

## Derivations that enable the testing of fetal urine production as a method of fetal surveillance

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### Abstract

**Purpose** To calculate the measurement error of the hourly fetal urine production rate (HFUPR) and evaluate the implication of different methods for measuring the HFUPR, i.e. ellipsoid versus sum-of-cylinders method.

**Methods** The calculation was based on sonographic documentation of the increased bladder volumes during the filling phase, the bladder volume measurement error and the number and time points of bladder image capture.

**Results** The probability of a false pathological reading was excluded (0%) with the sum-of-cylinders method for gestational ages of  $\geq 30$  weeks. With the ellipsoid method, the risk was higher. The maximum changes which could be

exclusively explained by measurement error were four to five times greater with the ellipsoid method compared with the sum-of-cylinders method.

**Conclusions** The present paper illustrates a careful evaluation of the HFUPR measurement error and the implications of using different ultrasound methods for bladder volume estimations.

**Keywords** Fetus · Urinary bladder · Ultrasonography · Organ volume · Reliability

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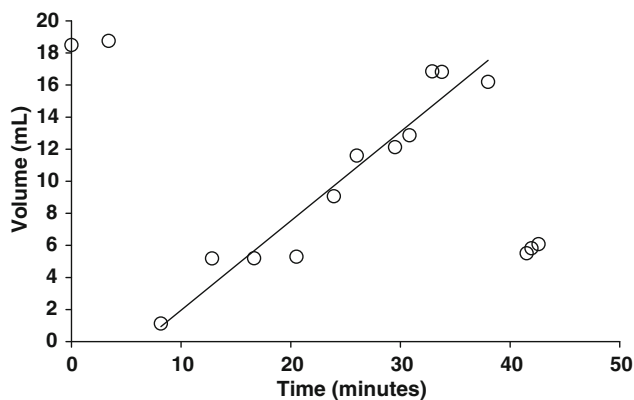
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### Introduction

The skillful management and timing of delivery in high-risk pregnancies is important in order to avoid a poor perinatal outcome [5, 16]. The challenge is the early identification of abnormal events. Different procedures to detect these abnormal events are available [6, 18]. However, the fetal urine production rate is a parameter that has not been utilised in clinical practice, even though several studies demonstrate a reduction in blood flow in the fetal renal arteries and urine production rate in compromised fetuses [8–10, 14, 19].

When utilising the hourly fetal urine production rate (HFUPR) to detect abnormal events during pregnancy, reliable reference HFUPR values for normality are needed. Several attempts have been made to assess these values. However, previous ultrasound studies have presented widely varying reference ranges for fetuses of identical gestational ages. For example, at term, the presented values have varied from as much as 28, 34, 51 and 71–125 mL/h [1, 7, 11, 12, 17]. The huge variation was also present, regardless of whether the 2D or 3D technique was used, suggesting considerable measurement errors. Furthermore, detailed data on the total measurement error in these



**Fig. 1** Initially, the bladder was filled up to 19 ml before emptying and a new filling phase began. For this 32-week fetus, the HFUPR of 33 mL/h was estimated by regression function and extrapolation to a time span of 1 h

studies are missing. This is unsatisfactory and a systematic investigation of the accuracy of HFUPR measurements is therefore needed.

When carrying out a systematic investigation of the accuracy of HFUPR measurements, it is important to recognize that the accuracy of HFUPR measurement in living fetuses cannot be assessed directly but only indirectly. The measurement error is made when assessing the volume of the bladder and only here. This measurement error will also be incorporated in the HFUPR estimation, which is based on a sequence of bladder images during the filling phase. There are some other factors that influence the HFUPR measurement error, i.e. the magnitude of the HFUPR and the number and time points of bladder image capture (Fig. 1).

In the current paper we illustrate the mathematical derivation of a formula to assess the HFUPR measurement error using these factors and the implication of using different methods for bladder volume. The objective of the paper was to enable responses to two clinically important questions: (1) what is the probability that the HFUPR will be falsely classified at the 2.5th percentile or a lower value, even though the true HFUPR is at a higher percentile point? and (2) if we are to use the HFUPR in the evaluation of at-risk pregnancies by daily measurements, we need to know how much of the change can be explained exclusively by measurement error.

## Methods and subjects

In spite of a constant volume, varying estimates will be found when assessing the volume of the fetal urinary bladder, due to measurement error [1–4]. This error was assumed to have a normal distribution and the standard deviation (SD) was therefore used as a measurement of estimation error (by us denoted  $SD_{\text{VOLUME}}$ ). This volume measurement

error will be incorporated in the HFUPR estimation and the SD was consequently also utilized as the measurement of HFUPR estimation error (by us denoted  $SD_{\text{HFUPR}}$ ).

To obtain a generally applicable formula for estimating  $SD_{\text{HFUPR}}$ , a mathematical derivation was applied (see Statistics section). Although it is an original derivation it can be scrutinized by each statistician without difficulty. It is pure mathematics. In clinical practice, there are two fundamental questions that need to be answered: (1) what is the probability that the HFUPR will be falsely classified at the 2.5th percentile or a lower value, even though the true HFUPR is at a higher percentile point? and (2) If we are to use the HFUPR in the evaluation of at-risk pregnancies by daily measurements, we need to know how much of the change can be explained exclusively by measurement error. These questions were answered by two supplementary formulas.

To illustrate the implication of the calculated  $SD_{\text{HFUPR}}$ , relevant values of HFUPR,  $SD_{\text{VOLUME}}$  number and time points of bladder image capture were required. The reference range of the HFUPR in an extensive 2D study (comprising 358 uncomplicated fetuses) was used and the 2.5th and 10th percentile point were calculated from a diagram in that study [15]. To date, detailed information on  $SD_{\text{VOLUME}}$  in living fetuses has been exclusively presented in studies of 2D ultrasound. To compare the implication of using different bladder volume methods (the ellipsoid or the sum-of-cylinders method), the calculated  $SD_{\text{VOLUME}}$  in two other 2D studies was applied [2, 4].

## Statistics

The measurement error when estimating the HFUPR

Assuming that  $x_1, x_2, \dots$  are the time points for bladder volume estimations during the filling phase (small letters for constants) and  $Y_1, Y_2, \dots$  are the estimated bladder volumes (capital letters for random variables), the HFUPR can be calculated as the coefficient of regression:

$$\text{HFUPR} = \frac{\sum Y_i (x_i - \bar{x})}{\sum (x_i - \bar{x})^2} \quad (1)$$

This derivation of the coefficient of regression can be found in a number of statistical manuals.

The SD of the bladder volume measurements was assumed to be a linear function of volume.

$$SD_{\text{volume}} = a + b \times \text{volume} \quad (2)$$

The volume  $Y_i$  at the time point  $x_i$  can be approximated as

$$Y_i = x_i \times \text{HFUPR} \quad (3)$$

and

$$SD_{\text{volume}} = a + b \times x_i \times \text{HFUPR}. \quad (4)$$

The different measurement errors, which are involved in each volume estimation during a filling phase, are regarded as statistically independent random variables.

When calculating  $SD_{\text{HFUPR}}$ , the corresponding variances are used. The variance in the HFUPR according to Eq. 1 equals the variance in  $\frac{\sum Y_i (x_i - \bar{x})}{\sum (x_i - \bar{x})^2}$ . The factors  $(x_i - \bar{x})$  and  $\sum (x_i - \bar{x})^2$  can be regarded as constants in this application.

Only the factor  $(Y_i)$  must be taken into consideration and the variance  $[SD(Y_i)]^2$  is used.

$$\text{SD}(Y_i) = SD_{\text{volume}} \quad (5)$$

according to Eqs. 4 and 5,  $[SD(Y_i)]^2 = (SD_{\text{volume}})^2 = (a + b \times x_i \times \text{HFUPR})^2$ .

Referring to Eq. 1, the variance in the measurement error when estimating the HFUPR is:  $(SD_{\text{HFUPR}})^2 = \text{Var} \left[ \frac{\sum Y_i (x_i - \bar{x})}{\sum (x_i - \bar{x})^2} \right]$  and according to Eqs. 4 and 5:

$$(SD_{\text{HFUPR}})^2 = \frac{\left\{ \frac{\sum (a + b \times x_i \cdot \text{HFUPR}) (x_i - \bar{x})}{\sum (x_i - \bar{x})^2} \right\}^2}{\sum (x_i - \bar{x})^2} = \frac{\sum (a + b \times x_i \times \text{HFUPR})^2 (x_i - \bar{x})^2}{\left[ \sum (x_i - \bar{x})^2 \right]^2}$$

and

$$SD_{\text{HFUPR}} = \frac{\left[ \sum (a + b \times x_i \times \text{HFUPR})^2 (x_i - \bar{x})^2 \right]^{1/2}}{\sum (x_i - \bar{x})^2}. \quad (6)$$

Using the valid values for the constants  $a$  and  $b$ , the mean time for bladder image documentation  $\bar{x}$  and the time points when images were captured, the  $SD_{\text{HFUPR}}$  turned out to be an approximately linear function of the HFUPR and can be expressed as:

$$SD_{\text{HFUPR}} = c + d \times \text{HFUPR}. \quad (7)$$

The values of the constants  $c$  and  $d$  depend on the  $SD_{\text{VOLUME}}$  and time points for bladder image capture.

The statistical derivations relating to the two clinical examples

1. What is the maximum change in the HFUPR that could be caused exclusively by measurement errors?

Assuming that the actual  $\text{HFUPR} = x$  on two occasions, what is the probability that the difference between these two determinations (in spite of a

constant HFUPR) is at least as extreme as a quantity  $\Delta$ ? Assuming that  $\Phi$  is the distribution function of the standardized normal distribution, the probability of assessing an HFUPR, which is a magnitude of  $\Delta$  less than 0, is:

$$\Phi \left( \frac{0 - \Delta}{SD} \right). \quad (8)$$

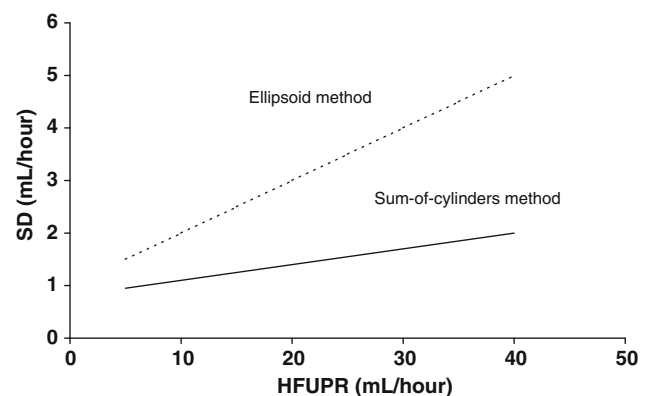
However, in this example,  $SD = SD_{\text{HFUPR}} \times \sqrt{2}$ , whereas  $\sqrt{2}$  depends on the evaluation of a difference and  $SD_{\text{HFUPR}} = c + d \times x$  according to (7). The probability that the difference between two determinations is at least as extreme as a quantity  $\Delta$  is:  $2 \times \Phi \left( \frac{-|\Delta|}{(c+d \times x) \sqrt{2}} \right)$ . For example, the probability attains a value of 5% if

$$\Delta = \pm 1.96 \left[ (c + d \times x) \sqrt{2} \right]. \quad (9)$$

2. What is the probability that the HFUPR will be falsely classified at the 2.5th percentile or a lower value, whereas the true HFUPR is at the 10th percentile point?

When the true HFUPR is exactly at the 10th percentile point ( $x_{10}$ ), the measured HFUPR will have a normal distribution with the mean value ( $x_{10}$ ). In line with the discussion in the previous example, the difference is  $x_{2.5} - x_{10}$  and the standard deviation  $SD = SD_{\text{HFUPR}} = c + d \times x_{10}$ . The probability of obtaining an HFUPR value less than the 2.5th percentile can be calculated as

$$\Phi \left( \frac{x_{2.5} - x_{10}}{c + d \times x_{10}} \right). \quad (10)$$



**Fig. 2** This calculation of the HFUPR measurement error ( $SD_{\text{HFUPR}}$ ) was based on images captured at five, 10, 15, 20, 25 and 30 min after an emptying phase, when applying the ellipsoid and the sum-of-cylinders method (different  $SD_{\text{VOLUME}}$ ). The  $SD_{\text{HFUPR}}$  ranged from 31 to 12% for the ellipsoid method and from 20 to 5% for the sum-of-cylinders method for HFUPRs of 5–40 mL/h

**Table 1** The influence of different numbers and times of image capture is illustrated for some situations, when calculating the  $SD_{HFUPR}$  ( $SD_{HFUPR} = c + d \times HFUPR$ )

Number and time points of volume estimations	$SD_{HFUPR}$	
	Ellipsoid method	Sum-of-cylinders method
6 (time points: 1, 2, 3, 4, 5, 6)	$1.0 + 0.10 \times HFUPR$	$0.8 + 0.03 \times HFUPR$
5 (time points: 1, 2, 3, 4, 6)	$1.1 + 0.12 \times HFUPR$	$0.9 + 0.03 \times HFUPR$
4 (time points: 1, 2, 3, 4)	$1.9 + 0.13 \times HFUPR$	$1.6 + 0.03 \times HFUPR$
3 (time points: 1, 2, 4)	$2.0 + 0.14 \times HFUPR$	$1.6 + 0.04 \times HFUPR$
2 (time points: 1, 3)	$3.0 + 0.15 \times HFUPR$	$2.5 + 0.04 \times HFUPR$
2 (time points: 1, 6)	$1.1 + 0.12 \times HFUPR$	$1.0 + 0.03 \times HFUPR$

The alternative image capture times (time points 1–6) were five, 10, 15, 20, 25 and 30 min after an emptying phase. It can be seen that  $SD_{HFUPR}$  is based on whether the time intervals between image capture are 10 or 25 min (rows 5 and 6). Moreover, the calculated  $SD_{HFUPR}$  is dependent on the volume estimation method that was used

## Results

The SD for the estimated HFUPR ( $SD_{HFUPR}$ ) depends on the method of bladder volume estimation ( $SD_{VOLUME}$ ), the magnitude of the HFUPR and the number and time points of bladder image capture. The derivation was presented in Formulas 6 and 7 in the Statistics section. The new

constants  $c$  and  $d$  in Eq. 7 are crucial for the further derivations (Fig. 2; Table 1).

The probability of falsely reading the 10th percentile point as a pathological value (i.e. below the 2.5th percentile point) was excluded (0%) with the sum-of-cylinders method for gestational ages of  $\geq 30$  weeks (see Formula 10, Statistics section). With the ellipsoid method, the risk was higher (Table 2).

Using Formula 9 (Statistics section), the maximum changes which might be exclusively explained by measurement error were four to five times greater (25–30%) with the ellipsoid method compared with the sum-of-cylinders method (6%) (Table 3).

## Discussion

A starting point for the present paper is the linear relationship between bladder volume and the measurement error:  $SD_{VOLUME} = a + b \times \text{volume}$ . This relationship has been thoroughly documented in three previous studies [2, 3, 4]. When all the cases in these studies are included, the distribution of the SD and residuals supports a linear relationship, which is a prerequisite for using a linear regression function [13] (Figs. 3 and 4).

The main finding in the present paper is a general formula for calculating the  $SD_{HFUPR}$ , which is valid when using 2D ultrasound. As we understand it, this measurement error can only be assessed indirectly by this kind of calculation. The measurement error is made when assessing the volume of

**Table 2** Shows the probability of false HFUPR readings at the 2.5th percentile point or a lower level, even though the true HFUPR was at the 10th percentile point

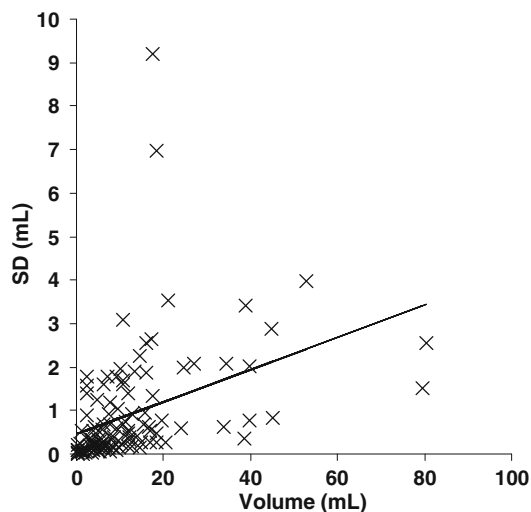
	Gestational age (weeks)	Mean (mL/h)	10th percentile (mL/h)	2.5th percentile (mL/h)	Probability (per cent)	
					Ellipsoid method	Sum-of-cylinders method
	22	7.4	4.3	2.7	13	5
	23	8.4	5.1	3.3	12	4
	24	9.4	5.8	3.9	11	3
	25	10.4	6.6	4.5	10	2
	26	11.5	7.3	5.1	10	2
	27	12.2	8.0	5.7	10	2
	28	12.9	8.6	6.3	10	2
	29	15.1	9.9	7.1	7	1
	30	17.4	11.3	8.0	6	0
	31	21.0	12.7	8.3	2	0
	32	24.7	14.7	9.3	1	0
	33	27.8	16.8	11.0	1	0
	34	30.9	19.0	12.7	1	0
	35	35.3	21.9	14.8	1	0
	36	39.7	24.9	17.1	2	0
	37	41.0	26.5	18.7	2	0
	38	42.4	28.0	20.4	2	0

The ellipsoid and the sum-of-cylinders methods were compared (different  $SD_{VOLUME}$ ). For the sum-of-cylinders method, the number of false readings was  $<3\%$  for fetuses of  $>24$  weeks

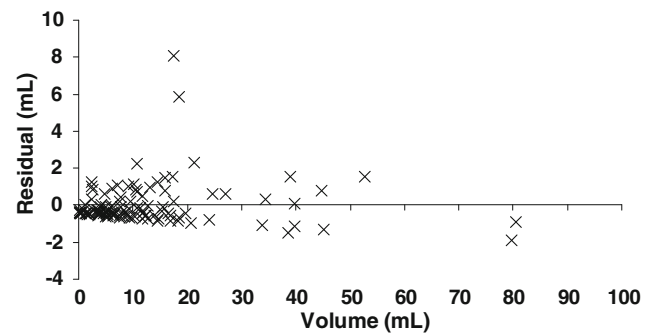
**Table 3** The magnitude of change in the estimated HFUPR from the initial 10th percentile point, which might be caused exclusively by measurement error, was calculated

Gestational age (weeks)	10th percentile (mL/h)	Measurement error (mL/h)	
		Ellipsoid method	Sum-of-cylinders method
22	4.3	1.2	0.3
23	5.1	1.3	0.3
24	5.8	1.6	0.4
25	6.6	1.7	0.4
26	7.3	1.9	0.4
27	8.0	2.1	0.5
28	8.6	2.3	0.5
29	9.9	2.6	0.6
30	11.3	3.0	0.7
31	12.7	3.4	0.8
32	14.7	3.9	0.9
33	16.8	4.4	1.0
34	19.0	5.0	1.1
35	21.9	5.8	1.3
36	24.9	6.6	1.5
37	26.5	7.7	1.6
38	28.0	7.4	1.7

Values higher than these may also be produced by measurement errors, but the probability was less than 5%. The change, which might be due exclusively to measurement error, is just a quarter when using the sum-of-cylinders method vs. the ellipsoid method

**Fig. 3** The SD was calculated when estimating the bladder volume of 120 fetuses. Different methods were used, which gave rise to 222 relationships between SD and bladder volume. The maximum and minimum bladder volumes were 80.5 and 0.1 mL, respectively. The distribution of the SDs supports a linear relationship

the bladder—and only then. When the linear relationship between the bladder volume and measurement error is taken into consideration, there is a specific  $SD_{VOLUME}$  related to each estimated volume. The magnitude of the constants  $a$  and  $b$  depends on the volume assessment method that is used, e.g. 2D ultrasound (ellipsoid and sum-of-cylinders method). The  $a$  and  $b$  for the ellipsoid method are 0.36516 and 0.09978, whereas they are 0.29911 and 0.02788 for the sum-of-cylinders method. For 3D ultrasound, the

**Fig. 4** The distribution of the residuals supports a linear relationship between the SD and bladder volume based on 222 relationships between the SD and bladder volume. The maximum and minimum of the residuals were 8.2 and  $-1.9$  mL, respectively. The mean was 0.00 mL and the median  $-0.37$  mL

relationship between  $SD_{VOLUME}$  and the estimated volume is as yet unknown. However, the current paper illustrates the usefulness of this relationship and the implication of using different 2D methods for volume estimation.

When utilizing the HFUPR for fetal surveillance, we need to know whether the estimated HUFPR is pathologically low, i.e. below the 2.5th percentile point. We therefore need to answer the question: What is the risk of false readings at the 2.5th percentile point, for example, even though the true HFUPR is at a higher percentile point? (see Formula 10 in Statistics).

Furthermore, we need to answer the question: How much of an observed HFUPR change (for example, during daily controls) can be explained exclusively by measurement error? (see Formula 9 in Statistics).

In some previous ultrasound studies, the quality of bladder volume as well as HFUPR measurements has been addressed [7, 11, 12, 17]. These studies lack detailed measurement error data and are not sufficient as a basis for HFUPR evaluation. With the assistance of our mathematical derivations of the  $SD_{HFUPR}$ , however, the answers to the two questions are within reach. Only three data are needed to obtain the  $SD_{HFUPR}$ : (1) the relationship between bladder volume and  $SD_{VOLUME}$  for the estimation method that is used (determines the constants  $a$  and  $b$ ), (2) the time points of image capture and (3) the estimated HFUPR. According to Statistics, there is also a linear relationship between  $SD_{HFUPR}$  and the HFUPR. This relationship  $SD_{HFUPR} = c + d \times HFUPR$  can be utilised for further calculations of the constants  $c$  and  $d$ , which provides the answers to the aforementioned questions. Moreover, the implication of using different methods for bladder volume is illustrated.

## Conclusions

When  $SD_{HFUPR}$ , the magnitude of the HFUPR and the time points of bladder image capture are taken into account, there is a probability of falsely classifying the HFUPR at the 2.5th percentile or a lower value, even though the true HFUPR at the 10th percentile point may be estimated. Moreover, when evaluating at-risk pregnancies by daily HFUPR measurements, we can assess how much of the change can be explained exclusively by measurement error.

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**Conflict of interest statement** None.

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