MicroRNA-Mediated Positive Feedback Loop and Optimized Bistable Switch in a Cancer Network Involving miR-17-92

Yichen Li^{1,2}, Yumin Li^{1,2}*, Hui Zhang³, Yong Chen^{2,3}*

1 School of Life Sciences, Lanzhou University, Lanzhou, China, 2 Key Laboratory of Digestive System Tumors, Lanzhou, China, 3 Institute of Theoretical Physics, Lanzhou University, Lanzhou, China

Abstract

MicroRNAs (miRNAs) are small, noncoding RNAs that play an important role in many key biological processes, including development, cell differentiation, the cell cycle and apoptosis, as central post-transcriptional regulators of gene expression. Recent studies have shown that miRNAs can act as oncogenes and tumor suppressors depending on the context. The present work focuses on the physiological significance of miRNAs and their role in regulating the switching behavior. We illustrate an abstract model of the Myc/E2F/miR-17-92 network presented by Aguda et al. (2008), which is composed of coupling between the E2F/Myc positive feedback loops and the E2F/Myc/miR-17-92 negative feedback loop. By systematically analyzing the network in close association with plausible experimental parameters, we show that, in the presence of miRNAs, the system bistability emerges from the system, with a bistable switch and a one-way switch presented by Aguda et al. instead of a single one-way switch. Moreover, the miRNAs can optimize the switching process. The model produces a diverse array of response-signal behaviors in response to various potential regulating scenarios. The model predicts that this transition exists, one from cell death or the cancerous phenotype directly to cell quiescence, due to the existence of miRNAs. It was also found that the network involving miR-17-92 exhibits high noise sensitivity due to a positive feedback loop.

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* E-mail: liym@lzu.edu.cn (YL); ychen@lzu.edu.cn (YC)

Introduction

MicroRNAs (miRNAs) are small, endogenous non-coding RNA molecules, typically ~ 22 nucleotides (nt) in length. Traditionally, miRNAs were thought to be an undesirable class of small RNAs that only served a relevant function in nonmammalian species. In 1993, Ambros and colleagues found that the lin-4 gene does not encode a protein product, but gives rise to a 61-nt precursor gene that matures to a more abundant 22-nt transcript in the model organism Caenorhabditis elegans [1]. The Ruvkun laboratory observed that lin-14 protein synthesis is regulated post-transcriptionally and that lin-14 levels are inversely proportional to those of lin-4 RNA [2]. Thus, they revealed the first miRNA and mRNA target interaction, where the lin-4 RNA has sequence complementarity to the 3' untranslated region of the lin-14 gene. Currently, there have been over 10000 miRNAs identified and published in public databases (miRBase database, http://microrna. sanger.ac.uk). These miRNAs have been identified in animals, plants, and viruses and are involved in the regulation of a variety of biological processes.

By post-transcriptionally down-regulating gene expression, it is currently predicted that miRNAs regulate up to $\sim 30\%$ of human genes and their targets include signaling proteins, enzymes, and transcription factors [3]. The diversity and abundance of miRNA targets result in miRNAs playing important roles in nearly all fundamental cellular processes, such as developmental timing, cell proliferation, apoptosis, stem cell maintenance, differentiation, signaling pathways, and pathogenesis including carcinogenesis [4–6]. It is remarkable that approximately half of the known miRNAs are located inside or close to fragile sites and in minimal regions of loss of heterozygosity, minimal regions of amplifications, and common breakpoints associated with cancer [7]. Recent studies have shown that miRNAs are involved in the initiation and progression of a variety of cancers and can act as oncogenes or tumor suppressors depending on the tissue and the expression level of their targets [8,9].

Clearly, miRNAs cannot independently perform a single task in cells. Instead, miRNAs regulate cellular networks as network components in many cellular functions. Indeed, it is thought that miRNAs lead to more effective noise buffering [10,11]. In addition, Aguda et al. found that miR-17-92 plays an oncogenic role in one setting but suppresses tumor formation in a different scenario [12]. Here, there are two determinative factors, the definition of the postulated cancer zone and the switch behaviors of the system dynamics [12]. Note that the Myc/E2F/miR-17-92 network is composed of two feedback loops: a positive self-feedback loop for protein module (Myc/E2F) and a negative loop between the miRNA and the protein (Figure 2 in [12] or Figure

S1). This network appears a typical bistable switch behavior and a one-way switch corresponding to the bistability and monostability, respectively [12]. In fact, a single positive feedback loop without miRNA is enough to realize a bistable switch. Consequently, it is interesting to investigate the physiological significance of miRNAs or why cancer networks require miRNA regulation and the contributions from miRNAs.

To examine this issue, we focus here on an abstract model of the Myc/E2F/miR-17-92 network described by Aguda et al. [12] and present simulations with experimental parameters. Our results show that the existence of miRNA improves the ability of the bistable switches in the systems. For the single-loop switch, there is a so-called fast/slow loop to describe the fast/slow response kinetics for the activation and inactivation [13]. Normally, the single fast-loop switch achieves more rapid responses. Moreover, we also found that miRNA can mediate the system between a fast loop and a slow loop due to the different rate coefficients of degradation for miR-17-92 and E2Fs/Myc (in general, miRNAs is more stable than protein), and can diversify the response behavior of the system to the input stimulus. Especially, the undamped relaxation oscillation behavior of the system indicates a possible digital regulation mode. Furthermore, the switching behaviors of the network involving miR-17-92 is both sensitive to stimuli and resistant to fluctuations in stimulus. Our finding show that miRNAs play a key role in the possibility to achieve a sensitive robustness in biological systems.

Results

Model Formulation

By following the mammalian G1-S regulatory network, the essential abstract structure of the Myc/E2F/miR-17-92 network is illustrated in Figure 1. P denotes the protein module (Myc and E2Fs), and M is the miRNA cluster module (see Ref. [12] or Figure S1 for the detailed reduction process). The positive feedback loop in module P represents an autocatalytic process, which is also inhibited by module M. At the same time, P induces the transcription of M.

The dynamics of the respective concentrations of P and M are described by the following ordinary differential equations [12]:

$$\frac{d[P]}{dt} = \alpha_P + \left(\frac{k_P[P]^2}{\Gamma_1 + [P]^2 + \Gamma_2[M]}\right) - \beta_P[P]$$
(1)



Figure 1. Schematic illustration of the cancer network involving miR-17-92, E2F, and Myc. *P* and *M* denote the protein module (Myc and E2Fs) and the miRNA cluster, respectively. doi:10.1371/journal.pone.0026302.q001

$$\frac{d[M]}{dt} = \alpha_M + k_M[P] - \beta_M[M], \qquad (2)$$

where [P] and [M] denote the concentrations of P and M, respectively. α_P describes the constitutive protein expression from the signal transduction pathway in the extracellular medium and is experimentally controlled in the cell culture medium. α_M depicts the P-independent constitutive transcription of M. β_P and β_M are the rate coefficients of degradation. k_P is the constant of protein expression, and k_M is the rate constant. Γ_1 is the coefficient of protein expression, and Γ_2 is a measure of the miRNA inhibition of protein expression.

Under a series of nondimensionalizing processes [12], Eqs. (1) and (2) can be rewritten as:

$$\varepsilon \frac{d\phi}{d\tau} = \alpha + \left(\frac{k\phi^2}{\gamma_1 + \phi^2 + \gamma_2\psi}\right) - \phi \tag{3}$$

$$\frac{d\psi}{d\tau} = 1 + \phi - \psi. \tag{4}$$

Here, $\phi = k_M [P] / \alpha_M$, $\psi = \beta_M [M] / \alpha_M$, and $\tau = \beta_M t$. In general, $\varepsilon = \beta_M / \beta_P$ is less than 1.0 because miRNA is more stable than protein. $k = k_P k_M / (\alpha_M \beta_P)$ is allowed to vary in the range of 2.0-5.0. The experimentally controllable parameters $\alpha = k_M \alpha_P / (\beta_P \alpha_M)$ and $\gamma_2 = \Gamma_2 k_M^2 / (\alpha_M \beta_M)$ vary from 0-0.4 and 0-2.5, respectively [12,14,15]. The last parameter $\gamma_1 = \Gamma_1 k_M^2 / \alpha_M^2$ is set as 1.0. The process to deduce the dimensionless parameters is presented in Text S1.

Steady States, One-way Switches, and bistable Switches

Setting Eqs. (3) and (4) equal to zero and solving for the roots of the algebraic equations from the right-hand sides, we obtain the steady states of the model. As shown in [12], there exists the following relationship:

$$\psi_s = 1 + \phi_s,\tag{5}$$

where ϕ_s and ψ_s represent the steady states of ϕ and ψ , respectively (see the explicit solutions in Text S2). Note that there is only a constant difference between ψ_s and ϕ_s . Moreover, ϕ denotes the dimensionless concentration of protein E2Fs and Myc which is directly correlated with the oncogene or tumor suppression. Thus, we present only the results of ϕ_s and ϕ in the following context.

Due to the positive feedback in module P, this system exhibits a switching behavior, and it has two stable fixed points in the appropriate parameter regime [16]. Steady-state ϕ_s bifurcation diagrams as a function of the parameter α for different values of γ_2 are presented in the top panels of Figure 2. Considering the physiological constraints, the horizontal axis α should be greater than 0 and terminates at a maximal value of 0.4. Clearly, it also shows the oncogenic and tumor suppressor properties of miR-17-92 using the concept of the cancer zone [12] (see Figure 2A–D). Note that ϕ_s decreases with decreasing k for fixed α and γ_2 . Therefore, the positive feedback loop has a similar reversely regulating function of miRNA.

In the case of a bistable switch, the system exhibits hysteresis, which is a property of bistable systems. For convenience, we denote the lower/upper steady state (lower/higher protein



Figure 2. Steady-state bifurcation diagrams of the dimensionless protein concentration ϕ (top panels) and phase diagrams (bottom panels) of switching behavior. The strength of the dimensionless measure of miRNA inhibition γ_2 is increased from 0 to 0.5, 1.0 and 1.5 (from left column to right one). In the bottom panels, the red dashed lines denote the range of the protein expression constant k, from 2.0 to 5.0. Clearly, the system is greatly improved with regard to the ability of the toggle switch with the inclusion of miRNA inhibition γ_2 . Here, $\gamma_1 = 1.0$. doi:10.1371/journal.pone.0026302.g002

concentration) as the off/on state. As an example, for k=2 in Figure 2A, as α increases along the lower stable branch, ϕ_s remains in the off-state until $\alpha = 0.1345$. When α is increased further, the off-state vanishes, and the switch moves towards the upper stable branch, corresponding to the on-state. Then, if we decrease α , the switch moves along the upper stable branch until $\alpha = 0.0$, and then a transition brings the switch back to the off-state. However, the system also acts as an extreme manifestation of hysteresis, a one-way switch, where the on-state branches into the negative domain but is actually eliminated due to a physically meaningful restriction (e.g., k=3, 4, 5 in Figure 2A and k=4, 5 in Figure 2B).

It is well-known a bistable region is enclosed by two saddle-node bifurcation points (the left and right knees of the curves in the top panels of Figure 2). For any α values in this region, the system has two stable solutions and one unstable one. The bottom panels of Figure 2 provide whole phase diagrams of switch behaviors including bistable and one-way switches and a monostable region for different γ_2 values. By increasing the strength of the positive feedback k, the system undergoes a transition from monostability to a bistable switch and then to a one-way switch. The parameter α exhibits a similar influence. When we increase α , the transition begins with a one-way switch to a bistable switch and then to monostablility. As for the dimensionless parameter of miRNA inhibition γ_2 , it reduces the switch region enclosed in the effective domain of k (from 2.0 to 5.0, denoted by two red dashed lines). However, it should be noted that the system only has one-way switching behavior without γ_2 (see Figure 2E). The effective region of the bistable switch is expanded by increasing the strength of γ_2 (Figures 2E–H). Otherwise, for higher values of α , the system is always monostable, but in the case of lower α values, the system produces diverse dynamical behaviors with the existence of γ_2 .

Note that there exists a cancer zone between levels associated with normal cell cycles and apoptosis, a range of Myc and E2F levels with increased probability of inducing cancer (see Figure S2 or Figures 3, 6 in [12]). In general, the off-state denotes cell quiescence and the on-states represent other processes (cell cycles, the cancer zone, and cell apoptosis). In all cases, the regulation imposed by miRNA or the positive feedback loop is confined to the upper state, from cell cycles to the cancer zone and to cell apoptosis or the inverse order (see Figure 2 and Figure 6 in [12]). Considering a perturbation of α along the on-state of a single bistable switch, ϕ_s changes slightly. For $\gamma_2 = 0$, the system almost stavs in the on-state because there only exists the one-way switch (In fact, the probability of transferring to another cell status is also very low. See Figure 2A.) however, for $\gamma_2 > 0$ (the existence of miRNA), it is possible to return to cell quiescence due to the bistable switch (Figures 2B-D). This means that the miRNAs lead to the recurrent process from the on-state to the off-state. Thus, the miRNA provides two possible regulation pathways, from cell apoptosis or the cancer zone to cell quiescence (Figure S3).

Diversification of the Signal-response Behaviors

As shown in Figure 2, the emergence of the inhibition of miRNA γ_2 induces diversification of the system dynamics in the physiological regions of k. In fact, the repression of P by M yields negative feedback (see Figure 1). This system, composed of positive and negative feedback, is a flexible motif that can exhibit various behaviors [17,18]. It has already been shown that the negative feedback makes oscillation possible [19,20]. Here, we show that the system can exhibit diverse signal-response behaviors corresponding to the different regimes of Figures 2F–H.

For any fixed strength of the positive feedback k, the behavior of the system is different for varying γ_2 (see the bottom panels of Figure 2). With k=4.0 and γ_2 ranging from 1.0 to 1.2 and 1.6, Figure 3 shows that the response of the system to the input signal is tuned by γ_2 . The top row shows the time evolution of ϕ under the input stimulus, and the bottom row depicts the corresponding bifurcation diagram of the system. The solid and dashed lines



Figure 3. The dynamical behaviors of the system when increasing the inhibition of miRNA γ_2 . The strength of positive feedback is set at k = 4.0, and the strength of negative feedback γ_2 is increased from 1.0 to 1.2 and 1.6 from left to right. Parameter $\gamma_1 = 1.0$ and $\varepsilon = 0.02$. The upper rows show the time course of the ϕ response to (A and B) the pulse input, $\alpha = 0.17$ for 20 < t < 25 and $\alpha = 0.10$ for others, or (C) a constant stimulus with $\alpha = 0.25$, where the red dashed lines denote the input signal. The lower rows show the corresponding bifurcation diagram, where S_1/S_2 denotes saddle point and H_1/H_2 represents a Hopf bifurcation. Clearly, the system undergoes transitions from bistability to excitability and to relaxation oscillation with increasing γ_2 .

denote stable and unstable steady states, respectively. S_1/S_2 denotes a saddle-node bifurcation and H_1/H_2 represents a Hopf bifurcation. The input stimulus is a pulse with $\alpha = 0.1$ except for when it is 0.16 from time 20 to 25 in Figures 3A and 3B, but it always is constant at $\alpha = 0.25$ in Figure 3C. The initial values used were $\phi = 0.1$ and $\psi = 1.1$.

First, in the case of $\gamma_2 = 1.0$, the system behaves irreversibly. Under the pulse input, the system settles to the on-state and cannot return to the initial off-state (Figure 3A). This behavior is typical of a one-way switch (Figure 3D). As γ_2 is increased to 1.2, the strength of the pulse input is in the range between S_1 and H_1 (Figure 3E). In this case, there are three steady states, but only the lower state (off-state) is stable while the others (the upper and middle ones) are unstable. The system exhibits excitability where ϕ is first driven to the on-state due to the instability from the pulse input and then completely recovers to the original off-state after a short shift (Figure 3B). Thus, the model system also generates a large-amplitude transient pulse to respond to the pulse input.

When γ_2 is further increased and the strength of the constant stimulus is between two Hopf bifurcation points H_1 and H_2 , the system enters into limit-cycle oscillations (see Figures 3C and 3F, and the respective 3-dimension bifurcation in Figure S4). ϕ rises gradually and then drops rapidly after reaching a maximum, and the cycle repeats. As we all know, the undamped relaxation oscillation is a periodic process in which slow smooth change of the state of an object over a finite interval of time is alternated with rapid irregular change of the state during an infinitely short time. Since van der Pol presented the classic example of a onedimensional system having relaxation oscillations [21], such oscillatory processes are observed in many real mechanical, radiotechnical, biological, laser physical etc., objects. So, such an oscillation is a type of undamped relaxation oscillation. Notably there is no time delay in the recent limit-cycle oscillation system. This means that this oscillation resulted from the hysteresis induced by the positive feedback [22,23].

As stated in Figure 3A and 3D, the system exhibits a fundamental phenomenon in nature, the so-called bistability. A bistable system is able to rest in two states, which need not be symmetric. The defining characteristic of bistability is simply that two stable states (minima) are separated by a barrier (local maximum). For example, for an ensemble of particles, the bistability comes from that free energy has three critical points. Two of them are minima and the last is a maximum. However, Figure 3B and 3E display the excitability of the system. Common to all excitable systems is the existence of a rest state, an excited (or firing) state, and a refractory (or recovery) state, such as action potential in neural systems. The system is in the presence of one stable and one or more unstable fixed points. If unperturbed, the system resides in the rest state; small perturbations result only in a small-amplitude response of the system. For a sufficiently strong stimulus (for example, larger than the α value of S_2 in Figure 3E), the system can leave the rest state, going through the firing and refractory states and then comes back to rest again [24].

As illustrated above, with increasing $\gamma_2,$ the system undergoes a transition from bistability to excitability and to undamped relaxation oscillation without a time delay. We suggest that there is a feasible way to produce diverse signal-response behaviors by combining the inhibition of miRNA γ_2 and the experimentally tunable parameter α . Figure 4 presents an overview of the tunability using the phase diagram of the system dynamics in $\gamma_2 - \alpha$ plane with k = 4.0. The bulk diagram is composed of four kinds of dynamics: monostability, bistability, excitability, and undamped relaxation oscillation where the borderlines between these dynamics (solid lines in Figure 4) are saddle-node and Hopf bifurcation points, respectively. We cannot observe the codimension 2 or other higher codimension bifurcations in our studied parameter range. It is obvious that the values of γ_2 and α can be cooperatively tuned in the corresponding regions to achieve desirable behaviors and functions. In fact, when we fix any one parameter in α , k, and γ_2 , the others can perform similar



Figure 4. Bifurcation diagram in the space spanned by α **and** γ_2 **with** k = 4.0, $\gamma_1 = 1.0$. The bulk diagram of the dynamical behavior of the system is composed of four regions: monostability, bistability, excitability, and undamped relaxation oscillation. The red and blue circles on borderlines denote the saddle-node and Hopf bifurcations, respectively.

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synergetic function to achieve the diverse response behaviors (see Figure S5).

Indeed, a single positive feedback loop with ultrasensitivity is able to act as a bistable switch and a single negative feedback loop with a time delay can produce sustained oscillations [25–27]. However a motif assembled by a positive loop and a negative loop not only performs the both functions without changing the topological structure, but also presents excitable behavior. Note that the last two behaviors resulted from the negative feedback loop of miR-17-92 because there can only be one-way switches without miRNAs (Figure 2A). These signal-response behaviors offer diverse regulating options. The oscillation (pulses) could provide potential precise regulation, such as the digital response of p53 to DNA damage [28,29].

Optimized Bistable Switch

According to Eqs. (3–4), the dimensionless parameter ε is a time constant for the activation and inactivation of ϕ and determines whether the switch is fast or slow. Note that $\varepsilon = \beta_M / \beta_P$ is the ratio of the degradation rate for E2Fs and Myc for miR-17-92. Consequently, the switching behavior of the protein concentration from the positive feedback loop can also be represented as interlinked dual-time feedback loops [13,30,31].

Figure 5 illustrates the switch responses of the system for two different time constants $\varepsilon = 0.05$ and 0.25 to a step stimulus with or without fluctuation. The basal strength of the stimulus strength is set at $\alpha = 0.05$, where the system is initially in the off-state, and then jumps to 0.20 at time t = 20, corresponding to the on-state of the system. The panels in the left column denote the stimulus input, where the left bottom panel corresponds to a fluctuating environment described by Gaussian white noise with mean 0 and variance 0.30 (Figures 5A, 5D). The middle and right columns show the response of the switch for $\gamma_2 = 0$ and 0.25, respectively. In all of the cases, the system with a smaller ε increases rapidly at the initial stage and responds much faster than that of the slower loop. The fluctuation amplitude of ϕ for larger ε values is much smaller than that of the faster loop (Figures 5E, 5F). That is, the fast loop is critical for the switching sensitivity, but the slow loop increases the switching stability to resist stimulus fluctuations.

Furthermore, the inhibition of miRNA γ_2 also slows down the switching process, especially near the on-state, and effectively represses fluctuations (Figures 5B and 5C, Figures 5E and 5F).

To clearly investigate the switching robustness to fluctuations in the stimulus, we use the definition of the fraction of transition F_t [17,30]. The system is driven by the same noisy stimulus $\alpha = \alpha_0 [1 + \zeta(t)]$ with different seeds, where $\alpha_0 = 0.16$ and $\zeta(t)$ is Gaussian white noise. Initially, we settled on a population of 2000 cells in the on-state of the system, with some cells that may flip to the off-state due to a noise-induced switch. F_t is defined as the ratio of the number of cells in the transition state to the number of all cells at each time point. Moreover, one can define the time required for F_t to reach the midpoint between its initial and steady-state values as the so-called response time t_r .

Figure 6 displays the time courses of F_t for $\gamma_2 = 1.80$, 1.85, and 1.90. For smaller γ_2 values, it takes a relatively long time for F_t to reach a smaller steady state. We denote F_s as the value of the steady state of F_t . For example, $F_s = 0.238$ and $t_r = 5.40$ for $\gamma_2 = 1.80$, which means that most of cells are still trapped in the on-state for a long time. In the case of $\gamma_2 = 1.90$, $F_s = 0.731$ and $t_r = 3.24$ indicating that a significant number of cells (73.1%) have flipped to the off-state and are taking less time to reach the steady state of F_t .

Furthermore, we show the fraction of transition F_s and the response time t_r as functions of α for different γ_2 and ε values in Figure 7. In the simulations, all 5000 cells initially settled in the onstate. The fluctuation of α follows a Gaussian white noise distribution with variance 0.20. With increasing α , F_s decreases from 1 to 0, but t_r also increases quickly in the case of $F_s=1$. Especially in the flipping region of F_s , t_r decreases when γ_2 increased, as can be similarly observed in Figure 6. These switching behaviors resulted from the binding between the on-state and the off-state decreasing when α or γ_2 increases in the region of the bistable switch (see the dynamic diagram of γ_2 vs α , Figure S6).

Note that ε is 0.05 in the left column of Figure 7 and is 0.10 in the right one. Obviously, for smaller values of ε (fast loop) and larger values of γ_2 , there exists a larger region of α for which almost all cells are trapped in the on-state ($F_s = 1$). In the critical region of α for F_s from 1 to 0, the flipping process with small ε values is less sensitive to α than with larger ones (Figures 7A and 7B). In addition, t_r for small ε values is significantly less than for larger ones (Figures 7C and 7D).

Cellular processes are essentially stochastic and occur in a fluctuating environment [32]. A small perturbation in the stimulus input could be amplified by positive feedback [33,34]. (Sometimes, positive feedback can work as a noise-filtering device [35]). Additionally, noise-induced switching behavior may induce a false decision regarding cell fate (case $\varepsilon = 0.05$ in Figure 5E). By involving the negative feedback loop of miRNAs, the Myc/E2F/miR-17-92 cancer network operates like a dual-time switch interlinked by fast and slow positive loops. The entire system exhibits high noise sensitivity in the off-state due to the rapid responses of the positive loop, which is regulated by the ratio between the miRNA and protein degradation rates (note that $\varepsilon = \beta_M / \beta_P$ is often much less than 1). At the same time, the system is resistant to noise when it is in the on-state as a result of the negative feedback.

Discussion

It has been reported that miR-17-92 behaves as an oncogene and a tumor suppressor depending on different situations [36,37]. For the first time, Aguda et al. analyzed the reduced model of the coupling between the E2F/Myc positive feedback loops and the



Figure 5. Responses of switches to a step stimulus input. (A) The jumping stimulus input from $\alpha = 0.05$ to 0.20 at time t = 20. (B) The responses of the system for a fast loop $\varepsilon = 0.05$ (red) and a slow loop $\varepsilon = 0.25$ (blue), where $\gamma_2 = 0$. (C) The same as (B) but with $\gamma_2 = 1.0$. (D) The same as (A) but with an imposed fluctuation $\alpha = \alpha_0[1 + \xi(t)]$, where $\xi(t)$ is Gaussian white noise with variance 2D = 0.30 and mean 0, and α_0 is the same as in (A). (E–F) The same as (B) and (C), respectively. All simulations used k = 4.0 and $\gamma_1 = 1.0$. doi:10.1371/journal.pone.0026302.q005

E2F/Myc/miR-17-92 negative feedback loop. They showed that miR-17-92 plays a critical role in regulating the protein levels (on/ off). Most important, they demonstrated the parallel oncogenic and tumor suppressor properties of miR-17-92 using the concept, cancer zone (Figure S2 or Figure 3 in [12]). By considering the bistable switch behaviors, Aguda et al. [12] predicted that

increasing miRNA level drives E2F/Myc level in normal cell cycle to enter the cancer zone (oncogene, case a), or drives protein levels to exit cancer zone and enter the cell apoptosis (tumor suppressor, case b), and vice versa (see Figure S2 or Figure 3 in [12]). The reduced abstract model of the Myc/E2F/miR-17-92 network is typically interlinked by positive and negative feedback



Figure 6. Time course of fluctuation-induced escape from the on-state (upper state) to the off-state (lower state). Each time course represents the evolution of the fraction F_t that has transitioned at least once to the off-state, for an ensemble of 2000 cells. Here, the parameters are k = 5.0, $\varepsilon = 0.15$, $\alpha = 0.16$, $\gamma_1 = 1.0$, and a Gaussian white noise with variance 0.30. doi:10.1371/journal.pone.0026302.g006

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Figure 7. Noise tolerance and response features of the systems including the inhibition of miRNA. (A) Steady values of the fraction F_t of transition from the initial on-state to the off-state as a function of α for $\varepsilon = 0.05$. (B) The same as (A) for $\varepsilon = 0.10$. (C–D) The response time t_r vs α for $\varepsilon = 0.05$ and 0.10, respectively. All of the simulations used k = 5.0, $\gamma_1 = 1.0$, and a Gaussian white noise with variance 0.20. doi:10.1371/journal.pone.0026302.g007

loops (Figure 1). A bistable system with interlinked loops has been illustrated in the yeast galactose-utilization network [38,39], the mitogen-activated protein kinase 1,2/protein kinase C signaling network [40,41], circadian clocks [42,43], the eukaryotic cell cycle [44,45], the p53-Mdm2 network [29], and so on. It has been shown that a system with interlinked loops behaves as a tunable motif and performs diverse behaviors [17]. The essential dynamic in the Myc/E2F/miR-17-92 network is a bistable switch, which can be realized only by a positive feedback loop without miRNAs (Figure 2A). Thus, the physiological importance of miRNAs remains unclear. The present work is based on the hypothesis that the miRNAs are essential in optimizing the switching behavior of the Myc/E2F/miR-17-92 network, and we focus on the role of miR-17-92 on the response-signal behavior without or with noise.

In this paper, using simulation parameters that are biologically plausible, we have shown that the system represents various behaviors (monostability, a bistable switch, a one-way switch) instead of a simple one-way switch because of the existence of miR-17-92 (see Figures 2E-H. The bistable region is also larger with miRNA present). As a result, the system is capable of generating a diverse array of signal-response behaviors with suitable combined parameters (Figures 3A-C). Especially, we find that, due to the the existence of miR-17-92, the range (parameter k) of normal cell cycles is enlarged and this transition (from cell death/cancer to quiescence) is probably realized by noise-induced switches. In addition, the response time constant of the protein module can be regulated by the miRNA degradation rate (ε in Figures 5B-C). The Myc/E2F/miR-17-92 network can run as a dual-time switch (interlinked fast and slow positive loops) and appears to be more sensitive to stimuli and resistant to stimulus fluctuations (Figures 5E-F and Figure 6). It means that miR-17-92 can perform efforts to optimize the bistable switch where miR-17-92 confers signaling robustness (to limit undesired signaling fluctuations, buffering effect) and achieves optimal signaling efficacy (balancing effect).

In addition, processes in gene regulatory systems are typically subject to considerable delays induced by underlying biochemical reactions. Time delays in combination with a positive/ negative feedback loop can induce sustained oscillations and multistability [12]. The model of the Myc/E2F/miR-17-92 network should also account for multiple time delays. It has been shown that the inclusion of a long-time delay in a negative feedback loop can generate oscillations and that the addition of a positive feedback loop can increase the oscillation amplitude and widen the stimulus regime for the oscillation, thus promoting the robustness of the oscillations [17,46]. Therefore, it is conjectured that the effect of a time delay would not qualitatively change our results.

Because an individual miRNA usually targets many genes that are involved in various cellular signaling pathways [11], modulations in the level of a single miRNA could eventually affect many pathways at the same time. The miR-17-92 cluster, which comprises six miRNAs (miR-17, miR-18a, miR-19a, miR-20a, miR-19b-1, and miR-92-1), plays an important role in the cell cycle (by targeting the E2F family) [47], apoptosis (by downmodulating the antiapoptotic protein Bim and tumor suppressors PTEN and p21) [48–50], and angiogenesis (activated by c-Myc and VEGF) [51]. In this study, the model is constrained in a network associated with the cell cycle, without considering other networks. It would be worthwhile to construct a large-scale gene regulation network including different biological functions of a small group of miRNAs and to develop potential strategies of miRNA-based therapeutic targets.

Materials and Methods

All numerical bifurcation analyses of the ordinary differential equations were performed with OSCILL 8.28 [52]. The ordinary differential equations and stochastic differential equations were numerically solved and separately integrated using the fourthorder Runge-Kutta scheme and the fourth-order stochastic Runge-Kutta scheme [53,54] in Fortran 95 codes, respectively.

Supporting Information

Text S1 The deduction of the dimensionless parameter ranges. (PDF)

Text S2 The explicit solutions for the steady states of protein and miRNA levels. (PDF)

Figure S1 Reducing process of the Myc/E2F/miR-17-92 network to an abstract model. Solid arrows mean activation and hammerhead means inhibition. (A) Summary of the interactions among the transcription factors Myc, E2F, and miR-17-92 cluster. (B) The first step in the model reduction. (C) The final abstract model is composed of the protein module P (Myc/E2F) and the miRNA module M (miR-17-92). It is also presented in detail in Figures 1 and 2 by Aguda et al. [12]. (EPS)

Figure S2 The schematic diagram of cancer zone. Clearly, the miR-17-92 clusters act as an oncogene or as a tumor suppressor designed by Aguda et al. [12]. (EPS)

Figure S3 The switching behavior between cell statuses corresponding to the transcriptional activities of E2F or Myc. Note that the plausible experimental range of k is $2 \sim 5$. Without the inhibition of miRNAs (left panel), the switch is limited in on-states (cell cycle, cancer, and cell death). Moreover, most of cells are settled on cancer or apoptosis which return back to cell cycles only by decreasing the positive feedback k. For example, the black dashed-line arrows from k = 4 to 2 denotes a regulation from cell death to cell cycles. In the presence of miRNAs (right panel), the protein concentration of steady states ϕ_s is significantly less than that in left panel. So, the range of normal cell cycles is enlarged and the regulation of α is also at work effectively.

References

- Lee RC, Feinbaum RL, Ambros V (1993) The C. elegans heterochronic gene lin-4 encodes small RNAs with antisense complementarity to lin-14. Cell 75: 843–854.
- Wightman B, Ha I, Ruvkun G (1993) Posttranscriptional regulation of the heterochronic gene lin-14 by lin-4 mediates temporal pattern formation in C. elegans. Cell 75: 855–862.
- Bartel DP (2004) MicroRNAs: genomics, biogenesis, mechanism, and function. Cell 116: 281–297.
- Carthew RW (2006) Gene regulation by microRNAs. Curr Opin Genet Dev 16: 203–208.
- Cui Q, Yu Z, Purisima EO, Wang E (2007) MicroRNA regulation and interspecific variation of gene expression. Trends Genet 23: 372–375.
- Kim VN (2005) MicroRNA biogenesis: coordinated cropping and dicing. Nat Rev Mol Cell Biol 6: 376–385.
- Calin GA, Sevignani C, Dumitru CD, Hyslop T, Noche E, et al. (2004) Human microRNA genes are frequently located at fragile sites and genomic regions involved in cancers. Proc Natl Acad Sci USA 101: 2999–3004.
- Garzon R, Calin GA, Croce CM (2009) MicroRNAs in Cancer. Annu Rev Med 60: 167–179.
- 9. Li M, Li J, Ding X, He M, Cheng SY (2010) microRNA and Cancer. The AAPS Journal 12: 309–317.
- Tsang J, Zhu J, van Oudenaarden A (2007) MicroRNAmediated feedback and feedforward loops are recurrent network motifs in mammals. Mol Cell 26: 753–767.
- Inui M, Martello G, Piccolo S (2010) MicroRNA control of signal transduction. Nat Rev Mol Cell Biol 11: 252–263.
- Aguda BD, Kim Y (2008) MicroRNA regulation of a cancer network: Consequences of the feedback loops involving miR-17-92, E2F, and Myc. Proc Natl Acad Sci USA 105: 19678–19683.
- Brandman O, Ferrell JE, Jr., Li R, Meyer T (2005) Interlinked fast and slow positive feedback loops drive reliable cell decisions. Science 310: 496–498.

Especially, it is possible that cells back to quiescence from cancer or apoptosis directly. As an example, for k = 4.5, there exists noise-induced switch from cancer zone to cell quiescence (the red dashed-line arrow). Similarly, the regulation of k can also realize the same function (see the black dashed-line arrow, regulation from k = 5 to one optional value between $2 \sim 4.5$). Here parameter $\gamma_1 = 1.0$.

(EPS)

Figure S4 The 2-dimension phase portraits for $\gamma_1 = 1.0$ and k = 4.0. The systems come into steady states for $\gamma_2 = 1.2$ and (A) $\alpha = 0.1$, (C) 0.15. In the case of $\gamma_2 = 1.6$, the systems appear periodic oscillations for (B) $\alpha = 0.25$ and (D) 0.30. The circles and the solid square denote the initial status ($\phi = 0.10$, $\psi = 1.10$) and the fixed steady states, respectively. The arrows indicate the time evolution of the systems. (EPS)

Figure S5 The diverse signal-response behaviors tuned by the positive feedback k and the miRNA inhibition γ_2 for fixed $\alpha = 0.1$. Note that the oscillation region appears for the high α (normally, $\alpha > 0.20$), but the bistable switch disappears. Parameter $\gamma_1 = 1.0$. (EPS)

Figure S6 The bifurcation diagram spanned by α and γ_2 for k = 5.0 and $\gamma_1 = 1.0$. Obviously, in the region of the bistable switch, the range of α or γ_2 between on-state and off-state decreases with increasing γ_2 (panel A) or α (panel B), respectively. The additional red dashed lines are the drawing borderlines between bistable and one-way switches under different preconditions (for a fixed value of γ_2/α in panel A/B). (EPS)

Author Contributions

Conceived and designed the experiments: YC YML YCL. Performed the experiments: YCL YC HZ. Analyzed the data: YC YML YCL. Wrote the paper: YCL YC.

- Yao G, Lee TJ, Mori S, Nevins JR, You L (2008) A bistable Rb-E2F switch underlies the restriction point. Nat Cell Biol 10: 476–482.
- Khanin R, Vinciotti V (2008) Computational modeling of post-transcriptional gene regulation by microRNAs. J Comput Biol 15: 305–316.
- Xiong W, Ferrell JE, Jr. (2003) A positive-feedback-based bistable 'memory module' that governs a cell fate decision. Nature 426: 460–465.
- Tian XJ, Zhang XP, Liu F, Wang W (2009) Interlinking positive and negative feedback loops creates a tunable motif in gene regulatory networks. Physical Review E 80: 011926.
- Nevozhay D, Adams RM, Murphy KF, Josić L, Balázsi G (2009) Negative autoregulation linearizes the doseresponse and suppresses the heterogeneity of gene expression. Proc Natl Acad Sci U S A 106: 5123–5128.
- Becskei A, Serrano L (2000) Engineering stability in gene networks by autoregulation. Nature 405: 590–593.
- Wolf DM, Arkin AP (2003) Motifs, modules and games in bacteria. Curr Opin Microbiol 6: 125–134.
- 21. van der Pol B (1926) On relaxation-oscillations. Phil Mag 7: 978-992.
- Novak B, Tyson JJ (2008) Design principles of biochemical oscillators. Nat Rev Mol Cell Biol 9: 981–991.
- Tyson JJ, Chen KC, Novak B (2003) Sniffers, buzzers, toggles and blinkers: dynamics of regulatory and signaling pathways in the cell. Curr Opin Cell Biol 15: 221–231.
- Lindner B, García-Ojalvo J, Neiman A, Schimansky-Geiere L (2004) Effects of noise in excitable systems. Phys Rep 392: 321–424.
- Schlicht R, Winkler G (2008) A delay stochastic process with applications in molecular biology. J Math Biol 57: 613–648.
- Barrio M, Burrage K, Leier A, Tian T (2006) Oscillatory regulation of Hes1: Discrete stochastic delay modelling and simulation. PLoS Comput Biol 2: e117.
- Bratsun D, Volfson D, Tsimring LS, Hasty J (2005) Delay-induced stochastic oscillations in gene regulation. Proc Natl Acad Sci U S A 102: 14593–14598.

- Zhang XP, Liu F, Cheng Z, Wang W (2009) Cell fate decision mediated by p53 pulses. Proc Natl Acad Sci U S A 106: 12245–12250.
- Wee KB, Surana U, Aguda BD (2009) Oscillations of the p53-Akt Network: Implications on Cell Survival and Death. PLoS ONE 4: e4407.
- Zhang XP, Zhang C, Liu F, Wang W (2007) Linking fast and slow positive feedback loops creates an optimal bistable switch in cell signaling. Physical Review E 76: 031924.
- Smolen P, Baxter DA, Byrne JH (92009) Interlinked dual-time feedback loops can enhance robustness to stochasticity and persistence of memory. Physical Review E 79: 031902.
- 32. Paulsson J (2004) Summing up the noise in gene networks. Nature 427: 415–418.
- Becskei A, Seraphin B, Serrano L (2001) Positive feedback in eukaryotic gene networks: cell differentiation by graded to binary response conversion. Embo J 20: 2528–2535.
- Blake WJ, Karn M, Cantor CR, Collins JJ (2003) Noise in eukaryotic gene expression. Nature 422: 633–637.
- Hornung G, Barkai N (2008) Noise propagation and signaling sensitivity in biological networks: A role for positive feedback. PLoS Comput Biol 4: e8.
- Mendell JT (2008) myRiad roles for the miR-17-92 cluster in development and disease. Cell 133: 217–222.
- Coller HA, Forman JJ, Legesse-Miller A (2007) Myced Messages: Myc induces transcription of E2F1 while inhibiting its translation via a microRNA polycistron. PLoS Genet 3: e146.
- Acar M, Becskei A, van Oudenaarden A (2005) Enhancement of cellular memory by reducing stochastic transitions. Nature 435: 228–232.
- Ramsey SA, Smith JJ, Orrell D, Marelli M, Petersen TW, et al. (2006) Dual feedback loops in the GAL regulon suppress cellular heterogeneity in yeast. Nat Genet 38: 1082–1087.
- Bhalla US, Iyengar R (2001) Robustness of the bistable behavior of a biological signaling feedback loop. Chaos 11: 221–226.
- Bhalla US, Ram PT, Îyengar R (2002) MAP kinase phosphatase as a locus of flexibility in a mitogen-activated protein kinase signaling network. Science 297: 1018–1023.

- Lee K, Loros JJ, Dunlap JC (2000) Interconnected feedback loops in the neurospora circadian system. Science 289: 107–110.
- Shearman LP, Sriram S, Weaver DR, Maywood ES, Chaves I, et al. (2000) Interacting molecular loops in the mammalian circadian clock. Science 288: 1013–1019.
- Pomerening JR, Kim SY, Ferrell JE, Jr. (2005) Systems-level dissection of the cell-cycle oscillator: Bypassing positive feedback produces damped oscillations. Cell 122: 565–578.
- Pomerening JR, Sontag ED, Ferrell JE, Jr. (2003) Building a cell cycle oscillator: hysteresis and bistability in the activation of Cdc2. Nat Cell Biol 5: 346–351.
- Tsai TY, Choi YS, Ma W, Pomerening JR, Tang C, et al. (2008) Robust, tunable biological oscillations from interlinked positive and negative feedback loops. Science 321: 126–129.
- O'Donnell KA, Wentzel EA, Zeller KI, Dang CV, Mendell JT (2005) c-Mycregulated microRNAs modulate E2F1 expression. Nature 435: 839–843.
- Ventura AG, Young MM, Winslow L, Lintault L, Meissner A, et al. (2008) Targeted deletion reveals essential and overlapping functions of the miR-17-92 family of miRNA clusters. Cell 132: 875–886.
- Xiao C, Srinivasan L, Calao DP, Patterson HC, Zhang B, et al. (2008) Lymphoproliferative disease and autoimmunity in mice with elevated miR-17-92 expression in lymphocytes. Nat Immunol 9: 405–414.
- Petrocca R, Visone MR, Onelli MH, Shah MH, Nicoloso MS, et al. (2008) E2F1-regulated microRNAs impair TGFβ-dependent cell cycle arrest and apoptosis in gastric cancer. Cancer Cell 13: 272–286.
- Dews M, Homayouni A, Yu D, Murphy D, Sevignani C, et al. (2006) Augmentation of tumor angiogenesis by a Myc-activated microRNA cluster. Nat Genet 38: 1060–1065.
- 52. See http://oscill8.sourceforge.net/.
- Kasdin J (1995) Runge-Kutta algorithm for the numerical integration of stochastic differential equations. J Guid Control Dynam 18: 114–120.
- Kasdin J (1995) Discrete simulation of colored noise and stochastic processes and 1/f^a power law noise generation. Proceedings of the IEEE 83: 802–827.