An Allosteric Model of the Molecular Interactions of Excitation–Contraction Coupling in Skeletal Muscle

EDUARDO RÍOS, MILOSLAV KARHANEK, JIANJIE MA, and Adom González

From the Department of Physiology, Rush University School of Medicine, Chicago, Illinois 60612

ABSTRACT A contact interaction is proposed to exist between the voltage sensor of the transverse tubular membrane of skeletal muscle and the calcium release channel of the sarcoplasmic reticulum. This interaction is given a quantitative formulation inspired in the Monod, Wyman, and Changeux model of allosteric transitions in hemoglobin (Monod, J., J. Wyman, and J.-P. Changeux. 1965. Journal of Molecular Biology. 12:88-118), and analogous to one proposed by Marks and Jones for voltage-dependent Ca channels (Marks, T. N., and S. W. Jones. 1992. Journal of General Physiology. 99:367-390). The allosteric protein is the calcium release channel, a homotetramer, with two accessible states, closed and open. The kinetics and equilibrium of this transition are modulated by voltage sensors (dihydropyridine receptors) pictured as four units per release channel, each undergoing independent voltage-driven transitions between two states (resting and activating). For each voltage sensor that moves to the activating state, the tendency of the channel to open increases by an equal (large) factor. The equilibrium and kinetic equations of the model are solved and shown to reproduce well a number of experimentally measured relationships including: charge movement (Q) vs. voltage, open probability of the release channel (Po) vs. voltage, the transfer function relationship P_0 vs. Q, and the kinetics of charge movement, release activation, and deactivation. The main consequence of the assumption of allosteric coupling is that primary effects on the release channel are transmitted backward to the voltage sensor and give secondary effects. Thus, the model reproduces well the effects of perchlorate, described in the two previous articles, under the assumption that the primary effect is to increase the intrinsic tendency of the release channel to open, with no direct effects on the voltage sensor. This modification of the open-closed equilibrium of the release channel causes a shift in the equilibrium dependency of charge movement with voltage. The paradoxical slowing of charge movement by perchlorate also results from reciprocal effects of the channel on the allosterically coupled voltage sensors. The observations of the previous articles plus the simulations in this article constitute functional evidence of allosteric transmission.

Address reprint requests to Dr. Eduardo Ríos, Department of Physiology, Rush University School of Medicine, 1750 West Harrison St., Chicago, IL 60612.

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INTRODUCTION

The first suggestion of mechanical transmission in excitation-contraction (EC) coupling was the well known "plunger" hypothesis of Chandler, Rakowski, and Schneider (1976). Even though no direct biochemical proof exists of a mechanical interaction (see, for instance, Brandt, Caswell, Wen, and Talvenheimo, 1989), the hypothesis has been made more attractive by the elucidation of the structure of the foot, now known to provide a plunger-like structure that spans the triadic gap (reviewed by Fleischer and Inui, 1989, and Ríos, Ma, and González, 1991); by structural features of the triadic junction, recently discovered by Block, Imagawa, Campbell, and Franzini-Armstrong (1988); by suggestions of a fixed stoichiometry between voltage sensors and Ca release channels, derived from binding measurements (Anderson, Grunwald, El-Hashem, Sealock, and Meissner, 1990); and by the functional observations of the effects of perchlorate, described in the previous two articles. In this article we propose a specific form of mechanical interaction and give it a quantitative formulation. This quantitative model makes predictions that are compared with specific experimental results obtained in situations that highly simplify the process under study.

Transmission in EC coupling is known to be complex. Indeed, in addition to what could be called the primary transmission process, through which the depolarization of the T membrane results in sarcoplasmic reticulum (SR) channel opening, there are a number of other processes that reinforce and modulate transmission. Thus, there has been evidence for some time of the coexistence of an inactivation of release, generally believed to be mediated by intracellular Ca²⁺ (Schneider and Simon, 1988), which causes release to decay after a peak. Additionally, there is evidence from fractionated SR (e.g., Meissner, Darling, and Eveleth, 1986), skinned fibers (Donaldson, 1985; Volpe and Stephenson, 1986), and whole cell studies (Jacquemond, Csernoch, Klein, and Schneider, 1991; Pizarro, Csernoch, Uribe, and Ríos, 1992) that a Ca²⁺-induced Ca²⁺ release process may amplify the voltage-controlled release, perhaps accounting for the inactivating portion (or peak) of the release waveform (but see Hollingworth, Harkins, Kurebayashi, Konishi, and Baylor, 1992). Finally, there is substantial agreement on the existence of another feedback mechanism, mediated by Ca²⁺, whereby the released Ca²⁺ affects the voltage sensors of the T membrane, either causing the component Q_{y} of intramembrane charge movement (Pizarro, Csernoch, Uribe, Rodríguez, and Ríos, 1991) or changing its kinetic properties (Pape, Jong, and Chandler, 1992).

Thus, the primary transmission mechanism coexists with three feedback processes, and this complicates the definition and quantification of the primary transmission function. Through what is known about the processes underlying the feedback mechanisms, we have designed experimental approaches or measurements that circumvent the complication and aim at quantifying the primary mechanism. In this article we describe those approaches, use them to quantify the transmission function in its simplest form, and then compare the simplified experimental results with the model. The model is an adaptation of the one developed by Monod, Wyman, and Changeux (1965) to describe allosteric transitions in hemoglobin and other multimeric proteins. Noteworthy in this model is that the original idea of a mechanical interaction (Chandler et al., 1976) is kept, while the "rigid link" aspect of it is abandoned. A similar application of the model of Monod et al. (1965) was introduced recently by Marks and Jones (1992) to explain gating in voltage-dependent Ca^{2+} channels.

METHODS

All the results were obtained on cut frog semitendinosus muscle fibers, with the voltage clamp and Ca²⁺ measurement techniques described in the first article of this series (González and Ríos, 1993). Specifically, all the data were obtained in a double Vaseline gap on slack fibers held at -80 or -90 mV, using antipyrylazo III (ApIII) for monitoring $\Delta Ca^{2+}(t)$, with solutions described in Table I of the first article of this series (González and Ríos, 1993) and in Csernoch, Pizarro, Uribe, Rodríguez, and Ríos (1991). Intramembrane charge movement currents were measured using pulses between -110 and -90 mV to elicit control currents, and no correction was introduced for charge in the controls (cf. González and Ríos, 1993, for discussion of errors).

Release flux $(\dot{R}(t))$ was derived from the calcium transients as described by González and Ríos (1993). A correction for depletion of calcium in the SR (Schneider, Simon, and Szucs, 1987) was applied to $\dot{R}(t)$ records to yield corrected records, $\dot{R}_c(t)$. This correction, Eq. 1 of González and Ríos (1993), yields an estimate of calcium content in the SR (Ca_{SR}) at rest. All experiments were carried out at or near 10°C. Double pulse protocols, which simplified the release under study, are described below.

RESULTS

In this section we first present the set of results that will be compared with simulations. The simulations are then presented in a Theory section. The goal is to study the primary transmission, as obtained after reducing as much as possible the three feedback mechanisms enumerated before: namely, Ca^{2+} -induced Ca^{2+} release, inactivation of Ca release flux, and the feedback processes that either cause or modify Q_{γ} . Since the measured variable, Ca release flux, can be thought of as the product of a permeability (or a conductance) and a driving force, a correction for depletion was desirable so that the release flux would reflect only the gated variable of interest, the permeability or openness of the release pathway.

A Conditioning Pulse Protocol Simplifies the Study

The procedures followed to avoid the complications due to feedback and depletion are twofold. First, we concentrated on the steady (or minimum) component of release flux, \dot{R}_m , rather than the peak or inactivating portion, which may be due to Ca²⁺-induced Ca release (Jacquemond et al., 1991; Pizarro et al., 1992; but cf. Hollingworth et al., 1992). Second, we carried out the experiments with a protocol proposed to us by Dr. Bruce Simon (used in Simon and Schneider, 1988, and Simon and Hill, 1992, and similar to protocol 1 of Csernoch et al., 1991) in which the test pulses to various voltages are preceded by a large conditioning pulse (Fig. 1).

The conditioning pulse has several purposes: it reduces the peak of release in the subsequent waveform, facilitating the measurement of the maintained flux; also, it largely eliminates the variability introduced by the phenomenon of depletion of Ca^{2+} in the SR, as it essentially equalizes the depletion among test pulses of different

voltage by introducing a similar depletion before the test pulses (the magnitude of which is illustrated below).

Moreover, we have found that other errors contribute to differences between individual Ca^{2+} transients and associated release records even if they are generated with the same pulses. These changes can be due to an increase in dye concentration as the dye diffuses from the ends of the fiber segment, plus other changes in uncontrolled variables. Perhaps the greatest benefit of the conditioning pulse technique is that each conditioning pulse of fixed voltage and duration provides a



FIGURE 1. Ca transients and Ca release flux elicited with a double pulse protocol. (Top) Schematic of pulse pattern. The holding potential was -80 mV. The test potential was variable and is indicated next to each release record. The second trace is the Ca transient elicited by a conditioning pulse and a test pulse to 0 mV. From this and other transients the records labeled release flux were derived, using the following removal model parameters: $k_{\text{OFF Ca T}}$, 1,200 s⁻¹; $k_{\text{ON Ca T}}$, 125 μ M⁻¹ s⁻¹; $k_{OFF Ca P}$, 1.0 s⁻¹; $k_{\rm ON \ Ga\ P}$, 20 μ M⁻¹ s⁻¹; $k_{\rm OFF \ Mg\ P}$, 9.0 s⁻¹, $k_{\rm ON \ Mg\ P}$, 0.03 μ M⁻¹ s⁻¹; M, 0.5 mM s⁻¹; $K_{\rm D}$ pump, 1.0 μΜ; [P], 300 μΜ; [T], 240 μΜ; [Mg²⁺], 900 µM; [EGTA], 5 mM; $k_{\rm ON \ Ca \ EGTA}$, 2.0 μ M⁻¹ s⁻¹; $k_{\text{OFF Ca EGTA}}$, 6.0 s⁻¹. Fiber 827. External solution, Ca-Co (González and Ríos, 1993); internal solution, 15 EGTA with calcium added for a nominal [Ca²⁺] of

20 nM. Diameter, 114 μ m; linear capacitance, 16.2 nF; concentration of ApIII ranged between 720 μ M at the beginning and 838 at the end of the series, which took 30 min to complete. Records are single sweeps. Temperature, 10°C.

measure of the state of the release system, which then can be used to normalize the release flux measured during the test pulse.

Some of the advantages of this protocol are exemplified in the experiment represented in Figs. 1–4. Fig. 1 shows the pulse protocol, one of several records of $[Ca^{2+}]_i(t)$ (calcium transients), and representative release flux records derived from the calcium transients. Fig. 2 illustrates an additional stage of analysis, the correction for depletion that resulted in the records labeled $\dot{R}_c(t)$ (thick traces). The figure illustrates two records obtained with exactly the same pulse protocol (a conditioning

pulse followed by a test pulse to -10 mV) early in the sequence (top records) and near the end of the experiment some 30 min later (middle records). The ratio of the corrected (thick) to the uncorrected (thin) flux during the test pulse gives the estimated magnitude of depletion caused by the conditioning pulse. This depletion is ~60% for the pulse shown early in the experiment and ~50% in the late record.

In this and other experiments, the release flux recorded during the conditioning pulse steadily decreased during the experiment. Additionally, the estimate of Ca content in the SR obtained from the depletion correction procedure (Ca_{SR}) decreased



FIGURE 2. Effects of the conditioning pulse. The top and middle records in thin trace are $\dot{R}(t)$ records obtained with a conditioning pulse (+20 mV) followed by a test pulse to -10 mV. The top record was obtained early and the middle record some 30 min later. The middle record is the record at -10 mV in Fig. 1 after digital filtering (7 ms smoothing). The thick traces are $\dot{R}_c(t)$, obtained from the corresponding $\dot{R}(t)$ using Eq. 1 of González and Ríos (1993). The value of Ca_{SR} was 1.5 mM (early) and 1.2 mM (late). The bottom records are the corrected records scaled to match the levels of sustained release at the end of the conditioning pulse (the late record was multiplied by 1.94).

substantially. This indicates that the decay in release flux was at least in part due to depletion. Normalization or scaling of the records to equalize the amplitude of the conditioning release waveform is illustrated in the bottom pair of records in the figure. The value of \dot{R}_m in the early and late test waveforms at -10 mV was 0.53 and 0.49 of \dot{R}_m in conditioning waveforms. Thus the normalization procedure reconciled the results to within a few percent. Fig. 4 plots values of \dot{R}_m in the test pulse divided by \dot{R}_m during the preceding conditioning pulse (so that the value at +20 mV is ~ 1). This normalization gets rid of the variability: after normalization all the values of release during the test pulses fell on the same curves, $\dot{R}_m(V)$ and $\dot{R}_m(Q)$ (Fig. 4).

Another problem in modeling transmission at the triad is posed by the existence of Q_{γ} . Even though there is universal agreement that Q_{γ} originates at EC coupling voltage sensors and participates in EC coupling, its kinetics, and for some researchers its existence, cannot be accounted for without considering processes of feedback mediated by changes in $[Ca^{2+}]_i$. Therefore, Q_{γ} is beyond the scope of the present model. In our view (Csernoch et al., 1991; García, Pizarro, Ríos, and Stefani, 1991; Pizarro et al., 1991; Szücs, Csernoch, Magyar, and Kovács, 1991; González and Ríos, 1992) Q_{γ} can be reduced or eliminated by the presence of high concentrations of calcium buffers, which have the direct effect of lowering the $[Ca^{2+}]_i$ and a cumulative depleting effect as the fiber is pulsed repeatedly in their presence. All the experiments simulated here were carried out in the presence of 15 mM EGTA intracellu-



FIGURE 3. Charge movement currents during test pulses preceded by conditioning. Same fiber and pulses as in Fig. 1. Records are the differences of a single test and the average of four control currents (obtained in positive-going pulses between -110 and -90 mV). Difference records were corrected for a horizontal pedestal calculated between 70 and 100 ms (except for pulses to 0 mV or greater, where the pedestal was measured at 30–40 ms).

larly; the Ca transients were small and were detectable because in all cases there were high concentrations of the calcium-sensitive dye in the cells. Charge movement currents had little kinetic evidence of Q_{γ} (Fig. 3) and Q(V) dependencies were well described by single Boltzmann distributions, an indication that Q_{γ} was small (Hui and Chandler, 1990). As described by Csernoch et al. (1991), the large conditioning pulse, which reduces the inactivating portion of release caused by a subsequent pulse, also reduces the hump component of charge movement current elicited by the subsequent pulse (or slows it, as recently argued by Hui and Chen, 1992). The conditioning pulse protocol used routinely here thus caused an added simplification, a reduction or slowing of Q_{γ} .

Representative equilibrium data using the conditioning pulse protocol are shown in Fig. 4. They include Q(V), $\dot{R}_m(V)$, and the transfer function $\dot{R}_m(Q)$. The dotted line in Fig. 4 B is the best fit to $R_m(Q)$ with a power function $y = aQ^{2\cdot78}$ (where a is a constant).

Effects of Perchlorate

The model will also be used to predict the effect of ClO_4^- on all the variables under the sole assumption (a hypothesis, substantiated in the second article of this series)



FIGURE 4. Voltage dependencies and transfer function. (A) Plots of charge (triangles, averages of ON and OFF) and steady release flux during test pulses as a function of test pulse voltage. Same records as in Figs. 1, 2, and 3. Release records were corrected for depletion (example in Fig. 2) and individually normalized to the steady level of release during the conditioning pulse. Continuous lines are obtained with Eqs. 6 and 7 and the parameter values listed in the 827 row of Table I. (To obtain Q(V), Eq. 7 was multiplied by 23.1 nC/ μ F, an estimate of Q_{max} . $P_0(V)$ was normalized in the same way as the experimental records, dividing by the theoretical value $P_{o}(20 \text{ mV})$). The dashed curve represents the best fit Boltzmann function of parameters: $Q_{\text{max}} = 23 \text{ nC}/\mu\text{F}, K = 13.4$ mV, and V = -26 mV. (B) The transfer function $R_m(Q)$ (symbols). The continuous line was obtained plotting the theoretical function $P_{o}(V)$ vs. the theoretical Q(V). The dashed line is $aQ^{2.78}$ (where a is a constant).

that ClO_4^- increases the tendency of the release channel to open. A complete example of the effects of 8 mM ClO_4^- on the release flux elicited with the conditioning pulse protocol is given in Fig. 5. The corresponding voltage dependencies of charge movement and the transfer functions are shown in Fig. 6. In short, ClO_4^- caused a leftward shift of Q(V), a minor steepness increase, a shift of $R_m(V)$, and a shift in $R_m(Q)$ toward lower values of Q with a reduced value of the exponent of the power function describing $\dot{R}_m(Q)$ (the exponent of the best fit power function in 8



FIGURE 5. Effect of ClO_4^- on release flux in a double pulse experiment. The release flux derived from Ca transients (not shown) and corrected for depletion in reference solution and in 8 mM ClO_4^- (obtained later in the experiment). Parameters of removal: $k_{\text{ON Ca P}}$, 100 μ M⁻¹ s⁻¹; $k_{\text{OFF Mg P}}$, 3 s⁻¹; *M*, 1.0 mM s⁻¹; [P], 200 μ M; [EGTA], 7 mM; $k_{\text{ON Ca EGTA}}$, 5 μ M⁻¹ s⁻¹; $k_{\text{OFF Ca EGTA}}$, 4 s⁻¹. Other parameters were as in Fig. 1. Fiber 908; external solution, *Cd-La-A9C* (Csernoch et al. 1991); internal solution, *15 EGTA* with calcium added for a nominal [Ca²⁺] of 50 nM and 1.6 mM ApIII. Diameter, 115 μ m. The linear capacitance in reference varied between 21.3 and 20.8 nF; upon changing the external solution to 8 mM ClO₄⁻ the linear capacitance was stable at 19.7 nF. The concentration of ApIII went from 911 μ M to 2.17 mM during the 37 min needed to complete the measurements in reference and to 2.88 after 29 min in ClO₄⁻. Records are single sweeps. Temperature, 10°C.

mM ClO_4^- in Fig. 6 is 1.70, while in reference it is 2.88; a similar reduction in the exponent was found in the experiment of Fig. 4, although data for ClO_4^- were not plotted in the figure).

A few experiments were carried out using a very high concentration of ClO_4^- . The purpose was to see the extreme of the ClO_4^- effect of linearization of the transfer

function. The study was limited by increases in ionic current, which made the measurement of charge movement questionable. Fig. 7 shows one in a series of calcium transients (top) and most of the corresponding release flux records in one of two experiments using 40 mM. This high $[ClO_4^-]$ exaggerated some effects described before (González and Ríos, 1993).



FIGURE 6. Equilibrium effects of ClO₄⁻: experiment and theory. Data are from two different fibers. (A) Voltage dependence of charge moved in the experiment of Fig. 5. Represented are averages of ON and OFF. Continuous lines were obtained with the allosteric model and parameters listed in Table I for fiber 908. Dashed lines are Boltzmann fits with the following parameters: $Q_{\text{max}} = 32 \text{ nC}/$ μ F, V = -37 mV, K = 14.8 mV (reference), $Q_{\text{max}} = 32.8 \text{ nC/}$ μ F, V = -37 mV, and K =12.2 mV (ClO_4^-). (B) Transfer functions in reference (open circles), 8 mM ClO₄⁻ (filled circles), and 40 mM ClO₄ (squares). Circles represent the same values as in A. Squares represent the experiment (911) whose records are illustrated in Figs. 7 and 8. Charges are actual values in all cases. Release fluxes are normalized to the steady value during the conditioning pulse (for 908) or to the steady release during a single pulse to -20 mV (for 911). Continuous lines were generated with the

allosteric model and parameter values listed in the corresponding rows of Table I and scaled as described in Fig. 4. The effect of 8 mM ClO_4^- on fiber 908 was simulated by multiplying k_L and dividing k_{-L} by 5. The effect of 40 mM ClO_4^- was simulated, increasing this factor to 10. Otherwise, the parameters were the same for both fibers.

In the calcium transients it could already be seen that the early decay phase at the end of the pulse was slowed and prolonged. A slow decay of $[Ca^{2+}]_i(t)$, early after the pulse, is an indication of slower channel closing. Simulations with the Ca^{2+} removal model (described in González and Ríos, 1993) illustrate this point. Normally the removal model simulates well the decay of $[Ca^{2+}]_i$ starting some 10 ms after the end



FIGURE 7. Effect of a high concentration of ClO_4^- on release flux. (Top) One of several calcium transients, elicited by a 200-ms pulse from a HP of -90 to -55 mV. The thick trace represents

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of the pulse, consistent with the idea that closure of the release pathway is complete by that time. In Fig. 7 (top) we represented by a solid thicker trace the best fit simulation (to the record shown and many others). This successful simulation was, however, possible only after 52 ms in the OFF. The dashed line represents the predicted time course of $[Ca^{2+}]_i$ when the simulation was started 14 ms after the end of the pulse. The simulation falls under the measured record, suggesting that the key assumption of the model, that release has stopped, did not hold at that time. A similar result was obtained with other sets of removal parameters that gave good fits of the late portions of the decay. More evidence that ClO_4^- slows deactivation of release can be found in an experiment illustrated in Fig. 12.

The release fluxes in Fig. 7 (bottom) show in addition that ClO_4^- caused a major reduction in the magnitude of the inactivating component of the release flux, again an extreme example of an effect described earlier for lower $[ClO_4^-]$ (González and Ríos, 1993). Finally, the release flux levels were smaller than usual, perhaps due to a faster depletion.

Fig. 8 shows records of charge movement current in the same experiment. Since slow phases of charge movement were expected and found, longer than usual pulses were applied. Before ClO_4^- , a pulse to -50 mV did not cause measurable release, while after ClO_4^- a pulse to -75 mV was suprathreshold. The very slow phases seen in the charge movement records at -70 and -60 mV in the figure are associated with the slow increase in release flux seen in the corresponding records of Fig. 7.

The records also show a very slow component of charge movement in the OFF; this slow phase, however, is absent from the record at -80 mV, which elicited no measurable release. Prolonged OFF charge movement currents in ClO_4^- have been studied in detail by Huang (1987); newly shown here is the association of these prolonged tails with slower deactivation of release. This, as shall be discussed, has implications for the choice among transmission models.

The record at -40 mV shows an indication of an outward current that activates during the ON. This current was more obvious at higher voltages and prevented determinations of charge movement beyond -40 mV. The value of OFF charge transfer at -40 mV (32 nC/µF) was close to the largest value in reference (28 nC/µF). The release flux at the end of the -40-mV pulse (7 µM/ms) was similar to the value obtained earlier during a 100-ms pulse to -20 mV in the same solution. These observations suggest that both the charge movement and release activation at

the best fit to this and many other Ca^{2+} transients; the fit and simulation start 52 ms after the end of the pulse. *Dashed curve*, simulated decay of the calcium concentration, obtained with the same Ca^{2+} removal model and parameters, but starting 14 ms after the end of the pulse. (*Bottom*) Release flux records derived from calcium transients elicited by 200- or 300-ms pulses to the potentials indicated. Parameters of removal: $k_{ON Ca}$ p. 100 μ M⁻¹ s⁻¹; $k_{OFF Mg}$ p. 3.0 s⁻¹; M, 1.3 μ M s⁻¹; $K_{D pump}$, 0.5 μ M; [P], 800 μ M; [EGTA], 6 mM; $k_{ON Ca}$ EGTA, 20 μ M⁻¹ s⁻¹; $k_{OFF Ca}$ EGTA, 5 s⁻¹; others are as in Fig. 1. Fiber 911; external solution, *Cd-La-A9C* with 40 mM ClO₄⁻¹ (substituted for methanesulfonate); internal solution, *15* EGTA with calcium added for a nominal [Ca²⁺] of 50 nM and 0.8 mM ApIII. Diameter, 118 μ m. The linear capacitance varied between 15.8 and 15.5 nF and the concentration of ApIII went from 1.1 to 1.31 mM during the 18 min taken by the measurements in ClO₄⁻. Records are derived from averages of 3 (at -45 and -45 mV), f, or 10 sweeps (at -80 and -75 mV). Temperature, 10°C.

-40 mV were close to maximal; a Boltzmann fit, however, could not be made to the Q(V) data.

The transfer function $(\hat{R}_m(Q))$ is plotted as squares in Fig. 6 *B*, together with data from another experiment at lower $[ClO_4^-]$. The point of plotting both fibers together is to stress the extreme linearization caused by the high $[ClO_4^-]$ (the exponent of the best fit power function was 1.03 in 40 mM ClO_4^-).

There was some concern that this high $[ClO_4^-]$ would alter the linear electrical properties. The capacitance measured in the control pulses is plotted in the inset of



FIGURE 8. Charge movement records in high $[ClO_4^-]$. Records are the differences between averages of all current sweeps during test pulses (numbers in previous figure legend) and double the number of intercalated controls (from -110 to -90 mV), corrected by a sloping baseline fitted to the last 70 ms (for 200-ms pulses) or 100 ms (for 300-ms pulses). The ON at -40 mV was corrected by subtraction of a constant, the level of the asymmetric current between 30 and 50 ms. (*Inset*) Evolution of the linear capacitance (calculated from integrals of the current transient during pulses from -110 to -90 mV). The abscissa is the time after exposure of the fiber to ApIII. The horizontal bar marks the time of exposure to high ClO_4^- .

Fig. 8 as a function of time during the experiment. It shows some decay after 160 min, but this is not unusual in our experience and was not correlated with the presence of ClO_4^- .

Kinetic Data

The kinetics of charge movement current were also modeled. The simulations were compared with experimental records obtained in fibers highly depleted by repeated pulsing at high voltage and frequency in the presence of EGTA and BAPTA. For obvious reasons, the extremely depleted condition is not useful for studying calcium release records; therefore, the kinetic records of charge movement that were compared with the simulations were not obtained in the same experiments that generated $\dot{R}_{\rm m}(V)$, Q(V), and $\dot{R}_{\rm m}(Q)$ data.



FIGURE 9. Kinetic effects of ClO_4^- : experiment and theory. (A) Intramembrane charge movement current during 100-ms pulses from a HP of -90 mV to the potentials indicated. These are the same records in Fig. 20 of González and Ríos (1993) (fiber 744). The internal solution is 15 EGTA, 1 BAPTA, with no added calcium. The fiber was subjected to a calcium depletion pulse protocol (~200 pulses to 20 mV at 12-s intervals). (B) Simulations (numerical solutions of the differential equations) of charge movement transients. For description of simulations see text and next figures. Parameters are the same as those listed in Table I for fiber 827.

Fig. 9A shows a group of records of charge movement current from a depleted fiber already presented as Fig. 20 in González and Ríos (1993). ClO_4^- caused a substantial slowing of both ON and OFF currents, plus the appearance, observed reproducibly, of small hump-like portions in both ON and OFF revealed by a change

in concavity (that is, in the sign of the second derivative) rather than an actual secondary rising phase.

THEORY

Glossary: Equivalence with MWC Nomenclature

MWC model:	Present model:
allosteric protein	Ca release channel
heterotropic ligand	voltage sensor molecules
T ₀ -T ₄ (tense states)	C ₀ -C ₄ (closed states)
R ₀ -R ₄ (relaxed states)	O ₀ -O ₄ (open states)
$k_{\rm C}, k_{-\rm C}$	$k_{\rm C}, k_{\rm -C}$ (rate constants among closed states)
K _T	$K_{\rm C}$ (equilibrium constant among closed states)
$\mathbf{K}_{\mathrm{T}} \equiv k_{-C}/k_{C}$	$K_{\rm C} \equiv k_{\rm -C}/k_{\rm C} = \exp\left[-(V-\overline{V})/4K\right]$
$k_{\rm L}, k_{\rm -L}$	$k_{\rm L}$, $k_{\rm -L}$ (rate constants for opening and closing)
$\mathbf{L} \equiv k_{-\mathbf{L}}/k_{\mathbf{L}}$	L (equilibrium constant of closing transition)
K _R	K ₀ (equilibrium constant among open states)
$c \equiv \mathbf{K}_{\mathbf{R}}/\mathbf{K}_{\mathrm{T}}$	$f^2 = K_0/K_C$ (allosteric factor)
F (concentration of ligand)	1
$\alpha \equiv F/K_{R}$	$f^{-2}\exp\left[-(V-\overline{V})/4K\right]$
$\overline{\mathbf{R}}$ (function of state)	$P_{\rm o}(V)$ (open probability)
$\overline{\mathbf{Y}}\mathbf{F}$ (saturation function)	$Q(V)/Q_{\text{max}}$ (fraction of charge moved)

The model specifies the formal properties of the system cartooned in Fig. 10. The unit of the model consists of one release channel, represented as a homotetramer (square blocks in the figure) and four voltage sensor molecules (the drop-like structures), each in contact with one protomer of the release channel. The bases for the structural assumptions are the recent observations of Block et al. (1988) and other evidence discussed by Ríos et al. (1991) and Ríos and Pizarro (1991).

The functional aspects of the model are closely inspired in the theory of allosteric transitions of Monod et al. (1965), henceforth termed "MWC model." The description here will stress the parallels with that model; a list of symbols, definitions, and the equivalencies between the present model and MWC are given in the Glossary.

The allosteric protein in MWC terminology is here called the Ca^{2+} release channel. It is interesting that the release channel is now believed to be a homotetramer with fourfold rotational symmetry (e.g., Wagenknecht, Grassucci, Frank, Saito, Inui, and Fleischer, 1989), thus satisfying the symmetry requirements of the MWC allosteric proteins, and in particular the fourfold repeat, to which J Monod gave so much value (the issue of symmetry is discussed by Perutz, 1990). As in the MWC model, the protein has two available states, tense and relaxed, which will here be called closed (C) and open (O). As in the original MWC model there is full cooperativity: the four protomers make a coordinated transition between open and closed, without subconductance levels allowed.

The essence of the model is the manner in which the voltage sensors interact with the release channel and control its state. The interaction is assumed to be allosteric; that is, the voltage sensors act at a contact site (a binding site) on the release channel, and through this action alter the properties of the protomers, leading to their cooperative opening or closing. The implications of the term allosteric are thus twofold: the action is by contact, and it affects other sites in the protein. Again following MWC terminology, the voltage sensors are heterotropic ligands, and by their interaction they modify the homotropic interaction between release protein protomers. Other details of the correspondence between the present model and MWC will be considered in the Discussion. The present model is close to the model of gating of L-type Ca^{2+} channels proposed by Marks and Jones (1992), and their relationships will be considered in the Discussion.



FIGURE 10. Allosteric model. (Top) Cartoon representing four independent voltage sensor molecules (presumably dihydropyridine receptors) in T membrane, aligned and in contact with the release channel. The channel is pictured as a tetramer of identical subunits. Two states of the release channel (closed and open) are pictured, as well as two of five possible dispositions of the voltage sensors. (Bottom) State diagram. States C_i are closed and O_j are open. j indicates the number of voltage sensors in the activating position. The vertical rate constants are intrinsically voltage dependent (Eqs. 2 and 3). The rate constants between closed states are identical except for integer factors indicating the multiplicity (degeneracy) of the origination state. Horizontal rate constants are voltage independent, but the forward (opening) rate constants are multiplied by 1/f every time a sensor is activated. Note that the same factor multiplies all forward rate constants of the voltage sensor between states O_i (for further explanation see text).

Each of the voltage sensors has two states available, a resting (r) and an activating (a) state, and the transitions involve the movement of a discrete amount of charge across the membrane field; that is, the transitions are voltage driven. In this sense there is no cooperativity among individual sensors, and the sensors are assumed to be identical. The model is therefore a 10-state Markov system, illustrated in Fig. 10,

where the 10 states arise from combining five different possibilities for the sensor and two for the release channel (the individual sensor molecules are considered indistinguishable and thus there are only five possible states for the sensor, corresponding to 0 through 4 molecules in state a). In Fig. 10 the situation represented on the left is one in which all sensors are in the r state (state C_1 of the complete system). On the right, one sensor has undergone the transition and the channel is represented as open (state O_1).

The parameters of the model are defined in Fig. 10. Consider first the four states at the top, C_0 , O_0 , C_1 , and O_1 (the others are a simple extension). The transitions between closed and open when all the sensors are in the resting state (C_0 and O_0) are determined by the rate constants k_L and k_{-L} . Using MWC terminology, the equilibrium constant of the closing reaction is named $L \equiv C_0/O_0$ (the symbols of the states are used here to represent their probabilities). The vertical transitions between the two top left states involve the change of one voltage sensor molecule. If the voltage-dependent forward rate constant is termed k_C and the backward rate constant k_{-C} , the overall forward rate constant will be $4k_C$ due to the degeneracy of the state with one voltage sensor molecule in the a state. In MWC terminology the equilibrium constant k_{-C}/k_C is named KT, and is a dissociation constant (as the corresponding transition is a binding reaction). The binding character of the reaction is of secondary relevance to our application (cf. Discussion). In our model we use the symbol K_C instead of KT.

Consider next the effect of moving one voltage sensor; it will favor the opening of the channel tetramer. In the model this is achieved by multiplying the opening rate constant $k_{\rm L}$ by a factor greater than one, which for traditional reasons is termed 1/f (f < 1) and dividing the backward rate constant $k_{\rm -L}$ by the same factor. Thus, the factor f embodies the allosteric effect. As regards the closing equilibrium constant, the result of moving one sensor is multiplying L by f^2 ($f^2 = c$ in MWC terms).

Having specified these rate constants, the other two rate constants linking O_0 and O_1 are also specified (to satisfy microscopic reversibility) and turn out to be $4k_C/f$ and fk_{-C} . Thus the dissociation constant K_C becomes K_0 for the open channel, and the relationship is again $K_0/K_C = f^2$. This completes the specification of the first ring of four states; the other rings can be specified following the same rules. Only two changes merit comment. The rate constants of the vertical transitions, relating states that are both open (or closed), are similar to those in the top ring of states except for a factor that takes into account the degeneracy of states of the voltage sensor. Thus the rate constant for activation of the second sensor molecule is $3k_C$ and for its deactivation $2k_{-C}$. Additionally, it is noted that the allosteric effect simply accumulates as a power of the allosteric factor f as the number of activated sensors increases, until the opening rate constant becomes k_L/f^4 for the transition from C_4 to O_4 .

Voltage Dependence

Voltage drives the system by driving the two-state transitions of individual voltage sensor molecules:

$$r = \frac{k_{\rm C}}{k_{\rm -C}} a \tag{1}$$

The two-state transition is governed by a Boltzmann distribution, so that $P_a/P_r = \exp([V - \overline{V}]/4K)$.¹ The kinetics of the transitions are described by exponential rate constants that assume a symmetric barrier

$$k_{\rm C} = 0.5\alpha e^{(V-\overline{V})/8K} \tag{2}$$

$$k_{-C} = 0.5\alpha e^{-(V - \bar{V})/8K}$$
(3)

and α is the inverse of the time constant at $V = \overline{V}$.

Normally at rest the sensor molecules are all in state r (V is approximately -40 mV) and the channel is closed. This requires $k_{\rm L} \ll k_{-\rm L}$ (typical values in the simulation are 0.003 and 1,000 ms⁻¹). Upon depolarization, voltage sensor molecules make transitions individually: for every molecule in state a, the forward opening constant is multiplied by ~5 (f is typically 0.2) and the backward rate constant by 0.2. As the lower states in the diagram become more populated the system shifts to the right side and the channel open probability increases. In the case when the resting tendency to open $(k_{\rm L}/k_{-\rm L} \equiv {\rm L}^{-1})$ is very small, only the movement of all four sensor molecules causes the channel to open. The amount of charge moved is simply proportional to the number of sensors that undergo the transition; thus, in the case of extremely high L (low tendency to opening), the open probability (and our measure of it, the release flux, corrected for depletion and normalized) will be proportional to the fourth power of the charge moved. In general, the model predicts a dependence of a lower order.

Simulations

The simulations include steady-state dependencies of charge movement and open probability with voltage and with each other (the open probability from the model is compared with the experimentally evaluated \dot{R}_m). Simulations also include kinetic solutions, time course of charge movement current, and release at various voltages. Since the model is analogous to MWC, whose steady-state solutions are analytical, it is possible to use these solutions essentially unmodified. The open channel probability is the fraction of release molecules in 0 states (the function of state \bar{R} in MWC terms):

$$P_{0} = \frac{O_{0} + O_{1} + O_{2} + O_{3} + O_{4}}{(O_{0} + O_{1} + O_{2} + O_{3} + O_{4}) + (C_{0} + C_{1} + C_{2} + C_{3} + C_{4})}$$
(4)

where the symbols represent the probabilities of each state. The fraction of charge moved $(Q(V)/Q_{\text{max}})$ is the sum of the (fractional) charges in each state multiplied by the state probability (the saturation function $\overline{Y}F$ in MWC):

$$Q/Q_{\rm max} = \frac{(O_1 + 2O_2 + 3O_3 + 4O_4) + (C_1 + 2C_2 + 3C_3 + 4C_4)}{4}$$
(5)

 $P_{\rm o}$ and $Q/Q_{\rm max}$ are functions of voltage only, and the expressions can be derived from the above equations and the equilibrium equations of the system. They can also

¹ Note that the steepness factor of the Boltzmann was written as 4K (rather than simply K). This is a matter of convenience in the simulations, responding to the fact that each transition involves one-fourth of the total available charge.

be taken from Eqs. 1 and 2 of Monod et al. (1965), making F (the concentration of the ligand) equal to 1:

$$P_{\rm o} = \frac{(1 + e^{V - \overline{V}/4K} f^{-2})^4}{(1 + e^{V - \overline{V}/4K} f^{-2})^4 + L(1 + e^{V - \overline{V}/4K})^4}$$
(6)

and

$$\frac{Q}{Q_{\max}} = \frac{f^{-2} e^{V - \overline{V}/4K} (1 + f^{-2} e^{V - \overline{V}/4K})^3 + L e^{V - \overline{V}/4K} (1 + e^{V - \overline{V}/4K})^3}{(1 + f^{-2} e^{V - \overline{V}/4K})^4 + L (1 + e^{V - \overline{V}/4K})^4}$$
(7)

Fiber No.	ClO ₄	K	k _L	kL	f	\overline{V}
	<i>mM</i> *	mV	1/ms	1/ms		mV
827	0	4.5	0.002	900	0.175	-20
827	8	4.5	0.006	300	0.175	-20
906	0	3.2	0.002	1,200	0.175	-24
906	8	3.2	0.014	200	0.175	-29
907	0	3.5	0.002	1,500	0.150	-22
907	8	3.5	0.008	375	0.150	-30
908	0	4.0	0.001	1,800	0.175	-26
908	8	4.0	0.005	360	0.175	-26
911	40	4	0.01	180	0.175	-26
Appendix‡	0	7	0.001	1,500	0.3	-10
Appendix	8	7	0.003	500	0.3	-10

TABLE I Parameter Values in Simulations

Parameter values used to simulate equilibrium dependencies of charge and open probability of the release channel with voltage, as well as kinetic records (charge movement currents as functions of time). One additional parameter, the kinetic constant of charge movement (α , cf. eq. 2), was always 0.2 ms⁻¹. The optimal values of the parameters were decided by inspection of simulated curves and data. The goodness of fits is exemplified in Figs. 4 and 6.

*The entries in column ClO_4^- are not parameters but reminders of the $[\text{ClO}_4^-]$ when obtaining the experimental records that were simulated. The records in the presence of ClO_4^- were simulated by multiplying the reference value of $k_{\rm L}$ and dividing $k_{-\rm L}$ by the same factor, as shown in the table. In the cases of fibers 906 and 907 the fits of data in ClO_4^- were improved if, in addition to changing $k_{\rm L}$ and $k_{-\rm L}$, \overline{V} was shifted by -5 and -8 mV, respectively. In the other cases, no improvement was obtained by changing \overline{V} . 'The entries in the row marked Appendix correspond to the parameter values used in simulations with the generalized (eight sensor) model described in the Appendix.

These are the equilibrium relationships of the system. They were used with suitable values of the parameters to generate the continuous lines in Figs. 4 and 6. The values of the parameters were selected to best describe the data as judged by eye, and are listed in Table I. In addition to the general adequacy of the simulations of voltage dependence, it is worth noting that the Q(V) dependence generated with the model, as well as the actual data, are well described by a single Boltzmann function (Figs. 4 A and 6 A). In Figs. 4 B and 6 B the experimental transfer function $\dot{R}_m(Q)$ is compared with the corresponding theoretical function, $P_o(Q)$. Again the agreement is good, and

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as shown in Fig. 4 B, the theoretical dependence is almost identical to the best fit power function plotted as a dashed curve. This was also true in the plot of Fig. 6 B (not shown).

The Equilibrium Effects of Perchlorate

Based on the results of Ma, Anderson, Shirokov, Levis, González, Karhanek, Hosey, Meissner, and Ríos (1993), we applied the model to the situation in the presence of ClO_4^- , assuming that the only change introduced by the anion was an increase in the equilibrium constant of channel opening (a reduction in L). The lines in Fig. 6, A and B are simulations of the results of fiber 908 using the parameters listed in Table I for that fiber. In this case the simulation of the effects of ClO_4^- required assuming a reduction of L by a factor of 25. Fig. 6A shows that the shift in voltage dependence of charge movement and the small increase in the steepness of the curve are well reproduced. Fig. 6B shows that the model simulates well the reduction in curvature of the transfer function. We included in Fig. 6B data from Figs. 7 and 8 in the presence of 40 mM ClO_4^- (squares). The model simulated well the results using the same parameters and a 100-fold decrease in the value of L. Even though the latter simulation required a normalization by maxima of release and charge that may not have actually been attained in the experiment, it does exhibit the striking linearization observed experimentally, and this feature is independent of any normalization.

It must be stressed that the changes in the distribution of Q were obtained with a change not involving any of the parameters that describe the voltage sensor. Similar parameter changes simulated the effects in the other fibers listed in Table I. In two of those, however, a visibly better simulation of the effect was achieved assuming an additional shift in V of the voltage sensors by -5 to -8 mV.

Simulations of Kinetics

To obtain the kinetic transients of charge movement and release channel open probability, the nine differential equations and one conservation equation of the model were solved numerically by the unmodified Euler method. Given the large magnitude of the constant k_{-L} (typically 1,000 ms⁻¹), the time increment (Δt_e) was usually 1 µs. A few transients were computed with $\Delta t_e = 0.2$ µs, with no detectable changes in the solutions. An increase in Δt_e beyond 1.5 µs led to catastrophic results. Working with $\Delta t_e = 1$ µs the computer time was not trivial, ~1 s time per ms of computed transient on a 486 processor-based PC clone at 33 MHz.

Fig. 9 B (thin traces) shows the transients of charge movement at several voltages in reference conditions. The model parameters were the same as those used for the reference equilibrium simulations of fiber 827 (shown in Fig. 3). They should be compared with the experimental records obtained in reference conditions in a highly depleted fiber, exemplified by the thin traces of Fig. 9 A. There is general qualitative agreement, as both the experimental and the simulated transients are approximately exponential relaxations. The time constants of the simulated records are voltage dependent, increasing at intermediate voltages as do the experimental ones. The time constant of the OFF transients is approximately the same in all records in both experiment and theory.

The surprising aspect of the kinetic simulations is the fidelity with which the effects

of ClO_4^- are simulated. In both experiment and theory the results in ClO_4^- are represented with thicker traces. The effect of ClO_4^- is simulated again as a reduction of the equilibrium constant L, in this case by a factor of 9. For kinetic purposes this factor was split evenly between the opening rate constant k_L , which was multiplied by 3, and the closing rate constant k_{-L} , which was divided by the same number.

The multiple experimental effects of ClO_4^- on kinetics are all reproduced by the model in striking detail: (1) The ON is slower but the current intensity is initially the same. It is only after the initial peak of charge movement current that the records in ClO_4^- become slower. (2) The difference in kinetics is essentially lost at high voltages where the ON becomes fast regardless of ClO_4^- . (3) The OFF is about twofold slower in ClO_4^- . (4) The ON current in ClO_4^- loses its simple exponential character and a hump-like portion appears, which is due to a change in the sign of the curvature rather than a secondary rising phase. (5) The OFF also acquires an inflection, which in the simulation is due to the appearance of a conspicuous rising phase. In the experimental records such a rising phase is obscured by the presence of a very fast component. This fast component is the only feature of the experimental records that is not present in the simulations (but see simulations in the Appendix). Again it should be remarked that these effects on charge movement kinetics are produced in the model by changing a parameter of the release channel, not of the voltage sensor.

The same simulation also generates a $P_0(t)$ record at every voltage. These, however, do not have a suitable experimental correlate, as the conditioning pulses used reduce but do not eliminate the peak component of the release waveform. Somewhat fortuitously, the experiments in high ClO_4^- result in release fluxes almost devoid of inactivation, and a comparison was attempted to see if the simulations had at least adequate qualitative features. Fig. 11 A shows $P_0(t)$ records generated with parameters similar to those used for Figs. 9 B and 6 (but the observations are not dependent on a particular choice of parameters). Fig. 11 (top) shows records in reference and ClO_4^- (meaning that the reference k_L is multiplied and k_{-L} divided by 3) at two different voltages (-40 mV in reference, -63 mV in ClO_{4}^{-}) chosen to make the final open probability similar. It is clear that the kinetics of activation are much slower in ClO_4^- , to the point that activation is not complete by 100 ms. This compares well with the release records at -60 or -65 mV in Fig. 7. Fig. 11 (bottom) shows the corresponding charge movement currents. They have a prolonged phase during the ON in Clo_4^- , which underlies the slow activation of release in the simulations and generally agrees with slow phases observed experimentally (Figs. 8 and 9). Finally, the simulations of $P_0(t)$ also exhibit slower OFF closing in ClO_4^- , as observed in the experiments.

The slower time course of release channel closing in ClO_4^- helps us understand the intriguing kinetic aspects of the simulated charge movement that so well resemble the experimentally observed effects. As we indicated, the essence of the allosteric effect (and a consequence of micro-reversibility in a closed system) is that the distribution of mobile charge shifts to more negative voltages when the channel opens. Therefore the transition to equilibrium, upon a depolarization that opens channels, occurs in two qualitatively different stages. First the closed channels activate their charge movement along the left side states of the diagram. At some point the channel opens

and the system moves further down in the set of states along the right side of the diagram. When ClO_4^- is present the opening is substantial with less depolarization, and this left-to-right flow in the diagram becomes more prominent and prolonged. This results in prolongation of the movement of charge (and opening).



FIGURE 11. How ClO_4^- affects kinetics in the model. Simulations of $P_o(t)$ (top) amd charge movement current (bottom). $P_{0}(t)$ was computed as the sum of the occupancies of states O_i. Charge movement current as the time derivative of Q/Q_{max} in turn is given by Eq. 5. The parameters are similar to those used for Fig. 9 (908 entries in Table I) but K was 6 mV and \overline{V} was -40 mV. The two voltages, -40 mV in reference and -63 mV in perchlorate simulations, were chosen to give approximately the same P_0 at the end of the pulse.

Similar considerations apply to deactivation: an initial fast phase of charge movement corresponds to movement of systems that were on the left set of states (closed). This is followed by a protracted phase of return of mobile charge, limited in its rate by the voltage-independent right-to-left (closing) transitions. In summary, the

kinetic peculiarities are explained in this coupled system because the charge movement cannot end until the gating (opening or closing) is completed.

A Failure of the Model

In the reference situation the transfer function can be described as a power function of a high order (Figs. 4 *B* and 6 *B*; see also Simon and Hill, 1992). This was explained as evidence that several sensors must move to significantly increase the open probability of the release channel (Simon and Hill, 1992). This in turn requires the system to be far from saturation; in other words, even with all four sensors activated, the open probability should be <1. This is reflected in the simulations. Thus in Fig. 3 the simulated open probability reaches a maximum of 0.72 when all voltage sensors are in the activating position (the plotted value is different because of normalization). Consequently, one of the simple predictions of the model is that ClO_4^- should increase the maximum absolute value of R_m , attainable at high voltage when all the sensors move to state a.

We carried out four experiments designed specifically to test this prediction using the reversibility of the effect of ClO_4^- . The experiments consisted in repeatedly changing the external solution back and forth from reference to ClO_4^- while repeating a large pulse (to +20 or +30 mV) that moved a maximal amount of charge. One such experiment is illustrated in Fig. 12. Fig. 12 *A* shows four release records obtained successively in reference, ClO_4^- (8 mM), a washout reference solution, and again in ClO_4^- . The records shown have already been corrected for depletion during the pulse (they are $R_c(t)$ records). It can be seen that both records in ClO_4^- exhibit slower deactivation than in reference.

In this experiment, as in two of the other three, the release flux was decaying in the successive pulses. The estimated Ca_{SR} of SR calcium content was also decaying. Steady release after correction (circles) and Ca_{SR} are plotted in Fig. 12 *B*. The plot shows that both values decreased more or less in parallel, suggesting that the decay in $\dot{R}_c(t)$ may have been due to depletion. Finally, the filled circles in Fig. 12 *C* plot the ratio \dot{R}_m/Ca_{SR} , which is a measure of the permeability of the release pathway. Other symbols in the same graph represent permeability values estimated in the same way in three other experiments. On the whole, we found no evidence of increase in \dot{R}_m (at high voltage) when the fibers were in ClO_4^- . This constitutes a major predictive failure of the model.

One intuitive explanation of this failure is that perhaps EC coupling does work close to saturation; that is, less than maximal amounts of charge movement result in full activation of the release channel. It is simple to increase the saturation of channel opening in the model by decreasing the value of L. However, this causes a decrease in the curvature of the transfer function (the exponent of the power function decreases). Thus, the model in its present form cannot both reach full saturation of channel opening and reproduce the third- or fourth-order power relationship between release and charge movement.

This failure may be due to a known oversimplification in the model, the fact that each voltage sensor molecule (of which we assume there to be four per release channel) has only two states available in the model. Since the voltage sensors presumably correspond to dihydropyridine receptors (Ríos and Brum, 1987; Tanabe, Beam, Powell, and Numa, 1988) and these have multiple charged segments in their structure (Tanabe, Takeshima, Mikami, Flockerzi, Takahashi, Kanagawa, Kojima, Matsuo, Hirose, and Numa, 1987), it is likely that a description in which every sensor has more than one moving charge will be more realistic.



FIGURE 12. Release at high voltage. (A) $R_c(t)$ during a pulse to +20 mV in a fiber exposed successively to external solutions reference (1), 8 mM ClO₄⁻, reference, and ClO₄⁻ again. (B) Timing of solution changes, R_m , in the successive pulses (*circles*), and values of the parameter Ca_{SR} derived in the correction procedure (*triangles*). (C) Ratio of R_m/Ca_{SR} (permeability) during the successive pulses in four different experiments (the abscissa, or timing of changes in ClO₄⁻, is accurate for the experiment illustrated in A and B, but only a rough approximation for the other three experiments). *Circles*, fiber 900, same as in A and B; diameter, 100 µm; [ApIII], 1.7-2.1 mM. *Inverted triangles*, 895; diameter, 98 µm; [ApIII], 0.72-1.1 mM. Squares, 894; diameter, 132 µm; sarcomere length, 1.8 µm; [ApIII] 1.5-2.1 mM. *Triangles*, 893; diameter, 155 µm; [ApIII], 1.8-2.1 mM. All fibers in external solution *Cd-La-A9C* and internal solution 15 *EGTA* with 1.6 mM ApIII at slack length. Temperature, 10-12°C.

One such description, with two independent moving charges per voltage sensor, is developed in the Appendix. It successfully predicts all the observations, including the high order power relationship $P_0(Q)$ and the failure of ClO_4^- to increase the absolute maximum of release. Its better performance can be understood intuitively: it is

analogous to a system with more than four voltage sensors (eight in the case treated in the Appendix) and therefore it may have a high order transfer function (implying that four or five sensors have to move to substantially increase P_0) and still reach maximum P_0 when less than the maximum number of sensors move to the a state.

DISCUSSION

We have constructed a model that assumes contact interaction between voltage sensors of the T tubules and release channels of the SR. The model accounts well for several sets of observations. It describes well the voltage distribution of mobile charge, reproducing both observed Q(V) dependencies and the Boltzmann function that is generally used in their description. It reproduces well the voltage dependence of release flux, including activation at higher voltage than charge movement and the fact that release initially increases with voltage more steeply and with more curvature than charge movement. Not surprisingly, since it describes well the separate V dependencies, it reproduces well the transfer function $R_m(Q)$. Finally, the model generates kinetic records of charge movement that are relatively uneventful monotonic relaxations, although on closer analysis they diverge from exponentials in interesting ways (see below).

Relationship with Previous Models

This model is directly inspired by the proposal of Chandler et al. (1976) of a mechanical link (plunger) in the T-SR junction. Two quantitative formulations have appeared that are somehow inspired by the plunger model (although they do not specifically assume or require a mechanical connection). One is by Melzer, Schneider, Simon, and Szucs (1986), in which the voltage sensor opens the channel in two stages, the first accounting for subthreshold charge and the second directly causing opening. Another is a Hodgkin-Huxley four-particle scheme recently proposed by Simon and Hill (1992). The present model has a noteworthy difference with the plunger concept and its above-mentioned formulations: it abandons the idea of a rigid link that unequivocally determines the state of the channel. The present model allows freedom in the Ca channel to be either open or closed in any of the five states of the voltage sensor. In that manner the coupling between sensor and channel becomes flexible, as reflected, for instance, in the fact that the threshold charge movement is no longer a constant (essentially arbitrary) parameter, as in Melzer et al. (1986), but a function of the rate constants of the system (which may vary under the influence of modulators).

The model of Simon and Hill (1992), in which four independent two-state voltage sensors must move to open the channel, is reached as a limiting case of the present model, when the intinsic open probability of the channel is so low that all four sensors must move before that probability becomes sizable. The present model accounts for the difference between our measurements (in which the exponent of the power describing the transfer function was less than 3) and those of Simon and Hill (in which the exponent was 4) simply as a difference in the value of L. One way of describing the present model is as a generalization of Simon and Hill's, in which the rigid link requisite that four sensors must move to open the channel has been removed.

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Dr. Bruce Simon pointed out to us that the present model has another major difference with the Hodgkin-Huxley m^4 formulation of Simon and Hill (1992). In that formulation the sensors are independent particles, and their rates of movement are determined by voltage only. Therefore the model of Simon and Hill predicts OFF time constants that are independent of the magnitude of the test pulse. Such prediction clearly fails in ClO_4^- (as demonstrated in Figs. 8 and 9); when release activates, the OFF current becomes slower or a slower phase appears. In reference, however, it seems to hold. These features are especially well reproduced in the simulations when the generalized model of the Appendix is used (Fig. 14).

Effects of Perchlorate

A significant feature of the allosteric model is that it reproduces in intriguing detail the effects of ClO_4^- on voltage distributions, transfer function, and kinetics. The most interesting aspect of the simulations of ClO_4^- effects is that only a property of the release channel is assumed to be changed by ClO_4^- , the tendency to opening, described by the equilibrium constant L (or two kinetic constants). This single change is sufficient to reproduce in good detail equilibrium and kinetic effects on both the release function and the charge movement properties. A model-independent conclusion of the previous articles of this series is that ClO_4^- does not have its most characteristic effects on DHP receptor molecules unless they are in physiological interaction with the release channel of skeletal muscle. The simulations in this article now show that an effect on the release channel will be transmitted backward to the voltage sensor and give secondarily the effects observed, provided that an allosteric interaction links sensors and channels. Thus, the observations of the previous articles plus the simulations in this article constitute functional evidence of allosteric interaction.

A more circumspect interpretation of the simulations in this paper is that the states represented in the diagram of Fig. 10 are states of a sensor-channel complex, without a specific molecular correspondence to dihydropyride and ryanodine receptors. In this view, the $C \Leftrightarrow O$ transitions could describe voltage-independent conformational changes in the sensor itself, which in turn determine opening of the release pathway. The effects of ClO_4^- would still be ascribed to this transition, and their formalization would be identical, making this version of the model isomorphic with the one presented before. In this view, the present observations would have no bearing on the mechanism of transmission.

We have, however, shown in the previous paper that ClO_4^- opens the ryanodine receptor channel in bilayers and increases the binding of ryanodine and the flow of ⁴⁵Ca from SR vesicles. Additionally, in the first article of this series we found that the SR lost its calcium content more rapidly in single fibers in the presence of ClO_4^- . Surprisingly, the gating currents of the L-type Ca²⁺ channels in rabbit ventricle were essentially insensitive to ClO_4^- (Ma et al., 1993). These observations favor the view that ClO_4^- has its characteristic EC coupling effects, or some of them, through a primary effect on the release channel. The kinetics of onset and reversal of the effects (González and Ríos, 1993), plus the observation that the effects are the same when the anion is present in the internal solution (Csernoch, Kovacs, and Szucs, 1987; Delay, García, and Sánchez, 1990), are also consistent with this view. Since the observations in bilayer and vesicle preparations are essential justifications of the present model, one wonders to what extent effects of ClO_4^- on release channels in bilayers can be extrapolated to the functioning cell. For instance, the mean open probability of a release channel in a bilayer with 20 mM ClO_4^- is 5.7% (Table II of Ma et al., 1993). At first sight this seems disproportionately greater than the activation of the release channel at rest that emerges in the present simulations. Of course, the resting interaction of the release channel with the voltage sensor, and other functional interactions lost in the processes of fractionation and reconstitution may change the properties of the release channel in many ways, including altered P_o and sensitivity to ClO_4^- (thus Ma et al. [1993] reported that purified ryanodine receptors had a much higher affinity for [³]ryanodine than ryanodine receptors in triadenriched vesicles).

The open probability in the simulations is, however, not negligible. For instance, in Fig. 11 (top) the P_o at rest, in the ClO_4^- simulation, is close to 1%. Not much can be made of this number; it depends strongly, for instance, on the number of moving particles assumed in the voltage sensor (cf. Appendix; note that P_o [-90 mV, in ClO_4^-] is much less than 1%). In general, however, this model predicts finite values of P_o at rest in the presence of ClO_4^- . The more rapid decay in calcium content in the SR, reported tentatively in González and Ríos (1993) as one of the effects of ClO_4^- , could be a simple consequence of this activation at rest. Both the experimental observations in muscle fibers and the simulations are thus generally consistent with the observations with fractionated SR.

Not all the effects of ClO_4^- described by González and Ríos (1993) are accounted for in these simulations. In particular, the simulations predict a small increase in steepness and a small leftward shift of Q(V). The large increase in steepness and the large shift observed in nondepleted fibers cannot be explained without assuming additional sites or mechanisms. It is possible that these effects involve the positive feedback processes proposed to take place between the voltage sensors and the locally increased $[Ca^{2+}]_i$ (Csernoch et al., 1991; Pape et al., 1992) plus a negative shift in voltage dependence shared with other anions.

On the other hand, the decrease in the proportion of inactivating release flux (relative to the noninactivating component $\dot{R}_{\rm m}$), which was shown to be a characteristic effect of ${\rm ClO}_4^-$ (González and Ríos, 1993), could be a simple consequence of slower activation in the presence of inactivation that proceeds at a constant rate. Such an effect is displayed by simulations (Ríos, E., manuscript in preparation) in which the decay of $\dot{R}(t)$ after the peak is modeled as a Ca²⁺-dependent inactivation of open channels (Simon and Schneider, 1988).

Cooperative Opening?

We gave the model a form identical to that chosen by Monod et al. (1965) to describe interactions in hemoglobin and other proteins with subunits. The MWC model is an oversimplified representation of the events in hemoglobin; Ackers, Doyle, Myers, and Daugherty (1992), for instance, have shown the existence of configurations intermediate between all T and all R. The full cooperativity assumed by Monod et al. (1965) is, however, not essential in our simulations. This assumption was made here to simplify the model and reduce the number of adjustable parameters; even though we

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have not used it, we feel that a more general model, like that of Koshland, Nemethy, and Filmer (1966) will simulate the results at least equally well.

There is a more interesting angle to the issue of full cooperativity. Monod (cited by Perutz, 1990) remarked that the expectation of a concerted transition in which all protomers of a protein undergo a conformational change simultaneously is strongest when there is identity of all protomers. In that case, by a simple argument of symmetry, it is difficult to imagine stable conformational changes affecting some but not all protomers. It is interesting that hemoglobin does not satisfy this full symmetry condition by not being a homotetramer. In contrast, and for all we know, the ryanodine receptor is a homotetramer and fulfills the conditions to expect a fully cooperative transition into the open state.

There have been reports of subconductance states of the release channel. Three conductances, scaled as 1, 2, and 4 (Ma, Fill, Knudson, Campbell, and Coronado, 1988) or four conductances, scaled as 1, 2, 3, and 4 (Smith, Imagawa, Fill, Campbell, and Coronado, 1988; Liu, Lai, Rousseau, Jones, and Meissner, 1989) have been described for the purified ryanodine receptor reconstituted in bilayers. In principle, these substates may correspond to a piecewise opening mechanism (see Liu, et al., 1989, for a discussion of possibilities), against the hypothesis of full cooperativity. In a study of native protein from heavy SR, however, substates were observed in only 4% of the incorporations (Fill, Mejfa-Alvarez, Zorzato, Volpe, and Stefani, 1991). Thus there is no strong experimental evidence against the assumption of fully cooperative opening in native channels.

Marks and Jones's (1992) model of gating of L-type Ca channels is formally identical to the one presented here. One of the most striking aspects of their work is the simulation of several effects of the dihydropyridine agonist (+)202-791, assuming that the agonist alters the channel open-closed equilibrium without directly affecting the voltage sensors. With this assumption they account for a leftward shift of the activation curve, a small increase in steepness, and kinetic effects that include a slowing of deactivation tail currents. Obviously the effect of ClO_4^- on Ca release channel gating is very similar and was modeled in this article using the same assumptions. (It was, in fact, the similarity of these effects that led us to investigate the applicability of an MWC model to our problem.) In a way, our hypothesis regarding the effect of ClO_4^- is that the anion is the Bay K of EC coupling! The analogy is limited, however, as ClO_4^- seems to be a low affinity ligand, relatively nonspecific (in the sense that its effects are shared with other anions of rather different structure like thiocyanate, Ma et al., 1993), and with multiple binding sites (as suggested by the gradation of effects with concentration).

Hump-like Kinetics

A somewhat unexpected feature of the kinetic simulations was the appearance of hump-like components in the charge movement current, especially visible in the simulations with a generalized model (Appendix, Fig. 14). This feature of the simulated records cannot be readily equated to Q_{γ} because it does not generate real humps (secondary raising phases in the current) but regions of downward concavity during the ON transient. Also at variance with Q_{γ} , the hump-like ONs are accompanied by hump-like OFFs. The generation of these departures from exponential relaxation is readily understandable: the allosteric coupling between individual sensors and the release channel results in a cooperative coupling among the four sensors of a channel. When a sensor moves and (especially if ClO_4^- is present) causes opening of the channel, the other sensors will be more likely to move at the same voltage. This phenomenon, which can also be considered a positive feedback, underlies the downward concave regions of the ON simulations.

The phenomenon has formal analogies with the Ca^{2+} -mediated positive feedback mechanism used by Pizarro et al. (1991) to simulate Q_{γ} , although the latter involves interchannel feedback, whereas the allosteric mechanism has its self-reinforcing effects limited to the sensors that operate on the same channel. It is, however, clear that a coupled system of the type proposed here will have cooperative properties that may help explain Q_{γ} . Cooperative mechanisms for Q_{γ} have been discussed by Huang (reviewed in 1989) and Hui and Chandler (1990), who specifically proposed that Q_{γ} could reflect the movement of a tetrad of sensors. The present model in fact features cooperative movement of multiple sensors mediated by coupling to the release channel. It is possible that the humps and other features described as Q_{γ} obey a dual mechanism: a feedback mediated by both local Ca^{2+} and allosteric coupling to the release channel.

In conclusion, the evidence presented in this series of articles, plus the success of the model in reproducing the observations, gives support to the hypothesis of mechanical transmission. This evidence for mechanical transmission is still obviously indirect. The model, however, makes more testable predictions. For instance, other substances that modify the open-closed equilibrium of the release channel should modify charge movement in predictable ways.

APPENDIX: A GENERALIZATION OF THE ALLOSTERIC MODEL

As noted in the text, the model fails in the sense that it cannot have two properties simultaneously: a close approach to saturation of the open probability when movement of the voltage sensors is complete and a high order dependency between release (open probability) and charge movement at low voltage. A generalized model can generate transfer functions with both high curvature and saturation.

Based on the consensual nature of the voltage sensors and the existence of four separate transmembrane segments with highly positive charge, the generalized model assumes that each voltage sensor molecule has multiple (n) moving charges. For simplicity, the charges are described as independent. A third assumption has to do with the manner in which charges from the same sensor determine the behavior of that sensor. One possibility is to make each voltage sensor molecule independently and allosterically controlled by its n moving charges, using, for instance, the formalism of Marks and Jones (1992) to determine the state of the individual voltage sensor molecules. In turn, the state of the release channel is decided by its four voltage sensors as developed in the text. This type of generalization leads to an n-branched, two-step allosteric model.

We did something more parsimonious, simply assuming that each of the *n* charges in one sensor would both move independently and independently control the release channel. This assumption is equivalent to a model with $4 \times n$ independent and indistinguishable sensors, of which the model described in the text is the simplest case (n = 1).

In Figs. 13 and 14 we present equilibrium and kinetic simulations with n = 2. The differences

with the simpler case are rather trivial: the model now has 18 states, C_0 to C_8 and O_0 to O_8 ; the form of the rate constants of the voltage-dependent transitions is the same but the degeneracy factors multiplying k_C and k_{-C} are different. Thus the rate constants connecting C_j and C_{j+1} are now (8–j) k_C and jk_{-C} . The rate constants of the horizontal transitions are still $k_{\perp}f^{-j}$ and $k_{-L}f^{j}$.

The model has the same number of parameters as the simpler case and the values used in the



FIGURE 13. Simulations with a generalized allosteric model. (Top) Voltage distribution of mobile charge (Q(V), continuous)lines) and activation of release flux (dashed lines) with the model described in the Appendix, having two independent charges in each of four voltage sensor molecules. The parameter values are listed in the Appendix line of Table I. The thick lines (labeled perchlorate) represent the corresponding functions when the rate constant $k_{\rm L}$ is multiplied and k_{-1} is divided by 3. (Bottom) The corresponding transfer functions, $P_{o}(Q).$

figures are listed in Table I in the rows labeled Appendix. As always, the effect of ClO_4^- was simulated by multiplying k_L and dividing k_{-L} by the same factor (3 in this case). The model performs as expected: it gives a large shift between the voltage dependencies of charge and release (Fig. 13 A). It generates a transfer function with high curvature (Fig. 13 B) corresponding to the fact that several charges have to move in order to induce opening. Since there are

now eight charges per channel, the open probability saturates; that is, it reaches a maximum at voltages where charge is still moving. In other words, the increased number of mobile charges per channel is sufficient to have the high order dependence of open probability on charge movement (multiple charges required to open a channel) and for some charges to be superfluous (saturation of open probability reached with fewer than the maximum number of charges).

This phenomenon of saturation, of course, solves the problem with the effect of ClO_4^- at high voltage. Fig. 13 *B* shows that ClO_4^- linearizes the transfer function but does not significantly increase the maximum open probability.

The kinetic simulations with the generalized model keep the properties seen with the simple model, including substantial slowing of the transients, and feature new intriguing properties. There is now an initial fast component during the OFF that was not present in the previous simulations but was observed in the experimental records (Fig. 9A). This fast component corresponds to the same saturation phenomenon indicated above (the charges that constitute the fast component move among O states without greatly changing P_0).



FIGURE 14. Kinetic simulations with the generalized allosteric model. Selected records using the generalized 8 sensor model with the same parameters used for Fig. 13.

There are also two phases during the ON, but those had already been noted in the simulations with the simpler model. From the simulations with either model it appears that part of the nonexponential phenomena described as Q_{γ} currents could be due to allosteric interactions.

Note added in proof: Gyorke and Palade (1992) recently reported that ClO_4^- has no effect on calcium release in crayfish skeletal muscle. This result does not support the view that the primary target of ClO_4^- is the release channel, suggesting instead, as the authors indicate, that skeletal muscle-style interaction between the two proteins is essential for the ClO_4^- sensitivity. This conclusion, however, is inconsistent with the observation in the second paper of this series (Ma et al., 1993) that ClO_4^- increases affinity for ryanodine in the same proportion in purified RyR protein and in triad enriched fractions.

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many ideas on control of calcium release, even when under the influence of strong electromagnetic fields.

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