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Preparation, characterization, and analysis of multi-walled carbon nanotube-based nanofluid: an aggregate based interpretation

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Nanofluids are gaining attention as an attractive solution for the sustainable machining of difficult-to-cut materials. Despite the enormous recent work in the literature, there are still contradictions concerning the effect of different preparation factors on the characteristics of nanofluids and the underlying mechanisms governing them. In the present study, the effect of varying the preparation factors, namely, multi-walled carbon nanotube (MWCNT) concentration, sonication time, and surfactant amount on various nanofluid characteristics and the interactions among these characteristics were studied. The characteristics are divided into two categories: (a) dispersion/stability and (b) viscosity/wettability. The analysis showed strong interactions between these two categories which were mainly attributed to aggregates' formation and dynamics. For the stability/dispersion responses, the effect of aggregation and saturation phenomena is discussed in relation to the different preparation factors. Our analysis shows that the nanofluid viscosity is strongly dependent on aggregate morphology. As for wettability, a novel mechanism is proposed and used to explain the nanoparticles' influence on wettability based on the nanolayering theory. Finally, multi objective optimization (MOO) based on grey relational analysis (GRA) was performed. It was found that moderate MWCNT concentration, high sonication time, and low surfactant amount show the optimal characteristics within the current study design variables search domain. The novelty in the present study lies in its consideration of the simultaneous interaction between the nanofluids' properties and stability. Unlike the common practice in the literature, which focuses on one or two aspects of nanofluids, our approach broadens the analysis and provides in-depth insights into the nanofluid as a complete physical system.

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1. Introduction

Optimizing the energy consumption and providing safe and environmentally friendly conditions are two essential requirements for sustainable machining processes. The inappropriate application of cutting fluids during machining operations is well known to impact the quality and cause economic, environmental, and health problems. The wider application of advanced materials such as titanium alloys, nickel-based alloys, structural ceramics, composites, and magnesium alloys in aerospace, automotive, oil and gas, and biomedical industries has been compromised due to several difficulties that arise during their machining. The use of nanofluids during

machining difficult-to-cut materials can offer an attractive solution since they provide significant enhancements in the tribological and heat transfer characteristics which facilitate the machining process especially when combined with recent more sustainable lubrication techniques such as minimum quantity lubrication (MQL).

Different types of nanoparticles have been added to cutting fluids. For example, multi-walled carbon nanotubes (MWCNTs) were added to the cutting fluid while turning Ti-6Al-4V,¹ while in another work, a hybrid of MWCNTs and aluminum oxide (Al₂O₃) nanoparticles was added during machining Inconel 718 and the tool wear mechanisms were investigated.² It was reported that both nanofluids showed better performance compared to traditional cutting fluids. A model that verified the benefit of using a MWCNT-based nanofluid during the machining process was provided in ref. 3. The superior performance of the nanofluids is attributed to their outstanding thermal and tribological characteristics, especially for MWCNT-based nanofluids. The advantages of the utilization of nanoparticles are not limited to one particular field. As a matter of fact, they have numerous applications such as in high capacity

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batteries⁴ and nanoelectronics,⁵ and they are also used in high performance heat transfer fluids in solar absorbers.^{6,7}

Preparing a uniform and stable nanofluid is critical for utilizing the full nanofluid potential. In fact, this is one of the main challenges hindering its wider utilization in industrial applications. This motivated researchers to develop different techniques to enhance the dispersion of nanoparticles in nanofluids through chemical modification (*i.e.*, covalent and non-covalent nanoparticles' surface treatment) or mechanical methods (*i.e.*, sonication and milling). The effectiveness of steric stabilization using Gum Arabic as a surfactant was studied in ref. 8. An optimum surfactant concentration of 1 wt% was reported to extend the stability up to 40 days. Sonication time was also studied, and the optimum time of 4 h was reported. However, extended sonication times beyond this value were found to lower the stability. The author postulated that initially sonication led to detangling the aggregates, thus enhancing stability. However, excessive sonication can lead to breaking the MWCNTs, thus lowering stability. The decrease in aggregate size with sonication by photon correlation spectroscopy (PCS) measurements was confirmed in ref. 9. TEM was used in ref. 10 to show that nanoparticles were re-clustering again with increasing sonication time. Although nanofluid stability is a critical factor to take into consideration, most end users are interested not in the stability itself but rather in its effect on the final nanofluid properties. In the literature, the interaction between nanofluid stability and its physical properties is one aspect that needs further investigation.

The effect of the Al₂O₃ aggregation on the aqueous based nanofluid viscosity was investigated in ref. 11. They reported that the relative viscosity decreased from 43 to only 1.6 due to aggregates breakage by re-sonication. In addition, they also reported that before re-sonication samples showed obvious shear thinning behavior, especially for the 5 vol% concentration

sample. However, after re-sonication, all samples showed shear thickening behavior. This demonstrates that aggregates existence can shift nanofluids' rheological characteristics from Newtonian to non-Newtonian. An increase in viscosity with sonication up to 7 min, followed by a final drop with further sonication has been reported.¹² The initial increase was claimed to be due to the detangling of aggregates by sonication. However, this claim contradicts the effects of aggregates reported in other studies. It was argued that, aggregates' existence boosts the viscosity of the NF.¹³ Regarding the final drop in ref. 12, the authors attributed it to the breakage of CNTs due to excessive sonication.

The effect of surfactant concentration on the viscosities of two nanofluids was investigated and a complex non-linear relation with the general trend of decreasing viscosity with increasing the surfactant concentration was reported for sodium dodecylbenzene sulfonate (SDBS) surfactant.¹⁴ Contradicting results for MWCNT and different surfactants, including SDBS was reported.¹⁵ All surfactants showed an increase in viscosity compared to base oil, with a different increase for each surfactant. Based on these contradicting findings, it is believed that the effect of the surfactant must be influenced by base fluid and particle type.

One of the important nanofluid properties that lacks attention is nanofluid wettability. The effect of the addition of bismuth telluride nanoparticles in water on the contact angle as an indicator for wettability was investigated in ref. 16. The authors reported an increase in contact angle with nanoparticle loading until a certain value before it started decreasing again. The effect of adding silica nanoparticles to water was investigated and a decrease in surface tension and contact angle with increasing concentration was reported.¹⁷ The authors attributed the decrease in contact angle to the decrease in surface tension. The layering of nanoparticles on the solid surface supporting

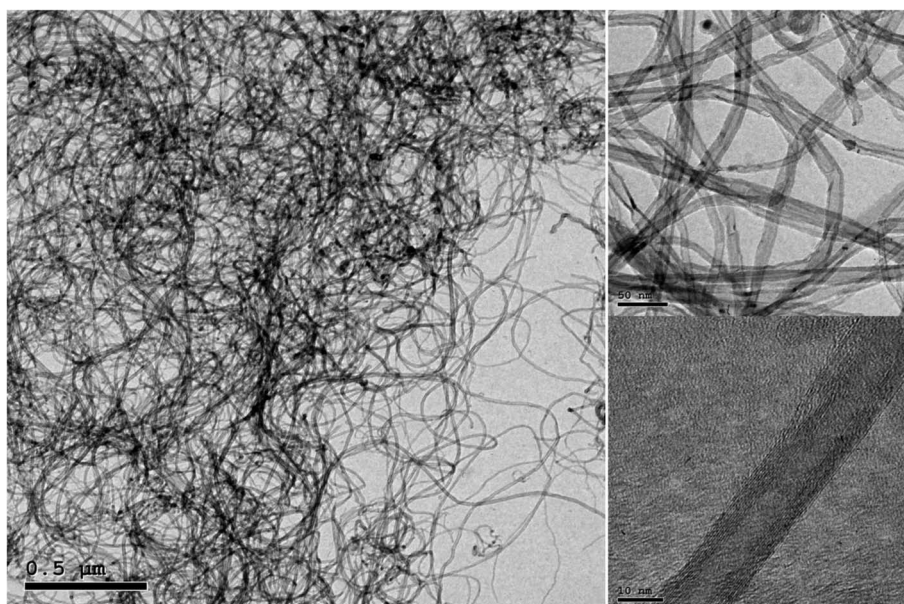


Fig. 1 TEM image of the pristine MWCNTs showing their highly entangled morphology.

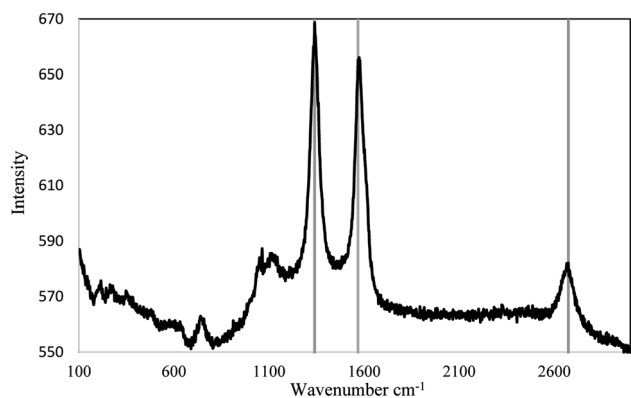


Fig. 2 Raman spectroscopy of the pristine MWCNTs.

the droplet was postulated to contribute to the contact angle variation. In contrast, in ref. 18, the authors reported that the surface tension of nanofluid-type fuels increased due to suspended Al_2O_3 or MWCNT, especially at high concentrations. Likewise, it was reported that surfactant concentration has an influence but in a different way. Based on the reviewed literature, it is evident that the wettability of nanofluids is much less discussed compared to rheological and thermal properties. In addition, the few works available are reporting contradicting results and no clear explanation for these results. Also, another factor that is overlooked in the literature is the effect of sonication and nanoparticles' aggregation on the contact angle. In the current study, this effect is studied for the first time, and attempts to explain it are made.

Based on the above-reviewed literature, it is evident that despite the increasing number of research efforts conducted on nanofluid properties and stability, there are still gaps that require investigation. For example, the role of the aggregates in altering nanofluid properties is usually overlooked in the

literature, even though, in some cases, it shows the most significant contribution. This motivated the inclusion of the interaction between viscosity, wettability, and the aggregates' morphology in our analysis. Also, as noted earlier, another property that needs more attention is nanofluids' wettability and how aggregates' existence, surfactant quantity, MWCNTs concentration, and sonication time affect the nanofluid wettability. In the current study, a novel mechanism is introduced in this regard. Our study offers a platform that deals with nanofluid preparation, characterization, and stability as an inseparable unit. This approach guarantees a complete understanding of nanofluid's unique nature, where all aspects are interconnected.

2. Preparation, characterization, and methodology

In this study, both mechanical and non-covalent techniques were applied during the preparation process. Since the base fluid used is organic (vegetable oil), Triton X (TRx) with >99% purity purchased from Sigma Aldrich was used, which is a non-ionic surfactant. 70–90% purity Elicarb MWCNTs purchased from Thomas Swan (UK), shown in Fig. 1, with an average diameter between 10–12 nm, and tens of microns lengths were used. Fig. 2 shows the Raman spectroscopy analysis of the pristine MWCNTs. The figure shows three distinctive peaks at 1340, 1568, and 2674 cm^{-1} . These three peaks correspond to the D, G, and G' bands. The G band is the result of carbon atom vibration along the MWCNTs walls, while the G' is the second harmonics of the D band. Finally, the peak located at the D band corresponds to impurities and structural damage of the MWCNTs. The quality factor (*i.e.*, the ratio between the G to D band intensities) is 0.98.

In the current study, the nanofluid preparation is based on the unzipping mechanism. Initial sonication and then

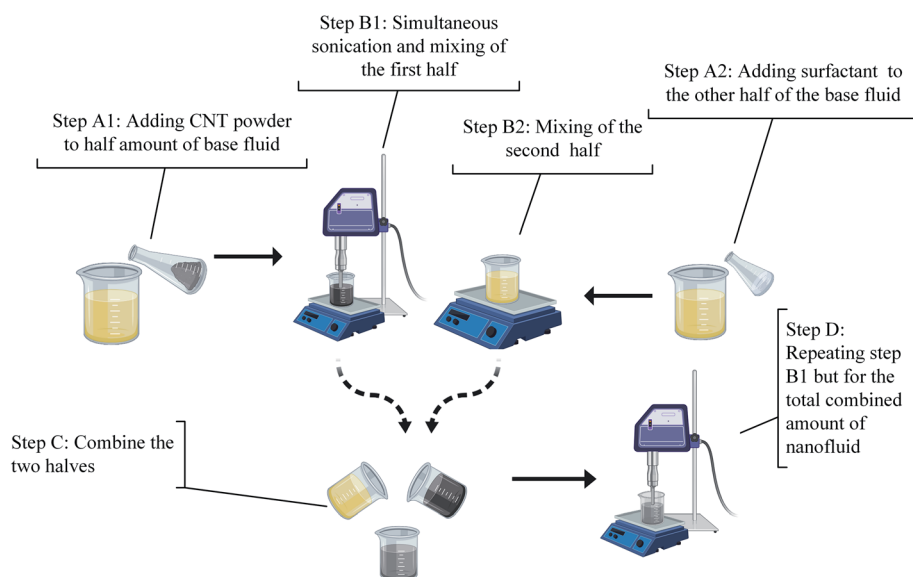


Fig. 3 Preparation procedures for the MWCNT-based nanofluid.

Table 1 Sonication energy for the different durations

Time [min]	Pre-sonication [kilojoule]	Second sonication [kilojoule]
2.5	13.9	18.2
5	26	34.6
15	81.7	114.4

subjecting the MWCNT bundles to surfactants would improve the uniformity of surfactant on the MWCNT and boost its deagglomeration.¹⁹ The procedures described in Fig. 3 were designed to prompt the unzipping mechanism and assure uniform adsorption of the surfactant on the MWCNT surface. Initially, MWCNTs were added to 250 ml of oil and pre-sonicated/mixed. Afterwards, another 250 ml of the oil-surfactant mixture were added, making the total sample volume 500 ml. Finally, the 500 ml sample was re-sonicated/mixed for the second time. Using Q Sonica 700 sonicator, a 15 s pulse on and 15 s pulse off program was used to avoid overheating the sample and the probe during sonication. The average sonication energies for pre-sonication and second sonication are shown in (Table 1).

2.1 Characterization of nanofluid

2.1.1 UV-visible spectroscopy. UV-visible spectroscopy was used to evaluate the concentration of samples at different time intervals. Such measurement is based on Beer-Lambert's law, which states that the UV absorbance is directly related to the concentration. In the present study, the absorbance spectrum was measured by Jenway 7415 spectrophotometer in a standard quartz cuvette. All samples were diluted by the base fluid as follows: 1 ml of the prepared nanofluid was mixed with 250 ml of the base fluid. This was necessary because the prepared samples were too opaque (absorbance more than 4). At such high absorbance, the stray light error's effect is very significant, and the reading of the detector lens is no longer reliable to measure the transmitted beam intensity.²⁰ Dilution was performed for three test samples, and the tests were repeated three times in order to eliminate any noise in the results due to dilution inconsistency. Peak absorbance was detected at 337 nm, as shown in Fig. 4. The variation in the absorbance

intensity at this particular peak is taken as an indication of variation in nanoparticle concentration, as will be discussed later.

2.1.2 Particle size. To measure the effective MWCNTs particles and aggregate size, the dynamic light scattering technique (DLS) was used. This technique is based on measuring the Brownian motion of particles and correlating it to particle size using laser beam scattering. Larger particles are known to show slower motion and less scattering. Zetasizer ZS90 from Malvern was used, and the sample was diluted by the base fluid with a ratio of 1 : 250, as described, for the UV samples, to overcome the high viscosity and opacity of the samples.

2.1.3 Viscosity. Viscosity was measured using model 900 viscometer from OFITE, which is a coaxial cylinder rotational type viscometer. Before measuring the viscosity of the prepared nanofluid, the device accuracy was checked by measuring water viscosity at the same shear rate (170.23 s^{-1}) and temperature ($27 \text{ }^\circ\text{C}$) used in the current analysis. The results showed adequate accuracy.

2.1.4 Contact angle. The contact angle was measured using a Drop Shape Analyzer DSA 25 from KRUSS, Germany. The device uses a precise microsyringe to place a specific volume of a droplet on a solid surface. Once the droplet is placed on the solid surface, it is allowed to spread governed by its wettability (*i.e.*, surface tension). A high-resolution camera aided with the manufacturer's image processing software was used to draw a tangent to this droplet. The angle made by this tangent and the horizontal is taken as the contact angle. A constant volume of $10 \text{ } \mu\text{l}$ (microliter) of all samples was dispensed using a micro-

Table 2 Experiment design and responses

Run	MWCNTs concentration (volume%)	Sonication time (min)	Surfactant per MWCNTs (weight ratio)
1	0.1	5	1 : 10
2	0.1	10	1 : 1
3	0.1	30	10 : 1
4	0.4	5	1 : 1
5	0.4	10	10 : 1
6	0.4	30	1 : 10
7	0.7	5	10 : 1
8	0.7	10	1 : 10
9	0.7	30	1 : 1

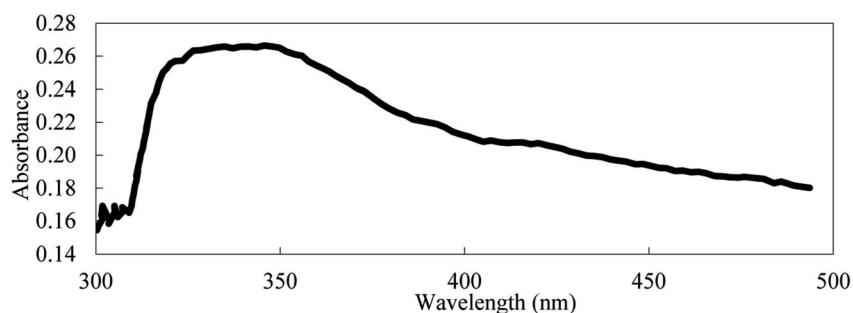


Fig. 4 UV absorbance for MWCNTs in vegetable oil.

Table 3 Factors and levels studied

Factor	Level 1	Level 2	Level 3
X: (ml MWCNT per ml oil%)	0.1	0.4	0.7
Y: (sonication time in minutes)	5	10	30
Z: TRx : MWCNT (ratio between surfactant weight to MWCNTs weight)	1 : 10	1 : 1	10 : 1

syringe on a polished glass slide, and measurements were repeated at least nine times. Measurements were taken after one minute of placing the droplet on the surface. The same type and condition of the glass slides were used for all samples to ensure a consistent setup.

2.2 Methodology: design of experiment and optimization

In the current study, the L9OA design in Table 2 was adopted with three factors (*i.e.*, design variables) and three levels for each factor. The factors and levels were chosen based on the most common values in the literature, as shown in Table 3. Special attention was paid to cover as wide a range as possible, keeping in mind the limitations of available measuring instruments and taking advantage of the non-linear capabilities of the chosen 3 level array. The relation between factors and responses was computed using the response graph (*i.e.*, main effect plot).

The variations in viscosity, UV absorbance with time were calculated as follows:

Variation =

$$\frac{\text{property of fresh sample} - \text{property of one day old sample}}{\text{property of fresh sample}} \quad (1)$$

While the drop in viscosity due to shear thinning was calculated as follows:

Drop in viscosity =

$$\frac{\text{viscosity at low shear rate} - \text{viscosity at high shear rate}}{\text{viscosity at low shear rate}} \quad (2)$$

3. Results and discussion

The measured responses are summarized in Table 4. This section analyzes these responses, starting with the dispersion-stability characteristics followed by a discussion of viscosity then contact angle (property-related characteristics). Throughout the entire discussion, the interaction between both the property-related and the dispersion-stability characteristics are addressed.

Optimum dispersion is only achieved if all the added powder is broken into the smallest possible size and uniformly distributed throughout the fluid. This is realized when instantaneous sedimentation (saturation phenomena), as discussed in the next section, is eliminated. In addition, uniform dispersion is not guaranteed to last unless stability is also fulfilled. To achieve stability, the van der Waals attraction forces and Brownian collisions should be resisted by electrostatic repulsion forces or steric hindrance. A comparison between instability and dispersion inadequacy (*i.e.* saturation) is shown in Fig. 5.

3.1 Dispersion and saturation

Increasing MWCNTs concentration is expected to magnify their influence on the physical properties of the nanofluid. Unfortunately, this is not always guaranteed since, in some instances, when the dispersion mechanism is not suitable, aggregates will instantaneously sediment due to their large size and higher density (relative to the base fluid), as shown in Fig. 5. In such cases, the properties of the nanofluid will not be enhanced upon further addition of nanoparticles.

3.1.1 Effect of particle loading. The saturation phenomenon is fundamental for explaining the behavior of nanofluids at different concentrations. Fig. 6 shows that the UV absorbance increased by 113% when the concentration was increased from

Table 4 Measured responses for each run

Run	UV fresh	UV one day	Viscosity (cP) fresh @ 100 rpm	Viscosity (cP) one day @ 100 rpm	Viscosity (cP) fresh @ 600 rpm	Effective size (nm) fresh	Effective size (nm) one day	Contact angle (degree)
1	0.23	0.01	55.6	30.0	43.8	634.9	800	22
2	0.316	0.29	83.8	89.2	71.2	430.8	500	25
3	0.36	0.31	80.8	85.9	71.7	450	460	17
4	0.67	0.5	216.8	227.3	147.1	959.2	1200	30.6
5	0.55	0.4	245.4	248.3	189.2	900	1120	28
6	0.71	0.7	268.1	265.0	201.4	818	1115	40
7	0.5	0.44	244	298.8	149.7	1000	1400	30
8	0.65	0.64	219	240.8	136.0	1200	1600	35
9	0.82	0.7	293	314.3	202.2	1000	1200	37

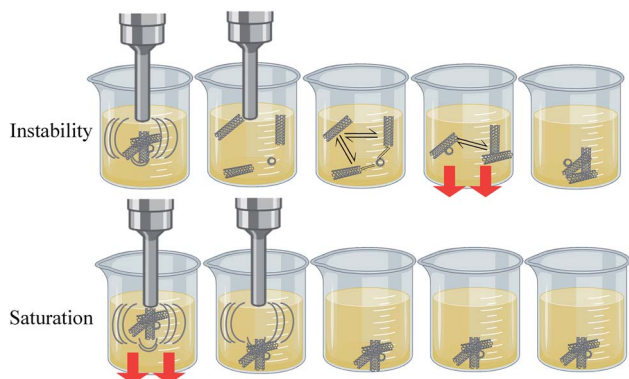


Fig. 5 Instability and saturation.

0.1 to 0.7%, while it only increased by 2% between 0.4 and 0.7%. It is important to note that, based on Beer–Lambert law, effective (true) nanoparticle concentration is directly related to the UV absorbance. The insignificant change in MWCNTs effective concentration towards higher particle loadings indicates that the saturation effect is in action. Such an effect is believed to cause lower improvements in nanofluid properties at higher concentrations, as shown later in Fig. 9 and 14. In these figures, the saturation damped the increase in viscosity and contact angle as nanoparticle concentration increased from mid to high. This phenomenon may be overcome by improving the mechanical dispersion method, such as increasing sonication time, power, or alternatively, ball milling the powder before adding it to the base fluid. However, it should be noted that the excessive mechanical dispersion techniques might lead to shortening or even damaging the MWCNTs.

3.1.2 Effect of sonication time. The increase in sonication time associated with using enough surfactant will allow more particles to be separated due to the unzipping mechanism. This mechanism illustrates how both mechanical and non-covalent stabilization (*i.e.* surfactant) mechanisms simultaneously de-bundle pristine MWCNTs. If no surfactant is used, the narrow gap induced by the mechanical method will most likely close again under the effect of van der Waals forces. By using surfactants, such forces can be minimized, and the colloid system stability can be enhanced. Sonication provides shear forces on the bundles due to the high and low-pressure wave cycles, inducing cavitation in the base fluid, which in turn induces a jet stream that impacts the MWCNTs. This explains why increasing sonication time will lead to better dispersion and smaller aggregates, as demonstrated in Fig. 6 and 7, respectively. The increase in sonication time from 5 to 30 minutes raised and lowered the UV absorbance and particle size by 35% and 12.5%, respectively.

3.1.3 Surfactant concentration effect. Since the unzipping mechanism depends on both sonication adequacy and availability of surfactants, increasing the availability of surfactant molecules is expected to enhance the unzipping efficiency. This is confirmed by the smaller effective particle size shown in Fig. 7. With regards to the UV absorbance, from the results presented in Fig. 6, it can be seen that when the surfactant increased from the low to the medium concentration, the effective concentration increased by 13.5%, but when Triton X (TRx) level increased from medium to high, the effective concentration decreased by 22%. Excessive surfactants can cause an adverse effect due to bridging between nanoparticles. Accordingly, a minimal amount of surfactant will decrease the unzipping action of sonication, and too much will cause

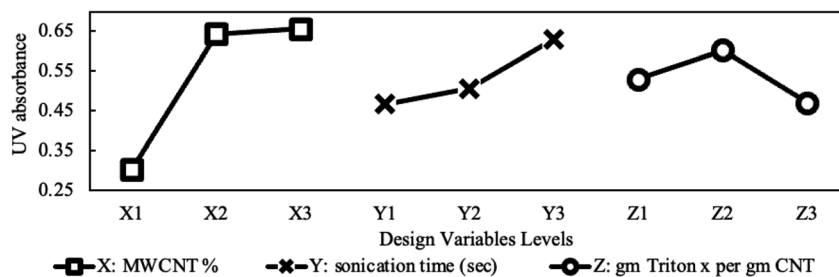


Fig. 6 UV absorbance of fresh samples and saturation effect.

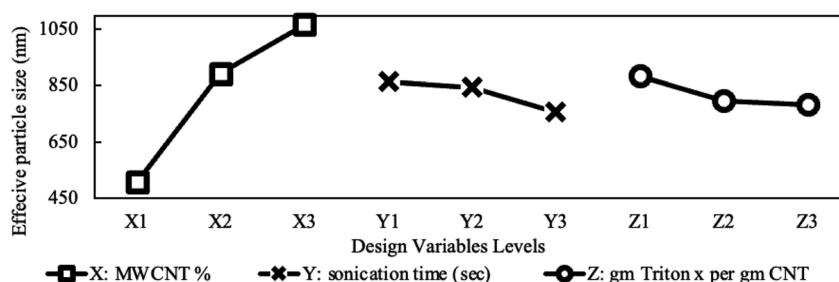


Fig. 7 Effective size of fresh samples.

bridging between particles. Fig. 6 shows that 0.1 TRx:MWCNT avoided these defects and improved the dispersion by 13.5% and 28% compared to the no TRx and high TRx concentration.

3.2 Stability

In the current study, the nanofluids stability was investigated by calculating the UV absorbance with time (*i.e.*, after 24 hours) according to eqn (1). Based on Beer–Lambert law, this variation to the UV absorbance is directly related to the change in concentration. According to Stokes law, the sedimentation velocity is affected by several factors, including the size of particles and viscosity. Higher viscosity and smaller particle size will lead to a lower sedimentation rate. To further explain this, the sedimentation process of nanoparticle should be considered. After the nanoparticles are dispersed, their size should be at its smallest value, and according to Stokes law, sedimentation is insignificant. However, under certain conditions, the aggregates will start to form due to van der Waal's forces. In the first stage of the sedimentation process, the effective viscosity and Brownian diffusion overcome the gravitational force wherein during the second stage gravity is dominant and sedimentation becomes significant.

Another parameter that affects the sedimentation velocity is the initial particle size. If the dispersion technique used is too weak, the initial size of aggregates is too large and accordingly stage one is skipped and sedimentation (*i.e.*, stage two) starts straight away, which in extreme cases leads to saturated nanofluids, as discussed earlier. Thus, various parameters affect the sedimentation rate differently. The initial particle size is proportional to the sedimentation rate, whereas the viscosity of the nanofluid is inversely related. The influence of these two parameters will be utilized in the next section to explain the variation in effective concentration after one day, as shown in Fig. 8.

3.2.1 Effect of particle loading. The increase in nanoparticle loading decreased the variation in the UV absorbance with time by 76% as MWCNTs concentration increased from 0.1 to 0.7%, as shown in Fig. 8. The lower the UV-absorbance-variation with time, the higher the stability. This seems counter-intuitive since increasing the MWCNTs concentration is expected to lower stability. To elucidate this behavior, two distinctive factors should be considered. Firstly, increasing nanoparticle loading will indeed increase the initial particle

size, as evident from Fig. 7 because particles are closer at higher concentrations. Thus, the variation in concentration is expected to increase in contrast to what Fig. 8 indicates. However, the second factor at play is related to the viscosity of the high concentration sample which shows a resisting effect. As shown later in the current study (Fig. 9), the increase in particle loading is associated with an increase in viscosity. This higher viscosity represents an extra drag force on the particle thus causing the sedimentation velocity to decrease. Finally, Fig. 8 indicates that the net outcome of these two aforementioned conflicting factors is the decrease of the variation in concentration. Although this may give a positive impression of good stability, it is a false one. This is because true stability is achieved when the preparation factors can resist the re-clustering of the dispersed nanoparticles. Nevertheless, in the case of the 0.7% sample, aggregations are indeed being re-formed, but the viscous drag resists their sedimentation leading to the false stability shown in Fig. 8. This idea of false stability will be re-visited later in the current study when focusing on nanofluid viscosity.

3.2.2 Effect of sonication time. Increasing sonication time leads to a smaller initial size, as shown in Fig. 7 and better adsorption of surfactant due to unzipping of the MWCNT bundles. It also increases the viscosity, as shown in Fig. 9, all of which lead to a lower sedimentation rate, as shown in Fig. 8. In addition, the sonication time showed the highest contribution among the other preparation factors regarding enhancing stability (lowering the concentration variation) by 77.5% when the sonication time increased from 5 to 30 minutes. In addition, the absence of an abrupt decrease in size in Fig. 7 postulates that no MWCNT damage occurred up to the 60 min sonication limit.

3.2.3 Effect of surfactant concentration. Fig. 8 shows that the lowest variation in concentration was found to occur at the middle surfactant concentration instead of the max one. The middle range of surfactant shows 9.2% less UV variation than the highest one. In order to elucidate this observation, the interaction between the surfactant molecules and the nanoparticles should be investigated. When the correct surfactant amount is used, it should adsorb to the surfaces of the nanoparticles, forming a space barrier between nanoparticles, thus resisting the attraction forces and Brownian collisions. This is known as steric stabilization and is driven by the repulsive osmotic force that is activated when the local concentration of surfactant increases as particles get closer. This explains the

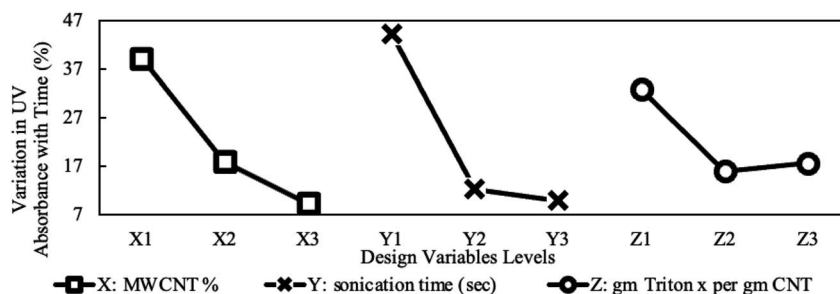


Fig. 8 Change in concentration after one day due to sedimentation.

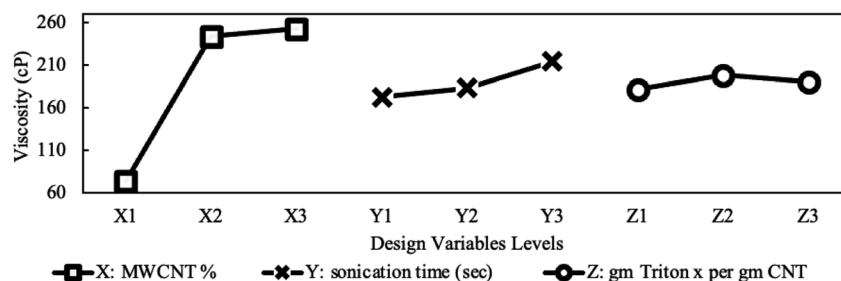


Fig. 9 Viscosity of fresh samples.

lower change in concentration shown in Fig. 8, when the surfactant increases from none to 1 : 1 TRx : MWCNT. However, excessive surfactant decreases stability due to micelle formation in the bulk fluid after the critical micelle concentration is reached. These micelles grow in size until finally, they start to self-aggregate. Surfactant molecules can also accumulate on the nanoparticle's surfaces, forming dense mono or double layers thus leading to higher sedimentation and lower dispersion due to bridging of adjacent nanoparticles rather than separating them. This explains sedimentation at the highest surfactant loading shown in Fig. 8.

3.3 Viscosity

3.3.1 Effect of nanoparticle loading. Fig. 9 shows a sub-linear rather than the expected super-linear increase in the viscosity with nanoparticle concentration due to the existence of complex aggregates structures, especially at high concentrations. The increase in the aggregates size was confirmed by DLS earlier in Fig. 7. Such an increase in size leads to an increase in the effective volume fraction of the nanoparticles, thus immobilizing the base fluid movement. In some extreme cases, aggregates get larger and collide with each other, thus increasing viscosity even further. However, in the present study, a slightly different trend is observed where the viscosity increased by 231.6% and 3.5% from 0.1 to 0.4% and 0.4 to 0.7%, respectively. This observed sub-linear increase could be attributed to the saturation that occurred at high concentrations. In other words, any particles added beyond the 0.4% has no significant effect on nanofluid viscosity, since they instantaneously sediment due to saturation as discussed earlier in Fig. 5. The sub-linear relation indicates that the poor dispersion due to saturation damped the aggregate existence and growth effect, thus constrained the increase in viscosity from 0.4% to 0.7%. However, from 0.1% to 0.4%, the effective nanofluid concentration significantly increased (good dispersion), as shown earlier by UV absorbance in Fig. 6, and the aggregate size increased, as shown in Fig. 7. Both are believed to have promoted the viscosity enhancement.

3.3.2 Effect of sonication time. As Fig. 9 indicates, as the sonication time increased, the viscosity increased. To understand this, the effect of sonication on the aggregates size and the dispersion's quality should be examined. Increasing sonication led to two contradicting effects. The first is breaking up aggregates, as indicated earlier by the decrease in average

effective size, as shown in Fig. 7. This reduces viscosity. The second effect is improving dispersion (*i.e.*, reducing saturation effect) indicated by increasing UV absorbance in fresh samples, as shown earlier in Fig. 6. This improved dispersion means more particles contributing to increasing the nanofluid viscosity. The increase in viscosity in Fig. 9 indicates that the latter outweighed the former. The same results were obtained in ref. 9; however, in this study, the viscosity started to drop again after reaching peak sonication time of 60 min, which is probably due to breaking and damaging of the nanoparticles.

3.3.3 Effect of surfactant concentration. The surfactant concentration showed the lowest impact on the viscosity, as shown in Fig. 9(c). Similar findings was reported in ref. 15 at which Triton-X (OP-10/TRx) caused the least increase in viscosity compared to five other tested surfactants due to the weak London force of OP-10. This makes Triton-X a strong candidate among other surfactants if lower viscosity is desired. In general, MWCNTs concentration showed the most significant influence on the viscosity followed by sonication time and TRx concentration as shown in Fig. 9.

3.3.4 Shear thinning. Most nanofluids are non-Newtonian (*i.e.* shear-thinning). The nanofluid viscosity at a high strain rate was measured and compared to that at the lower strain rate, which was previously analyzed. The two strain rates used were 170.23 s^{-1} and 1021.38 s^{-1} . All prepared samples showed shear-thinning. The shear-thinning behavior is explained by changes in the morphology of the aggregates at high shear rates. The high hydrodynamic forces can break the aggregates, which lowering their ability to immobilize the fluid flow thus leading to a lower viscosity. On the other hand, the high shear rate can also cause the re-alignment of aggregate structures within the flow field, in the way shown in Fig. 11. Such alignment can reduce the drag, thus lowering the viscosity.²¹ Both re-alignment and breaking of the aggregates can contribute to shear-thinning with different weights according to the shear rate and aggregates morphology.²²

The variation in viscosity-drop due to shear thinning, defined in eqn (2), is presented in Fig. 10 for the studied design variables. The figure shows that viscosity-drop increases as concentration increases also reported in a previous study.²³ As discussed earlier, the shear-thinning behavior is due to the breakage or alignment of aggregates, and therefore, it is expected that the viscosity drop due to shear thinning increases if more aggregates exist. Fig. 7 shows that the average particle size

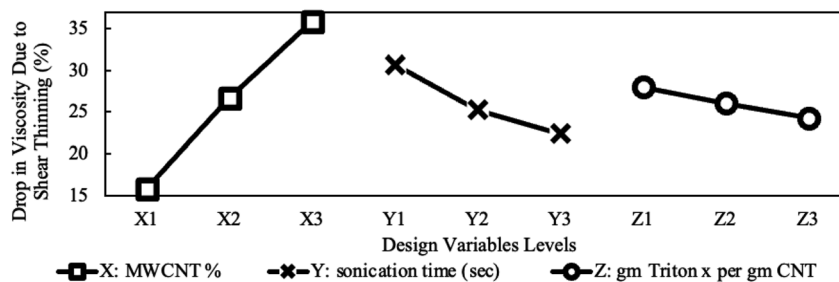


Fig. 10 Change in viscosity due to shear thinning.

increased with concentration. This confirms the existence of more and larger aggregates and explains the higher viscosity-drop at higher concentrations. The opposite can be assumed for sonication time and the surfactant amount. Increasing any of them leads to a decrease in particle size, thus causing a lower viscosity-drop due to shear thinning as shown in Fig. 10. Finally, the MWCNT concentration showed the most noticeable influence on the viscosity drop due to shear thinning. The influence of different preparation factors is quantified as can be seen in the main plot effects in Fig. 10. It is evident that MWCNTs concentration is considered the most significant design variable followed by the sonication time and surfactant concentration.

3.3.5 Effect of stability on nanofluid viscosity. The instability of nanofluids can alter their properties in an unpredicted manner. Fig. 11 shows the variation in viscosity after one day according to eqn (1). It shows two distinct behaviors of instability, where the change in viscosity can be positive or negative. This can be explained by considering the two stages of instability presented in Fig. 12. In cases where the nanofluid is highly unstable, it reaches stage two within one day, and thus the viscosity will decrease. This is due to the higher portion of the particle-free fluid. In other cases, when nanofluid stability is a little higher, and the sample is still within stage one, aggregates will be formed and kept suspended in the fluid, leading to increased viscosity. In other words, if the elapsed time is less than aggregating time, the viscosity will increase, but if it is more than settling time, viscosity will decrease. In Fig. 11, the cases of low concentration, low sonication, and low surfactant samples showed a decrease in viscosity. The same finding was reported for viscosity and thermal conductivity.²⁴ The drop in viscosity shown in Fig. 11 for low concentration, low sonication,

and low surfactant samples aligns with their highest UV absorbance drop in Fig. 8. Thus, in all these cases, it can be said that these samples were very unstable and reached the end of stage two in Fig. 12.

Fig. 11 exemplifies the false stability mentioned earlier for the highest nanoparticle loading. It shows that 0.7% caused a more substantial increase in viscosity compared to 0.4% even though the 0.7% showed a lower change in concentration as UV absorbance indicates in Fig. 8. As explained earlier, this can be attributed to the higher capabilities of 0.7% sample to hold larger aggregates without sedimentation. The maximum stability achieved by the 0.4% sample suggests that the combination of its moderate aggregate size (less than the 0.7% sample) and moderate effective viscosity (more than the 0.1% sample) add up to maximize stability. Finally, the trend of the surfactant effect in Fig. 11 aligns perfectly with the change in concentration shown earlier in Fig. 8. Fig. 11 also shows that the three studied design variables have comparable importance. However, the MWCNTs concentration and surfactant concentration are the two most significant design variable, while the sonication time is less significant.

3.4 Contact angle

One of the essential properties of any fluid is its wetting behavior. This was analyzed in the present study using contact angle measurements, as presented in Table 4, Fig. 13 and 14.

3.4.1 Effect of nanoparticle loading. For MWCNTs concentration, the increase in the concentration caused an increase in the contact angle. The 0.7% concentration showed a 37.2% higher contact angle compared to the 0.1% concentration. However, like viscosity, the same damped increase in

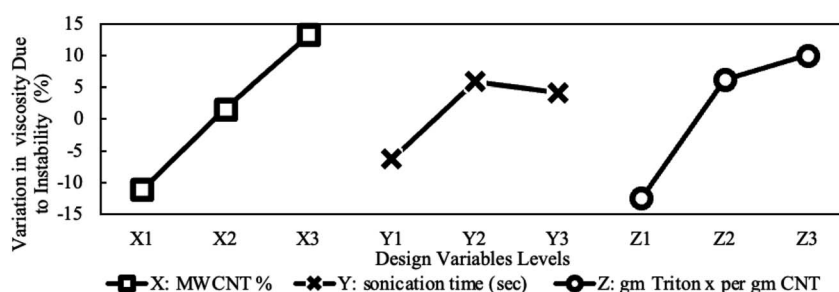


Fig. 11 Change in viscosity after one day.

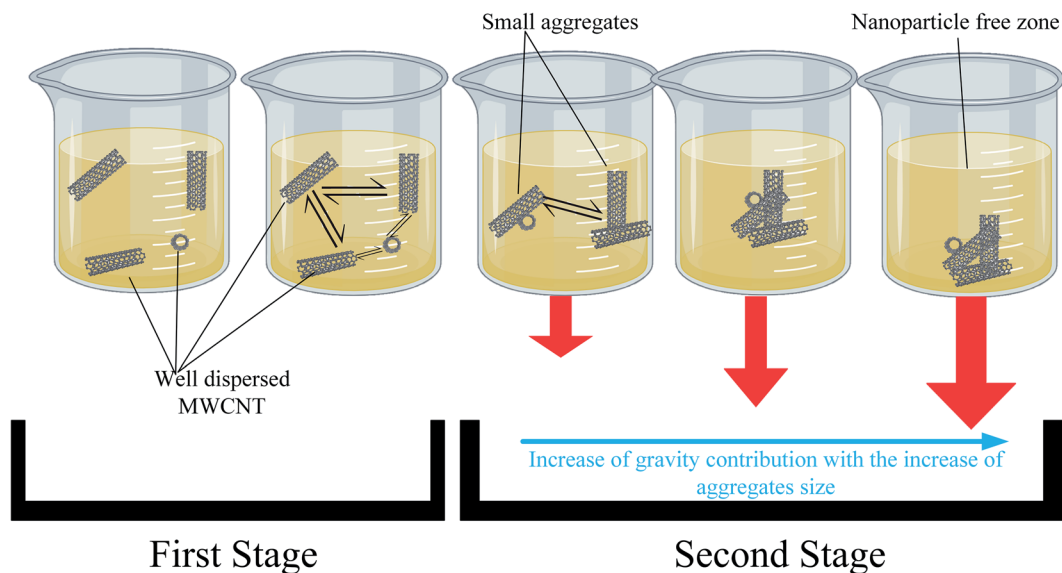


Fig. 12 Sedimentation process of nanoparticles.

contact angle with increasing the concentration from mid to high was noticed. This effect can be explained by the saturation of the nanofluid, as discussed earlier. The effect of nanoparticles on the contact angle is not agreed upon in the literature. Some reported a similar trend as in Fig. 14.²⁵ In contrast,

others reported a decrease of contact angle with concentration.²⁶

The contact angle is directly related to surface tension. This is a force generated from the cohesion between fluid molecules that minimize the surface of a given droplet volume. The

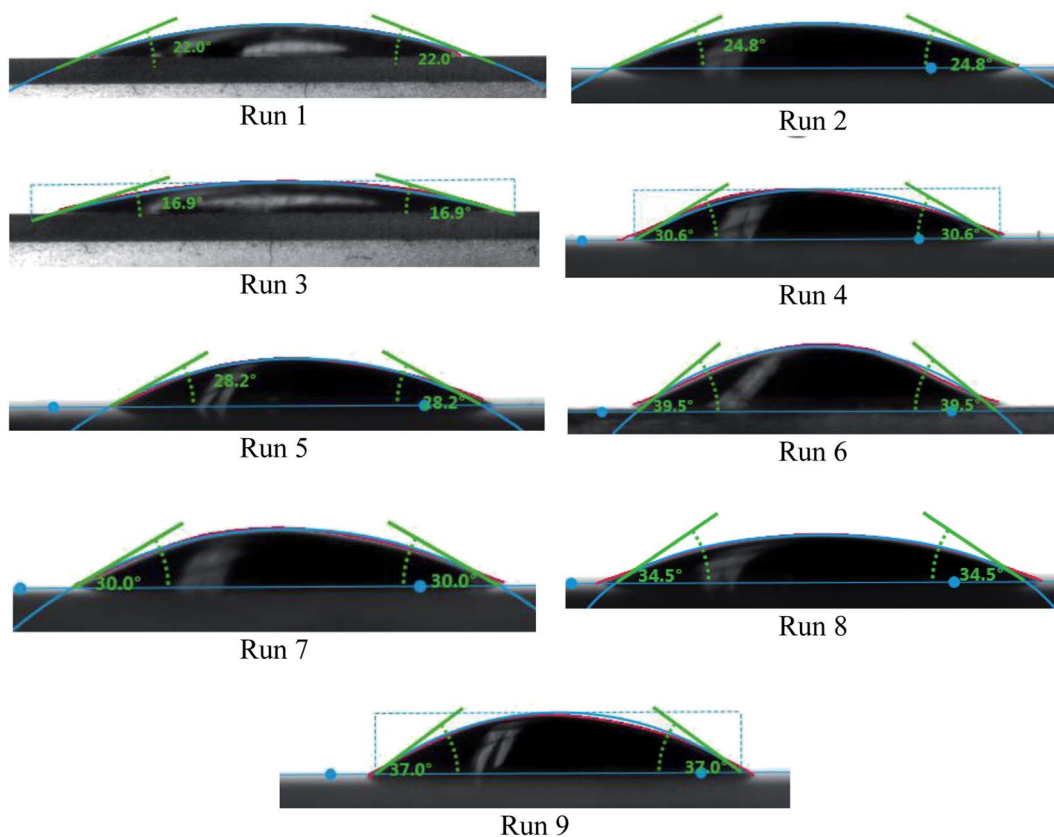


Fig. 13 Measured contact angle for every run.

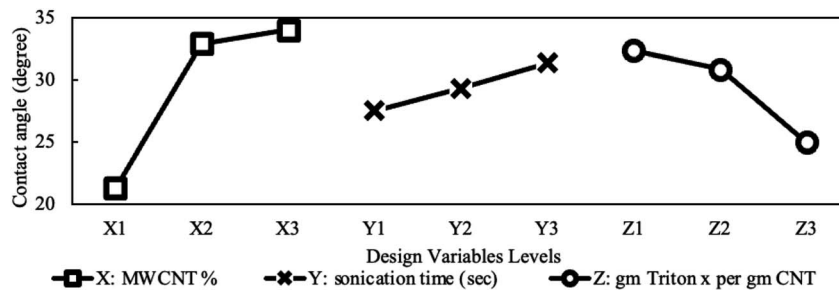


Fig. 14 Contact angle of fresh samples.

Table 5 Optimization criteria

Responses	Objective
Concentration variation	Minimum is better
Viscosity variation	Minimum is better
Contact angle fresh	Maximum is better
Viscosity fresh	Minimum is better

increase in contact angle indicates an increase in this force. Many theories tried to find out the effect of nanoparticles on this force. For functionalized nanoparticles in polar solutions, functionalized groups attached to the surface of MWCNTs was considered as the main driver to increasing the attraction force.²⁷ However, since un-functionalized nanoparticles, as in our case and others, showed the same increase in contact angle, this effect could not be solely responsible for the observed increase in contact angle and surface tension.

Another factor that could contribute to increasing base fluid molecule adhesion is the formation of nanolayers. The existence of nanoparticles in the base fluid is associated with an ordered layer of base fluid around the nanoparticle. The reason behind this layered fluid formation is due to high particle to liquid molecule interaction force. This force leads to attracting and organizing the liquid molecules in a strong solid-like structure, as shown in Fig. 15. Thus, at this ordered layer, liquid particles are forced to get closer, forming a packed, organized structure that is difficult to disturb. Such a constrained structure can be thought of as an immobilization mechanism for NF droplet spreading (wettability). This is because spreading requires the liquid molecules to be flexible to move around freely and be re-oriented to form a thin film maximizing the wetted surface area. The effect of forming these ordered nanolayers resembles a powerful cohesion force between layered molecules. Additionally, the extra MWCNT to MWCNT van der Waal's attraction force will add to the droplet's internal attraction. This further works on immobilizing the

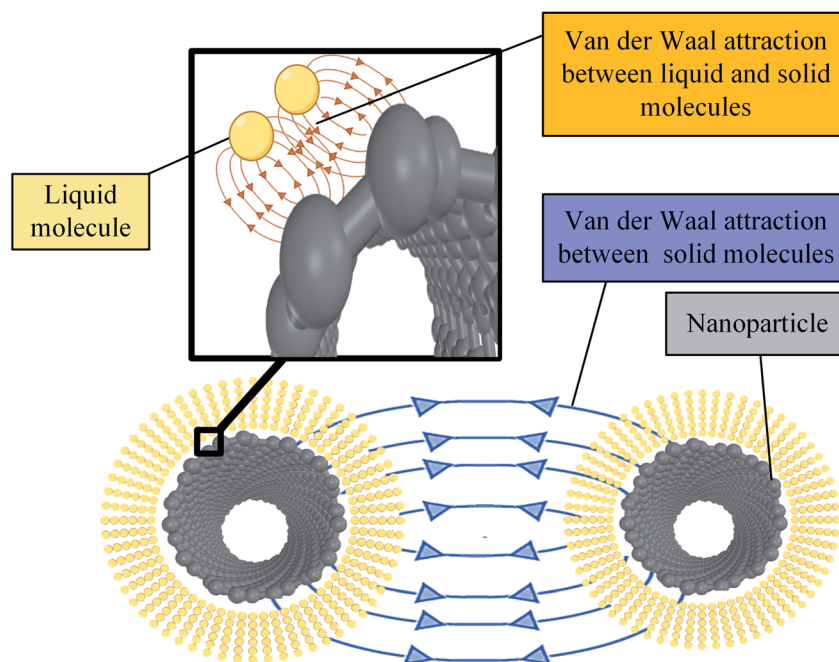


Fig. 15 Role of MWCNT nanoparticles in increasing cohesion.

Table 6 Gray relation analysis summary

Run	GRC				
	UV variation	Viscosity drop	Viscosity fresh	CA fresh	GRG
1	0.33	1.00	0.33	0.39	0.51
2	0.87	0.81	0.90	0.43	0.75
3	0.79	0.82	0.90	0.33	0.71
4	0.66	0.42	0.92	0.55	0.64
5	0.65	0.38	1.00	0.49	0.63
6	1.00	0.36	0.99	1.00	0.84
7	0.82	0.39	0.71	0.53	0.61
8	0.99	0.42	0.84	0.70	0.74
9	0.78	0.33	0.88	0.79	0.70

relative motion between different formed nanolayers around different MWCNT particles, thus boosting the fluid cohesion and lowering its wettability.

Another mechanism believed to be playing a role in influencing the contact angle is related to the contact line dynamics. It was proposed that spreading of droplets is controlled by the contact line's displacement on the solid surface as follows, the contact line will spread by moving between adsorption sites until it reaches equilibrium at one of those sites.²⁸ Based on this theory, the increase in the contact angle and accordingly the lower spreading was attributed to roughening of the surface due to pinning of the contact line by the nanoparticles.²⁹ Contrary to this view, other researchers suggested and reported the opposite. For example, it was suggested that nanoparticles enhance the contact line's spreading by a rolling and lubricating effect.³⁰ This point of view is suggested for spherical nanoparticles because of their high rolling capacities. The difference in the form (spherical or tubular) might be the reason behind the different proposed effects. In conclusion, in this study, the two mechanisms related to the cohesion enhancement in Fig. 15 and the contact line pinning were consistent with our findings.

3.4.2 Effect of sonication time. Fig. 14 shows the effect of sonication time on the contact angle. Increasing sonication time has two effects. Firstly, it improves dispersion by increasing the effective MWCNTs concentration as indicated by UV absorbance, as shown in Fig. 6. This influence on contact angle is like adding an extra nanoparticle, and this should

increase the contact angle if it were solely in action. Secondly, increasing sonication time can lead to breaking aggregates, as indicated by lowering the aggregates' size shown in Fig. 7, which in turn leads to increasing the MWCNT surface area. This gives a chance for more liquid molecules to participate in the ordered nanolayer in Fig. 15. Besides, the broken and smaller aggregates can boost the contact line's pinning as smaller aggregates will have higher penetration and adsorption capabilities. Thus, all of these mechanisms will add up to increase the contact angle. This was confirmed in Fig. 14, where the 30 min sonication time showed a 13.8% higher contact angle than the 5 min sonication time.

3.4.3 Effect of surfactant concentration. The last factor that is shown in Fig. 14 is the surfactant concentration. The contact angle was found to decrease by increasing the surfactant concentration, indicating a decrease in surface tension. This effect is the most agreed upon factor in the literature. This is because the surfactant molecules attached to the MWCNT surfaces generate repulsive forces between them. Besides, another goal behind adding a surfactant to the base fluid is to increase the base fluid wettability to wet the high-energy surface of the MWCNTs particle and improve nanofluid dispersion. This increase of base fluid wettability is the exact opposite of the fluid molecules cohesion concept. Finally, Fig. 14 shows that MWCNTs concentration is the most influential design factor, followed by the surfactant concentration and finally, the sonication time, respectively.

3.5 Multi objective optimization

Due to the conflict between the studied characteristics at different levels of the studied design variables, gray relation analysis (GRA) was adopted. GRA is a flexible and computationally straightforward multi objective optimization technique. Table 5 shows the followed optimization criteria. Concentration and viscosity variations due to instability were set to a minimum is better. The same goes for the nanofluid viscosity. This is to reduce the increase in the pumping power associated with nanoparticles' addition. Finally, the contact angle was set to maximum is better. The higher contact angle can lead to a better lubricating effect due to stronger lubricating film.

A detailed outline of the procedures followed in the present study to calculate the GRC and GRG in Table 6 can be found in ref. 31. Optimum runs for individual responses are shown in

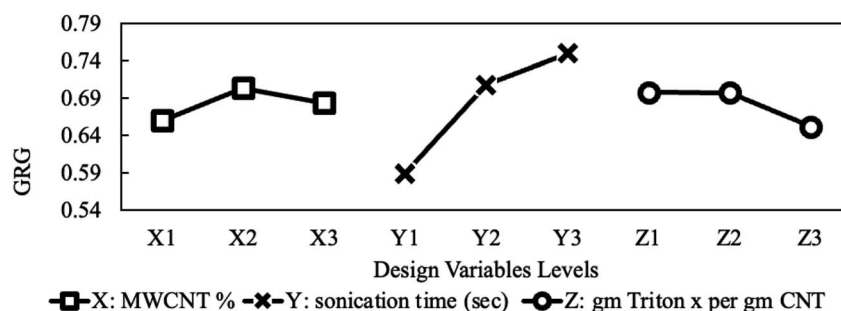


Fig. 16 Mean effect plot for the gray relation grade (GRG).

italics.. The disagreement of the different optimum runs for each response elucidates the importance of multi-objective optimization.

The mean plot effect of the GRG in Fig. 16 indicates that the mid MWCNT concentration, max sonication time showed optimum overall characteristics. It also depicts the adverse effect of using too much surfactant. The figure shows that the sonication time possesses the most influential impact, followed by MWCNT concentration and the surfactant amount, respectively. It is critical to note that optimums presented in Fig. 16 are only valid for the criteria specified in Table 6. If other criteria are desired, the above-mentioned optimums are no longer valid, and the optimization problem must be re-visited.

4. Conclusions

In the present study, the interaction between different nanofluid characteristics was studied with a special focus on aggregates' role and how this role is affected by the preparation factors. Three different preparation factors were tuned, namely, nanoparticle concentration, sonication time, and surfactant amount. The effect of these factors on nanofluid stability, dispersion, rheological properties, and wettability were investigated. The holistic inter-connected approach that was followed allowed an in-depth physical understanding of the nanofluid response to different preparation conditions. Results show a significant influence of aggregates formation and dynamics on nanofluids, which can be summarized in the following points:

- Nanofluid saturation can explain the plateau in nanofluid characteristics when the nanoparticle concentration increases to higher values.
- Nanofluid samples with higher sample concentration could show higher sample stability due to their higher viscosity.
- Nanofluid instability can influence the nanofluid viscosity in two distinctive ways (*i.e.*, increase or decrease it) based on aggregation dynamics.
- The aggregate size is directly correlated to the nanofluid degree of shear-thinning.
- Liquid nanolayering and contact line pinning are two valid theories that can be utilized to explain the role of nanoparticles in increasing the nanofluid's contact angle.
- Based on the GRA, nanofluid prepared with mid MWCNT concentration, high sonication time, and low surfactant amount showed optimum characteristics.

Conflicts of interest

There are no conflicts to declare.

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