# A simple method using Pyrosequencing ${ }^{\text {TM }}$ to identify de novo SNPs in pooled DNA samples 

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#### Abstract

A practical way to reduce the cost of surveying single-nucleotide polymorphism (SNP) in a large number of individuals is to measure the allele frequencies in pooled DNA samples. Pyrosequencing ${ }^{\text {TM }}$ has been frequently used for this application because signals generated by this approach are proportional to the amount of DNA templates. The Pyrosequencing ${ }^{\text {TM }}$ pyrogram is determined by the dispensing order of dNTPs, which is usually designed based on the known SNPs to avoid asynchronistic extensions of heterozygous sequences. Therefore, utilizing the pyrogram signals to identify de novo SNPs in DNA pools has never been undertook. Here, in this study we developed an algorithm to address this issue. With the sequence and pyrogram of the wild-type allele known in advance, we could use the pyrogram obtained from the pooled DNA sample to predict the sequence of the unknown mutant allele (de novo SNP) and estimate its allele frequency. Both computational simulation and experimental Pyrosequencing ${ }^{\text {TM }}$ test results suggested that our method performs well. The web interface of our method is available at http://life.nctu.edu.tw/ ~yslin/PSM/.


## INTRODUCTION

In human genomes, single-nucleotide polymorphisms (SNPs) compose the majority of genetic variation, and may, therefore, largely determine the differences among individuals. SNPs among human populations have been extensively explored in this decade (1,2). Their abundance and high potential for automation make them become a
powerful tool for identifying genetic factors, especially those contributing to complex disease susceptibility.

However, it is still expensive and time consuming to perform SNP genotyping in a large number of individuals (3). An efficient and low-cost method is important for large-scale SNP scoring. The application of current genotyping platforms for pooled DNA samples might be a practical way (3), because allele frequencies in a group of individuals could be measured using far fewer reactions (4). DNA pooling combined with whole genome analysis is usually considered as the first step to identify potential genetic markers for subsequent genotyping of individuals (5-7). Several genotyping methods suitable for measuring frequencies of SNPs in DNA pools have been proposed in the literatures $(3,8)$.

Pyrosequencing ${ }^{\text {TM }}$, which was first described in 1988 (9), might be one of the most successful non-Sanger methods developed in the two decades (10). Instead of using $3^{\prime}$-modified dNTPs to terminate DNA polymerization, Pyrosequencing ${ }^{\text {TM }}$ adds dNTP bases one at a time in limiting amounts to control DNA synthesis. The dNTPs are dispensed in a specific order. DNA polymerase extends the primer while the complementary dNTP is added and pauses when it encounters a noncomplementary base. The reinitiation of DNA synthesis follows the addition of the next complementary dNTP (10). As a nonfluorescence technique, Pyrosequencing ${ }^{\mathrm{TM}}$ measures the release of inorganic pyrophosphate, which is proportionally transformed into visible light by a cascade of enzymatic reactions $(11,12)$. The generated light is recorded as a series of peaks called a pyrogram, which represents the order of complementary dNTPs and implies the underlying DNA sequence (10).

Because the light generated by the Pyrosequencing ${ }^{\text {TM }}$ reactions is proportional to the amount of DNA template, this technique was frequently used to measure allelic gene expression $(13,14)$ or allele frequency, including in tumor tissue (15), in parasites or microbial community

[^0]$(16,17)$ and in DNA pools $(18-22)$. Pyrosequencing ${ }^{\text {TM }}$ has been recommended for allele frequency studies because of its high reliability in detecting variations between populations $(23,24)$.

The 'next-generation' sequencing technology, including the array-based pyrosequencing ( 454 sequencing platform), has recently been applied for high-throughput resequencing and SNP genotyping (8,25). However, although this strategy is powerful, the expense makes it less applicable when our research interest only focuses on specific genes in specific populations. At present, most clinical laboratories use the low-throughput Pyrosequencing ${ }^{\text {TM }}$ platform to identify known alleles (among organisms, strains or SNPs) (26). In this study, 'Pyrosequencing ${ }^{\text {TM, }}$, refers to this core technology but not the array-based 454 sequencing platform. No study has applied Pyrosequencing ${ }^{\text {TM }}$ for de novo SNP discovery (10). It is because base-calling for de novo SNPs is difficult and still performed manually (27). The Pyrosequencing ${ }^{\mathrm{TM}}$ pyrogram is determined by the dispensing order of dNTPs. To avoid asynchronistic extensions of heterozygous sequences, the dispensing order used to be carefully designed (10). Current
sequencing software cannot detect new polymorphisms in pooled DNA samples (27), including the application of multiplex genotyping techniques (27-30).

Here, in this study, we developed an algorithm based on the normality test and dynamic programming to automatically read the pyrogram profile when unexpected mutations occurred. The performance of our method was evaluated using both computational simulation and experimental Pyrosequencing ${ }^{\text {TM }}$ assays.

## MATERIALS AND METHODS

The object of our method is using a pyrogram of a pooled DNA sample to estimate the frequency of the mutant allele in the sample and predict its sequence. The sequence and pyrogram from the wild-type allele have to be known in advance. The flowchart is shown in Figure 1.

## The expected pyrogram

To illustrate our method, we used a DNA fragment, GAT CGGTTCACGTC, as an example, and assumed that this is the wild-type allele. The Pyrosequencing ${ }^{\text {TM }}$ dispensing


Figure 1. The flowchart of the algorithm developed in this study.


Figure 2. (A) The hypothetical pyrogram profile, $W$, for the wild-type DNA fragment, GATCGGTTCACGTC; (B) the hypothetical pyrogram profile, $M$, for the mutant allele, GAGCGGTTCACGTC; (C) the expected pyrogram profile, $S$, for the pooled DNA sample with $95 \%$ wild-type allele and $5 \%$ mutant allele ( $95 \%$ black bars $+5 \%$ white bars). All the three pyrogram profiles were simulated under the same Pyrosequencing ${ }^{\text {TM }}$ dispensing order of dNTPs, GATCGTCACGTC, with $C V=0.5 \%$.
order of dNTPs, GATCGTCACGTC, was designated to complement this DNA fragment. Figure 2A shows the pyrogram profile, $W$, for this wild-type fragment. The signal intensity for the $n$th dispensed dNTP in $W$ is represented as $w_{n}$. To simulate the real experiments, we defined coefficient of variation ( $C V$ ) here as the standard deviation divided by the mean, and therefore obtained $w_{n}$ :
$w_{n} \sim \operatorname{Normal}\left[\hat{w}_{n},\left(\hat{w}_{n} \times C V\right)^{2}\right]$
$C V$ reflects the degree of precision for the Pyrosequencing ${ }^{\mathrm{TM}}$ experiments. In this example, we let $C V=0.5 \%$.

For a mutant allele with a thymine-to-guanine substitution at the third nucleotide, GAGCGGTTCACGTC, asynchronistic extensions would occur under the designated dispensing order of dNTPs described above. Figure 2B displays the pyrogram profile, $M$, for this mutant allele. Similarly, we could also obtain $m_{n}$ :
$m_{n} \sim \operatorname{Normal}\left[\hat{m}_{n},\left(\hat{m}_{n} \times C V\right)^{2}\right]$
In this circumstance, for a pooled DNA sample with $95 \%$ wild-type allele and $5 \%$ mutant allele, the expected pyrogram profile, $S$, would be nonsynchronistic as


Figure 3. (A) The blue bars represent the pyrogram, $S^{\text {blue }}$, of a pooled DNA sample composed of $95 \%$ wild-type allele and $5 \%$ mutant allele as in Figure 2C. The red bars represent the pyrogram, $S^{\text {red }}$, of a DNA sample composed of $100 \%$ wild-type allele. The two pyrogram profiles were simulated with $C V=0.5 \%$. (B) The ratio profiles $R^{\text {blue }}$ and $R^{\text {red }}$. (C) The relative cumulative frequencies of profiles $Q^{\text {blue }}$ (blue circles) and $Q^{\text {red }}$ (red triangles). The blue crosses represent the expected cumulative normal distribution, $E^{\text {blue }}$, which has the same mean and standard deviation as $Q^{\text {blue }}$. See the main text for the details.
shown in Figure 2C. The pyrogram could be predicted using the equation
$s_{n}=a \times w_{n}+(1-a) \times m_{n}$
where $s_{n}$ is the signal intensity at the $n$th dispensing site for $S$, and $a$ represents the proportion of wild-type allele in the DNA sample. In this example, $a=0.95$.

## The pyrogram to be tested

Assume that we have two unknown pooled DNA samples to be tested, and that one is actually composed of $95 \%$ wild-type allele and $5 \%$ mutant allele as in Figure 2C, while the other is composed of $100 \%$ wild-type allele as in Figure 2A. Their pyrograms, $S^{\text {blue }}$ and $S^{\text {red }}$, respectively, were simulated with $C V=0.5 \%$ and represented in Figure 3A. To distinguish $S^{\text {blue }}$ and $S^{\text {red }}$, we calculated the ratio profile, $R$ :
$r_{n}^{\text {sample }}=s_{n}^{\text {sample }} / w_{n}$

The obtained $R^{\text {blue }}$ and $R^{\text {red }}$ are shown in Figure 3B. Note that pyrogram $S^{\text {blue }}$ has nonsynchronistic extensions. Therefore, when the added nucleotide during Pyrosequencing ${ }^{\text {TM }}$ is not complementary to the mutant allele (for $S^{\text {blue }}, n=3,4,6,8$ and 9 ), decreased signal would be detected. For these dispensing sites, $\hat{r}_{n}^{\text {blue }}=a^{\text {blue }}=0.95$; while for the other sites, $\hat{r}_{n}^{\text {blue }}>a^{\text {blue }}$ because $\hat{m}_{n}>0$. As a result, the values of $R^{\text {blue }}{ }^{n}$ would not be normally distributed. By contrast, the distribution of the values of $R^{\text {red }}$ should be normal, and $\hat{r}_{n}^{\text {red }}=a^{\text {red }}=1$. We performed the Shapiro-Wilk test (31) on the normality of $R$, and sorted the values of $R$ to obtain another profile, $Q$ :
$Q=\operatorname{sort}(R)$
The relative cumulative frequencies of $Q^{\text {blue }}$ and $Q^{\text {red }}$ are shown in Figure 3C. When the normality of $R$ is rejected, possible nonsynchronistic extensions are implied. We therefore constructed an expected cumulative normal distribution, $E$, with the same mean and standard deviation as $Q$, and compared $Q$ with $E$. In our example, the blue circles and the blue crosses represent $Q^{\text {blue }}$ and $E^{\text {blue }}$, respectively (Figure 3C). As described above, for certain dispensing sites, $\hat{r}_{n}^{\text {blue }}=a^{\text {blue }}$, which corresponds to a group of the smallest values of $Q^{\text {blue }}$. To estimate the value of $a^{\text {blue }}$, we looked for a variable $i$ that can maximize $e_{i}^{\text {blue }}-q_{i}^{\text {blue }}$, and then found another variable $j$ that can minimize $q_{j+1}^{\text {blue }}-q_{j-1}^{\text {blue }} \mid j<i$. We then speculated that
$a^{\text {sample }} \approx q_{j}^{\text {sample }}$
In our example, $i=5, \quad j=4, \quad$ and $\quad q_{4}^{\text {blue }}=0.9502$ (Figure 3C).

## The sequence of the mutant allele

Because $a \approx q_{j}$, we used $q_{j}$ to construct another profile, $T$ :
$t_{n}=s_{n}-q_{j} \times w_{n} \approx(1-a) \times m_{n}$
The obtained $T^{\text {blue }}$ is shown in Figure 4A. $T$ is basically proportional to $M$, and could be used to infer it. However, it is inappropriate to read the sequence of the mutant allele directly from profile $T$, because its values are highly influenced by the coefficient of variation. Since profiles $W$ and $M$ could be perfectly aligned by adding gaps to $W$ (Figure 2A and B), we used $T$ to replace the unknown profile $M$, and used dynamic programming to align $W$ and $T$ (Figure 4). The obtained alignment was thus used to speculate the sequence of the mutant allele.

Before we perform the dynamic programming, it is worth to emphasize the ad hoc nature of Pyrosequencing ${ }^{\text {TM }}$ :
(i) We can only add gaps to profile $W$, because the dispensing order was designated to complement the wild-type DNA fragment.
(ii) The implied sequence of the mutant allele is the set of nucleotides in $T$ that are aligned to nucleotides in $W$ (skipping nucleotides in $T$ that are aligned to the added gaps). In our example, the implied sequence is GAGCGGTTC according to the alignment result in Figure 4.


Figure 4. The alignment between (A) the profile $T^{\text {blue }}$, which is basically proportional to the unknown profile $M$, and (B) the profile $W$. See the main text for the details.
(iii) When one gap is added to $W$, the corresponding nucleotide in $T$ is suggested to be the added dNTP during Pyrosequencing ${ }^{\text {TM }}$ that is noncomplementary to the mutant allele. The extension was therefore paused at that time. In our example (Figure 4), the third and fourth nucleotides in $T$ (thymine and cytosine) are aligned to the gap in $W$. This alignment implies that both thymine and cytosine are not complementary to the third nucleotide of the mutant allele.
(iv) When the gap added to $W$ is elongated, the set of the corresponding nucleotides in $T$ cannot include all the four dNTPs. Otherwise, all the four dNTPs are suggested to be noncomplementary to the next base of the mutant allele. In our example (Figure 4), for the first gap in $W$, only two dNTPs, thymine and cytosine, are included in the set of the corresponding nucleotides in $T$.
(v) When the extension is reinitiated, the added dNTP (the nucleotide in $T$ that is aligned to the current nucleotide in $W$ ) should be complementary, and therefore cannot be one of these noncomplementary dNTPs that have appeared in the positions of $T$ that correspond to the adjacent prior gap of $W$. In our example (Figure 4), when the extension is reinitiated following the first gap in $W$, the added complementary dNTP is guanine. This dNTP cannot be thymine or cytosine.
(vi) For the two sites flanking the gap, the corresponding nucleotides in $T$ cannot be the same, because the second added dNTP should be noncomplementary to the first nucleotide. In our example (Figure 4), for the two sites flanking the first gap in $W$, the corresponding nucleotides in $T$ are adenine and guanine.

It should be noted that the dynamic programming is performed when the normality of profile $R$ has been rejected, which implies possible nonsynchronistic extensions. The
nonsynchronistic extensions could result from either substitutions or insertions in the mutant allele. On the other hand, mutations are rare. We do not expect that a mutant allele with more than one de novo SNP in the short fragment would frequently be discovered. Therefore, the scoring scheme for the dynamic programming used in this study is defined as follows:

- The match score: $\left(\bar{t} \times w_{m}+\bar{w} \times t_{n}\right) / 2-2 \times$ $\left|\bar{t} \times w_{m}-\bar{w} \times t_{n}\right| ; \bar{t}$ and $\bar{w}$ are used to even the values of the two profiles.
- The mismatch score: $-\infty$
- The gap penalty for profile $W:-\left(\bar{w} \times t_{n}\right)$
- The gap penalty for profile $T:-\infty$
- One mismatch site with score $\left(\bar{t} \times w_{m}+\bar{w} \times t_{n}\right) / 2-$ $2 \times\left|\bar{t} \times w_{m}-\bar{w} \times t_{n}\right|$ or one gap inserted to profile $W$ with penalty 0 is allowed.


## The estimated proportion of the wild-type allele in the pooled DNA sample

In the previous example, we assumed that the DNA quantity used for the pyrograms, $W$ and $S$, are the same. However, this may not always hold. We therefore introduced another parameter, $c$, to represent the DNA quantity ratio:
$s_{n}=c \times\left[a \times w_{n}+(1-a) \times m_{n}\right]$
Similar to previous sections, we speculated that $q_{j} \approx a c$. We could also obtain two equations:

$$
\begin{aligned}
& \frac{\sum s_{n}-a c \sum w_{n}}{\sum m_{n}}=c \times(1-a) \\
& a \approx \frac{q_{j}}{q_{j}+\frac{\sum s_{n}-q_{j} \sum w_{n}}{\sum m_{n}}}
\end{aligned}
$$

Although $\sum m_{n}$ is unknown, we could use the alignment result to infer it. Assume that there are $x$ elements in the pyrogram $W$, and $y$ of them are aligned to profile $T$, which suggests that there are $(x-y)$ gap sites in the alignment. We could speculate that $\sum_{n=1}^{x} m_{n} \approx \sum_{n=1}^{y} w_{n}$. Therefore, the proportion of the wild-type allele $n=n=1$ in the pooled DNA sample was estimated as

$$
a \approx \frac{q_{j}}{q_{j}+\frac{\sum_{n=1}^{x} s_{n}-q_{j} \sum_{n=1}^{x} w_{n}}{\sum_{n=1}^{y} w_{n}}}
$$

Considering that in some cases the predicted mutant alleles may be derived from insertions, for example, an insertion at site $z$, we modified the equation as the following for these alleles:

$$
a \approx \frac{q_{j}}{q_{j}+\frac{\left(\sum_{n=1}^{x} s_{n}-s_{z}\right)-q_{j}\left(\sum_{n=1}^{x} w_{n}-w_{z}\right)}{\sum_{n=1}^{y} w_{n}}}
$$

## The position of the mutation site

It should be noted that the value of $i$, which maximizes $e_{i}-q_{i}$, depends on the position of the mutant site. When
the mutant site is located close to the end of the pyrogram, the value of $i$ (and the proportion of $i$ to $x$ ) would be small. In this circumstance, the normality of profile $R$ may not be rejected because the signals of nonsynchronistic extensions are likely to be diluted. To overcome this problem, we tested the normality in a sliding window. The window size was designated as 30 in our study. As the window slides, if the normality is rejected for a certain window, we would use this window and its downstream pyrogram to derive the profile $Q$, and variables $i, j$ and $q_{j}$.

## Performance testing by computational simulation

We utilized simulation tests to evaluate the performance of our algorithm. The tested DNA fragments are listed below:

## ACACCAAGTCGTGTTCACAGTGGCTAAGTTCCG

 CCAGCCTCAC-the wild-type allele;ACGCCAAGTCGTGTTCACAGTGGCTAAGTTCCG $\overline{\text { CCAGCCTCAC - the mutant allele with an adenosine- }}$ to-guanine substitution at the third nucleotide;
ACAGCCAAGTCGTGTTCACAGTGGCTAAGTTCC GCCAGCCTCAC-the mutant allele with a guanine inserted between the third and fourth nucleotides;
ACACCAAGTCGTGTTCACAGTGGCTAAGTTCCG CCATCCTCAC-the mutant allele with a guanine-to-thymine substitution at the 37th nucleotide; and
ACACCAAGTCGTGTTCACAGTGGCTAAGTTCCG CCAGCCACAC-the mutant allele with a thymine-to-adenosine substitution at the 40th nucleotide.

The Pyrosequencing ${ }^{\text {TM }}$ dispensing order of dNTPs, ACA CAGTCGTGTCACAGTGCTAGTCGCAGCTCAC, was designated to complement the wild-type allele. The tested DNA pools contained $0 \%, 1 \%, 2 \%, 4 \%, 8 \%$, $16 \%, 32 \%$ or $64 \%$ mutant allele. The pyrograms of these pooled DNA samples were simulated with different degrees of experimental precision $(C V=0.01 \%, 0.02 \%$, $0.04 \%, 0.08 \%, 0.16 \%, 0.32 \%, 0.64 \%, 1.28 \%, 2.56 \%$, $5.12 \%, 10.24 \%$ and $20.48 \%$ ). When the normality of profile $R$ was rejected ( $P<0.01$, Shapiro-Wilk test), dynamic programming was performed to speculate the sequence of the mutant allele; otherwise, no mutant allele was inferred. If the speculated sequence of the mutant allele was identical to the wild-type (except for the last couple nucleotides, which may not be well aligned when $C V$ is high), no mutant allele was inferred, either. The simulation tests were repeated 10000 times. If our method positively identified a mutant allele, we estimated the proportion of the wild-type allele in the DNA pool, despite whether the speculated sequence is correct or not. The mean and standard deviation of the estimated proportion of the wild-type allele in the DNA pool were thus calculated.

## Performance testing by real Pyrosequencing ${ }^{\text {TM }}$

We first used a real Pyrosequencing ${ }^{\mathrm{TM}}$ assay as an example. The DNA samples were obtained from mitochondrial cytochrome $b$ gene of Pseudorasbora parva specimens. The test region was amplified using a specific primer pair: forward - GTGTGAAGTTGTCGGGGT

CT; reverse - CCGCAACGGTTATCCATCTT. The Biotin tag was attached on the reverse primer. Polymerase chain reaction (PCR) was conducted using Taq DNA polymerase (Biokit Biotechnology, Taiwan) in a reaction mixture containing 25 ng of DNA template, 100 nM of biotin-labeled reverse primer and 100 nM of the forward primer. The PCR cycling program consisted of denaturation at $94^{\circ} \mathrm{C}$ for 1 min ; followed by 40 cycles of denaturation at $94^{\circ} \mathrm{C}$ for 20 s , annealing at $60^{\circ} \mathrm{C}$ for 20 s , and extension at $72^{\circ} \mathrm{C}$ for 15 s ; and the final extension at $72^{\circ} \mathrm{C}$ for 7 min . PCR products were purified with PCR clean-up kit (Biokit Biotechnology). The pooled DNA sample contained $90 \%$ PCR products of one allele (CCT AACAGGTTAGGGGAAAATAGCGCTAGAGATGT AAGGGCCAACAATATTAATACAAAGCCAAGAA
GGTCTTTGT for the first 76 bases) as the wild-type and $10 \%$ PCR products of another allele with a cytosine-to-thymine substitution at the 6th nucleotide (CCTAA TAGGTTAGGGGAAAATAGCGCT for the first $\overline{27}$ bases) as the mutant allele. The concentrations of the DNA samples were measured using ND-1000 (Nanodrop Technologies, Wilmington, DE, USA) at $\mathrm{OD}_{260}$. Biotinylated single-stranded DNA in $40 \mu \mathrm{l}$ PCR solution containing 600 ng pooled DNA samples and the forward primer were used for the Pyrosequencing ${ }^{\mathrm{TM}}$ reaction, which was performed in accordance with the manufacturer's instructions (www.pyrosequencing.com) using Pyro Gold SQA Reagents (Qiagen, Hilden, Germany) by model PyroMark ID (Biotage AB, Uppsala, Sweden).

To reveal how practical our method is in real experiments, another large-scale Pyrosequencing ${ }^{\text {TM }}$ assay was conducted. A partial region of YBR114W gene was amplified for both the two yeast strains, BY4741 (BY, a laboratory strain) and RM11-1a (RM, a wild strain) with a specific primer pair: forward - AAGCAAAGTATTGT TAGCCGTCTA; reverse - ATCCAGCTCTTTTCAATC TCC. The Biotin tag was also attached on the reverse primer. Another forward sequencing primer, GCCGTCT AAACATGAGT, was used for the Pyrosequencing ${ }^{\text {TM }}$ reaction. The sequences to be read in the Pyrosequencing ${ }^{\text {TM }}$ reactions for BY and RM are GGCA AGTGGCAATCATCAACGAAAATCGAAGCACT and GGTAAGTGGCAATCATCAACGAAAATCGAA GCACT, respectively. A cytosine-to-thymine substitution is at the third nucleotide. We prepared the wild-type sample using $100 \%$ RM and the unknown pooled DNA sample using $90 \% \mathrm{RM}+10 \%$ BY. Both samples were repeated 12 times. One hundred and forty-four sample pairs could therefore be obtained. The derived pyrograms are represented in Supplementary Data.

## RESULTS AND DISCUSSION

The simulation results are listed in Tables 1 and 2. When the variation in the pyrogram signals was limited (the level of precision was high), e.g. $C V<0.1 \%$, in most cases, our method could perfectly predict the DNA sequence of the mutant allele, either a substitution or an insertion, and its proportion in the DNA pools. However, when the signal variation was high (the level of precision was low), the
prediction power of our method decreased with the proportion of the mutant allele in the DNA pool. For example, in Table 1 , when $C V=2.56 \%$, we precisely estimated the proportion of the mutant allele (with one substitution at the third nucleotide) in the DNA pool while its real proportion is $16 \%$ (estimated as $16.00 \pm 2.87 \%$ ); however, when the real proportion decreased to $1 \%$, our method tended to overestimate its value $(3.32 \pm 2.69 \%)$. Similarly, in Table 2, when $C V=2.56 \%$, we accurately predicted the sequence of the mutant allele (with one substitution at the third nucleotide) in all the 10000 repeats while its proportion in the DNA pool is $32 \%$; however, when the real proportion decreased to $1 \%$, we only identified a mutant allele 507 times from the 10000 repeats, and only nine of them had their sequence accurately predicted. Note that the standard deviation of the estimated allele frequencies also increased with $C V$ (Table 1). These results suggested that the performance of our method is highly correlated to the variation in the pyrogram signals (the level of experimental precision) and the proportion of the mutant allele in the DNA pool. We also examined the possibility that we inaccurately predicted the existence of a mutant allele in a DNA pool consisting of $100 \%$ wild-type allele. The false positive ratio was $<5 \%$ when $C V<5 \%$ (Table 2). Moreover, even in these cases, the estimated proportion of the wild-type allele in the DNA pool did not deviate from $100 \%$ too much when the signal variation was limited (Table 1).

Since sufficient signals of nonsynchronistic extensions are crucial for our algorithm, one might argue that it would be difficult to identify a mutant allele if its mutant site was located close to the end of the pyrogram. Our simulation revealed that, when the substitution was located at the 40th nucleotide, our algorithm almost did not have the identification power (Tables 1 and 2) because the generated profile $R$ had only two sites with $\hat{r}_{n}=a$. In this circumstance, it was difficult to obtain a reasonable $i$, and also the variables $j$, and $q_{j}$. We therefore were unable to correctly align the profiles and predict the mutant sequence. However, when the substitution was located at the 37th nucleotide instead (with four sites $\hat{r}_{n}=a$ ), our algorithm performed almost the same as when the substitution was located at the third nucleotide (Tables 1 and 2). This result suggested that our method should have a wide application.

We also performed real Pyrosequencing ${ }^{\text {TM }}$ assays to reveal how our algorithm works. In our first example (Figure 5), the mitochondrial cytochrome $b$ gene of $P$. parva was used. Figure 5A and B display the pyrograms for the wild-type DNA fragment and the pooled DNA sample containing $10 \%$ mutant allele, respectively. Although it might not be easy to distinguish these two pyrograms by eyes, our algorithm successfully identified the sequence of the mutant allele (Figure 5D and E), and estimated its proportion in the DNA pool as $12.0 \%$. The deviation of this estimated value is likely due to the variation in the pyrogram signals. This variation could be revealed from the constructed profile $T$ in Figure 5D. According to the Pyrosequencing ${ }^{\text {TM }}$ dispensing order of dNTPs and the sequence of the mutant allele, the
Table 1. The estimated proportion of the wild-type allele in the DNA pool under various simulated conditions

| CV | The mean $\pm$ standard deviation of the estimated proportion of the wild-type allele in the DNA pool |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $a=1.00$ | $a=0.99$ | $a=0.98$ | $a=0.96$ | $a=0.92$ | $a=0.84$ | $a=0.68$ | $a=0.36$ |
|  | Mutant allele with an adenosine-to-guanine substitution at the third nucleotide |  |  |  |  |  |  |  |
| 0.01\% | $0.9999 \pm 0.0001$ | $0.9900 \pm 0.0001$ | $0.9800 \pm 0.0001$ | $0.9600 \pm 0.0001$ | $0.9200 \pm 0.0001$ | $0.8400 \pm 0.0001$ | $0.6800 \pm 0.0001$ | $0.3600 \pm 0.0001$ |
| 0.02\% | $0.9997 \pm 0.0002$ | $0.9900 \pm 0.0003$ | $0.9800 \pm 0.0003$ | $0.9600 \pm 0.0003$ | $0.9200 \pm 0.0002$ | $0.8400 \pm 0.0002$ | $0.6800 \pm 0.0002$ | $0.3600 \pm 0.0001$ |
| 0.04\% | $0.9994 \pm 0.0004$ | $0.9900 \pm 0.0006$ | $0.9800 \pm 0.0006$ | $0.9600 \pm 0.0005$ | $0.9200 \pm 0.0005$ | $0.8400 \pm 0.0004$ | $0.6800 \pm 0.0003$ | $0.3600 \pm 0.0002$ |
| 0.08\% | $0.9988 \pm 0.0009$ | $0.9900 \pm 0.0011$ | $0.9800 \pm 0.0011$ | $0.9600 \pm 0.0011$ | $0.9200 \pm 0.0010$ | $0.8400 \pm 0.0009$ | $0.6800 \pm 0.0007$ | $0.3600 \pm 0.0004$ |
| 0.16\% | $0.9977 \pm 0.0018$ | $0.9899 \pm 0.0024$ | $0.9800 \pm 0.0022$ | $0.9600 \pm 0.0021$ | $0.9200 \pm 0.0020$ | $0.8400 \pm 0.0018$ | $0.6800 \pm 0.0013$ | $0.3600 \pm 0.0008$ |
| 0.32\% | $0.9954 \pm 0.0036$ | $0.9898 \pm 0.0059$ | $0.9798 \pm 0.0049$ | $0.9599 \pm 0.0042$ | $0.9200 \pm 0.0040$ | $0.8400 \pm 0.0035$ | $0.6800 \pm 0.0026$ | $0.3600 \pm 0.0017$ |
| 0.64\% | $0.9910 \pm 0.0070$ | $0.9881 \pm 0.0086$ | $0.9796 \pm 0.0117$ | $0.9598 \pm 0.0092$ | $0.9199 \pm 0.0079$ | $0.8399 \pm 0.0069$ | $0.6799 \pm 0.0052$ | $0.3600 \pm 0.0033$ |
| 1.28\% | $0.9822 \pm 0.0138$ | $0.9830 \pm 0.0142$ | $0.9763 \pm 0.0170$ | $0.9593 \pm 0.0229$ | $0.9196 \pm 0.0167$ | $0.8401 \pm 0.0138$ | $0.6799 \pm 0.0105$ | $0.3599 \pm 0.0066$ |
| 2.56\% | $0.9654 \pm 0.0275$ | $0.9668 \pm 0.0269$ | $0.9652 \pm 0.0283$ | $0.9541 \pm 0.0340$ | $0.9206 \pm 0.0449$ | $0.8400 \pm 0.0287$ | $0.6802 \pm 0.0213$ | $0.3599 \pm 0.0132$ |
| 5.12\% | $0.9352 \pm 0.0546$ | $0.9336 \pm 0.0528$ | $0.9363 \pm 0.0532$ | $0.9335 \pm 0.0565$ | $0.9111 \pm 0.0675$ | $0.8437 \pm 0.0837$ | $0.6801 \pm 0.0457$ | $0.3597 \pm 0.0267$ |
| 10.24\% | $0.8807 \pm 0.1069$ | $0.8871 \pm 0.1073$ | $0.8862 \pm 0.1071$ | $0.8848 \pm 0.1076$ | $0.8784 \pm 0.1126$ | $0.8395 \pm 0.1387$ | $0.6919 \pm 0.1505$ | $0.3603 \pm 0.0526$ |
| 20.48\% | $0.8315 \pm 0.2466$ | $0.8314 \pm 0.2546$ | $0.8280 \pm 0.2627$ | $0.8282 \pm 0.2467$ | $0.8283 \pm 0.2743$ | $0.8130 \pm 0.2543$ | $0.7490 \pm 0.3271$ | $0.3464 \pm 4.3826$ |
|  | Mutant allele with a guanine inserted between the third and fourth nucleotides |  |  |  |  |  |  |  |
| 0.01\% | $0.9999 \pm 0.0001$ | $0.9900 \pm 0.0001$ | $0.9800 \pm 0.0001$ | $0.9600 \pm 0.0001$ | $0.9200 \pm 0.0001$ | $0.8400 \pm 0.0001$ | $0.6800 \pm 0.0001$ | $0.3600 \pm 0.0001$ |
| 0.02\% | $0.9998 \pm 0.0002$ | $0.9900 \pm 0.0003$ | $0.9800 \pm 0.0003$ | $0.9600 \pm 0.0003$ | $0.9200 \pm 0.0002$ | $0.8400 \pm 0.0002$ | $0.6800 \pm 0.0002$ | $0.3600 \pm 0.0001$ |
| 0.04\% | $0.9997 \pm 0.0005$ | $0.9900 \pm 0.0005$ | $0.9800 \pm 0.0005$ | $0.9600 \pm 0.0005$ | $0.9200 \pm 0.0005$ | $0.8400 \pm 0.0004$ | $0.6800 \pm 0.0003$ | $0.3600 \pm 0.0002$ |
| 0.08\% | $0.9994 \pm 0.0010$ | $0.9900 \pm 0.0011$ | $0.9800 \pm 0.0010$ | $0.9600 \pm 0.0010$ | $0.9200 \pm 0.0010$ | $0.8400 \pm 0.0008$ | $0.6800 \pm 0.0006$ | $0.3600 \pm 0.0004$ |
| 0.16\% | $0.9986 \pm 0.0019$ | $0.9899 \pm 0.0023$ | $0.9801 \pm 0.0021$ | $0.9600 \pm 0.0020$ | $0.9200 \pm 0.0019$ | $0.8400 \pm 0.0017$ | $0.6800 \pm 0.0013$ | $0.3600 \pm 0.0008$ |
| 0.32\% | $0.9974 \pm 0.0037$ | $0.9903 \pm 0.0059$ | $0.9798 \pm 0.0044$ | $0.9601 \pm 0.0041$ | $0.9200 \pm 0.0038$ | $0.8399 \pm 0.0034$ | $0.6800 \pm 0.0026$ | $0.3600 \pm 0.0016$ |
| 0.64\% | $0.9947 \pm 0.0075$ | $0.9888 \pm 0.0089$ | $0.9811 \pm 0.0115$ | $0.9597 \pm 0.0093$ | $0.9199 \pm 0.0076$ | $0.8399 \pm 0.0067$ | $0.6800 \pm 0.0051$ | $0.3600 \pm 0.0032$ |
| 1.28\% | $0.9892 \pm 0.0157$ | $0.9867 \pm 0.0159$ | $0.9789 \pm 0.0176$ | $0.9615 \pm 0.0220$ | $0.9195 \pm 0.0169$ | $0.8400 \pm 0.0134$ | $0.6799 \pm 0.0102$ | $0.3600 \pm 0.0063$ |
| 2.56\% | $0.9808 \pm 0.0296$ | $0.9756 \pm 0.0289$ | $0.9697 \pm 0.0284$ | $0.9580 \pm 0.0342$ | $0.9251 \pm 0.0453$ | $0.8393 \pm 0.0291$ | $0.6797 \pm 0.0205$ | $0.3601 \pm 0.0128$ |
| 5.12\% | $0.9502 \pm 0.0547$ | $0.9538 \pm 0.0560$ | $0.9508 \pm 0.0544$ | $0.9413 \pm 0.0606$ | $0.9254 \pm 0.0773$ | $0.8492 \pm 0.0863$ | $0.6801 \pm 0.0477$ | $0.3599 \pm 0.0257$ |
| 10.24\% | $0.9170 \pm 0.1206$ | $0.9188 \pm 0.1193$ | $0.9223 \pm 0.1269$ | $0.9144 \pm 0.1222$ | $0.9006 \pm 0.1369$ | $0.8573 \pm 0.1565$ | $0.7043 \pm 0.1812$ | $0.3556 \pm 0.5902$ |
| 20.48\% | $0.8898 \pm 0.3129$ | $0.8969 \pm 0.3699$ | $0.9005 \pm 0.5321$ | $0.8804 \pm 0.3253$ | $0.8773 \pm 0.3134$ | $0.8779 \pm 0.5953$ | $0.7953 \pm 1.6143$ | $0.3580 \pm 3.9309$ |
|  | Mutant allele with a guanine-to-thymine substitution at the 37th nucleotide |  |  |  |  |  |  |  |
| 0.01\% | $0.9999 \pm 0.0001$ | $0.9900 \pm 0.0001$ | $0.9800 \pm 0.0001$ | $0.9600 \pm 0.0001$ | $0.9200 \pm 0.0001$ | $0.8400 \pm 0.0001$ | $0.6800 \pm 0.0001$ | $0.3600 \pm 0.0000$ |
| 0.02\% | $0.9998 \pm 0.0002$ | $0.9900 \pm 0.0002$ | $0.9800 \pm 0.0002$ | $0.9600 \pm 0.0002$ | $0.9200 \pm 0.0002$ | $0.8400 \pm 0.0002$ | $0.6800 \pm 0.0001$ | $0.3600 \pm 0.0001$ |
| 0.04\% | $0.9997 \pm 0.0005$ | $0.9900 \pm 0.0004$ | $0.9800 \pm 0.0004$ | $0.9600 \pm 0.0003$ | $0.9200 \pm 0.0003$ | $0.8400 \pm 0.0003$ | $0.6800 \pm 0.0003$ | $0.3600 \pm 0.0002$ |
| 0.08\% | $0.9993 \pm 0.0009$ | $0.9900 \pm 0.0007$ | $0.9800 \pm 0.0007$ | $0.9600 \pm 0.0007$ | $0.9200 \pm 0.0007$ | $0.8400 \pm 0.0006$ | $0.6800 \pm 0.0005$ | $0.3600 \pm 0.0004$ |
| 0.16\% | $0.9985 \pm 0.0018$ | $0.9900 \pm 0.0015$ | $0.9800 \pm 0.0015$ | $0.9600 \pm 0.0014$ | $0.9200 \pm 0.0014$ | $0.8400 \pm 0.0012$ | $0.6800 \pm 0.0010$ | $0.3600 \pm 0.0008$ |
| 0.32\% | $0.9975 \pm 0.0037$ | $0.9900 \pm 0.0047$ | $0.9800 \pm 0.0031$ | $0.9601 \pm 0.0028$ | $0.9200 \pm 0.0027$ | $0.8400 \pm 0.0024$ | $0.6800 \pm 0.0020$ | $0.3600 \pm 0.0016$ |
| 0.64\% | $0.9948 \pm 0.0076$ | $0.9916 \pm 0.0085$ | $0.9803 \pm 0.0096$ | $0.9598 \pm 0.0058$ | $0.9201 \pm 0.0054$ | $0.8400 \pm 0.0049$ | $0.6801 \pm 0.0041$ | $0.3600 \pm 0.0032$ |
| 1.28\% | $0.9885 \pm 0.0144$ | $0.9881 \pm 0.0146$ | $0.9853 \pm 0.0170$ | $0.9595 \pm 0.0172$ | $0.9198 \pm 0.0111$ | $0.8401 \pm 0.0098$ | $0.6799 \pm 0.0083$ | $0.3600 \pm 0.0065$ |
| 2.56\% | $0.9774 \pm 0.0296$ | $0.9774 \pm 0.0276$ | $0.9741 \pm 0.0277$ | $0.9700 \pm 0.0342$ | $0.9173 \pm 0.0304$ | $0.8395 \pm 0.0198$ | $0.6799 \pm 0.0164$ | $0.3601 \pm 0.0129$ |
| 5.12\% | $0.9531 \pm 0.0535$ | $0.9590 \pm 0.0577$ | $0.9552 \pm 0.0542$ | $0.9533 \pm 0.0567$ | $0.9367 \pm 0.0640$ | $0.8463 \pm 0.0670$ | $0.6798 \pm 0.0329$ | $0.3600 \pm 0.0255$ |
| 10.24\% | $0.9108 \pm 0.1205$ | $0.9112 \pm 0.1175$ | $0.9142 \pm 0.1161$ | $0.9162 \pm 0.1199$ | $0.9059 \pm 0.1164$ | $0.8901 \pm 0.1305$ | $0.6954 \pm 0.1258$ | $0.3595 \pm 0.0516$ |
| 20.48\% | $0.8806 \pm 0.3044$ | $0.8952 \pm 0.3788$ | $0.8890 \pm 0.3120$ | $0.8957 \pm 0.3257$ | $0.8863 \pm 0.3063$ | $0.8816 \pm 0.3128$ | $0.8718 \pm 0.3127$ | $0.5032 \pm 0.4090$ |
|  | Mutant allele with a thymine-to-adenosine substitution at the 40th nucleotide |  |  |  |  |  |  |  |
| 0.01\% | $0.9999 \pm 0.0001$ | $1.0008 \pm 0.0003$ | $1.0015 \pm 0.0005$ | $1.0031 \pm 0.0011$ | $1.0061 \pm 0.0021$ | $1.0124 \pm 0.0043$ | $1.0250 \pm 0.0088$ | $1.0518 \pm 0.0187$ |
| 0.02\% | $0.9998 \pm 0.0002$ | $1.0008 \pm 0.0003$ | $1.0015 \pm 0.0006$ | $1.0030 \pm 0.0011$ | $1.0061 \pm 0.0021$ | $1.0123 \pm 0.0043$ | $1.0248 \pm 0.0088$ | $1.0511 \pm 0.0185$ |
| 0.04\% | $0.9997 \pm 0.0005$ | $1.0008 \pm 0.0006$ | $1.0015 \pm 0.0007$ | $1.0031 \pm 0.0012$ | $1.0061 \pm 0.0022$ | $1.0124 \pm 0.0044$ | $1.0250 \pm 0.0088$ | $1.0515 \pm 0.0186$ |
| 0.08\% | $0.9992 \pm 0.0009$ | $1.0011 \pm 0.0013$ | $1.0016 \pm 0.0012$ | $1.0031 \pm 0.0014$ | $1.0061 \pm 0.0023$ | $1.0124 \pm 0.0044$ | $1.0251 \pm 0.0089$ | $1.0515 \pm 0.0187$ |
| 0.16\% | $0.9985 \pm 0.0018$ | $1.0003 \pm 0.0035$ | $1.0022 \pm 0.0025$ | $1.0033 \pm 0.0025$ | $1.0062 \pm 0.0027$ | $1.0124 \pm 0.0047$ | $1.0252 \pm 0.0091$ | $1.0516 \pm 0.0188$ |
| 0.32\% | $0.9974 \pm 0.0038$ | $0.9974 \pm 0.0061$ | $1.0004 \pm 0.0070$ | $1.0044 \pm 0.0051$ | $1.0066 \pm 0.0047$ | $1.0124 \pm 0.0055$ | $1.0250 \pm 0.0095$ | $1.0517 \pm 0.0191$ |
| 0.64\% | $0.9947 \pm 0.0073$ | $0.9939 \pm 0.0090$ | $0.9948 \pm 0.0124$ | $1.0010 \pm 0.0139$ | $1.0089 \pm 0.0098$ | $1.0132 \pm 0.0093$ | $1.0249 \pm 0.0109$ | $1.0513 \pm 0.0201$ |
| 1.28\% | $0.9881 \pm 0.0141$ | $0.9873 \pm 0.0154$ | $0.9869 \pm 0.0187$ | $0.9908 \pm 0.0246$ | $1.0037 \pm 0.0269$ | $1.0178 \pm 0.0199$ | $1.0263 \pm 0.0177$ | $1.0517 \pm 0.0233$ |
| 2.56\% | $0.9757 \pm 0.0298$ | $0.9751 \pm 0.0299$ | $0.9751 \pm 0.0285$ | $0.9710 \pm 0.0331$ | $0.9808 \pm 0.0487$ | $1.0100 \pm 0.0497$ | $1.0358 \pm 0.0380$ | $1.0547 \pm 0.0376$ |
| 5.12\% | $0.9578 \pm 0.0584$ | $0.9507 \pm 0.0559$ | $0.9510 \pm 0.0544$ | $0.9506 \pm 0.0580$ | $0.9489 \pm 0.0625$ | $0.9658 \pm 0.0896$ | $1.0293 \pm 0.0910$ | $1.0742 \pm 0.0820$ |
| 10.24\% | $0.9179 \pm 0.1261$ | $0.9043 \pm 0.1042$ | $0.9236 \pm 0.1298$ | $0.9050 \pm 0.1095$ | $0.9180 \pm 0.1220$ | $0.9013 \pm 0.1217$ | $0.9420 \pm 0.1700$ | $1.0736 \pm 0.1752$ |
| 20.48\% | $0.8923 \pm 0.3268$ | $0.8918 \pm 0.3525$ | $0.8920 \pm 0.3403$ | $0.8880 \pm 0.3378$ | $0.8931 \pm 0.3038$ | $0.8825 \pm 0.2935$ | $0.8715 \pm 0.2986$ | $0.9362 \pm 0.3909$ |

Table 2. The accuracy of the mutant allele identification in the DNA pool under various simulated conditions

| CV | True positive/positive |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $a=1.00$ | $a=0.99$ | $a=0.98$ | $a=0.96$ | $a=0.92$ | $a=0.84$ | $a=0.68$ | $a=0.36$ |
|  | Mutant allele with an adenosine-to-guanine substitution at the third nucleotide |  |  |  |  |  |  |  |
| 0.01\% | - / 387 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ |
| 0.02\% | - / 370 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | 10000 / 10000 | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ |
| 0.04\% | - / 380 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ |
| 0.08\% | -/ 401 | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | 10000 / 10000 |
| 0.16\% | - / 371 | 9242 / 9504 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ |
| 0.32\% | - / 363 | 1932 / 3057 | 9304 / 9568 | 10000 / 10000 | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ |
| 0.64\% | -/ 363 | 209 / 1006 | 1978 / 3087 | 9436 / 9676 | 10000 / 10000 | $10000 / 10000$ | 10000 / 10000 | $10000 / 10000$ |
| 1.28\% | -/ 401 | $31 / 609$ | 234 / 1084 | 2224 / 3311 | 9616 / 9801 | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ |
| 2.56\% | - / 445 | 9 / 507 | $38 / 718$ | 285 / 1236 | 2742 / 3922 | 9818 / 9939 | $10000 / 10000$ | $10000 / 10000$ |
| 5.12\% | -/ 541 | $5 / 634$ | 11/690 | 67 / 995 | 452 / 1697 | 3801 / 5166 | 9932 / 9997 | 10000 / 10000 |
| 10.24\% | - / 1099 | $3 / 1158$ | 10 / 1205 | $35 / 1391$ | 117 / 1758 | 820 / 2856 | 6132 / 7503 | 9969 / 10000 |
| 20.48\% | - / 3287 | 15/3303 | 27 / 3400 | 45 / 3565 | 95 / 3909 | 361 / 4430 | 2058 / 5874 | 8086 / 9374 |
|  | Mutant allele with a guanine inserted between the third and fourth nucleotides |  |  |  |  |  |  |  |
| 0.01\% | -/ 366 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ |
| 0.02\% | - / 368 | $10000 / 10000$ | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ |
| 0.04\% | - / 354 | 10000 / 10000 | $10000 / 10000$ | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ |
| 0.08\% | -/ 378 | 9995 / 10000 | $10000 / 10000$ | $10000 / 10000$ | 10000 / 10000 | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ |
| 0.16\% | - / 366 | 8604 / 8882 | 9998 / 10000 | 10000 / 10000 | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ | 10000 / 10000 |
| 0.32\% | - / 381 | 1351 / 2389 | 8667 / 8936 | 9994 / 10000 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ |
| 0.64\% | - / 384 | 166 / 946 | 1425 / 2385 | 8894 / 9138 | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ | 10000 / 10000 |
| 1.28\% | - / 358 | 19 / 604 | 181 / 1042 | 1571 / 2610 | 9184 / 9396 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ |
| 2.56\% | -/ 424 | $6 / 547$ | 21/698 | 219 / 1188 | 1971 / 3104 | 9600 / 9793 | 10000 / 10000 | $10000 / 10000$ |
| 5.12\% | - / 573 | $0 / 663$ | $7 / 699$ | $31 / 903$ | 260 / 1499 | 2829 / 4125 | 9856 / 9987 | $10000 / 10000$ |
| 10.24\% | - / 1032 | 1/1079 | $3 / 1221$ | 15 / 1389 | 79 / 1795 | 621 / 2765 | 5134 / 6494 | 9934 / 10000 |
| 20.48\% | -/ 3231 | 4 / 3288 | 6 / 3432 | 16/3553 | $32 / 3875$ | 208 / 4513 | 1613 / 5737 | 7559 / 8853 |
|  | Mutant allele with a guanine-to-thymine substitution at the 37th nucleotide |  |  |  |  |  |  |  |
| 0.01\% | - / 402 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ |
| 0.02\% | -/ 382 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ |
| 0.04\% | - / 394 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ |
| 0.08\% | - / 393 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ |
| 0.16\% | - / 385 | 8867 / 8944 | 10000 / 10000 | $10000 / 10000$ | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ |
| 0.32\% | - / 427 | 918 / 1152 | 9005 / 9060 | 10000 / 10000 | 10000 / 10000 | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ |
| 0.64\% | - / 392 | 77 / 386 | 855 / 1091 | 9050 / 9107 | 10000 / 10000 | 10000 / 10000 | $10000 / 10000$ | $10000 / 10000$ |
| 1.28\% | - / 394 | 24 / 397 | 76 / 401 | 869 / 1056 | 9220 / 9256 | $10000 / 10000$ | $10000 / 10000$ | $10000 / 10000$ |
| 2.56\% | - / 452 | $3 / 443$ | 13/429 | 60 / 385 | 868 / 1026 | 9480 / 9497 | 10000 / 10000 | 10000 / 10000 |
| 5.12\% | - / 552 | $3 / 529$ | $3 / 576$ | 17 / 521 | 99 / 504 | 947 / 1112 | 9767 / 9775 | $10000 / 10000$ |
| 10.24\% | -/ 1048 | 2/1058 | 5/1054 | 11/1052 | $43 / 1111$ | 160 / 963 | 1145 / 1332 | 9820 / 9824 |
| 20.48\% | - / 3227 | 8/3282 | $9 / 3461$ | 10 / 3260 | $31 / 3439$ | 99 / 3428 | 480 / 3043 | 1901 / 2481 |
|  | Mutant allele with a thymine-to-adenosine substitution at the 40th nucleotide |  |  |  |  |  |  |  |
| 0.01\% | - / 367 | 111 / 10000 | $111 / 10000$ | 95 / 10000 | $82 / 10000$ | $96 / 10000$ | 116 / 10000 | $97 / 10000$ |
| 0.02\% | - / 372 | 100 / 10000 | 112 / 10000 | 99 / 10000 | $98 / 10000$ | 96 / 10000 | 126 / 10000 | 122 / 10000 |
| 0.04\% | - / 379 | 110 / 10000 | 109 / 10000 | 118 / 10000 | 100 / 10000 | 117 / 10000 | 91 / 10000 | 110 / 10000 |
| 0.08\% | - / 384 | 115 / 10000 | 121 / 10000 | 123 / 10000 | 99 / 10000 | 109 / 10000 | 92 / 10000 | 118 / 10000 |
| 0.16\% | - / 379 | 934 / 7882 | 126 / 10000 | 111/10000 | 120 / 10000 | 112 / 10000 | 114 / 10000 | 103 / 10000 |
| 0.32\% | - / 358 | 386 / 1438 | 921 / 7837 | 100 / 10000 | 105 / 10000 | 117 / 10000 | $88 / 10000$ | 111 / 10000 |
| 0.64\% | - / 382 | 99 / 566 | 423 / 1465 | 929 / 7948 | 106 / 10000 | 120 / 10000 | 110 / 10000 | 117 / 10000 |
| 1.28\% | -/ 401 | 37 / 418 | 105 / 541 | 373 / 1460 | 806 / 8201 | 96 / 10000 | 99 / 10000 | 104 / 10000 |
| 2.56\% | -/ 403 | $21 / 468$ | $50 / 484$ | 109 / 566 | 421 / 1523 | 663 / 8525 | 105 / 10000 | 87 / 10000 |
| 5.12\% | - / 566 | 29 / 572 | $35 / 564$ | 43 / 559 | 122 / 677 | 400 / 1592 | 479 / 9017 | 121 / 10000 |
| 10.24\% | -/ 1083 | $30 / 1100$ | 40 / 1063 | $58 / 1109$ | $81 / 1092$ | 184 / 1182 | 424 / 2003 | $253 / 9156$ |
| 20.48\% | -/ 3238 | 62 / 3344 | 64 / 3271 | 86 / 3374 | 102 / 3374 | 183 / 3520 | 403 / 3644 | $550 / 4127$ |

Positive: the total number of simulation repeats that positively identified a mutant allele in the DNA pool. True positive: the number of simulation repeats that correctly identified the mutant allele.
$a$ indicates the real proportion of the wild-type allele in the DNA pool.


Figure 5. The real Pyrosequencing ${ }^{\text {TM }}$ examination of the mitochondrial cytochrome $b$ gene of $P$. parva: (A) the pyrogram of the wild-type DNA fragment, $W ;(\mathbf{B})$ the pyrogram of a pooled DNA sample containing $10 \%$ mutant DNA, $S ;(\mathbf{C})$ the profile $R$; (D) the profile $T$; (E) the profile $W$ which is aligned to profile $T$. See the main text for the details.

29th-39th and 42 nd -45 th sites were supposed to have no signal being detected; however, unexpected high values (due to the signal variation) were represented on some of these sites (Figure 5D). Our dynamic programming overcame this difficulty by considering the ad hoc nature
of Pyrosequencing ${ }^{\text {TM }}$. We were therefore able to correctly align the profiles $T$ and $W$, and predicted the sequence of the mutant allele (Figure 5D and E).

Given that the performance of our algorithm heavily depends on the level of experimental precision as
described above, it is worth to know the reproducibility of general Pyrosequencing ${ }^{\text {TM }}$ reactions. Previous studies indicated that, when the same PCR products were sequenced several times, the standard deviation of the signals ranged $0.006-0.024$ (32) and $0.008-0.031$ (15). Doostzadeh et al. (22) further suggested that it is possible to reduce the values of standard deviation to $0.0003-0.0018$ if the signal intensity was appropriately measured. If the coefficient of variation was limited in this range, our method could easily be used to detect rare mutant alleles (Tables 1 and 2). It should be emphasized that the purpose of our study was not to improve the quality of Pyrosequencing ${ }^{\mathrm{TM}}$ reactions and our experiments were not performed by experienced technicians. However, the result of our large-scale assay indicates that the proposed algorithm still performs well for such general Pyrosequencing ${ }^{\mathrm{TM}}$ tests (Table 3). Among all the 144 sample pairs, only one pair failed to satisfy the criteria: Shapiro-Wilk test, $P<0.05$. Moreover, we accurately predicted the sequence of BY strain (the unknown allele) for 141 of the rest 143 pairs. The proportion of BY strain in the pooled DNA sample was estimated as $12.82 \pm 3.81 \%$. We also tested the false-positive ratio using the 12 repeats with $100 \%$ RM as both wild-type sample and pooled DNA sample. In the possible 132 sample pairs, only three pairs were inaccurately predicted as with the existence of a mutant allele, i.e. W3/W6, W5/W8 and W6/W3 as the wild-type sample/the pooled sample, respectively. These examinations are consistent with our computational simulation results.

The deficiency of our algorithm is that it might fail if the pooled DNA sample contained more than one unexpected mutant allele (de novo SNP). Combining more than two pyrograms into one would make the derived pyrogram become too complicated to be decomposed. Fortunately, we could design a specific dispensing order of dNTPs for all the known haplotypes, and our method only has to deal with de novo SNPs. It is unlikely that we would frequently find two or more de novo SNPs in a short Pyrosequencing ${ }^{\mathrm{TM}}$ read. The other difficulty is that one haplotype might include more than one mutant
site. Modifying the scoring scheme of our dynamic programming (e.g. reducing the penalty for the second mismatch site) might help to identify some of these haplotypes. This is especially true if the mutant sites were located close to the start of the pyrogram, because sufficient signals of nonsynchronistic extensions could thus be provided to overcome the penalty of the mismatch sites. However, this kind of modifications would also increase the false-positive ratio and decrease the specificity of our prediction. Therefore, our method only focused on haplotypes with one mutant site, since mutations are supposed to be rare.
In recent years, Pyrosequencing ${ }^{\text {TM }}$ has been frequently utilized to estimate the frequencies or expression levels of known alleles (13-24,26). Because the dispensing order of dNTPs was designed based on the known SNPs, the de novo SNPs probably used to be ignored, especially if their frequencies were not high enough to generate obvious signals of asynchronistic extensions. For this kind of studies, our method could easily be applied to examine the existence of unexpected mutant alleles in the DNA samples by comparing the obtained pyrograms. This is a simple and economical strategy for SNP genotyping surveys. On the other hand, our algorithm also has the potential to be applied for the highthroughput Pyrosequencing ${ }^{\text {TM }}$ (454 platform) data. An appropriate DNA-to-bead ratio is essential for the 454 platform because only beads carrying single type of amplified templates could generate readable signals (flowgrams) (33-35). The mixed signals generated from either wells each containing multiple beads or beads each carrying multiple amplified templates are usually filtered out. In some of these cases, asynchronistic extensions may occur and our algorithm could be modified to identify these mixed DNA templates. More information could therefore be obtained. In other words, the method proposed in this study not only creates a new application for the low-throughput Pyrosequencing ${ }^{\text {TM }}$ platform, but also provides a possible strategy to improve the highthroughput Pyrosequencing ${ }^{\text {TM }}$ platform that might be useful in the future.

Table 3. The estimated proportion of BY strain (the unknown allele) in the pooled DNA samples in our large-scale Pyrosequencing ${ }^{\text {TM }}$ assay

|  | S1 | S2 | S3 | S4 | S5 | S6 | S7 | S8 | S9 | S10 |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| W1 | 0.0954 | 0.1851 | 0.0977 | 0.1434 | 0.0916 | 0.1443 | 0.0875 | 0.1662 | 0.1045 | 0.1387 | 0.1199 |
| W2 | 0.1147 | 0.1387 | 0.1049 | 0.1380 | 0.1705 | 0.1417 | 0.1158 | 0.0755 | 0.1299 | 0.1026 | 0.1445 |
| W3 | 0.1185 | 0.1469 | 0.1480 | 0.1312 | 0.0894 | 0.1361 | 0.1623 | 0.1638 | 0.1484 | 0.1349 | 0.1130 |
| W4 | 0.1032 | 0.1774 | 0.1273 | 0.1281 | 0.1394 | 0.1655 | 0.1569 | 0.1593 | 0.1735 | 0.1668 | 0.1500 |
| W5 | 0.1252 | 0.1979 | 0.1424 | 0.1154 | 0.1980 | 0.1651 | 0.1448 | 0.1583 | 0.1451 | 0.1165 | 0.1433 |
| W6 | 0.0618 | 0.0412 | 0.0829 | 0.1335 | 0.1304 | 0.0330 | - | 0.2073 | 0.0708 | $0.2122^{*}$ | 0.0909 |
| W7 | 0.1084 | 0.1065 | 0.1460 | 0.1055 | 0.1099 | 0.1579 | 0.1553 | 0.1383 | 0.0756 | 0.1667 | 0.0901 |
| W8 | 0.0702 | 0.1562 | 0.1979 | 0.1360 | 0.0464 | 0.1264 | 0.1452 | 0.0779 | 0.2001 | 0.1095 | 0.0779 |
| W9 | 0.0704 | 0.0874 | 0.1002 | 0.1596 | 0.1459 | 0.1398 | -0.0616 | 0.1846 | 0.1994 | 0.1871 | 0.1551 |
| W10 | 0.1262 | 0.1078 | 0.0904 | 0.1550 | 0.1237 | 0.1111 | 0.1274 | 0.0721 | 0.1249 | $0.1502 *$ | 0.0993 |
| W11 | 0.1183 | 0.1043 | 0.1240 | 0.1320 | 0.1162 | 0.1601 | 0.1049 | 0.1372 | 0.1226 | 0.1703 | 0.1256 |
| W12 | 0.1136 | 0.1300 | 0.1408 | 0.1078 | 0.0983 | 0.1164 | 0.1195 | 0.1472 | 0.1366 | 0.1760 | 0.1414 |

The 12 wild-type samples ( $100 \% \mathrm{RM}$ ) are denoted as W1-W12, while the 12 pooled DNA samples $(90 \% \mathrm{RM}+10 \% \mathrm{BY})$ are denoted as $\mathrm{S} 1-\mathrm{S} 12$. The sample pair failed to satisfy the criteria: Shapiro-Wilk test, $P<0.05$, is marked with $(-)$, and the two pairs we failed to identify the correct sequence of the unknown allele are marked with $\left(^{*}\right)$.

## SUPPLEMENTARY DATA

Supplementary Data are available at NAR Online.

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