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## Whole-brain 3D mapping of oxygen metabolism using constrained quantitative BOLD

Hyunyeol Lee<sup>a,b</sup>, Felix W Wehrli<sup>a,\*</sup>

<sup>a</sup>Laboratory for Structural, Physiologic, and Functional Imaging, Department of Radiology, University of Pennsylvania, Philadelphia, Pennsylvania, United States

<sup>b</sup>School of Electronics Engineering, Kyungpook National University, Daegu, South Korea

### Abstract

Quantitative BOLD (qBOLD) MRI permits noninvasive evaluation of hemodynamic and metabolic states of the brain by quantifying parametric maps of deoxygenated blood volume (DBV) and hemoglobin oxygen saturation level of venous blood ( $Y_v$ ), and along with a measurement of cerebral blood flow (CBF), the cerebral metabolic rate of oxygen ( $CMRO_2$ ). The method, thus should have potential to provide important information on many neurological disorders as well as normal cerebral physiology. One major challenge in qBOLD is to separate de-oxyhemoglobin's contribution to  $R_2'$  from other sources modulating the voxel signal, for instance,  $R_2$ ,  $R_2'$  from non-heme iron ( $R'_{2,nh}$ ), and macroscopic magnetic field variations. Further, even with successful separation of the several confounders, it is still challenging to extract DBV and  $Y_v$  from the heme-originated  $R_2'$  because of limited sensitivity of the qBOLD model. These issues, which have not been fully addressed in currently practiced qBOLD methods, have so far precluded 3D whole-brain implementation of qBOLD. Thus, the purpose of this work was to develop a new 3D MRI oximetry technique that enables robust qBOLD parameter mapping across the entire brain. To achieve this goal, we employed a rapid,  $R_2'$ -sensitive, steady-state 3D pulse sequence (termed 'AUSFIDE') for data acquisition, and implemented a prior-constrained qBOLD processing pipeline that exploits a plurality of preliminary parameters obtained via AUSFIDE, along with additionally measured cerebral venous blood volume. Numerical simulations and in vivo studies at 3 T were performed to evaluate the performance of the proposed, constrained qBOLD mapping in comparison to the parent qBOLD method. Measured parameters ( $Y_v$ , DBV,  $R'_{2,nh}$ , nonblood magnetic susceptibility) in ten healthy subjects demonstrate the expected contrast across brain territories, while yielding group-averages of  $64.0 \pm 2.3$  % and  $62.2 \pm 3.1$  % for  $Y_v$  and  $2.8 \pm 0.5$  % and  $1.8 \pm 0.4$  % for DBV in cortical gray and white matter, respectively. Given the  $Y_v$  measurements, additionally quantified CBF in seven of the ten study subjects enabled whole-brain 3D  $CMRO_2$  mapping, yielding group averages of  $134.2 \pm 21.1$  and  $79.4 \pm 12.6$   $\mu\text{mol}/100$  g/min for cortical gray and white matter, in good agreement with literature values. The

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\*Corresponding author. felix.wehrli@pennmedicine.upenn.edu (F.W. Wehrli).

Declaration of Competing Interest

None

Supplementary materials

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results suggest feasibility of the proposed method as a practical and reliable means for measuring neurometabolic parameters over an extended brain coverage.

## Keywords

Quantitative BOLD; 3D; Constrained inverse problem; Brain metabolism; Hemoglobin oxygen saturation; Cerebral metabolic rate of oxygen

## 1. Introduction

The cerebrovascular system adaptively regulates itself in close interaction with neuronal cells. Thus, changes in oxygen metabolism reflect alterations in cerebral hemodynamics or perturbations of brain function, for example, during aging (Yamaguchi et al., 1986) and in disease states such as ischemic stroke (Girouard and Iadecola, 2006). Further, the brain's oxygen demand decreases during states of reduced consciousness, including sleep (Caporale, 2021; Madsen et al., 1991) and anesthesia (Renou et al., 1978). Hence, cerebral metabolic rate of oxygen (CMRO<sub>2</sub>) representing brain oxygen utilization and consumption is an important parameter that provides valuable information about cerebral physiology in health and disease. As cerebral metabolism is tightly coupled to oxygen supply from arterial blood and oxygen extraction in the capillary bed, CMRO<sub>2</sub> is typically expressed by the following equation (known as Fick's principle):

$$CMRO_2 = C_a \cdot CBF \cdot (Y_a - Y_v) \quad (1)$$

Here,  $C_a$  is the oxygen carrying capacity of arterial blood in  $\mu\text{mol O}_2$  per ml blood, CBF is the cerebral blood flow in units of ml blood per minute per 100 g tissue, and  $Y_a$  and  $Y_v$  are the percent hemoglobin oxygen saturation levels of arterial and venous blood, respectively. Eq. [1] indicates that both CBF and oxygen extraction fraction ( $OEF = (Y_a - Y_v)/Y_a$ ) must be ascertained to derive CMRO<sub>2</sub>.

Positron emission tomography is generally regarded as the gold standard for regional CMRO<sub>2</sub> mapping (Frackowiak et al., 1980; Mintun et al., 1984), in which radioactive tracers in the form of  $^{15}\text{O}_2$  and  $\text{H}_2^{15}\text{O}$  are separately administered to the subject for measurements of OEF and CBF, respectively. However, the method's clinical utility has been limited largely by high radiation exposure, long imaging time, and the cost and complexity of the experimental setting. As a potentially more practical and noninvasive alternative, MRI-based methods have emerged, such as arterial-spin-labeling (ASL) (Alsop et al., 2015) in conjunction with quantitative BOLD (qBOLD) (An and Lin, 2000; He and Yablonskiy, 2007) yielding CBF and OEF, respectively, on a pixel-by-pixel basis. Additionally, methods generally referred to as calibrated BOLD (cBOLD) (Blockley et al., 2013) permit voxel-wise estimation of relative changes of CMRO<sub>2</sub> in response to neural stimulation by calibrating BOLD signal in two presumed isometabolic states of the brain (Davis et al., 1998). Recent dual-gas calibration approaches further enable measurements of resting-state CMRO<sub>2</sub> in absolute physiologic units (Gauthier and Hoge, 2013; Wise et al., 2013). Nevertheless, in cBOLD experimental preparation for gas administration and subject discomfort from the

procedure are limiting factors. Furthermore, some of the assumptions made in the calibration model remain arguable (e.g., Grubb's constant (Chen and Pike, 2010) and isometabolicity of gas challenges (Englund et al., 2020; Peng et al., 2017)).

qBOLD is a calibration-free technique and instead directly quantifies the two critical determinants of the BOLD signal, i.e., deoxygenated hemoglobin (dHb) concentration in venous blood ( $[dHb]_v = C_a(1-Y_v)$ ) and deoxygenated blood volume (DBV). Under the static dephasing regime (Yablonskiy and Haacke, 1994), the qBOLD model characterizes the MR signal evolution at short and long time scales, and particularly for the latter the RF-reversible portion of the transverse relaxation rate ( $R_2'$ ) is linearly proportional to the two parameters ( $Y_v$  and DBV). Thus, the qBOLD method typically acquires  $R_2'$ -weighted time-series data and then attempts to separate measured  $R_2'$  into  $Y_v$  and DBV. However, conventional qBOLD presents two major problems. First, on the data acquisition side, currently practiced  $R_2'$  mapping methods (Ni et al., 2015), generally referred to as GESSE (gradient-echo sampling of spin-echo) (Yablonskiy, 1998), GESFIDE (gradient-echo sampling of free-induction-decay and echo) (Ma and Wehrli, 1996), or ASE (asymmetric spin-echo) (An and Lin, 2003), commonly rely on the spin-echo mechanism applying a  $180^\circ$  RF pulse. Thus, the utility of these methods has been largely limited to 2D quantifications, and their extension to 3D qBOLD would entail impractically long scan times for 3D encoding. Second, from the parameter estimation perspective, the qBOLD model presents limited parameter sensitivity (Lee et al., 2018; Sedlacik and Reichenbach, 2010). Specifically, mutual coupling between  $Y_v$  and DBV in the signal model renders the quantification error-prone and unstable, resulting in relatively low reproducibility of the method. Furthermore, in the original qBOLD model, contribution of non-heme iron to  $R_2'$  is not accounted for (i.e., the relative magnetic susceptibility of extravascular tissue is approximated to that of fully oxygenated blood  $\sim -0.1$  ppm (Yablonskiy et al., 2013a)), which may result in erroneous estimates, particularly in deep brain structures presenting susceptibility values higher on the positive side (up to +0.2 ppm (Lim et al., 2013)) due to high non-heme iron content in the basal ganglia.

More recently, an approach combining qBOLD and quantitative susceptibility mapping (QSM) has been suggested (referred to as qBOLD+QSM (Cho et al., 2018)). The method employs a 3D multi-echo spoiled gradient-echo (GRE) pulse sequence, a typical choice in QSM for local field estimation by means of phase analysis (Wang and Liu, 2015), and utilizes  $R_2^*$ -weighted magnitude images for qBOLD processing. Compared to the original qBOLD method, the parameter estimation model was modified such that non-blood tissue susceptibility ( $\chi_{nb}$ ) was explicitly included in the temporal signal decay while four-pool decomposition of voxel susceptibility ( $\chi$ ) (i.e., deoxygenated arterial and venous blood, fully oxygenated blood, and non-blood tissue (Zhang et al., 2015)) was added as a constraint. It was shown that qBOLD+QSM with 3D multi-echo spoiled GRE achieves rapid 3D qBOLD scanning while reducing noise sensitivity in the parameter estimation (Cho et al., 2018). However, a more recent analysis (Hubertus et al., 2019) has revealed that qBOLD+QSM yields overall higher measurement accuracy in gray matter regions with GESSE than that obtainable with multi-echo spoiled GRE. This would have resulted from the fact that, unlike GRE, GESSE is able to extract  $R_2'$  directly from signal decay curves.

In this work, we aimed to address the above noted challenges in 3D qBOLD parameter mapping, i.e., high-speed scanning and robust quantification. To this end, in the data acquisition, a recently developed, scan-time efficient 3D  $R_2'$  mapping pulse sequence (Lee and Wehrli, 2021), termed ‘Alternating Unbalanced Steady-state-free-precession Free-Induction-Decay and Echo (AUSFIDE)’, was employed, while in the qBOLD processing pipeline, parametric information obtained from AUSFIDE ( $R_2$ ,  $R_2'$ ,  $\chi$ , macroscopic magnetic field inhomogeneity) was fully integrated into a prior-constrained non-linear inverse problem. Additionally, venous cerebral blood volume ( $CBV_v$ ) was separately measured using an in-house developed method (Lee and Wehrli, 2020), termed ‘velocity-selective venous-spin-labeling (VS-VSL)’, serving as prior information for DBV. The obtained  $Y_v$  maps along with separate CBF measurements enabled 3D  $CMRO_2$  mapping across the entire brain. Numerical simulations and in-vivo experiments were performed to evaluate the performance of the proposed qBOLD method in comparison to the existing techniques.

## 2. Methods

### 2.1. AUSFIDE-based 3D qBOLD

One key challenge that currently practiced qBOLD techniques face is separation of the four competing mechanisms that affect temporal signal decays across echoes collected:  $R_2$  (microscopic),  $R_2'$  from heme ( $R_2',_h$ ) and non-heme ( $R_2',_{nh}$ ) iron contributions (mesoscopic), and background magnetic field inhomogeneity ( $B_0$ ; macroscopic). Further, extracting  $Y_v$  and DBV from the measured  $R_2',_h$  is generally nontrivial as noted in Introduction. The following subsections along with Fig. 1 detail the proposed approach in terms of data acquisition and parameter estimation so as to disentangle the above confounders and thereby achieving reliable measurements of the qBOLD parameters. Symbols used to represent parameters and their corresponding descriptions are listed in Table 1.

**2.1.1. Estimation of preliminary parameters**—The proposed 3D qBOLD protocol consists of two pulse sequences: AUSFIDE (Fig. 1a) yielding a set of volumetric maps ( $R_2$ ,  $R_2'$ ,  $\chi$ ,  $B_0$ ; Fig. 1c), and additionally VS-VSL (Fig. 1b) leading to voxel-wise  $CBV_v$  estimates (Fig. 1d) across the entire brain.

Based on the unbalanced steady-state-free-precession (SSFP) mechanism (Scheffler, 1999) generating steady-state signals in a number of spin configurations, AUSFIDE deploys SSFP-FID and SSFP-ECHO modules in an alternating and time-symmetric fashion along the entire pulse train (Fig. 1a) for selective acquisition of SSFP signals in the 0th and -1st spin pathways, respectively, with a plurality of gradient-recalled signals within each time-of-repetition (TR). The decay rate of SSFP-FID and SSFP-ECHO signals along time is then expressed by  $R_2+R_2'$  ( $= R_2^*$ ) and  $R_2-R_2'$ , respectively, while temporal evolution of signal phase therein is governed by magnetic fields both at voxel and larger scales. Thus, AUS-FIDE enables quantification of  $R_2$  and  $R_2'$  from magnitude data processing (Fig. 1c), and  $\chi$  and  $B_0$  from phase analysis (Fig. 1d) (see Eq. [2] below for signal modeling). This is a key advantage over the currently practiced qBOLD pulse sequences. On one

hand, compared to the 2D-limited  $R_2'$  measurement techniques, AUSIFDE achieves rapid 3D volumetric scanning, thus allowing for additional estimation of  $\chi$  via QSM. On the other hand, compared to multi-echo 3D spoiled GRE, AUSIFDE is able to separate  $R_2^*$  into  $R_2$  and  $R_2'$  contributions directly. Additional components in the AUSIFDE sequence include 3D z-shimming gradients along the multi-echo train (Han et al., 2015) and the radial stack-of-stars k-space sampling scheme (Block et al., 2014) so as to make the  $R_2'$  mapping relatively immune to large-scale magnetic field inhomogeneity and physiologic bulk fluid motion, respectively (Lee and Wehrli, 2021).

In the VS-VSL pulse sequence (Fig. 1b), two magnetization preparation modules are sequentially applied to respective spatial positions to null signals for both upstream arterial blood and cerebrospinal-fluid, followed by a control/tag VS pulse train to sensitize moving spins, thereby ensuring labeling of venous blood only. Subsequently, single-slab 3D fast SE with variable refocusing flip angles and center-out k-space view ordering schemes is employed to achieve rapid and  $B_0$ -insensitive signal readout with a minimal loss of the labeled venous blood population. In the quantification, a simplified VS-VSL signal model yields  $CBV_v$  directly from control/tag difference (Lee and Wehrli, 2020).

**2.1.2. Prior-constrained qBOLD model**—In the absence of blood vessel network, the signal evolution of SSFP-FID ( $S_F$ ) and SSFP-ECHO ( $S_E$ ) modules in AUSIFDE can be written as:

$$\begin{cases} S_F(T E_F) = S_0 s^{-(R_2 + R_2')T E_F} F_{V S F}(\Delta B_0, T E_F) e^{-j\Phi} \\ S_E(T E_E) = \eta S_0 e^{(R_2 - R_2')T E_E} F_{V S F}(-\Delta B_0, T E_E) e^{j\Phi} \end{cases} \quad (2)$$

where the subscripts F and E represent SSFP-FID and SSFP-ECHO, TE is the echo time,  $S_0$  is the baseline steady-state signal level of SSFP-FID,  $\eta$  is the ratio of  $S_E$  to  $S_F$  at TE = 0,  $F_{V S F}$  is the voxel-spread-function representing  $B_0$ -induced voxel signal modulations (Yablonskiy et al., 2013b), and  $\Phi$  is the signal phase as a function of total magnetic field (i.e.,  $B_0 + \chi$ -induced local field). Given the estimates of  $B_0$  and the resultant  $F_{V S F}$ , the unknown parameters in Eq. [2],  $S_0$ ,  $\eta$ ,  $R_2$ , and  $R_2'$ , can be jointly estimated (Lee and Wehrli, 2021).

In the presence of a blood vessel network, heme iron and non-heme iron both perturb local magnetic field, altering the transverse relaxation rate  $R_2'$  made up of  $R'_{2,h} + R'_{2,nh}$ . In the qBOLD framework aiming to resolve the dHb-related  $R_2'$  ( $R'_{2,h}$ ) into  $Y_v$  and DBV, the two sources of  $R_2'$  modulation thus needs to be separately taken into account. Accordingly, Eq. [2] is modified to:

$$\begin{cases} S_F(T E_F) = S_0 e^{-(R_2 + R'_{2,nh})T E_F} e^{-\zeta \cdot f(T E_F \delta\omega)} F_{V S F}(\Delta B_0, T E_F) e^{-j\Phi} \\ S_E(T E_E) = \eta S_0 e^{(R_2 - R'_{2,nh})T E_E} e^{-\zeta \cdot f(T E_E \delta\omega)} F_{V S F}(-\Delta B_0, T E_E) e^{j\Phi} \end{cases} \quad (3)$$

Here, the term  $e^{-\zeta \cdot f(\cdot)}$  is the qBOLD model representing the effect of dHb on the extravascular tissue signal,  $\zeta$  is DBV, and  $f(\cdot)$  characterizes the rate of signal decay as quadratic and linear functions of its argument asymptotically at short and long TEs, respectively (Yablonskiy and Haacke, 1994).  $\delta_\omega$  is the characteristic frequency due to the susceptibility of deoxygenated blood relative to the surrounding tissue, expressed by (Cho et al., 2018; Yablonskiy et al., 2013a):

$$\delta_\omega(Y_v, \chi_{nb}) = \frac{1}{3}\gamma B_0(\Delta\chi_0 Hct(1 - Y_v) + \chi_{ba} - \chi_{nb}) \quad (4)$$

where  $\gamma$  is the gyromagnetic ratio,  $B_0$  is the static field strength,  $\chi_0$  is the susceptibility difference between fully oxygenated and fully deoxygenated red blood cells ( $\sim 4\pi \times 0.27$  ppm (Spees et al., 2001)), and Hct is the blood hematocrit level.  $\chi_{ba}$  is the susceptibility of fully oxygenated blood, which can be calculated by volume-weighted combination of susceptibilities of oxygenated hemoglobin ( $\chi_{oHb} \sim -0.813$  ppm) and blood plasma ( $\chi_p \sim -0.038$  ppm) (Zhang et al., 2015; Zhang et al., 2017).

To estimate the qBOLD parameters ( $Y_v$  and DBV), AUSFIDE images along the multi-echo train may be fitted directly to the signal model in Eq. [3], which, however, makes the problem computationally intensive and potentially unstable because of many unknowns ( $S_0$ ,  $\eta$ ,  $R_2$ ,  $R_2'$ ,  $\chi_{nb}$ ,  $Y_v$ ,  $\zeta$ ) being solved jointly. Instead, the solutions can be found in two steps: 1) estimating  $S_0$ ,  $\eta$ ,  $R_2$ , and  $R_2'$  using Eq. [2], and based on this information, 2) seeking the remaining parameters by solving the following nonlinear least-squares problem:

$$\operatorname{argmin}_{\Theta} \sum_{TE} |y(TE) - \Xi(\Theta, TE)|^2 \quad (5)$$

where  $\mathbf{y}$  is the acquired AUSFIDE signals at the sampling time TE for each voxel,  $\Xi = \{|S_F|, |S_E|\}$  is the corresponding model (Eq. [3]), and  $\theta = \{Y_v, \zeta, R_2', \chi_{nb}\}$  is the set of unknown parameters to be solved. Furthermore, to enhance solution accuracy while reducing noise amplifications in the parameter estimation,  $R_2'$  and  $\chi$  obtainable from magnitude and phase processing of the AUSFIDE data are utilized as prior information, leading to the following optimization problem:

$$\operatorname{argmin}_{\Theta} \sum_{TE} |y(TE) - \Xi(\Theta, TE)|^2 + w|\Delta\chi - \Psi(\Theta)|^2 + p|R_2' - Y(\Theta)|^2 \quad (6)$$

Here,  $\Psi$  decomposes  $\chi$  into susceptibility contributions of the four compartments in a voxel, i.e., deoxygenated arterial and venous blood, fully oxygenated blood, and non-blood tissue, given by (Zhang et al., 2015; Zhang et al., 2017):

$$\Psi = \frac{\zeta}{\alpha}[\Delta\chi_0 Hct\{(1 - \alpha)(1 - Y_a) + \alpha(1 - Y_v)\} + \chi_{ba}] + \left(1 - \frac{\zeta}{\alpha}\right)\chi_{nb} \quad (7)$$

where  $\alpha$  is the volume fraction of venous blood relative to total blood, assumed to be 0.77 (An and Lin, 2002). In Eq. [6],  $Y$  disentangles  $R_2'$  contributions from the non-heme iron ( $R_{2, nh}'$ ) and dHb ( $R_{2, h}'$ ), written by:

$$Y = R_{2, nh}' + R_{2, h}' = R_{2, nh}' + \zeta \cdot \delta_{\omega}(Y_v, \chi_{nb}) \quad (8)$$

and  $w$  and  $p$  are the regularization parameters that enforce prior knowledge of  $\chi$  and  $R_2'$ , respectively. Thus, with  $w = p = 0$  Eq. [6] represents the original qBOLD problem, while with  $w > 0$  but  $p = 0$  it is equivalent to the qBOLD+QSM approach.

Additionally, based on the recent analysis (Lee et al., 2018) suggesting substantially improved stability of the qBOLD mapping with prior information for DBV, in this work VS-VSL-derived  $CBV_v$  was employed to initialize and constrain the solution of DBV. Nevertheless, since the VS-VSL method may result in measurement errors in some voxels in which its assumptions are not valid (Lee and Wehrli, 2020), here DBV was refined during the iterative process of solving Eq. [6], rather than being fixed to  $CBV_v$ . Details in solving Eq. [6] are provided in Section 2.4.1 below.

## 2.2. Numerical simulations

The performance of the proposed AUSFIDE-based qBOLD in comparison to the spoiled GRE-based approach was investigated numerically in Matlab (MathWorks, Natick, MA). To this end, simulations were performed involving the following steps: 1) baseline steady-state signals (i.e.,  $S_0$  and  $\eta S_0$  in Eq. [2]) were calculated using summation of isochromats (Shkarin and Spencer, 1997), 2) given a set of nominal parameters chosen, a time series of AUSFIDE signals was computed using Eq. [3], 3) Gaussian noise was added to each of the multi-echo signals in Step 2, and 4) Eq. [5] was solved to yield a solution for  $R_2$ ,  $R_2'$ ,  $Y_v$ , and DBV. Steps 1–4 were repeated 10,000 times independently, leading to the mean absolute error (MAE) of the estimated parameters relative to corresponding nominal values. In each of the 10,000 simulations, nominal values for  $R_2$ ,  $Y_v$ , and DBV were varied randomly in the ranges:  $10 \text{ s}^{-1} < R_2 < 20 \text{ s}^{-1}$ ,  $40 \% < Y_v < 80 \%$ , and  $1 \% < \text{DBV} < 5 \%$ , while the following parameters were set to zero for simplicity:  $R_{2, nh}'$ ,  $\chi_{ba}$ ,  $\chi_{nb}$ , and  $B_0$ . The entire procedure above was repeated seven times by changing standard deviations (SD) of the Gaussian noise from  $-7$  to  $-4$  (increment: 0.5) in the natural log scale (corresponding signal-to-noise ratio (SNR) levels of approximately 1100, 670, 400, 240, 150, 90, and 50). Furthermore, the effectiveness of using prior knowledge of  $CBV_v$  was also evaluated by initializing the solution for DBV to its nominal value at each time of parameter estimation. Simulation parameters pertinent to the AUSFIDE pulse sequence were: TR = 30 ms, first  $TE_F = 1.6$  ms, first  $TE_E = 2.2$  ms, echo spacing = 3 ms, number of echoes = 9, and flip angle =  $25^\circ$ . The SSFP-FID portion of the AUSFIDE signals was used to simulate the spoiled GRE signal because the steady-state signal of spoiled GRE with TR = 30 ms and flip angle  $\sim 15^\circ$  (Ernst angle for brain tissues) is at a level comparable to  $S_{FID}$  resulting from the parameters stated above.

To examine the effect of potential bias in  $CBV_v$  prior on the qBOLD parameter estimation, simulations were performed by varying errors in  $CBV_v$  with respect to a nominal value for

DBV from  $-40\%$  to  $40\%$  (increment:  $10\%$ ). Here, in addition to varying nominal values for  $R_2$ ,  $Y_v$ , and DBV as above, a reference for  $\chi_{nb}$  was also chosen randomly in the range  $0.01 \text{ ppm} < \chi_{nb} < 0.1 \text{ ppm}$  over the simulations, while a linear relationship between  $\chi_{nb}$  and  $R'_{2,nh}$  was assumed, leading to a nominal value for  $R'_{2,nh}$  given the reference  $\chi_{nb}$ . It is noted that  $\chi_{nb}$  also resides on the negative side for some regions of the brain (particularly white matter) where the assumed slope defining  $R'_{2,nh}$  against  $\chi_{nb}$  may differ (Chen et al., 2021; Emmerich et al., 2020). However, since the primary focus of this work was to separate  $R_2'$  contributions from heme- and non-heme iron, in the simulations  $\chi_{nb}$  values only within the positive range were examined, typical of non-heme iron. In experimental data processing (see Section 2.4.1 below), the solution for  $\chi_{nb}$  was sought for both positive and negative sides.  $\chi_{ba}$  was computed assuming Hct of 0.357. Given the resultant AUSFIDE signals computed, Gaussian noise yielding a SNR of  $\sim 140$  for the first echo of SSFP-FID was added. The value of 140 was based on the SNR measurement on actual brain images obtained using the AUSFIDE pulse sequence. Subsequently, Eq. [6] was solved with a biased  $CBV_v$  prior in three different manners: 1)  $w = p = 0$ ; 2)  $w > 0, p = 0$ ; 3)  $w > 0, p > 0$ . MAE of the solutions ( $Y_v, DBV, R'_{2,nh}, \chi_{nb}$ ) estimated over 10,000 simulations was calculated for the three scenarios.

### 2.3. Experiments

All experimental studies were approved by the Institutional Review Board of the University of Pennsylvania. Informed written consent was obtained from all study subjects ( $N = 10$ ; five males; age mean  $\pm$  SD =  $31 \pm 7$  years) individually prior to scanning at 3 T (Siemens Prisma, Erlangen, Germany) with a 32-channel head-coil for signal reception. Following MRI data collections, hemoglobin concentration in each subject was measured via a finger stick test. The resultant value was then scaled up by 2.5 to yield Hct in a microvascular system (Eichling et al., 1975).

Data were acquired in all study participants using the AUSIFDE and VS-VSL pulse sequences, implemented in SequenceTree (Magland et al., 2016). Imaging parameters used in AUSFIDE were: field-of-view (FOV) =  $240 \times 240 \times 120 \text{ mm}^3$ , reconstruction matrix =  $160 \times 160 \times 40$ , number of radial views = 144, echo spacing = 1.5 ms, number of echoes = 17 (nine regularly encoded + eight z-shimmed), yielding a scan time of 8 minutes. The remaining parameters were identical to those specified in the section of Numerical Simulations. Imaging parameters specific to VS-VSL were: FOV =  $220 \times 220 \times 180 \text{ mm}^3$  (sagittal orientation), reconstruction matrix =  $72 \times 72 \times 60$ , TR = 3 seconds, saturation time = 1.6 seconds, inversion time = 1.14 seconds, cut-off velocity = 7.5 mm/s in the VS pulse train, echo train length = 40 and echo spacing = 2.5 ms in the fast SE readout, and k-space subsampling factor = 3.3, yielding a scan time of 3.3 minutes. A high-resolution  $T_1$ -weighted MP-RAGE scan (Mugler III and Brookeman, 1990) was also performed (1 mm isotropic resolution, scan duration = 5 minutes) for brain segmentation.

Additional data were collected in seven of the 10 study subjects using 3D pseudo-continuous ASL (pCASL) with stack-of-spirals readout (Vidorreta et al., 2017) and  $T_2$ -relaxation under spin tagging (TRUST) (Lu and Ge, 2008) for measuring CBF and whole-brain averaged  $Y_v$ , respectively. Imaging parameters in the pCASL pulse sequence were: FOV =  $240 \times$



$240 \times 120 \text{ mm}^3$ , reconstruction matrix =  $64 \times 64 \times 32$ , slice partial Fourier factor =  $6/8$ , labeling duration = 1.8 seconds, post labeling delay = 1.5 seconds, background suppression with four RF pulses, variable-density spiral-out trajectory with a readout duration of 340 ms, TR = 4 seconds, and measurements = 15 control/tag pairs, acquired in a scan time of 4.5 minutes. Based on a time-of-flight angiogram, the labeling plane was selected individually at a position superior to the carotid bifurcation. Acquisition parameters for TRUST were: FOV =  $230 \times 230 \text{ mm}^2$ , reconstruction matrix =  $64 \times 64$ , phase partial Fourier factor =  $5/8$ , TR = 3 seconds,  $T_2$  preparation times = 0, 40, 80, and 160 ms, and measurements = 3 control/tag pairs, with a scan time of 1.2 minutes.

## 2.4. Data processing and analysis

Unless otherwise stated, all data processing and analysis involving image reconstruction, parameter quantifications, and statistical comparisons were carried out in Matlab custom scripts.

**2.4.1. qBOLD processing**—VS-VSL data were subjected to sparsity-constrained image reconstruction (Lee et al., 2017a), and subsequently to the control/tag image difference divided by the control image, yielding  $CBV_v$  maps. Multi-echo AUSFIDE images, reconstructed by applying a Tukey window and Fourier transform along the  $k_z$ -direction and subsequent in-plane grid-ding, were processed in three steps: 1) estimating  $B_0$  and corresponding VSF (Yablonskiy et al., 2013b), 2) solving Eq. [2] on magnitude images, and 3) QSM reconstruction using the MEDI toolbox (Liu et al., 2012), leading to the maps of  $F_{VSF}$ ,  $S_0$ ,  $\eta$ ,  $R_2$ ,  $R_2'$ ,  $\chi$  as prior information for the qBOLD processing described below. Refer to (Lee and Wehrli, 2020; Lee and Wehrli, 2021) for details in the above process.

Based on the time-course of AUSFIDE images along with the derived preliminary parametric maps, qBOLD parameters were estimated by solving Eq. [6] on a voxel-by-voxel basis using the curve fitting tool-box in Matlab. In the optimization procedure, initial values (indicated by subscript 0) for the unknown parameter set,  $\theta = \{Y_v, \zeta, \chi_{nb}, R'_{2,nh}\}$ , was determined as follows:  $Y_{v,0}$  was set equal to  $Y_v$  in large draining veins ( $Y_{v,s}$ ; superior sagittal sinus and straight sinus), derived from measured  $\chi$  in the respective regions. To this end, Eq. [7] was solved with  $\alpha = \zeta = 1$  and Hct scaled up by 1.18 (inverse of 0.85 representing the Hct ratio of microvasculature relative to large vessels).  $\zeta_0$  and  $\chi_{nb,0}$  were initialized to  $CBV_v$  and  $\chi$ , respectively. Finally,  $R'_{2,nh,0}$  was computed by subtracting  $\zeta_0 \delta_\omega$  from measured  $R_2'$  lower and upper bounds of the solutions were restricted to:  $10\% Y_v - 90\%$ ,  $0.5\zeta_0 - \zeta - 2\zeta_0$ ,  $0.5R'_{2,nh,0} \leq R'_{2,nh} \leq 2R'_{2,nh,0}$ , and  $-0.1 \text{ ppm} \leq \chi_{nb} \leq 0.2 \text{ ppm}$ .  $Y_a$  was assumed 98%. The regularization parameters  $w$  and  $p$  were empirically determined to 10 and 0.1, respectively. The validity of the selected values for  $w$  and  $p$  is evaluated via L-curve analysis in Supplementary Material.

To investigate the effectiveness of prior information in solving the qBOLD problem, AUSFIDE images acquired in a subject were processed in four different manners such that Eq. [6] was solved with: 1)  $w = p = 0$  and 2)  $w > 0$  and  $p = 0$ , 3)  $w > 0$  and  $p > 0$ , and 4)  $w > 0$  and  $p > 0$  with  $CBV_v$  prior. Thus, processing 1, 2, and 4 represent conventional qBOLD, qBOLD+QSM, and the proposed method, respectively, in terms of utilizing preliminary

parameters (i.e.,  $\chi$ ,  $R_2'$ , and  $CBV_v$ ). In processing 1 – 3, all parameter initialization and solution bounds were identical to those stated above, but  $\zeta_0 = 3\%$ . Resulting maps of  $Y_v$ , DBV, and  $\chi_{nb}$  were qualitatively compared across the four processing scenarios.

**2.4.2. 3D whole-brain CMRO<sub>2</sub> mapping**—Control and tag pCASL images were realigned to the proton-density image ( $M_0$ ) acquired prior to the actual pCASL data collection using SPM12 (Penny et al., 2011), and their pair-wise difference was averaged over multiple measurements, yielding SI. Subsequently, CBF was computed on a voxel-by-voxel basis using the following equation (Alsop et al., 2015):

$$CBF(\text{ml}/100\text{g}/\text{min}) = \frac{3000 \cdot \lambda \cdot \Delta SI \cdot e^{\frac{PLD}{T_{1,b}}}}{\beta \cdot T_{1,b} \cdot M_0 \cdot \left(1 - e^{\frac{\tau}{T_{1,b}}}\right)} \quad (9)$$

where  $\lambda$  is the blood-brain partition coefficient (0.9 ml/g (Herscovitch and Raichle, 1985)),  $T_{1,b}$  is the  $T_1$  of arterial blood at 3 T (1.65 seconds (Lu et al., 2004)), PLD is the post labeling delay,  $\tau$  is the labeling duration, and  $\beta$  is the labeling efficiency (0.72 (Vidorreta et al., 2013)). Finally, given the CBF measurements along with qBOLD-derived  $Y_v$  across the entire brain, 3D CMRO<sub>2</sub> maps were constructed using Eq. [1] in units of  $\mu\text{mol O}_2$  per 100 g tissue per minute.

**2.4.3. Data analysis**—Brain tissue segmentation was performed based on the  $T_1$ -weighted MP-RAGE images using the FreeSurfer software package (Fischl, 2012), yielding the following six regions-of-interests (ROIs): cerebral cortex (cortical gray matter (GM)), cerebral white matter (WM), thalamus, pallidum, putamen, and caudate. Then, the MP-RAGE images along with the segmentation maps were coregistered to the first echo of SSFP-FID images, leading to ROI analysis of the parameters quantified in the preliminary ( $CBV_v$ ,  $R_2$ ,  $R_2'$ ,  $\chi$ ) and qBOLD processing (DBV,  $Y_v$ ,  $R_{2,nh}$ ,  $\chi_{nb}$ ) steps computing regional averages (mean  $\pm$  SD) across the 10 study subjects. Furthermore, correlation between the two parameter estimates,  $R_{2,nh}$  and  $\chi_{nb}$ , in the six ROIs was evaluated using linear regression.

Measured  $Y_v$ , CBF, and CMRO<sub>2</sub> were averaged over cortical GM and WM voxels in the seven study subjects and tabulated. Additionally, TRUST data in each subject were processed via the following steps: 1) taking difference between control and tag images at the four  $T_2$  preparation times, 2) fitting the difference signals in the superior sagittal sinus with respect to  $T_2$ , and 3) converting  $T_2$  to  $Y_v$  using the calibration curve provided in (Lu et al., 2012). The resulting global  $Y_v$  value was compared with whole-brain averaged  $Y_v$  obtained in the proposed qBOLD method using two-tailed, paired  $t$ -test.

### 3. Results

#### 3.1. Numerical simulations

Fig. 2 shows MAE of  $R_2$  (Fig. 2a),  $R_2'$  (Fig. 2b),  $Y_v$  (Fig. 2c), and DBV (Fig. 2d) estimates with increasing noise SD from  $-7$  to  $-4$  (natural log scale), obtained using SSFP-FID signals

only, and using entire AUS-FIDE signals without and with  $CBV_v$  prior information. Over the entire range of noise levels, the  $R_2^*$ -based parameter estimation with SSFP-FID yielded substantially greater measurement errors than the  $R_2'$ -based approaches using AUSFIDE. Furthermore, in the presence of  $CBV_v$  prior the estimation errors of  $Y_v$ , and DBV in the AUSFIDE qBOLD method were substantially reduced, thus suggesting the need of prior knowledge of  $CBV_v$  in qBOLD parameter mapping.

Fig. 3 plots MAE of  $Y_v$  (Fig. 3a), DBV (Fig. 3b),  $\chi_{nb}$  (Fig. 3c), and  $R'_{2,nh}$  (Fig. 3d), obtained via the AUSFIDE-based qBOLD parameter estimation with respect to a bias in the  $CBV_v$  prior ranging from  $-40\%$  to  $40\%$ , comparing three different approaches to solving Eq. [6]: 1)  $w = p = 0$ , 2)  $w > 0, p = 0$ , and 3)  $w > 0, p > 0$ . In all parameters but DBV, estimation errors in case 1 across the given error range of  $CBV_v$  are considerably larger than those predicted with the other two methods applying either constraints (i.e.,  $\chi$  or  $R_2'$ ). The proposed approach (case 3), when compared with case 2, further reduces estimation errors of  $Y_v$  and  $R'_{2,nh}$ , implying the effectiveness of constraining  $R_2'$  additionally to  $\chi$  in solving the qBOLD problem.

### 3.2. Experiments and analysis

Fig. 4 compares four sets of  $Y_v$ , DBV, and  $\chi_{nb}$  maps for which preliminary estimates are utilized in four different ways in solving Eq. [6]: no constraints ( $w = p = 0$ ; Figs. 4a, 4e, 4i),  $\chi$ -constrained only ( $w > 0, p = 0$ ; Figs. 4b, 4f, 4j), both  $\chi$  and  $R_2'$  constrained ( $w > 0, p > 0$ ; Figs. 4c, 4g, 4k), and both  $\chi$  and  $R_2'$  constrained and inclusion of a  $CBV_v$  prior (Figs. 4d, 4h, 4l). Quantification without constraining any prior information (i.e., conventional qBOLD) results in physiologically implausible values in many voxels of all three parameter maps (Figs. 4a, 4e, 4i). Compared to conventional qBOLD, employing  $\chi$  information (i.e., qBOLD+QSM) leads to the expected  $\chi_{nb}$  contrast (e.g., basal ganglia versus cortex; Fig. 4j), but no noticeable improvements in  $Y_v$  and DBV maps (Figs. 4b, 4f). With an additional application of  $R_2'$  constraint,  $Y_v$  estimation is substantially stabilized yielding relatively uniform spatial distribution (Fig. 4c), but at the expense of physiologically unrealistic, nearly homogeneous DBV map (Fig. 4g). However, the proposed method, which makes full use of available prior knowledge ( $\chi, R_2', CBV_v$ ), appears to improve DBV estimation (Fig. 4h) depicting some level of contrast between GM and WM as is the case in physiology (Leenders et al., 1990).

Fig. 5 shows whole-brain 3D maps of  $Y_v$  (Fig. 5b), DBV (Fig. 5c),  $R'_{2,nh}$  (Fig. 5d), and  $\chi_{nb}$  (Fig. 5e) in the sagittal, coronal, and axial planes in two representative subjects, obtained using the proposed qBOLD method, along with the corresponding sectional images of T<sub>1</sub>-weighted MP-RAGE on which six color-coded ROIs are overlaid (Fig. 5a). All parametric maps exhibit the physiologically expected contrast, i.e., nearly uniform  $Y_v$ , higher DBV in cortical GM relative to WM, and distinction of  $R'_{2,nh}$  in the basal ganglia, including caudate, putamen, and pallidum, versus cortical regions, in parallel with  $\chi_{nb}$  estimates. Table 2 lists group averages ( $N = 10$ ; mean  $\pm$  SD) of the eight parameters pertinent to the proposed qBOLD processing: four preliminaries ( $CBV_v, R_2, R_2', \chi$ ) and four resultants (DBV,  $Y_v, R'_{2,nh}, \chi_{nb}$ ). In all ROIs, qBOLD yielded elevated DBV and decreased  $R'_{2,nh}$  and  $\chi_{nb}$  compared to their corresponding priors,  $CBV_v, R_2',$  and  $\chi$ . Fig. 6 displays a scatter plot

of regional averages  $R'_{2,nh}$  against  $\chi_{nb}$  across the six ROIs in the ten study subjects ( $r = 0.7$ ,  $p < 0.001$ ), suggesting the expected relationship between the two parameters.

Fig. 7 displays whole-brain 3D images in the three orthogonal planes in two study subjects:  $T_1$ -weighted magnitude (Fig. 7a), and CBF (Fig. 7b),  $Y_v$  (Fig. 7c), and  $CMRO_2$  (Fig. 7d) maps. Consistent with the results in Fig. 5,  $Y_v$  obtained using the proposed qBOLD method is largely invariable across the entire brain. In contrast, CBF maps high-light GM/WM differences, thereby contributing predominantly to the contrast of the derived  $CMRO_2$  maps. Table 3 compares TRUST's global  $Y_v$  against the proposed method's  $Y_v$  averaged across the entire brain voxels in the seven study volunteers, and summarizes individual averages of both CBF and  $CMRO_2$  estimates in cortical GM and WM regions, respectively. Two-tailed, paired  $t$ -test suggests that the difference of whole-brain average  $Y_v$  values in TRUST and the proposed method is not statistically significant ( $p = 0.98$ ).

#### 4. Discussion and conclusion

This work introduces a new, MRI-based, regional oximetry technique by means of 3D qBOLD parameter mapping. At the core of the present qBOLD method is the AUSFIDE pulse sequence that enables rapid, high-resolution 3D scanning for the full brain while providing prior information of voxel-averaged magnetic susceptibility ( $\chi$ ) and associated parameters at different scales ( $R_2, R'_2, B_0$ ), which is difficult to achieve with the currently practiced 2D  $R'_2$ -based qBOLD (Stone and Blockley, 2017) as well as 3D  $R_2^*$ -based approaches (Cho et al., 2018; Ulrich and Yablonskiy, 2016). Furthermore, the proposed qBOLD model (Eq. [6]) decomposes both  $\chi$  and  $R'_2$  into dHb and non-dHb contributions, and constrains their respective estimates for stabilizing the solution process. In combination, along with additional, rapid  $CBV_v$  mapping, the proposed method achieves separation of several sources that complicate a voxel signal decay, i.e., 1)  $R_2^*$  being resolved into  $R_2$  and  $R'_2$ , 2)  $R'_2$  being separated into heme iron ( $R'_{2,h}$ ) and non-heme iron ( $R'_{2,nh} \propto \chi_{nb}$ ) contributions, and 3)  $R'_{2,h}$  being solved into DBV and  $Y_v$ , with all being relatively insensitive to macroscopic-scale magnetic field variations.

The group-averaged DBV values obtained using the proposed method (Table 2), while physiologically plausible (e.g., 2.8 % and 1.8 % for cortical GM and WM), differ from some of those in the literature. Indeed, different qBOLD methods, including the conventional approach (He and Yablonskiy, 2007), qBOLD+QSM (Cho et al., 2018), and Bayesian qBOLD (Cherukara et al., 2019), have so far reported disparate DBV estimates, ranging from 1.8 %, 4.5 %, up to 7.0 % for GM, which indicates that qBOLD parameter mapping is generally prone to error. Nonetheless, the DBV values found in this work agree well with those (3.1 % and 2.0 % for GM and WM) obtained via an interleaved qBOLD method (Lee et al., 2018), which also employs prior knowledge of unknown parameters, albeit being limited to 2D single-slice quantification. Hence, in the framework of prior-guided qBOLD, the proposed technique is expected to be reproducible to some extent, warranting further validation studies.

In this study, the DBV estimates are higher than their  $CBV_v$  counterparts consistently across all six ROIs by approximately 30 – 50 % (Table 2). Ideally, higher DBV values

relative to  $CBV_v$  are expected, because DBV should represent the portion of deoxygenated blood across the entire blood vessels in a voxel while  $CBV_v$  only captures post-capillary venules and downstream blood thereafter. Additionally,  $CBV_v$  itself may also have been underestimated due to the following two limitations inherent to VS-VSL: 1) post-capillary venular blood (which flows more slowly than the set cutoff velocity of the VS block), may not have been fully captured, and 2) the simplified  $CBV_v$  estimation model, which assumes equal  $T_1/T_2$  relaxation times between brain tissues and venous blood, can lead to errors by up to 45 % according to the authors' prior analysis (Lee and Wehrli, 2020). Despite the above sources of systematic underestimation, the  $CBV_v$  estimates obtained here clearly distinguish GM from WM regions, and serve as an effective initializer for DBV quantification (Fig. 4g vs. Fig. 4h), thus suggesting the need for providing  $CBV_v$  as prior information and updating it to DBV in the qBOLD processing. Alternatively, quantifying  $Y_v$  from separate measurements and providing the values to the qBOLD problem might be considered. However, methods based on venous blood  $T_2$  mapping (Bolar et al., 2011; Guo and Wong, 2012), the only feasible alternative to qBOLD for voxelwise measurements of baseline  $Y_v$  in the microvasculature, would require impractically long scan times. In fact, the need for repeated scans with a range of  $T_2$  preparation times is one possible reason that has limited their extension to 3D  $Y_v$  quantifications. Additionally, it has been numerically and experimentally shown that preliminary estimation of  $Y_v$ , when compared to the DBV prior ( $CBV_v$ ), is less efficient in stabilizing the qBOLD problem (Lee et al., 2018).

The regional averages of AUSFIDE-derived preliminary parameters ( $R_2$ ,  $R_2'$ , and  $\chi$ ; Table 2) are consistent with those reported in our previous study (Lee and Wehrli, 2021). Furthermore, the  $\chi_{nb}$  values obtained in this study agree well with those reported in the qBOLD+QSM paper ( $-0.02 \pm 0.004$  ppm and  $-0.019 \pm 0.004$  ppm for cortical GM and WM) (Cho et al., 2018). However, to the best of the authors' knowledge, no  $R_{2,nh}'$  have been published elsewhere. Nevertheless, the measured  $R_{2,nh}'$  shows clear distinction across different brain territories (Fig. 5d and Table 2) while presenting the expected, strong correlation with  $\chi_{nb}$  (Fig. 6), with the elevated values in the iron-rich, deep brain structures relative to cortical GM and WM areas. Furthermore, both  $R_{2,nh}'$  and  $\chi_{nb}$  estimates in Table 2 are smaller than their corresponding priors,  $R_2'$  and  $\chi$ , across all six ROIs. The respective mean differences ranging from 1.5 to 2.3  $s^{-1}$  and from 0.011 to 0.014 ppm are plausible according to Eq. [8] and Eq. [7], thus suggesting that dHb-induced modulations of RF-reversible transverse relaxation rate and magnetic susceptibility have been correctly extracted from the qBOLD processing.

The group-averaged whole-brain  $Y_v$  obtained via the proposed qBOLD method (62.2 %; Table 3) is in good agreement with values obtained by TRUST (62.1 %; Table 3). When assuming  $Y_a \sim 98$  %, one obtains a mean OEF of 36.5 %, which is consistent with values reported for a range of imaging modalities: Dual-calibrated fMRI: 35 % (Gauthier and Hoge, 2012) and 38 % (Bulte et al., 2012), other qBOLD MRI techniques: 38.3 % (He and Yablonskiy, 2007) and 39.3 % (Cho et al., 2018), as well as PET-based measurements: 35.7 % (Perlmutter et al., 1987) and 30 – 40 % (Raichle et al., 2001). Given the nearly uniform spatial distribution of  $Y_v$ ,  $CMRO_2$  contrast in the normal brain is largely driven by CBF (Fig. 7). The group average of the  $CMRO_2$  estimates in cortical GM ( $134.2 \pm$

21.1  $\mu\text{mol}/100\text{ g}/\text{min}$ ; Table 3) also agrees well with the values measured by means of dual-calibrated fMRI:  $145 \pm 30$  (Gauthier and Hoge, 2012) and  $155 \pm 39$  (Bulte et al., 2012), and  $^{15}\text{O}$  PET:  $133 \pm 20$  (Ito et al., 2004) and 128 – 144 (Leenders et al., 1990), all in units of  $\mu\text{mol}/100\text{ g}/\text{min}$ . In WM, on the other hand, the mean  $\text{CMRO}_2$  of  $79.4 \pm 12.6\ \mu\text{mol}/100\text{ g}/\text{min}$  (Table 3) is somewhat higher than the values obtained via  $^{15}\text{O}$  PET:  $57 \pm 10\ \mu\text{mol}/100\text{ g}/\text{min}$  (Leenders et al., 1990) and  $62 \pm 11\ \mu\text{mol}/100\text{ g}/\text{min}$  (Hatazawa et al., 1995). The discrepancy has likely resulted from CBF measurement errors because with current ASL techniques it is challenging to achieve accurate CBF mapping for WM region (Alsop et al., 2015). In fact, some of WM voxels presented negative CBF values, and thus were excluded in the statistical analysis of this study.

A close look at Fig. 4 suggests that the  $R_2'$  constraint acts as a strong smoothing operator for both  $Y_v$  (Fig. 4b versus Fig. 4c) and DBV (Fig. 4f versus Fig. 4g) maps. The results may also imply that constraining measured  $R_2'$  has compromised the sensitivity of the original qBOLD model to DBV. Nonetheless, additionally measured  $\text{CBV}_v$  serves as an initializer for DBV (Fig. 4h), suggesting that it has complemented the model's limited sensitivity. However, it is uncertain whether that is the case for  $Y_v$  as  $Y_v$  is well-known to be rather homogeneous in healthy brains. Therefore, further investigation would be needed to ascertain the effect of regularization on  $Y_v$  estimation, particularly in the brain where  $Y_v$  is regionally altered, for example, due to ischemic lesions. A validation study that can be performed before testing on patients would be experiments with gas-breathing challenges, in which relative to baseline,  $Y_v$  alteration is expected in response to gas mixtures (e.g., hyperoxia and hypercapnia).

Several studies (Dickson et al., 2010; Dickson et al., 2011; Stone et al., 2019) have shown that the static dephasing regime is not valid for small vessels (approximately  $<30\ \mu\text{m}$ ) where the effect of water diffusion becomes significant. Furthermore, the diffusion-induced signal modulation is dependent on data sampling time, being relatively higher for echoes collected after the refocusing RF pulse compared to FID samples (Dickson et al., 2010; Dickson et al., 2011). As a result, the GESFIDE/GESSE methods under the static dephasing regime are potentially prone to systematic errors in qBOLD parameter estimation. The AUSFIDE pulse sequence acts similar to the GESFIDE data acquisition in that it samples time-courses of FID (SSFP-FID) and RF-refocused signal (SSFP-ECHO) until before a SE point. Hence, one could expect that the proposed qBOLD method, which does not take the diffusion effect into account in the signal model, would cause systematic errors comparable to those in GESFIDE in the very small vessel regime. Nevertheless, since in AUSFIDE steady-state signals following a number of spin pathways contribute to SSFP-FID and SSFP-ECHO, the effect of water diffusion is complicated by spin history, making it difficult to predict to what extent the present qBOLD mapping is affected. This is an issue that would need further scrutiny, possibly via simulations accounting for water diffusion in the AUSFIDE signal model.

It has been shown that  $R_2$  also presents a dependence on blood oxygenation levels, manifesting itself as a significant BOLD contributor (Kida et al., 2000). In fact, blood oximetry relies on the measurement of  $R_2$  (Wright et al., 1991), and some techniques for the quantification of brain iron make use of the modulation of  $R_2$  via diffusion in microscopic

induced fields from brain iron stores (Vymazal et al., 1996). Given these prior studies, our quantification model can be expanded such that an additional constraint is added to enforce measured  $R_2$  to the sum of heme and non-heme contributions. Here, a calibration model relating blood  $R_2$  (heme-originated  $R_2$ ) to  $Y_v$  could be employed. The additional  $R_2$  constraint may help the present method further enhance sensitivity to the qBOLD parameters. On the other hand, this approach adds one more parameter (non-heme-related  $R_2$ ) to the solution set as well as one more regularization parameter to be determined, and thus would result in increased computational complexity. Additionally, quantification errors may be propagated from the employed  $R_2$ - $Y_v$  calibration model. Given the above considerations, the impact of additional  $R_2$  constraint on the qBOLD parameter estimation would need to be investigated in future studies.

The qBOLD model in this study does not account for signal contributions from extracellular fluid or intravascular compartments. Compared to the extravascular tissues, intravascular venous blood contribution to baseline AUFIDE signals remains close to noise levels, because of its relatively low  $T_2/T_1$  ratio and small DBV. By contrast, signal contribution from the extracellular space would not be insignificant, considering the fact that interstitial fluid and cerebrospinal fluid present a high  $T_2/T_1$  ratio. Additionally, an offset frequency of the extracellular fluid may result in modulation of the signal decay. Given the above considerations, it appears desirable to account for the extracellular compartment in the AUFIDE-based qBOLD analysis. Nevertheless, it would need further scrutiny whether the qBOLD mapping benefits from the inclusion of additional signal sources relative to increased complexity and potential errors resulting from an accordingly increased number of fitting parameters.

The present 3D qBOLD method may find further improvements in data acquisition, modeling, and data processing. First, data collection for AUFIDE and VS-VSL, currently separated, may be integrated into one single pulse sequence by inserting the AUFIDE component into the long dead time in VS-VSL ( $\sim 1.65$  seconds; Fig. 1b) in a segmented manner. Doing so would break down the steady-state nature of the AUFIDE data, which, however, should not alter the signal time-course along echoes within each TR, and thus would not penalize qBOLD analysis. Second, the current qBOLD model may be expanded to account for multiple compartments in WM (e.g., myelin water) and local frequency shift (and thus  $R_2'$ ) depending on the fiber orientation relative to  $B_0$  (Lee et al., 2017b). Since the multi-echo AUFIDE data can also be utilized for myelin water fraction mapping (Alonso-Ortiz et al., 2015), the information from the procedure may serve as additional prior information to address such confounders in WM qBOLD mapping. Finally, while the stack-of-stars trajectory in the current implementation of AUFIDE makes it relatively insensitive to physiologic bulk fluid motion (Lee and Wehrli, 2021), it is still sensitive to subject's involuntary head movements. Full 3D radial encoding can be considered as an alternative, which enables data-driven detection and correction of large-scale head motion (Lee et al., 2020) as well as isotropic spatial resolution of quantified parameter maps, albeit at the cost of increased scan times.

In conclusion, we introduced a new, noninvasive, MRI-based approach to mapping resting-state brain oxygen metabolism by means of prior information guided 3D qBOLD. The

AUSFIDE data acquisition strategy permits rapid 3D qBOLD scanning and preliminary parameter estimation ( $R_2$ ,  $R_2'$ ,  $\chi$ ,  $B_0$ ), and constraining prior information ( $R_2'$ ,  $\chi$ ,  $CBV_v$ ) to the parent qBOLD model is effective in stabilizing the qBOLD problem, leading to expected contrast of all measured parameters across brain territories. Although results suggest feasibility of the AUSFIDE-based qBOLD technique as a practical means to measuring brain oxygen utility, the method would benefit from further validation in terms of modeling (i.e., assumption of static dephasing regime and inclusion of extracellular compartment as discussed above) and its sensitivity to focal abnormalities in which tissue oxygen metabolism is regionally altered, for example, due to arterial stenosis/occlusion.

## Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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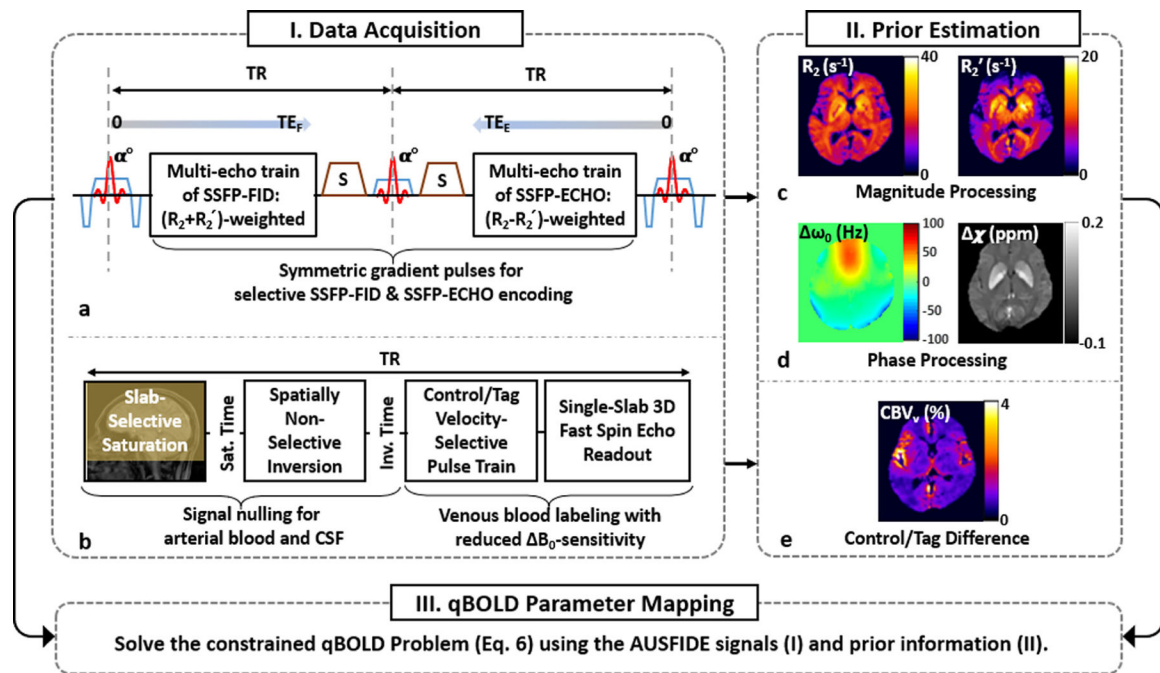
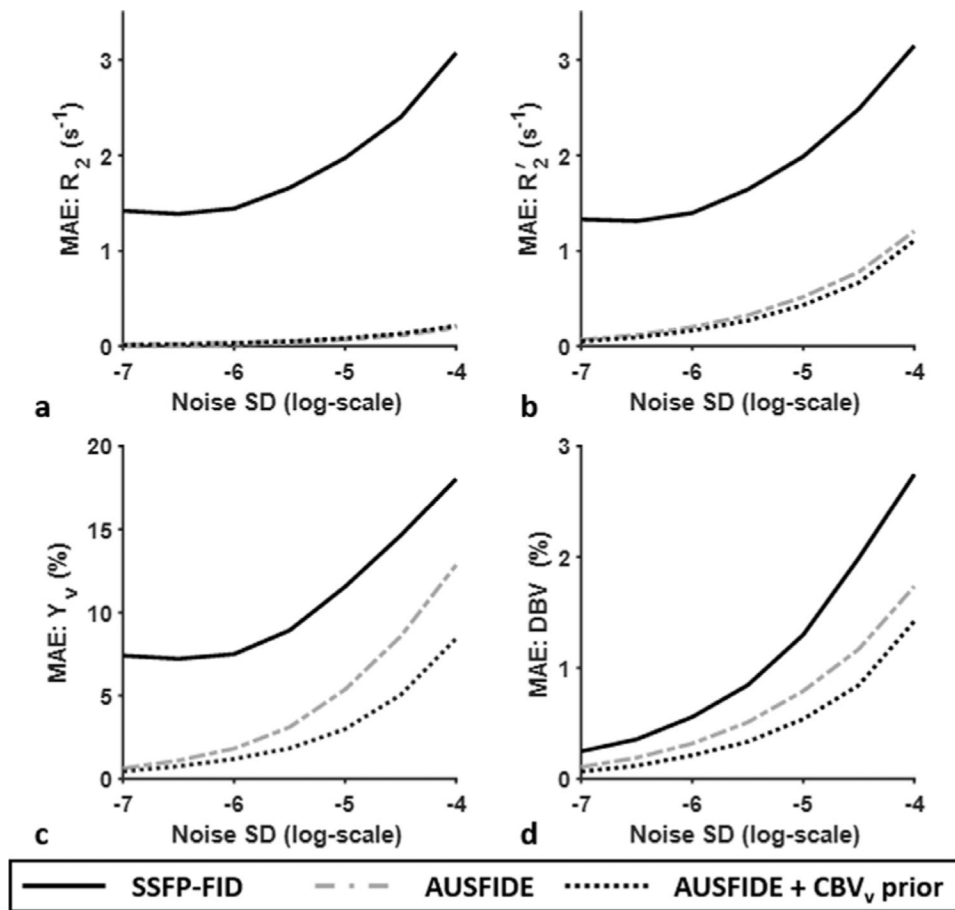
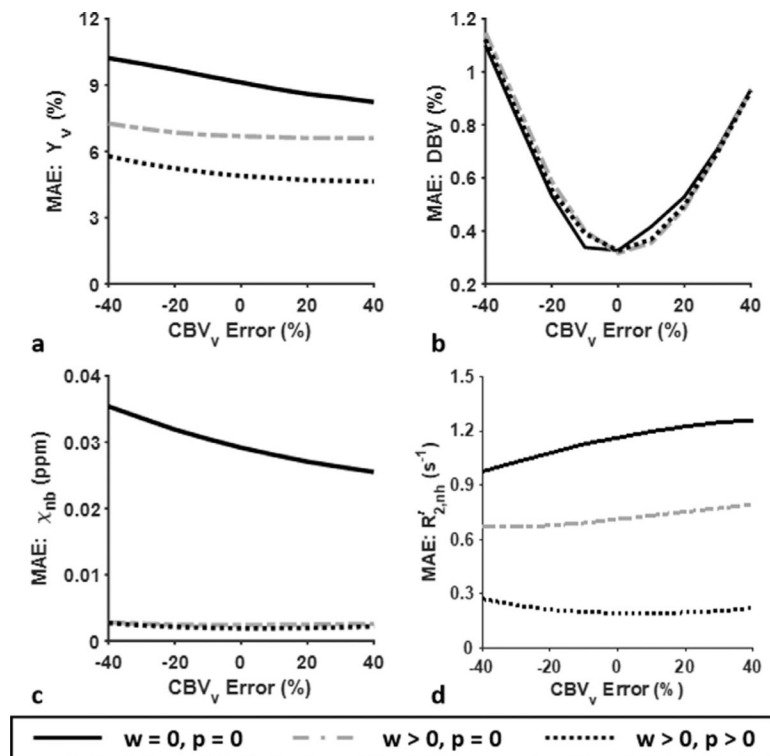


Fig. 1.

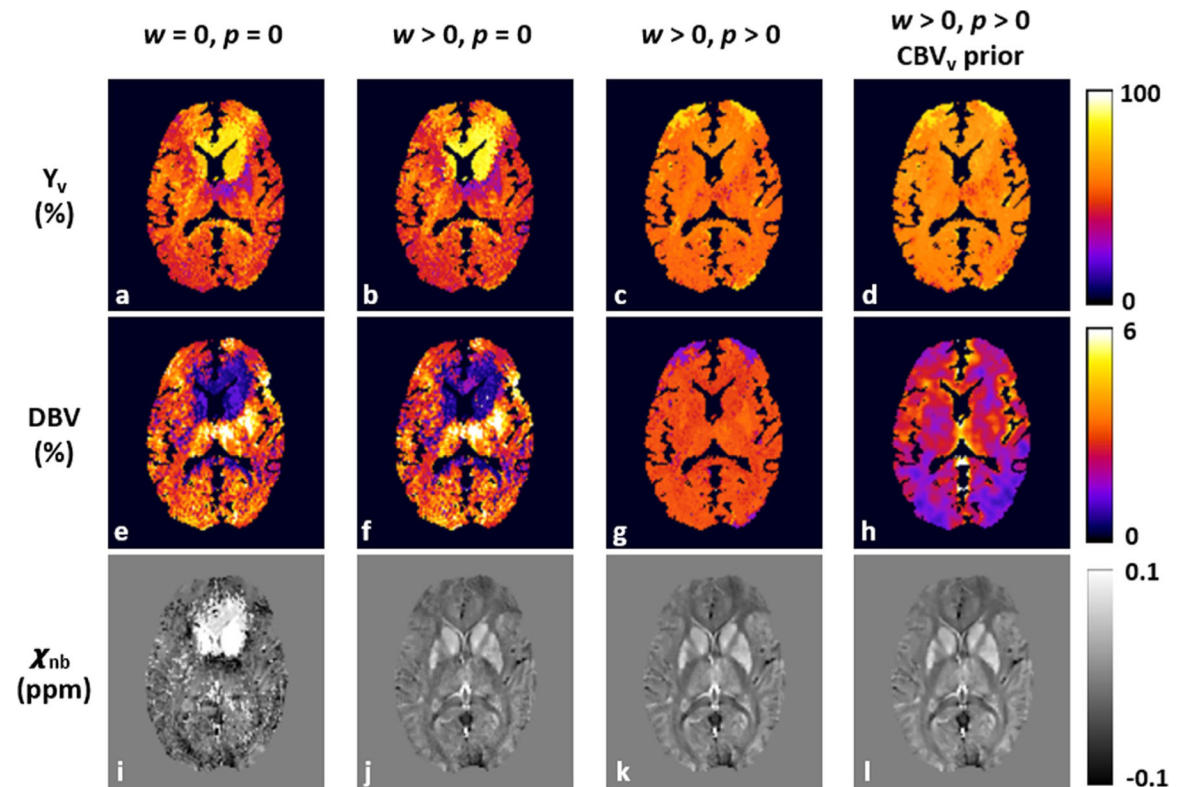
Schematic of the proposed, three-step quantification of qBOLD parameters. Step I. Data acquisition: Imaging data are collected in two separate scans using ‘Alternating Unbalanced Steady-state-free-precession (SSFP) Free-Induction-Decay and Echo (AUSFIDE)’ (a) and ‘Velocity-Selective Venous-Spin-Labeling (VS-VSL)’ (b) pulse sequences. In AUSFIDE, the SSFP-FID and SSFP-ECHO modules alternate with each other across the entire pulse train while sampling multiple echoes decaying with rate constants  $R_2+R_2'$  and  $R_2-R_2'$ , respectively. The VS-VSL method achieves  $B_0$ -resistant, selective labeling of venous blood by applying saturation, inversion, and VS modules sequentially before 3D fast spin-echo readout. Step II. Prior estimation: The AUSFIDE data are processed in magnitude and phase, leading to maps of  $R_2$  and  $R_2'$  (c) and  $\omega_0 (= \gamma B_0)$  and  $\chi$  (d), respectively, while the difference between control and tag VS-VSL images approximates  $CBV_v$  (e). Step III. qBOLD parameter mapping: Given acquired time-series AUSFIDE images and preliminary parametric maps derived therefrom, along with  $CBV_v$  prior information, the constrained nonlinear inverse problem in Eq. [6] is solved, yielding solutions for qBOLD parameters ( $DBV$  and  $Y_v$ ) and nonblood contributions to  $R_2'$  and  $\chi$  (see main text for details).



**Fig. 2.** Simulated maximum absolute error (MAE) of  $R_2$  (a),  $R_2'$  (b),  $Y_v$  (c), and DBV (d) estimation with increasing noise levels from  $-7$  to  $-4$  (natural log scale), obtained by solving Eq. [5] 10,000 times independently using the SSFP-FID portion of AUSFIDE signals (mimicking  $R_2^*$ -based qBOLD) and the entire AUSFIDE dataset without and with prior information for DBV (i.e.,  $CBV_v$  prior), respectively. See main text for detailed simulation setting. Compared with the  $R_2^*$ -based qBOLD approach with SSFP-FID, the  $R_2'$ -based method with AUSFIDE yields superior performance for all parameter quantifications (solid versus dash-dotted lines). Note further enhancement of measurement accuracy in  $Y_v$  and DBV with prior knowledge of  $CBV_v$  (dotted lines).

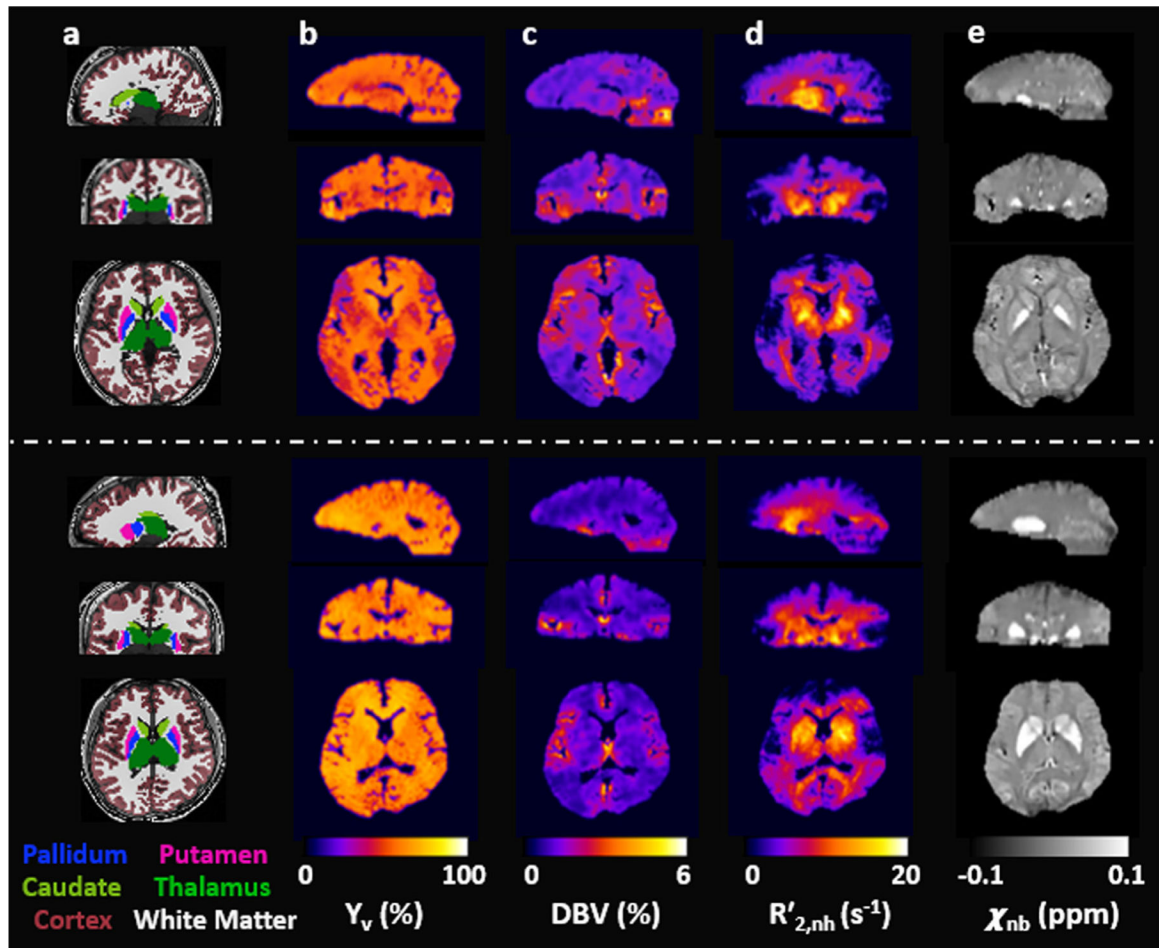


**Fig. 3.** MAE of the estimated  $Y_v$  (a), DBV (b),  $\chi_{nb}$  (c), and  $R'_{2,nh}$  (d) in AUSFIDE-based qBOLD with varying  $CBV_v$  errors ranging from  $-40\%$  to  $40\%$ , obtained by solving Eq. [6] with three different combinations of the regularization parameters: 1)  $w = p = 0$ , 2)  $w > 0$  but  $p = 0$ , and 3)  $w > 0$  and  $p > 0$ , simulating conventional qBOLD, qBOLD+QSM, and the proposed qBOLD processing, respectively. Measurement SNR of 140 was assumed. See main text for further details in the simulations. All three cases yield comparable level of DBV estimation error (b). However, when compared to conventional qBOLD (solid lines), measurement accuracy of the remaining three parameters (a, c, d) is substantially increased with qBOLD+QSM (dash-dotted lines). Note also that MAE of  $Y_v$  and  $R'_{2,nh}$  is further reduced with the proposed method (dotted lines).

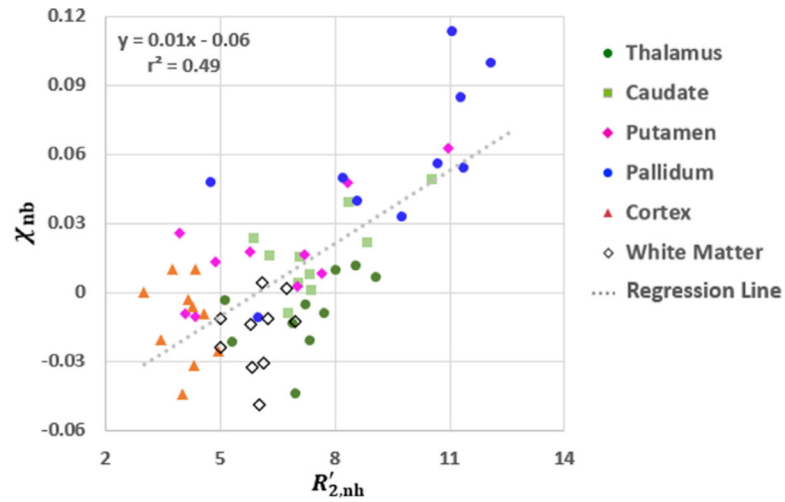


**Fig. 4.** Parametric maps of  $Y_v$  (a-d), DBV (e-h), and  $\chi_{nb}$  (i-l) in an axial plane of a representative study subject, obtained by solving Eq. [6] in four different ways of using prior information: no constraints applied ( $w = p = 0$ ; first column),  $\chi$ -only constrained ( $w > 0, p = 0$ ; second column), both  $\chi$ - and  $R_2'$ -constrained ( $w > 0, p > 0$ ; third column), and both constraints applied with  $CBV_v$  prior (fourth column), representing conventional qBOLD, qBOLD+QSM, and the proposed qBOLD processing without and with prior knowledge of  $CBV_v$ , respectively. In the absence of any priors, all resultant maps exhibit artifactual values in many voxels (first column). The addition of  $\chi$  and  $R_2'$  constraints significantly stabilizes the qBOLD problem, leading to physiologically plausible contrast of  $\chi_{nb}$  (i versus j) and  $Y_v$  (b versus c) maps, respectively, results consistent with the simulations in Fig. 3c and Fig. 3a. Nonetheless, the DBV map is nearly flat (g), which contradicts physiology. However, by using  $CBV_v$  prior information in addition to both constraints, the proposed method yields expected contrast in all parameter maps (last column).

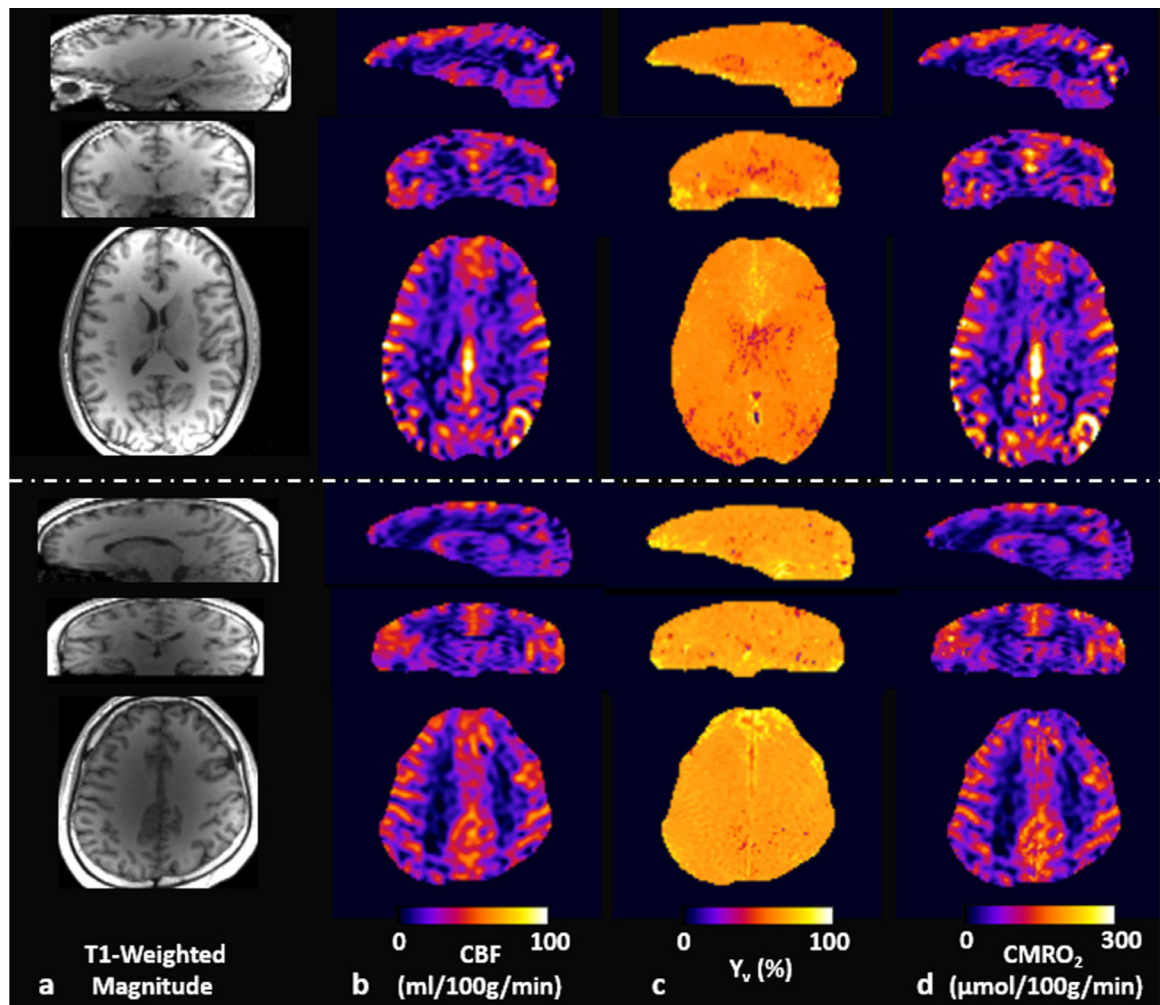




**Fig. 5.** Five columns of whole-brain 3D images in the three orthogonal planes in two representative study subjects. a: color-coded six regions-of-interests (ROIs) overlaid onto T<sub>1</sub>-weighted MP-RAGE images. b-e: Quantitative maps of  $Y_v$ , DBV,  $R'_{2,nh}$  and  $\chi_{nb}$ , obtained using the proposed qBOLD method. Note that all parameter maps depict expected contrast across brain territories, i.e., near-uniform distribution of  $Y_v$  (b), distinction between cortical gray and white matter in DBV (c), and highlighted deep brain structures in both  $R'_{2,nh}$  (d) and  $\chi_{nb}$  (e).



**Fig. 6.** Correlation between  $R'_{2,nh}$  and  $\chi_{nb}$ , quantified in the six ROIs (Fig. 5a) across 10 study participants. Each symbol represents a regional average in each subject. The linear regression (dotted line) is statistically significant ( $p < 0.001$ ), and the resultant equation along with  $r^2$  value is provided at the top-left corner. Parameter estimates in deep brain structures (caudate, putamen, pallidum) present overall high values extending over a wide range of values across subjects.



**Fig. 7.**

Whole-brain 3D images of two representative subjects in sagittal (top row), coronal (middle row), and axial (bottom row) planes. a: T<sub>1</sub>-weighted magnitude images, b: pCASL-derived CBF maps, c: Y<sub>v</sub> maps obtained via the proposed qBOLD method, and d: CMRO<sub>2</sub> maps computed by using the maps in b and c. Note that the CMRO<sub>2</sub> contrast, being physiologically plausible between gray and white matter regions, is largely determined by CBF measurements because of the relatively homogenous Y<sub>v</sub> across the brain.

Table 1

A list of symbols used in this paper and their definitions. Values for the known or assumed parameters are provided in corresponding parentheses.

Measured/ Derived	Symbols (units)	Descriptions
	$C_a$ ( $\mu\text{mol/ml}$ )	Oxygen carrying capacity of arterial blood
	CBF (ml/100 g/min)	Cerebral blood flow
	$Y_v$ (%)	Hemoglobin oxygen saturation level of venous blood
	CMRO <sub>2</sub> ( $\mu\text{mol}/100 \text{ g}/\text{min}$ )	Cerebral metabolic rate of oxygen
	CBV <sub>v</sub> (%)	Venous cerebral blood volume
	$\zeta$ (%)	Deoxygenated blood volume (DBV)
	$R_2$ ( $\text{s}^{-1}$ )	RF-irreversible transverse relaxation rate
	$R_2'$ ( $\text{s}^{-1}$ )	RF-reversible transverse relaxation rate
	$R_{2,h}'$ ( $\text{s}^{-1}$ )	Heme-originated portion of $R_2'$
	$R_{2,nh}'$ ( $\text{s}^{-1}$ )	Non-heme-originated portion of $R_2'$
	$\chi$ (ppm)	Voxel-averaged magnetic susceptibility
	$\chi_{\text{nb}}$ (ppm)	Magnetic susceptibility of non-blood tissue
	$B_0$ (T)	Macroscopic magnetic field inhomogeneity
	$S_0$	Baseline steady-state signal level of SSFP-FID
	$\eta$	Signal ratio of SSFP-ECHO to SSFP-FID at TE = 0
	$\delta_{\omega}$ (Hz)	Characteristic frequency due to magnetic susceptibility of deoxygenated blood relative to surrounding tissue
Known/Assumed	Hct	Blood hematocrit level
	$Y_a$ ( $\sim 98\%$ )	Hemoglobin oxygen saturation level of arterial blood
	$\chi_0$ ( $\sim 3.393$ ppm)	Difference in magnetic susceptibility between fully oxygenated and fully deoxygenated red blood cells
	$\chi_{\text{oth}}$ ( $\sim -0.813$ ppm)	Magnetic susceptibility of oxygenated hemoglobin
	$\chi_p$ ( $\sim -0.038$ ppm)	Magnetic susceptibility of blood plasma
	$\gamma(2.675 \times 10^8 \text{ radian/s/T})$	Gyromagnetic ratio for water proton
	$B_0$ (2.89 T)	Static magnetic field strength
	$\alpha$ ( $\sim 0.77$ )	Volume fraction of venous blood relative to total blood
	$\lambda$ ( $\sim 0.9 \text{ ml/g}$ )	Blood-brain partition coefficient
	$T_{1,b}$ ( $\sim 1.65 \text{ s}$ )	$T_1$ of arterial blood at 3 T

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Descriptions	Symbols (units)
Efficiency of pseudo-continuous arterial spin labeling	$\beta$ (~ 0.72)
Duration of pseudo-continuous arterial spin labeling	$\tau$ (1.8 s)

Group averages (mean  $\pm$  SD;  $N = 10$ ) of the four preliminary parameters ( $CBV_v$ ,  $R_2$ ,  $R_2'$ , and  $\chi$ ) and the four qBOLD-processed parameters ( $DBV$ ,  $Y_v$ ,  $R_{2, nh}'$ , and  $\chi_{nb}$ ), quantified using the proposed method in the six ROIs (cortical GM, WM, pallidum, putamen, caudate, and thalamus).

Table 2

ROI	Preliminary Parameters				qBOLD-Processed Parameters			
	$CBV_v$ (%)	$R_2$ ( $s^{-1}$ )	$R_2'$ ( $s^{-1}$ )	$\chi$ (ppm)	$DBV$ (%)	$Y_v$ (%)	$R_{2, nh}'$ ( $s^{-1}$ )	$\chi_{nb}$ (ppm)
Cortical GM	2.1 $\pm$ 0.4	13.8 $\pm$ 0.4	5.8 $\pm$ 0.6	0.002 $\pm$ 0.003	2.8 $\pm$ 0.5	64.0 $\pm$ 2.3	4.1 $\pm$ 0.5	-0.012 $\pm$ 0.017
WM	1.3 $\pm$ 0.3	17.6 $\pm$ 0.9	7.5 $\pm$ 0.4	-0.006 $\pm$ 0.003	1.8 $\pm$ 0.4	62.1 $\pm$ 2.8	6.0 $\pm$ 0.6	-0.018 $\pm$ 0.015
Pallidum	1.5 $\pm$ 0.4	21.0 $\pm$ 3.2	11.1 $\pm$ 2.0	0.070 $\pm$ 0.025	2.2 $\pm$ 0.5	58.7 $\pm$ 2.9	9.4 $\pm$ 2.3	0.057 $\pm$ 0.034
Putamen	1.7 $\pm$ 0.4	18.7 $\pm$ 2.2	8.4 $\pm$ 1.9	0.029 $\pm$ 0.014	2.4 $\pm$ 0.5	60.2 $\pm$ 2.8	6.4 $\pm$ 2.1	0.018 $\pm$ 0.022
Caudate	1.7 $\pm$ 0.5	18.6 $\pm$ 2.1	9.9 $\pm$ 0.9	0.031 $\pm$ 0.009	2.6 $\pm$ 0.7	61.7 $\pm$ 3.1	7.6 $\pm$ 1.3	0.017 $\pm$ 0.017
Thalamus	1.7 $\pm$ 0.3	17.0 $\pm$ 1.1	9.3 $\pm$ 1.0	0.003 $\pm$ 0.004	2.4 $\pm$ 0.4	62.0 $\pm$ 2.3	7.2 $\pm$ 1.2	-0.010 $\pm$ 0.016

**Table 3**

Regional means of  $Y_V$ , CBF, and  $CMRO_2$  measurements in seven study subjects.

Subject #	$Y_V$ (%)			CBF		$CMRO_2$	
	TRUST <sup>a</sup>	Proposed qBOLD <sup>b</sup>	WM	Cortical GM	WM	Cortical GM	WM
1	56.0	61.7	25.7	34.7	18.5	111.3	82.1
2	67.4	68.6	18.5	37.6	26.7	105.7	52.7
3	61.7	60.7	26.7	44.0	23.3	131.0	87.4
4	66.2	62.9	23.3	42.8	26.3	134.9	80.5
5	62.2	57.5	26.3	52.1	27.2	174.3	91.9
6	56.7	61.7	27.2	46.1	27.7	135.7	79.9
7	64.6	62.0	27.7	49.9	25.1±3.2	146.5	81.6
Mean±SD	62.1±4.1	62.2±3.1	25.1±3.2	43.9±5.8	25.1±3.2	134.2±21.1	79.4±12.6

<sup>a</sup>The values were measured on the superior sagittal sinus, representing whole-brain global  $Y_V$ .

<sup>b</sup>The values were obtained by averaging voxel  $Y_V$  across the entire brain.

<sup>a,b</sup> p-value from two-tailed, paired t-test: 0.98.