 |
|  |  | B | 2545.3990 | 2545.3990 | 2545.3990 | 2545.3990 | 2545.3990 | 2545.3990 | 2545.3990 | 2545.3990 | 2545.3876 |
|  | 5 | R | 2358.0556 | 2358.0605 | 2358.0653 | 2358.0653 | 2358.0653 | 2358.0653 | 2358.0633 | 2358.0653 | 2350.7479 |
|  |  | G | 5235.3007 | 5235.3022 | 5235.3028 | 5235.3028 | 5235.2993 | 5235.2990 | 5235.3028 | 5235.3028 | 5232.3926 |
|  |  | B | 2886.5770 | 2886.8465 | 2886.7221 | 2886.8519 | 2886.2012 | 2886.8506 | 2886.5912 | 2886.7221 | 2878.8699 |
|  | 8 | R | 2400.5133 | 2401.0892 | 2400.6929 | 2401.1075 | 2396.4526 | 2401.1010 | 2400.7760 | 2401.0872 | 2382.6225 |
|  |  | G | 5305.0591 | 5305.5828 | 5305.3512 | 5305.5993 | 5305.0611 | 5305.4588 | 5305.5667 | 5304.9028 | 5292.0115 |
|  |  | B | 2952.7949 | 2952.8199 | 2952.8482 | 2952.8503 | 2952.8455 | 2952.7965 | 2952.6386 | 2952.8550 | 2944.9897 |
|  | 10 | R | 2413.3195 | 2414.3844 | 2413.0339 | 2414.4026 | 2410.0243 | 2414.3864 | 2413.1526 | 2414.4272 | 2392.8014 |
|  |  | G | 5322.6833 | 5323.2472 | 5322.9468 | 5323.2486 | 5322.5828 | 5322.8612 | 5323.2275 | 5323.2621 | 5305.1676 |
|  |  | B | 2968.2615 | 2968.9581 | 2968.3933 | 2968.9885 | 2968.3039 | 2968.1777 | 2967.9752 | 2968.9109 | 2960.8309 |

Table 2 Fitness values of Image 3 and Image 4

|  |  | K | Color | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 3 | kapur | 2 | R | 12.291294 | 12.291294 | 12.291294 | 12.291294 | 12.291294 | 12.291294 | 12.291294 | 12.291294 | 12.290830 |
|  |  |  | G | 11.403050 | 11.403050 | 11.403050 | 11.403050 | 11.403050 | 11.403050 | 11.403050 | 11.403050 | 11.402998 |
|  |  |  | B | 11.281663 | 11.281663 | 11.281663 | 11.281663 | 11.281663 | 11.281663 | 11.281663 | 11.281663 | 11.281584 |
|  |  | 5 | R | 21.031903 | 21.030366 | 21.025004 | 21.003236 | 21.034637 | 21.042328 | 20.878209 | 20.956416 | 20.886269 |
|  |  |  | G | 19.751055 | 19.794187 | 19.796310 | 19.793889 | 19.797222 | 19.796574 | 19.796615 | 19.796748 | 19.626686 |
|  |  |  | B | 18.729892 | 18.887606 | 18.888730 | 18.887239 | 18.878486 | 18.888530 | 18.775965 | 18.887909 | 18.700802 |
|  |  | 8 | R | 28.055990 | 28.054417 | 28.058352 | 28.055487 | 28.061566 | 28.059131 | 28.061638 | 28.048979 | 27.760383 |
|  |  |  | G | 27.001710 | 27.017876 | 27.003858 | 27.0155210 | 27.005196 | 27.0119786 | 27.021176 | 27.001105 | 26.356683 |
|  |  |  | B | 26.092771 | 26.241450 | 26.143653 | 26.240878 | 26.174391 | 26.238050 | 26.227804 | 26.236016 | 25.695290 |
|  |  | 10 | R | 32.057228 | 32.067446 | 32.062962 | 32.070388 | 32.060278 | 32.056516 | 32.074887 | 32.075519 | 31.739260 |
|  |  |  | G | 31.057274 | 31.237465 | 30.952461 | 31.190502 | 31.032936 | 31.092619 | 31.103508 | 31.207569 | 30.400521 |
|  |  |  | B | 30.315514 | 30.551967 | 30.304227 | 30.547003 | 30.290965 | 30.456497 | 30.454080 | 30.561148 | 29.741036 |
|  | otsu | 2 | R | 1848.8312 | 1848.8312 | 1848.8312 | 1848.8312 | 1848.8312 | 1848.8312 | 1848.8312 | 1848.8312 | 1848.8246 |
|  |  |  | G | 1047.9308 | 1047.9308 | 1047.9308 | 1047.9308 | 1047.9308 | 1047.9308 | 1047.9308 | 1047.9308 | 1047.9100 |
|  |  |  | B | 991.40433 | 991.40433 | 991.40433 | 991.40433 | 991.40433 | 991.40433 | 991.40433 | 991.40433 | 991.39895 |
|  |  | 5 | R | 2107.6433 | 2107.6465 | 2107.6472 | 2107.6472 | 2107.6472 | 2107.6463 | 2107.6472 | 2107.6472 | 2099.5810 |
|  |  |  | G | 1215.8271 | 1215.8289 | 1215.8289 | 1215.8289 | 1215.8289 | 1215.8275 | 1215.8289 | 1215.8289 | 1207.8897 |
|  |  |  | B | 1209.6561 | 1209.6613 | 1208.9458 | 1209.6619 | 1209.6619 | 1209.6604 | 1209.6605 | 1209.6619 | 1198.9441 |
|  |  | 8 | R | 2142.9055 | 2142.9742 | 2142.9467 | 2142.9795 | 2142.9696 | 2142.9503 | 2142.9703 | 2142.9788 | 2136.2455 |
|  |  |  | G | 1245.7437 | 1245.7947 | 1245.6794 | 1245.7966 | 1245.7944 | 1245.7782 | 1245.6820 | 1245.7968 | 1237.4876 |
|  |  |  | B | 1240.7066 | 1240.7664 | 1240.7666 | 1240.7754 | 1240.7624 | 1240.7457 | 1240.7478 | 1240.7754 | 1233.1521 |
|  |  | 10 | R | 2151.5508 | 2151.7445 | 2151.5807 | 2151.7516 | 2151.6248 | 2151.6560 | 2151.6117 | 2151.7570 | 2146.3745 |
|  |  |  | G | 1254.4264 | 1254.4488 | 1254.5314 | 1254.5626 | 1254.4166 | 1254.4525 | 1254.4607 | 1254.5588 | 1247.7149 |
|  |  |  | B | 1248.6223 | 1248.6957 | 1248.7244 | 1248.8211 | 1248.6846 | 1248.5334 | 1248.4866 | 1248.8328 | 1243.0356 |
| Image 4 | kapur | 2 | R | 12.702121 | 12.702121 | 12.702121 | 12.702121 | 12.702121 | 12.702121 | 12.702121 | 12.702121 | 12.701896 |
|  |  |  | G | 12.272001 | 12.272001 | 12.272001 | 12.272001 | 12.272001 | 12.272001 | 12.272001 | 12.272001 | 12.271890 |
|  |  |  | B | 12.567272 | 12.567272 | 12.567272 | 12.567272 | 12.567272 | 12.567272 | 12.567272 | 12.567272 | 12.565750 |
|  |  | 5 | R | 21.621497 | 21.621287 | 21.621418 | 21.621207 | 21.621534 | 21.621208 | 21.621484 | 21.621254 | 21.592733 |
|  |  |  | G | 20.301826 | 20.300886 | 20.295287 | 20.30018 | 20.301862 | 20.300753 | 20.301807 | 20.3011196 | 20.225679 |
|  |  |  | B | 21.101447 | 21.095670 | 21.095169 | 21.098768 | 21.101938 | 21.102155 | 21.102100 | 21.096283 | 21.027340 |
|  |  | 8 | R | 29.048428 | 29.050683 | 29.046852 | 29.051759 | 29.051878 | 29.049261 | 29.049136 | 29.051064 | 28.885892 |
|  |  |  | G | 27.018084 | 27.019959 | 27.018414 | 27.021286 | 27.023012 | 27.016488 | 27.019820 | 27.020738 | 26.824234 |
|  |  |  | B | 28.176694 | 28.215559 | 28.175845 | 28.212806 | 28.178609 | 28.189916 | 28.182138 | 28.188811 | 28.105777 |
|  |  | 10 | R | 33.406770 | 33.451707 | 33.384690 | 33.371454 | 33.403845 | 33.337967 | 33.340673 | 33.392079 | 32.922182 |
|  |  |  | G | $30.706307$ | 30.768322 | 30.693262 | 30.760078 | 30.709459 | 30.722779 | 30.687167 | 30.730489 | 30.392419 |
|  |  |  | B | 32.406350 | 32.404275 | 32.382758 | 32.399444 | 32.414234 | 32.390566 | 32.412764 | 32.409662 | 31.996483 |
|  | otsu | 2 | R | 3154.5198 | 3154.5198 | 3154.5198 | 3154.5198 | 3154.5198 | 3154.5198 | 3154.5198 | 3154.5198 | 3154.4998 |
|  |  |  | G | 1446.2514 | 1446.2514 | 1446.2514 | 1446.2514 | 1446.2514 | 1446.2514 | 1446.2514 | 1446.2514 | 1446.2348 |
|  |  |  | B | 1497.7029 | 1497.7029 | 1497.7029 | 1497.7029 | 1497.7029 | 1497.7029 | 1497.7029 | 1497.7029 | 1497.7004 |
|  |  | 5 | R | 3408.0065 | 3408.0065 | 3408.0065 | 3408.0065 | 3408.0065 | 3408.0047 | 3408.0043 | 3408.0065 | 3406.4441 |
|  |  |  | G | 1579.6046 | 1579.6102 | 1579.6102 | 1579.6102 | 1579.6102 | 1579.6099 | 1579.6102 | 1579.6102 | 1569.6511 |
|  |  |  | B | 1657.0532 | 1657.0037 | 1657.0264 | 1657.0048 | 1657.0588 | 1657.0169 | 1657.0203 | 1657.0242 | 1651.7061 |
|  |  | 8 | R | 3456.3291 | 3456.4767 | 3456.3732 | 3456.4781 | 3456.3125 | 3456.4497 | 3456.4291 | 3456.4826 | 3452.6821 |
|  |  |  | G | 1608.2817 | 1608.6150 | 1607.9583 | 1608.6161 | 1607.8449 | 1608.6039 | 1608.4153 | 1608.6171 | 1599.8342 |
|  |  |  | B | 1701.7142 | 1701.9509 | 1701.7316 | 1701.9555 | 1701.5893 | 1701.9391 | 1701.8621 | 1701.9569 | 1694.5229 |
|  |  | 10 | R | 3468.5617 | 3469.7650 | 3468.9095 | 3469.8057 | 3468.5095 | 3468.7043 | 3468.6594 | 3469.8060 | 3464.6132 |
|  |  |  | G | 1616.1023 | 1616.5897 | 1614.7736 | 1616.5972 | 1616.0020 | 1616.4179 | 1616.3880 | 1616.5904 | 1610.9169 |
|  |  |  | B | 1712.0581 | 1712.5404 | 1712.1088 | 1712.5434 | 1711.8068 | 1712.4504 | 1712.3493 | 1712.5299 | 1707.1319 |

Table 3 F values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | $8.594 \mathrm{E}-6$ | $8.594 \mathrm{E}-6$ | $8.594 \mathrm{E}-6$ | $8.594 \mathrm{E}-6$ | $8.594 \mathrm{E}-6$ | $8.594 \mathrm{E}-6$ | $8.594 \mathrm{E}-6$ | $8.594 \mathrm{E}-6$ | $8.946 \mathrm{E}-6$ |
|  |  | 5 | $6.838 \mathrm{E}-5$ | $6.885 \mathrm{E}-5$ | $7.185 \mathrm{E}-5$ | $7.106 \mathrm{E}-5$ | $6.846 \mathrm{E}-5$ | $6.832 \mathrm{E}-5$ | $7.027 \mathrm{E}-5$ | $7.134 \mathrm{E}-5$ | $6.773 \mathrm{E}-5$ |
|  |  | 8 | 0.0001628 | 0.0001589 | 0.0001624 | 0.0001612 | 0.0001603 | 0.0001575 | 0.0001621 | 0.0001659 | 0.0001726 |
|  |  | 10 | 0.0002549 | 0.0002626 | 0.0002639 | 0.0002651 | 0.0002574 | 0.0002562 | 0.0002564 | 0.0002679 | 0.0002618 |
|  | Otsu | 2 | $2.821 \mathrm{E}-5$ | $2.821 \mathrm{E}-5$ | $2.821 \mathrm{E}-5$ | $2.821 \mathrm{E}-5$ | $2.821 \mathrm{E}-5$ | $2.821 \mathrm{E}-5$ | $2.821 \mathrm{E}-5$ | $2.821 \mathrm{E}-5$ | $3.077 \mathrm{E}-5$ |
|  |  | 5 | $7.914 \mathrm{E}-5$ | $8.084 \mathrm{E}-5$ | $8.072 \mathrm{E}-5$ | $8.083 \mathrm{E}-5$ | $8.031 \mathrm{E}-5$ | $8.126 \mathrm{E}-5$ | $8.092 \mathrm{E}-5$ | $8.083 \mathrm{E}-5$ | $7.391 \mathrm{E}-5$ |
|  |  | 8 | 0.0002145 | 0.0002216 | 0.0002223 | 0.0002219 | 0.0002014 | 0.0002209 | 0.0002288 | 0.0002221 | 0.0001864 |
|  |  | 10 | 0.0003224 | 0.0003615 | 0.0003229 | 0.0003590 | 0.0002930 | 0.0003331 | 0.0003337 | NaN | 0.0002865 |
| Image 2 | Kapur | 2 | $9.812 \mathrm{E}-6$ | $9.812 \mathrm{E}-6$ | $9.812 \mathrm{E}-6$ | $9.812 \mathrm{E}-6$ | $9.812 \mathrm{E}-6$ | $9.812 \mathrm{E}-6$ | $9.812 \mathrm{E}-6$ | $9.812 \mathrm{E}-6$ | $1.022 \mathrm{E}-5$ |
|  |  | 5 | $6.060 \mathrm{E}-5$ | $6.212 \mathrm{E}-5$ | $6.040 \mathrm{E}-5$ | $5.848 \mathrm{E}-5$ | $5.993 \mathrm{E}-5$ | $6.242 \mathrm{E}-5$ | $5.933 \mathrm{E}-5$ | $5.748 \mathrm{E}-5$ | $6.660 \mathrm{E}-5$ |
|  |  | 8 | 0.0001784 | 0.0001759 | 0.0001831 | 0.0001790 | 0.0001812 | 0.0001746 | 0.0001785 | 0.0001810 | 0.0001595 |
|  |  | 10 | 0.0002777 | 0.0002720 | 0.0002726 | 0.0002703 | 0.0002778 | 0.0002710 | 0.0002632 | 0.0002665 | 0.0002852 |
|  | Otsu | 2 | $1.703 \mathrm{E}-5$ | $1.703 \mathrm{E}-5$ | $1.703 \mathrm{E}-5$ | $1.703 \mathrm{E}-5$ | $1.703 \mathrm{E}-5$ | $1.703 \mathrm{E}-5$ | $1.703 \mathrm{E}-5$ | $1.703 \mathrm{E}-5$ | $1.758 \mathrm{E}-5$ |
|  |  | 5 | $8.314 \mathrm{E}-5$ | $8.327 \mathrm{E}-5$ | $8.297 \mathrm{E}-5$ | $8.302 \mathrm{E}-5$ | $8.258 \mathrm{E}-5$ | $8.302 \mathrm{E}-5$ | $8.296 \mathrm{E}-5$ | $8.297 \mathrm{E}-5$ | $7.886 \mathrm{E}-5$ |
|  |  | 8 | 0.0002138 | 0.0002071 | 0.0002084 | 0.0002063 | 0.0002048 | 0.0002072 | 0.0002084 | 0.0002173 | 0.0001995 |
|  |  | 10 | 0.0003225 | 0.0003260 | 0.0003152 | 0.0003214 | 0.0003084 | 0.0003342 | 0.0003235 | 0.0003116 | 0.0003295 |
| Image 3 | Kapur | 2 | $2.331 \mathrm{E}-6$ | $2.331 \mathrm{E}-6$ | $2.331 \mathrm{E}-6$ | $2.331 \mathrm{E}-6$ | $2.331 \mathrm{E}-6$ | $2.331 \mathrm{E}-6$ | $2.331 \mathrm{E}-6$ | $2.331 \mathrm{E}-6$ | $2.332 \mathrm{E}-6$ |
|  |  | 5 | $1.212 \mathrm{E}-5$ | $1.431 \mathrm{E}-5$ | $1.331 \mathrm{E}-5$ | $1.366 \mathrm{E}-5$ | $1.345 \mathrm{E}-5$ | $1.366 \mathrm{E}-5$ | $1.169 \mathrm{E}-5$ | $1.331 \mathrm{E}-5$ | $1.314 \mathrm{E}-5$ |
|  |  | 8 | $3.114 \mathrm{E}-5$ | $3.189 \mathrm{E}-5$ | $3.173 \mathrm{E}-5$ | $3.258 \mathrm{E}-5$ | $3.206 \mathrm{E}-5$ | $3.398 \mathrm{E}-5$ | $3.323 \mathrm{E}-5$ | $3.245 \mathrm{E}-5$ | $3.348 \mathrm{E}-5$ |
|  |  | 10 | $5.896 \mathrm{E}-5$ | $6.120 \mathrm{E}-5$ | $5.936 \mathrm{E}-5$ | $6.088 \mathrm{E}-5$ | $5.751 \mathrm{E}-5$ | $5.438 \mathrm{E}-5$ | $5.509 \mathrm{E}-5$ | $6.215 \mathrm{E}-5$ | $5.556 \mathrm{E}-5$ |
|  | Otsu | 2 | $3.813 \mathrm{E}-6$ | $3.813 \mathrm{E}-6$ | $3.813 \mathrm{E}-6$ | $3.813 \mathrm{E}-6$ | $3.813 \mathrm{E}-6$ | $3.813 \mathrm{E}-6$ | $3.813 \mathrm{E}-6$ | $3.813 \mathrm{E}-6$ | $3.783 \mathrm{E}-6$ |
|  |  | 5 | $1.322 \mathrm{E}-5$ | $1.323 \mathrm{E}-5$ | $1.312 \mathrm{E}-5$ | $1.324 \mathrm{E}-5$ | $1.324 \mathrm{E}-5$ | $1.322 \mathrm{E}-5$ | $1.324 \mathrm{E}-5$ | $1.324 \mathrm{E}-5$ | $1.375 \mathrm{E}-5$ |
|  |  | 8 | $4.485 \mathrm{E}-5$ | $4.266 \mathrm{E}-5$ | $4.466 \mathrm{E}-5$ | $4.277 \mathrm{E}-5$ | $4.405 \mathrm{E}-5$ | $4.420 \mathrm{E}-5$ | $4.432 \mathrm{E}-5$ | $4.300 \mathrm{E}-5$ | $3.986 \mathrm{E}-5$ |
|  |  | 10 | $7.468 \mathrm{E}-5$ | $7.202 \mathrm{E}-5$ | $7.374 \mathrm{E}-5$ | $7.215 \mathrm{E}-5$ | $7.313 \mathrm{E}-5$ | $7.512 \mathrm{E}-5$ | $7.653 \mathrm{E}-5$ | $7.183 \mathrm{E}-5$ | $6.522 \mathrm{E}-5$ |
| Image 4 | Kapur | 2 | $1.441 \mathrm{E}-5$ | $1.441 \mathrm{E}-5$ | $1.441 \mathrm{E}-5$ | $1.441 \mathrm{E}-5$ | $1.441 \mathrm{E}-5$ | $1.441 \mathrm{E}-5$ | $1.441 \mathrm{E}-5$ | $1.441 \mathrm{E}-5$ | $1.446 \mathrm{E}-5$ |
|  |  | 5 | $6.945 \mathrm{E}-5$ | $6.612 \mathrm{E}-5$ | $6.627 \mathrm{E}-5$ | $6.706 \mathrm{E}-5$ | $6.925 \mathrm{E}-5$ | $6.968 \mathrm{E}-5$ | $6.969 \mathrm{E}-5$ | $6.536 \mathrm{E}-5$ | $6.386 \mathrm{E}-5$ |
|  |  | 8 | 0.0001940 | 0.0001923 | 0.0001947 | 0.0001916 | 0.0001983 | 0.0001918 | 0.0001945 | 0.0001951 | 0.0001789 |
|  |  | 10 | 0.0003137 | 0.0002969 | 0.0003227 | 0.0002825 | 0.0003172 | 0.0002951 | 0.0003127 | 0.0003072 | 0.0002760 |
|  | Otsu | 2 | $1.159 \mathrm{E}-5$ | $1.159 \mathrm{E}-5$ | $1.159 \mathrm{E}-5$ | $1.159 \mathrm{E}-5$ | $1.159 \mathrm{E}-5$ | $1.159 \mathrm{E}-5$ | $1.159 \mathrm{E}-5$ | $1.159 \mathrm{E}-5$ | $1.150 \mathrm{E}-5$ |
|  |  | 5 | $6.098 \mathrm{E}-5$ | $7.101 \mathrm{E}-5$ | $6.678 \mathrm{E}-5$ | $7.150 \mathrm{E}-5$ | $5.969 \mathrm{E}-5$ | $6.597 \mathrm{E}-5$ | $6.291 \mathrm{E}-5$ | $6.725 \mathrm{E}-5$ | $6.973 \mathrm{E}-5$ |
|  |  | 8 | 0.0002204 | 0.0002256 | 0.0002202 | 0.0002252 | 0.0002241 | 0.0002258 | 0.0002272 | 0.0002251 | 0.0001944 |
|  |  | 10 | 0.0003645 | 0.0004136 | 0.0003377 | 0.0004180 | 0.0003563 | 0.0003790 | 0.0003646 | 0.0004073 | 0.0003220 |

of clusters comparing to other algorithms for same number of threshold value.

After careful observation to the tabulated results, it becomes apparent that ChOA gave excel performance when image clustering is considered. In these four images, the pixels distribution are not deterministic and the nature of ChOA is stochastic. Taken into consideration that the nature of the pixel distribution is quite random, since ChOA performed relatively well in these four images considering the above clustering parameters, it can be concluded that using ChOA
is the better choice in image clustering comparing to other algorithms. ChOA has outperformed all other algorithms in most of the cases in terms of these clustering parameters. It is further evident that ChOA has shown more superior performance in Otsu's class variance method than it had done for Kapur's entropy method, implying that it is more compatible for image clustering approaches based on Otsu's class variance method (Fig. 14).

Table 4 F' Values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | $9.179 \mathrm{E}-7$ | $9.179 \mathrm{E}-7$ | $9.179 \mathrm{E}-7$ | $9.179 \mathrm{E}-7$ | $9.179 \mathrm{E}-7$ | $9.179 \mathrm{E}-7$ | $9.179 \mathrm{E}-7$ | $9.179 \mathrm{E}-7$ | $9.528 \mathrm{E}-7$ |
|  |  | 5 | $9.582 \mathrm{E}-6$ | $1.081 \mathrm{E}-5$ | $8.418 \mathrm{E}-6$ | $8.543 \mathrm{E}-6$ | $9.858 \mathrm{E}-6$ | $1.089 \mathrm{E}-5$ | $8.377 \mathrm{E}-6$ | $8.611 \mathrm{E}-6$ | $1.157 \mathrm{E}-5$ |
|  |  | 8 | 7.175E-5 | $6.926 \mathrm{E}-5$ | $7.671 \mathrm{E}-5$ | $7.100 \mathrm{E}-5$ | 7.399E-5 | $6.863 \mathrm{E}-5$ | $7.040 \mathrm{E}-5$ | 6.323E-5 | $6.712 \mathrm{E}-5$ |
|  |  | 10 | 0.0001941 | 0.0001881 | 0.0002062 | 0.0001854 | 0.0001935 | 0.0001842 | 0.0001846 | 0.0001940 | 0.0001770 |
|  | Otsu | 2 | $2.986 \mathrm{E}-6$ | $2.986 \mathrm{E}-6$ | $2.986 \mathrm{E}-6$ | $2.986 \mathrm{E}-6$ | $2.986 \mathrm{E}-6$ | $2.986 \mathrm{E}-6$ | $2.986 \mathrm{E}-6$ | $2.986 \mathrm{E}-6$ | $3.212 \mathrm{E}-6$ |
|  |  | 5 | $1.078 \mathrm{E}-5$ | $1.147 \mathrm{E}-5$ | $1.141 \mathrm{E}-5$ | $1.146 \mathrm{E}-5$ | $1.115 \mathrm{E}-5$ | $1.182 \mathrm{E}-5$ | $1.144 \mathrm{E}-5$ | $1.146 \mathrm{E}-5$ | $1.186 \mathrm{E}-5$ |
|  |  | 8 | $8.571 \mathrm{E}-5$ | $9.167 \mathrm{E}-5$ | 9.132E-5 | 0.0001038 | 7.627E-5 | $8.116 \mathrm{E}-5$ | $8.581 \mathrm{E}-5$ | $8.056 \mathrm{E}-5$ | $6.477 \mathrm{E}-5$ |
|  |  | 10 | 0.0002471 | 0.0002232 | 0.0002320 | 0.0002363 | 0.0002370 | 0.0002830 | 0.0002393 | NaN | 0.0002086 |
| Image 2 | Kapur | 2 | $9.833 \mathrm{E}-7$ | $9.833 \mathrm{E}-7$ | $9.833 \mathrm{E}-7$ | $9.833 \mathrm{E}-7$ | $9.833 \mathrm{E}-7$ | $9.833 \mathrm{E}-7$ | $9.833 \mathrm{E}-7$ | $9.833 \mathrm{E}-7$ | $1.024 \mathrm{E}-6$ |
|  |  | 5 | $6.825 \mathrm{E}-6$ | $6.951 \mathrm{E}-6$ | $6.610 \mathrm{E}-6$ | $6.390 \mathrm{E}-6$ | $6.703 \mathrm{E}-6$ | $6.918 \mathrm{E}-6$ | $6.586 \mathrm{E}-6$ | $6.313 \mathrm{E}-6$ | $7.232 \mathrm{E}-6$ |
|  |  | 8 | $2.425 \mathrm{E}-5$ | $2.384 \mathrm{E}-5$ | $2.546 \mathrm{E}-5$ | $2.426 \mathrm{E}-5$ | $2.622 \mathrm{E}-5$ | $2.427 \mathrm{E}-5$ | $2.785 \mathrm{E}-5$ | $2.508 \mathrm{E}-5$ | $2.233 \mathrm{E}-5$ |
|  |  | 10 | 5.123E-5 | $4.888 \mathrm{E}-5$ | 5.377E-5 | $5.028 \mathrm{E}-5$ | $5.405 \mathrm{E}-5$ | $4.935 \mathrm{E}-5$ | $4.729 \mathrm{E}-5$ | 5.197E-5 | $5.900 \mathrm{E}-5$ |
|  | Otsu | 2 | $1.770 \mathrm{E}-6$ | $1.770 \mathrm{E}-6$ | $1.770 \mathrm{E}-6$ | $1.770 \mathrm{E}-6$ | $1.770 \mathrm{E}-6$ | $1.770 \mathrm{E}-6$ | $1.770 \mathrm{E}-6$ | $1.770 \mathrm{E}-6$ | $1.867 \mathrm{E}-6$ |
|  |  | 5 | $9.338 \mathrm{E}-6$ | $9.203 \mathrm{E}-6$ | $9.066 \mathrm{E}-6$ | $9.112 \mathrm{E}-6$ | $9.077 \mathrm{E}-6$ | $9.256 \mathrm{E}-6$ | $9.078 \mathrm{E}-6$ | $9.066 \mathrm{E}-6$ | $8.579 \mathrm{E}-6$ |
|  |  | 8 | $3.206 \mathrm{E}-5$ | $3.952 \mathrm{E}-5$ | $3.370 \mathrm{E}-5$ | $3.637 \mathrm{E}-5$ | $3.005 \mathrm{E}-5$ | $3.798 \mathrm{E}-5$ | $3.235 \mathrm{E}-5$ | $3.401 \mathrm{E}-5$ | $3.082 \mathrm{E}-5$ |
|  |  | 10 | $7.464 \mathrm{E}-5$ | $7.425 \mathrm{E}-5$ | $6.706 \mathrm{E}-5$ | $7.086 \mathrm{E}-5$ | $6.660 \mathrm{E}-5$ | $8.497 \mathrm{E}-5$ | $7.360 \mathrm{E}-5$ | $6.991 \mathrm{E}-5$ | $7.862 \mathrm{E}-5$ |
| Image 3 | Kapur | 2 | $2.331 \mathrm{E}-7$ | $2.331 \mathrm{E}-7$ | $2.331 \mathrm{E}-7$ | $2.331 \mathrm{E}-7$ | $2.331 \mathrm{E}-7$ | $2.331 \mathrm{E}-7$ | $2.331 \mathrm{E}-7$ | $2.331 \mathrm{E}-7$ | 2.332E-7 |
|  |  | 5 | $1.312 \mathrm{E}-6$ | $1.547 \mathrm{E}-6$ | $1.458 \mathrm{E}-6$ | $1.434 \mathrm{E}-6$ | $1.525 \mathrm{E}-6$ | $1.538 \mathrm{E}-6$ | $1.234 \mathrm{E}-6$ | $1.432 \mathrm{E}-6$ | $1.368 \mathrm{E}-6$ |
|  |  | 8 | $3.570 \mathrm{E}-6$ | $3.612 \mathrm{E}-6$ | $3.746 \mathrm{E}-6$ | $3.713 \mathrm{E}-6$ | $3.600 \mathrm{E}-6$ | $3.828 \mathrm{E}-6$ | $3.854 \mathrm{E}-6$ | $3.759 \mathrm{E}-6$ | $4.012 \mathrm{E}-6$ |
|  |  | 10 | $8.179 \mathrm{E}-6$ | $7.642 \mathrm{E}-6$ | $8.391 \mathrm{E}-6$ | $7.782 \mathrm{E}-6$ | $7.726 \mathrm{E}-6$ | $7.478 \mathrm{E}-6$ | $7.672 \mathrm{E}-6$ | 7.882E-6 | $7.810 \mathrm{E}-6$ |
|  | Otsu | 2 | $3.813 \mathrm{E}-7$ | $3.813 \mathrm{E}-7$ | $3.813 \mathrm{E}-7$ | $3.813 \mathrm{E}-7$ | $3.813 \mathrm{E}-7$ | $3.813 \mathrm{E}-7$ | $3.813 \mathrm{E}-7$ | $3.813 \mathrm{E}-7$ | $3.783 \mathrm{E}-7$ |
|  |  | 5 | $1.369 \mathrm{E}-6$ | $1.372 \mathrm{E}-6$ | $1.353 \mathrm{E}-6$ | $1.365 \mathrm{E}-6$ | $1.365 \mathrm{E}-6$ | $1.374 \mathrm{E}-6$ | $1.367 \mathrm{E}-6$ | $1.365 \mathrm{E}-6$ | $1.432 \mathrm{E}-6$ |
|  |  | 8 | 6.077E-6 | 6.413E-6 | $6.440 \mathrm{E}-6$ | $6.290 \mathrm{E}-6$ | $6.372 \mathrm{E}-6$ | $6.270 \mathrm{E}-6$ | 6.333E-6 | 6.290E-6 | $5.049 \mathrm{E}-6$ |
|  |  | 10 | $1.248 \mathrm{E}-5$ | $1.229 \mathrm{E}-5$ | $1.207 \mathrm{E}-5$ | $1.256 \mathrm{E}-5$ | $1.243 \mathrm{E}-5$ | $1.250 \mathrm{E}-5$ | $1.225 \mathrm{E}-5$ | $1.217 \mathrm{E}-5$ | $1.044 \mathrm{E}-5$ |
| Image 4 | Kapur | 2 | $1.441 \mathrm{E}-6$ | $1.441 \mathrm{E}-6$ | $1.441 \mathrm{E}-6$ | $1.441 \mathrm{E}-6$ | $1.441 \mathrm{E}-6$ | $1.441 \mathrm{E}-6$ | $1.441 \mathrm{E}-6$ | $1.441 \mathrm{E}-6$ | $1.446 \mathrm{E}-6$ |
|  |  | 5 | $7.480 \mathrm{E}-6$ | $7.091 \mathrm{E}-6$ | $7.099 \mathrm{E}-6$ | $7.274 \mathrm{E}-6$ | $7.485 \mathrm{E}-6$ | $7.450 \mathrm{E}-6$ | $7.546 \mathrm{E}-6$ | $6.972 \mathrm{E}-6$ | $7.066 \mathrm{E}-6$ |
|  |  | 8 | $3.459 \mathrm{E}-5$ | $4.276 \mathrm{E}-5$ | $3.033 \mathrm{E}-5$ | $3.945 \mathrm{E}-5$ | $3.369 \mathrm{E}-5$ | $3.649 \mathrm{E}-5$ | $3.201 \mathrm{E}-5$ | $3.457 \mathrm{E}-5$ | $3.603 \mathrm{E}-5$ |
|  |  | 10 | 0.0001097 | $8.978 \mathrm{E}-5$ | 0.0001030 | $9.266 \mathrm{E}-5$ | 0.0001037 | 0.0001005 | 0.0001014 | 0.0001003 | $9.412 \mathrm{E}-5$ |
|  | Otsu | 2 | $1.159 \mathrm{E}-6$ | $1.159 \mathrm{E}-6$ | $1.159 \mathrm{E}-6$ | $1.159 \mathrm{E}-6$ | $1.159 \mathrm{E}-6$ | $1.159 \mathrm{E}-6$ | $1.159 \mathrm{E}-6$ | $1.159 \mathrm{E}-6$ | $1.152 \mathrm{E}-6$ |
|  |  | 5 | $8.242 \mathrm{E}-6$ | $8.529 \mathrm{E}-6$ | $8.399 \mathrm{E}-6$ | $8.545 \mathrm{E}-6$ | $8.181 \mathrm{E}-6$ | $8.367 \mathrm{E}-6$ | $8.228 \mathrm{E}-6$ | $8.414 \mathrm{E}-6$ | $8.209 \mathrm{E}-6$ |
|  |  | 8 | $4.466 \mathrm{E}-5$ | $3.997 \mathrm{E}-5$ | $4.194 \mathrm{E}-5$ | $4.043 \mathrm{E}-5$ | $4.501 \mathrm{E}-5$ | $4.132 \mathrm{E}-5$ | $4.574 \mathrm{E}-5$ | $4.010 \mathrm{E}-5$ | $3.827 \mathrm{E}-5$ |
|  |  | 10 | 0.0001291 | 0.0001433 | 0.0001035 | 0.0001411 | 0.0001178 | 0.0001378 | 0.0001246 | 0.0001429 | 0.0001127 |

### 7.5 Image segmentation

The values of GCE, PRI, VOI, PSNR, FSIM, SSIM for different algorithms along with ChOA can be found from Tables 7, 8, 9, 10, 11, 12 respectively.

For the case of PRI, using Kapur's entropy, for image 1, ChOA gives the best value for $\mathrm{K}=5$. It gives competitive value while standing at third position comparing to other algorithms for $K=8,10$. For image 2, it gives the best value for $\mathrm{K}=5$. For image 3, it gives the best value for $\mathrm{K}=2$. For image 4, it gives the best value for $\mathrm{K}=2$. Using Otsu's
entropy, for image 1, ChOA gives the best value for $\mathrm{K}=5$. For image 2, it does not provide best value for any case all of the values are nearly close to the other competing algorithms. For image 3, ChOA gives the best value for $\mathrm{K}=2$. For image 4, it provides the best value for $K=2$ and while standing at third position, gives competitive value for $\mathrm{K}=5$.

Now in case of GCE, using Kapur's entropy, for image 1, ChOA gives the best value for $\mathrm{K}=2$, and provides good, competitive values for $K=8,10$. For image 2, it gives the best value for $K=2$ and second best value for $K=8$. For image 3, it provides the best values for $\mathrm{K}=5,8$, and third

Table 5 Q Values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | $3.378 \mathrm{E}-6$ | $3.378 \mathrm{E}-6$ | $3.378 \mathrm{E}-6$ | $3.378 \mathrm{E}-6$ | $3.378 \mathrm{E}-6$ | $3.378 \mathrm{E}-6$ | $3.378 \mathrm{E}-6$ | 3.378E-6 | $3.418 \mathrm{E}-6$ |
|  |  | 5 | $2.025 \mathrm{E}-5$ | $2.073 \mathrm{E}-5$ | $2.013 \mathrm{E}-5$ | $2.004 \mathrm{E}-5$ | $2.035 \mathrm{E}-5$ | $2.073 \mathrm{E}-5$ | $1.995 \mathrm{E}-5$ | $2.012 \mathrm{E}-5$ | $2.066 \mathrm{E}-5$ |
|  |  | 8 | $7.664 \mathrm{E}-5$ | $7.327 \mathrm{E}-5$ | $8.287 \mathrm{E}-5$ | $7.505 \mathrm{E}-5$ | $8.013 \mathrm{E}-5$ | $7.422 \mathrm{E}-5$ | $7.444 \mathrm{E}-5$ | $6.491 \mathrm{E}-5$ | $7.079 \mathrm{E}-5$ |
|  |  | 10 | 0.0002739 | 0.0002524 | 0.0002930 | 0.0002429 | 0.0002730 | 0.0002532 | 0.0002522 | 0.0002639 | 0.0002360 |
|  | Otsu | 2 | $7.013 \mathrm{E}-6$ | $7.013 \mathrm{E}-6$ | $7.013 \mathrm{E}-6$ | $7.013 \mathrm{E}-6$ | $7.013 \mathrm{E}-6$ | $7.013 \mathrm{E}-6$ | $7.013 \mathrm{E}-6$ | $7.013 \mathrm{E}-6$ | $7.314 \mathrm{E}-6$ |
|  |  | 5 | $2.306 \mathrm{E}-5$ | $2.355 \mathrm{E}-5$ | $2.350 \mathrm{E}-5$ | $2.353 \mathrm{E}-5$ | $2.328 \mathrm{E}-5$ | $2.369 \mathrm{E}-5$ | $2.355 \mathrm{E}-5$ | $2.353 \mathrm{E}-5$ | $2.303 \mathrm{E}-5$ |
|  |  | 8 | $8.700 \mathrm{E}-5$ | $9.003 \mathrm{E}-5$ | $8.976 \mathrm{E}-5$ | 0.0001014 | $8.080 \mathrm{E}-5$ | $8.149 \mathrm{E}-5$ | $8.399 \mathrm{E}-5$ | $8.152 \mathrm{E}-5$ | $7.114 \mathrm{E}-5$ |
|  |  | 10 | 0.0003514 | 0.0002630 | 0.0003114 | 0.0002965 | 0.0003621 | 0.0004279 | 0.0003278 | NaN | 0.0002937 |
| Image 2 | Kapur | 2 | $1.118 \mathrm{E}-5$ | $1.118 \mathrm{E}-5$ | $1.118 \mathrm{E}-5$ | $1.118 \mathrm{E}-5$ | $1.118 \mathrm{E}-5$ | $1.118 \mathrm{E}-5$ | $1.118 \mathrm{E}-5$ | $1.118 \mathrm{E}-5$ | $1.125 \mathrm{E}-5$ |
|  |  | 5 | $2.973 \mathrm{E}-5$ | $2.978 \mathrm{E}-5$ | $2.946 \mathrm{E}-5$ | $2.892 \mathrm{E}-5$ | $2.953 \mathrm{E}-5$ | $2.967 \mathrm{E}-5$ | $2.928 \mathrm{E}-5$ | $2.872 \mathrm{E}-5$ | $2.957 \mathrm{E}-5$ |
|  |  | 8 | $5.703 \mathrm{E}-5$ | $5.641 \mathrm{E}-5$ | $5.776 \mathrm{E}-5$ | $5.693 \mathrm{E}-5$ | $5.791 \mathrm{E}-5$ | 5.672E-5 | $5.891 \mathrm{E}-5$ | $5.753 \mathrm{E}-5$ | $5.571 \mathrm{E}-5$ |
|  |  | 10 | $8.795 \mathrm{E}-5$ | $8.746 \mathrm{E}-5$ | $9.076 \mathrm{E}-5$ | $8.891 \mathrm{E}-5$ | $8.987 \mathrm{E}-5$ | $8.844 \mathrm{E}-5$ | $8.554 \mathrm{E}-5$ | $8.954 \mathrm{E}-5$ | $9.588 \mathrm{E}-5$ |
|  | Otsu | 2 | $1.388 \mathrm{E}-5$ | $1.388 \mathrm{E}-5$ | $1.388 \mathrm{E}-5$ | $1.388 \mathrm{E}-5$ | $1.388 \mathrm{E}-5$ | $1.388 \mathrm{E}-5$ | $1.388 \mathrm{E}-5$ | $1.388 \mathrm{E}-5$ | $1.392 \mathrm{E}-5$ |
|  |  | 5 | $3.470 \mathrm{E}-5$ | $3.471 \mathrm{E}-5$ | $3.479 \mathrm{E}-5$ | $3.482 \mathrm{E}-5$ | $3.471 \mathrm{E}-5$ | $3.485 \mathrm{E}-5$ | $3.473 \mathrm{E}-5$ | $3.479 \mathrm{E}-5$ | $3.453 \mathrm{E}-5$ |
|  |  | 8 | $6.966 \mathrm{E}-5$ | $7.429 \mathrm{E}-5$ | $7.008 \mathrm{E}-5$ | $7.192 \mathrm{E}-5$ | $6.749 \mathrm{E}-5$ | $7.311 \mathrm{E}-5$ | $6.947 \mathrm{E}-5$ | $7.090 \mathrm{E}-5$ | $6.664 \mathrm{E}-5$ |
|  |  | 10 | 0.0001120 | 0.0001156 | 0.0001049 | 0.0001120 | 0.0001043 | 0.0001236 | 0.0001113 | 0.0001097 | 0.0001188 |
| Image 3 | Kapur | 2 | $3.295 \mathrm{E}-6$ | $3.295 \mathrm{E}-6$ | $3.295 \mathrm{E}-6$ | $3.295 \mathrm{E}-6$ | $3.295 \mathrm{E}-6$ | $3.295 \mathrm{E}-6$ | $3.295 \mathrm{E}-6$ | $3.295 \mathrm{E}-6$ | $3.290 \mathrm{E}-6$ |
|  |  | 5 | $6.075 \mathrm{E}-6$ | $6.464 \mathrm{E}-6$ | $6.348 \mathrm{E}-6$ | $6.280 \mathrm{E}-6$ | $6.481 \mathrm{E}-6$ | $6.500 \mathrm{E}-6$ | $5.947 \mathrm{E}-6$ | $6.342 \mathrm{E}-6$ | $6.074 \mathrm{E}-6$ |
|  |  | 8 | $1.188 \mathrm{E}-5$ | $1.170 \mathrm{E}-5$ | $1.177 \mathrm{E}-5$ | $1.180 \mathrm{E}-5$ | $1.193 \mathrm{E}-5$ | $1.215 \mathrm{E}-5$ | $1.188 \mathrm{E}-5$ | $1.179 \mathrm{E}-5$ | $1.187 \mathrm{E}-5$ |
|  |  | 10 | $1.842 \mathrm{E}-5$ | $1.810 \mathrm{E}-5$ | $1.853 \mathrm{E}-5$ | $1.814 \mathrm{E}-5$ | $1.806 \mathrm{E}-5$ | $1.742 \mathrm{E}-5$ | $1.764 \mathrm{E}-5$ | $1.838 \mathrm{E}-5$ | $1.718 \mathrm{E}-5$ |
|  | Otsu | 2 | $2.675 \mathrm{E}-6$ | $2.675 \mathrm{E}-6$ | $2.675 \mathrm{E}-6$ | $2.675 \mathrm{E}-6$ | $2.675 \mathrm{E}-6$ | $2.675 \mathrm{E}-6$ | $2.675 \mathrm{E}-6$ | $2.675 \mathrm{E}-6$ | $2.665 \mathrm{E}-6$ |
|  |  | 5 | $6.389 \mathrm{E}-6$ | $6.410 \mathrm{E}-6$ | $6.363 \mathrm{E}-6$ | $6.402 \mathrm{E}-6$ | $6.402 \mathrm{E}-6$ | $6.410 \mathrm{E}-6$ | $6.404 \mathrm{E}-6$ | $6.402 \mathrm{E}-6$ | $6.437 \mathrm{E}-6$ |
|  |  | 8 | $1.514 \mathrm{E}-5$ | $1.543 \mathrm{E}-5$ | $1.547 \mathrm{E}-5$ | $1.531 \mathrm{E}-5$ | $1.539 \mathrm{E}-5$ | $1.536 \mathrm{E}-5$ | $1.540 \mathrm{E}-5$ | $1.530 \mathrm{E}-5$ | $1.348 \mathrm{E}-5$ |
|  |  | 10 | $2.370 \mathrm{E}-5$ | $2.327 \mathrm{E}-5$ | $2.332 \mathrm{E}-5$ | $2.356 \mathrm{E}-5$ | $2.396 \mathrm{E}-5$ | $2.359 \mathrm{E}-5$ | $2.339 \mathrm{E}-5$ | $2.312 \mathrm{E}-5$ | $2.058 \mathrm{E}-5$ |
| Image 4 | Kapur | 2 | $8.742 \mathrm{E}-6$ | $8.742 \mathrm{E}-6$ | $8.742 \mathrm{E}-6$ | $8.742 \mathrm{E}-6$ | $8.742 \mathrm{E}-6$ | $8.742 \mathrm{E}-6$ | $8.742 \mathrm{E}-6$ | $8.742 \mathrm{E}-6$ | $8.761 \mathrm{E}-6$ |
|  |  | 5 | $2.481 \mathrm{E}-5$ | $2.454 \mathrm{E}-5$ | $2.450 \mathrm{E}-5$ | $2.457 \mathrm{E}-5$ | $2.475 \mathrm{E}-5$ | $2.489 \mathrm{E}-5$ | $2.482 \mathrm{E}-5$ | $2.428 \mathrm{E}-5$ | $2.394 \mathrm{E}-5$ |
|  |  | 8 | $5.688 \mathrm{E}-5$ | $6.097 \mathrm{E}-5$ | $5.483 \mathrm{E}-5$ | $5.874 \mathrm{E}-5$ | $5.662 \mathrm{E}-5$ | $5.751 \mathrm{E}-5$ | $5.554 \mathrm{E}-5$ | $5.704 \mathrm{E}-5$ | $5.565 \mathrm{E}-5$ |
|  |  | 10 | 0.0001263 | 0.0001048 | 0.0001176 | 0.0001105 | 0.0001189 | 0.0001193 | 0.0001169 | 0.0001159 | 0.0001123 |
|  | Otsu | 2 | $8.021 \mathrm{E}-6$ | $8.021 \mathrm{E}-6$ | $8.021 \mathrm{E}-6$ | $8.021 \mathrm{E}-6$ | $8.021 \mathrm{E}-6$ | $8.021 \mathrm{E}-6$ | $8.021 \mathrm{E}-6$ | $8.021 \mathrm{E}-6$ | $7.984 \mathrm{E}-6$ |
|  |  | 5 | $2.593 \mathrm{E}-5$ | $2.718 \mathrm{E}-5$ | $2.664 \mathrm{E}-5$ | $2.724 \mathrm{E}-5$ | $2.574 \mathrm{E}-5$ | $2.653 \mathrm{E}-5$ | $2.612 \mathrm{E}-5$ | $2.670 \mathrm{E}-5$ | $2.657 \mathrm{E}-5$ |
|  |  | 8 | $6.994 \mathrm{E}-5$ | $6.746 \mathrm{E}-5$ | $6.766 \mathrm{E}-5$ | $6.770 \mathrm{E}-5$ | $6.987 \mathrm{E}-5$ | $6.835 \mathrm{E}-5$ | $7.110 \mathrm{E}-5$ | $6.756 \mathrm{E}-5$ | $6.052 \mathrm{E}-5$ |
|  |  | 10 | 0.0001497 | 0.0001517 | 0.0001225 | 0.0001476 | 0.0001382 | 0.0001578 | 0.0001438 | 0.0001514 | 0.0001336 |

best value for $K=10$. For image 4 , it provides second best value for $K=8$ and fifth best for $K=5$. Using Otsu's entropy, for image 1, ChOA gives the best value for $\mathrm{K}=2$, 8 , it also provides competitive value for $\mathrm{K}=10$ by giving the third best value. For image 2, it provides the best value for $K=2,5,10$, and third best value for $K=8$. For image 3, it provides the best value for $K=5$ and competitive values for other cases. For image 4, it provides best value for $\mathrm{K}=$ 8 and second value for $\mathrm{K}=10$, while providing competitive values for the other two cases (Fig. 15).

For the case of VOI, using Kapur's entropy, for image 1 , ChOA gives the best value for $\mathrm{K}=2,5$, and competitive values for higher thresholds. For image 2, it gives the best values for $K=2$ and competitive value for $K=5$. For image 3 , it provides the best value for $\mathrm{K}=5$ while providing nearly the best values for the other cases. For image 4, it gives the second best value for $\mathrm{K}=5$. Using Otsu's variance, for image 1, it provides the best value for $\mathrm{K}=2$. For image 2 , it provides the best values for $\mathrm{K}=2,5$. For image 3 , it provides the best value for $\mathrm{K}=2$ and competitive values for

Table 6 Number of Clusters

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | 22 | 22 | 22 | 22 | 22 | 22 | 22 | 22 | 22 |
|  |  | 5 | 109 | 110 | 110 | 110 | 110 | 110 | 109 | 110 | 115 |
|  |  | 8 | 296 | 289 | 298 | 292 | 296 | 293 | 292 | 288 | 296 |
|  |  | 10 | 460 | 467 | 468 | 466 | 466 | 462 | 460 | 476 | 457 |
|  | Otsu | 2 | 25 | 25 | 25 | 25 | 25 | 25 | 25 | 25 | 25 |
|  |  | 5 | 138 | 141 | 141 | 141 | 139 | 141 | 141 | 141 | 135 |
|  |  | 8 | 341 | 341 | 341 | 341 | 337 | 341 | 345 | 346 | 320 |
|  |  | 10 | 539 | 552 | 528 | 562 | 524 | 546 | 541 | NaN | 482 |
| Image 2 | Kapur | 2 | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 15 | 15 |
|  |  | 5 | 59 | 59 | 58 | 58 | 59 | 59 | 58 | 58 | 56 |
|  |  | 8 | 124 | 123 | 124 | 123 | 124 | 123 | 126 | 125 | 121 |
|  |  | 10 | 179 | 183 | 182 | 183 | 180 | 191 | 182 | 181 | 191 |
|  | Otsu | 2 | 19 | 19 | 19 | 19 | 19 | 19 | 19 | 19 | 19 |
|  |  | 5 | 66 | 66 | 66 | 66 | 66 | 66 | 66 | 66 | 64 |
|  |  | 8 | 141 | 145 | 143 | 143 | 141 | 144 | 143 | 143 | 138 |
|  |  | 10 | 211 | 215 | 208 | 213 | 206 | 217 | 211 | 211 | 213 |
| Image 3 | Kapur | 2 | 17 | 17 | 17 | 17 | 17 | 17 | 17 | 17 | 17 |
|  |  | 5 | 52 | 52 | 53 | 52 | 54 | 53 | 48 | 52 | 51 |
|  |  | 8 | 112 | 110 | 112 | 110 | 110 | 112 | 111 | 110 | 110 |
|  |  | 10 | 179 | 167 | 183 | 170 | 177 | 171 | 173 | 172 | 163 |
|  | Otsu | 2 | 16 | 16 | 16 | 16 | 16 | 16 | 16 | 16 | 16 |
|  |  | 5 | 65 | 65 | 65 | 65 | 65 | 65 | 65 | 65 | 59 |
|  |  | 8 | 147 | 149 | 150 | 149 | 149 | 148 | 149 | 149 | 127 |
|  |  | 10 | 232 | 226 | 228 | 228 | 226 | 231 | 230 | 226 | 191 |
| Image 4 | Kapur | 2 | 20 | 20 | 20 | 20 | 20 | 20 | 20 | 20 | 20 |
|  |  | 5 | 98 | 96 | 96 | 97 | 98 | 98 | 98 | 96 | 93 |
|  |  | 8 | 244 | 243 | 244 | 242 | 245 | 243 | 243 | 244 | 235 |
|  |  | 10 | 379 | 356 | 383 | 361 | 378 | 373 | 383 | 374 | 357 |
|  | Otsu | 2 | 23 | 23 | 23 | 23 | 23 | 23 | 23 | 23 | 23 |
|  |  | 5 | 108 | 109 | 109 | 109 | 108 | 109 | 108 | 109 | 105 |
|  |  | 8 | 286 | 292 | 279 | 292 | 282 | 292 | 289 | 292 | 253 |
|  |  | 10 | 439 | 437 | 419 | 436 | 435 | 447 | 440 | 436 | 398 |

other cases. For image 4, it provides values close to the best value in the list for all four threshold values.

In case of image 1, ChoA gave the best result in PSNR for $k=2,5$ using Kapur's method; SSIM result was best in $k=1$, and for FSIM the result was best when $k=2,5$ for Kapur's method and when $k=2$ for otsus' method.

For image 2, ChOA's best result result in PSNR was when $k=5$ using Kapur's method, and SSIM result was best when $k=5$ using Kapur's method, and FSIM results were exactly similar to that of SSIM and PSNR (Fig. 16).

In case of image 3, PSNR was best when $k=2$ using Kapur's method and when $k=2,8$ using Otsu's method,
and the algorithm gave the second best PSNR when $k=10$ using Otsu's method. For SSIM, in both Kapur's and Otsu's method, the best result was when $k=2$. For FSIM, ChOA gave the best for $k=2$ in Kapur's method and $k=2$ in Otsu's method; ChOA also gave third best FSIM using Otsu's method.

For image 4, best result for PSNR was given by ChOA when $k=2$ in both of the method.

In case of other threshold numbers, ChOA gave competitive result in the rest of the parameters.

The result achieved for different image segmentation parameters signifies Chimp Optimization Algorithm's

Table 7 GCE values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | 0.7401022 | 0.7401022 | 0.7401022 | 0.7401022 | 0.7401022 | 0.7401022 | 0.7401024 | 0.7401022 | 0.7398421 |
|  |  | 5 | 0.8090890 | 0.8087080 | 0.8122764 | 0.8115658 | 0.8095260 | 0.8076563 | 0.8114339 | 0.8126369 | 0.8127623 |
|  |  | 8 | 0.8375948 | 0.8362083 | 0.8377495 | 0.8341675 | 0.8401173 | 0.8346083 | 0.8342278 | 0.8478774 | 0.8371196 |
|  |  | 10 | 0.8377620 | 0.8465624 | 0.8346650 | 0.8469645 | 0.8383987 | 0.8378010 | 0.8424697 | 0.8409490 | 0.8404271 |
|  | Otsu | 2 | 0.7380297 | 0.7380297 | 0.7380297 | 0.7380297 | 0.7380297 | 0.7380297 | 0.7380297 | 0.7380297 | 0.7352447 |
|  |  | 5 | 0.8184662 | 0.8151762 | 0.8155834 | 0.8151739 | 0.8179646 | 0.8126813 | 0.8121230 | 0.8151739 | 0.8157110 |
|  |  | 8 | 0.8364772 | 0.8394654 | 0.8378076 | 0.8408182 | 0.8351204 | 0.8368324 | 0.8374493 | 0.8383382 | 0.8293978 |
|  |  | 10 | 0.8268988 | 0.8255083 | 0.8306147 | 0.8267042 | 0.8362147 | 0.8222586 | 0.8322172 | NaN | 0.8234572 |
| Image 2 | Kapur | 2 | 0.7067648 | 0.7067648 | 0.7067648 | 0.7067648 | 0.7067648 | 0.7067648 | 0.7067648 | 0.7067648 | 0.6995715 |
|  |  | 5 | 0.7692075 | 0.7666628 | 0.7700412 | 0.7652705 | 0.7687575 | 0.7683177 | 0.7676031 | 0.7664471 | 0.7729088 |
|  |  | 8 | 0.7847124 | 0.7885286 | 0.7855112 | 0.78114062 | 0.7847000 | 0.7844945 | 0.7873781 | 0.7852935 | 0.7814643 |
|  |  | 10 | 0.7861190 | 0.7885115 | 0.7892061 | 0.7895727 | 0.7879943 | 0.7893165 | 0.7932822 | 0.7860364 | 0.7897926 |
|  | Otsu | 2 | 0.7189673 | 0.7189673 | 0.7189673 | 0.7189673 | 0.7189673 | 0.7189673 | 0.7189673 | 0.7189673 | 0.7189496 |
|  |  | 5 | 0.7840605 | 0.7849918 | 0.7881583 | 0.7872190 | 0.7878117 | 0.7843835 | 0.7878127 | 0.7881583 | 0.7788456 |
|  |  | 8 | 0.7935995 | 0.8027025 | 0.7979745 | 0.8047776 | 0.7987591 | 0.7973333 | 0.7934298 | 0.7944037 | 0.7936273 |
|  |  | 10 | 0.7961882 | 0.7955455 | 0.7950484 | 0.7961843 | 0.7957715 | 0.7921153 | 0.7993835 | 0.7962816 | 0.7914766 |
| Image 3 | Kapur | 2 | 0.7071777 | 0.7071777 | 0.7071777 | 0.7071777 | 0.7071777 | 0.7071777 | 0.7071777 | 0.7071777 | 0.7098366 |
|  |  | 5 | 0.7169523 | 0.7202978 | 0.7270952 | 0.7263886 | 0.7254977 | 0.7175942 | 0.7281371 | 0.7313596 | 0.7152261 |
|  |  | 8 | 0.7592833 | 0.7524897 | 0.7514513 | 0.7549964 | 0.7571284 | 0.7521763 | 0.7487347 | 0.7503311 | 0.7368054 |
|  |  | 10 | 0.7511133 | 0.7568617 | 0.7561045 | 0.7544547 | 0.7530906 | 0.7652466 | 0.7628362 | 0.7554382 | 0.7535885 |
|  | Otsu | 2 | 0.7068947 | 0.7068947 | 0.7068947 | 0.7068947 | 0.7068947 | 0.7068947 | 0.7068947 | 0.7068947 | 0.7069815 |
|  |  | 5 | 0.7377244 | 0.7419418 | 0.7414628 | 0.7416817 | 0.7416817 | 0.7414860 | 0.7405943 | 0.7416817 | 0.7353298 |
|  |  | 8 | 0.7494254 | 0.7521713 | 0.7516004 | 0.7519477 | 0.7557806 | 0.7490750 | 0.7473474 | 0.7522846 | 0.7504423 |
|  |  | 10 | 0.7430081 | 0.7372852 | 0.7422038 | 0.7385129 | 0.7414544 | 0.7467788 | 0.7401779 | 0.7376211 | 0.7505356 |
| Image 4 | Kapur | 2 | 0.7633346 | 0.7633346 | 0.7633346 | 0.7633346 | 0.7633346 | 0.7633346 | 0.7633346 | 0.7633346 | 0.7677439 |
|  |  | 5 | 0.8048444 | 0.8010997 | 0.8007615 | 0.8044664 | 0.8043818 | 0.8063933 | 0.8045323 | 0.8004366 | 0.8044034 |
|  |  | 8 | 0.8251521 | 0.8213815 | 0.8246816 | 0.8197151 | 0.8279487 | 0.8239419 | 0.8296359 | 0.8231953 | 0.8201649 |
|  |  | 10 | 0.8194140 | 0.8252892 | 0.8124996 | 0.8168426 | 0.8160397 | 0.8153317 | 0.8122309 | 0.8173751 | 0.8202654 |
|  | Otsu | 2 | 0.7748162 | 0.7748162 | 0.7748162 | 0.7748162 | 0.7748162 | 0.7748162 | 0.7748162 | 0.7748162 | 0.7773568 |
|  |  | 5 | 0.8232756 | 0.8079247 | 0.8144996 | 0.8078039 | 0.8245431 | 0.8151019 | 0.8191737 | 0.8138300 | 0.8180743 |
|  |  | 8 | 0.8242975 | 0.8220828 | 0.8236080 | 0.8216555 | 0.8264061 | 0.8235773 | 0.8256691 | 0.8222287 | 0.8201661 |
|  |  | 10 | 0.8230292 | 0.8220396 | 0.828461 | 0.8216130 | 0.8220380 | 0.8197402 | 0.8223072 | 0.8166962 | 0.8173459 |

effectiveness in multilevel thresholding based applications. ChOA can keep up with moderate to competitive performance in most of the cases, and in many cases it outperforms all other algorithms that we have compared with. It is to mention that ChOA provided comparatively better performance in terms of these segmentation parameters while lower levels of thresholding were used. The different chaotic maps available in the ChOA can be utilized to generate better results by switching to different values of $m$ (23). However, there is no universal metaheuristic algorithm that can
outperform all other algorithms in all segmentation tasks. That is why, ChOA can be considered as quite an important one in this regard.

### 7.6 Image quality

To measure the quality of the segmented image, parameters BRISQUE,PIQE, and NIQE were used to evaluate, and the values of the paremeters are given in the Table 13, Table 14, Table 15 accordingly.

Table 8 PRI values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | 0.9514666 | 0.9514666 | 0.9514666 | 0.9514666 | 0.9514666 | 0.9514666 | 0.9514666 | 0.9514666 | 0.9513863 |
|  |  | 5 | 0.9727083 | 0.9726548 | 0.9733310 | 0.9732004 | 0.9727636 | 0.9725107 | 0.9731275 | 0.9733631 | 0.9743540 |
|  |  | 8 | 0.9815287 | 0.9815430 | 0.9820300 | 0.9814921 | 0.9819127 | 0.9812118 | 0.9814995 | 0.9829055 | 0.9819686 |
|  |  | 10 | 0.9833491 | 0.9839416 | 0.9833330 | 0.9840665 | 0.9834140 | 0.9834156 | 0.9836827 | 0.9838227 | 0.9838362 |
|  | Otsu | 2 | 0.9515554 | 0.9515554 | 0.9515554 | 0.9515554 | 0.9515554 | 0.9515554 | 0.9515554 | 0.9515554 | 0.9509178 |
|  |  | 5 | 0.9767826 | 0.9764159 | 0.9764649 | 0.9764209 | 0.9767403 | 0.9760988 | 0.9760339 | 0.9764209 | 0.9777553 |
|  |  | 8 | 0.9835268 | 0.9835102 | 0.9835367 | 0.9835569 | 0.9832785 | 0.9833973 | 0.9836028 | 0.9837485 | 0.9824061 |
|  |  | 10 | 0.9844744 | 0.9848700 | 0.9846917 | 0.9848447 | 0.9851909 | 0.9842573 | 0.9847806 | NaN | 0.9829497 |
| Image 2 | Kapur | 2 | 0.9335052 | 0.9335052 | 0.9335052 | 0.9335052 | 0.9335052 | 0.9335052 | 0.9335052 | 0.9335052 | 0.9291518 |
|  |  | 5 | 0.971205 | 0.9711415 | 0.9724253 | 0.9713595 | 0.9711347 | 0.9713116 | 0.9714544 | 0.9713961 | 0.9734346 |
|  |  | 8 | 0.9816942 | 0.9818422 | 0.9818438 | 0.9812145 | 0.9816557 | 0.9816419 | 0.9817693 | 0.9817147 | 0.9792358 |
|  |  | 10 | 0.9836498 | 0.9835151 | 0.9839184 | 0.9838088 | 0.9838458 | 0.9834957 | 0.9841798 | 0.9836209 | 0.9823904 |
|  | Otsu | 2 | 0.9441387 | 0.9441387 | 0.9441387 | 0.9441387 | 0.9441387 | 0.9441387 | 0.9441387 | 0.9441387 | 0.9440744 |
|  |  | 5 | 0.9775444 | 0.9775307 | 0.9777809 | 0.9776590 | 0.9778562 | 0.9773850 | 0.9778163 | 0.9777809 | 0.9772468 |
|  |  | 8 | 0.9832419 | 0.9840568 | 0.9836675 | 0.9841374 | 0.9838575 | 0.9835854 | 0.9832675 | 0.9834995 | 0.9823950 |
|  |  | 10 | 0.9853449 | 0.9855164 | 0.985329 | 0.9855252 | 0.9851840 | 0.9853058 | 0.9856893 | 0.9854580 | 0.9839688 |
| Image 3 | Kapur | 2 | 0.9111205 | 0.9111205 | 0.9111205 | 0.9111205 | 0.9111205 | 0.9111205 | 0.9111205 | 0.9111205 | 0.9128027 |
|  |  | 5 | 0.9310841 | 0.9320394 | 0.9339085 | 0.9370163 | 0.9318510 | 0.9293245 | 0.9331559 | 0.9351969 | 0.9300046 |
|  |  | 8 | 0.9663346 | 0.9649999 | 0.9650456 | 0.9648381 | 0.9665265 | 0.9635618 | 0.9632104 | 0.9644666 | 0.9584711 |
|  |  | 10 | 0.9680131 | 0.9682988 | 0.9683558 | 0.9687684 | 0.9679444 | 0.9692214 | 0.9686050 | 0.9680466 | 0.9674254 |
|  | Otsu | 2 | 0.9085145 | 0.9085145 | 0.9085145 | 0.9085145 | 0.9085145 | 0.9085145 | 0.9085145 | 0.9085145 | 0.9086484 |
|  |  | 5 | 0.9595404 | 0.9598124 | 0.9596954 | 0.9597562 | 0.9597562 | 0.9598261 | 0.9597341 | 0.9597562 | 0.9566119 |
|  |  | 8 | 0.9702900 | 0.9700872 | 0.9701775 | 0.9699262 | 0.9705375 | 0.9700931 | 0.9697596 | 0.9699806 | 0.9693644 |
|  |  | 10 | 0.9741403 | 0.9732780 | 0.9736777 | 0.9734191 | 0.9739932 | 0.9743388 | 0.9743474 | 0.9732717 | 0.9725623 |
| Image 4 | Kapur | 2 | 0.9307807 | 0.9307807 | 0.9307807 | 0.9307807 | 0.9307807 | 0.9307807 | 0.9307807 | 0.9307807 | 0.9323508 |
|  |  | 5 | 0.9671772 | 0.9659721 | 0.9655904 | 0.9665656 | 0.9671403 | 0.9673020 | 0.9670801 | 0.9658614 | 0.9654510 |
|  |  | 8 | 0.9782044 | 0.9760988 | 0.9787477 | 0.9763018 | 0.9785625 | 0.9777054 | 0.9794284 | 0.9778260 | 0.9756341 |
|  |  | 10 | 0.9806452 | 0.9804251 | 0.9797207 | 0.9791084 | 0.9798526 | 0.9793233 | 0.9790864 | 0.9800520 | 0.9789193 |
|  | Otsu | 2 | 0.9457497 | 0.9457497 | 0.9457497 | 0.9457497 | 0.9457497 | 0.9457497 | 0.9457497 | 0.9457497 | 0.9466141 |
|  |  | 5 | 0.9747321 | 0.9726784 | 0.9735348 | 0.9726290 | 0.9748935 | 0.9736714 | 0.9743312 | 0.9734442 | 0.9745284 |
|  |  | 8 | 0.9805452 | 0.9809622 | 0.9800648 | 0.9809254 | 0.9807647 | 0.9811282 | 0.9811564 | 0.9809844 | 0.9791631 |
|  |  | 10 | 0.9833113 | 0.9837541 | 0.9832399 | 0.9836989 | 0.9831646 | 0.9830735 | 0.9834571 | 0.9831194 | 0.9810584 |

In terms of BRISQUE values, ChOA gave such threshold values that the segmented images' BRISQUE values were best for the most test images.For $k=2,5,10$, segmented image 1 through ChOA generated threshold values using kapur's method gave the best BRISQUE scores. In case of Otsu's method, for $k=2,5$ best result was observed. In case of test image 2, best score was observed when $k=2$ using kapur's method and when $k=2,5$ using otsu's method. For test image 3 , when $k=2,8$ using kapur's method,
best BRISQUE score was given by the segmented image, and for otsu's method best BRISQUE score was observed when $k=2,8,10$. For test image 4, best BRISQUE score was when $k=2$, 5 using otsu's method and when $k=2$ kapur's method.

PIQE value was the lowest for test image 1 when $k=2,8$ using kapur's method. For test image 2, Lowest PIQE score was observed using otsu's method, when $k=5,8,10$ and when $k=2$ the result was same as other score. For test image 3, using the kapur's method best score was observed

Table 9 VOI values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | 7.7414537 | 7.7414537 | 7.7414537 | 7.7414537 | 7.7414537 | 7.7414537 | 7.7414537 | 7.7414537 | 7.7392359 |
|  |  | 5 | 7.6464127 | 7.6473644 | 7.6586971 | 7.6542860 | 7.6491390 | 7.6407346 | 7.6563863 | 7.6589395 | 7.6198831 |
|  |  | 8 | 7.3209785 | 7.2953370 | 7.2686000 | 7.2812488 | 7.3214487 | 7.3031276 | 7.2792588 | 7.3684446 | 7.3043113 |
|  |  | 10 | 7.0872033 | 7.1561476 | 7.0397532 | 7.1626582 | 7.1028853 | 7.0699888 | 7.1227961 | 7.1053111 | 7.1163711 |
|  | Otsu | 2 | 7.7454406 | 7.7454406 | 7.7454406 | 7.7454406 | 7.7454406 | 7.7454406 | 7.7454406 | 7.7454406 | 7.7384476 |
|  |  | 5 | 7.5359435 | 7.5208049 | 7.5207965 | 7.5196001 | 7.5327450 | 7.5109894 | 7.5078136 | 7.5196001 | 7.5586077 |
|  |  | 8 | 7.1565769 | 7.1989957 | 7.1756813 | 7.2162831 | 7.1735594 | 7.1704616 | 7.1565963 | 7.1508188 | 7.2519053 |
|  |  | 10 | 6.8640768 | 6.8314111 | 6.8897506 | 6.8419384 | 6.9388738 | 6.8066352 | 6.9008102 | NaN | 7.0459398 |
| Image 2 | Kapur | 2 | 7.8948613 | 7.8948613 | 7.8948613 | 7.8948613 | 7.8948613 | 7.8948613 | 7.8948613 | 7.8948613 | 7.882368 |
|  |  | 5 | 7.3635814 | 7.3520387 | 7.3433963 | 7.3400988 | 7.3620559 | 7.3503067 | 7.3505597 | 7.3348338 | 7.3475186 |
|  |  | 8 | 6.8739086 | 6.9013682 | 6.8810830 | 6.8584328 | 6.8710377 | 6.8697184 | 6.8928478 | 6.8759233 | 7.0089640 |
|  |  | 10 | 6.6894738 | 6.7292648 | 6.7076410 | 6.7193950 | 6.6864872 | 6.7205817 | 6.7448233 | 6.7156823 | 6.8161101 |
|  | Otsu | 2 | 7.7596360 | 7.7596360 | 7.7596360 | 7.7596360 | 7.7596360 | 7.7596360 | 7.7596360 | 7.7596360 | 7.7571894 |
|  |  | 5 | 7.2477956 | 7.2556980 | 7.2738335 | 7.2712954 | 7.2676890 | 7.2605806 | 7.2682256 | 7.2738335 | 7.2462195 |
|  |  | 8 | 6.8826767 | 6.9289199 | 6.9064509 | 6.9353297 | 6.8957024 | 6.9073685 | 6.8688403 | 6.9018369 | 6.9496651 |
|  |  | 10 | 6.6563287 | 6.6494782 | 6.6547930 | 6.6481812 | 6.6635680 | 6.6203637 | 6.6643406 | 6.6427772 | 6.7412509 |
| Image 3 | Kapur | 2 | 7.2418652 | 7.2418652 | 7.2418652 | 7.2418652 | 7.2418652 | 7.2418652 | 7.2418652 | 7.2418652 | 7.2486244 |
|  |  | 5 | 6.8934430 | 6.9236784 | 6.9468805 | 6.8870208 | 6.9618974 | 6.9548914 | 6.9256135 | 6.9443456 | 6.8818086 |
|  |  | 8 | 6.4523966 | 6.4471165 | 6.4335926 | 6.4597450 | 6.4347797 | 6.4693338 | 6.4547459 | 6.4502595 | 6.4652110 |
|  |  | 10 | 6.2466067 | 6.2667075 | 6.2403861 | 6.2393676 | 6.2480174 | 6.3146049 | 6.3083116 | 6.2519319 | 6.2919275 |
|  | Otsu | 2 | 7.2727034 | 7.2727034 | 7.2727034 | 7.2727034 | 7.2727034 | 7.2727034 | 7.2727034 | 7.2727034 | 7.2719195 |
|  |  | 5 | 6.5187494 | 6.5475902 | 6.5483656 | 6.5451919 | 6.5451919 | 6.5445444 | 6.5370799 | 6.5451919 | 6.6139727 |
|  |  | 8 | 6.2166216 | 6.2429659 | 6.2219199 | 6.2455054 | 6.2499061 | 6.2207273 | 6.1996692 | 6.2464193 | 6.2654107 |
|  |  | 10 | 5.9134495 | 5.9558019 | 5.9378976 | 5.9560140 | 5.9140732 | 5.9383446 | 5.8725698 | 5.9577600 | 6.0753521 |
| Image 4 | Kapur | 2 | 8.2033327 | 8.2033327 | 8.2033327 | 8.2033327 | 8.2033327 | 8.2033327 | 8.2033327 | 8.2033327 | 8.2225951 |
|  |  | 5 | 7.6615819 | 7.6410822 | 7.6319375 | 7.6499954 | 7.6485510 | 7.6689197 | 7.6510448 | 7.6252340 | 7.6301180 |
|  |  | 8 | 7.1798438 | 7.2404103 | 7.1640516 | 7.2128221 | 7.1962700 | 7.2066466 | 7.2040319 | 7.1886314 | 7.2833056 |
|  |  | 10 | 6.8815728 | 6.9812881 | 6.8304234 | 6.9186151 | 6.8609963 | 6.8567897 | 6.8379102 | 6.8771390 | 7.0486096 |
|  | Otsu | 2 | 7.9352456 | 7.9352456 | 7.9352456 | 7.9352456 | 7.9352456 | 7.9352456 | 7.9352456 | 7.9352456 | 7.9571057 |
|  |  | 5 | 7.4766521 | 7.4261800 | 7.4488390 | 7.4277320 | 7.4804995 | 7.4486894 | 7.4582465 | 7.4467283 | 7.4831069 |
|  |  | 8 | 6.9162132 | 6.8438346 | 6.9444255 | 6.8400796 | 6.9535993 | 6.8530490 | 6.8951099 | 6.8449935 | 7.0930089 |
|  |  | 10 | 6.7137583 | 6.6534381 | 6.7947227 | 6.6611856 | 6.7079663 | 6.6771988 | 6.6959007 | 6.6500289 | 6.8004151 |

when $k=8$, and for otsu's method the best result was given by the segmented image through ChOA generated set of threholds when $k=5,10$. For image 4, best result score was given by otsu's method when $k=2,5$.

In the case of NIQE value for test image 1, best result was observed when $k=2,10$ using kapur's method, but while using otsu's method, all the algorithm gave same result for $k=2$, and ChOA gave second best result when $k=10$. For test image 2, ChOA gave the best result when $k=2$ for kapur's method and when $k=5$ for otsu's method. For image 3, best result was observed when $k=5,10$ using otsu's method. For image 4 , when $k=8$, ChOA gave best result using kapur's method, and when $k=5$, ChOA gave best result using otsu's method.

### 7.7 Convergence curve

From Figs. 17, 18, 19, 20, 21, 22 and 23 represent the convergence curve of the all applied algorithms. ChOA shows sharp increasing rate when the threshold value is 2 and this behaviour was common for all the test image. As for higher threshold values ChOA showed almost flat line behaviour and other algorithms performed performed nicely in terms of convergence; however, ChOA gave maximum objective value even with poor convergence. When threhold value is low ChOA performed consistently, giving the best results in terms of objective function value (Fig. 24).

Table 10 PSNR values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | 28.440419 | 28.440419 | 28.440419 | 28.440419 | 28.440419 | 28.440419 | 28.440419 | 28.440419 | 28.452249 |
|  |  | 5 | 32.351433 | 32.400800 | 32.292423 | 32.281401 | 32.359172 | 32.413187 | 32.272944 | 32.319795 | 32.660504 |
|  |  | 8 | 35.722752 | 35.702646 | 35.908669 | 35.757708 | 35.803129 | 35.709419 | 35.774554 | 35.846677 | 35.425915 |
|  |  | 10 | 37.127203 | 37.179786 | 37.218245 | 37.130356 | 37.132836 | 37.228318 | 37.102577 | 37.210059 | 36.209800 |
|  | Otsu | 2 | 28.123691 | 28.123691 | 28.123691 | 28.123691 | 28.123691 | 28.123691 | 28.123691 | 28.123691 | 28.113286 |
|  |  | 5 | 33.337560 | 33.319674 | 33.317595 | 33.316819 | 33.328843 | 33.316702 | 33.325509 | 33.316819 | 33.239077 |
|  |  | 8 | 36.708543 | 36.658679 | 36.675625 | 36.649052 | 36.724064 | 36.683214 | 36.709888 | 36.725963 | 35.657104 |
|  |  | 10 | 38.150669 | 38.278731 | 38.151941 | 38.303141 | 38.203479 | 38.149190 | 38.212074 | NaN | 36.508223 |
| Image 2 | Kapur | 2 | 25.857437 | 25.857437 | 25.857437 | 25.857437 | 25.857437 | 25.857437 | 25.857437 | 25.857437 | 25.824765 |
|  |  | 5 | 31.829167 | 31.913280 | 32.007579 | 31.993688 | 31.834822 | 31.928337 | 31.920072 | 31.979089 | 32.180175 |
|  |  | 8 | 36.232772 | 36.133439 | 36.302014 | 36.186282 | 36.224685 | 36.223779 | 36.173569 | 36.205566 | 34.819399 |
|  |  | 10 | 37.348654 | 37.530843 | 37.530000 | 37.533199 | 37.331486 | 37.535321 | 37.520433 | 37.473257 | 35.746845 |
|  | Otsu | 2 | 26.519673 | 26.519673 | 26.519673 | 26.519673 | 26.519673 | 26.519673 | 26.519673 | 26.519673 | 26.535550 |
|  |  | 5 | 33.007137 | 33.002360 | 33.009911 | 33.004080 | 33.026311 | 33.003262 | 33.014204 | 33.009911 | 32.771950 |
|  |  | 8 | 36.182207 | 36.227699 | 36.173640 | 36.169374 | 36.292544 | 36.176238 | 36.134697 | 36.157687 | 35.596727 |
|  |  | 10 | 37.998159 | 37.977712 | 37.987644 | 37.978985 | 37.909767 | 38.035465 | 38.052298 | 37.971090 | 36.592628 |
| Image 3 | Kapur | 2 | 27.238564 | 27.238564 | 27.238564 | 27.238564 | 27.238564 | 27.238564 | 27.238564 | 27.238564 | 27.271631 |
|  |  | 5 | 32.200322 | 32.081054 | 32.127274 | 32.484471 | 31.933075 | 31.818954 | 32.159671 | 32.211432 | 31.907360 |
|  |  | 8 | 36.913962 | 36.750383 | 36.848534 | 36.701875 | 36.966275 | 36.515399 | 36.558050 | 36.777986 | 35.962618 |
|  |  | 10 | 37.954458 | 37.837659 | 38.053994 | 38.009902 | 37.942377 | 37.879142 | 37.896664 | 37.893732 | 37.921900 |
|  | Otsu | 2 | 28.608519 | 28.608519 | 28.608519 | 28.608519 | 28.608519 | 28.608519 | 28.608519 | 28.608519 | 28.623584 |
|  |  | 5 | 35.201047 | 35.180165 | 35.171299 | 35.177109 | 35.177109 | 35.190577 | 35.183305 | 35.177109 | 34.640436 |
|  |  | 8 | 37.604194 | 37.596324 | 37.604888 | 37.569438 | 37.587983 | 37.597968 | 37.601087 | 37.566961 | 37.726866 |
|  |  | 10 | 38.975646 | 38.965201 | 39.059186 | 38.949959 | 38.982014 | 38.936565 | 39.109834 | 38.933496 | 39.102334 |
| Image 4 | Kapur | 2 | 25.827964 | 25.827964 | 25.827964 | 25.827964 | 25.827964 | 25.827964 | 25.827964 | 25.827964 | 25.828374 |
|  |  | 5 | 32.861925 | 32.809276 | 32.804067 | 32.839241 | 32.867054 | 32.865091 | 32.867840 | 32.820803 | 32.579941 |
|  |  | 8 | 36.641179 | 36.331353 | 36.695096 | 36.399663 | 36.650502 | 36.525197 | 36.655586 | 36.573710 | 35.870206 |
|  |  | 10 | 38.186096 | 37.946014 | 38.303392 | 38.033067 | 38.182733 | 38.215559 | 38.276485 | 38.208637 | 37.193032 |
|  | Otsu | 2 | 27.069915 | 27.069915 | 27.069915 | 27.069915 | 27.069915 | 27.069915 | 27.069915 | 27.069915 | 27.073884 |
|  |  | 5 | 33.894314 | 34.078302 | 34.001326 | 34.081949 | 33.880391 | 33.989084 | 33.933373 | 34.009388 | 33.615425 |
|  |  | 8 | 37.544554 | 37.664917 | 37.504057 | 37.662937 | 37.496286 | 37.638538 | 37.615286 | 37.666288 | 36.861737 |
|  |  | 10 | 39.072244 | 39.045143 | 39.007044 | 38.981624 | 39.084399 | 39.118601 | 39.129383 | 38.920229 | 38.472067 |

### 7.8 Observation and summary

Observing all the parameters, ChOA didn't give best results consistently. For higher threshold the algorithm gave almost flat line convergence curve. When threshold is 2 , the algorithm's convergence curve had a sharp increment towards the global optimum. The possible reason could be the entrapment of search agents of ChOA by multi-modal search space rising from higher threshold values. Even in the original work of ChOA, it was observed that ChOA performed relatively poor in some of the multi-modal functions. This issue
can be solved by using other versions of ChOA that employs different chaotic map to diversify search agents.In Houssein et al. (2021), authors used Levy flight to improve algorithm efficiency. There can be other ways to improve ChOA.

In case of objective function, the used algorithm to implement the Kapur's function and Otsu's function can be modified to give better results. Since stochastic algorithm generates random search agents, it doesn't always generate discrete and ascending threshold values that can be evaluated by either Kapur's or Otsu's function. Kapur's and Otsu's function can only take discrete and ascending

Table 11 FSIM values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | 0.840559 | 0.840559 | 0.840559 | 0.840559 | 0.840559 | 0.840559 | 0.840559 | 0.840559 | 0.840585 |
|  |  | 5 | 0.920810 | 0.920489 | 0.921740 | 0.921506 | 0.920802 | 0.920466 | 0.921496 | 0.921822 | 0.922871 |
|  |  | 8 | 0.956185 | 0.956611 | 0.958265 | 0.957139 | 0.957226 | 0.956513 | 0.957194 | 0.957968 | 0.955393 |
|  |  | 10 | 0.967603 | 0.967897 | 0.968163 | 0.967937 | 0.967688 | 0.968179 | 0.967967 | 0.968330 | 0.964482 |
|  | Otsu | 2 | 0.842626 | 0.842626 | 0.842626 | 0.842626 | 0.842626 | 0.842626 | 0.842626 | 0.842626 | 0.842780 |
|  |  | 5 | 0.930398 | 0.930382 | 0.930389 | 0.930392 | 0.930353 | 0.930403 | 0.930381 | 0.930392 | 0.925230 |
|  |  | 8 | 0.961796 | 0.961615 | 0.961596 | 0.961441 | 0.961574 | 0.961678 | 0.961959 | 0.962526 | 0.954122 |
|  |  | 10 | 0.972135 | 0.972140 | 0.971904 | 0.972694 | 0.972774 | 0.971812 | 0.972286 | NaN | 0.962240 |
| Image 2 | Kapur | 2 | 0.770299 | 0.770299 | 0.770299 | 0.770299 | 0.770299 | 0.770299 | 0.770299 | 0.770299 | 0.769619 |
|  |  | 5 | 0.857914 | 0.858560 | 0.860277 | 0.859594 | 0.857929 | 0.858511 | 0.858847 | 0.859447 | 0.863357 |
|  |  | 8 | 0.914322 | 0.9143504 | 0.916417 | 0.914266 | 0.914216 | 0.914366 | 0.915251 | 0.914788 | 0.906757 |
|  |  | 10 | 0.931493 | 0.931609 | 0.932380 | 0.931393 | 0.931270 | 0.931313 | 0.931200 | 0.931356 | 0.9226307 |
|  | Otsu | 2 | 0.774892 | 0.774892 | 0.774892 | 0.774892 | 0.774892 | 0.774892 | 0.774892 | 0.774892 | 0.774767 |
|  |  | 5 | 0.874577 | 0.874794 | 0.874762 | 0.874809 | 0.874543 | 0.874779 | 0.874724 | 0.874762 | 0.871927 |
|  |  | 8 | 0.914904 | 0.915005 | 0.914990 | 0.914877 | 0.916857 | 0.915032 | 0.914741 | 0.915427 | 0.913923 |
|  |  | 10 | 0.935913 | 0.933419 | 0.934923 | 0.933248 | 0.935793 | 0.936358 | 0.935601 | 0.933554 | 0.928870 |
| Image 3 | Kapur | 2 | 0.822938 | 0.822938 | 0.822938 | 0.822938 | 0.822938 | 0.822938 | 0.822938 | 0.822938 | 0.823001 |
|  |  | 5 | 0.896473 | 0.895169 | 0.895499 | 0.899030 | 0.894081 | 0.892958 | 0.897964 | 0.897028 | 0.894255 |
|  |  | 8 | 0.944715 | 0.943191 | 0.944140 | 0.942881 | 0.945533 | 0.940668 | 0.940966 | 0.943038 | 0.935226 |
|  |  | 10 | 0.954399 | 0.953651 | 0.953879 | 0.954447 | 0.954414 | 0.953765 | 0.953443 | 0.952818 | 0.949903 |
|  | Otsu | 2 | 0.826202 | 0.826202 | 0.826202 | 0.826202 | 0.826202 | 0.826202 | 0.826202 | 0.826202 | 0.826305 |
|  |  | 5 | 0.926220 | 0.925754 | 0.925606 | 0.925764 | 0.925764 | 0.925781 | 0.925963 | 0.925764 | 0.920650 |
|  |  | 8 | 0.950123 | 0.949262 | 0.949465 | 0.949070 | 0.949579 | 0.949730 | 0.949622 | 0.949099 | 0.949689 |
|  |  | 10 | 0.961428 | 0.961404 | 0.961159 | 0.961271 | 0.961952 | 0.960784 | 0.962236 | 0.961474 | 0.960805 |
| Image 4 | Kapur | 2 | 0.789832 | 0.789832 | 0.789832 | 0.789832 | 0.789832 | 0.789832 | 0.789832 | 0.789832 | 0.789598 |
|  |  | 5 | 0.909151 | 0.908696 | 0.908999 | 0.908971 | 0.909365 | 0.908996 | 0.909382 | 0.908718 | 0.904972 |
|  |  | 8 | 0.945327 | 0.943294 | 0.945280 | 0.943423 | 0.944913 | 0.944275 | 0.944578 | 0.944375 | 0.939712 |
|  |  | 10 | 0.958685 | 0.957340 | 0.9593667 | 0.957810 | 0.958701 | 0.959220 | 0.959387 | 0.958811 | 0.952971 |
|  | Otsu | 2 | 0.830418 | 0.830418 | 0.830418 | 0.830418 | 0.830418 | 0.830418 | 0.830418 | 0.830418 | 0.830283 |
|  |  | 5 | 0.919870 | 0.921300 | 0.920723 | 0.921355 | 0.919776 | 0.920561 | 0.920125 | 0.920786 | 0.915629 |
|  |  | 8 | 0.955408 | 0.956310 | 0.955097 | 0.956294 | 0.954843 | 0.956447 | 0.955812 | 0.956305 | 0.947662 |
|  |  | 10 | 0.965971 | 0.965944 | 0.964779 | 0.965613 | 0.965779 | 0.966354 | 0.966469 | 0.965426 | 0.961469 |

set of threshold values to evaluate the objective function. So, when an stochastic algorithm generates any value that is not in ascending order the kapur's and Otsu's currently implemented method gives Zero as result, and there is no method implemented in ChOA to generate only ascending set of threshold values. As a results, many iterations are wasted in generating zero as objective value, but due to exiting cognisant component in the algorithm, the algorithm can
generate ascending threshold values after many iterations. So, one improvement can be to make ChOA cognisant in generating only ascending order values.

Another issue in ChOA is that it is a continuous algorithm. So, it can generate any threshold values between $[0,255]$. In current method, solution set is rounded to generate discrete values. This method is inefficient because many iterations are wasted in generating different decimal values,

Table 12 SSIM Values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | 0.7918196 | 0.7918196 | 0.7918196 | 0.7918196 | 0.7918196 | 0.7918196 | 0.7918196 | 0.7918196 | 0.7916691 |
|  |  | 5 | 0.8515985 | 0.8515301 | 0.8521869 | 0.8520201 | 0.8516498 | 0.8515387 | 0.8519308 | 0.8522966 | 0.8542401 |
|  |  | 8 | 0.8909610 | 0.8901224 | 0.8925359 | 0.8910390 | 0.8915917 | 0.8902823 | 0.8914495 | 0.8917443 | 0.8880165 |
|  |  | 10 | 0.9064684 | 0.9061279 | 0.9069916 | 0.9060128 | 0.9063522 | 0.9068684 | 0.9061212 | 0.9070064 | 0.9000728 |
|  | Otsu | 2 | 0.7943324 | 0.7943324 | 0.7943324 | 0.7943324 | 0.7943324 | 0.7943324 | 0.7943324 | 0.7943324 | 0.7943536 |
|  |  | 5 | 0.8697263 | 0.8698344 | 0.8698296 | 0.8698380 | 0.8697111 | 0.8698738 | 0.8698589 | 0.8698380 | 0.8631996 |
|  |  | 8 | 0.9024935 | 0.9032744 | 0.9026491 | 0.9031359 | 0.9022195 | 0.9031444 | 0.9029160 | 0.9037240 | 0.8920301 |
|  |  | 10 | 0.9183362 | 0.9206070 | 0.9178337 | 0.9204159 | 0.9177207 | 0.9179366 | 0.9178194 | NaN | 0.9033850 |
| Image 2 | Kapur | 2 | 0.7381052 | 0.7381052 | 0.7381052 | 0.7381052 | 0.7381052 | 0.7381052 | 0.7381052 | 0.7381052 | 0.7374410 |
|  |  | 5 | 0.8316037 | 0.8329436 | 0.8336456 | 0.8339786 | 0.8317861 | 0.8331025 | 0.8328995 | 0.8336116 | 0.8368826 |
|  |  | 8 | 0.8948718 | 0.8943560 | 0.8963653 | 0.8948223 | 0.8953343 | 0.8950658 | 0.895129 | 0.8949714 | 0.8803619 |
|  |  | 10 | 0.9085048 | 0.9108405 | 0.9104283 | 0.9106738 | 0.9084714 | 0.9120375 | 0.9103258 | 0.9097330 | 0.8982321 |
|  | Otsu | 2 | 0.7494828 | 0.7494828 | 0.7494828 | 0.7494828 | 0.7494828 | 0.7494828 | 0.7494828 | 0.7494828 | 0.7493831 |
|  |  | 5 | 0.8545080 | 0.8545495 | 0.8544388 | 0.8544629 | 0.8542291 | 0.8544344 | 0.8544506 | 0.8544388 | 0.8476260 |
|  |  | 8 | 0.8968954 | 0.8985209 | 0.8974504 | 0.8984323 | 0.8973888 | 0.8986785 | 0.8968397 | 0.8971918 | 0.890594 |
|  |  | 10 | 0.9175194 | 0.9166383 | 0.9166181 | 0.9164011 | 0.9164443 | 0.9182397 | 0.9174849 | 0.9161740 | 0.9060393 |
| Image 3 | Kapur | 2 | 0.8260656 | 0.8260656 | 0.8260656 | 0.8260656 | 0.8260656 | 0.8260656 | 0.8260656 | 0.8260656 | 0.8261581 |
|  |  | 5 | 0.8902364 | 0.8898632 | 0.8903845 | 0.8938270 | 0.8887642 | 0.8876132 | 0.8907992 | 0.8915735 | 0.8883194 |
|  |  | 8 | 0.9331523 | 0.9314820 | 0.9330983 | 0.9315839 | 0.9344141 | 0.9300816 | 0.9298874 | 0.9320946 | 0.9231071 |
|  |  | 10 | 0.9426619 | 0.9410390 | 0.9426921 | 0.9423984 | 0.9425457 | 0.9411709 | 0.9412509 | 0.9406771 | 0.9367924 |
|  | Otsu | 2 | 0.8316937 | 0.8316937 | 0.8316937 | 0.8316937 | 0.8316937 | 0.8316937 | 0.8316937 | 0.8316937 | 0.8317416 |
|  |  | 5 | 0.9227556 | 0.9222944 | 0.9222069 | 0.9222840 | 0.9222840 | 0.9223567 | 0.9224754 | 0.9222840 | 0.9165334 |
|  |  | 8 | 0.9446697 | 0.9440481 | 0.9444181 | 0.9438437 | 0.9442943 | 0.9444317 | 0.9446580 | 0.9438648 | 0.9406071 |
|  |  | 10 | 0.9560552 | 0.9554046 | 0.9553085 | 0.9554416 | 0.9558450 | 0.9557022 | 0.9569164 | 0.9554424 | 0.9508221 |
| Image 4 | Kapur | 2 | 0.7724818 | 0.7724818 | 0.7724818 | 0.7724818 | 0.7724818 | 0.7724818 | 0.7724818 | 0.7724818 | 0.7722685 |
|  |  | 5 | 0.8950666 | 0.8947921 | 0.8950790 | 0.8952765 | 0.8952010 | 0.8951351 | 0.8952332 | 0.8947384 | 0.8916416 |
|  |  | 8 | 0.9291307 | 0.9276792 | 0.9288186 | 0.9276195 | 0.9287985 | 0.9282517 | 0.9280903 | 0.9284786 | 0.9244445 |
|  |  | 10 | 0.9440305 | 0.9420389 | 0.9449645 | 0.9427996 | 0.9441784 | 0.9446729 | 0.9451792 | 0.9441357 | 0.9367905 |
|  | Otsu | 2 | 0.8365728 | 0.8365728 | 0.8365728 | 0.8365728 | 0.8365728 | 0.8365728 | 0.8365728 | 0.8365728 | 0.8365128 |
|  |  | 5 | 0.9058635 | 0.9069077 | 0.9064874 | 0.9069540 | 0.9057876 | 0.9063778 | 0.9061099 | 0.9065341 | 0.9025555 |
|  |  | 8 | 0.9412635 | 0.9424368 | 0.9408417 | 0.9424116 | 0.9405580 | 0.9424614 | 0.9419765 | 0.9424334 | 0.9323812 |
|  |  | 10 | 0.9516377 | 0.9521257 | 0.9507344 | 0.9518093 | 0.9515765 | 0.9521749 | 0.9520560 | 0.9516390 | 0.9465455 |

but all of those are useless because after generation of such values all are being rounded up. So, in summary, the cognisant component of algorithm wastes iteration on finding precise decimal values. So, efficiency can be improved if ChOA can only generate discrete values for solution. This can be done by making a Binary version of ChOA. Binary
algorithm in multi-level thresholding was implemented in Djerou et al. (2009)

The computational time of the whole program can be reduced significantly using fast recursive segmentation algorithm (Kiani et al. 2009).

Table 13 BRISQUE Values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | 53.621232 | 53.621232 | 53.621232 | 53.621232 | 53.621232 | 53.621232 | 53.621232 | 53.621232 | 53.461269 |
|  |  | 5 | 48.399142 | 48.038926 | 48.227661 | 48.227661 | 48.107758 | 48.107758 | 48.227661 | 48.227661 | 47.354246 |
|  |  | 8 | 46.766363 | 47.003490 | 45.715101 | 47.003490 | 45.495538 | 46.504801 | 46.701251 | 45.093831 | 46.809605 |
|  |  | 10 | 43.852158 | 44.924561 | 43.064319 | 45.114398 | 45.239352 | 44.553634 | 45.638469 | 44.918923 | 42.422688 |
|  | Otsu | 2 | 53.089912 | 53.089912 | 53.089912 | 53.089912 | 53.089912 | 53.089912 | 53.089912 | 53.089912 | 53.089912 |
|  |  | 5 | 47.681770 | 47.767186 | 47.748683 | 47.748683 | 47.767186 | 47.744132 | 47.748683 | 47.748683 | 46.745034 |
|  |  | 8 | 44.412728 | 46.025417 | 46.188126 | 46.184392 | 44.963372 | 44.505551 | 44.209560 | 44.306356 | 46.721979 |
|  |  | 10 | 42.655581 | 42.699412 | 42.757367 | 42.605971 | 42.409884 | 42.781425 | 42.502356 | NaN | 43.547966 |
| Image 2 | Kapur | 2 | 53.744095 | 53.744095 | 53.744095 | 53.744095 | 53.744095 | 53.744095 | 53.744095 | 53.744095 | 53.363598 |
|  |  | 5 | 49.376413 | 49.349576 | 47.473984 | 49.376413 | 49.376413 | 49.884907 | 49.376413 | 49.591822 | 50.005100 |
|  |  | 8 | 44.638258 | 44.488551 | 43.981701 | 44.599148 | 44.237874 | 44.544333 | 44.541907 | 43.849820 | 44.188143 |
|  |  | 10 | 42.937088 | 43.101586 | 42.620880 | 41.916158 | 41.932326 | 42.922646 | 44.068029 | 42.707416 | 43.420969 |
|  | Otsu | 2 | 52.976313 | 52.976313 | 52.976313 | 52.976313 | 52.976313 | 52.976313 | 52.976313 | 52.976313 | 52.976313 |
|  |  | 5 | 46.224601 | 46.237927 | 46.280826 | 46.280826 | 46.280826 | 46.224601 | 46.280826 | 46.524064 | 45.096439 |
|  |  | 8 | 43.562668 | 43.952136 | 43.933452 | 43.852208 | 42.644095 | 43.772070 | 43.119901 | 43.994197 | 43.652669 |
|  |  | 10 | 41.944597 | 42.342318 | 42.966887 | 42.471998 | 42.642062 | 41.676957 | 43.942745 | 42.600163 | 43.332645 |
| Image 3 | Kapur | 2 | 49.115084 | 49.115084 | 49.115084 | 49.115084 | 49.115084 | 49.115084 | 49.115084 | 49.115084 | 49.115084 |
|  |  | 5 | 45.142081 | 43.661876 | 48.542706 | 43.239438 | 43.654126 | 43.582539 | 48.335490 | 43.654126 | 49.220157 |
|  |  | 8 | 48.118491 | 47.624803 | 48.415016 | 47.305845 | 47.965350 | 49.344652 | 48.116079 | 48.064481 | 47.266019 |
|  |  | 10 | 47.750451 | 47.353671 | 47.373715 | 47.746143 | 47.323979 | 47.906879 | 48.046371 | 47.464224 | 48.618302 |
|  | Otsu | 2 | 51.592703 | 51.592703 | 51.592703 | 51.592703 | 51.592703 | 51.592703 | 51.592703 | 51.592703 | 51.561485 |
|  |  | 5 | 49.998673 | 50.050136 | 50.090989 | 50.090989 | 50.090989 | 50.090989 | 50.090989 | 50.090989 | 49.581261 |
|  |  | 8 | 48.767788 | 48.542366 | 48.651871 | 48.455135 | 48.731072 | 48.941247 | 48.412035 | 48.455135 | 48.914361 |
|  |  | 10 | 44.970710 | 46.492298 | 46.349024 | 46.104870 | 45.683070 | 46.382987 | 44.958708 | 45.918083 | 44.916714 |
| Image 4 | Kapur | 2 | 51.814695 | 51.814695 | 51.814695 | 51.814695 | 51.814695 | 51.814695 | 51.814695 | 51.814695 | 51.814695 |
|  |  | 5 | 45.359126 | 45.579581 | 45.437545 | 45.326340 | 45.488929 | 45.488929 | 45.488929 | 45.425273 | 46.370587 |
|  |  | 8 | 42.879882 | 43.895046 | 43.089536 | 43.496135 | 42.700859 | 42.677284 | 42.698178 | 43.676720 | 42.815786 |
|  |  | 10 | 42.025559 | 41.917361 | 41.932548 | 41.849512 | 42.462290 | 41.952950 | 42.009516 | 41.958266 | 42.050140 |
|  | Otsu | 2 | 46.994321 | 46.994321 | 46.994321 | 46.994321 | 46.994321 | 46.994321 | 46.994321 | 46.994321 | 46.829640 |
|  |  | 5 | 45.377122 | 45.308196 | 45.308196 | 45.308196 | 45.377122 | 45.261731 | 45.377122 | 45.308196 | 44.812601 |
|  |  | 8 | 42.303135 | 42.467727 | 42.303986 | 42.467727 | 42.043004 | 42.286388 | 42.296964 | 42.467727 | 42.630137 |
|  |  | 10 | 41.618813 | 41.798283 | 41.460606 | 41.809775 | 42.306550 | 42.066605 | 42.309135 | 41.202211 | 41.650446 |

## 8 Conclusion

This work details the efficiency and performance of the Chimp Optimization Algorithm in image clustering, which is accomplished using multilevel thresholding. The results denote effectiveness of ChOA in the following application.

ChOA, like most other metaheuristic algorithms, provides appropriate threshold values for each color channel of an RGB image by maximizing the Kapur's entropy function and Otsu's class variance function to generate image clusters. It appeared as a comparatively good algorithm in terms of its performance in image clustering, but this algorithm has

Table 14 PIQE Values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | 84.069403 | 84.069403 | 84.069403 | 84.069403 | 84.069403 | 84.069403 | 84.069403 | 84.069403 | 83.970519 |
|  |  | 5 | 79.271978 | 79.361424 | 79.194809 | 79.194809 | 79.471779 | 79.471779 | 79.194809 | 79.194809 | 79.307642 |
|  |  | 8 | 76.692983 | 77.139599 | 77.028845 | 77.139599 | 76.358350 | 76.262309 | 77.031903 | 76.421931 | 75.694658 |
|  |  | 10 | 73.913909 | 75.227705 | 72.047464 | 74.561676 | 74.519471 | 75.244528 | 75.796042 | 74.161480 | 75.581571 |
|  | Otsu | 2 | 84.594611 | 84.594611 | 84.594611 | 84.594611 | 84.594611 | 84.594611 | 84.594611 | 84.594611 | 84.594611 |
|  |  | 5 | 78.854402 | 79.440858 | 79.462360 | 79.462360 | 79.440858 | 79.162742 | 79.462360 | 79.462360 | 79.840960 |
|  |  | 8 | 75.922614 | 75.787572 | 75.431440 | 75.706442 | 75.555729 | 74.362837 | 74.227601 | 74.173920 | 77.038554 |
|  |  | 10 | 72.606767 | 71.875219 | 73.657577 | 73.063446 | 71.855961 | 73.147550 | 71.624828 | NaN | 73.250089 |
| Image 2 | Kapur | 2 | 82.976454 | 82.976454 | 82.976454 | 82.976454 | 82.976454 | 82.976454 | 82.976454 | 82.976454 | 84.025259 |
|  |  | 5 | 82.289071 | 82.371697 | 82.383127 | 82.289071 | 82.289071 | 83.123606 | 82.289071 | 82.996455 | 82.485613 |
|  |  | 8 | 78.445970 | 79.615300 | 77.518025 | 78.120845 | 78.036568 | 78.089644 | 80.542365 | 79.792383 | 76.790092 |
|  |  | 10 | 75.723473 | 76.082870 | 75.265179 | 75.463102 | 78.047920 | 73.992252 | 77.214337 | 76.339110 | 75.441784 |
|  | Otsu | 2 | 85.190165 | 85.190165 | 85.190165 | 85.190165 | 85.190165 | 85.190165 | 85.190165 | 85.190165 | 85.190165 |
|  |  | 5 | 83.898181 | 83.878921 | 83.091099 | 83.091099 | 83.091099 | 83.898181 | 83.091099 | 80.619413 | 79.080217 |
|  |  | 8 | 77.918011 | 76.371845 | 76.267562 | 76.594999 | 81.147527 | 76.892436 | 78.087414 | 75.127219 | 74.974852 |
|  |  | 10 | 77.422758 | 76.339474 | 76.970718 | 78.599004 | 78.033361 | 75.725783 | 78.888245 | 78.068736 | 74.501565 |
| Image 3 | Kapur | 2 | 83.298082 | 83.298082 | 83.298082 | 83.298082 | 83.298082 | 83.298082 | 83.298082 | 83.298082 | 83.298082 |
|  |  | 5 | 80.076455 | 79.961155 | 79.651000 | 79.083577 | 79.946206 | 79.677668 | 79.975990 | 79.946206 | 80.599417 |
|  |  | 8 | 79.218795 | 79.203657 | 78.950823 | 79.383494 | 78.894796 | 77.853477 | 79.216928 | 79.164179 | 78.630666 |
|  |  | 10 | 77.510763 | 79.055467 | 77.848400 | 77.585597 | 78.637234 | 77.755724 | 77.304581 | 78.229627 | 77.787952 |
|  | Otsu | 2 | 82.801871 | 82.801871 | 82.801871 | 82.801871 | 82.801871 | 82.801871 | 82.801871 | 82.801871 | 82.795508 |
|  |  | 5 | 78.813608 | 79.009382 | 78.821801 | 78.821801 | 78.821801 | 78.821801 | 78.821801 | 78.821801 | 80.166419 |
|  |  | 8 | 76.423727 | 77.501118 | 77.460440 | 77.230554 | 77.881480 | 76.528798 | 76.274886 | 77.230554 | 79.249595 |
|  |  | 10 | 77.083338 | 76.635097 | 77.466857 | 76.998507 | 75.154058 | 76.045796 | 78.017429 | 76.760354 | 78.758977 |
| Image 4 | Kapur | 2 | 78.100314 | 78.100314 | 78.100314 | 78.100314 | 78.100314 | 78.100314 | 78.100314 | 78.100314 | 78.100314 |
|  |  | 5 | 75.909814 | 76.042515 | 76.085644 | 76.134706 | 76.201580 | 76.201580 | 76.201580 | 76.741091 | 79.221426 |
|  |  | 8 | 69.894840 | 69.974942 | 71.949848 | 67.677496 | 70.562302 | 71.018802 | 71.388941 | 70.037700 | 70.255357 |
|  |  | 10 | 68.706228 | 65.667785 | 66.289437 | 67.162749 | 67.578108 | 67.306149 | 67.196939 | 67.061353 | 66.216111 |
|  | Otsu | 2 | 82.161905 | 82.161905 | 82.161905 | 82.161905 | 82.161905 | 82.161905 | 82.161905 | 82.161905 | 81.657816 |
|  |  | 5 | 74.781423 | 71.692465 | 71.692465 | 71.692465 | 74.781423 | 71.694488 | 74.781423 | 71.692465 | 70.391586 |
|  |  | 8 | 67.428402 | 67.348063 | 66.820822 | 67.348063 | 68.891963 | 66.055139 | 67.256012 | 67.348063 | 70.289545 |
|  |  | 10 | 63.888869 | 65.545047 | 66.062033 | 65.750524 | 64.710628 | 66.505048 | 65.774101 | 65.975582 | 66.809983 |

showed limitations in terms of converging in higher value of threshold. Even with such limitation ChOA didn't deviate from the best result given by other algorithms. So, some adjustment can improve this potential algorithm to outperform all algorithms in this application. One such improvement can be done in improving the convergence of ChOA in image threhsolding and improving the exploration of ChOA such that search agents don't get trapped in local optimum
point in image thresholding application. Keeping this as a springboard of subsequent research, Chimp Optimization Algorithm can be regarded as a vital tool in image processing tasks that requires image clustering and multilevel thresholding based techniques, which may extensively used in fields like: Medical imaging, disease detection, Satelite imaging, underwater image segmentation, agricultar sector and so on. The strength of this algorithm is its ability to

Table 15 NIQE Values

|  |  | K | PSO | WOA | SSA | HHO | MFO | GWO | AOA | AVOA | ChOA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Image 1 | Kapur | 2 | 12.690589 | 12.690589 | 12.690589 | 12.690589 | 12.690589 | 12.690589 | 12.690589 | 12.690589 | 12.605161 |
|  |  | 5 | 8.431372 | 8.474302 | 8.416693 | 8.416693 | 8.487638 | 8.487638 | 8.416693 | 8.416693 | 9.554108 |
|  |  | 8 | 7.599817 | 7.414079 | 7.344207 | 7.414079 | 7.375476 | 7.832244 | 7.784895 | 7.541709 | 7.537691 |
|  |  | 10 | 7.298654 | 7.180083 | 7.531204 | 7.306799 | 7.195615 | 7.322891 | 7.022125 | 7.324398 | 6.380568 |
|  | Otsu | 2 | 11.015396 | 11.015396 | 11.015396 | 11.015396 | 11.015396 | 11.015396 | 11.015396 | 11.015396 | 11.015396 |
|  |  | 5 | 9.277213 | 9.158389 | 9.156650 | 9.156650 | 9.158389 | 9.155717 | 9.156650 | 9.156650 | 9.412136 |
|  |  | 8 | 8.018206 | 7.897808 | 8.075584 | 7.914684 | 7.787260 | 7.338613 | 7.702348 | 7.584185 | 7.938624 |
|  |  | 10 | 7.232905 | 7.588708 | 7.669821 | 7.373784 | 7.921728 | 7.880181 | 7.573669 | NaN | 7.2928538 |
| Image 2 | Kapur | 2 | 16.600981 | 16.600981 | 16.600981 | 16.600981 | 16.600981 | 16.600981 | 16.600981 | 16.600981 | 17.076540 |
|  |  | 5 | 15.568347 | $15.318708$ | 14.927598 | 15.568347 | 15.568347 | 15.119358 | 15.568347 | 15.147642 | 14.670107 |
|  |  | 8 | 13.624276 | 13.819721 | 13.612558 | 13.309971 | 13.012649 | 12.875449 | 13.353471 | 13.650584 | 13.858738 |
|  |  | 10 | 12.582878 | 11.967544 | 12.896179 | 12.926069 | 12.418457 | 11.903346 | 12.379177 | 12.320520 | 11.980013 |
|  | Otsu | 2 | 18.246331 | 18.246331 | 18.246331 | 18.246331 | 18.246331 | 18.246331 | 18.246331 | 18.246331 | 18.246331 |
|  |  | 5 | 15.362327 | 15.584403 | 15.153128 | 15.153128 | 15.153128 | 15.362327 | 15.153128 | 15.154227 | 15.116049 |
|  |  | 8 | 12.685410 | 12.721154 | 12.823890 | 13.016140 | 13.025352 | 12.630501 | 12.055146 | 12.744823 | 12.697156 |
|  |  | 10 | 11.710033 | 12.358268 | 12.377702 | 12.49515 | 11.812346 | 11.855017 | 12.037243 | 12.294211 | 11.945242 |
| Image 3 | Kapur | 2 | 13.221289 | 13.221289 | 13.221289 | 13.221289 | 13.221289 | 13.221289 | 13.221289 | 13.221289 | 13.221289 |
|  |  | 5 | 10.835557 | 11.945607 | 9.679653 | 10.58388 | 11.953600 | 11.947049 | 10.69437 | 11.953600 | 10.956103 |
|  |  | 8 | 10.827368 | 10.772011 | 10.041925 | 10.551097 | 10.232425 | 10.099727 | 10.908308 | 10.924787 | 11.166871 |
|  |  | 10 | 9.679320 | 10.127578 | 9.884964 | 10.065292 | 9.875765 | 9.709259 | 9.463496 | 9.998562 | 10.754164 |
|  | Otsu | 2 | 13.467866 | 13.467866 | 13.467866 | 13.467866 | 13.467866 | 13.467866 | 13.467866 | 13.467866 | 13.552009 |
|  |  | 5 | 10.593847 | 10.546547 | 10.587649 | 10.587649 | 10.587649 | 10.587649 | 10.58764 | 10.587649 | 10.215918 |
|  |  | 8 | 10.723455 | 10.246826 | 10.132994 | 10.217441 | 9.8482032 | 10.838086 | 10.590114 | 10.217441 | 10.079855 |
|  |  | 10 | 10.475210 | 10.424366 | 10.441787 | 10.437724 | 10.394407 | 10.574333 | 9.953972 | 10.315368 | 9.878908 |
| Image 4 | Kapur | 2 | 12.670875 | 12.670875 | 12.670875 | 12.670875 | 12.670875 | 12.670875 | 12.670875 | 12.670875 | 12.670875 |
|  |  | 5 | 9.134000 | 8.967988 | 8.727195 | 9.793276 | 8.970005 | 8.970005 | 8.970005 | 9.554190 | 9.995601 |
|  |  | 8 | 8.951120 | 8.671288 | 8.527100 | 8.794746 | 9.034496 | 8.508955 | 8.466784 | 8.688792 | 8.507614 |
|  |  | 10 | 8.254413 | 8.221178 | 8.637974 | 8.323878 | 8.009598 | 8.856883 | 7.358278 | 8.113561 | 7.898697 |
|  | Otsu | 2 | 10.096202 | 10.096202 | 10.096202 | 10.096202 | 10.096202 | 10.096202 | 10.096202 | 10.096202 | 10.088656 |
|  |  | 5 | 9.966926 | 9.459786 | 9.459786 | 9.459786 | 9.966926 | 9.466435 | 9.966926 | 9.459786 | 9.317724 |
|  |  | 8 | 8.569605 | 8.289457 | 8.265960 | 8.289457 | 8.748086 | 8.168667 | 8.202904 | 8.289457 | 8.465271 |
|  |  | 10 | 8.270119 | 7.834744 | 7.897771 | 8.048213 | 8.340841 | 7.517954 | 8.270765 | 8.084830 | 7.570792 |

provide competitive performance in terms of image quality and image clustering metrics, specially in lower level thresholding. The main weakness is its inability of fast convergence for higher level of thresholding applications, although the results denote significant competitiveness.

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