

# How to achieve a higher selection plateau in forest tree breeding? Fostering heterozygote × homozygote relationships in optimal contribution selection in the case study of *Populus nigra*

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## Abstract

In breeding, optimal contribution selection (OCS) is one of the most effective strategies to balance short- and long-term genetic responses, by maximizing genetic gain and minimizing global coancestry. Considering genetic diversity in the selection dynamic—through coancestry—is undoubtedly the reason for the success of OCS, as it avoids preliminary loss of favorable alleles. Originally formulated with the pedigree relationship matrix, global coancestry can nowadays be assessed with one of the possible formulations of the realized genomic relationship matrix. Most formulations were optimized for genomic evaluation, but few for the management of coancestry. We introduce here an alternative formulation specifically developed for genomic OCS (GOCS), intended to better control heterozygous loci, and thus better account for Mendelian sampling. We simulated a multigeneration breeding program with mate allocation and under GOCS for twenty generations, solved with quadratic programming. With the case study of *Populus nigra*, we have shown that, although the dynamic was mainly determined by the trade-off between genetic gain and genetic diversity, better formulations of the genomic relationship matrix, especially those fostering individuals carrying multiple heterozygous loci, can lead to better short-term genetic gain and a higher selection plateau.

## KEYWORDS

genomic selection, heterozygote × homozygote relationship, optimal contribution selection, quantitative genetics, simulation

## 1 | INTRODUCTION

Genomic selection (Meuwissen et al., 2001), in spite of using more precise Mendelian sampling terms compared to pedigree-based selection, and drastically increasing genetic response doing so, might accelerate the loss of genetic diversity and the useful variation per

unit of time (Goddard, 2009; Hayes et al., 2009; Rutkoski et al., 2015). The loss of genetic diversity depends on a compromise between the co-selection of less relative individuals, which decreases the inbreeding rate per generation (Daetwyler et al., 2007), and the reduction of generation intervals, which gradually reduces the selective response (Grattapaglia, 2017). Yet, over the past decades, a

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growing number of authors have emphasized the importance of balancing loss of diversity and short-term genetic gain to sustain a long-term genetic response (Brisbane & Gibson, 1995; Jannink, 2010; Woolliams et al., 2002). This is especially true for perennial trees, for which minimal husbandry is provided while they can face harsh environments over a long period.

Optimal contribution selection (or OCS) was introduced by Meuwissen (1997) as a complement to the widely used best linear unbiased predictor (BLUP). BLUP conveniently integrates family information for increased accuracy, but also leads to rapid co-selection of relatives. On the other hand, OCS maximizes genetic gain while maintaining the inbreeding rate to a predefined level, thus accounting for the impact of genetic relationships on the population dynamics. OCS was originally formulated with the pedigree-based relationship matrix ( $A$ ), but nowadays it can be easily adapted to the realized genomic relationship matrix ( $G$ ). Its simplicity has made it today one of the most successful strategies to address the problem of selection-induced loss of diversity (Meuwissen et al., 2020). Furthermore, its flexibility has facilitated countless extensions. As a nonexhaustive illustration of its potential, De Beukelaer et al. (2017) extended OCS for different measures, such as heterozygosity, or the criterion of Li et al. (2008); Gebregiwergis et al. (2020) incorporated an alternative formulation of the genomic relationship matrix via QTL and markers; several studies proposed to combine OCS with mate selection, mainly to account for logistic constraints (e.g., the number of mating per individual), and to account for dominant effects (Akdemir & Sánchez, 2016; Toro & Varona, 2010; Varona & Misztal, 1999; Vitezica et al., 2013).

The realized genomic relationship matrix carries precise information on the relationship between pairs of individuals, but most of its formulations focused on shared homozygosity, which we could call homozygote  $\times$  homozygote relationships. However, managing heterozygosity has a significant impact on the long-term genetic gain (De Beukelaer et al., 2017). Following the approach of Gebregiwergis et al. (2020), we propose here an alternative formulation of the genomic relationship matrix that focuses on individual carrying an excess of heterozygous loci relative to the population, or, in other words, the effect of individual-wise heterozygosity (for the study of population-wise heterozygosity, see De Beukelaer et al., 2017). Previous formulations of the realized genomic relationship matrix focused on increasing accuracy (Fragomeni et al., 2017; Nejati-Javaremi et al., 1997), or comparing genomic vs genealogical information (De Cara et al., 2011; Gómez-Romano et al., 2016). On the contrary, our method is intended to be used only in the context of Genomic OCS (GOCS), corresponding to the second genomic matrix in Gebregiwergis et al. (2020). Our study showed that developing different genomic relationship matrix for different usage can be beneficial, as our formulation increased long-term genetic gain when used in GOCS, but decreased accuracy when used in genomic evaluation.

In the present study, we will focus on heterozygote  $\times$  homozygote relationships, and the objective is to exploit the impact of

Mendelian sampling in the framework of genetic contribution (Avendaño et al., 2004; Cole & VanRaden, 2011). To do so, we devised a way to integrate heterozygote  $\times$  homozygote relationship in the genomic relationship matrix, either to promote it or penalize it. We have developed a deterministic algorithm capable of solving both classical OCS and our alternative formulation, with quadratic programming. We have applied our method to the case study a population of *Populus nigra* L. (Salicaceae), to show by simulations that managing heterozygous loci in a multigeneration breeding program can achieve higher performances than with a classical OCS, and reach a higher Pareto curve. Among all the possible ways of constructing the genomic relationship matrix, the best strategy was to foster the heterozygote  $\times$  homozygote relationship between pairs, which appeared to be the best compromise between genetic fixation and diversity.

## 2 | MATERIALS AND METHODS

### 2.1 | Optimal contribution selection and convex optimization

Genetic contributions, first introduced by James and McBride (1958), are the cornerstone of OCS. The two opposing items in the optimization of OCS, gain and diversity, can be formulated according to the same decision variable, genetic contribution. The genetic contribution can be defined as the proportion of genes from a given ancestor that are present in a given cohort of descendants. More generally, the genetic contribution of an individual is its proportional contribution to the gene pool of the descendant population (Woolliams & Mäntysaari, 1995). In our case, when considering nonoverlapping generations, the genetic contribution of a given parent would simply be its proportional contribution to the offspring of the next generation. We denote  $c$  the vector of  $N$  genetic contributions, with  $N$  being the size of the parental population. Defined as such,  $\sum c_i = 1$ .

With the knowledge of  $Y$  the vector of parental breeding values and  $A$  the numerator relationship matrix between parents (or  $G$  the realized genomic relationship matrix), and assuming no epistasis, it is possible to formulate the expected future performance or inbreeding coefficient of the population as  $c^T Y$  ( $cY$  for simplicity) or as  $\frac{1}{2} c^T A c$ , respectively (or  $c^T G c$  when using the genomic relationship matrix;  $cAc$  and  $cGc$  for simplicity). Deriving optimal selection decisions simultaneously accounting for future performance and future inbreeding is then possible through OCS, using genetic contributions as a decision variable. One of the possible formulations of such a problem is to solve  $\min. \lambda cGc - cY$ , with  $\lambda$  a weighting parameter (see Woolliams et al., 2002 and references therein). It is important to note that the weighted average of  $cAc$  (or  $cGc$ ) represents the expected inbreeding assuming *panmixia* or, more precisely, uniting in a full diallelic way all parents while respecting each parental  $c$ . This corresponds to the best expectation for inbreeding when the mating regime is unknown or not under the control of the breeder, which

is often the case when, for example, mating is allowed to follow an open pollination regime as in a seed orchard.

As classical selection over cycles tends to accelerate the change of frequencies when they are intermediate, that is, when the variances are at the highest levels, the risks of loss of favorable alleles by hitchhiking the alternative detrimental would also increase (Sánchez et al., 2006). OCS would reduce this risk by maintaining frequencies at intermediate levels (when using an identity-by-state matrix  $G$ , see Nejati-Javaremi et al., 1997), leading to a potentially slower fixation of favorable alleles, but overall benefits over the long-term genetic gain.

Originally, Meuwissen et al. (2001) formulated OCS as the maximization of genetic gain ( $cY$ ) subject to a constrained inbreeding coefficient ( $cAc$ ). Likewise, it is also possible to minimize the inbreeding rate while constraining the genetic gain (Akdemir & Sánchez, 2016). Choosing the adequate constraint is critical for populations never confronted to OCS. The methodology was primarily devised with long-term domesticated populations in mind, where records of change in inbreeding and genetic gain are typically known over several cycles, facilitating the choice of the constraints. In the absence of historical references, for novel species, a gradient of constraints would need to be evaluated a priori. In this sense, a holistic approach allowing visualization of the optimized function over a wide range of scenarios would be preferable as a start.

Following the approach of Akdemir et al. (2019), we considered OCS as a multiobjective optimization, where gain and diversity are improved simultaneously, that is, maximizing gain and minimizing coancestry, by pondering weights that set the balance between the two items. The solutions of a multiobjective optimization, namely Pareto optima (Figure S1), delineate a two-dimensional curve. Optimizing in two dimensions (genetic gain and coancestry) is mathematically equivalent to the scalarized version of the problem: minimize  $\lambda cGc - cY$  for any  $\lambda > 0$ . The scalarized problem has a unique global solution since the objective function is strictly convex ( $G$  is positive definite, as shown below). In other words, the curve of Pareto optima is the parametric curve, as a function of  $\lambda$ , of solutions minimizing  $\lambda cGc - cY$ . It is therefore the set of  $(c^*Gc^*, c^*Y)$ , where  $c^*$  is the optimal contribution vector for a given  $\lambda$ . Without loss of generality, we consider the scalarized problem parameterized by  $\alpha$  such that the problem becomes:

$$\min. \alpha c^T G c - (1 - \alpha) c^T Y \quad (1)$$

where  $\alpha \in [0;1]$  can be interpreted as the trade-off value between coancestry and genetic gain (or the weight of coancestry compared to that of genetic gain).

Each OCS solution given a constraint (as in Meuwissen et al., 2001) is a particular Pareto optimum, or, in other words, is the solution of the scalarized problem for a particular  $\alpha$  (if the constraint is not ill-formulated, i.e., not out of range). Both formulations—with  $\alpha$  or with an inbreeding constraint—are strictly equivalent, and choosing a value for  $\alpha$  is as arbitrary and difficult as choosing a value for a constraint

without any a priori. Here, we will develop the framework with  $\alpha$ , and different selection scenarios will be expressed in terms of  $\alpha$ .

As in Meuwissen, 1997, we have added some operational constraints to the multiobjective problem: the contributions must be larger than 0 to have a biological meaning but smaller than 0.5 to avoid selfing ( $0 \leq c \leq 0.5$ ), and the sum of all contributions must be equal to 1 ( $1^T c = 1$ ). The constrained scalarized problem for a particular value of  $\alpha$  is a constrained quadratic programming and can therefore be solved deterministically with an interior point method, adequate to solve constrained convex optimization (Boyd et al., 2004).

## 2.2 | Different genomic matrices

Let  $X$  be the matrix describing the genotypes of the population, with  $L$  rows (number of markers) and  $N$  columns (number of individuals). The two homozygous states are encoded as  $-1$  and  $1$ , and the heterozygous state as  $0$  (as in VanRaden, 2008). We will consider the realized genomic relationship matrix formulated as  $G = X^T X$  ( $N \times N$  matrix). Note that the elements of  $X$  are not corrected by minor allele frequencies, nor is the resulting  $G$  scaled by the expected heterozygosity, as is usually done in genomic evaluation. Therefore, the diagonal elements of  $G$  provide information on the number of homozygous loci per individual, while the off-diagonal elements reflect the number of homozygous states shared by individuals across loci. Thus, for off-diagonals, the same homozygous state at a given locus adds one unit to the count, while one unit is subtracted for opposite homozygous states (not accounting for heterozygote by heterozygote, as pointed out by Gao & Martin, 2009), producing overall large values for pairs with resembling parents and small values for pairs with genetically distinct parents.

Using the  $G$  matrix defined above, OCS will penalize individuals with some particular relationship with the rest. For instance, an individual carrying multiple homozygous loci that are common in the population is less prone to be selected, as opposed to those carrying rare homozygous loci or heterozygous loci. In other words, per construction, individuals are scored depending on their homozygosity compared with other individuals' homozygosity. We propose here to also score individuals on their heterozygosity compared with other individuals' homozygosity; in other words, to account for the relative excess of heterozygous loci within an individual. The objective is to distinguish different Mendelian samplings occurring in identical homozygote  $\times$  homozygote, which value in the  $G$  matrix is  $1$  ( $1 \times 1$  or  $-1 \times -1$  with the notation introduced above); opposite homozygote  $\times$  homozygote, which value is  $-1$  ( $-1 \times 1$ ); heterozygote  $\times$  homozygote, which value is  $0$  ( $0 \times 1$  or  $0 \times -1$ ); and heterozygote  $\times$  heterozygote, which value is also  $0$  ( $0 \times 0$ ). To distinguish heterozygote  $\times$  homozygote ( $He \times Ho$ ), and heterozygote  $\times$  heterozygote ( $He \times He$ ), we propose to change the value of  $He \times Ho$  to  $\beta$ , which ranges from  $-1$  to  $1$ . A positive value of  $\beta$  means that few offspring will be generated from individuals with a large number of loci in  $He \times Ho$  relationship with others. Hereafter, we denote  $G^*$  the

matrix constructed with  $\beta$ , where  $G^* = G + \beta Q$ ,  $Q$  being the matrix accounting for He  $\times$  Ho loci, as  $G$  already account for homozygote loci (details in Supporting Information).

In addition, we can derive that (details in Supporting Information):

$$c^T G^* c = c^T G c + \beta c^T Q c = c^T G c + \beta \text{He}^T \text{Ho} \quad (2)$$

where He is the vector (of size  $L$ ) of the proportion of heterozygous individuals contributing to the next generation for each locus, and Ho the equivalent for homozygous individuals. We can see from Equation (2) that controlling  $\beta$  allows us to change the frequency of the carriers of favorable genotypic states, which in turn would favor the occurrence of certain crosses increasing the segregation of diversity, for instance by increasing the chance of double heterozygous pairs over homozygous  $\times$  heterozygous pairs. Such extra segregation could intuitively allow for a more sustainable genetic progress over the long term, without the risk of genetic hitchhiking.

For the objective function to be strictly convex,  $G^*$  must be positive definite. Therefore, we performed a spectral projection of  $G^*$  on the set of positive definite matrices, ensuring that the projected matrix is the closest positive definite matrix to  $G^*$  (according to the spectral norm; Boyd et al., 2004). We will from here onward denote the projection of  $G^*$  as  $G^*$  itself to ease the reading.

## 2.3 | Genomic data

The population used in the study included 1009 individuals from the French breeding population of *P. nigra* (Pégard et al., 2020). All of them were genotyped with a 12k Infinium array (Faivre-Rampant et al., 2016) resulting in 5253 usable SNP markers after quality and frequency filtering (minor allele frequency higher than 0.05). The resulting genotypes were phased, imputed and a consensus recombination map derived (Pégard et al., 2019) by using FImpute software (Sargolzaei et al., 2014). The allelic effects were estimated from a genomic multitrait evaluation using breedR (Muñoz & Sánchez, 2020). In this study, we considered the trunk circumference as a focal trait, with a heritability of  $h^2 = 0.5134$  (Pégard et al., 2020). All the individuals were phenotyped.

Poplar is a dioecious species. Sex, however, cannot be determined before seven years of age, nor can it be predicted from the genomic profile yet. For this study, and to overcome the missing sex of unsexed candidates, we assumed a monoecious population. However, our method could be easily extended to dioecious populations by adding one simple constraint:  $d^T c = 0.5$ , where  $d$  is a design vector indicating the female/male individuals.

The population *Populus nigra* was genetically structured (Figure S2), with a high linkage disequilibrium. In order to check for possible effects of the linkage, in addition to the original dataset, we shuffled the alleles at each locus so that the allele frequencies remained unchanged, while linkage disequilibrium could be partly removed. Hereafter, we will refer to it as “shuffled dataset”, as

opposed to the original dataset that we will refer to as “unshuffled dataset”.

## 2.4 | Simulation pipeline

We considered different simulation scenarios, assuming different values of  $\alpha$  and  $\beta$ . We simulated multigeneration breeding schemes of a constant population size  $N$  at each generation, and the parameters ( $\alpha$  and  $\beta$ ) remained constant across generations within a given scenario. No introgression of external genetic material was considered here. As mentioned above, we estimated the allelic effects from the genotype data with a real phenotype (trunk circumference). The resulting allelic effects were considered “true” and constant across generations and used to obtain the true breeding value (TBV) of the newly simulated candidates. Phenotypes and genotypes of all simulated individuals were considered to be known at each generation.

When simulating multigeneration breeding programs, the question arises as to how genomic estimated breeding values (GEBVs) should be assessed at each new virtual generation. With a heritability of  $h^2 = 0.5134$ , environmental deviation was simulated as a normally distributed perturbation of mean 0 and variance  $(1 - h^2)\sigma_g^2$ , where  $\sigma_g^2$  was the TBV variance. At each generation, as was done in Jannink (2010) and De Beukelaer et al. (2017), GEBV was assessed with a ridge regression model (Searle, 2009), using the matrix  $G$  (not  $G^*$ ). Genomic evaluation included all previous generations, so the reference population incrementally increased over time.

OCS was then applied at each generation on the simulated GEBVs, and the resulting contributions were converted into a mating plan that fits the OCS solution. We can notice that once the genetic contributions are fixed, the mating plan will not change the average breeding value, nor the average coancestry in the selected candidates. The mating, however, can change the progeny homozygosity—the diagonal elements of the matrix  $G$  at generation  $t + 1$  (Pryce et al., 2012; Sonesson et al., 2012). Expected progeny homozygosity is equal to parents' genomic relatedness (up to a constant). To optimize the complementation of parents in mating, we computed the mating plan by minimizing the average progeny homozygosity per mating, that is, the trace of the matrix  $G$  at generation  $t + 1$ , with a linear programming (see Supporting Information). Mate allocation was done with the transformed matrix  $G^*$ . In order to assess the effect of mate allocation, random mating was also simulated. Finally, with the mating plan, we simulated the next generation with an ad hoc program (written in C++17). All scenarios started with the same initial population: the initial average breeding value was equal to  $27.7 \pm 25.9$  and the population coancestry was equal to  $0.214 \pm 0.086$ .

Every simulated replicate proceeded for 20 (nonoverlapping) generations and was devised without mutation. The simulation followed a grid of parameters:  $\alpha$  ranged from 0.1 to 0.9 (with steps of 0.1), and  $\beta$  was equal to  $-0.5$ , 0, or 0.5. Each parametric setting was simulated 100 times. In order to compare the results from different  $\beta$ , we also computed for each simulation the “true” coancestry, which is the coancestry the population would have had if  $\beta$  was equal to 0

(in line with the methods of Gebregiweris et al., 2020). The whole pipeline was coded in R – 3.6.3 (R Core Team, 2020) and is available on github (<https://github.com/mtiret/ocs.git>).

## 2.5 | Statistical analyses

Finally, in order to determine the relative importance of the factors  $\alpha$ ,  $\beta$  and mate allocation on genetic gain and true coancestry (through an analysis of variance) at a given generation, we considered the following statistical model:

$$Y \sim \alpha + \beta + \alpha^2 + m + e,$$

where  $Y$  is the output variable (either genetic gain or true coancestry),  $\alpha$  and  $\beta$  the simulation parameters treated as fixed effects,  $\alpha^2$  as the fixed effect of the squared parameter of  $\alpha$ ,  $m$  as the fixed effect of mate allocation (equal to 0 or 1), and  $e$  the residual fitted to a normal distribution. We considered here a polynomial regression (quadratic term  $\alpha^2$ ) as there were symmetrical boundary effects of  $\alpha$  upon  $Y$ : adding the quadratic term resulted in a gain of up to 70% in terms of adjusted coefficient of determination ( $r^2$ ). Quadratic  $\alpha$  increases with a slower rate than linear  $\alpha$ ; hence, the quadratic term can be interpreted as an effect that is constant for low values of  $\alpha$ , but highly variable among high values of  $\alpha$ . We will hereafter refer to this model as model (1). In some cases however, we focused on a given value of  $\alpha$ , where we considered the following model:

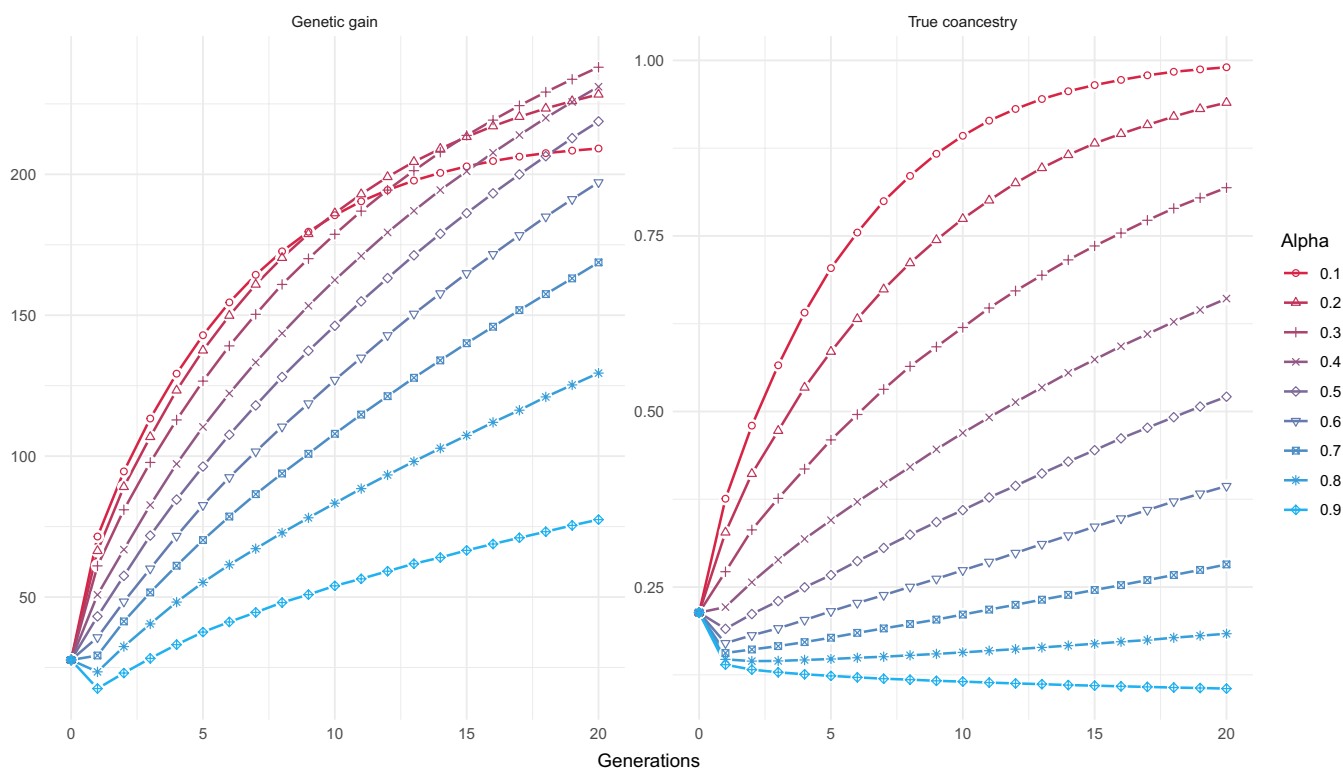
$$Y \sim \beta + m + e,$$

with equal notations and assumptions as model (1). We will hereafter refer to this model as model (2). These two models were analyzed using R - 3.6.3 (functions *lm* and *anova* from the base R package *stats*). We performed a type I analysis of variance, and the statistical significance of each factor was assessed with a Fisher's  $F$  test.

## 3 | RESULTS

### 3.1 | Overall evolution of genetic gain and coancestry met common expectations

When considering the unshuffled dataset, only studying the effect of  $\alpha$  (representing the weight of coancestry compared to that of genetic gain), and considering  $\beta$  (representing the value of  $He \times Ho$  relationships) equal to 0—corresponding then to the classical formulation of OCS—as expected, the average value of genetic gain increased for the whole period of selection, especially for low  $\alpha$  (Figure 1, Table 1). True coancestry increased over time, but less so with higher  $\alpha$ —as expected, when focusing on coancestry, genetic diversity increased over time. For the largest value of  $\alpha$  (0.9), a consistent decrease was obtained for the whole period of selection. In other words, when  $\alpha$  is high enough, though genetic gain is lower, producing genetic gain has no perceptible cost in terms of coancestry. De Cara et al. (2011) has already shown similar results,



**FIGURE 1** Evolution over time of genetic gain (left panel) and true coancestry (right panel), for different values of  $\alpha$  (red for  $\alpha = 0.1$  till blue for  $\alpha = 0.9$ ), with  $\beta = 0$ , with the unshuffled dataset and  $h^2 = 0.5134$  (trunk circumference)

**TABLE 1** Average values and standard deviations of genetic gain or true coancestry for trunk circumference ( $h^2 = 0.5134$ ) at generation 20, for the unshuffled dataset ( $S = 0$ ) and shuffled dataset ( $S = 1$ ), and without mate allocation ( $M = 0$ ) or with mate allocation ( $M = 1$ )

	Genetic gain				True coancestry				
	$S = 0$		$S = 1$		$S = 0$		$S = 1$		
	$M = 0$	$M = 1$	$M = 0$	$M = 1$	$M = 0$	$M = 1$	$M = 0$	$M = 1$	
$\alpha = 0.1$									
$\beta = -0.5$	208.1 ± 12.3	210.88 ± 11.7	123.2 ± 6.6	124.3 ± 5.6	0.988 ± 0.005	0.988 ± 0.007	0.985 ± 0.006	0.984 ± 0.007	
$\beta = 0$	207.1 ± 13.3	208.4 ± 10.5	123.1 ± 6.1	123.8 ± 7.1	0.988 ± 0.006	0.990 ± 0.005	0.987 ± 0.006	0.986 ± 0.007	
$\beta = 0.5$	204.7 ± 12.5	203.3 ± 15	121.5 ± 5.4	119.2 ± 4.7	0.992 ± 0.004	0.992 ± 0.004	0.989 ± 0.006	0.990 ± 0.005	
$\alpha = 0.9$									
$\beta = -0.5$	146.4 ± 2.0	150.3 ± 1.6	113.7 ± 1.3	115.3 ± 1.1	0.225 ± 0.001	0.227 ± 0.001	0.229 ± 0.001	0.230 ± 0.001	
$\beta = 0$	74.5 ± 2.1	77.2 ± 2.1	93.3 ± 1.9	93.5 ± 2	0.107 ± 0.002	0.105 ± 0.002	0.181 ± 0.003	0.179 ± 0.003	
$\beta = 0.5$	59.1 ± 2.7	60.8 ± 2.6	77.8 ± 2.7	77.3 ± 2.3	0.115 ± 0.003	0.103 ± 0.002	0.194 ± 0.004	0.173 ± 0.003	

Note: The initial states of genetic gain was  $27.7 \pm 25.9$ , and coancestry was 0.214.

but is only possible when using genomic information (as opposed to pedigree information).

There is, however, no expectation regarding the genetic gain and coancestry variances, since OCS formulates its objective function and constraints in terms of expected values, not of variances. Compared to the initial standard deviation of genetic gain (25.9), simulations showed a consistent decrease over time (Table 1). Surprisingly, the decrease in standard deviation was even more pronounced for high  $\alpha$ , but the coefficient of variation was lower. The same pattern was observed for true coancestry, where the standard deviation decreased in a more pronounced way for high  $\alpha$ , but with a lower coefficient of variation. The lower coefficient of variation for both genetic gain and coancestry for high  $\alpha$  suggests that the risk associated with a targeted genetic gain was better controlled when restricting coancestry, likely due to lower drift.

Different long-term horizons of genetic gain were reached depending on the value of  $\alpha$  (Figure 1). In the relatively short term, less than 6 generations, the achieved genetic gain decreased with increasing  $\alpha$ . Eventually, in the longer term, the optimum  $\alpha$  for genetic gain shifted from lower values to intermediate (at generation 20) and then to higher values of  $\alpha$  (when reaching the selection plateau; Figure S3). The lower the value of  $\alpha$ , the sooner the bend marking the start of the plateau. Such a plateau has already been described in the literature (De Beukelaer et al., 2017; Jannink, 2010), indicating a trade-off between the short- and long-term horizons when setting the importance of gain versus diversity ( $\alpha$ ).

On the opposite, the optimum  $\alpha$  for coancestry (i.e.,  $\alpha = 1$ ) did not change across generations, that is, the same ranking of  $\alpha$  according to coancestries occurred for all generations. The most relevant feature, however, is that the change in coancestry between extreme values of  $\alpha$  was larger than those observed for gain. In the long term (at generation 20), coancestry was multiplied by 10.23 when  $\alpha$  shifted from 0.9 to 0.1, whereas for the same shift of  $\alpha$ , genetic gain was only multiplied by 1.28. Such a difference in scale of response between gain and coancestry is clear even at the first generation of application of OCS. This trend can also be observed in the Pareto curve, where a substantial reduction in coancestry can have a minimum cost in gain whenever  $\alpha$  is set between zero and intermediate values ( $\alpha < 0.5$ ; Figure S1).

### 3.2 | The effect of $\alpha$ as the most explanatory factor after a long run

Statistical analyses of model (1) showed strong adjusted coefficients of determination for both genetic gain (unshuffled:  $r^2 = 0.91$ ; shuffled:  $r^2 = 0.92$ ) and coancestry (unshuffled:  $r^2 = 0.98$ ; shuffled:  $r^2 = 0.99$ ), suggesting a strong explanatory power of the parameters  $\alpha$ ,  $\beta$ , and mate allocation. Overall, for both unshuffled and shuffled datasets,  $\alpha$  was the most explanatory factor, with more than 84.6% of genetic gain variance explained, and more than 97.6% of coancestry variance explained (Table 2). When the dataset is not shuffled, genetic gain was mainly explained by the linear term of  $\alpha$ ,

**TABLE 2** Statistical analysis (model (1)) of the simulations for trunk circumference ( $h^2 = 0.5134$ ), for the unshuffled ( $S = 0$ ) and the shuffled ( $S = 1$ ) datasets, for the genetic gain and true coancestry, at generation 20

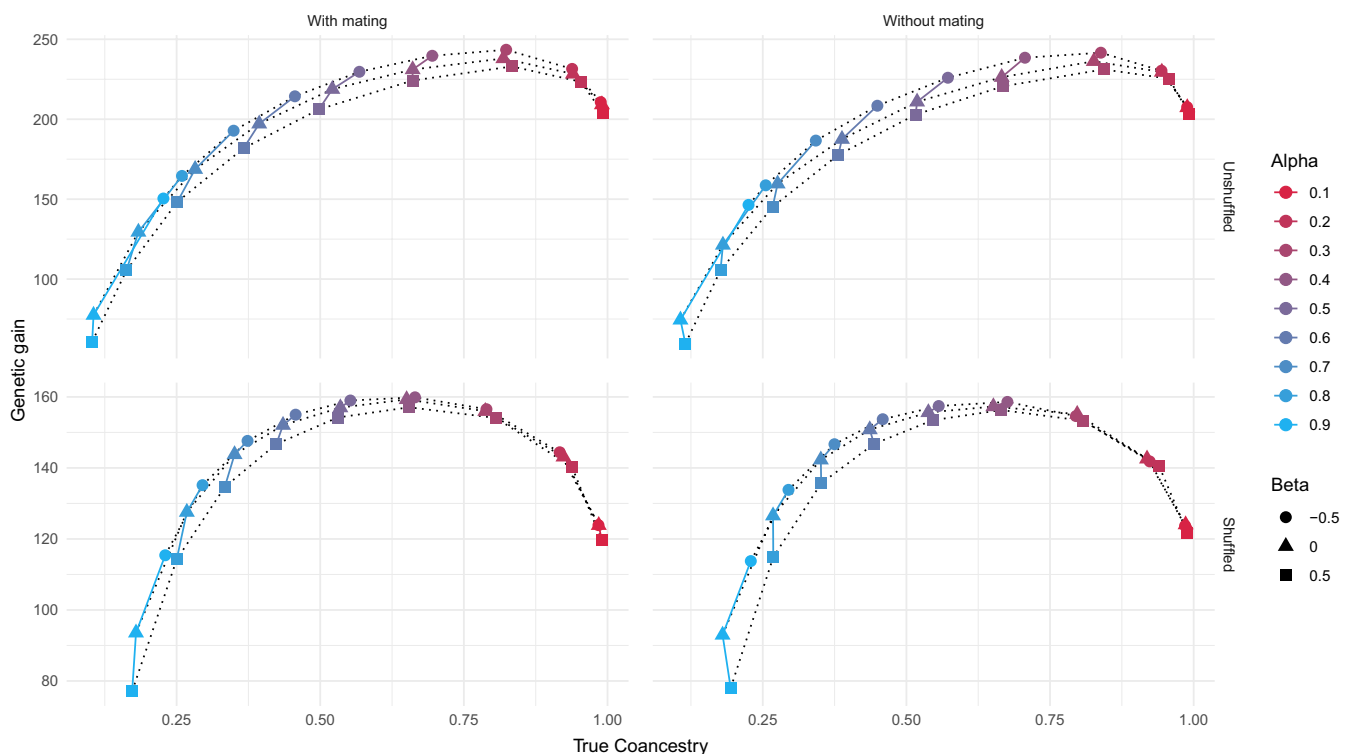
Effect	Genetic gain				True coancestry			
	$S = 0$ ( $r^2 = 0.91$ )		$S = 1$ ( $r^2 = 0.92$ )		$S = 0$ ( $r^2 = 0.98$ )		$S = 1$ ( $r^2 = 0.99$ )	
	Estimate	% Variance	Estimate	% Variance	Estimate	% Variance	Estimate	% Variance
$\alpha$	267***	58.7	276***	15.5	-1.26***	97.5	-1.25***	98.9
$\alpha^2$	-415***	25.9	-310***	72.7	0.151***	0.100	0.236***	0.302
$\beta$	-34.0***	6.49	-11.9***	3.98	-0.0514***	0.434	-0.0153***	0.0470
M	3.35***	0.0877	0.679 <sup>n.s.</sup>	0.0195	-0.00443 <sup>n.s.</sup>	0.00485	-0.00527***	0.00842

Note: Estimate are from model (1), and  $p$ -values from the analysis of variance. Significance levels are \*\*\* $p < .001$ ; \*\* $p < .01$ ; \* $p < .05$ ; <sup>n.s.</sup> $p > .05$ . 'Variance': percentage of variance explained.  $r^2$ : adjusted coefficient of determination of model (1).

whereas when it is shuffled, genetic gain was mainly explained by the quadratic term. This result suggests that when linkage disequilibrium is not fully broken (unshuffled), every bit of increase in  $\alpha$  has a perceptible effect on genetic gain, whereas for a broken linkage disequilibrium (shuffled), low  $\alpha$  does not have any effect on genetic gain, only high values do. Coancestry, on the opposite, is always fully explained by the linear term, suggesting that although the effect of  $\alpha$  is not always perceptible for genetic gain, it always is for coancestry. Mate allocation did only explain 0.0877% of the genetic gain variance in the unshuffled dataset and was not significant in the shuffled dataset, suggesting that mating (defined as the minimization

of progeny homozygosity) had only a small effect on genetic gain. Likewise, mate allocation only explained 0.00485% of the variance of coancestry in the unshuffled dataset, and only 0.00842% in the shuffled dataset.

Favoring individuals with  $H_e \times H_o$  relationship with other individuals (negative  $\beta$ ) increased both genetic gain and coancestry (Table 1).  $\beta$  explained a slightly more important proportion of genetic gain variance for unshuffled dataset (6.49%) than for shuffled dataset (3.98%), suggesting that high linkage disequilibrium can benefit from a management of heterozygous loci. For coancestry,  $\beta$  only explained 0.434% (unshuffled) and 0.0470% (shuffled) of the variance.



**FIGURE 2** The Pareto optimum curve of true coancestry versus genetic gain, at generation 20, for different values of  $\alpha$  (red for  $\alpha = 0.1$  till blue for  $\alpha = 0.9$ ) and  $\beta$  (circle for  $\beta = -0.5$ ; triangle for  $\beta = 0$ ; square for  $\beta = 0.5$ ), with  $h^2 = 0.5134$  (trunk circumference). Left panels with mate allocation and right panels without mate allocation (random mating); top panels with the unshuffled dataset and bottom panels with the shuffled dataset

In the unshuffled dataset, when analyzing the effect of  $\beta$  on genetic gain with a fixed value of  $\alpha$  (model (2)),  $\beta$  was not significant for  $\alpha = 0.1$  (Fisher's  $F$  test,  $p = 0.177$ ), but significant for  $\alpha = 0.9$  (Fisher's  $F$  test,  $p < .001$ ); the same pattern was observed in the shuffled dataset. The fact that  $\beta$  cannot have an impact for low  $\alpha$  was expected by construction, but its significance for high  $\alpha$  pinpoints that managing heterozygous loci can be beneficial in terms of genetic gain when there is sufficient diversity. On the opposite,  $\beta$  had a significant effect on coancestry (Fisher's  $F$  test, all  $p < 0.01$ ), for low and high values of  $\alpha$ , in the unshuffled and shuffled dataset. Overall, genetic gain and coancestry were mostly determined by  $\alpha$ , even if the parameter was defined at the OCS level, and so, being blind to mate allocation. This result highlights the strikingly consistency of predictions with the genetic contribution framework. Similar results have been shown in previous studies (see Clark et al., 2013).

### 3.3 | Favoring $H_e \times H_o$ relationship as the most sustainable strategy

The effect of  $\beta$  after twenty generations on genetic gain and true coancestry were different according to  $\alpha$  (Figure 2). In the unshuffled dataset, for the lowest values of  $\alpha$  ( $<0.2$ , i.e., promoting the maximization of genetic gain over the minimization of coancestry), both genetic gain and coancestry were strongly influenced by  $\alpha$ , but only negligibly by  $\beta$ . At this horizon, the population is detached from the Pareto curve. However, for larger  $\alpha$  ( $>0.2$ , i.e., promoting the minimization of coancestry over the maximization of gain), favoring  $H_e \times H_o$  relationship ( $\beta < 0$ ) resulted in best performances, that is, a higher genetic gain for a given value of true coancestry. In other words, favoring  $H_e \times H_o$  relationship allows the population to be on a higher Pareto curve (Figure 2). In addition, although mate allocation was almost negligible compared with  $\alpha$ , it slightly shifted the Pareto curve upwards. On the opposite, in the shuffled dataset,  $\beta = 0$  and  $\beta = -0.5$  are on the same Pareto curve, suggesting again that the management of heterozygous loci would mainly be beneficial for population with a high linkage disequilibrium.

Considering an alternative way of assessing the potential of a breeding program by measuring the GEBV of the population from favorable alleles that are not fixed yet, namely the breeding potential, the best strategy for the unshuffled dataset was to promote  $H_e \times H_o$  relationship, especially for high values of  $\alpha$  (Figure 3). Except for  $\alpha = 0.1$ , the breeding potential of  $\beta = -0.5$  was significantly higher than other values of  $\beta$  (Student's  $t$  test, all  $p < .05$ ). For shuffled dataset however, the best strategy was to promote  $H_e \times H_o$  relationship only for high values of  $\alpha$ , as the breeding potential of  $\beta = -0.5$  was significantly higher than other values of  $\beta$  only when  $\alpha > 0.6$  (Student's  $t$  test, all  $p < .05$ ). The breeding potential of  $\beta = -0.5$  and of a given  $\alpha$  can almost reach that of a lower value of  $\alpha$ . Therefore, favoring  $H_e \times H_o$  relationship would increase short-term genetic gain, while guaranteeing a high selection plateau—as its level is determined by  $\alpha$ , not  $\beta$ .

## 4 | DISCUSSION

### 4.1 | Long-term strategy in breeding programs

In a multigeneration breeding program, being able to select favorable alleles with little losses of favorable alleles on other loci would be the most desirable feature, that is, avoiding the Bulmer effect (Bulmer, 1971). Drift often occurs through unwanted genetic hitchhiking when favorable and unfavorable alleles are trapped by limited sampling in continuous segments in linkage disequilibrium. There is therefore always a risk of loss as recombination might not be able to cope with the pace of selection and sampling generating the unfavorable linkage. One way to render recombination more efficient without slowing down the selection process would be to favor the pairing of candidates with a high potential for segregation in the offspring. It can be done more or less explicitly. One of the classical approaches, as shown in previous works (Allier et al., 2019; De Beukelaer et al., 2017; Jannink, 2010), consists in accounting for diversity through the trade-off parameter  $\alpha$ , where diversity among candidates is modeled through relatedness or coancestry. This weighted approach, or the constrained formulation, can enhance the selection plateau, but often at the cost of slowing down the rate of progress. When such a perspective is applied to late maturing perennials, the cost in time for slow progress becomes a heavy drawback.

Another alternative to accelerate breeding without the drawback of drift is to minimize the uncertainties concerning the consequences of selection decisions, so that decisions can be based on sound predictions of the impact of selection on future generations. A way of doing this is to account for the  $H_e \times H_o$  relationship between candidates, which is generally not considered in classical OCS. We have shown that optimizing mating, and modifying the genomic relationship matrix to account for  $H_e \times H_o$  relationship, that is, gain control over the Mendelian sampling, has always resulted in better performances, for both genetic gain and coancestry. The mating optimization was particularly important in the first generations, as already reported by Toro and Varona (2010).

When focusing on genetic gain (low  $\alpha$ ), better controlling Mendelian sampling had a small effect, meaning that the effect of drift cannot be counterbalanced. However, when considering higher  $\alpha$ , controlling Mendelian sampling, especially by favoring  $H_e \times H_o$  relationship (lower  $\beta$ ) had a strong effect on the Pareto curve. Increasing genetic gain usually means: (i) a lower genetic (and genic) variance after selection, (ii) a higher level of fixation of favorable alleles, which constitutes the matter making up genetic gain, and (iii) a higher level of negative linkage disequilibrium covariance due to the Bulmer effect. The extra gain obtained from  $\beta < 0$  could come from using more efficiently the genic variance, resulting in more depletion compared to that of higher  $\beta$  levels, and thus converting this available variation into favorable allele fixation, or likewise unfavorable allele elimination.



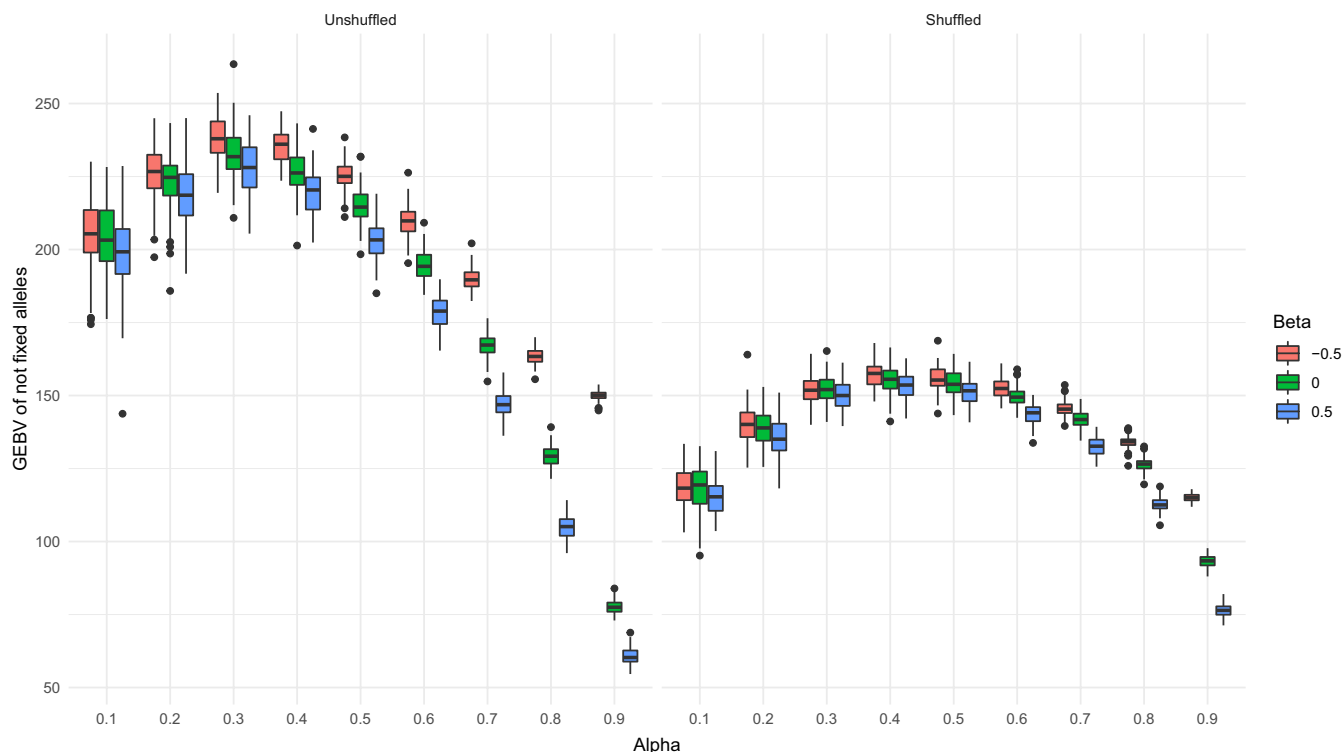


FIGURE 3 Boxplots of GEBV of not fixed alleles, at generation 20, for different values of  $\alpha$  and  $\beta$ , with the unshuffled (right panel) and the shuffled (left panel) dataset,  $h^2 = 0.5134$  (trunk circumference)

## 4.2 | Alternative construction of genomic relationship matrix

Several studies proposed alternative formulations of the realized genomic relationship matrix (Fragomeni et al., 2017; Nejati-Javaremi et al., 1997; VanRaden, 2008) to improve accuracy in genomic evaluation, mainly assessing the efficiency of genomic information compared to genealogical information. Using alternative formulations might even lead to different long-term performance when used in the context of OCS (Gebregiwergis et al., 2020). However, a matrix that increases accuracy of genomic predictions does not necessarily measure inbreeding efficiently (Villanueva et al., 2021), so developing different formulations for different purposes seems preferable. Indeed, genomic information has been used differently in different contexts (as reviewed in Maltecca et al., 2020): minimum coancestry mating (Fernández et al., 2021), selection against unfavorable alleles (Upperman et al., 2019), or genomic selection with dominance effects (Sun et al., 2014). In line with this recommendation, we developed a method specific to GOCS that showed consistently better long-term performances, although genomic evaluation with our alternative formulation ( $G^*$ ) showed a consistently lower accuracy than with  $G$  (5%–10%, data not shown). In addition, when linkage disequilibrium was the highest (unshuffled dataset), our method performed best in terms of the Pareto curve.

Fostering the  $H_e \times H_o$  relationships with the realized genomic relationship matrix might have the consequence of maintaining dominance effects, since it maintains potential for segregation. In

addition to previous studies that showed the importance of accounting for dominance effects in genomic evaluation (Sun et al., 2013; Toro & Varona, 2010), our results show that a strategy that maintains dominance effects is also important for breeding programs. Consequently, we can argue that GOCS might benefit from including dominance effects in genomic evaluation, and optimize progeny homozygosity accordingly (Fernández et al., 2021). Whether dominance effects and its variance are only important to account for as a correction term in genomic evaluation (e.g., to improve accuracy), or have deeper implications in the population dynamic remains an open question.

## 4.3 | Variance in OCS

The main challenge of OCS lies in the management of stochasticity: the objective function, as stated above, is formulated with expected values, and not with variances, thus neglecting the variability caused by the uncertainties of random mating and Mendelian sampling. This leads to stochasticity around the predicted Pareto optima, in which analytical formula are only known for very few special cases (Garcia-Cortes et al., 2013). In our study, the undesired stochasticity was fixed by mate allocation, making segregation and environmental deviation the only sources of random variation. Mate allocation did, however, have a surprisingly low proportion of variance explained compared with what was reported previously (Hamrick & Godt, 1996; Nybom, 2004). The main challenge remains to efficiently

convert the remaining additive variance (from segregation and environmental deviation) in future genetic gain (Santos et al., 2019), which can be done by integrating variance terms in the objective function.

Introducing variability in the parameter  $\alpha$  and  $\beta$  could also be desirable in the case of multigeneration breeding, such as considering different values of  $\alpha$  and  $\beta$  at each generation, depending on the current state of the population. For instance, considering a high value of  $\alpha$  (high diversity) could be important at the very short term to prevent losses of favorable alleles in low frequency, but once the Bulmer effect is absorbed by recombination, it could be safe to switch to a more aggressive strategy such as with lower values of  $\alpha$ . Preliminary works showed indeed that a geometrically decreasing  $\alpha$  along the generations with a rate of 0.99 brings better long-term performances. Differential selection over generation is therefore a field worth investigating, and warrants further studies.

## 5 | CONCLUSION

In this article, we have extended OCS by proposing an alternative formulation of the realized genomic relationship matrix that better accounts for the Mendelian sampling. In multigeneration breeding programs, it is important to account for diversity to reach a higher selection plateau, even though the speed at which it is reached can be slow. We have shown by and large that the population dynamic is overall dominated by the trade-off value  $\alpha$  between genetic gain and genetic diversity. However, better accounting for Mendelian sampling, even implicitly as proposed here by fostering individuals with multiple loci in  $H_e \times H_o$  relationship with others, could minimize the speed problem, by “accelerating” the breeding while maintaining a high level of diversity and selective potential for future generations.

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## CONFLICT OF INTEREST

The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

## DATA AVAILABILITY STATEMENT

The data that support the findings of this study are openly available in DRYAD at <https://doi.org/10.5061/dryad.0rxwdb51k>.

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## REFERENCES

- Akdemir, D., Beavis, W., Fritsche-Neto, R., Singh, A. K., & Isidro-Sánchez, J. (2019). Multi-objective optimized genomic breeding strategies for sustainable food improvement. *Heredity*, 122(5), 672–683. <https://doi.org/10.1038/s41437-018-0147-1>
- Akdemir, D., & Sánchez, J. I. (2016). Efficient breeding by genomic mating. *Frontiers in Genetics*, 7, 210. <https://doi.org/10.3389/fgene.2016.00210>
- Allier, A., Lehermeier, C., Charcosset, A., Moreau, L., & Teyssède, S. (2019). Improving short-and long-term genetic gain by accounting for within-family variance in optimal cross-selection. *Frontiers in Genetics*, 10, 1006. <https://doi.org/10.3389/fgene.2019.01006>
- Avendaño, S., Woolliams, J. A., & Villanueva, B. (2004). Mendelian sampling terms as a selective advantage in optimum breeding schemes with restrictions on the rate of inbreeding. *Genetics Research*, 83(1), 55–64. <https://doi.org/10.1017/S0016672303006566>
- Boyd, S., Boyd, S. P., & Vandenberghe, L. (2004). *Convex optimization*. Cambridge University Press.
- Brisbane, J. R., & Gibson, J. P. (1995). Balancing selection response and rate of inbreeding by including genetic relationships in selection decisions. *Theoretical and Applied Genetics*, 91(3), 421–431. <https://doi.org/10.1007/BF00222969>
- Bulmer, M. (1971). The effect of selection on genetic variability. *The American Naturalist*, 105(943), 201–211. <https://doi.org/10.1086/282718>
- Clark, S. A., Kinghorn, B. P., Hickey, J. M., & van der Werf, J. H. (2013). The effect of genomic information on optimal contribution selection in livestock breeding programs. *Genetics Selection Evolution*, 45(1), 1–8. <https://doi.org/10.1186/1297-9686-45-44>
- Cole, J. B., & VanRaden, P. M. (2011). Use of haplotypes to estimate Mendelian sampling effects and selection limits. *Journal of Animal Breeding and Genetics*, 128(6), 446–455. <https://doi.org/10.1111/j.1439-0388.2011.00922.x>
- Daetwyler, H. D., Villanueva, B., Bijma, P., & Woolliams, J. A. (2007). Inbreeding in genome-wide selection. *Journal of Animal Breeding and Genetics*, 124(6), 369–376. <https://doi.org/10.1111/j.1439-0388.2007.00693.x>
- De Beukelaer, H., Badke, Y., Fack, V., & De Meyer, G. (2017). Moving beyond managing realized genomic relationship in long-term genomic selection. *Genetics*, 206(2), 1127–1138. <https://doi.org/10.1534/genetics.116.194449>
- De Cara, M. A. R., Fernández, J., Toro, M. A., & Villanueva, B. (2011). Using genome-wide information to minimize the loss of diversity in conservation programmes. *Journal of Animal Breeding and Genetics*, 128(6), 456–464. <https://doi.org/10.1111/j.1439-0388.2011.00971.x>
- Faivre-Rampant, P., Zaina, G., Jorge, V., Giacomello, S., Segura, V., Scalabrin Guérin, V., De Paoli, E., Aluome, C., Viger, M., Cattonaro, F., Payne, A., PaulStephenRaj, P., Le Paslier, M. C., Berard, A., Allwright, M. R., Villar, M., Taylor, G., Bastien, C., & Morgante, M. (2016). New resources for genetic studies in *Populus nigra*: Genome-wide SNP discovery and development of a 12k Infinium array. *Molecular Ecology Resources*, 16(4), 1023–1036. <https://doi.org/10.1111/1755-0998.12513>
- Fernández, J., Villanueva, B., & Toro, M. A. (2021). Optimum mating designs for exploiting dominance in genomic selection schemes for aquaculture species. *Genetics Selection Evolution*, 53(1), 1–13. <https://doi.org/10.1186/s12711-021-00610-9>
- Fragomeni, B. O., Lourenco, D. A., Masuda, Y., Legarra, A., & Misztal, I. (2017). Incorporation of causative quantitative trait nucleotides in single-step GBLUP. *Genetics Selection Evolution*, 49(1), 1–11. <https://doi.org/10.1186/s12711-017-0335-0>

- Gao, X., & Martin, E. R. (2009). Using allele sharing distance for detecting human population stratification. *Human Heredity*, 68(3), 182–191. <https://doi.org/10.1159/000224638>
- García-Cortes, L. A., Legarra, A., Chevalet, C., & Toro, M. A. (2013). Variance and covariance of actual relationships between relatives at one locus. *PLoS One*, 8(2), e57003. <https://doi.org/10.1371/journal.pone.0057003>
- Gebregiwergis, G. T., Sørensen, A. C., Henryon, M., & Meuwissen, T. H. E. (2020). Controlling coancestry and thereby future inbreeding by optimum-contribution selection using alternative genomic-relationship matrices. *Frontiers in Genetics*, 11, 345. <https://doi.org/10.3389/fgene.2020.00345>
- Goddard, M. (2009). Genomic selection: Prediction of accuracy and maximisation of long term response. *Genetica*, 136(2), 245–257. <https://doi.org/10.1007/s10709-008-9308-0>
- Gómez-Romano, F., Villanueva, B., Fernández, J., Woolliams, J. A., & Pong-Wong, R. (2016). The use of genomic coancestry matrices in the optimisation of contributions to maintain genetic diversity at specific regions of the genome. *Genetics Selection Evolution*, 48(1), 1–17. <https://doi.org/10.1186/s12711-015-0172-y>
- Grattapaglia, D. (2017). Status and perspectives of genomic selection in forest tree breeding. In R. Varshney, M. Roorkiwal & M. Sorrells (Eds.), *Genomic selection for crop improvement* (pp. 199–249). Springer.
- Hamrick, J. L., & Godt, M. W. (1996). Effects of life history traits on genetic diversity in plant species. *Philosophical Transactions of the Royal Society of London. Series B: Biological Sciences*, 351(1345), 1291–1298. <https://doi.org/10.1098/rstb.1996.0112>
- Hayes, B. J., Bowman, P. J., Chamberlain, A. J., & Goddard, M. E. (2009). Invited review: Genomic selection in dairy cattle: Progress and challenges. *Journal of Dairy Science*, 92(2), 433–443. <https://doi.org/10.3168/jds.2008-1646>
- James, J. W., & McBride, G. (1958). The spread of genes by natural and artificial selection in closed poultry flock. *Journal of Genetics*, 56(1), 55. <https://doi.org/10.1007/BF02984720>
- Jannink, J. L. (2010). Dynamics of long-term genomic selection. *Genetics Selection Evolution*, 42(1), 1–11. <https://doi.org/10.1186/1297-9686-42-35>
- Li, Y., Kadarmideen, H. N., & Dekkers, J. C. M. (2008). Selection on multiple QTL with control of gene diversity and inbreeding for long-term benefit. *Journal of Animal Breeding and Genetics*, 125(5), 320–329. <https://doi.org/10.1111/j.1439-0388.2007.00717.x>
- Maltecca, C., Tiezzi, F., Cole, J. B., & Baes, C. (2020). Symposium review: Exploiting homozygosity in the era of genomics – Selection, inbreeding, and mating programs. *Journal of Dairy Science*, 103(6), 5302–5313. <https://doi.org/10.3168/jds.2019-17846>
- Meuwissen, T. H. E. (1997). Maximizing the response of selection with a predefined rate of inbreeding. *Journal of Animal Science*, 75(4), 934–940. <https://doi.org/10.2527/1997.754934x>
- Meuwissen, T. H. E., Hayes, B. J., & Goddard, M. E. (2001). Prediction of total genetic value using genome-wide dense marker maps. *Genetics*, 157(4), 1819–1829. <https://doi.org/10.1093/genetics/157.4.1819>
- Meuwissen, T. H. E., Sonesson, A. K., Gebregiwergis, G., & Woolliams, J. A. (2020). Management of genetic diversity in the era of genomics. *Frontiers in Genetics*, 11, 880. <https://doi.org/10.3389/fgene.2020.00880>
- Muñoz, F., & Sánchez, L. (2020). breedR: Statistical Methods for Forest Genetic Resources Analysts. R package version 0.12-5. <https://github.com/famuvie/breedR>
- Nejati-Javaremi, A., Smith, C., & Gibson, J. P. (1997). Effect of total allelic relationship on accuracy of evaluation and response to selection. *Journal of Animal Science*, 75(7), 1738–1745. <https://doi.org/10.2527/1997.7571738x>
- Nybom, H. (2004). Comparison of different nuclear DNA markers for estimating intraspecific genetic diversity in plants. *Molecular Ecology*, 13(5), 1143–1155. <https://doi.org/10.1111/j.1365-294X.2004.02141.x>
- Pégard, M., Rogier, O., Bérard, A., Favier-Rampant, P., Le Paslier, M. C., Bastien, C., Jorge, V., & Sánchez, L. (2019). Sequence imputation from low density single nucleotide polymorphism panel in a black poplar breeding population. *BMC Genomics*, 20(1), 1–16. <https://doi.org/10.1186/s12864-019-5660-y>
- Pégard, M., Segura, V., Muñoz, F., Bastien, C., Jorge, V., & Sánchez, L. (2020). Favorable conditions for genomic evaluation to outperform classical pedigree evaluation ed by a proof-of-concept study in poplar. *Frontiers in Plant Science*, 11, 1552. <https://doi.org/10.3389/fpls.2020.581954>
- Pryce, J. E., Hayes, B. J., & Goddard, M. E. (2012). Novel strategies to minimize progeny inbreeding while maximizing genetic gain using genomic information. *Journal of Dairy Science*, 95(1), 377–388. <https://doi.org/10.3168/jds.2011-4254>
- R Core Team. (2020). *R: A language and environment for statistical computing*. Vienna, Austria: R Foundation for Statistical Computing. <https://www.R-project.org/>
- Rutkoski, J., Singh, R. P., Huerta-Espino, J., Bhavani, S., Poland, J., Jannink, J. L., & Sorrells, M. E. (2015). Efficient use of historical data for genomic selection: A case study of stem rust resistance in wheat. *The Plant Genome*, 8(1), plantgenome2014-09. <https://doi.org/10.3835/plantgenome2014.09.0046>
- Sánchez, L., Caballero, A., & Santiago, E. (2006). Palliating the impact of fixation of a major gene on the genetic variation of artificially selected polygenes. *Genetics Research*, 88(2), 105–118. <https://doi.org/10.1017/S0016672306008421>
- Santos, D. J. A., Cole, J. B., Lawlor, T. J. Jr, VanRaden, P. M., Tonhati, H., & Ma, L. (2019). Variance of gametic diversity and its application in selection programs. *Journal of Dairy Science*, 102(6), 5279–5294. <https://doi.org/10.3168/jds.2018-15971>
- Sargolzaei, M., Chesnais, J. P., & Schenkel, F. S. (2014). A new approach for efficient genotype imputation using information from relatives. *BMC Genomics*, 15(1), 1–12. <https://doi.org/10.1186/1471-2164-15-478>
- Searle, S. R., Casella, G., & McCulloch, C. E. (2009). *Variance components* (Vol. 391). John Wiley & Sons.
- Sonesson, A. K., Woolliams, J. A., & Meuwissen, T. H. E. (2012). Genomic selection requires genomic control of inbreeding. *Genetics Selection Evolution*, 44(1), 1–10. <https://doi.org/10.1186/1297-9686-44-27>
- Sun, C., VanRaden, P. M., Cole, J. B., & O'Connell, J. R. (2014). Improvement of prediction ability for genomic selection of dairy cattle by including dominance effects. *PLoS One*, 9(8), e103934. <https://doi.org/10.1371/journal.pone.0103934>
- Sun, C., VanRaden, P. M., O'Connell, J. R., Weigel, K. A., & Gianola, D. (2013). Mating programs including genomic relationships and dominance effects. *Journal of Dairy Science*, 96(12), 8014–8023. <https://doi.org/10.3168/jds.2013-6969>
- Toro, M. A., & Varona, L. (2010). A note on mate allocation for dominance handling in genomic selection. *Genetics Selection Evolution*, 42(1), 1–9. <https://doi.org/10.1186/1297-9686-42-33>
- Upperman, L. R., Kinghorn, B. P., MacNeil, M. D., & Van Eenennaam, A. L. (2019). Management of lethal recessive alleles in beef cattle through the use of mate selection software. *Genetics Selection Evolution*, 51(1), 1–16. <https://doi.org/10.1186/s12711-019-0477-3>
- VanRaden, P. M. (2008). Efficient methods to compute genomic predictions. *Journal of Dairy Science*, 91(11), 4414–4423. <https://doi.org/10.3168/jds.2007-0980>
- Varona, L., & Misztal, I. (1999). Prediction of parental dominance combinations for planned matings, methodology, and simulation results. *Journal of Dairy Science*, 82(10), 2186–2191. [https://doi.org/10.3168/jds.S0022-0302\(99\)75463-9](https://doi.org/10.3168/jds.S0022-0302(99)75463-9)
- Villanueva, B., Fernández, A., Saura, M., Caballero, A., Fernández, J., Morales-González, E., Toro, M. A., & Pong-Wong, R. (2021). The value of genomic relationship matrices to estimate levels of inbreeding. *Genetics Selection Evolution*, 53(1), 1–17. <https://doi.org/10.1186/s12711-021-00635-0>

- Vitezica, Z. G., Varona, L., & Legarra, A. (2013). On the additive and dominant variance and covariance of individuals within the genomic selection scope. *Genetics*, *195*(4), 1223–1230. <https://doi.org/10.1534/genetics.113.155176>
- Woolliams, J. A., & Mäntysaari, E. A. (1995). Genetic contributions of Finnish Ayrshire bulls over four generations. *Animal Science*, *61*(2), 177–187. <https://doi.org/10.1017/S1357729800013709>
- Woolliams, J. A., Pong-Wong, R., & Villanueva, B. (2002). Strategic optimisation of short-and long-term gain and inbreeding in MAS and non-MAS schemes. In *Proceedings of the 7th world congress on genetics applied to livestock production* (Vol. 33, pp. 155–162). Montpellier.

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