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Conductance fluctuations in InAs quantum wells possibly driven by Zitterbewegung

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The highly successful Dirac equation predicts peculiar phenomena such as Klein tunnelling and Zitterbewegung (ZB) of electrons. From its conception by Erwin Schrödinger, ZB has been considered key in understanding relativistic quantum mechanics. However, observing the ZB of electrons has proved difficult, and instead various emulations of the phenomenon have been proposed producing several successes. Concerning charge transport in semiconductors and graphene, expectations were high but little has been reported. Here, we report a surprisingly large ZB effect on charge transport in a semiconductor nanostructure playing “flat pinball”. The setup is a narrow strip of InAs two-dimensional electron gas with strong Rashba spin–orbit coupling. Six quantum point contacts act as pinball pockets. In transiting between two contacts, ZB appears as a large reproducible conductance fluctuation that depends on the in-plane magnetic field. Numerical simulations successfully reproduced our experimental observations confirming that ZB causes this conductance fluctuation.

In 1930, Erwin Schrödinger¹ found that the free relativistic particle described by the Dirac equation undergoes an oscillatory motion at the speed of light c . This phenomenon, called Zitterbewegung (from German, meaning “trembling motion”; and abbreviated to ZB), originates from the pure quantum nature of relativistic particles, for which the operator corresponding to its velocity does not commute with the Dirac Hamiltonian. This means the velocity, despite long being a most familiar quantity to physicists, is not a good quantum number for free relativistic particles. Although this remarkable nature stimulated much interest among researchers, its estimated amplitude $\hbar/m_0c \sim 386$ fm, and angular frequency $2m_0c^2/\hbar \sim 1.6 \times 10^{21}$ rad/s for electrons, kept it out of experimental reach². Successful ZB emulations have been achieved in entity models, including those with a single trapped ion³ and ultra-cold atoms in Bose–Einstein condensates^{4,5}. However, in more realistic emulations, a clear observation of ZB with electrons in artificial vacua, specifically solids^{6–8}, has been a major open question. In two-dimensional electron systems with Rashba-type spin–orbit coupling (SOC)⁹, ZB is predicted to appear as a meandering of charge density⁶ with relatively large amplitude of more than ten nanometers⁸, which remains barely observable using nanoscale techniques and superfine structures. A possible observation was reported in a mesoscopic device¹⁰.

Here, we report the observation of ZB as a reproducible conductance fluctuation (CF) versus magnetic field in an InAs two-dimensional electron gas (2DEG) fabricated into an open billiard geometry with quantum point contacts (QPCs) as emitters and billiard pockets. However, the experiment resembles pinball played on a flat table (see Fig. 1) rather than as a billiard table, because the table has a considerable number of fixed scatterers (impurities). Using a numerical simulation, this “flat pinball” model was verified and demonstrated to exhibit meandering charge density with CF.

Results

ZB in Rashba model. Let us briefly view how ZB appears in the Rashba model described by the Hamiltonian

$$H = \frac{\mathbf{p}^2}{2m^*} + (\mathbf{a} + \mathbf{b}) \cdot \boldsymbol{\sigma}, \quad \mathbf{a} \equiv \frac{\alpha}{\hbar} \begin{pmatrix} p_y \\ -p_x \end{pmatrix}, \quad \mathbf{b} \equiv \frac{g^*}{2} \mu_B \begin{pmatrix} B_x \\ B_y \end{pmatrix}, \quad \boldsymbol{\sigma} \equiv \begin{pmatrix} \sigma_x \\ \sigma_y \end{pmatrix}, \quad (1)$$

where \mathbf{p} is the electron momentum, m^* the effective mass, α the Rashba SOC parameter, g^* the effective Landé g-factor, μ_B the Bohr magneton, $\mathbf{B} \equiv B_x \hat{x} + B_y \hat{y}$ (with \hat{x} and \hat{y} as unit coordinate vectors) the in-plane magnetic

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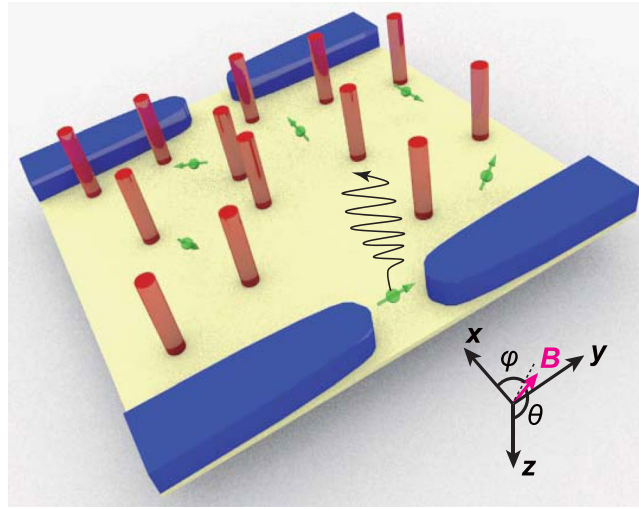


Figure 1. Pinball on a flat table. QPCs (blue) emit electrons (green balls) into a 2DEG (yellow) with impurities (red cylinders) scattering the electrons in the x - y plane. A 3D external magnetic field \mathbf{B} is applied where azimuth ϕ and zenith θ are defined with respect to a z -axis set perpendicular to the x - y plane.

flux density, and $\sigma_{x,y}$ the Pauli matrices. As an initial condition (at $t = 0$), we consider a spin-up electron (the quantization axis is taken along z -axis) and a Gaussian wave packet centred on the origin with central wave vector $\mathbf{k} = k_0 \hat{k}_x$ (a vector of length k_0 directed along the k_x -axis). After an elapsed time t , the expectation value of the y -coordinate for finite $|\mathbf{a} + \mathbf{b}|$ is¹¹,

$$\langle y(t) \rangle = \frac{\alpha (\mathbf{a} + \mathbf{b})_y}{2 [\hbar \omega(k_0)]^2} \{1 - \cos[\omega(k_0)t]\} \equiv y_0 \{1 - \cos(\omega_0 t)\}, \quad (2)$$

where

$$\hbar \omega(k_0) = |\mathbf{a} + \mathbf{b}|, \quad (3)$$

and the spin part of the wavefunction is written as $(\cos[\omega(k_0)t], \sin[\omega(k_0)t])$. The ZB amplitude in equation (2) vanishes in the limit $\alpha \rightarrow 0$ but approaches k_0^{-1} for $\alpha \rightarrow \infty$.

Figure 2(a) depicts the trace of a wave packet oscillating in the y direction according to equation (2) with its spin directions. As is easily understood, in a Rashba system, ZB appears as an electron orbit that meanders with a spin precession around the vector sum of \mathbf{B} and an effective magnetic field originating from the SOC,

$$\mathbf{B}_{\text{eff}} = \frac{2}{g^* \mu_B} \mathbf{a} = \frac{2\alpha}{g^* \mu_B} \begin{pmatrix} k_0 \\ 0 \end{pmatrix}, \quad (4)$$

which is perpendicular to the momentum.

In the above formulae, the difficulties in the detection are apparent in that 1) the ZB amplitude is at most the Fermi wavelength, and 2) to attain this amplitude the ZB frequency in equation (3) should be very high—above 1 THz. We resolve these problems in the experimental setup introduced in the following.

Experimental setup. To create a Rashba system, a 2DEG in a pseudomorphic InAs quantum well was grown by molecular beam epitaxy (see Supplementary Fig. 1 online). The layered structure has asymmetric (In, Ga)As/InAs interfaces in the well region, a structure that is commonly adopted for strong Rashba spin-orbit interaction (SOI)¹². The electron mobility $\mu = 6.6 \times 10^4 \text{ cm}^2/\text{Vs}$ and the sheet carrier concentration $n = 1.1 \times 10^{12}/\text{cm}^2$ were obtained from the longitudinal and Hall resistances. They produced a Fermi wavenumber of $k_F = 2.6 \times 10^8 \text{ m}^{-1}$, which corresponds to wavelength $\lambda_F = 2.4 \times 10^{-8} \text{ m}$. The effects of quantum confinement, wavefunction penetration into (In,Ga)As, and strain are renormalized as a shift in the in-plane effective mass in InAs from a bulk value of $0.023 m_0$ to $0.025 m_0$ ¹³. A Fermi velocity of $v_F = 1.2 \times 10^6 \text{ m/s}$ and a Fermi energy of $E_F = 106 \text{ meV}$, $g^* = 8.6$ ¹⁴ are then obtained. A value for the Rashba parameter $\alpha = 3.6 \times 10^{-11} \text{ eVm}$ is obtained (see Supplementary Fig. 2 online) from the amplitude modulation of the Shubnikov–de Haas (SdH) conductance oscillation¹⁵. These parameter values give an effective magnetic field strength in equation (4) of 38 T, and hence a ZB frequency of 4.6 THz.

The high-frequency problem can be resolved by fixing the ZB in a steady state using spin-polarized electrons. This can be accomplished with a quantum point contact (QPC) on a plateau of quantum conductance $G_q \equiv 2e^2/h$ ^{16–18}, which was predicted theoretically¹⁹ and confirmed experimentally²⁰. Figure 2(c) illustrates the mechanism by which polarized spins of electrons pass through a QPC with Rashba SOI on conductance plateau G_q . The right panel depicts the energy dispersion diagram of the 1D Rashba Hamiltonian. The lines A, B, and C, correspond to positions in the QPC are shown in the left panel. As an electron adiabatically passes through the QPC, its energy shifts sequentially from $A \rightarrow B \rightarrow C \rightarrow B' \rightarrow A'$. During the transition from C to B', the avoided

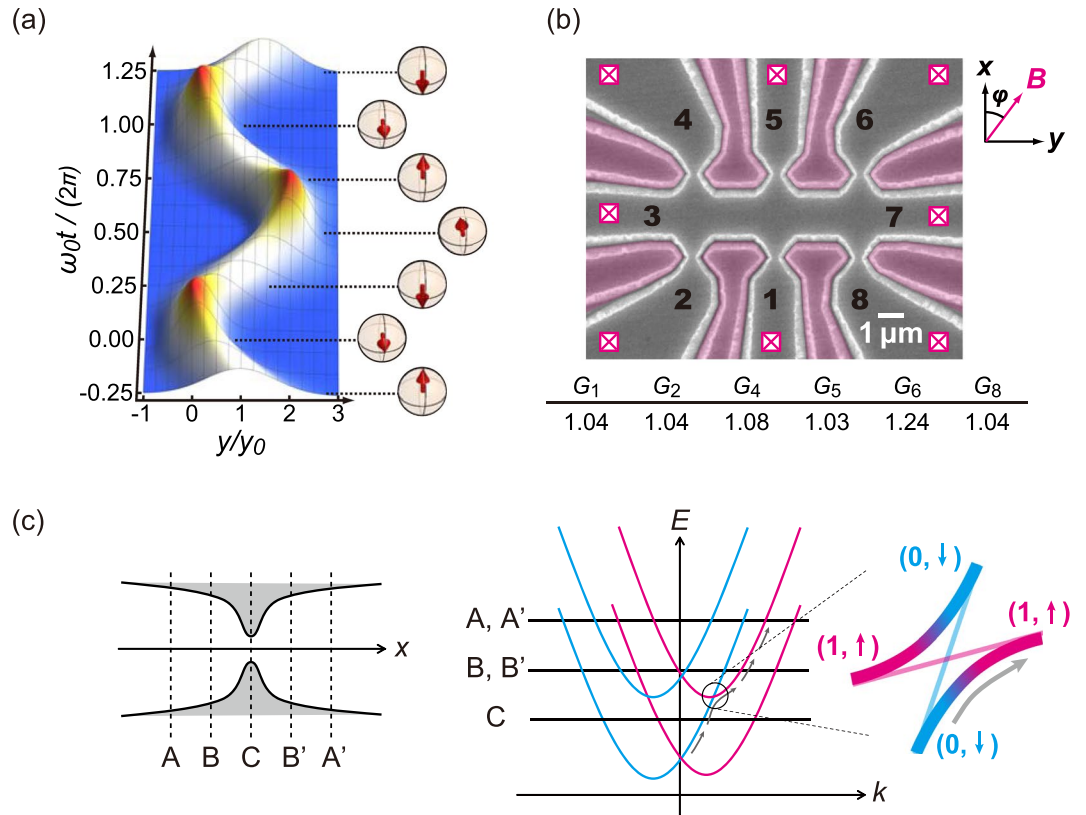


Figure 2. Experimental setup. **(a)** ZB in the Rashba model (for ω_0 and y_0 , refer to equation (2)). An electron wave packet, with spin parallel to the z -axis and an averaged momentum along x at time $t=0$, oscillates along the y -axis in synchrony with the rotating spin in the z - x plane. **(b)** Scanning electron micrograph of the sample with terminals marked. The pink false-colour areas act as gates isolated by trenches to define the QPCs. Conductance of each QPC is listed below the micrograph in units of G_q ($T=55\text{mK}$). **(c)** QPC diagram (left) and dispersion curves for the one-dimensional bands with a Rashba SOI (right). Red and blue curves indicate spin up and spin down, respectively. The magnification of a crossing point reveals a small avoided crossing. Within the spatial movement from C to B, an electron experiences the avoided crossing where the spin is flipped from down to up. A, C, and B indicate the positions of the Fermi energy during traversals—at the outlet, at the middle, and at a point between them, respectively¹⁹.

crossing between $(0, \downarrow)$ and $(1, \uparrow)$ flips the electron spin. As a result of the “one-way spin rotation”, the spin polarization on plateau G_q reaches 0.7. Here, the spin separation of the dispersion branch comes from the $\alpha p_x \sigma_y / \hbar$ term, and the avoided crossing comes from $-\alpha p_x \sigma_y / \hbar$ in (1). The Rashba SOI is thus necessary for spin polarization.

Figure 2(b) shows a scanning electron micrograph of the sample with terminals marked. We take Cartesian coordinates as shown in the figure. The z -axis is perpendicular to the plane. The structure was fabricated by electron beam lithography and dry etching of trenches. The trench-gate technique is commonly used for InAs-based heterostructures²¹ as the Schottky gate technique is unsuitable. The structure consists of a main conducting strip (terminal 3–7) with a width of $2\mu\text{m}$ and six QPCs opened on it. The main problem is that the gates (pink false-coloured regions) are common to adjacent QPCs and hence individual control of the QPC conductance is difficult. Fortunately, after much trial and error, we succeeded in tuning the QPC conductances at around $1.0 G_q$ with all gates grounded (except QPC-6); see Fig. 2(b). The fact that such a coarse tuning was successful indicates that the QPCs are on the $1.0 G_q$ plateau, where the conductance is less sensitive to the gate voltages than in other regions (see Supplementary Fig. 3 online).

Then, in a plot of the conduction through any combination of two QPCs, we emitted spin-polarized electrons into the main strip region in one QPC and collected them through the other one. Because of the electron-hole symmetry, this holds even for conduction paths with QPC-6, in which the polarization may be insufficient because G_6 is slightly higher than $1.0 G_q$ (Fig. 2(b)). However, the effective opening of the QPCs is around 500nm , which is still much wider than the maximum amplitude of ZB. Here, we attempted to solve the problem using scatterers in the strip as amplifiers of the meandering motion. Because the width of the present mean free path $l_0 \sim 1\mu\text{m}$ is about half that of the main strip, the emitted electrons should experience a few scatterings before reaching a pocket. If we approximate such a scattering with a classical scattering for a hard cylindrical wall of radius R , the scattering angle γ given impact factor b_i is $\gamma = 2\cos^{-1}(b_i/R)$. As b_i oscillates via ZB with in-plane magnetic field B with amplitude Δb , the oscillation is amplified by $l_0 \Delta b_i / R$. The potential range R is roughly

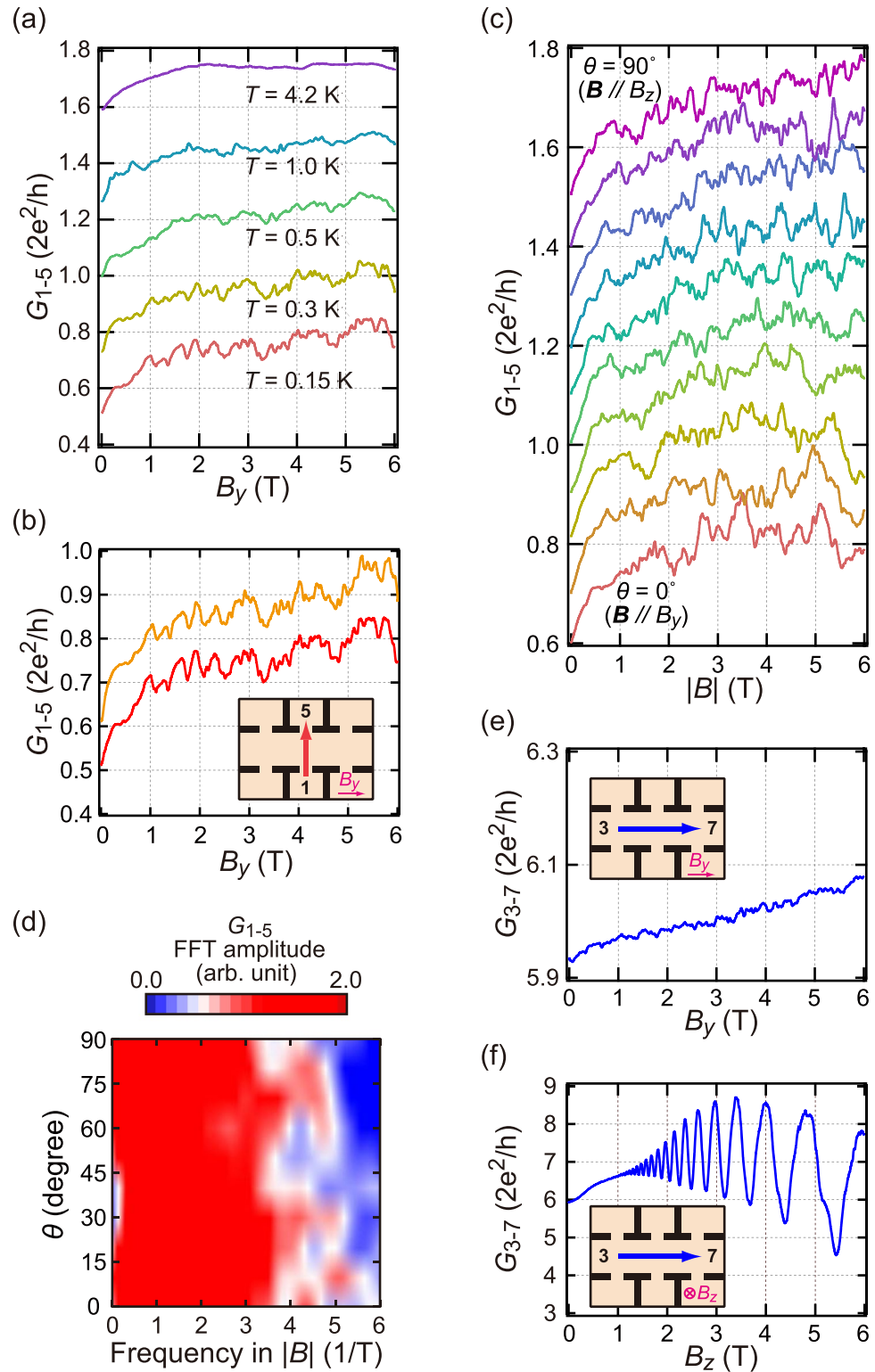


Figure 3. Reproducible conductance fluctuation versus magnetic field. (a) G_{1-5} as a function of B_y for different temperatures with offset $0.2 G_q$. (b) G_{1-5} for two individual magnetic sweeps with offset $0.1 G_q$. The inset shows the terminal configuration. (c) G_{1-5} at 70 mK versus field amplitude $|B|$. The direction of the magnetic field (the zenith angle θ) is rotated from $\theta = 0$ to 90° at azimuth angle $\varphi = 90^\circ$. The steps in the angle and conductance offsets are 10° and $0.2 G_q$, respectively. (d) 2D plot of the FFT amplitude spectrum of the conductance fluctuation versus $|B|$ from 1.5 to 6 T and θ . (e) and (f) G_{3-7} at 70 mK (see inset for the configuration) plotted against B_y and B_z , respectively.

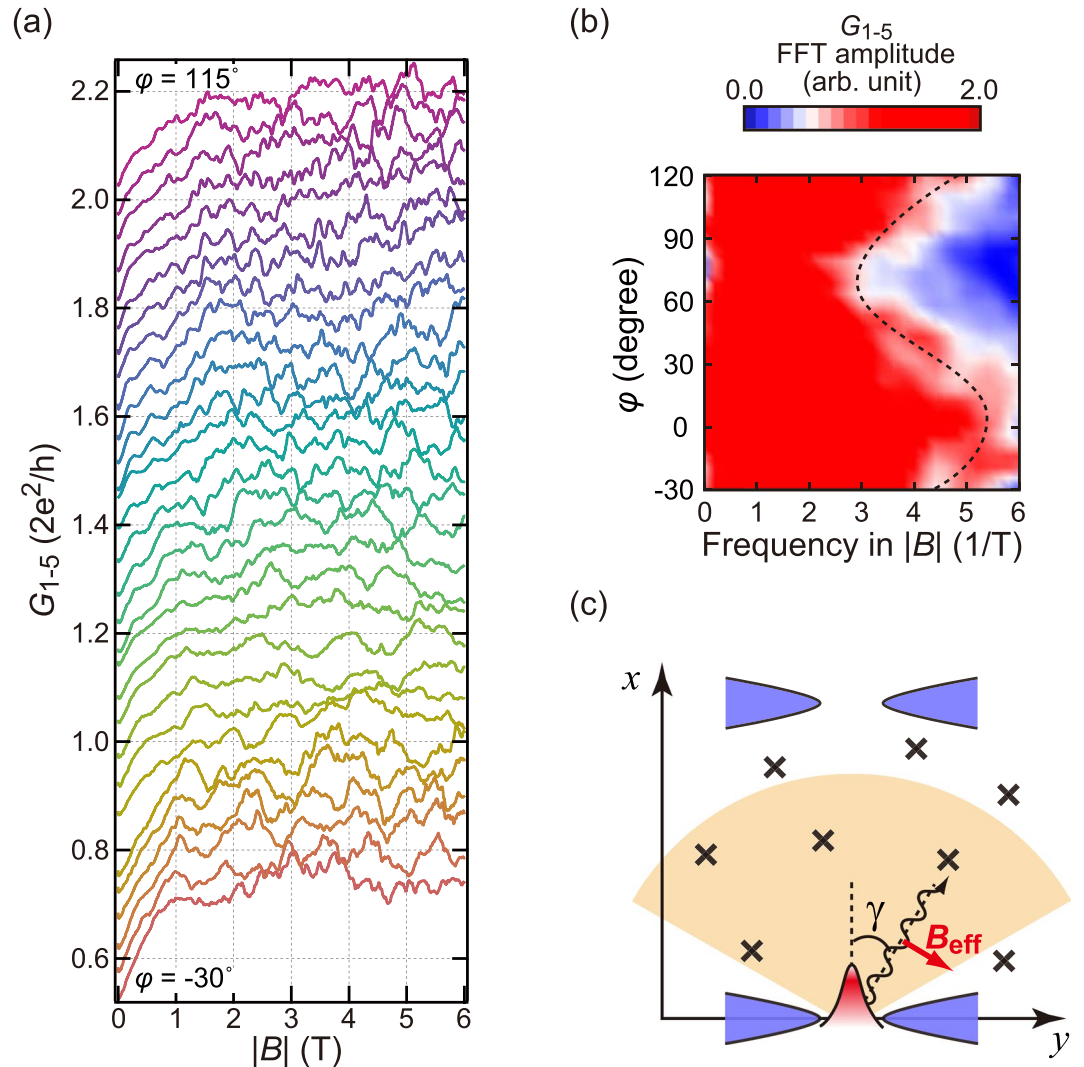


Figure 4. Effect of azimuth angle in the magnetic field on the conductance fluctuation. **(a)** Conductance fluctuation in G_{1-5} at 150 mK versus the magnetic field amplitude $|B|$ for different azimuth angles φ from -30° (bottom) to 115° (top). The step in φ and the offset in G_{1-5} are 5° and $0.05 G_Q$, respectively. **(b)** FFT amplitude spectrum of the conductance fluctuation plotted against $|B|$ ranging from 1.5 to 6 T and φ . The broken line represents the smoothed φ -tendency given in equation (5). **(c)** Schematic of an electron path. Electrons transit over the fan-like beige area.

estimated to be an effective Bohr radius of 34 nm in InAs, which is even smaller than k_F^{-1} . Hence, the amplified ZB can reach an order of $l_0 \sim 1 \mu\text{m}$, which can be resolved with the present QPCs.

This rough classical sketch of scattering needs correcting in a quantum mechanical treatment, in that the spread of the wave packets weakens the amplification. However, as experimentally confirmed in scanning gate microscopy²², the wave packets emitted from a QPC travel for surprisingly long distances without smooth spreading because wave focusing occurs. Therefore, we can expect that semi-quantitatively the above classical analysis holds, and hence the experiment can be viewed as pinball played on a flat table with six pockets. The size of the ball (wave packet) may be larger than the pins (scattering centres), although minor wobbling in the orbits (*i.e.*, ZB) is amplified by the scattering.

Conductance fluctuations. Hereinafter, we denote the two-wire conductance between terminals i and j by G_{i-j} . Figure 3(a) shows the temperature variation of the two-wire conductance G_{1-5} as a function of the in-plane magnetic field along the y -axis B_y . As temperature decreases, aperiodic CFs with increasing B_y became visible and its amplitude increases. CFs are reproducible, that is, for two independent field sweeps at the same temperature, almost the same pattern appears [Fig. 3(b)]. Resemblances are also appreciable between patterns for different temperatures. CFs were observed for an arbitrary pair of electrodes with a QPC connection.

The result indicates that CFs are modulated by an external magnetic field similar to how they appear in the pinball model simulation. However, these features of CFs are also reminiscent of the so-called universal conductance fluctuations (UCF)²³. We therefore checked whether this was possible. Because the applied field is in-plane,

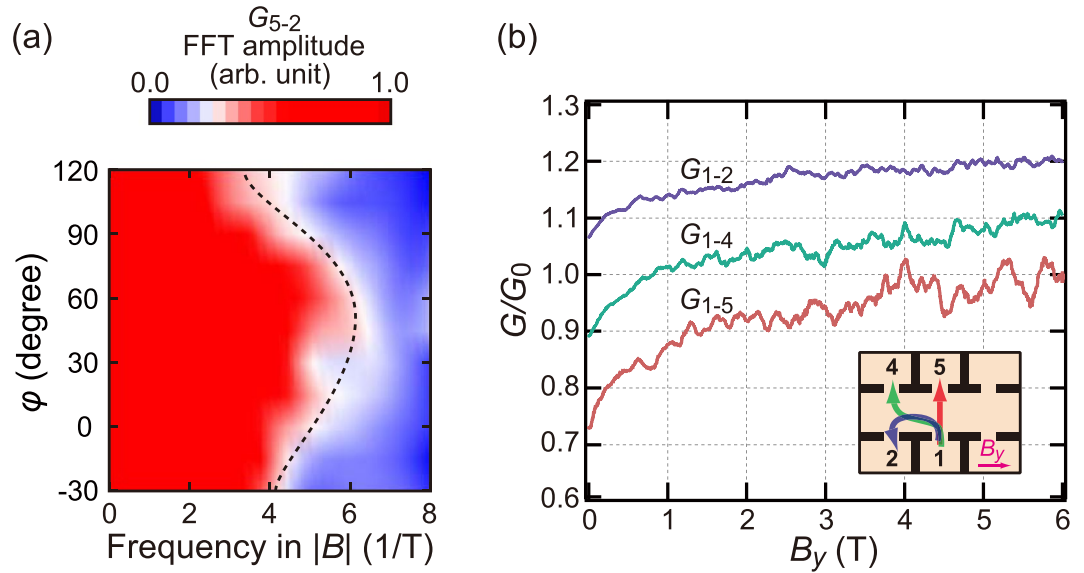


Figure 5. Effect of probe configuration. (a) The same FFT map as Fig. 4(b) but for G_{5-2} at $T = 150$ mK. (b) G_{1-2} , G_{1-4} and G_{1-5} versus B_y , for the configurations illustrated in the inset. The data are normalized by $G_0 = G$ ($B_y = 6$ T) and displayed with offset $0.1 G_q$.

we can eliminate the quantum interference effect through random paths tuned via the Aharonov–Bohm (AB) phase. However, there still remains the possibility of interference in the spin part of the wavefunction, which is modified by a spin precession tuned via the in-plane magnetic field (spin-UCF)²⁴; to eliminate this possibility, we performed the following two experiments.

The first is the rotation of the field direction from in-plane to perpendicular-to-plane (*i.e.*, rotating the elevation angle from 0 to $\pi/2$). The result [Fig. 3(c)] shows there is no significant variation in the amplitude and frequency distributions resulting from pattern changes involving angle [Fig. 3(d)]. This is inconceivable for an interference-type CF because, if there is such a network of spatial interference and the perpendicular component of the field is increased, the AB phase modulation participates in the interference modulation introducing some qualitative and systematic change in CF that stems from the geometric nature of the AB phase. The second is the magnetic response of G_{3-7} , *i.e.*, transport without QPCs (and hence without spin polarization). Figure 3(e,f) displays the result, for which a considerable change is seen from Fig. 3(c), in that in G_{3-7} almost no fluctuation is seen in the in-plane field and an ordinary SdH oscillation appears in the perpendicular field (although the SOI modulation is reduced, probably resulting from loose confinement into the strip). This also indicates that the CFs are not caused by an interference because if such an interference occurred, it inevitably appears in G_{3-7} , the path of which passes through the strip. Note that in the configuration of 1 to 5, the QPCs dominating the absolute value of the conductance are connected in series to the strip. Hence the difference in the average number of conductance channels does not explain the diminishing fluctuation in G_{3-7} .

The source of the CFs is then the ZB modulation of scattering in the pinball system; therefore, we further checked the nature of CFs. The pinball model has two temperature factors; one is the spin polarization at QPCs and the other is the strength of the effective field B_{eff} . The latter is related to Rashba splitting, which is approximately 6 K in the present case. The CF is visible at temperatures of an order-of-magnitude lower. Hence, within the model, the temperature dependence observed [Fig. 3(b)] should come from spin polarization, which depends on the energy diagram inside the QPCs. A derivation of the explicit temperature dependence is difficult, although an order-of-magnitude estimation is reasonable because the effective E_F is lower by an order of magnitude inside the QPCs.

Azimuth angle dependence. Figure 4(a) shows the variation of CF with azimuth angle ϕ for in-plane magnetic field. The fluctuation pattern changes with ϕ depending on its resemblance to neighbouring patterns. A fast-Fourier-transform (FFT) plot of the amplitudes versus ϕ (Fig. 4(b)) indicates some systematic angular dependence on spectral width.

Let us check the correspondence between the pinball model and the experimental results. First we consider electrons emitted from a QPC parallel to the x -axis. Their spins as well as B_{eff} are parallel to the y -axis; the former is concluded from the theory in ref. 16 and the latter from equation (1). Because the spin and the effective field are parallel, there is neither a spin-precession nor a trembling motion.

Next we consider a path with an oblique angle γ to the x -axis [Fig. 4(c)]. The length of $B_{\text{eff}} + B$ is approximated as $B_{\text{eff}} + B \cos \xi$ for $|B_{\text{eff}}| \gg |B|$, where B is the external field strength and $\xi \equiv \pi/2 - \phi + \gamma$ is the angle between B_{eff} and B vectors. The “wavelength” of ZB is estimated as $\lambda_{\text{ZB}} \equiv \pi \hbar^2 / \alpha m^* \approx 270$ nm and the maximum modification of λ_{ZB} with an external field for $B = 6$ T and $\xi = 0$ is 34 nm. This means only a single cycle of meander changes in traversing $2 \mu\text{m}$ in a magnetic field of strength $B = 6$ T.

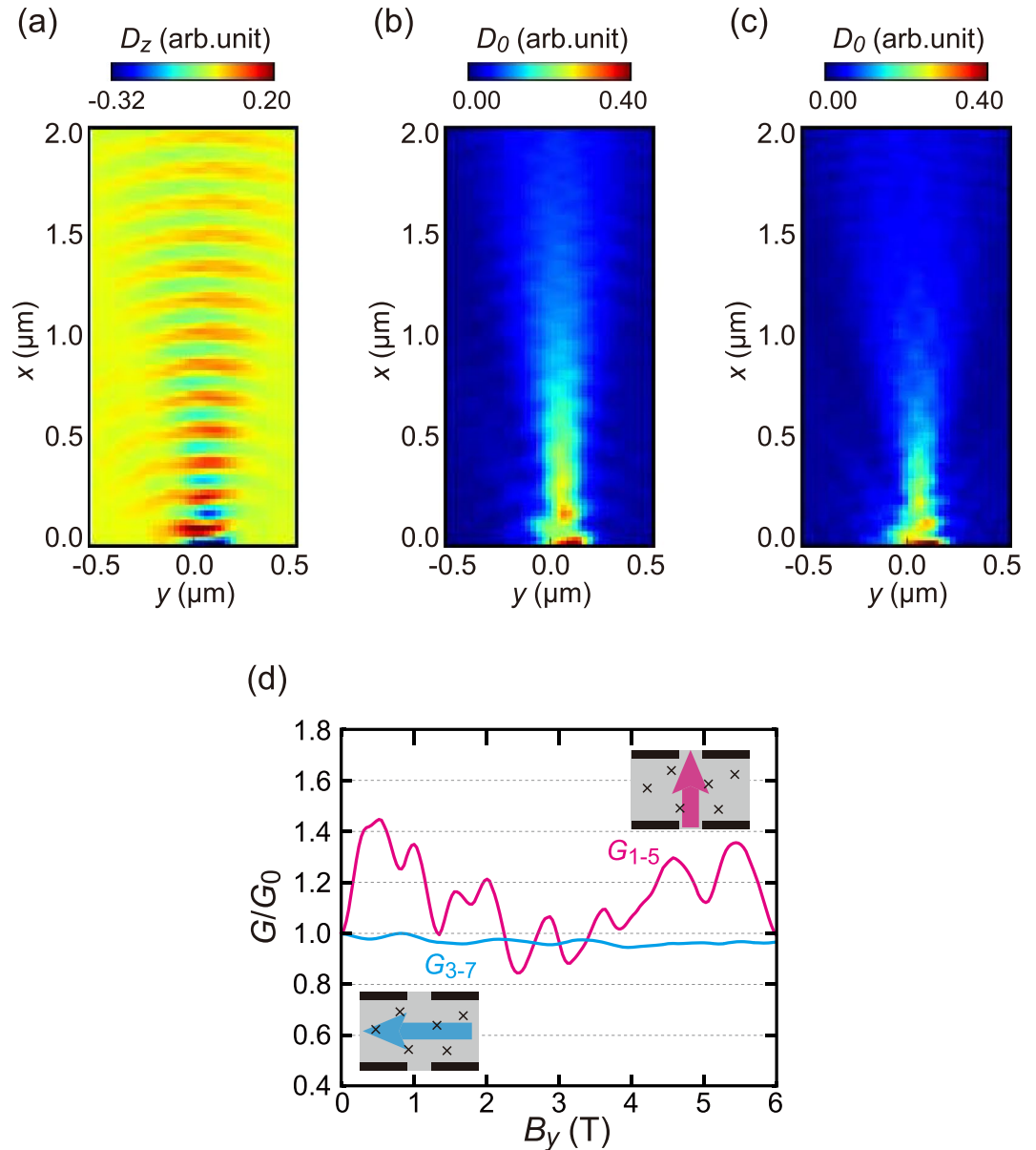


Figure 6. Numerical simulation with ZB reproducing the conductance fluctuation. (a) and (b) Calculated spatial distributions of the z -component of spin (D_z) and the probability amplitude (D_0), respectively, for a two-dimensional electron propagating from the emitter QPC at the origin under a zero-magnetic field. As boundary condition, the spin at the QPC is taken to be polarized along x ; no scattering centre is introduced. (c) The same plot of D_0 as (b), but with $B_y = -3.5$ T. (d) Calculated G_{1-5} (with polarization) and G_{3-5} (without polarization) as a function of B_y . Random scattering centres are introduced. The data are normalized by $G_0 = G(B = 0)$. The probe configurations are illustrated in the insets.

However, this does not mean maximum frequency $1/6 \text{ T}^{-1}$ is expected in the CF. As noted the magnetic field change of 6 T on average corresponds to the change of single cycle in the ZB. The width of the strip is designed to be about twice the electron mean free path and many of the electrons traversing across it experience single scattering, which angularly amplifies the ZB. Hence N scatterings inside the fan of electron diffraction (the beige region in Fig. 4(c)), there should appear N to $2N$ such conductance peaks within the 6 T field, forming a fluctuation pattern. The density and sharpness of the conductance peaks increase for channels with more scatterings, whereas peak heights decrease. In the FFT power spectra, such gradual tailing to high frequencies is actually observed. In the conduction from terminal 5 to 1, the paths should distribute around $\gamma = 0$. Hence, we made the further approximation $B \cos \xi \sim -B \cos \gamma \sin \phi$. Moreover, the φ -dependence of the power spectral width W_p is roughly

$$W_p(\varphi) \propto \frac{l_0}{\lambda_{ZB}^2} \left| \frac{\Delta \lambda_{ZB}}{\Delta B} \right| = l_0 \frac{\pi g^* \mu_B}{v_F} |\sin \varphi|, \quad (5)$$

where l_0 is the averaged ZB path length. Although the approximation is very coarse, equation (5) suggests that W_p takes a maximum at $\varphi = 90^\circ$ and a minimum at $\varphi = 0^\circ$. In Fig. 4(b), the $|B|$ frequency has a maximum at $\varphi = 70^\circ$ and a minimum at $\varphi = 10^\circ$, which agrees qualitatively with equation (5).

An interesting test is to change the combination of electrodes. Figure 5(a) shows results of the same experiment as Fig. 4(b) but for conduction between electrodes 5 and 2. Now, the centre of the path distribution is around $\gamma = \pi/4$, and the φ -dependence in equation (5) changes to $|\sin(\pi/4 + \varphi)|$ as is indeed observed in Fig. 5(a). Figure 5(b) shows the CFs for three different combinations of electrodes under an external magnetic field with $\varphi = \pi/2$. The most interesting is G_{1-2} , in which backscattering is inevitable; hence, paths with multiple scatterings survive, resulting in a reduced amplitude fluctuation and higher frequencies. Similarly G_{1-4} is affected by multiple scatterings, although their proportion is not as large as G_{1-2} .

Tight binding calculation. Thus far, we have checked ZB in a simple pinball model from various viewpoints. Here, we show that ZB and the impurity scattering cause significant fluctuations in the conductance between QPCs in the Rashba model with numerical calculations.

Figure 6(a–c) shows the spatial distribution of spin-polarized electrons in a steady flow from a narrow constriction into a clean two-dimensional region. Clear meandering is observed, confirming the existence of ZB. Figure 6(d) plots the electron conductance with and without spin-polarization between two constrictions through a strip region with scatterers.

The conductance for spin-polarized electrons G_{1-5} shows a large aperiodic response with the amplitude of more than $0.1 G_0$ for an in-plane magnetic field ranging from 0 T to 6 T, whereas this CF is much smaller for unpolarized electrons G_{3-7} . Note that we take an absorptive boundary condition, that is, the electrons are annihilated without reflection at the boundaries. The condition breaks unitarity while suppresses the unrealistically strong interference coming from the lack of phase decoherence in the calculation. The unitarity is also not preserved in experiments as well because of the open geometry of the sample. The residual interference causes ordinary CF in G_{3-7} for spin-unpolarized electrons.

In the experiment, diffusive conductance constitutes offset conductance ($0.5 G_0$ in Fig. 3(b) for example). Nevertheless, in the calculation, it is eliminated by the absorptive boundary, which explains why the simulated fluctuations are much larger (about $0.4 G_0$) than the experimental fluctuations (about $0.1 G_0$); see Fig. 6(d).

The result indicates that, in a Rashba system with scatterers, ZB may cause CF, providing evidence supporting the pinball model (see Supplementary Fig. 4 online). An alternative explanation of the results is a chaotic quantum or classical billiards effect. Measuring other samples with different impurities distribution would provide effective verification.

Methods

Two-dimensional electron system in an InAs quantum well. The substrate is an InAs quantum well, grown on a (001) InP using molecular beam epitaxy. From the bottom up, it consists of InAlAs and InGaAs (700 nm) as buffer layers, InAs (4 nm), InGaAs (4 nm), InAlAs (10 nm), n-InAlAs (40 nm), InAlAs (5 nm), and InGaAs (2 nm). QPCs were fabricated by electron-beam lithography and Ar dry-etching with a depth of 300 nm. Contacts were fabricated by AuGe deposition (100 nm) and subsequent annealing (280 degree, 5 min).

The specimen was cooled to 70 mK in a dilution fridge with a superconducting solenoid supplying the magnetic field. A conventional lock-in technique was used for measuring two-wire conductances with frequencies lower than 1 kHz.

Setups for numerical calculations. For numerical calculations we employed the “Kwant” package²⁵, which is based on a tight-binding approximation. The distance between two QPCs $L = 1.8 \mu\text{m}$, QPC width $w = 400 \text{ nm}$, and Rashba strength $\alpha = 3.6 \times 10^{-11} \text{ eVm}$ were adopted to simulate the experiment. The effective mass $m^* = 0.025 m_0$ (where m_0 is the electron mass in a vacuum) and g-factor $g^* = +8.6$ were adopted from previous studies¹³. E_F was tuned to give the QPC conductance $G_{\text{QPC}} = 1.0 G_0$. The calculated area was $3.6 \mu\text{m} \times 3.0 \mu\text{m}$, and was surrounded by absorption walls (except for the QPC passes) and simplified to a square lattice with lattice constant $a = 25 \text{ nm}$. Impurities were introduced by adding randomly-distributed values to the on-site energy. Typical amplitudes of the impurities were 0.2 eV.

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Author Contributions

Y.I. conceived the experiment and performed measurements. Y.H. grew the substrate. Y.I., T.N. and S.K. discussed the results and derived the theoretical model. Y.I. and S.K. wrote the manuscript.

Additional Information

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