



Evolution of resilience in protein interactomes across the tree of life

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Phenotype robustness to environmental fluctuations is a common biological phenomenon. Although most phenotypes involve multiple proteins that interact with each other, the basic principles of how such interactome networks respond to environmental unpredictability and change during evolution are largely unknown. Here we study interactomes of 1,840 species across the tree of life involving a total of 8,762,166 protein–protein interactions. Our study focuses on the resilience of interactomes to network failures and finds that interactomes become more resilient during evolution, meaning that interactomes become more robust to network failures over time. In bacteria, we find that a more resilient interactome is in turn associated with the greater ability of the organism to survive in a more complex, variable, and competitive environment. We find that at the protein family level proteins exhibit a coordinated rewiring of interactions over time and that a resilient interactome arises through gradual change of the network topology. Our findings have implications for understanding molecular network structure in the context of both evolution and environment.

protein–protein interaction networks | molecular evolution | ecology | network resilience | network rewiring

The enormous diversity of life shows a fundamental ability of organisms to adapt their phenotypes to changing environments (1). Most phenotypes are the result of an interplay of many molecular components that interact with each other and the environment (2–5). The study of life’s diversity has a long history and extensive phylogenetic studies have demonstrated evolution at the DNA sequence level (6–8). While studies based on sequence data alone have demonstrated evolution of genomes, mechanistic insights into how evolution shapes interactions between proteins in an organism remain elusive (9, 10).

DNA sequence information has been used to associate genes with their functions (11), determine properties of ancestral life (12, 13), and understand how the environment affects genomes (14). Despite these advances in understanding DNA sequence evolution, little is known about basic principles that govern the evolution of interactions between proteins. In particular, evolution of DNA and amino acid sequences could lead to pervasive rewiring of protein–protein interactions and create or destroy the ability of the interactions to perform their biological functions.

The importance of protein–protein interactions has spurred experimental efforts to map all interactions between proteins in a particular organism, its interactome, namely the complex network of protein–protein interactions in that organism. A large number of high-throughput experiments have reported high-quality interactomes in a number of organisms (15–19). Because interactomes underlie all living organisms, it is critical to understand how these networks change during evolution (20, 21) and elucidate key principles of their structure.

Here, we use protein interactions measured by these large-scale interactome mapping experiments and study the evolutionary dynamics of the interactomes across the tree of life. Our protein interaction dataset contains a total of 8,762,166

physical interactions between 1,450,633 proteins from 1,840 species, encompassing all current protein interaction information at a cross-species scale (*SI Appendix, section S1 and Table S4*). We group these interactions by species and represent each species with a separate interactome network, in which nodes indicate a species’ proteins and edges indicate experimentally documented physical interactions, including direct biophysical protein–protein interactions, regulatory protein–DNA interactions, metabolic pathway interactions, and kinase–substrate interactions measured in that species. We integrate into the dataset (22) the evolutionary history of species provided by the tree of life constructed from small subunit ribosomal RNA gene sequence information (12) (*SI Appendix, section S2*). Using network science, we study the network organization of each interactome, in particular its resilience to network failures, a critical factor determining the function of the interactome (23–26). We identify the relationship between the resilience of an interactome and evolution and use this resilience to uncover relationships with natural environments in which organisms live. Although the interactomes are incomplete and biased toward much-studied proteins and model species (*SI Appendix, section S1 and Fig. S7*), our analyses give results that are consistent across taxonomic groups, that are not sensitive to network data quality or network size change (*SI Appendix, section S8 and Fig. S8*), and indicate that our conclusions will still hold when more protein interaction data become available.

Significance

The interactome network of protein–protein interactions captures the structure of molecular machinery that underlies organismal complexity. The resilience to network failures is a critical property of the interactome as the breakdown of interactions may lead to cell death or disease. By studying interactomes from 1,840 species across the tree of life, we find that evolution leads to more resilient interactomes, providing evidence for a longstanding hypothesis that interactomes evolve favoring robustness against network failures. We find that a highly resilient interactome has a beneficial impact on the organism’s survival in complex, variable, and competitive habitats. Our findings reveal how interactomes change through evolution and how these changes affect their response to environmental unpredictability.

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Results

Modeling Resilience of the Interactome. Natural selection has influenced many features of living organisms, both at the level of individual genes (27) and at the level of whole organisms (13). To determine how natural selection influences the structure of interactomes, we study the resilience of interactomes to network failures (23, 25, 26). Resilience is a critical property of an interactome as the breakdown of proteins can fundamentally affect the exchange of any biological information between proteins in a cell (Fig. 1A). Network failure could occur through the removal of a protein (e.g., by a nonsense mutation) or the disruption of a protein–protein interaction (e.g., by environmental factors, such as availability of resources). The removal of even a small number of proteins can completely fragment the interactome and lead to cell death and disease (4, 5) (*SI Appendix, section S5.1 and Table S3*). Disruptions of interactions can thus affect the interactome to the extent that its connectivity can be completely lost and the interactome loses its biological function and increases the risk of disease (5).

We formally characterize the resilience of an interactome of a species by measuring how fragmented the interactome becomes when all interactions involving a fraction f of the proteins (nodes) are randomly removed from the interactome (Fig. 1A). The resulting isolated network components then determine the interactome fragmentation. A network component is a connected subnetwork of the interactome in which any two nodes can reach each other by a path of edges. The smaller the network component is, the fewer nodes can be reached from any given node in the component. To characterize how the interactome fragments into isolated components we use the Shannon diversity index (28–31), which we modify to ensure that the resilience of interactomes with different numbers of proteins can be compared (Fig. 1B and *SI Appendix, section S5.2*). In particular, when the interactome G is subjected to a network failure rate f , it is fragmented into a number of isolated components of varying sizes (*SI Appendix, Fig. S1*). We quantify connectivity of the resulting fragmented interactome G_f by calculating the modified Shannon diversity on the resulting set of isolated components. Let $\{C_1, C_2, \dots, C_k\}$ be k isolated components in G_f . The modified Shannon diversity of G_f is then calculated as the entropy of $\{C_1, C_2, \dots, C_k\}$ as

$$H_{\text{msh}}(G_f) = -\frac{1}{\log N} \sum_{i=1}^k p_i \log p_i, \quad [1]$$

where N is the number of proteins in the interactome and $p_i = |C_i|/N$ is the proportion of proteins in the interactome G that are in component C_i . We can interpret p_i as the probability of seeing a protein from component C_i when sampling one protein from the fragmented interactome G_f . That is, Eq. 1 quantifies the uncertainty in predicting the component identity of a protein that is taken at random from the interactome. Finally, we use the normalization factor $1/\log N$ because it corrects for differences in the numbers of proteins in the interactomes and ensures that interactomes of different species can be compared. The range of possible H_{msh} values is between 0 and 1, where these limits correspond, respectively, to a connected interactome in which any two proteins are connected by a path of edges and a completely fragmented interactome in which every protein is its own isolated component. If the fragmented interactome has one large component and only a few small broken-off components, then the modified Shannon diversity is low, providing evidence that the interactome has network structure that is resilient to network failures (23) (*SI Appendix, Fig. S2*). In contrast, if the interactome breaks into many small components, it becomes fragmented, and its modified Shannon diversity is high (*SI Appendix, Fig. S2*),

indicating that the interactome is not resilient to network failures.

To fully characterize the interactome resilience of a species we measure fragmentation of the species' interactome across all possible network failure rates (*SI Appendix, Fig. S3*). Consider the interactome of the pathogenic bacterium *Haemophilus influenzae* and the interactome of humans, which have different resilience (Fig. 1C). In the *H. influenzae* interactome, on removing small fractions of all nodes many network components of varying sizes appear, producing a quickly increasing Shannon diversity. In contrast, the human interactome fragments into a few small components and one large component whose size slowly decreases as small components break off, resulting in Shannon diversity that increases linearly with the network failure rate (Fig. 1C). Thus, unlike the fragmentation of the *H. influenzae* interactome, the human interactome stays together as a large component for very high network failure rates, providing evidence for the topological stability of the interactome. In general, the calculation of modified Shannon diversity over all possible network failure rates f yields a monotonically increasing function that reaches its minimum value of 0 at $f = 0$ (i.e., a connected interactome) and its maximum value of 1 at $f = 1$ (i.e., a completely fragmented interactome) as the interactome becomes increasingly fragmented with increasing network failure rate f (*SI Appendix, section S5.3 and Fig. S3*). We therefore define resilience of interactome G as one minus the area under the curve defined by that function,

$$\text{Resilience}(G) = 1 - \int_0^1 H_{\text{msh}}(G_f) df, \quad [2]$$

which takes values between 0 and 1; a higher value indicates a more resilient interactome.

Resilience of Interactomes Throughout Evolution. We characterize systematically the resilience of interactomes for all species in the dataset (Fig. 1D and *SI Appendix, Table S5*). We find that species display varying degrees of interactome resilience to network failures (Fig. 1E). At a global, cross-species scale, we find that a greater amount of genetic change is associated with a more resilient interactome structure [locally weighted scatterplot smoothing (LOWESS) fit; $R^2 = 0.36$; Fig. 1F], and this association remains strong even after statistical adjustments for the influence of many other variables (*SI Appendix, section S8*). The more genetic change a species has undergone, the more resilient is its interactome. The evolution of a species, which is represented by the total branch length from the root to the leaf taxon representing that species in the tree of life (12), thus predicts resilience of the species' interactome, providing empirical evidence that interactome resilience is an evolvable property of organisms (26). This finding also suggests that the structure of present-day interactomes reflects their history or that interactomes must have a certain structure because that structure is well suited to the network's biological function. From an evolutionary standpoint, this finding points in the direction of topologically stable interactomes, which suggests that evolutionary forces may shape protein interaction networks in such a way that their large-scale connectivity, i.e., the network's biological function, remains largely unaffected by small network failures as long as the failures are random.

We also find that species from the same taxonomic domain have more similar interactome resilience than species from different domains ($P = 6 \cdot 10^{-11}$ for bacteria against eukaryotes; see *SI Appendix, Fig. S10* for comparisons between other taxonomic groups). Furthermore, the degree of interactome resilience is significantly higher than expected by chance alone (*SI Appendix, Fig. S9*); that is, in a similar random network of identical size and degree distribution ($P = 5 \cdot 10^{-12}$), indicating that naturally occurring interactomes have higher

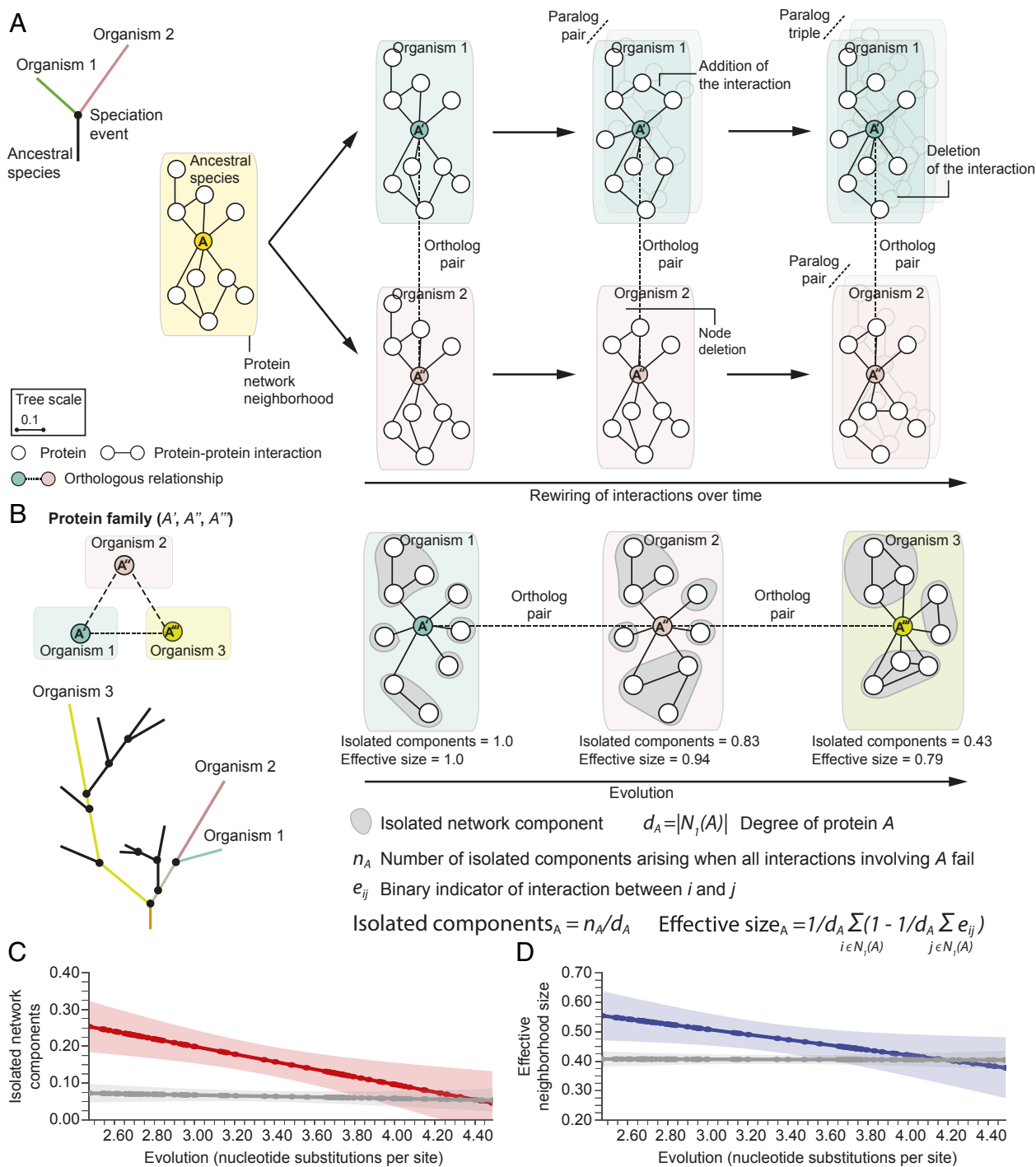


Fig. 3. Evolution mitigates local network structural changes in protein interactomes. (A) A hypothetical phylogenetic tree illustrates a speciation event that gives rise to two lineages according to the speciation-divergence model (11) and leads to present-day organisms “1” (green) and “2” (pink). In this example, a single ancestral protein A that was present in the ancestral species gives rise to proteins A' and A'' upon speciation; A' and A'' form an orthologous protein pair. As the two newly arising species diverge and protein sequences evolve, protein network neighborhoods (SI Appendix, Fig. S4) in their interactomes can rewire independently over time. Shown are also in-paralogs, proteins which arise through gene duplication events in species 1 and 2 after speciation. (B) A hypothetical protein family with three protein members (A' , A'' , A'''), each from a different organism. In the phylogenetic tree, organism 1 is located at the tip of the lineage with the shortest branch length, whereas organism 3 is in the lineage with the longest branch length in the tree. We represent the protein family by a sequence of orthologous proteins ordered by the branch length of proteins' originating species (SI Appendix, section S3). We then characterize the network neighborhood of each protein in the family by calculating two network metrics (SI Appendix, Fig. S5). Isolated components are given by the degree-adjusted number of connected components in the neighborhood that arise when the central protein is removed from the interactome (gray) (SI Appendix, section S6). The neighborhood size down-weighted by the redundancy of local interactions gives the effective size of the neighborhood (SI Appendix, section S6). (C and D) The number of isolated network components and the effective size of protein neighborhoods both decrease with evolution ($P = 3 \cdot 10^{-8}$ and $P = 0.03$, respectively; Spearman's ρ rank correlation), suggesting that local interaction neighborhoods rewire via a coordinated evolutionary mechanism. Lines in C and D show the LOWESS fit of median-aggregated network metric values for 81,673 proteins from 2,224 protein families; color bands indicate 95% confidence band for the LOWESS fit; gray lines show random expectation.

evolution. These structural changes in the neighborhoods suggest a molecular network model of evolution (Fig. 3B): For orthologous proteins in two species, as the evolutionary distance between the species increases, the proteins' local network neighborhoods become increasingly different and the neighborhood becomes more interconnected in the species that has undergone more genetic change.

Network Rewiring of Protein–Protein Interactions. To study evolutionary mechanisms of structural changes in the interactomes, we investigate network motifs (34, 35). We first identify orthologous protein pairs from evolutionarily close species (*SI Appendix, section S3*), resulting in 2,485,564 protein pairs, which we then use to calculate interaction rewiring rates (IRRs) for selected network motifs (Fig. 4A). We calculate the number of times each motif appears in each protein neighborhood and derive the IRR by comparing the motif occurrences between the interactomes of the older and the younger species of each protein pair (*SI Appendix, section S7.1*). We find strong statistical evidence that network motifs rewire during evolution ($P < 10^{-33}$ for all network motifs; Fig. 4B), suggesting that rewiring of interactions is an important mechanism for the evolution of interactomes. For example, proteins in evolutionarily older species on average participate in a factor of 0.861 fewer protein–protein interactions compared with proteins in evolutionarily younger species (IRR = -0.215 ; Fig. 4B). This significant negative correlation between a protein's number of interactions and the protein's evolutionary age confirms earlier studies of *Saccharomyces cerevisiae* (36). We also find that square motifs of interactions become more common in protein neighborhoods during evolution (IRR = 0.016; Fig. 4B). A range of biological evidence (18, 37, 38) supports this positive rate of change in the number of square motifs: From a structural perspective (38), protein–protein interactions often require complementary interfaces; hence two proteins with similar interfaces share many of their neighbors. However, they might not interact directly with each other, which manifests in the interactome as a square motif of interactions (see *SI Appendix, Fig. S6* for an illustration of interaction interfaces recognizing the binding sites in proteins). Evolutionary arguments following gene duplication (18) reach the same conclusion; proteins with multiple shared interaction partners are likely to share even more partners and thereby produce new square motifs of interactions. To test the predictive power of our motif-based model of structural network changes, we estimate the size of the whole human interactome by extrapolating the *S. cerevisiae* interactome, using IRRs from Fig. 4B (*SI Appendix, section S7.3*). Assuming one splice isoform per gene, we predict the number of interactions in humans to be $\sim 160,000$. This prediction is in surprisingly good agreement with three previous estimates of the size of the human interactome, which range from 150,000 to 370,000 interactions (15, 17, 39) and have proved crucial in establishing the complexity of the human interactome (19).

Discussion

Our analyses reveal how protein–protein interaction networks change through evolution and how changes in these networks affect phenotypes and organismal response to environmental complexity. This systematic investigation of protein–protein interaction networks from an evolutionary perspective was enabled by a dataset of interactomes, consisting of protein–protein interaction networks from 1,840 species. To date, most evolutionary analyses of biological networks have focused on a small number of organisms with high-coverage protein–protein

interaction data, such as *S. cerevisiae*, *Mus musculus*, and humans. This is because interactomes mapped by unbiased tests of all possible pairwise combinations of proteins on the same platform remain scarce, an important limitation of the present study. Furthermore, experimentally documented protein interactions are currently subject to a high number of false positives and negatives. As more protein interaction data are collected, and more genomes become available, the generalizability of our findings can be further evaluated. However, our results are consistent across both different subsets of protein interaction data (*SI Appendix, Table S2*) and different phylogenetic lineages (*SI Appendix, Fig. S10*) and are not explained by many possible genomic and network confounders (*SI Appendix, section S8, Fig. S8, and Table S1*), thus providing confidence that our key findings cannot be attributed to biases in the datasets.

Interactome resilience is an important aspect of our study. The resilience measures fragmentation of the interactome into isolated components and thus represents a global measure of the interactome's topological stability. Beyond fragmentation, there are other possible modifications of the interactome that could alter the network's biological function without necessarily disconnecting the network (40–42). As more detailed information about functions of individual proteins in the interactome (43), as well as dynamic protein-expression data (44), becomes available, our measure of interactome resilience could be adapted to give a more complex definition of resiliency, which might yield more detailed evolutionary predictions. Additionally, information on how protein–protein interactions change dynamically both in time and space (45–47) might reveal how topological stability of the interactome depends on large-scale interactome connectivity as well as on the interactome's dynamic properties (40).

Our study presents an additional paradigm for evolutionary studies by demonstrating that interactomes reveal fundamental structural principles of molecular networks. Our findings highlight evolution as an important predictor of structural network change and show that evolution of a species predicts resilience of the species' interactome to protein failures. The findings offer quantitative evidence for the biological proposition that an organism that has undergone more genetic change has a more resilient interactome, which, in turn, is associated with the greater ability of the organism to survive in a more complex, variable, or competitive environment. Our findings can also help clarify the mechanisms of how interactomes change during evolution, why currently observed network structures exist, and how they may change in the future and facilitate the extrapolation of functional information from experimentally characterized proteins to their orthologous proteins in poorly studied organisms.

Materials and Methods

Detailed description of data, statistical methodology, and additional analyses are provided in *SI Appendix*.

Code and Data Availability. Software implementation of statistical methodology is publicly available at snap.stanford.edu/tree-of-life. All data used in this paper, including the processed interactomes, are shared with the community and available from snap.stanford.edu/tree-of-life.

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