

(2*R*)-2-Benzene-sulfonamido-2-phenyl-ethanoic acid

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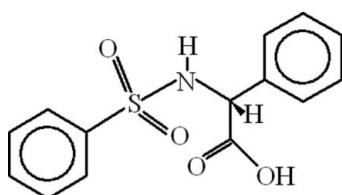
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Key indicators: single-crystal X-ray study; $T = 296\text{ K}$; mean $\sigma(\text{C}-\text{C}) = 0.005\text{ \AA}$; R factor = 0.051; wR factor = 0.091; data-to-parameter ratio = 15.5.

In the title compound, $\text{C}_{14}\text{H}_{13}\text{NO}_4\text{S}$, the dihedral angle between the aromatic ring planes is $45.52(18)^\circ$. In the crystal structure, intermolecular $\text{N}-\text{H}\cdots\text{O}$ and $\text{O}-\text{H}\cdots\text{O}$ hydrogen bonds lead to chains of molecules propagating in [100] in which the ring motifs $R_2^1(8)$, $R_2^2(8)$ and $R_3^3(11)$ are apparent. These polymeric chains are linked through $\text{C}-\text{H}\cdots\text{O}$ interactions.

Related literature

For related structures, see: Chaudhuri (1984); Shan & Huang (1999). For background, see: Arshad *et al.* (2008); Cama *et al.* (2003); Dankwardt *et al.* (2002); Zhi-jian *et al.* (2006). For graph-set notation, see: Bernstein *et al.* (1995).



Experimental

Crystal data

$\text{C}_{14}\text{H}_{13}\text{NO}_4\text{S}$	$V = 1386.03(19)\text{ \AA}^3$
$M_r = 291.31$	$Z = 4$
Orthorhombic, $P2_12_12_1$	$\text{Mo K}\alpha$ radiation
$a = 5.6022(5)\text{ \AA}$	$\mu = 0.25\text{ mm}^{-1}$
$b = 12.5026(9)\text{ \AA}$	$T = 296\text{ K}$
$c = 19.7886(15)\text{ \AA}$	$0.22 \times 0.18 \times 0.15\text{ mm}$

Data collection

Bruker Kappa APEXII CCD diffractometer

Absorption correction: multi-scan (*SADABS*; Bruker, 2005)
 $T_{\min} = 0.944$, $T_{\max} = 0.966$

8476 measured reflections
 2818 independent reflections

1679 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.050$

Refinement

$R[F^2 > 2\sigma(F^2)] = 0.051$
 $wR(F^2) = 0.091$
 $S = 1.01$
 2818 reflections
 182 parameters
 H-atom parameters constrained

$\Delta\rho_{\text{max}} = 0.23\text{ e \AA}^{-3}$
 $\Delta\rho_{\text{min}} = -0.28\text{ e \AA}^{-3}$
 Absolute structure: Flack (1983),
 1092 Friedel Pairs
 Flack parameter: 0.02 (10)

Table 1
 Hydrogen-bond geometry (\AA , $^\circ$).

$D-\text{H}\cdots A$	$D-\text{H}$	$\text{H}\cdots A$	$D\cdots A$	$D-\text{H}\cdots A$
N1—H1 \cdots O3 ⁱ	0.86	2.55	3.155 (4)	128
O3—H3O \cdots O4 ⁱⁱ	0.82	1.83	2.646 (3)	176
C2—H2 \cdots O1 ⁱⁱⁱ	0.93	2.56	3.340 (5)	142
C3—H3 \cdots O2 ^{iv}	0.93	2.54	3.225 (5)	131
C7—H7 \cdots O1 ⁱⁱⁱ	0.98	2.55	3.432 (4)	150

Symmetry codes: (i) $x + 1, y, z$; (ii) $x - \frac{1}{2}, -y + \frac{3}{2}, -z$; (iii) $x - 1, y, z$; (iv) $-x + 1, y + \frac{1}{2}, -z + \frac{1}{2}$.

Data collection: *APEX2* (Bruker, 2007); cell refinement: *SAINT* (Bruker, 2007); data reduction: *SAINT*; program(s) used to solve structure: *SHELXS97* (Sheldrick, 2008); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *ORTEP-3 for Windows* (Farrugia, 1997) and *PLATON* (Spek, 2009); software used to prepare material for publication: *WinGX* (Farrugia, 1999) and *PLATON*.

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: HB2938).

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$M_r = 291.31$	$Z = 4$
Orthorhombic, $P2_12_12_1$	$\text{Mo K}\alpha$ radiation
$a = 5.6022(5)\text{ \AA}$	$\mu = 0.25\text{ mm}^{-1}$
$b = 12.5026(9)\text{ \AA}$	$T = 296\text{ K}$
$c = 19.7886(15)\text{ \AA}$	$0.22 \times 0.18 \times 0.15\text{ mm}$

supplementary materials

Acta Cryst. (2009). E65, o940 [doi:10.1107/S1600536809011611]

(2*R*)-2-Benzenesulfonamido-2-phenylethanoic acid

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Comment

Amino acid derived sulfonamides have been synthesized as ligands (Zhi-jian *et al.*, 2006) which showed potent procollagen C-proteinase (PCP) inhibition (Dankwardt *et al.*, 2002) and arginase inhibition (Cama *et al.*, 2003). The title compound (I), (Fig 1), has been prepared as an intermediate for the synthesis of our ongoing studies of thiazine (Arshad *et al.*, 2008) related heterocycles.

The crystal structure of (II) *R*-(-)-*N*-benzenesulfonylglutamic acid (Shan & Huang, 1999) and (III) *N*-Benzenesulfonyl-DL-alanine (Chaudhuri, 1984) have been published. These structures have a common group with (I) except the benzene ring of phenyl glycine.

The title compound has a chiral center at C7 with slightly distorted tetrahedral geometry with H7 at the apical position. The coordination around the S-atom is distorted tetrahedral. The molecules of the compound are stabilized due to strong intermolecular H-bonding (Table 1). Three ring motifs $R_2^1(8)$, $R_2^2(8)$ and $R_3^3(11)$ (Bernstein *et al.*, 1995) are formed due to two H-bonds of C—H···O type, H-bonding of types C—H···O and N—H···O, and two O—H···O and N—H···O, respectively (Fig 2). The ring motifs are connected to each other in such a way that a rod-shaped attachment of molecules exist along the *a* axis. These polymeric chains are linked through the remaining H-bonding of C—H···O type.

Experimental

Phenyl glycine (1 g, 6.6 mmol) was dissolved in distilled water (10 ml) in a round bottom flask (25 ml). The pH of the solution was maintained at 8–9 using 1*M*, Na₂CO₃ solution. Benzene sulfonyl chloride (1.16 g, 6.6 mmol) was then added to the solution and stirred at room temperature until all the benzene sulfonyl chloride was consumed. On completion of the reaction the pH was adjusted 1–2, using 1 N HCl. The precipitate obtained was filtered, washed with distilled water, dried and recrystallized in dichloromethane and methanol to yield colourless prisms of (I).

Refinement

The H-atoms were positioned geometrically, with O—H = 0.82 Å N—H = 0.86 Å and C—H = 0.93–0.98 Å for aromatic, C—H = 0.98 Å and refined as riding with U_{iso}(H) = 1.2U_{eq}(carrier).

supplementary materials

Figures

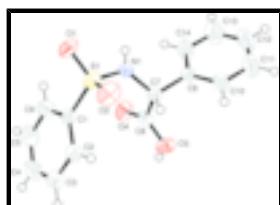


Fig. 1. View of (I) with displacement ellipsoids drawn at the 50% probability level. H-atoms are shown by small circles of arbitrary radius.

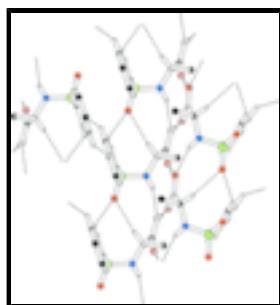


Fig. 2. The partial packing of (I) showing that molecules form ring motifs through intermolecular H-bonding. The H-atoms not involved in H-bonding and the benzene ring of phenyl glycine are omitted for clarity.

(2*R*)-2-Benzenesulfonamido-2-phenylethanoic acid

Crystal data

C ₁₄ H ₁₃ NO ₄ S	$F_{000} = 608$
$M_r = 291.31$	$D_x = 1.396 \text{ Mg m}^{-3}$
Orthorhombic, $P2_12_12_1$	Mo $K\alpha$ radiation
Hall symbol: P 2ac 2ab	$\lambda = 0.71073 \text{ \AA}$
$a = 5.6022 (5) \text{ \AA}$	Cell parameters from 2818 reflections
$b = 12.5026 (9) \text{ \AA}$	$\theta = 2.6\text{--}26.7^\circ$
$c = 19.7886 (15) \text{ \AA}$	$\mu = 0.25 \text{ mm}^{-1}$
$V = 1386.03 (19) \text{ \AA}^3$	$T = 296 \text{ K}$
$Z = 4$	Prism, colorless
	$0.22 \times 0.18 \times 0.15 \text{ mm}$

Data collection

Bruker Kappa APEXII CCD diffractometer	2818 independent reflections
Radiation source: fine-focus sealed tube	1679 reflections with $I > 2\sigma(I)$
Monochromator: graphite	$R_{\text{int}} = 0.050$
Detector resolution: 7.80 pixels mm^{-1}	$\theta_{\text{max}} = 26.7^\circ$
$T = 296 \text{ K}$	$\theta_{\text{min}} = 2.6^\circ$
ω scans	$h = -7 \rightarrow 3$
Absorption correction: multi-scan (SADABS; Bruker, 2005)	$k = -15 \rightarrow 15$
$T_{\text{min}} = 0.944, T_{\text{max}} = 0.966$	$l = -25 \rightarrow 25$
8476 measured reflections	

Refinement

Refinement on F^2	Hydrogen site location: inferred from neighbouring sites
Least-squares matrix: full	H-atom parameters constrained
$R[F^2 > 2\sigma(F^2)] = 0.051$	$w = 1/[\sigma^2(F_o^2) + (0.0304P)^2]$ where $P = (F_o^2 + 2F_c^2)/3$
$wR(F^2) = 0.091$	$(\Delta/\sigma)_{\max} < 0.001$
$S = 1.01$	$\Delta\rho_{\max} = 0.23 \text{ e \AA}^{-3}$
2818 reflections	$\Delta\rho_{\min} = -0.28 \text{ e \AA}^{-3}$
182 parameters	Extinction correction: none
Primary atom site location: structure-invariant direct methods	Absolute structure: Flack (1983), 1092 Friedal Pairs
Secondary atom site location: difference Fourier map	Flack parameter: 0.02 (10)

Special details

Geometry. Bond distances, angles *etc.* have been calculated using the rounded fractional coordinates. All su's are estimated from the variances of the (full) variance-covariance matrix. The cell e.s.d.'s are taken into account in the estimation of distances, angles and torsion angles

Refinement. Refinement of F^2 against ALL reflections. The weighted R -factor wR and goodness of fit S are based on F^2 , conventional R -factors R are based on F , with F set to zero for negative F^2 . The threshold expression of $F^2 > \sigma(F^2)$ is used only for calculating R -factors(gt) *etc.* and is not relevant to the choice of reflections for refinement. R -factors based on F^2 are statistically about twice as large as those based on F , and R -factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*/U_{\text{eq}}$
S1	0.8906 (2)	0.51683 (6)	0.15187 (4)	0.0387 (3)
O1	1.1438 (4)	0.50754 (15)	0.15986 (10)	0.0489 (9)
O2	0.7303 (5)	0.44742 (17)	0.18723 (11)	0.0554 (9)
O3	0.2940 (5)	0.62039 (15)	0.01637 (12)	0.0456 (10)
O4	0.6710 (5)	0.68015 (15)	0.01169 (12)	0.0496 (9)
N1	0.8409 (5)	0.49873 (16)	0.07161 (11)	0.0338 (9)
C1	0.8088 (7)	0.6505 (2)	0.17079 (15)	0.0363 (13)
C2	0.5942 (8)	0.6698 (3)	0.20125 (16)	0.0533 (14)
C3	0.5343 (9)	0.7746 (4)	0.21780 (18)	0.0723 (19)
C4	0.6886 (11)	0.8565 (3)	0.2012 (2)	0.075 (2)
C5	0.8993 (9)	0.8359 (3)	0.16954 (19)	0.0640 (18)
C6	0.9639 (7)	0.7318 (2)	0.15472 (16)	0.0521 (14)
C7	0.6001 (7)	0.49830 (19)	0.04431 (13)	0.0316 (12)
C8	0.5281 (8)	0.6104 (2)	0.02287 (14)	0.0340 (13)
C9	0.5829 (7)	0.4265 (2)	-0.01808 (14)	0.0318 (13)
C10	0.3966 (8)	0.3565 (2)	-0.02540 (17)	0.0507 (13)
C11	0.3774 (10)	0.2936 (3)	-0.0832 (2)	0.0690 (18)
C12	0.5456 (10)	0.3020 (3)	-0.1324 (2)	0.072 (2)

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C13	0.7293 (9)	0.3721 (3)	-0.1256 (2)	0.080 (2)
C14	0.7496 (7)	0.4351 (3)	-0.06873 (18)	0.0583 (16)
H1	0.95974	0.48921	0.04478	0.0406*
H2	0.49001	0.61383	0.21076	0.0640*
H3	0.39147	0.78931	0.23985	0.0865*
H3O	0.26138	0.68249	0.00676	0.0547*
H4	0.64818	0.92669	0.21182	0.0899*
H5	1.00004	0.89197	0.15781	0.0768*
H6	1.10972	0.71706	0.13426	0.0624*
H7	0.48902	0.47247	0.07892	0.0379*
H10	0.28216	0.35094	0.00847	0.0608*
H11	0.25062	0.24614	-0.08804	0.0827*
H12	0.53489	0.25964	-0.17091	0.0872*
H13	0.84273	0.37763	-0.15968	0.0956*
H14	0.87550	0.48313	-0.06466	0.0702*

Atomic displacement parameters (\AA^2)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
S1	0.0371 (7)	0.0395 (4)	0.0395 (4)	0.0025 (5)	-0.0015 (5)	0.0072 (4)
O1	0.0308 (18)	0.0569 (13)	0.0590 (14)	0.0051 (14)	-0.0105 (13)	0.0060 (12)
O2	0.055 (2)	0.0573 (14)	0.0538 (14)	-0.0093 (13)	0.0066 (13)	0.0230 (11)
O3	0.037 (2)	0.0322 (13)	0.0677 (16)	0.0072 (13)	0.0039 (16)	0.0136 (12)
O4	0.048 (2)	0.0318 (11)	0.0690 (16)	-0.0128 (14)	-0.0048 (14)	0.0143 (10)
N1	0.030 (2)	0.0351 (13)	0.0364 (13)	0.0025 (15)	0.0059 (13)	-0.0056 (11)
C1	0.031 (3)	0.0481 (19)	0.0297 (18)	-0.0040 (18)	0.0001 (17)	-0.0046 (14)
C2	0.045 (3)	0.067 (2)	0.048 (2)	0.001 (3)	0.000 (2)	-0.0200 (17)
C3	0.049 (4)	0.096 (3)	0.072 (3)	0.016 (3)	-0.006 (2)	-0.039 (3)
C4	0.085 (5)	0.059 (3)	0.082 (3)	0.015 (3)	-0.011 (3)	-0.033 (2)
C5	0.070 (4)	0.046 (2)	0.076 (3)	-0.010 (2)	-0.004 (3)	-0.0124 (19)
C6	0.057 (3)	0.0494 (19)	0.050 (2)	0.001 (2)	0.009 (2)	-0.0060 (19)
C7	0.032 (3)	0.0251 (15)	0.0378 (16)	0.0002 (19)	0.0039 (17)	0.0037 (12)
C8	0.041 (3)	0.0298 (18)	0.0311 (17)	0.002 (2)	0.003 (2)	-0.0001 (14)
C9	0.030 (3)	0.0242 (14)	0.0412 (18)	0.0008 (17)	0.0001 (18)	0.0012 (13)
C10	0.057 (3)	0.0360 (17)	0.059 (2)	-0.006 (2)	0.003 (2)	-0.0045 (16)
C11	0.082 (4)	0.045 (2)	0.080 (3)	-0.014 (2)	-0.017 (3)	-0.012 (2)
C12	0.093 (5)	0.062 (3)	0.062 (3)	-0.005 (3)	-0.011 (3)	-0.027 (2)
C13	0.078 (5)	0.103 (3)	0.059 (3)	-0.017 (3)	0.020 (3)	-0.029 (2)
C14	0.059 (4)	0.068 (2)	0.048 (2)	-0.022 (2)	0.013 (2)	-0.017 (2)

Geometric parameters (\AA , $^\circ$)

S1—O1	1.432 (3)	C9—C14	1.374 (5)
S1—O2	1.432 (3)	C9—C10	1.370 (5)
S1—N1	1.628 (2)	C10—C11	1.392 (5)
S1—C1	1.773 (3)	C11—C12	1.359 (7)
O3—C8	1.324 (5)	C12—C13	1.358 (7)
O4—C8	1.204 (4)	C13—C14	1.378 (5)
O3—H3O	0.8200	C2—H2	0.9300

N1—C7	1.453 (5)	C3—H3	0.9300
N1—H1	0.8600	C4—H4	0.9300
C1—C2	1.366 (6)	C5—H5	0.9300
C1—C6	1.375 (4)	C6—H6	0.9300
C2—C3	1.392 (6)	C7—H7	0.9800
C3—C4	1.380 (7)	C10—H10	0.9300
C4—C5	1.361 (7)	C11—H11	0.9300
C5—C6	1.382 (5)	C12—H12	0.9300
C7—C8	1.519 (4)	C13—H13	0.9300
C7—C9	1.530 (4)	C14—H14	0.9300
O1—S1—O2	121.22 (14)	C10—C11—C12	119.4 (4)
O1—S1—N1	105.42 (14)	C11—C12—C13	120.3 (4)
O1—S1—C1	108.01 (15)	C12—C13—C14	120.8 (4)
O2—S1—N1	106.58 (14)	C9—C14—C13	119.7 (4)
O2—S1—C1	107.82 (16)	C1—C2—H2	121.00
N1—S1—C1	107.03 (13)	C3—C2—H2	121.00
C8—O3—H3O	109.00	C2—C3—H3	120.00
S1—N1—C7	121.5 (2)	C4—C3—H3	120.00
S1—N1—H1	119.00	C3—C4—H4	120.00
C7—N1—H1	119.00	C5—C4—H4	120.00
C2—C1—C6	121.9 (3)	C4—C5—H5	120.00
S1—C1—C2	119.2 (3)	C6—C5—H5	120.00
S1—C1—C6	119.0 (3)	C1—C6—H6	121.00
C1—C2—C3	118.8 (4)	C5—C6—H6	121.00
C2—C3—C4	119.5 (4)	N1—C7—H7	109.00
C3—C4—C5	120.8 (4)	C8—C7—H7	109.00
C4—C5—C6	120.2 (4)	C9—C7—H7	109.00
C1—C6—C5	118.8 (4)	C9—C10—H10	120.00
C8—C7—C9	107.4 (2)	C11—C10—H10	120.00
N1—C7—C9	111.2 (3)	C10—C11—H11	120.00
N1—C7—C8	110.3 (3)	C12—C11—H11	120.00
O3—C8—O4	124.9 (3)	C11—C12—H12	120.00
O3—C8—C7	112.2 (3)	C13—C12—H12	120.00
O4—C8—C7	122.9 (4)	C12—C13—H13	120.00
C7—C9—C10	120.6 (3)	C14—C13—H13	120.00
C7—C9—C14	120.0 (3)	C9—C14—H14	120.00
C10—C9—C14	119.4 (3)	C13—C14—H14	120.00
C9—C10—C11	120.4 (4)		
O1—S1—N1—C7	177.57 (18)	C4—C5—C6—C1	1.8 (6)
O2—S1—N1—C7	47.6 (2)	N1—C7—C8—O3	-161.7 (2)
C1—S1—N1—C7	-67.6 (2)	N1—C7—C8—O4	20.1 (4)
O1—S1—C1—C2	-145.8 (3)	C9—C7—C8—O3	77.0 (3)
O1—S1—C1—C6	33.9 (3)	C9—C7—C8—O4	-101.2 (4)
O2—S1—C1—C2	-13.2 (3)	N1—C7—C9—C10	134.8 (3)
O2—S1—C1—C6	166.5 (3)	N1—C7—C9—C14	-48.0 (4)
N1—S1—C1—C2	101.2 (3)	C8—C7—C9—C10	-104.5 (3)
N1—S1—C1—C6	-79.2 (3)	C8—C7—C9—C14	72.7 (4)
S1—N1—C7—C8	90.6 (2)	C7—C9—C10—C11	178.0 (3)

supplementary materials

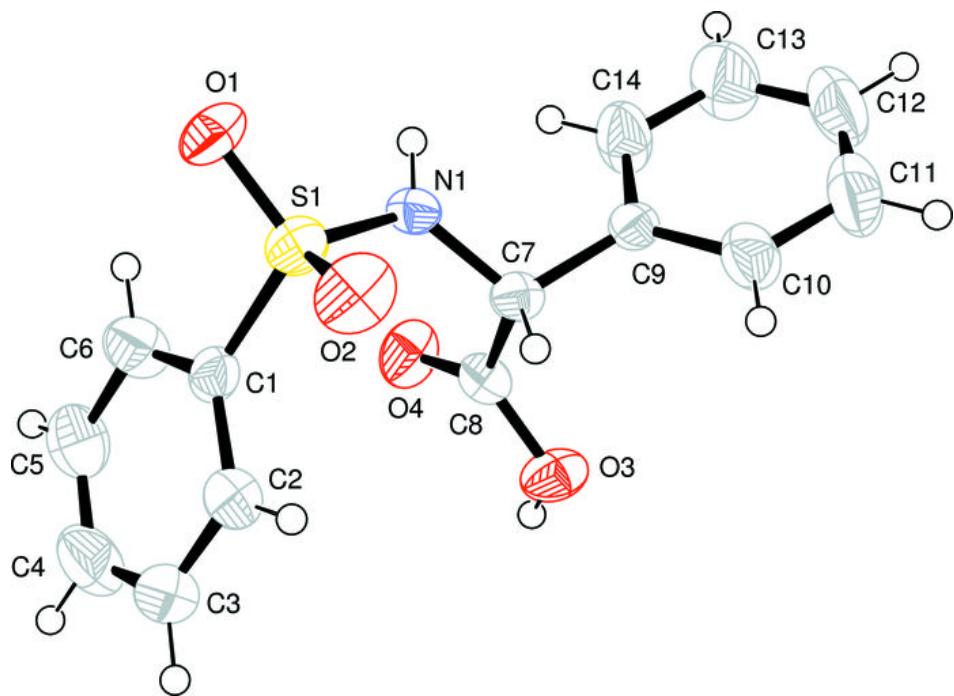
S1—N1—C7—C9	−150.35 (18)	C14—C9—C10—C11	0.8 (5)
S1—C1—C2—C3	178.1 (3)	C7—C9—C14—C13	−178.3 (3)
C6—C1—C2—C3	−1.5 (5)	C10—C9—C14—C13	−1.0 (5)
S1—C1—C6—C5	180.0 (3)	C9—C10—C11—C12	0.1 (6)
C2—C1—C6—C5	−0.4 (5)	C10—C11—C12—C13	−0.8 (7)
C1—C2—C3—C4	2.1 (6)	C11—C12—C13—C14	0.5 (7)
C2—C3—C4—C5	−0.7 (6)	C12—C13—C14—C9	0.4 (6)
C3—C4—C5—C6	−1.3 (6)		

Hydrogen-bond geometry (\AA , °)

$D\cdots H$	$D—H$	$H\cdots A$	$D\cdots A$	$D—H\cdots A$
N1—H1···O3 ⁱ	0.86	2.55	3.155 (4)	128
O3—H3O···O4 ⁱⁱ	0.82	1.83	2.646 (3)	176
C2—H2···O1 ⁱⁱⁱ	0.93	2.56	3.340 (5)	142
C3—H3···O2 ^{iv}	0.93	2.54	3.225 (5)	131
C7—H7···O1 ⁱⁱⁱ	0.98	2.55	3.432 (4)	150

Symmetry codes: (i) $x+1, y, z$; (ii) $x-1/2, -y+3/2, -z$; (iii) $x-1, y, z$; (iv) $-x+1, y+1/2, -z+1/2$.

Fig. 1



supplementary materials

Fig. 2

