# Gender and Age Patterns in NSGA Swim Competitions 

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#### Abstract

We estimate two common nonlinear models (quadratic and semilog) and one new model (exponential) of the time-age relationship in 500 -yard freestyle swim times in the U.S. National Senior Games (ages 50 and up) in six biennial NSGA competitions ( $2009,2011,2013,2015,2017$, and 2019) for 468 men and 587 women. We use OLS and quantile regression ( $25 \%, 50 \%$, and $75 \%$ ) separately for each gender. The semilog model predicts faster times than the quadratic or exponential models. Our hypothesis that women slow down faster than men after age 50 is supported by both models as well as by our unique within-gender comparisons. Our findings of a nonlinear performance decline agree with studies of elite swimmers (Olympic, FINA). Our first-time study of NSGA data provides new guidelines to inform senior competitors. Our findings will assist trainers and community organizations that support NSGA competitions to promote a healthy senior lifestyle.


## 1. Introduction

Elite swimmers (Olympic, FINA, U.S. Masters) have been studied extensively to establish performance limits and to reveal patterns by age and gender. Most studies cover a wide range of ages [1-8], although some focus on older swimmers [9-13]. Specific attention has been given to how records have improved over time [4, 14-19]. Longitudinal studies [6, 9] are less common than cross-sectional or hybrid studies (see [20] for a good summary). Studies emphasizing the physiology of aging in sports [21], including nonswimming events [10, 22, 23], raise methodological issues that will be discussed in this paper.

Our research seeks to inform and encourage individuals, trainers, and organizations that support senior swimming and healthy aging. For most recreational senior swimmers, ultimate physiological frontiers and Olympic records are an unapproachable asymptote that offers no realistic target to assess their own progress. To provide performance benchmarks that inform and guide a broader cross-section of senior competitors, we examined published times in an endurance swim event (500-yard freestyle short course) in
six consecutive competitions of the National Senior Games Association (NSGA).

How does NSGA data differ from elite competition data? First, only those aged 50 and over can compete. Second, while some NSGA athletes may be elite, many are novices who are attracted to local NSGA competitions through senior centers and community organizations that focus on healthy aging and senior physical and mental health. For example, the sponsors of Michigan Senior Olympics NSGA include a local university, county parks and recreation, health care providers, and senior living groups [24]. NSGAsponsored games and self-organized teams provide a social nexus for older adults with community involvement and volunteer opportunities (e.g., setup, judging, coaching) for nonseniors and seniors alike, publicized by local media [25].

To participate in NSGA nationals, one must qualify in an NSGA-approved state competition and be at least 50 years old in the qualifying year. Medal sports include archery, badminton, basketball, bowling, cycling, golf, horseshoes, pickleball, race walk, racquetball, road race, shuffleboard, softball, swimming, table tennis, tennis, track and field, triathlon, and volleyball. In most sports, including
swimming, the top 4 finishers in each age group (50-54, $55-59, \ldots$.$) in state competitions are eligible to compete in$ the nationals.

We hypothesize (a) a nonlinear relationship between age and performance and (b) a greater slowdown for women than for men after age 50 . We investigate these hypotheses using both conventional and novel models, methods of estimation, and comparisons of performance as a function of gender and age.

## 2. Methods

Table 1 shows the number of entrants who completed the 500 -yard freestyle event in six consecutive NSGA competitions. Although as many as 200 could qualify within each gender ( 50 states times 4 per state), the actual participant counts are lower. Participation in the national games is affected by the host city's attractiveness and travel costs. The NSGA summer games last two weeks, so hotel and meal costs may discourage athletes who feel that their medal chances are too low to justify a trip. Moreover, athletes can qualify in up to six events (including track and field and other sports), so swimmers may choose only events where they have the best chance for a medal. Senior athletes may also face health issues that force them to drop out.

Table 2 shows the age distribution of participants in our data set. As expected, there are fewer participants in higher age categories (only one woman and no men in the 95-99 age category). The tabulation of individual participant names (with correction for inconsistent name spelling and crosschecking of ages) revealed that 215 swimmers had competed in multiple years. We assigned each swimmer a unique ID, yielding 678 unique participants. Our data, therefore, has a longitudinal as well as a cross-sectional component.

## 3. Results

We estimate the relationship between swim time (Time) and age (Age) for each gender separately (as opposed, say, to regression with a gender binary and interaction). All six years are pooled because our exploratory regressions revealed no consistent time trends. For men, exploratory regression revealed two extremely slow times (standardized residuals of 7.05 and 7.76), which we chose to omit in subsequent regressions. For women, one extremely slow swimmer (standardized residual 5.27) was retained as its effect on the overall fit was modest. Figure 1 shows a modelfree regression with time as the response and predictor dummy ( $0-1$ ) variables for each 5 -year age group. Average times increase more than linearly with age, with a possible trend break starting in the 80-84 age group.

Table 3 shows estimates of three continuous models of the time-age relationship. We used ordinary least squares (OLS) regression for the quadratic and semilog models and Excel's Solver for the exponential model. For comparability, we calculate $R^{2}$ and standard error from fitted model predictions for semilog models (semilog residuals are reported in log form) and Solver models (gradient estimation produces no residuals).

Table 1: NSGA biennial venues and 500-yard freestyle competitors.

| 2009 | San Francisco, CA | $n=199(89$ men, 110 women $)$ |
| :--- | :---: | :---: |
| 2011 | Houston, TX | $n=189(76$ men, 113 women $)$ |
| 2013 | Cleveland, OH | $n=178(83$ men, 95 women $)$ |
| 2015 | Minneapolis, MN | $n=158(78$ men, 80 women $)$ |
| 2017 | Birmingham, AL | $n=154(69$ men, 85 women $)$ |
| 2019 | Albuquerque, NM | $n=177(73$ men, 104 women $)$ |

Table 2: Swimmers by age group.

| Age | Men | Women | Total |
| :--- | :---: | :---: | :---: |
| $50-54$ | 34 | 53 | 87 |
| $55-59$ | 54 | 88 | 142 |
| $60-64$ | 89 | 106 | 195 |
| $65-69$ | 91 | 93 | 184 |
| $70-74$ | 81 | 103 | 184 |
| $75-79$ | 53 | 71 | 124 |
| $80-84$ | 32 | 52 | 84 |
| $85-89$ | 26 | 13 | 39 |
| $90-94$ | 8 | 7 | 15 |
| $95-99$ | -- | 1 | 1 |
| Total | 468 | 587 | 1055 |

The quadratic form implies a turning point. Equating $d$ (Time) $/ d$ (Age) to zero and solving we get Age $=39$ for the women and Age $=51$ for the men as the "best" age. However, because our sample did not cover swimmers below age 50, the utility of this result is doubtful. Yet this finding is consistent with research showing that elite women swimmers start to slow down at an earlier age than male swimmers [13, 23]. Regarding gender, the semilog slope for women (0.0209 Age) exceeds that of men ( 0.0196 Age), implying a more rapid increase in time with increasing age.

An attraction of the Solver (exponential form) is that it allows the Age exponent to vary. We set its origin at 50 to specify a monotonic increase in swim times after age 50 . Our Solver exponents are less than 2 , in contrast to the quadratic model whose quadratic term ( $\mathrm{Age}^{2}$ ) always has an exponent of 2. The exponent for women (Age ${ }^{1.699}$ ) exceeds that of men (Age ${ }^{1.639}$ ), which suggests that women's times increase more rapidly than men's after age 50.

Table 4 shows that semilog predicted times are consistently less than those from the quadratic, especially after age 80. For women, OLS and Solver give similar predictions. Despite their differences in form, Solver's predictions closely match the quadratic at all ages for women and for men, except at the highest and lowest ages. As far as we know, no previous research has explored allowing the age exponent to vary in this way. This topic may merit further scrutiny. However, because the quadratic is more commonly used and is easier to estimate, we will omit the Solver (exponential) model from further discussion here.

Next, we used quantile regression to estimate $25 \%, 50 \%$, and $75 \%$ quantiles (Table 5). An advantage of quantile regression is that it lessens the impact of unusual observations (e.g., extremely slow swimmers) as well as allowing estimation ofspecific percentiles. Because of sparse data for higher age groups, a finer breakdown (e.g., deciles) is not


Figure 1: Predicted swim times by age group.

Table 3: OLS regressions and solver estimates.

|  | Fitted model | $R^{2}$ | Std err |
| :--- | :---: | :---: | :---: |
| Men $(n=466)$ | Time $=1142.9-29.338$ Age +0.28783 Age $^{2}$ |  |  |
| Quadratic | Time $=\exp (4.8573+0.019601$ Age $)$ | 0.5556 | 100.19 |
| Semilog | Time $=363.582+(\text { Age }-49)^{1.6394}$ | 0.5305 | 98.53 |
| Solver |  | 0.5469 |  |
| Women $(n=587)$ | Time $=764.03-17.894$ Age +0.22788 Age ${ }^{2}$ | 0.5169 | 126.51 |
| Quadratic | Time $=\exp (4.9730+0.020885$ Age $)$ | 127.33 |  |
| Semilog | Time $=450.301+(\text { Age-49 })^{1.69903}$ | 0.5099 | 126.59 |
| Solver |  | 0.5163 |  |

Note. Quadratic and semilog results are from Stata's reg procedure with bootstrap standard error. All regression coefficients are highly significant. Solver coefficient estimates are from Excel's Generalized Reduced Gradient method.

Table 4: Predictions from three models.

|  |  | Men $(n=466)$ |  | Women $(n=487)$ |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Age | Quad | Semilog | Solver | Quad | Semilog |  |
| 50 | 396 | 343 | 365 | 439 | 410 |  |
| 60 | 419 | 417 | 415 | 511 | 506 |  |
| 70 | 500 | 507 | 511 | 628 | 623 | 451 |
| 80 | 638 | 617 | 642 | 791 | 509 |  |
| 90 | 834 | 751 | 804 | 999 | 627 |  |

practical. Because quantile regression minimizes the sum of the absolute residuals rather than the sum of the squared residuals, the software does not report a comparable standard error or $R^{2}$. If needed, those statistics can be generated by making predictions and summing the squared errors.

For both genders, the semilog slope (coefficient of the Age term) of the 75th percentile (the slowest swimmers) exceeds that of the 25th percentile (fastest swimmers). That is, the fastest swimmers' performance declines more slowly with Age. As with the OLS estimates, the coefficients of the age terms in the semilog model suggest that women's times increase faster than men's after age 50.

Figure 2 shows quantiles for the quadratic plotted for each gender. An aspiring swimmer who hopes to compete in the NSGA Summer Games could use these quantiles to assess his/her relative standing against recent competitors in national NSGA competitions. Given the typical number of

NSGA competitors in each age group, a swimmer in the fastest 25 percent would have a reasonable chance of placing in the top 8, thereby qualifying for recognition on the winner's dais (although only the top 3 receive medals).

Table 6 illustrates that the OLS prediction (conditional mean) generally lies above the $50 \%$ quantile prediction (conditional median). The 50\% coefficient estimates are less affected by high extremes (unusually slow swimmers).

Table 7 shows that predictions from the semilog quantiles match those of the quadratic quantiles up to about age 75 but diverge noticeably for higher ages (especially for men).

We hypothesize that female swimmers slow down at a greater rate than male swimmers after a certain age. To focus explicitly on age-related change within each gender (as opposed to comparisons between genders), we express predicted times relative to the age of 50 using an index (age

Table 5: Quantile regression benchmarks.

| Men $(n=466)$ <br> Quantile | Quadratic model |  |
| :--- | :---: | :---: |
| $25 \%$ | Time $=769.30-17.994$ Age $+0.19044 \mathrm{Age}^{2}$ | Semilog model |
| $50 \%$ | Time $=1037.10-26.872 \mathrm{Age}+0.27113 \mathrm{Age}^{2}$ | Time $=\exp (4.9078+0.017181 \mathrm{Age})$ |
| $75 \%$ | Time $=1259.77-34.071 \mathrm{Age}+0.34075 \mathrm{Age}^{2}$ | Time $=\exp (4.8508+0.019357 \mathrm{Age})$ |
| Women $(n=587)$ |  |  |
| Quantile | Quadratic model | Semilog model |
| $25 \%$ | Time $=975.222-24.163$ Age $+0.25293 \mathrm{Age}^{2}$ | Time $=\exp (5.0279+0.017915$ Age $)$ |
| $50 \%$ | Time $=1006.75-26.088 \mathrm{Age}+0.29046 \mathrm{Age}^{2}$ | Time $=\exp (4.8820+0.021932 \mathrm{Age})$ |
| $75 \%$ | Time $=639.46-14.587 \mathrm{Age}+0.21992 \mathrm{Age}^{2}$ | Time $=\exp (4.9627+0.022685 \mathrm{Age})$ |

Note. Quantiles are estimated using Stata's bsqreg procedure with bootstrapped standard errors.


Figure 2: Quantiles for fitted quadratic model.

Table 6: Predicted times for selected ages using quadratic model.

| Age Men | Women |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | OLS | $25 \%$ | $50 \%$ | $75 \%$ | OLS | $25 \%$ | $50 \%$ | $75 \%$ |
|  | 396 | 346 | 371 | 408 |  | 439 | 399 | 429 |
| 460 |  |  |  |  |  |  |  |  |
| 60 | 419 | 375 | 401 | 442 | 511 | 436 | 487 | 556 |
| 70 | 500 | 443 | 485 | 544 |  | 628 | 523 | 604 |
| 80 | 638 | 549 | 623 | 715 | 791 | 661 | 779 | 880 |
| 90 | 834 | 692 | 815 | 953 |  | 999 | 849 | 1012 | 1108.

Table 7: Predicted times for selected ages using semilog model.

| Age | Men |  |  |  | Women |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | OLS | $25 \%$ | $50 \%$ | $75 \%$ | OLS | $25 \%$ | $50 \%$ | $75 \%$ |
| 50 | 343 | 320 | 337 | 359 |  | 410 | 374 | 395 |
| 445 |  |  |  |  |  |  |  |  |
| 60 | 417 | 379 | 408 | 449 | 506 | 447 | 492 | 558 |
| 70 | 507 | 451 | 496 | 561 |  | 623 | 535 | 612 |
| 700 |  |  |  |  |  |  |  |  |
| 80 | 617 | 535 | 601 | 703 |  | 768 | 640 | 762 |
| 978 |  |  |  |  |  |  |  |  |
| 90 | 751 | 635 | 730 | 879 |  | 946 | 765 | 949 |

$50=1.00$ ). The quadratic model (Figure 3(a)) does show a more rapid slowdown for women, at least until age 70. The semilog model (Figure 3(b)) agrees that women slow down more rapidly with age, on average. Thus, the evidence supports our hypothesis.

## 4. Discussion

To capture nonlinearity, other researchers have often used the quadratic model [2, 3, 9-11]. Other methods include linear regression [1, 4], the semi-log model [6], hybrid models [4], and GLM [22]. In most studies (including ours), data are sparse at the highest ages, a problem noted by Rubin et al. [6]. Studies of the 800 m or 1500 m events [3,8] offer an approache somewhat comparable to ours (i.e., endurance events), although for elite athletes.

Other studies, e.g., [22], agree with our conclusion that women's performance declines faster than men's after age 50. Several researchers have suggested a possible point of inflection in athletic performance near age 70 or a bit later [ $2,3,5,8,9,23,27-29]$, as we have also suggested. A point of inflection implies a continuous monotonic function relating swim time to age. Mathematical issues aside, what physiological breakdown might create a discontinuity? Lazarus and Harridge [28] ask why there should be "an increased rate of decline occurring in many events at 70 and 80 years of age" (Leibniz's natura non facit saltus). They consider various explanations, concluding it is likely that "this breakpoint is a reflection of a decline in the synchrony and integration of the systems that go to make up whole-body performance" of physiological mechanisms [19, 31-33]. Yet, the search for a


Figure 3: Predicted ratios (age $50=1.00$ ).
single predictive model may be moot given the wide variation in competitive swimming performance at later ages. For swimmers aged 50-75, any of the several continuous models described in our paper would provide useful benchmarks.

While the role of gender in swimming has been studied $[2,8,13,18,26]$, along with the "peak" age question [2, 26, 27], we feel that our within-gender comparison provides a clearer focus on the role of gender on age-related performance decline.

## 5. Conclusion

Our use of quantile regressions and the semi-log model adds new perspectives on model estimation. Our analysis complements extant research on elite athletes showing that swim times are best predicted using a quadratic model based on age and gender, with more rapid slowing after age 50, especially for women. Our within-gender performance comparisons offer a new way to visualize performance declines by gender. Our study of NSGA competitors adds a new dimension to existing studies of FINA, Masters, and Olympic athletes, which we believe will inform and encourage a broader spectrum of senior swimmers. Over time, NSGA swim performance may become more comparable with Master's events as better-trained entrants enter the games [34]. We know of one other study [30] using NSGA data, although it was for track and field events. We hope that our work will stimulate the analysis of other NSGA sports.

## Data Availability

NSGA biennial competition swim times are publicly accessible (https://nsga.com/nsgresults/) by year, event, gender, and age group. Formatted data (Excel, CSV, or PDF) from this study are available upon request from the author David P. Doane.

## Conflicts of Interest

The authors declare that they have no conflicts of interest.

## References

[1] A. B. Baker and Y. Q. Tang, "Aging performance for Masters records in athletics, swimming, rowing, cycling, triathlon, and weightlifting," Experimental Aging Research, vol. 36, pp. 453-477, 2010.
[2] A. J. Donato, K. Tench, D. H. Glueck, D. R. Seals, I. Eskurza, and H. Tanaka, "Declines in physiological functional capacity with age: a longitudinal study in peak swimming performance," Journal of Applied Physiology, vol. 94, pp. 764-769, 2003.
[3] J. T. Fairbrother, "Prediction of $1500-\mathrm{m}$ freestyle swimming times for older Masters All-American swimmers," Experimental Aging Research, vol. 33, pp. 461-471, 2007.
[4] R. H. Rahe and R. J. Arthur, "Swim performance decrement over middle life," Medicine \& Science in Sports, vol. 7, no. 1, pp. 53-58, 1975.
[5] R. T. Rubin and R. H. Rahe, "Effects of aging in Masters swimmers: 40-year review and suggestions for optimal health benefits," Open Access Journal of Sports Medicine, vol. 8, pp. 39-44, 2010.
[6] R. T. Rubin, S. Lin, A. Curtis, D. Auerbach, and C. Win, "Declines in swimming performance with age: a longitudinal study of Masters swimming champions," Open Access Journal of Sports Medicine, vol. 4, pp. 63-70, 2013.
[7] J. Senefeld, M. J. Joyner, A. Stevens, and S. K. Hunter, "Sex differences in elite swimming with advanced age are less than marathon running," Scandinavian Journal of Medicine o Science in Sports, vol. 26, no. 1, pp. 17-28, 2016.
[8] H. Tanaka and D. R. Seals, "Age and gender interactions in physiological functional capacity: insight from swimming performance," Journal of Applied Physiology, vol. 2, no. 3, pp. 846-851, 1997.
[9] R. C. Fair, "Estimated age effects in athletic events and chess," Experimental Aging Research, vol. 33, no. 1, pp. 37-57, 2007.
[10] J. Stones and A. Kozma, "Adult age trends in record running performances," Experimental Aging Research, vol. 6, no. 5, pp. 407-416, 1980.
[11] M. J. Stones and A. Kozma, "Adult age trends in athletic performances," Experimental Aging Research, vol. 7, no. 3, pp. 269-280, 1981.
[12] M. J. Stones and A. Kozma, "Age by distance effects in running and swimming records: a note on methodology," Experimental Aging Research, vol. 12, no. 4, pp. 203-206, 1986.
[13] M. Wolfrum, B. Knechtle, C. A. Rüst, T. Rosemann, and R. Lepers, "Sex-related differences and age of peak performance in breaststroke versus freestyle swimming," $B M C$ Sports Science, Medicine and Rehabilitation, vol. 5, no. 29, pp. 1-10, 2013.
[14] A. Akkari, D. Machin, and H. Tanaka, "Greater progression of athletic performance in older Masters athletes," Age and Ageing, vol. 44, pp. 683-686, 2015.
[15] J. S. Katz and L. Katz, "Power laws and athletic performance," Journal of Sports Sciences, vol. 17, no. 6, pp. 467-476, 1999.
[16] B. Knechtle, P. T. Nikolaidis, S. König, T. Rosemann, and C. A. Rüst, "Performance trends in master freestyle swimmers aged 25-89 years at the FINA World Championships from 1986 to 2014," Age, vol. 38, no. 18, pp. 1-8, 2016.
[17] S. König, F. Valeri, S. Wild, T. Rosemann, C. A. Rüst, and B. Knechtle, "Change of the age and performance of swimmers across World Championships and Olympic Games finals from 1992 to 2013 - a cross-sectional data analysis," SpringerPlus, vol. 3, no. 652, pp. 1-13, 2014.
[18] S. Wild, C. A. Rüst, T. Rosemann, and B. Knechtle, "Changes in sex difference in swimming speed in finalists at FINA World Championships and the Olympic Games from 1992 to 2013," BMC Sports Science, Medicine and Rehabilitation, vol. 6, no. 25, pp. 1-29, 2014.
[19] P. Zamparo, G. Gatta, and P. di Prampero, "The determinants of performance in master swimmers: an analysis of master world records," European Journal of Applied Physiology, vol. 112, no. 10, pp. 3511-3518, 2012.
[20] M. I. Ferreira, T. M. Barbosa, M. J. Costa, H. P. Neiva, and D. A. Marinho, "Energetics, biomechanics, and performance in Masters' swimmers: a systematic review," The Journal of Strength \& Conditioning Research, vol. 30, pp. 2069-2081, 2016.
[21] P. Reaburn and B. Dascombe, "Endurance performance in Masters athletes," European Review of Aging and Physical Activity, vol. 5, no. 1, pp. 31-42, 2008.
[22] M. J. Stones, "Age differences, age changes, and generalizability in marathon running by Master athletes," Frontiers in Psychology, vol. 10, p. 2161, 2019.
[23] H. Tanaka and D. R. Seals, "Dynamic exercise performance in Masters athletes: insight into the effects of primary human aging on physiological functional capacity," Journal of Applied Physiology, vol. 95, no. 5, pp. 2152-2162, 2003.
[24] See https://www.michiganseniorolympics.org/.
[25] D. Kazburski, Michigan Senior Olympics Back in Full Force, The Oakland Press, 2021.
[26] C. A. Rüst, B. Knechtle, T. Rosemann, and R. Lepers, "The changes in age of peak swim speed for elite male and female Swiss freestyle swimmers between 1994 and 2012," Journal of Sports Sciences, vol. 32, no. 3, pp. 248-258, 2014.
[27] R. Schulz and C. Curnow, "Peak performance and age among superathletes: track and field, swimming, baseball, tennis, and golf," Journal of Gerontology, vol. 43, no. 5, pp. 113-120, 1988.
[28] N. R. Lazarus and S. D. R. Harridge, "Inherent ageing in humans: the case for studying master athletes," Scandinavian Journal of Medicine \& Science in Sports, vol. 17, pp. 461-463, 2007.
[29] B. Reider, "Live long and prosper," The American Journal of Sports Medicine, vol. 36, no. 3, pp. 441-442, 2008.
[30] V. J. Wright and B. C. Perricelli, "Age-related rates of decline in performance among elite senior athletes," The American Journal of Sports Medicine, vol. 36, no. 3, pp. 443-450, 2008.
[31] P. Zamparo, A. Dall'Ora, A. Toneatto, M. Cortesi, and G. Gatta, "The determinants of performance in master
swimmers: a cross-sectional study on the age-related changes in propelling efficiency, hydrodynamic position and energy cost of front crawl," European Journal of Applied Physiology, vol. 112, no. 12, pp. 3949-3957, 2012.
[32] J. Rittweger, A. Kwiet, and D. Felsenberg, "Physical performance in aging elite athletes-challenging the limits of physiology," Journal of Musculoskeletal and Neuronal Interactions, vol. 4, no. 2, pp. 159-160, 2004.
[33] J. Rittweger, P. E. di Prampero, N. Maffulli, and M. V. Narici, "Sprint and endurance power and ageing: an analysis of master athletic world records," Proceedings of the Royal Society Series B, vol. 276, pp. 683-689, 2009.
[34] H. Suominen, "Ageing and maximal physical performance," European Review of Aging and Physical Activity, vol. 8, no. 1, pp. 37-42, 2011.

