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CauseMap: fast inference of causality from complex time series

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ABSTRACT

Background. Establishing health-related causal relationships is a central pursuit in biomedical research. Yet, the interdependent non-linearity of biological systems renders causal dynamics laborious and at times impractical to disentangle. This pursuit is further impeded by the dearth of time series that are sufficiently long to observe and understand recurrent patterns of flux. However, as data generation costs plummet and technologies like wearable devices democratize data collection, we anticipate a coming surge in the availability of biomedically-relevant time series data. Given the life-saving potential of these burgeoning resources, it is critical to invest in the development of open source software tools that are capable of drawing meaningful insight from vast amounts of time series data.

Results. Here we present CauseMap, the first open source implementation of convergent cross mapping (CCM), a method for establishing causality from long time series data (\$\ge25\$ observations). Compared to existing time series methods, CCM has the advantage of being model-free and robust to unmeasured confounding that could otherwise induce spurious associations. CCM builds on Takens' Theorem, a well-established result from dynamical systems theory that requires only mild assumptions. This theorem allows us to reconstruct high dimensional system dynamics using a time series of only a single variable. These reconstructions can be thought of as shadows of the true causal system. If reconstructed shadows can predict points from opposing time series, we can infer that the corresponding variables are providing views of the same causal system, and so are causally related. Unlike traditional metrics, this test can establish the directionality of causation, even in the presence of feedback loops. Furthermore, since CCM can extract causal relationships from times series of, e.g., a single individual, it may be a valuable tool to personalized medicine. We implement CCM in Julia, a high-performance programming language designed for facile technical computing. Our software package, CauseMap, is platform-independent and freely available as an official Julia package.

Conclusions. CauseMap is an efficient implementation of a state-of-the-art algorithm for detecting causality from time series data. We believe this tool will be a valuable resource for biomedical research and personalized medicine.

Subjects Bioinformatics, Mathematical Biology, Computational Science, Coupled Natural and Human Systems

Keywords Causality, Open source software, Time series methods, Dynamical systems, Personalized medicine

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INTRODUCTION

Establishing health-related causal relationships is a pivotal objective in biomedical research. Yet, the interdependent non-linearity of biological systems often impedes a thorough understanding of causal dynamics. Existing and forthcoming time series data will likely play an important role in taming this complexity. Traditional cross-sectional sampling have the limitation that they may average out non-linear patterns by pooling heterogeneous signals across subjects. Long time series from a single source, on the other hand, can allow us to understand dynamic and context-specific patterns of change.

We are just beginning to grasp the biomedical relevance of such a dynamical systems perspective. Consider, for example, the human microbiome. Dysbiosis in the gut has been implicated in, e.g., irritable bowel disease (IBD), obesity, diabetes, asthma, anxiety, and depression (*Foster & McVey Neufeld, 2013*; *Arrieta et al., 2014*). Meanwhile, recent studies on microbiome dynamics have found that the ecological makeup of the human microbiome is dynamic and individual-specific. These dynamics may also interact with pathogens in interesting and therapeutically important ways. For example, there is evidence that ecological time series dynamics within the body may play a role in the progression from HIV to AIDS (*Vujkovic-Cvijin et al., 2013*).

Complex, dynamically evolving interdependent systems such as the microbiome pose a significant challenge to existing time series methods. Several metrics exist for detecting static non-linear relationships. These include: Spearman rank correlation, (*Spearman*, 1904), distance correlation (*Székely & Rizzo*, 2009), and mutual information content (*Kullback & Leibler*, 1951). Causal relationships, on the other hand, can be examined using methods such as time-lagged regression, instrumental variables, and dynamical Bayesian networks (*Granger*, 1969).

These causal methods are heavily model-based, however. As a result, they often falter when examining arbitrary non-linear or context-dependent relationships. Furthermore, the approaches mentioned above cannot adequately handle feedback loops, and they frequently generate both false positives and false negatives due to the influence of unmeasured confounders (*Sugihara et al.*, 2012). These are significant liabilities, particularly in biomedicine, where relationships are usually embedded within a broad network of incompletely observed interactions.

In this paper, we present the first publicly available, open source implementation of convergent cross mapping (CCM), a model-free approach to detecting dependencies and inferring causality in complex non-linear systems (even in the presence of feedback loops and unmeasured confounding; *Sugihara et al.*, 2012). CCM derives this power from explicitly capturing time-dependent dynamics through a technique known as state-space reconstruction (SSR). SSR has demonstrated utility for problems as diverse as wildlife management and cerebral autoregulation (*Vanderweele & Arah*, 2011). In practice, this analysis typically requires at least 25 data points, measured with relatively high accuracy and with sufficient density to capture system dynamics. One benefit of this approach is that, unlike most causal inference methods, the performance of CCM improves for increasingly non-linear systems. In addition, CCM can properly disentangle

causal relationships that involve feedback loops, provided that strong forcing from external variables does not overwhelm the dynamics of the relationships of interest.

CCM leverages the fact that time series can be viewed as projections of higher-dimensional system dynamics (*Sugihara et al.*, 2012). As a logical result of this property, the time series of individual variables must contain information about the full causal system. Causal dynamics (conceptualized as the state space, or manifold) can then be reconstructed using individual time series. These reconstructions can be thought of as shadows of the true causal system. If the shadows reconstructed from distinct variables can be used to predict points from each other's time series, we can infer that these variables provide views of the same causal system and so are causally related. Since these relationships are fundamentally asymmetric, this test can also establish the directionality of causation.

Further details on CCM are available in the Supplemental Information of this paper, as well as in that of *Sugihara et al.* (2012). Additional explanatory resources can also be accessed through the project website (http://cyrusmaher.github.io/CauseMap.jl).

MATERIALS AND METHODS

Convergent cross mapping algorithm

Consider time series of hypothetical variables X and Y. Convergent cross mapping (CCM) employs time-lagged coordinates of each of these variables to produce shadow versions of their respective source manifolds. To illustrate, suppose the time series for X were $\{1, 2, 3, 4\}$. Reconstructing a two-dimensional shadow manifold for X using a time lag of one would yield the following path: $(2,1) \rightarrow (3,2) \rightarrow (4,3)$. For sufficiently long time series, the path of this shadow manifold is expected to reveal important properties of the full causal system.

We will refer to the shadow manifolds reconstructed from X and Y as M_x and M_y , respectively. To test whether X causes Y, CCM applies the following logic: because manifold reconstruction preserves important structural components of the original system (i.e., the Lyapunov exponents; *Casdagli et al.*, 1991), if X causes Y, then time points that are close in M_y should also be close in M_x . Since M_x is constructed from lags of the observations of X, the points that are close in M_x will also have similar values in the corresponding time series. Therefore, if X causes Y, then M_y can tell us which observations of X should best predict a given held-out point from X. Furthermore, predictability should increase with the number of manifold points in M_y that are considered.

Assessing predictive skill

To test whether X causes Y, M_y is used to infer the points in X that will best predict a given held-out point from X. We measure this performance using predictive skill, quantified by $\rho_{\rm ccm}$ as follows. To begin, we withhold a point from X that we will then attempt to predict. We use M_y to infer the points in M_x that will be closest to this point of interest. This is accomplished using relative pairwise distances of corresponding points in M_y . We then perform a weighted average of the corresponding observations in X using exponential weights derived from these pairwise distances in M_y . We similarly produce predicted values

Table 1 Runtime versus time series length. Results are presented for one to six catenations of the dataset presented in Fig. 1. Runtime values are for comprehensive parameter optimizations on a single 2.6 GHz Intel Core i7 processor.

Time series length	Runtime (s)
71	10.2
142	40.4
213	116.6
284	317.2
355	534.7
426	1080.5

for each held-out point in X. ρ_{ccm} is then calculated as the Pearson correlation between held-out and predicted points. The cross validated nature of this measure serves to reduce over-fitting with respect to the model's tuning parameters described below. To examine whether the signal converges as expected for a causal relationship, these steps are repeated using increasing numbers of points from M_{γ} and M_{x} .

CauseMap is fast

CauseMap implements CCM in Julia, a high-performance programming language designed for facile technical computing. By way of an intelligent JIT (just in time) compilation, Julia offers much of the speed of low-level, low-productivity languages like C, while also providing the ease of use and platform independence of much slower high-level languages like Python, R, or Matlab.

At the core of CauseMap is the calculation of distances between a large number of manifold points in potentially high dimensional spaces. To optimize efficiency, CauseMap precomputes all necessary manifolds and pairwise distances using a state-of-the-art, BLAS-based protocol (for benchmarks, see: https://github.com/JuliaStats/Distance.jl).

To illustrate the speed of CauseMap as a function of time series length, in Table 1 we present the runtimes for successive catenations of the time series presented in Fig. 1. For our time series of length 71, CauseMap finishes in approximately 10 s. For a time series of over 400 observations, CauseMap still finishes in less than 20 min on a single CPU. Note that for this dataset, predictive skill was nearly perfect at a time series length of 213. This calculation finished in less than two minutes. Through this example, we observe that CauseMap can reach superb levels of performance long before increasing time series length generates significant computational challenge.

Tuning parameter values aid causal interpretation

Beyond the speed and comparative simplicity resulting from cutting-edge JIT compilation, CauseMap offers a number of conveniences and performance enhancements. For CCM, it is particularly important to optimize two tuning parameters: E and τ_p .

E is the number of dimensions of the reconstructed shadow manifold. If E_{max} is the optimal embedding dimension, Whitney's Theorem tells us that the dimensionality of the

full causal system is generically between $(E_{\text{max}} - 1)/2$ and E_{max} , inclusive (*Eelles & Toledo*, 1992; *Deyle & Sugihara*, 2011). Note though that E_{max} is usually unknown and must be inferred from the data. This procedure is described in the following section.

 τ_p denotes the time delay of the causal effect of interest. By examining the optimal values of these two parameters, we may place bounds on the number of variables involved in the full causal system, gain insight into the timeframe of causal effects, and obtain a built-in sensitivity analysis of the final results. The estimation of these parameters is described below.

CauseMap optimizes and visualizes tuning parameters

E and τ_p are optimized by multiple iterations of cyclic coordinate descent. This process chooses the values of E and τ_p that optimize the predictive skill of the model for held-out data points. Typically convergence of the cross map signal as a function of the time series length (L) alone is taken as the practical criterion for causality. However, measuring the dependence of this signal on E and τ_p is also useful for evaluating whether the result is suitably specific with respect to the assumed structure of the causal system. CauseMap therefore also includes a plotting function to visualize the dependence of the predictive skill $(\rho_{\rm ccm})$ on L, as well as on the joint values of E and τ_p .

Interpretation of output

The systematic increase of predictive skill (ρ_{ccm}) with L constitutes a practical, qualitative criterion for causality ($Sugihara\ et\ al.,\ 2012$). Generally, non-causal ρ_{ccm} curves are flat with respect to L, while ρ_{ccm} signals associated with causal signals show striking convergence given sufficient data. One exception is in the case of strong external forcing. An outside variable can introduce a cross map correlation between two quantities if it exerts a sufficiently strong influence over both. We speculate that such situations can produce ρ_{ccm} values that, compared to true causal relationships, have a noisier or less interpretable dependence on E and τ_p . Furthermore, it is necessary to inspect the dependence of the cross map correlation on the joint distribution of E and τ_p in order to properly understand the meaning of the maximal values of these two variables. Note that for high throughput analyses, convergence with respect to E and sensitivity to E and E0 could be assessed with, e.g., relative difference- and entropy-based measures, respectively.

CauseMap is easy to use

Beyond the tuning parameters mentioned above, CCM requires one to specify a range of library sizes, as well as the window of time points for which cross mapping should be performed. Valid values for these parameters depend in turn on E and τ_p . To reduce complexity for the user, CauseMap calculates intelligent defaults for these parameters, while also offering the option of specifying them directly.

Caveats and considerations

The strengths and weaknesses of CCM make it nicely complementary to the existing tools for causal inference. Unlike most algorithms for this task, the performance of CCM improves for increasingly non-linear systems. However, this capacity depends upon

relatively long time series. CCM requires at least 25 data points, measured with relatively high accuracy and with sufficient density to capture system dynamics.

There are also theoretical and practical limitations to the types of relationships that CCM can disentangle. For example, if both X and Y are almost entirely determined by a third variable Z, we would be at risk of inferring a spurious relationship between X and Y (as we would be with any other causal inference method). If the forcing from Z is relatively weak, however, CCM is expected to provide a lower false positive rate relative to other methods (*Sugihara et al.*, 2012).

CCM also examines relationships between variables in a pairwise fashion. However, by leveraging dynamical systems theory, it has the ability to measure possibly bidirectional causal effects even in the presence of unmeasured confounding. Finally, CCM performs best with complete data sampled at regular intervals. This is particularly important for inferring the time lag of the causal effect. This limitation can be partially addressed through filtering or appropriate interpolation of input data.

RESULTS AND DISCUSSION

To demonstrate CauseMap's functionality and performance, we examined the predator–prey relationship between *Paramecium aurelia* and *Didinium nasutum* (*Heskamp et al.*, 2013). Observations were collected every 12 h for 30 days, yielding a total of 60 data points (*Veilleux*, 1976). Plotted in Fig. 1 is the CauseMap visualization of the dependence of predictive skill (ρ_{ccm}) on L, E, and τ_p . In Fig. 1A, we observe convergence in ρ_{ccm} with respect to E, the number of data points used for prediction of held-out observations. This convergence is a practical criterion for causality and the source of the name *convergent* cross mapping.

The interpretation of this result is that the causal relationship between *P. aurelia* and *D. nasutum* is bi-directional. That is, the number of predators influences the number of prey, and vice-versa. Furthermore, relative strengths of convergence indicate that the top-down influence of the predator (*D. nasutum*) is stronger than the bottom-up influence of the prey (*P. Aurelia*). As pointed out by *Sugihara et al.*, this finding is consistent with experimental results and illustrates the ability of CCM to investigate asymmetrical bi-directional coupling in non-linear systems.

Figures 1B and 1C show the dependence of the max $\rho_{\rm ccm}$ on E (the dimensionality of the reconstructed system), and the supposed time lag of the causal effect (τ_p). Overall, the patterning of these heatmaps demonstrates that max ρ_{ccm} has a reasonable and moderately specific dependence on the dimensionality of the reconstructed system (E) and on the time lag of the causal effect (τ_p). We expect this built-in sensitivity analysis to rule out some cases of spurious convergent signal caused by external forcing. In addition, this analysis can alert the researcher when alternative combinations of E and τ_p explain the data approximately as well as the optimal values of E and τ_p .

For the system presented in Fig. 1, while the max ρ_{ccm} is relatively insensitive to the assumed dimensionality, the best-performing τ_p values correspond to either immediate causal effects, or those delayed by five days. Note that $\tau_p = 5$ corresponds to the principal

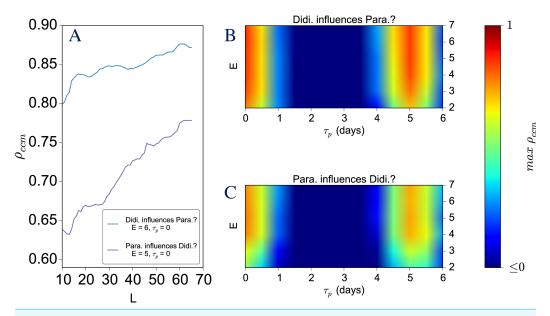


Figure 1 An example visualization from CauseMap using abundances of *Paramecium aurelia* and *Didinium nasutum*. See Supplemental Information for more information on this system. (A) For optimal parameter values, the convergence of the cross-map correlation with library size. (B–C). The dependence of the maximum cross-map correlation on assumed dimensionality (measured by E) and the time lag of the causal effect (measured by t_p). Note that the second maximum at $t_p = t_p$ corresponds to the principal frequency of the t_p aurelia and t_p in a series, as determined by Fourier transform analysis.

frequency of the *Paramecium aurelia* and *Didinium nasutum* time series, as determined by Fourier transform analysis (see Supplemental Information for further details). This suggests that the peak at $\tau_p = 5$ is artifactual. Therefore, we are able to infer from the data that, as we would expect, predator and prey populations exert bidirectional effects in real-time.

Performance

Approximately 100 CCM evaluations were conducted to produce Fig. 1. These calculations finished in approximately 10 s on a single 2.6 GHz processor. Each of these evaluations involved the prediction of over 60,000 points, compiled across all sliding windows of libraries of varying lengths. At an average of 1.7 ms per prediction, this is a highly efficient implementation given the computational challenges.

Dependence of predictive skill on time series length

CauseMap is designed to examine causal relationships in time series with 25 or more observations. In order to illustrate the effects of shorter time series, we thinned the *Paramedium-Didinium* data set by one-half and by one-third, yielding series of 30 and 20 observations, respectively. Figure 2 demonstrates the effect of this reduction on the convergence of predictive skill (ρ_{ccm}). We see that the 1/2 thinned data set recapitulates the trends observed in the full series, including the relative magnitudes of ρ_{ccm} between the mappings of *Didinium* to *Paramecium* and vice versa. The 1/3 thinned sample set, on the other hand, no longer demonstrates convergence. In addition, compared to the longer sets,

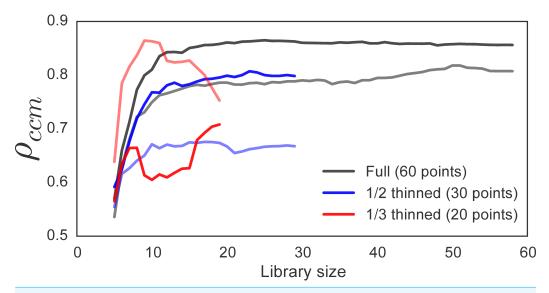


Figure 2 The effect of time series length on $ρ_{\rm ccm}$ convergence. Black, blue, and red lines illustrate $ρ_{\rm ccm}$ for the full, 1/2 thinned, and 1/3 thinned datasets, respectively. For a given color, darker lines show $ρ_{\rm ccm}$ for the test of whether *Didinium* abundance influences *Paramecium* abundance. Lighter lines examine the converse.

it exhibits the opposite trend in relative predictive skill between the two mappings. Patterns in max ρ_{ccm} versus E and τ_p are approximately conserved, however (Fig. S1).

This example illustrates that CCM performance drops off sharply between 20 and 30 data points. This behavior is partially due to the fact that the predictive skill for a given library size is averaged across sliding windows of that size. As time series get shorter, there are fewer windows of appropriate size across which to average, so the estimate for predictive skill becomes much less reliable.

POTENTIAL BIOMEDICAL APPLICATIONS

Despite its requirement for relatively long time series (>25 observations), CauseMap has the advantage of requiring only a single time series for each variable. In dynamical systems with widely varying or context-specific behavior, this would allow researchers to draw conclusions that are tailored to a given patient, for example. Rather than acting on population averages, biomedical researchers would be free to fully personalize therapy to the unique biology and ecology of the patient. One example of this is in the treatment of microbiome dysbiosis. Imbalances in the microbiome have been implicated in, e.g., irritable bowel disease (IBD), obesity, diabetes, asthma, anxiety, and depression. While fecal transplantation therapy is effective in treating specific types of dysbiosis, next generation therapeutics may offer a blend of purified strains, tailored to the gut ecology of the patient. We believe CauseMap has the potential to be a valuable tool for designing such breakthrough therapies.

Additional examples include understanding patient-to-patient variability in drug response using time series metabolomics, and examining the basis of, for example, influenza seasonality using global time series. We expect that such applications will continue to proliferate as the costs of data collection decrease over the coming years.

For this reason, we believe it is vitally important that the biomedical research community have access to an efficient implementation of CCM that is user-friendly and available for immediate field testing.

Planned future development

In future versions, we will include S-map calculations to evaluate the non-linearity of the causal system. We will also add a bootstrap-based procedure for library selection, as opposed to the current approach using sliding windows. This has been shown to reduce the effect of secular trends on the cross map correlation (H Ye & G Sugihara, pers. comm., 2014). In addition, we will re-implement the plotting functionality in Julia, removing the requirements of Python and matplotlib for visualization. Finally, we will design Python and R wrappers for CauseMap functions so that our codebase can be easily leveraged from those environments as well. User suggestions will also be considered as we decide how best to develop the tool.

CONCLUSIONS

CauseMap provides a fast, user-friendly implementation of CCM, a powerful new method for exploring dependencies and even establishing causality in complex, highly non-linear datasets with many unobserved variables. We believe that CCM holds a great deal of promise for a wide range of applications, including personalized microbiome therapy and metabolic dynamics analysis. As novel time series datasets continue to emerge, it is our hope that CauseMap will allow researchers to uncover interesting and biomedically actionable causal relationships using this next-generation time series method.

List of abbreviations

CCM Convergent cross mapping SSR State space reconstruction

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ADDITIONAL INFORMATION AND DECLARATIONS

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Competing Interests

The authors declare there are no competing interests.

Author Contributions

- M. Cyrus Maher conceived and designed the experiments, performed the experiments, analyzed the data, contributed reagents/materials/analysis tools, wrote the paper, prepared figures and/or tables, reviewed drafts of the paper.
- Ryan D. Hernandez contributed reagents/materials/analysis tools, wrote the paper, prepared figures and/or tables, reviewed drafts of the paper.

Data Deposition

The following information was supplied regarding the deposition of related data: All examples and associated data are available in the project repository (https://github.com/cyrusmaher/CauseMap.jl).

Supplemental Information

Supplemental information for this article can be found online at http://dx.doi.org/10.7717/peerj.824#supplemental-information.

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