Supporting Information for

The complex rupture evolution behind the long and slow, tsunamigenic 2021 South Sandwich Islands earthquake

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Contents

Tables S1 to S3. 1-D structure models used for calculating the Green's function.

Figure S1. Summary of the empirical Green's function analysis.

Figure S2. Comparison of observed waveforms with synthetic waveforms.

Figure S3. Full snapshots of potency-rate density evolution for Episode 1 and 2.

Figure S4. Full snapshots of potency-rate density evolution for Episode 3.

Figure S5. Full snapshots of potency-rate density evolution for Episode 4.

Figure S6. Comparison of the potency-rate density evolution projected along strike and sub-events identified by previous studies.

Figure S7. The dip angle distribution.

Table S1. 1-D structure around the source used for calculating the Green's function, based on CRUST1.0 model¹

$V_{P}\left(km/s\right)$	V_{S} (km/s)	Density (10 ³ kg/m ³)	Thickness (km)
1.50	0.00	1.02	3.80
5.75	3.20	2.70	3.20
7.10	4.05	3.05	4.80
8.04	4.47	3.32	- (below moho)

Table S2. 1-D structure around the source used for calculating the Green's function, based on CRUST2.0 model²

$V_{P}\left(km/s\right)$	V_{S} (km/s)	Density (10 ³ kg/m ³)	Thickness (km)
1.50	0.00	1.02	3.61
5.00	2.50	2.60	1.70
6.60	3.65	2.90	2.30
7.10	3.90	3.05	2.50
8.15	4.65	3.35	- (below moho)

Table S3. 1-D structure around the source used for calculating the Green's function, based on ak135-F model^{3,4}

$V_{P}(km/s)$	V_{S} (km/s)	Density (10 ³ kg/m ³)	Thickness (km)
1.45	0.00	1.02	3.00
5.80	3.20	2.60	6.70
6.80	3.90	2.92	8.00
8.04	4.48	3.64	- (below moho)

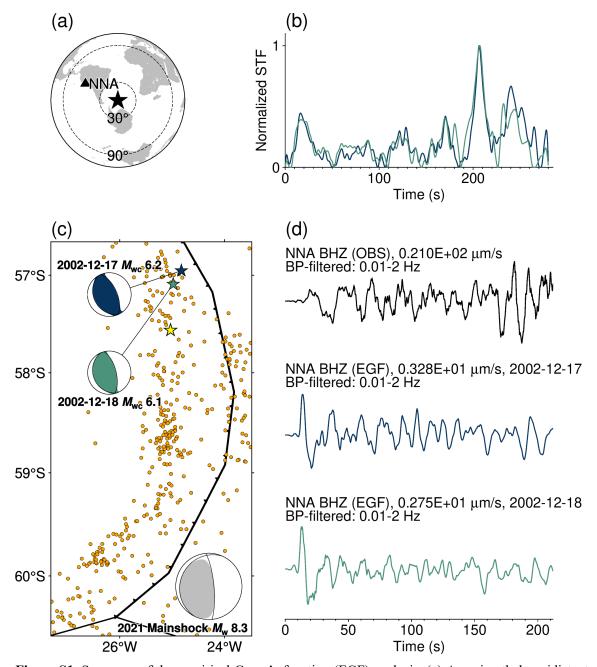


Figure S1. Summary of the empirical Green's function (EGF) analysis. (a) An azimuthal equidistant projection of the location of NNA station. (b) The normalized source time function obtained by using observed waveforms of the 2002-12-17 (blue) and the 2002-12-18 (green) event as EGFs. A band-pass filter of 0.01 to 2 Hz was applied to the observed waveform and EGFs. (c) Map projection of the GCMT^{5,6} solution of the mainshock (grey beachball) and the USGS's⁷ two events used as EGFs. The blue and green stars are the epicentres of the 2002-12-17 and 2002-12-18 event, respectively. The yellow star is the epicentre of the first event of the 2021 SSI earthquake. Orange dots are aftershocks that occurred within 3 days of the mainshock detected by the USGS. The black lines are the plate boundary⁸. (d) Observed waveform of the 2021 SSI earthquake (upper) and observed waveforms of the 2002-12-17 event (blue) and the 2002-12-18 event (green) used as EGFs. Both observed waveform and EGFs are band-pass (0.01–2 Hz) filtered. This figure was made with the Generic Mapping Tools (v 6.5.0) software⁹.

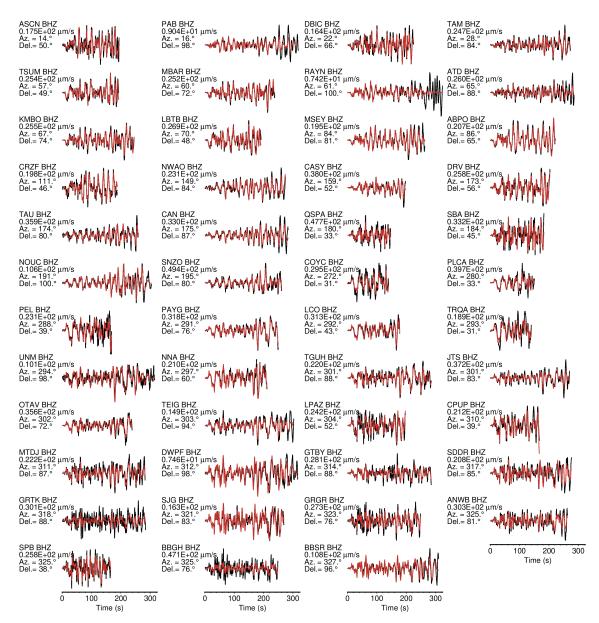


Figure S2. Comparison of observed waveforms (black) with synthetic waveforms (red). Each panel is labelled with the station name, maximum amplitude, azimuth (Az.), and epicentral distance (Del.) from the mainshock. These waveforms were resampled to 20 Hz for plotting. This figure was made with the Generic Mapping Tools (v 6.5.0) software⁹.

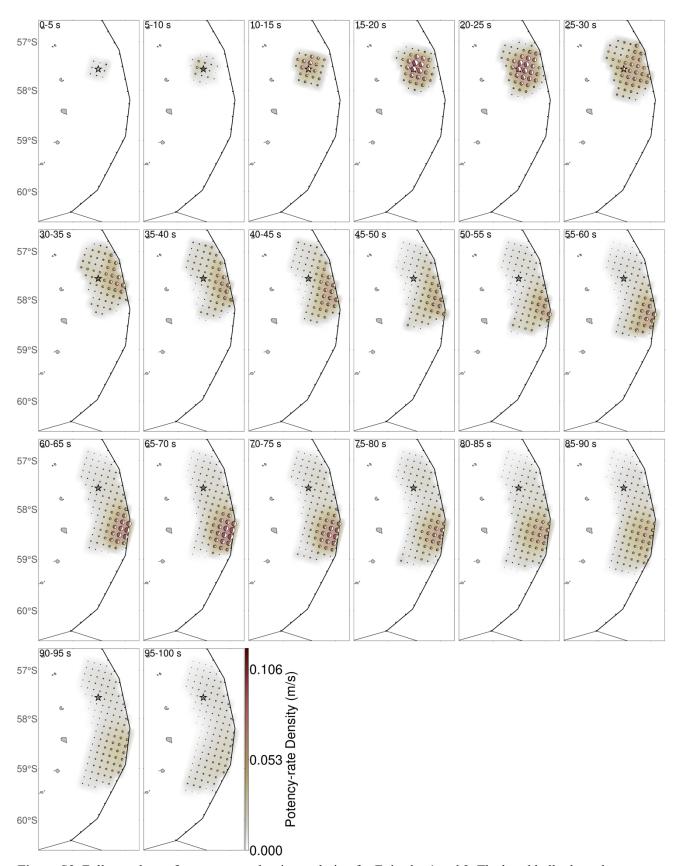


Figure S3. Full snapshots of potency-rate density evolution for Episodes 1 and 2. The beachballs show the potency-rate density tensors. This figure was made with the Generic Mapping Tools (v 6.5.0) software⁹.

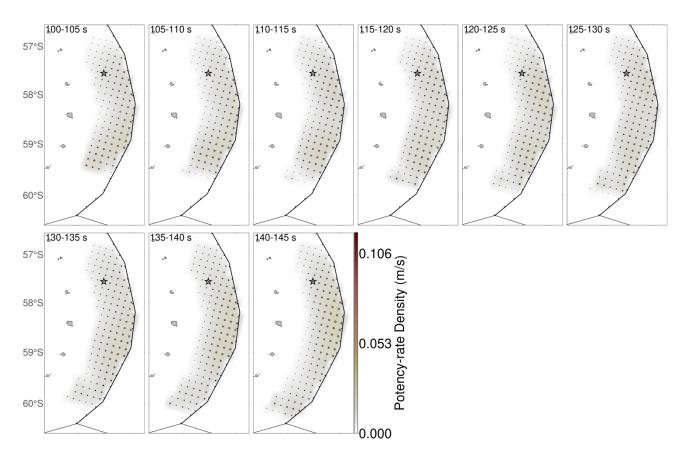


Figure S4. Full snapshots of potency-rate density evolution for Episode 3. The beachballs show the potency-rate density tensors. This figure was made with the Generic Mapping Tools (v 6.5.0) software⁹.

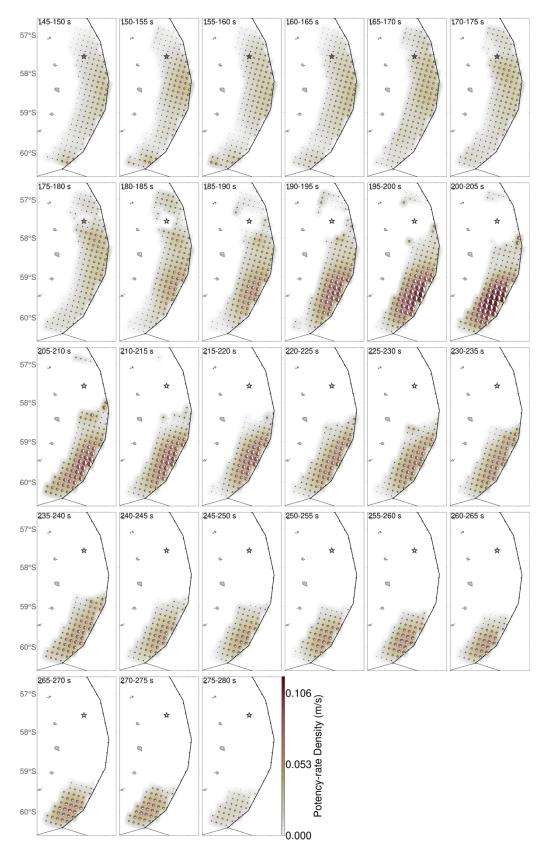


Figure S5. Full snapshots of potency-rate density evolution for Episode 4. The beachballs show the potency-rate density tensors. This figure was made with the Generic Mapping Tools (v 6.5.0) software⁹.

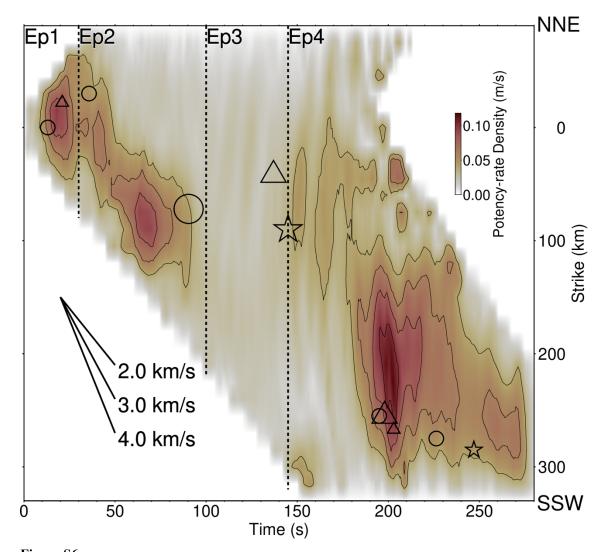
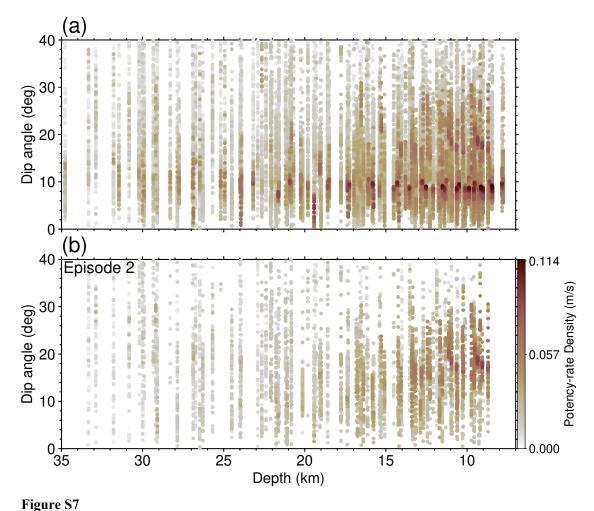


Figure S6

Comparison of the potency-rate density evolution projected along strike and sub-events identified by previous studies^{10,11}. The circle indicates the centroid of the sub-events reported by Jia et al.¹⁰, and the triangle indicates the location of the centroid moment tensor reported by Metz et al.¹¹ The larger markers are the events with duration longer than 100 s. The large and small stars are the epicentres of the M_W 8.1 and mb 6.7 events determined by the USGS⁷, respectively. The style of contours is the same as drawn in Fig. 2d. This figure was made with the Generic Mapping Tools (v 6.5.0) software⁹.



The dip angle distribution. The dip angle is derived from our best-fitting double couple solution of our potency-rate density tensor in a 1-s time window at each source knot in the model domain. The dip angle from the two possible nodal planes is selected based on the subducted plate surface. (a) The dip angle distribution of all the model space. (b) The dip angle distribution during OT+70–100 s in Episode 2.

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