scientific reports



OPEN Evolution of cooperation and consistent personalities in public goods games

Mohammad Salahshour

The evolution of cooperation has remained an important problem in evolutionary theory and social sciences. In this regard, a curious question is why consistent cooperative and defective personalities exist and if they serve a role in the evolution of cooperation? To shed light on these questions, here, I consider a population of individuals who possibly play two consecutive rounds of public goods game, with different enhancement factors. Importantly, individuals have independent strategies in the two rounds. However, their strategy in the first round affects the game they play in the second round. I consider two different scenarios where either only first-round cooperators play a second public goods game, or both first-round cooperators and first-round defectors play a second public goods game, but in different groups. The first scenario can be considered a reward dilemma, and the second can be considered an assortative public goods game but with independent strategies of the individuals in the two rounds. Both models show cooperators can survive either in a fixed point or through different periodic orbits. Interestingly, due to the emergence of a correlation between the strategies of the individuals in the two rounds, individuals develop consistent personalities during the evolution. This, in turn, helps cooperation to flourish. These findings shed new light on the evolution of cooperation and show how consistent cooperative and defective personalities can evolve and play a positive role in solving social dilemmas.

As cooperation is costly, an individual is better off not cooperating. This leads to a tragedy of the commons where everyone ends up being worse off than if otherwise, all had cooperated. However, contrary to what a rational argument suggests, empirical evidence shows that tragedies of the commons are not that common in nature². Over the past decades, many efforts have been devoted to understanding how evolution has prevented tragedies of the commons and promoted high levels of cooperation $^{2-5}$. Prisoner's dilemma, and its extension to n players, public goods game (PGG), have been the most common frameworks in many of these studies^{3,3-6}. In the latter game, each player in a group of *n* players can decide whether to invest an amount *c* in a public good or not. All the investments are multiplied by an enhancement factor r < n and are divided equally among the players. Defectors, refraining from investment, receive the highest payoff and are expected to dominate the population. This expectation contradicts observation^{2,3}. Past researches have revealed different mechanisms through which this puzzle can be solved. For instance, when interactions are repeated, cooperation can evolve due to the threat of retaliation of a defective act in future rounds^{3,7,8}. However, in many cases, interactions are not repeated. A similar mechanism, indirect reciprocity⁸⁻¹¹, based on which an individual's reputation determines others' behavior towards the individual can be at work to promote cooperation in non-repeated interactions. Similarly, punishment of defectors^{12–19} or rewarding cooperators^{20–22} can promote social behavior. Cooperation can also evolve when interactions are not obligatory^{23,24}, or when individuals have a choice between different institutions^{25,26}. Furthermore, it is shown that the very existence of population structure can promote cooperation due to the assortativity of interactions in structured populations^{5,27}. Other studies have shown assortativity²⁸, for instance $resulting from \ kin \ selection, group \ selection^4 \ or \ tag-based \ mechanisms^{29}, social \ diversity^{30,31}, heterogeneity^{32-34},$ conformity^{35,36}, costly signaling^{37,38}, moral norms^{11,39}, and coevolution of cooperation and language⁴⁰, to mention a few, can play a positive role in the evolution of cooperation.

Despite the valuable insights reached on the subject, open questions regarding the mechanisms and conditions under which cooperative behavior is expected to flourish, remain to be addressed. A curious question in this regard is the existence of consistent cooperative and defective personalities. For instance, public goods experiments have shown that while about half of the people are conditional cooperators who are willing to cooperate provided their group-mates cooperate, others tend to free-ride on others' contributions 41-44. Similar observations

Max Planck Institute for Mathematics in the Sciences, Inselstrasse 22, 04103 Leipzig, Germany. email: mohammad. salahshour@mis.mpq.de

regarding consistent personality differences in humans and animals, in different contexts, have been made⁴⁵. These observations raise the question of how such consistent cooperative and defective personality differences evolve, and if this can play a constructive role in the evolution of cooperation?

To gain a better insight into this question, here, I consider a context where individuals possibly play two consecutive PGGs. Individuals have independent strategies in the two PGGs. However, their strategy in the first PGG determines the PGG they enter for the second round. This feature of the model has similarities with stochastic games⁴⁶, where individuals' strategy can affect the game they play in future rounds. However, while in stochastic games, the future interaction occurs in the same context for all the individuals 46, here, I consider a situation where individuals may have different future interactions based on their strategies. I consider two different scenarios. In the first scenario, only first-round cooperators play a second PGG. In the second scenario, both first-round cooperators and first-round defectors are offered the chance to play a second PGG, but in different groups. In the first scenario, playing a second public good can be considered as a potential reward for cooperative behavior. This scenario is motivated by the observations that in many contexts, cooperation serves as a signal of merit^{9,37,38,47} or offers a high social status^{48–50} which can increase others' willingness to interact with a cooperator. This can increase an individual's chance of having future interaction, which I model by allowing a cooperator to enter a second PGG. However, in contrast to a certain reward for a cooperative act, the outcome of the second PGG can be positive or negative, depending on the groups' ability to solve the second public goods dilemma, which I call a prosocial reward dilemma. Then, the question arises whether the community can solve a reward dilemma and if this can promote cooperation in the first PGG in the first place?

In the second scenario, I consider an assortative context where not only first-round cooperators, but both first-round cooperators and first-round defectors enter a second PGG, but in different groups. This scenario is motivated by many pieces of evidence of assortative behavior^{51,52}, such as breaking or forming ties^{53,54}, according to which individuals are more likely to interact with similar individuals, and can be considered as a context where both cooperative and defective behavior are rewarded, by, respectively, a prosocial and an antisocial reward dilemma. Importantly, in the model introduced here, the strategies of the individuals are independent in the two rounds. Thus, while it is noted that associativity can promote cooperation when individuals have the same strategy in different interactions - a fact which in a sense underlies many mechanisms for the evolution of cooperation such as network reciprocity, tag based mechanisms, group selection and kin selection - it is not clear whether assortativity of the interactions can play a positive role when individuals have a priori independent strategies in different interactions.

The analysis of the models show that cooperation evolves in both the presence of a reward dilemma and in the presence of assortative interaction. As the comparison of the two scenarios reveals, offering defectors the chance to play a second PGG, that is, an antisocial reward dilemma, can have a surprisingly positive impact on the evolution of cooperation. Interestingly, in an assortative context, in the course of evolution, individuals tend to develop consistent strategies in the two consecutive games. By increasing the likelihood that the benefit of a cooperative act is reaped by fellow cooperators, such a personality consistency, in turn, facilitates the evolution of cooperation. These findings shed new light on the evolution of consistent personalities^{45,55–59}, and shows how in an attempt to solve social dilemmas, evolution may have given rise to the evolution of consistent cooperative and defective personalities.

The model

In our model, in a well-mixed population of *N* individuals, groups of size *g* are randomly formed to play a PGG with enhancement factor r_1 , possibly followed by a second PGG with enhancement factor r_2 . That is, at each time step, the whole population is divided into N/g randomly formed groups. Strategies of the individuals in the second PGG are independent of the first PGG. Thus, there are four possible strategies: cooperation in both games (C_1C_2) , cooperation in the first game and defection in the second one (C_1D_2) , defection in the first and cooperation in the second game (D_1C_2) , and finally, defection in both games (D_1D_2) . I consider two different scenarios. In the first scenario, called a (prosocial) reward dilemma, while defection entails no more round of PGG, cooperation in the first game leads to the entrance to a second PGG. This scenario is consistent with a situation where cooperation serves as a signal of merit^{9,37,38,47} or offers a high social status^{48–50} which can increase others' willingness to interact with a cooperator, and thus, the individual is permitted to enter an elite PGG. In the second scenario, called the assortative public goods game, all the individuals in the group proceed to play a second PGG. However, motivated by many pieces of evidence of assortative behavior^{51,52}, such as breaking or forming ties^{53,54}, I assume individuals are sorted based on their strategies in the first round, such that all the individuals who cooperate in the first round form a subgroup to play a PGG (which is called the cooperative or prosocial PGG), and all those who defect in the first round form a different subgroup to play their second PGG (which is called the defective or anti-social PGG). In this way, the corresponding PGG can be considered an assortative PGG, in which individuals are sorted based on their strategy in the first round.

Individuals gather payoff according to the outcome of the games. Besides, I assume individuals receive a base payoff π_0 from other activities not related to the PGG. After playing the games, individuals reproduce with a probability proportional to their payoff, such that the population size remains constant. That is, the whole population is updated synchronously such that each individual in the next generation is offspring to an individual i in the past generation with a probability proportional to its payoff π_i . Offspring inherit the strategy of their parent. However, mutations can occur. Mutations in the strategy of the individuals in each round (s_1 and s_2 , where s_i can be C or D) occur independently, and each with probability ν . When a mutation occurs, the corresponding variable's value switches to its opposite value (C to D and vice versa).

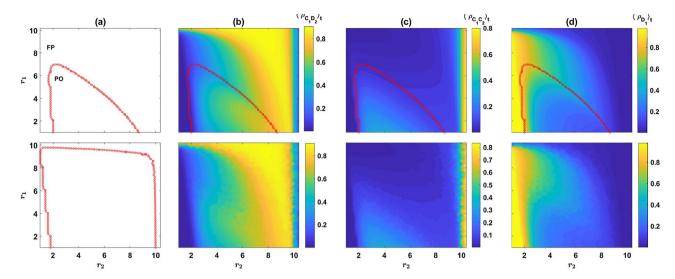


Figure 1. A reward dilemma solves the social dilemma. (a) The phase diagram of the model derived from solutions of the replicator dynamics, for two different mutation rates (top $v=10^{-3}$ and bottom $v=10^{-5}$). The dynamics settle in a periodic orbit or a fixed point depending on the parameters of the model. (b)–(d) Color plots of, respectively, $\langle \rho_{C_1C_2} \rangle_t$, $\langle \rho_{C_1D_2} \rangle_t$ and $\langle \rho_{D_1} \rangle_t = \langle \rho_{D_1C_1} + \rho_{D_1D_2} \rangle_t$. Top panels result from solutions of the replicator dynamics, and bottom panels result from simulations. Cooperation evolves in the second game (c) and is maximized for moderate values of r_2 . This renders entering the second game an incentive to cooperate in the first game, which promotes cooperation in the first game. Here, g=10, c=1, and $\pi_0=2$. In (b)–(d), $\nu=10^{-3}$. Simulations are performed in a population of size N=5000. The simulation is performed for T=3000 time steps starting from an initial condition with random assignment of strategies, and the time averages are taken over the last 2000 time steps. The replicator dynamics are solved for T=5000 time steps starting from homogeneous initial conditions. Time averages are taken over the last 2000 time steps. As the model is mono-stable in the entire phase diagrams, the results are independent of the initial conditions.

Results

The first scenario: a reward dilemma solves the social dilemma. As shown in the "Methods" section, both models can be described in terms of the replicator dynamics, which gives an exact description of the model in infinite population limit. Beginning with the reward dilemma model, I note that when $r_2 > g$, the second PGG is no longer a dilemma. Cooperation becomes the most rational strategy, which guarantees for the second PGG to yield a positive reward to those who enter it by cooperating in the first PGG. As it is known^{20–22}, and as our model confirms, such a certain reward promotes cooperation. The situation becomes more interesting when $r_2 < g$. In this case, the second PGG can even yield a negative outcome. For a promise of having future interaction to promote cooperation, the community needs to solve a second dilemma. As I show below, such coupled dilemmas can be solved through evolution.

I begin by plotting the phase diagram of the model for two different mutation rates, $v = 10^{-3}$ (top), and $v = 10^{-5}$ (bottom), in Fig. 1a. Here and in the following, g = 10, c = 1, $\pi_0 = 2$. For too large values of r_1 , the dynamics settle in a fixed point (denoted by FP in the figures). On the other hand, for smaller values of r_1 , cyclic behavior occurs for intermediate values of r_2 (indicated by PO in the figures). For both too large and too small r_2 , a transition to a phase where the dynamics settle in a fixed point is observed. Comparison of the phase diagram for two different mutation rates shows that lower mutation rates increase the size of the region where the dynamics settle in a periodic orbit.

To see how the cooperation changes with r_1 and r_2 , in Fig. 1b–d, I plot, respectively, the time average of $\rho_{C_1C_2}$, $\rho_{C_1D_2}$ and $\rho_{D_1} = \rho_{D_1C_2} + \rho_{D_1D_2}$. For small r_2 , such that the second PGG is not profitable enough to motivate cooperation in the first PGG, the dynamics settle into a defective fixed point, where the majority of the individuals defect in the first game and do not play the second game. Consequently ρ_{D_1} takes a large value approximately equal to $1 - \nu$, and both $\rho_{C_1C_2}$ and $\rho_{C_1D_2}$ take small values maintained by mutations. As r_2 increases, cooperation in both rounds evolve. To see how this happens, I note that the cost of cooperation in the first round is equal to $c(r_1/g-1)$. As a single mutant C_1C_2 receives a payoff of $c(r_2-1)$ from the second round, cooperation evolves when the payoff of a mutant C_1C_2 from the second round becomes larger than the cost of cooperation in the first round. That is when $r_2 > 2 - r_1/g$. By increasing r_2 beyond this point, $\rho_{C_1C_2}$ rapidly increases. This increases the effective group size in the second round PGG, and thus the expected payoff of second-round defectors, which is an increasing function in $\rho_{C_1C_2}$, increases. To see why this is the case, I note that the payoff of a C_1D_2 individual from the second round in a group composed of $n_{C_1C_2}C_1C_2$ group-mates and $n_{C_1D_2}C_1D_2$ group-mates is equal to $cr_2\rho_{C_1C_2}/(1+n_{C_1C_2}+n_{C_1D_2})$, which is larger in groups with a higher number of C_1C_2 individuals. The probability of formation of groups with a higher number of C_1C_2 individuals, in turn, increases with increasing $\rho_{C_1C_2}$ (see "Methods"), and thus, the expected payoff of a second-round defector increases by increasing $\rho_{C_1C_2}$. Consequently $\rho_{C_1D_2}$ increases by further increasing r_2 beyond $2 - r_1/g$. While this leads to enhanced cooperation in the first round, it also reduces the frequency of second-round cooperators due to the exploitation by second-round defectors. Consequently, the profitability of the second-round PGG decreases and fewer individuals cooperate in

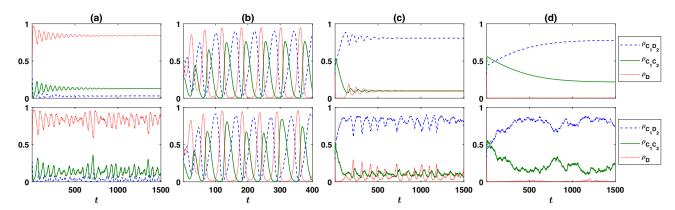


Figure 2. Time evolution of the reward dilemma model. The frequency of different strategies as a function of time is plotted. The top panels represent numerical solutions of the replicator dynamics, and the bottom panel results from a simulation in a population of N=5000 individuals. In all the cases, $r_1=1.8$. In (a), $r_2=2$, which is slightly larger than the threshold necessary for the evolution of cooperation, $2-r_1/g=1.82$, and thus a small fraction of C_1C_2 strategies evolve. In (b) $r_2=3.8$, corresponding to the cyclic phase where different strategies cyclically dominate the population. In (c) and (d), respectively, $r_2=8.8$ and $r_2=9.8$, both corresponding to the cooperative fixed point. Parameter values: $v=10^{-3}$, g=10, c=1, and $\pi_0=2$. The replicator dynamics is solved starting from homogeneous initial conditions, and simulations are performed starting from random assignment of strategies.

the first round to enter the second round PGG. Thus the density of first-round defectors shows a local maximum at a moderate value of r_2 at the transition between the cyclic orbit and partially cooperative fixed point at large r_2 .

The time evolution of the system for different strength of reward dilemma r_2 is presented in Fig. 2. Here, the result of the numerical solution of the replicator dynamics (top) and a simulation in a population of size N=5000 (bottom) are presented. Here, g=10, $\nu=10^{-3}$, c=1, $\pi_0=2$, and $r_1=1.8$. In Fig. 2a, $r_2=2$. This is slightly larger than $2-r_1/g=1.82$, and thus C_1C_2 strategy survive in the population. For larger values of r_2 , the fixed point becomes unstable, and the dynamics settle in the cyclic orbit. An example of the cyclic orbit for $r_2=3.8$ is presented in Fig. 2b. In the cyclic phase, when the density of individuals who cooperate in the first round and thus enter the second PGG is small, individuals can reach a high payoff by entering and cooperating in the second PGG. Thus $\rho_{C_1C_2}$ increases. When $\rho_{C_1C_2}$ increases enough, individuals can reach a higher payoff by defecting in the second PGG. At this point, $\rho_{C_1D_2}$ begins to increase, while $\rho_{C_1C_2}$ decreases. As the density of defectors in the second PGG increases, its profitability decreases, and thus individuals have no incentive to cooperate in the first round. Consequently, both $\rho_{D_1D_2}$ and $\rho_{D_1C_2}$, as well as $\rho_D=\rho_{D_1D_2}+\rho_{D_1C_2}$ increase, while other strategies decrease (I note that, since those who defect in the first round do not enter the second game, the two strategies D_1D_2 and D_1C_2 are degenerate as they lead to the same payoff and are found in the same densities).

The time evolution of the system in the partially cooperative fixed point in large r_2 is presented in Fig. 2c,d. In Fig. 2c, $r_2 = 8.8$. This corresponds to just above the transition line from the periodic solution to the fixed point. Consequently, the replicator dynamics settle in the fixed point after showing transient damped osculations around the fixed point. The simulation results show small fluctuations around the stationary state due to finite-size effects. Comparison of the case of $r_2 = 3.8$ in Fig. 2b and $r_2 = 8.8$ in Fig. 2c shows that $\rho_{C_1D_2}$ increases for larger r_2 due to the higher profitability of the second-round PGG, which motivates more individuals to cooperate in the first round to enter this PGG. This, in turn, can have an adverse effect on $\rho_{C_1C_2}$ due to the larger effective group size of the second round PGG. For larger r_2 , as in Fig. 2d where $r_2 = 9.8$, the dynamics settles in the fixed point without showing damped osculations. Furthermore, $\rho_{C_1C_2}$ increases and $\rho_{C_1D_2}$ decrease as r_2 approaches g.

The second scenario: the evolution of cooperation and consistent personalities in assortative public goods. As we have seen so far, a reward dilemma solves the social dilemma. An interesting question is whether such a mechanism can be competitive if defectors have the chance of forming a PGG of their own? This brings us to an assortative public goods game where both first-round cooperators and first-round defectors are rewarded by a second round of interaction, but in separate groups.

The phase diagram of the assortative public goods game is presented in Fig. 3a, top panel. For both too small and too large r_2 , the system settles into a fixed point, and cyclic behavior emerges in between. However, there are two qualitatively different periodic orbits, each stable in some region of the parameter space. For smaller r_2 , the dynamics settle into a defective periodic orbit (DPO). In this orbit, while cooperation in the cooperative PGG evolves, cooperation does not evolve in the defective PGG. I note that this is the same periodic orbit observed in the reward dilemma model. That such a periodic orbit endures in the second scenario shows its competitive stability. In other words, just as prosocial reward is stable in the presence of an antisocial reward²¹, a prosocial reward dilemma is stable in the presence of an anti-social reward dilemma. On the other hand, for large r_2 , the dynamics settle into the cooperative periodic orbit (CPO), where cooperation in both cooperative and defective PGGs evolves.

Interestingly, for small fixed r_1 , by increasing r_2 the system shows a cross-over from the DPO to CPO without passing any singularity. However, for large r_1 , starting from a uniform initial condition, in which the initial

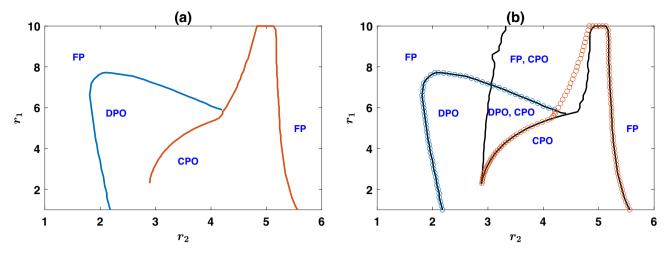


Figure 3. The phase diagram of the assortative public goods game. (a) The phase diagram in the $r_1 - r_2$ plane. For both small and large values of r_2 the model settles into a fixed point (FP). In between, the model shows the cyclic dominance of different strategies. Two different periodic orbits, DPO and CPO, separated by a singular transition exist. (b) Different stability regions in the $r_1 - r_2$ plane (black lines). The phase boundaries are superimposed (empty circles). The model shows two bistability regions where either both the fixed point and the CPO, or both DPO and CPO are stable. Here, g = 10, $v = 10^{-3}$, c = 1, and $\pi_0 = 2$.

densities of all the strategies are equal, as r_2 increases, the equilibrium state of the system changes singularly in a certain value of r_2 . This indicates the transition between DPO and CPO resembles a discontinuous transition for larger r_1 . As a discontinuous transition is usually accompanied by bistability⁶⁰, this raises the question of whether the system possesses a bistable region as well? To address this question, I present the boundaries of bistability in Fig. 3b (black lines). The phase boundaries, which result from a homogeneous initial condition, are superimposed in this figure as well. The boundaries of bistability are derived by solving the replicator dynamics starting from different initial conditions and checking for hysteresis (see "Methods"). The system is monostable outside of the bistable region, indicated by black lines. In the monostable regions, the dynamics settle in the same stationary state, starting from all the initial conditions. In the bistable region (inside the black line), two different stable states, indicated in the figure, are possible depending on the initial conditions. I note that, while the cooperative periodic orbit is stable in the bistable region, it has a very small basin of attraction, such that the replicator dynamics does not settle into this orbit starting from most randomly generated initial conditions (see the Supplementary Information, figures SI.4 and SI.5). For this reason, to derive the boundaries of bistability, a hysteresis analysis is used (see "Methods").

As can be seen in the figure, the transition from a fixed point to the DPO in small r_2 does not show any bistability and occurs at the same value for all the initial conditions. Similarly, the transition from CPO to a fixed point in large r_2 does not show any bistability. In contrast, the transition to CPO by increasing r_2 shows bistability: For medium r_2 , there is a region of the phase diagram where both CPO and DPO are stable. Similarly, the model shows a bistability region for large r_1 where both the fixed point and the cooperative periodic orbit are stable.

In Fig. 4, I present the time evolution of different strategies. An example of different periodic orbits is presented in Fig. 4a (CPO) and Fig. 4b (DPO). Top panels present the result of the replicator dynamics, and the bottom panels present the result of a simulation in a population of size N = 5000. In Fig. 4a, $r_1 = 2.8$ and $r_2 = 4.8$, and in Fig. 4b, $r_1 = 2.8$ and $r_2 = 2.4$. For larger r_2 , as in Fig. 4a, defective and cooperative PGGs perform competitively, and competition between these two maintains cooperation in the system. When $\rho_{C_1D_1}(\rho_{D_1D_2})$ is small, the cooperative (defective) PGG is profitable, and thus, it motivates individuals to cooperate (defect) in the first game in order to enter to this PGG. Consequently, $\rho_{C_1C_2}(\rho_{D_1C_2})$ increases. As $\rho_{C_1C_2}(\rho_{D_1C_2})$ increases enough, the cooperative (defective) PGG becomes vulnerable to defection, due to high frequency of cooperators in this PGG which increase the expected payoff of a second round defector, $\rho_{C_1D_2}$ ($\rho_{D_1D_2}$). At this point, $\rho_{C_1D_1}(\rho_{D_1D_2})$ starts to increase. This in turn decreases the profitability of the cooperative (defective) PGG, and individuals are better off by switching to defection (cooperation) in the first round to enter the defective (cooperative) PGG. Consequently, both $\rho_{C_1C_2}$ and $\rho_{C_1D_2}$ ($\rho_{D_1C_2}$ and $\rho_{D_1D_2}$) decrease, while $\rho_{D_1C_2}$ and $\rho_{D_1D_2}$ ($\rho_{C_1C_2}$ and $\rho_{C_1D_2}$) increase. In this way, competition between cooperative and defective PGGs maintain cooperation in the population. Interestingly, individuals tend to have compatible strategies in the two rounds. That is, those who cooperate in the first round are more likely to cooperate in the second round. This can be seen by noting that on average $\rho_{C_1D_2}$ is much smaller than $\rho_{D_1D_2}$, even though defection in cooperative and defective PGGs leads to, on average, similar payoffs as the density of cooperators in these two games ($\rho_{C_1C_2}$ and $\rho_{D_1C_2}$) are similar.

As mentioned before, the situation is different for smaller r_2 . For smaller r_2 , as can be seen in Fig. 4b, while cooperation in the cooperative PGG evolves, cooperation in the defective PGG does not evolve. This again hints at the evolution of compatible strategies in the two rounds. Consequently, for smaller r_2 , while the cooperative PGG can become profitable due to the evolution of fully cooperative C_1C_2 strategies and motivates individuals to cooperate in the first game, the defective PGG does not perform competitively and can not attract individuals. As mentioned before, this periodic orbit is the same periodic orbit observed in the reward dilemma model.

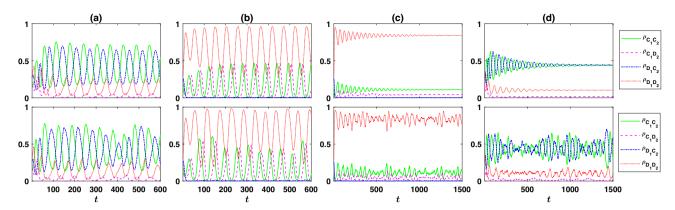


Figure 4. The time evolution of the system in assortative public goods games. (a)–(d) The frequency of different strategies as a function of time. Top panels show replicator dynamics solutions and the bottom panels result form the simulations in a population of N=5000 individuals. The system shows two different periodic orbits. A cooperative periodic orbit, with higher level of cooperation for larger r_2 , $r_2=4.8$ in (a), and a defective periodic orbit, for small r_2 , $r_2=2.4$ in (b). In the fixed point of the dynamics for small r_2 but larger than $2-r_1/g$, as in (c) where $r_2=2$, only C_1C_2 cooperators evolve, and for large r_2 , $r_2=5.6$ in (d), both C_1C_2 and D_1C_2 evolve. Here, g=10, $v=10^{-3}$, c=1, $\pi_0=2$, and $r_1=2.8$. The replicator dynamics is solved starting from homogeneous initial conditions and simulations are performed starting from random assignment of strategies.

The dynamics settle in fixed points for both small and large r_2 . Example of the dynamics of the system in this regime are presented in Fig. 4c, for small r_2 , $r_2 = 2$ and Fig. 4d, for large r_2 , $r_2 = 5.6$. As for small r_2 , cooperation evolves only in the cooperative PGG, the situation is similar to the reward dilemma model: C_1C_2 individuals are found in the population (beyond that maintained by mutations) if $r_2 > 2 - r_1/g$. This is what we observe in Fig. 4c. This again hints at the evolution of consistent personalities, as only fist round cooperators cooperate in the second round. The fixed point for large r_2 is presented in Fig. 4d. As r_2 is chosen just slightly beyond the transition line between cooperative periodic orbit and the fixed point, the dynamics shows damped oscillations around the stationary state before settling in the fixed point. Simulations in a finite population, on the other hand, show that small fluctuations around the stationary state occur in this region. I note that the evolution of consistent personalities can be observed in this regime as well, as the frequency of defectors in the defective PGG is larger than that in the cooperative PGG. That is, first-round defectors are more likely to defect in the second round compared to first-round cooperators.

The fact that individuals' strategies in the two games tend to be compatible can be studied in more depth. To do this, I consider two measures of consistency of the strategies in the two rounds. As a first measure of compatibility of the strategies of the individuals in the two rounds, I define $\gamma = [P(C_2|C_1) + P(D_2|D_1) - P(D_2|C_1) - P(C_2|D_1)]/2$. Here, $P(s_2|s_1)$ is the conditional probability that an individual has strategy s_2 in the second game, given its strategy in the first game s_1 . γ takes a value between one and minus one, and the more positive γ , the more individuals' strategies in the two rounds are consistent. As a second measure of personality consistency, I consider the connected correlation function of the strategies of the individuals in the two rounds $\langle s_1 s_2 \rangle_c = \langle s_1 s_2 \rangle - \langle s_1 \rangle \langle s_2 \rangle$. To calculate this, I assign -1 to the strategy D, and +1to the strategy C. These are plotted in Fig. 5a (top). For comparison, the density of different strategies is plotted as well (bottom panel). Both personality measures show cyclic behavior and always remain non-negative. Importantly, the latter holds in all the phases. This can be seen in Fig. 5b, where the color plot of the time average of γ , for numerical solutions of the replicator dynamics (top) and a simulation in a population of size N = 10,000 (bottom) is presented. Interestingly, for fixed r_2 , personality consistency measures show a maximum close to (but not exactly on) the transition from the fixed point to the defective periodic orbit. This corresponds to $r_2 = 2 - r_1/g$, where the benefit of cooperation in the cooperative PGG starts to become large enough to compensate the cost of cooperation in the first round necessary to enter this PGG. Our results thus show that individuals develop consistent cooperative and defective personalities [see the Supplementary Information for the validity of this result for other parameter values]. This, in turn, plays a positive role in promoting cooperation, as individuals behaving consistently in the two rounds, together with the assortative nature of the public goods, allows first-round cooperators to be more likely to reap the benefit of cooperation in the second round, compared to first-round defectors.

I begin the study of the cooperation by plotting the average cooperation in the first game in Fig. 5c, and the average cooperation in the second game in Fig. 5d. Here, the phase transition lines are indicated in the figure as well. As can be seen, cooperation in the first game is maximized for a moderate value of r_2 , and it drops for both too small and too large values of r_2 . Increasing r_2 beyond this value has a detrimental effect on cooperation in the first round. This is due to the fact that for larger values of r_2 , cooperation in the second round increases in both the defective and the cooperative PGGs. This decreases individuals' incentive to cooperate in the first round to be sorted with fellow cooperators in the second round. On the other hand, for too small r_2 , any potential benefit from the second round can be too small to promote high cooperation in the first round. Interestingly, the maximum cooperation level is achieved exactly on the transition line between the cooperative and the defective

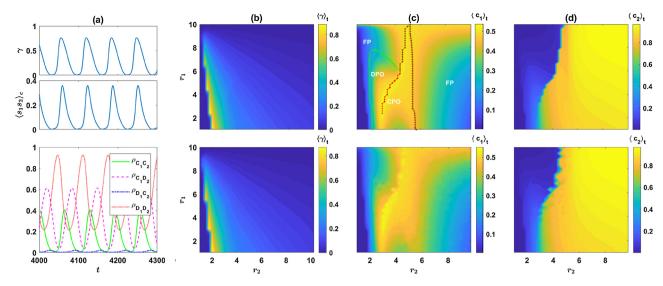


Figure 5. Evolution of cooperation and consistent personalities in assortative public goods game. (a) The time series of the personality consistency measure γ (top), and the connected correlation function between the strategies of the individuals in the two rounds $\langle s_1 s_2 \rangle_t$ (middle). For comparison, the densities of different strategies are plotted in the bottom panel. Both measures always remain non-negative. This shows individuals evolve consistent personalities in the two rounds. (b) The contour plot of the time average personality measure $\langle \gamma \rangle_t$, in $r_1 - r_2$ plane. γ remains non-negative in the whole phase diagram, which indicates consistent cooperative and defective personalities evolve. (c) The contour plot of the time average cooperation level in the first round $\langle \rho_{C_1} \rangle_t = \langle \rho_{C_1C_2} + \rho_{C_1D_2} \rangle_t$. The phase boundaries are plotted in the top panel as well. Interestingly, the cooperation level in the first round is maximized on the singular transition between the two periodic orbits. (e) The contour plot of the time average cooperation level in the second round $\langle \rho_{C_2} \rangle_t = \langle \rho_{C_1 C_2} + \rho_{D_1 C_2} \rangle_t$. $\langle \rho_C, \rangle_t$ increases with increasing r_2 . Here, g = 10, $\nu = 10^{-3}$, c = 1, and $\pi_0 = 2$. In (a) numerical solutions of the replicator dynamics are used. In (b)-(d), top panels result from numerical solutions of the replicator dynamics, and bottom panels result from simulation on a population of size N = 10,000. The replicator equations are solved for T = 5000 time steps starting from a homogeneous initial condition, and the time averages are taken over the last 2000 steps. The simulations are performed for T = 4000 steps starting from a random assignment of strategies, and the averages are taken over the last 3500 steps.

periodic orbits, which coincides with the edge of bistability. This aligns with some arguments that being on the edge of bistability can be beneficial for biological systems ⁶¹.

Finally, the level of cooperation in the second PGG is plotted in Fig. 5d. Here, it can be seen the cooperation increases by increasing r_2 . On the other hand, as we have seen in Fig. 1, in the reward dilemma model, cooperation in the second game is maximized in an intermediate value of r_2 . This contrast can be argued to result from competition between the two cooperative and defective PGGs, such that evolution favors the more cooperative one. Consequently, if individuals in one of the two cooperative or defective PGGs start to defect, the other more cooperative one is favored by evolution. This, in turn, shows that a potential reward to defection, by promoting competition, can have a surprisingly positive impact on the evolution of cooperation in an assortative context.

Discussion

The fact that individuals consistently show cooperative or defective strategies had been noticed in public goods experiments ⁴¹⁻⁴⁴, and in many animal populations ⁴⁵. It is argued this persistent personality differences can partly explain why cooperation is observed in laboratory experiments and many human and animal societies ⁴¹⁻⁴⁵. However, while some theoretical work had shed light on the evolution of some aspects of personality differences, such as the evolution of responsive and unresponsive personalities ⁵⁷, risk-averse and risk-taking personalities ⁵⁵, or personality differences in leadership ⁵⁹, the evolution of cooperative and defective personalities had alluded theoretical understanding. Our findings address this gap by showing how such consistent personality differences can evolve naturally in an evolutionary process when individuals need to work collectively to solve a social dilemma. Importantly, as the analysis of the model shows, the evolution of consistent personalities, in turn, helps solving social dilemmas by increasing the likelihood that the benefit of a cooperative act is reaped by those who behave cooperatively. In this regard, the evolution and maintenance of consistent cooperative and defective personalities can be regarded as an important mechanism at work in promoting cooperation in biological populations.

An interesting question is that why consistent personality differences evolve in an assortative context? The key to the question is that entering the cooperative PGG in the second round is costly, while entering the defective PGG is costless. As it has been shown recently, an entrance cost for a PGG can promote cooperation in a costly PGG, due to the smaller effective size of a costly PGG²⁶. For this reason, cooperation is more frequent and defection less frequent in the cooperative, costly PGG, compared to the defective, cost-less PGG. This phenomenon naturally leads to the evolution of consistent cooperative and defective personalities in an assortative context.

Our analysis also reveals new roads to the evolution of cooperation. In this regard, as the analysis of the reward dilemma model shows, a population of self-interested agents can successfully solve a reward dilemma and this, in turn, helps to solve the social dilemma. This mechanism can be at work to promote cooperation in a context where cooperation increases an individual's chance of having more social interaction, even if actually benefiting from those interactions requires solving another social dilemma. The second scenario model, on the other hand, shows cooperation still evolves when defection is rewarded by a promise of future interaction as well, provided an assortative mechanism is at work. In other words, just as prosocial reward is stable against antisocial reward²¹, a prosocial reward dilemma is competitively stable in promoting cooperation in the presence of an anti-social reward dilemma. In the presence of both prosocial and antisocial reward dilemmas, competition between the prosocial and anti-social public goods maintains cooperation in the system, and moreover, surprisingly increase cooperation in the second round, compared to a case where such competition is lacking. This shows a potential reward to defection, by fostering competition, can have a surprisingly positive impact in promoting cooperation.

Methods

Replicator dynamics. The model can be described in terms of replicator-mutation equations⁶², which provide an exact description of the model in infinite population limit. These equations can be written as follows:

$$\rho_{xy}(t+1) = \sum_{x',y'} \nu_{xy}^{x'y'} \rho_{x'y'}(t) \frac{\pi_{x'y'}(t)}{\sum_{x'',y''} \rho_{x''y''}(t) \pi_{x''y''}(t)}.$$
 (1)

Here, xy (as well as x'y' and x''y'') refer to the strategies of the individuals, such that x is the strategy of an individual in the first round, and y is its strategy in the second round. x, x' etc. can be either cooperation C or defection D. $v_{xy}^{x,y}$ is the mutation rate from the strategy x'y' to the strategy xy. These can be written in terms of mutation rate v as follows:

$$\begin{cases} v_{xy'}^{x'y'} = 1 - 2v + v^2 & \text{if } (x = x' \text{ and } y = y'), \\ v_{xy}^{x'y'} = v - v^2 & \text{if } (x \neq x' \text{ and } y = y') \text{ or } (x = x' \text{ and } y \neq y'), \\ v_{xy'}^{x'y'} = v^2 & \text{if } (x \neq x' \text{ and } y \neq y'). \end{cases}$$
(2)

In Eq. (1), $\pi_{x'y'}$ is the expected payoff of an individuals with strategy x'y'. In the case of the first scenario, these are given by the following equations:

$$\begin{split} \pi_{C_1C_2} &= \sum_{n_{D_1C_2}=0}^{g-1-n_{C_1C_2}} \sum_{n_{C_1D_2}=0}^{g-1-n_{C_1C_2}} \sum_{n_{C_1C_2}=0}^{g-1} \left[cr_1 \frac{1+n_{C_1}}{g} + cr_2 \frac{1+n_{C_1C_2}}{1+n_{C_1}} \right] \rho_{C_1C_2}{}^{n_{C_1C_2}} \rho_{C_1D_2}{}^{n_{C_1D_2}} \rho_{D_1C_2}{}^{n_{D_1C_2}} \rho_{D$$

Here, we have $n_{C_1} = n_{C_1C_2} + n_{C_1D_2}$. To write these equations, I used the fact that in a group with $n_{C_1C_2}$ individuals with strategy C_1D_2 , and $n_{C_1D_2}$ individuals with strategy C_1D_2 , $r_1\frac{1+n_{C_1}}{g}-c$ and $r_1\frac{n_{C_1}}{g}$ are, respectively, the expected payoff of an individual who cooperates, defects, in the first game. Those who defect in the first game do not gather payoff from the second game. On the other hand, those who cooperate in the first game, obtain a payoff from the second game as well (which can be negative or positive). This is $r_2\frac{1+n_{C_1}C_2}{1+n_{C_1}}-c$ for an individual with strategy C_1C_2 , and $r_2\frac{n_{C_1C_2}}{1+n_{C_1}}$ for an individual with strategy C_1D_2 . Finally, $\rho_{C_1C_2}\frac{n_{C_1C_2}\rho_{C_1D_2}\frac{n_{C_1D_2}\rho_{D_1C_2}}{n_{C_1D_2}\rho_{D_1C_2}}$ and $\rho_{D_1D_2}\frac{g-1-n_{C_1C_2}-n_{C_1D_2}-n_{D_1C_2}}{n_{C_1C_2}-n_{C_1D_2}-n_{D_1C_2}}$, is the probability that a focal individual finds itself in a group with $\rho_{C_1C_2}\frac{n_{C_1D_2}}{n_{C_1C_2}}\frac{n_{C_1D_2}}{n_{D_1C_2}}$, $\rho_{D_1D_2}\frac{n_{D_1D_2}}{n_{D_1D_2}}$ and $\rho_{D_1D_2}$ individuals with, respectively, strategies

 C_1C_2, C_1D_2, D_1C_2 , and D_1D_2 . Here, $\binom{g-1}{n_{C_1C_2}, n_{C_1D_2}, n_{D_1D_2}, g-1 - n_{C_1C_2} - n_{C_1D_2} - n_{D_1C_2}}$ is the multinational coefficients (that is the number of ways that among the g-1 group mates of a focal individual, $n_{C_1C_2}, n_{C_1D_2}, n_{D_1D_2}, g-1 - n_{C_1C_2} - n_{C_1D_2} - n_{D_1C_2}$ individuals have strategies, respectively, C_1C_2, C_1D_2, D_1C_2 , and D_1D_2). Summation over all the possible configurations gives the expected payoff of the focal individual with the given strategy from the games. Finally, as all the individuals receive a base payoff π_0 , this is added to the total payoff. Using the expressions in Eq. (3) for the expected payoff of differentstrategies in Eq. (1), I have a set of four equations which gives an analytical description of the model, in the limit of infinite population size.

In the same way, it is possible to write down equations for the expected payoffs of individuals with different strategies in the second scenario. The difference with the preceding scenario is that, in the second scenario those who defect in the first round proceed to a second PGG as well. Thus, under the same notation and conventions as before, the individuals with strategies D_1C_2 and D_1D_2 , obtain a payoff of, respectively, $r_2\frac{1+n_{D_1}C_2}{1+n_{D_1}}-c$ and $r_2\frac{n_{D_1}C_2}{1+n_{D_1}}$, from their second game. Here, $n_{D_1}=n_{D_1C_1}+n_{D_1D_2}$. Thus, we have for the expected payoffs of different strategies in the second scenario:

$$\pi_{C_1C_2} = \sum_{n_{D_1C_2}=0}^{g-1-n_{C_1C_2}-n_{C_1D_2}} \sum_{n_{C_1D_2}=0}^{g-1-n_{C_1C_2}} \sum_{n_{C_1C_2}=0}^{g-1} \left[cr_1 \frac{1+n_{C_1}}{g} + cr_2 \frac{1+n_{C_1C_2}}{1+n_{C_1}} \right] \rho_{C_1C_2}^{n_{C_1C_2}} \rho_{C_1D_2}^{n_{C_1D_2}} \rho_{D_1C_2}^{n_{D_1C_2}} \rho_{D_1C_2}^{n_{D_1C_$$

Using these expressions for the expected payoffs of individuals with different strategies in Eq. (1), we have the analytical description of the second scenario model, in the limit of infinite population size.

The simulations and numerical solutions. Numerical solutions of the replicator dynamics result from numerically solving the replicator dynamics of the models derived in the "Methods" section. Simulations of the models are performed according to the model definition. Unless otherwise stated, both the simulations and numerical solutions of the replicator dynamics are performed with an initial condition in which all the strategies are found in similar frequencies in the population pool. For the solutions of the replicator dynamics, this is assured by setting the initial frequency of all the four strategies equal to 1/4. For simulations, this is assured by a random assignment of the strategies. The phase diagram presented in Fig. 5a is derived by locating the parameter values where a transition between different attractors occurs starting from a homogeneous initial condition. The boundary of bistability in Fig. 5a is derived by examining history dependence and checking for the existence of hysteresis in the evolution of the system. That is, the replicator dynamics are solved starting from parameter values belonging to different phases. Then, the parameter values are changed in small steps, using the stationary state of the preceding steps as the initial condition for the solution of the replicator dynamics in the next step. In this way, the boundary of bistability beyond which a solution becomes unstable is found. See the Supplementary Information for more details.

Received: 17 January 2021; Accepted: 26 November 2021

Published online: 09 December 2021

References

- 1. Hardin, G. The tragedy of the commons. Science 162(3859), 1243–1248 (1968).
- 2. Boyd, R. et al. Tragedy revisited. Science 362(6420), 1236–1241 (2018).
- 3. Axelrod, R. & Hamilton, W. D. The evolution of cooperation. Science 211(4489), 1390-6 (1981).

- 4. Nowak, M. A. Five rules for the evolution of cooperation. Science 314(5805), 1560-1563 (2006).
- Perc, M., Gómez-Gardenes, J., Szolnoki, A., Floría, L. M. & Moreno, Y. Evolutionary dynamics of group interactions on structured populations: A review. J. R. Soc. Interface 10(80), 20120997 (2013).
- 6. Doebeli, M. & Hauert, C. Models of cooperation based on the Prisoner's Dilemma and the Snowdrift game. *Ecol. Lett.* **8**(7), 748–766 (2005).
- 7. Hilbe, C., Chatterjee, K. & Nowak, M. A. Partners and rivals in direct reciprocity. Nat. Hum. Behav. 2(7), 469-477 (2018).
- 8. Schmid, L., Chatterjee, K., Hilbe, C. & Nowak, M. A. A unified framework of direct and indirect reciprocity. *Nat. Hum. Behav.* 5, 1292–1302 (2021).
- 9. Milinski, M., Semmann, D. & Krambeck, H. J. Reputation helps solve the 'tragedy of the commons'. Nature 415(6870), 424 (2002).
- Panchanathan, K. & Boyd, R. Indirect reciprocity can stabilize cooperation without the second-order free rider problem. Nature 432(7016), 499 (2004).
- 11. Alexander, R. D. The Biology of Moral Systems (Routledge, 2017).
- 12. Fehr, E. & Gächter, S. Altruistic punishment in humans. Nature 415(6868), 137-140 (2002).
- 13. Salahshour, M., Oberhauser, V. & Smerlak, M. The cost of noise: Stochastic punishment falls short of sustaining cooperation in social dilemma experiments. arXiv preprint arXiv:2109.13547 (2021).
- 14. Perc, M. et al. Statistical physics of human cooperation. Phys. Rep. 687, 1-51 (2017).
- 15. Salahshour, M. Evolution of prosocial punishment in unstructured and structured populations and in the presence of antisocial punishment. *PLoS One* **16**(8), e0254860 (2021).
- 16. Boyd, R., Gintis, H. & Bowles, S. Coordinated punishment of defectors sustains cooperation and can proliferate when rare. *Science* **328**(5978), 617–620 (2010).
- 17. Szolnoki, A. & Perc, M. Second-order free-riding on antisocial punishment restores the effectiveness of prosocial punishment. *Phys. Rev. X* 7(4), 041027 (2017).
- 18. Hauert, C., Traulsen, A., Brandt, H., Nowak, M. A. & Sigmund, K. Via freedom to coercion: The emergence of costly punishment. *Science* 316(5833), 1905–1907 (2007).
- 19. Hilbe, C. & Traulsen, A. Emergence of responsible sanctions without second order free riders, antisocial punishment or spite. *Sci. Rep.* **2**, 458 (2012).
- 20. Rand, D. G., Dreber, A., Ellingsen, T., Fudenberg, D. & Nowak, M. A. Positive interactions promote public cooperation. *Science* 325(5945), 1272–1275 (2009).
- 21. Szolnoki, A. & Perc, M. Antisocial pool rewarding does not deter public cooperation. *Proc. R. Soc. B Biol. Sci.* **282**(1816), 20151975 (2015).
- 22. Hilbe, C. & Sigmund, K. Incentives and opportunism: from the carrot to the stick. *Proc. R. Soc. B Biol. Sci.* 277(1693), 2427–2433 (2010).
- 23. Szabó, G. & Hauert, C. Phase transitions and volunteering in spatial public goods games. Phys. Rev. Lett. 89(11), 118101 (2002).
- 24. Hauert, C., De Monte, S., Hofbauer, J. & Sigmund, K. Volunteering as red queen mechanism for cooperation in public goods games. *Science* **296**(5570), 1129–1132 (2002).
- 25. Salahshour, M. Freedom to choose between public resources promotes cooperation. PLoS Comput. Biol. 17(2), e1008703 (2021).
- 26. Salahshour, M. Evolution of cooperation in costly institutions exhibits Red Queen and Black Queen dynamics in heterogeneous public goods. *Commun. Biol.* **4**, 1340; https://doi.org/10.1038/s42003-021-02865-w (2021).
- 27. Ohtsuki, H., Hauert, C., Lieberman, E. & Nowak, M. A. A simple rule for the evolution of cooperation on graphs and social networks. *Nature* **441**(7092), 502–505 (2006).
- 28. Iyer, S. & Killingback, T. Evolution of cooperation in social dilemmas with assortative interactions. Games 11(4), 41 (2020).
- 29. Riolo, R. L., Cohen, M. D. & Axelrod, R. Évolution of cooperation without reciprocity. Nature 414(6862), 441-443 (2001).
- 30. Santos, F. C., Santos, M. D. & Pacheco, J. M. Social diversity promotes the emergence of cooperation in public goods games. *Nature* 454(7201), 213 (2008).
- 31. Qin, J., Chen, Y., Kang, Y. & Perc, M. Social diversity promotes cooperation in spatial multigames. *Europhys. Lett.* **118**(1), 18002 (2017).
- 32. Stilwell, P. et al. Resource heterogeneity and the evolution of public goods cooperation. Evol. Lett. 4(2), 155-163 (2020).
- 33. Kun, A. & Dieckmann, U. Resource heterogeneity can facilitate cooperation. Nat. Commun. 4(1), 1-8 (2013).
- 34. Perc, M. Does strong heterogeneity promote cooperation by group interactions?. N. J. Phys. 13(12), 123027 (2011).
- 35. Szolnoki, A. & Perc, M. Conformity enhances network reciprocity in evolutionary social dilemmas. *J. R. Soc. Interface* 12(103), 20141299 (2015).
- 36. Hu, K., Guo, H., Geng, Y. & Shi, L. The effect of conformity on the evolution of cooperation in multigame. *Phys. A Stat. Mech. Appl.* **516**, 267–272 (2019).
- 37. Salahshour, M. Evolution of costly signaling and partial cooperation. Sci. Rep. 9(1), 1-7 (2019).
- 38. Gintis, H., Smith, E. A. & Bowles, S. Costly signaling and cooperation. J. Theor. Biol. 213(1), 103-119 (2001).
- 39. Salahshour, M. Playing soft with cooperators emerges as a moral norm and promotes cooperation in evolutionary games. *bioRxiv* (2021).
- 40. Salahshour, M. Coevolution of cooperation and language. Phys. Rev. E 102(4), 042409 (2020).
- 41. Chaudhuri, A. Sustaining cooperation in laboratory public goods experiments: A selective survey of the literature. *Exp. Econ.* **14**(1), 47–83 (2011).
- 42. Fischbacher, U., Gächter, S. & Fehr, E. Are people conditionally cooperative? Evidence from a public goods experiment. *Econ. Lett.* 71(3), 397–404 (2001).
- 43. Burlando, R. M. & Guala, F. Heterogeneous agents in public goods experiments. Exp. Econ. 8(1), 35-54 (2005).
- 44. Fischbacher, U. & Gachter, S. Social preferences, beliefs, and the dynamics of free riding in public goods experiments. *Am. Econ. Rev.* **100**(1), 541–56 (2010).
- 45. Bergmüller, R., Schürch, R. & Hamilton, I. M. Evolutionary causes and consequences of consistent individual variation in cooperative behaviour. *Philos. Trans. R. Soc. B Biol. Sci.* **365**(1553), 2751–2764 (2010).
- 46. Hilbe, C., Šimsa, Š, Chatterjee, K. & Nowak, M. A. Evolution of cooperation in stochastic games. Nature 559(7713), 246–249 (2018).
- 47. Van Vugt, M. & Hardy. C. L. Cooperation for reputation: Wasteful contributions as costly signals in public goods. *Group Process. Intergroup Relat.* 13(1), 101-111 (2010).
- 48. Smith, E. A. & Bird, R. L. B. Turtle hunting and tombstone opening: Public generosity as costly signaling. *Evol. Hum. Behav.* 21(4), 245–261 (2000).
- 49. Bird, R. B. Smith, E. & Bird. D. W. The hunting handicap: Costly signaling in human foraging strategies. *Behav. Ecol. Sociobiol.* **50**(1), 9–19 (2001).
- 50. Marlowe, F. The Hadza: Hunter-Gatherers of Tanzania, vol. 3. (Univ of California Press, 2010).
- 51. Kossinets, G. & Watts, D. J. Empirical analysis of an evolving social network. Science 311(5757), 88-90 (2006).
- 52. Brekke, K. A., Hauge, K. E., Lind, J. T. & Nyborg, K. Playing with the good guys. A public good game with endogenous group formation. *J. Public Econ.* **95**(9–10), 1111–1118 (2011).
- 53. Wang, J., Suri, S. & Watts, D. J. Cooperation and assortativity with dynamic partner updating. *Proc. Natl. Acad. Sci.* 109(36), 14363–14368 (2012).

- 54. Santos, F. C., Pacheco, J. M. & Lenaerts, T. Cooperation prevails when individuals adjust their social ties. *PLoS Comput. Biol.* 2(10), e140 (2006).
- 55. Wolf, M., Van Doorn, G. S., Leimar, O. & Weissing, F. J. Life-history trade-offs favour the evolution of animal personalities. *Nature* 447(7144), 581 (2007).
- 56. Wolf, M. & Weissing, F. J. Animal personalities: Consequences for ecology and evolution. Trends Ecol. Evol. 27(8), 452-461 (2012).
- 57. Wolf, M., Van Doorn, G. S. & Weissing, F. J. Evolutionary emergence of responsive and unresponsive personalities. *Proc. Natl. Acad. Sci.* **105**(41), 15825–15830 (2008).
- 58. Dall, S. R., Bell, A. M., Bolnick, D. I. & Ratnieks, F. L. An evolutionary ecology of individual differences. *Ecol. Lett.* 15(10), 1189–1198 (2012).
- 59. Johnstone, R. A. & Manica, A. Evolution of personality differences in leadership. Proc. Natl. Acad. Sci. 108(20), 8373-8378 (2011).
- 60. Binder, K. Theory of first-order phase transitions. Rep. Prog. Phys. 50(7), 783 (1987).
- 61. Salahshour, M. Phase diagram and optimal information use in a collective sensing system. Phys. Rev. Lett. 123(6), 068101 (2019).
- 62. Nowak, M. A. Evolutionary Dynamics: Exploring the Equations of Life (Harvard University Press, 2006).

Acknowledgements

The author acknowledges funding from Alexander von Humboldt Foundation in the framework of the Sofja Kovalevskaja Award endowed by the German Federal Ministry of Education and Research.

Author contributions

M.S. designed and performed the research, and wrote the paper.

Funding

Open Access funding enabled and organized by Projekt DEAL.

Competing interests

The author declares no competing interests.

Additional information

Supplementary Information The online version contains supplementary material available at https://doi.org/10.1038/s41598-021-03045-w.

Correspondence and requests for materials should be addressed to M.S.

Reprints and permissions information is available at www.nature.com/reprints.

Publisher's note Springer Nature remains neutral with regard to jurisdictional claims in published maps and institutional affiliations.

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit http://creativecommons.org/licenses/by/4.0/.

© The Author(s) 2021