

Article



Simulation of the Continuous Casting and Cooling Behavior of Metallic Glasses

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Abstract: The development of melt spinning technique for preparation of metallic glasses was summarized. The limitations as well as restrictions of the melt spinning embodiments were also analyzed. As an improvement and variation of the melt spinning method, the vertical-type twin-roll casting (VTRC) process was discussed. As the thermal history experienced by the casting metals to a great extent determines the qualities of final products, cooling rate in the quenching process is believed to have a significant effect on glass formation. In order to estimate the ability to produce metallic glasses by VTRC method, temperature and flow phenomena of the melt in molten pool were computed, and cooling rates under different casting conditions were calculated with the simulation results. Considering the fluid character during casting process, the material derivative method based on continuum theory was adopted in the cooling rate calculation. Results show that the VTRC process has a good ability in continuous casting metallic glassy ribbons.

Keywords: metallic glass; critical cooling rate; twin-roll casting; simulation

1. Introduction

Amorphous metallic alloys exhibit outstanding mechanical, magnetic, and chemical properties that are unusual for solid metals. More than half a century has passed since Pol Duwez reported his remarkable findings in 1960 [1], and the subject area has moved a long way. Once the potential of metallic glasses for any certain application was recognized, it was seen that a scaling-up method was needed to deploy metallic glasses commercially [2]. To produce metallic glasses continuously, in the early 1970s, researchers at Allied Chemical Corporation developed continuous casting or melt spinning processes for commercial manufacture of metallic glasses started gaining momentum [3–7]. Relations between processing parameters and ribbon quality and dimensions have been discussed by some researchers in recent years [8–11]; however, only a small fraction of the metallic glasses have so far been commercially deployed mainly due to the difficulty in obtaining good quality in such thin products. For applications in transformer cores, metallic glasses such as Metglas[®] Alloy 2605SA1 can reduce transformation losses by 70% compared to crystalline iron cores [2,12].

In the melt spinning process, conditions between the roll-contact surface and free surface of ribbon are different, and these will affect the final ribbon quality [9,13]. In contrast, metallic ribbons produced by twin-roll casting technique are casted and hot rolled at the same time and a better surface quality is expected. The concept of continuous casting in a single stage dates back to Bessemer, in 1846, who envisioned using a twin-roll technique to cast steel strips [14], but technical realization was more than a century later. In 1970, after Duwez's seminal discoveries, a twin-roll casting (TRC) technique

for preparing uniform films of metastable phases was devised by Chen and Miller [15]. To date, this technique in producing metallic glass ribbons is still almost limited to laboratory scale studies [16–22]. It turns out that TRC is an available process for producing amorphous alloy sheets with a wide range of cooling rates. Nevertheless, most of the studies so far have been based on horizontal type twin-roll casters. Studies on TRC technique for producing metallic glasses are listed in Table 1.

Year	Туре	Cooling Rate (K/s)	Speed (rpm)	References
1970	Vertical	10 ⁵	100-5000	[15]
1974	Vertical	10^{5}	—	[16]
2005	Horizontal	$10^2 - 10^3$	1, 3	[17,18,23]
2007	Horizontal	—	0.75 m/s	[20]
2010	Horizontal	—	102 m/s	[22]
2013	Vertical	$1-10^{3}$	—	[21]

Table 1. Papers on the research of twin-roll casting (TRC) of metallic glasses.

Because the influence of gravity, it shows that the casting speed of vertical type twin-roll casting (VTRC) is higher than horizontal-type twin-roll casting (HTRC), and the heat transmission of the former is more effective [24–26]. In the present study, based on the VTRC process, thermal history experienced by metallic materials during casting process was computed, and the cooling rate was also calculated. In order to make a judgment on the process cooling ability in producing metallic glasses, a continuous cooling transformation (CCT) diagram was proposed. The influences of casting parameters on glass forming were discussed. As Al-rich metallic glasses are interesting lightweight alloys with a high specific strength (compressive fracture strength exceeded 1000 MPa) which make them a potential material for aerospace applications [27,28], material property parameters of high aluminum alloys (Al contents as high as 35–40 at %, e.g., Al₃₅La₅₀Ni₁₅) are adopted in this paper.

2. TRC Simulation

Amorphization or crystallization can occur depending on the cooling rates and thermal behavior experienced by the melt [17,25]. For a better understanding of the solidification behavior of TRC process, thermal flow simulation was carried out based on the condition of a pilot vertical twin-roll caster with roll radius of 150 mm, roll width of 100 mm. Figure 1 shows the schematic of TRC process, with melt supplied in two ways (i.e., center pouring mode shown in Figure 1a, and one side pouring mode shown in Figure 1b). Because the ratio of the width to thickness is quite large, if one ignores the effect of side dams, a 2D finite element method (FEM) model is used. Considering the high speed feeding flow of liquid metal during the strip casting process, flow phenomenon in the molten pool is characterized as turbulent flow. Moreover, the following assumptions are made for steady-state simulations: there is no relative slip between the roll and strip, and heat transfer coefficient between them is constant (i.e., 18 kW·m⁻²·K⁻¹); surface temperature of the roller is 373 K; free surface of the melt is steady. Influences of melt level *h*, strip thickness δ , casting speed *v* (i.e., rotating speed) and pouring temperature T_p are considered in simulation. Considering geometric symmetry of the center pouring mode (i.e., Figure 1a), half of the twin-roll casting model was employed.



Figure 1. Schematic of TRC process: (a) Center pouring mode; (b) One side pouring mode.

Figure 2 illustrates the formation of the molten pool of the one side pouring mode. The process and dimensions are specified as follows: the melt is ejected on one roll through a nozzle, a strip shell forms along the roll surface, and the strip shell thickness is marked as d, which has the same value as nozzle. The metal shell of this part is cooled by the roll (the metal-roll contact side) and the atmosphere around it (the metal-air contact side), nearly the same as melt spinning process. As the metal shell rolling down towards to the nip, it contacts to the other side roll, and the height to the nip from this location is marked as h. The metal of this part is cooled by both of the rolls. In Figure 2a, h, which is marked as h_a , depends on the metal shell thickness d and the roll gap. We can get a larger value of h with a smaller roll gap under a certain metal shell thickness d. In Figure 2b, a molten liquid level has formed, and h here is marked as h_b , which is higher than h_a under the same metal shell thickness and roll gap, and can change independently. With the effect of roll pressure (i.e., roll separating force), a thin solidified strip forms and escapes from the roll nip. The total height of the molten pool is marked as L.



Figure 2. Schematic of the molten pool of one side pouring mode: (a) h_a depends on the roll gap and *d*; (b) $h_b > h_a$ and can change independently.

3. Calculation of Time Reduced Temperature Transformation (T-T_r-T) and CCT Diagrams

3.1. Calculation of T- T_r -T Diagram

The following equation based on the steady-state homogeneous nucleation theory proposed by Davies and derived by Inoue [29]:

$$t = \left\lfloor \frac{31}{k} \left(\frac{xa_0^9}{N_v} \right)^{1/4} \right\rfloor \times \left[\frac{1}{T_r \Delta T_r^{3/4}} \exp\left(\frac{0.268}{T_r^3 \Delta T_r^2} \right) \exp\left\{ \frac{2}{5} \left(\frac{T_r}{\Delta T_r} \right)^{3/4} \right\} \right] \times \left[\eta_{0r} \exp\left(\frac{B_r}{T_r - T_{0r}} \right) \right]$$
(1)

Equation (1) gives a time transformation curve (C-curve) that expresses the time to transform to crystal as a function of temperature. Here, *k* is the Boltzmann constant, *x* is the fraction of crystal formed in time *t*, and a volume fraction of 10^{-6} as a just-detectable concentration of crystals was used [30]. a_0 is the mean atomic diameter, N_v is the volume concentration of atoms. T_r (= T/T_m) is the reduced temperature, and ΔT_r (= $1 - T_r$) is the reduced undercooling of the melt. B_r , T_{0r} and η_{0r} are defined as B/T_m , T_0/T_m and η_0/T_m respectively. B, T_0 and η_0 are the parameters in the Vogel-Fulcher-Tammann (VFT) equation:

$$\eta(T) = \eta_0 \exp\left(\frac{B}{T - T_0}\right) = \eta_0 \exp\left(\frac{D^* T_0}{T - T_0}\right)$$
(2)

where T_0 is known as an ideal glass transition temperature and B is constant depending on materials. D^* is the fragility parameter ($1 \le D^* \le 100$). η_0 has the relation of $\eta_0 = N_A h/V$, with N_A , Avogadro's constant, h, Planck's constant and V, the molar volume [31]. In this paper, the values of V are calculated

by the JMatPro software and then we can get the value of η_0 . The first term of Equation (1) is considered a constant [29], in this paper it is $0.89 \times 10^{-6} \text{ J}^{-1} \cdot \text{K} \cdot \text{m}^3$. Since *B* and T_0 are empirical parameters and were not known clearly for the alloys below, referring to the data summarized by Takeuchi and B.A. Sun [27,29,32], considering the mostly used processing method of high aluminum content bulk metallic glasses [2,33,34], parameters of hypothetical alloys used in this paper are listed in Table 2. These hypothetical alloys are assumed to have compositions range near the given alloy (i.e., $Al_{35}La_{50}Ni_{15}$).

Alloy	η ₀ (Pa·s)	<i>B</i> (K)	B_r	D^*	T ₀ (K)	T_{0r}	<i>T_m</i> (K)	x
Al ₃₅ La ₅₀ Ni ₁₅ /Hypothetical alloys	$2.39 imes 10^{-5}$	4893.84 7049.46 6059.04 4466.6 3884	5.04 7.26 6.24 4.6 4	18 22 16 10 8	271.88 320.43 378.69 446.66 485.5	0.28 0.33 0.39 0.46 0.5	971	10 ⁻⁶
		2621.7	2.7	5	524.34	0.54		

Table 2. Parameters used for the calculation of T-Tr-T diagram for aluminum alloys.

3.2. Calculation of CCT Diagram

In order to determine the critical cooling rate for a glass-forming material solidified from liquid state without crystallization, constructing a CCT curve instead of time-temperature-transformation (TTT) curve is more realistic [35]. Here, we used the additivity rule to relate the transformation behavior during continuous cooling with the isothermal transformation data calculated above. The additivity rule was proposed by Scheil firstly and can be expressed by [36]:

$$\sum_{i=1}^{n} \frac{t_i}{\tau_i} = 1 \tag{3}$$

where t_i is the time spent at a particular temperature and τ_i is the incubation time at that temperature. According to the additivity rule, CCT curve could be gained using the calculated T-T_r-T diagram. The cooling routes used in calculation are given by:

$$T(t) = T_m + qt \tag{4}$$

where *q* is the cooling rate, and here it is negative.

4. Results and Discussion

4.1. Estimation of the Critical Cooling Rates Using CCT Curves

It was found that strong glass formers exhibit a very small T_0 and a very high melt viscosity, while fragile glass formers, show a T_0 near T_g , as well as low melt viscosities [37]. The T-T_r-T curves of Al-rich alloys listed in Table 1 calculated by Equation (1) are shown in Figure 3. Alloys with compositions close to Al₃₅La₅₀Ni₁₅ could have small D^* and T_0 near T_g , and they may have "C-curves" located between the area of the two curves which with B_r of 2.7 and 4. The curve with B_r of 2.7 has a "nose time" of 1.9×10^{-3} s at T_r of 0.76 and a critical cooling rate of 1.22×10^5 K/s. The curve with B_r of 4 has a "nose time" of 0.043 s at T_r of 0.75 and a critical cooling rate of 5.55×10^3 K/s. Therefore, according to the T-T_r-T curve, a critical cooling rate of four orders of magnitude was estimated for these alloys.



Figure 3. Calculated T-Tr-T diagram: alloys with compositions close to Al₃₅La₅₀Ni₁₅.

Figure 4 shows the calculated CCT curve of the alloy which has composition close to Al₃₅La₅₀Ni₁₅ with B_r of 2.7. It can be found that the critical cooling rate of the hypothetical alloy is 3.71×10^4 K/s, and it is lower than the value attained from T-T_r-T diagram.



Figure 4. Calculated continuous cooling transformation (CCT) diagram: alloy with composition close to Al₃₅La₅₀Ni₁₅.

4.2. Influence of Casting Parameters

In the evaluation of the cooling ability of the twin-roll caster, average cooling rate, R_{AVG} , was calculated with the following equation:

$$R_{AVG} = \frac{\Delta T}{\Delta t} \approx \frac{T_p - T_{nip}}{h} \times v_c \tag{5}$$

where T_p and T_{nip} are, respectively, pouring temperature and temperature at the roll nip, *h* the melt level of molten pool, and v_c the casting speed. Figure 5 shows the influences of different casting conditions on the average cooling rate for Al₃₅La₅₀Ni₁₅ alloy based on simulated results, and CP indicates the center pouring mode, OSP indicates the one side pouring mode. For the OSP mode, molten pool has a shape shown in Figure 2a. Here, we call *L* the melt level. From these results we can see that the average cooling rate under the CP mode is faster than that under the OSP mode. Figure 5a shows the results under the casting conditions of pouring temperature 918 K, casting speed 0.5 m/s and strip thickness 0.08 mm. We can see that average cooling rate becomes slower with the increasing of melt level. Well, for the melt level of 5 mm, it is too fast to solidify within such a short metal-roll contact distance that temperature at the roll nip is 876.11 K, and the process will not continue. When the strip thickness (i.e., nip width) comes to 0.2 mm and 0.5 mm with a melt level of 10 mm, as shown in Figure 5c, much more heat needs to be dissipated for the liquid to become fully solidified before it passes the roll nip, and the process cannot be continued. On the other hand, when setting the melt level smaller and strip thickness thinner, a faster cooling rate could be attained and temperature at the roll nip is also appropriate. However, it may cause a rolling block if the temperature at the roll nip gets too low since a fully amorphous metal is formed before it passes the roll nip. From Figure 5b we can see that there is no influence of the pouring temperature on the average cooling rate, but it can adjust the temperature at roll nip, a lower pouring temperature leads to a lower nip temperature. As a faster casting speed causes a faster cooling rate and a higher nip temperature (Figure 5d), we can control the nip temperature through adjusting the pouring temperature. However, if the nip temperature is so high that it makes the temperature of the supercooled alloy still well above T_g before it passes the roll nip area, full formation of an amorphous structure might not be possible [17], therefore the casting speed has an upper limit. Incidentally, the cooling rates at current conditions, as illustrated in Figure 5b,d, are all in the order of magnitude of 10^4 K/m, which has a same level with the calculated critical cooling rate.



Figure 5. Effects of casting conditions on cooling rate: (**a**) Effect of melt level; (**b**) Effect of pouring temperature; (**c**) Effect of strip thickness; (**d**) Effect of casting speed.

Based on the continuum theory, a special form of material (or material-time) derivative for any physical quantity ψ under motion status in Eulerian coordinate has been proposed by Ju [38]:

$$\dot{\psi} = \frac{D\psi}{Dt} = \frac{\partial\psi}{\partial t} + v \times \frac{\partial\psi}{\partial x}$$
(6)

where v is the velocity vector of material point, x is a vector and represents a space-fixed coordinate system. According to the theory above, considering the thermal phenomenon of the molten pool, cooling rate R(T) at the center of pool was calculated by:

$$R(T) = \frac{DT}{Dt} = \frac{\partial T}{\partial t} + \nu \times \frac{\partial T}{\partial y}$$
(7)

where *T* is the temperature at pool center, *y* is the location in the pool height direction, v is the velocity of the local melt, and *t* is the time.

According to the analyses of results in Figure 5, in the twin-roll casting process, one of the most important factors is the melt level *L*. The influences to the temperature distribution under different conditions were discussed as below. Casting conditions are as follows: pouring temperature 981 K, casting speed 32 m/min, strip thickness 0.1 mm, and melt levels under the two pouring mode are listed in Table 3. For the one side pouring mode (Figure 2b), it has a strip shell thickness of 1 mm (i.e., d = 1 mm).

Table 3. Influence	of melt level to	cooling rates an	d nip temperatur	e under the two	pouring modes.
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Melt Level/L (mm)	11.63	15	20	25	30	35	
Cooling Rate (10^4 K/s)	СР	3.24	3.88	3.27	38	39.6	_
Ř (737.96)	OSP	—	3.53	2.77	3.59	2.21	2.74
$T \cdot (\mathbf{K})$	СР	497.16	445.27	405.11	396.25	395.44	—
$I_{nip}(\mathbf{K})$	OSP	—	470.54	501.07	458.26	423.21	417.58

It can be seen from Table 3 that, for a certain melt level, we can get a faster cooling rate with using the CP mode, and also nip temperature is lower than that under OSP mode. On the other hand, however, it is not expected to get a temperature too low at the roll nip because the special properties of metallic glass. Fully solidified metallic glass deforms hardly due to its very high strength. Therefore, we can use the OSP mode to adjust the strip temperature at nip for a certain melt level.

5. Conclusions

- 1. A CCT diagram of a certain alloy could be attained by the combination of an equation derived by Inoue and the additivity rule.
- 2. Critical cooling rate of a metallic alloy for forming metallic glass could be evaluated using the current method.
- 3. Changing the casting conditions or adopting the one side pouring mode could improve the temperature distribution of the pool metal, and the rolling block can be avoided in the VTRC process.
- 4. Cooling rates with 4 orders of magnitude by the VTRC process under the current conditions can be attained, which shows that the VTRC technique has a potential ability in continuous fabrication of Al-rich bulk metallic alloys in sheet form.

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References

- Klement, W.; Willens, R.H.; Duwez, P.O.L. Non-crystalline Structure in Solidified Gold-Silicon Alloys. *Nature* 1960, 187, 869–870. [CrossRef]
- Löffler, J.F.; Kündig, A.A.; Dalla Torre, F.H. Rapid Solidification and Bulk Metallic Glasses—Processing and Properties. In *Materals Processing Handbook*; Powers, M.T., Lavernia, E.J., Groza, J.R., Shackelford, J.F., Eds.; CRC Press: Boca Raton, FL, USA, 2007; pp. 17-1–17-44.
- 3. Bedell, J.R.; Polk, D.E. Method of Continuous Casting Metal Filament on Interior Groove of Chill Roll. Patents US3,881,542 A, 6 May 1975.
- Sheldon, K. Method of Forming Metallic Filament Cast on Interior Surface of Inclined Annular Quench Roll. U.S. Patent 3,881,540, 6 May 1975.

- Liebermann, H.; Graham, C. Production of amorphous alloy ribbons and effects of apparatus parameters on ribbon dimensions. In Proceedings of the IEEE Transactions on Magnetics, New York, NY, USA, 6 January 1976; Volume 12, pp. 921–923.
- Johnson, W.L. Bulk Glass-Forming Metallic Alloys: Science and Technology. MRS Bull. 1999, 24, 42–56. [CrossRef]
- Aqida, S.N.; Shah, L.H.; Naher, S.; Brabazon, D. Rapid Solidification Processing and Bulk Metallic Glass Casting. In *Comprehensive Materials Processing*; Hashmi, S., Ed.; Elsevier: Singapore, 2014; pp. 69–88.
- Huang, S.C.; Fiedler, H.C. Amorphous ribbon formatin and the effects of casting velocity. *Mater. Sci. Eng.* 1981, 51, 39–46. [CrossRef]
- 9. Carpenter, J.; Steen, P. Planar-flow spin-casting of molten metals: Process behaviour. *J. Mater. Sci.* **1992**, 27, 215–225. [CrossRef]
- 10. Wilde, P.D.; Matthys, E.F. Experimental investigation of the planar flow casting process: Development and free surface characteristics of the solidification puddle. *Mater. Sci. Eng. A* **1992**, 150, 237–247. [CrossRef]
- Sohrabi, S.; Arabi, H.; Beitollahi, A.; Gholamipour, R. Planar Flow Casting of Fe₇₁Si_{13.5}B₉Nb₃Cu₁Al_{1.5}Ge₁ Ribbons. *J. Mater. Eng. Perform.* 2013, 22, 2185–2190. [CrossRef]
- 12. Metglas®. Avaliable online: http://www.metglas.com/ (accessed on 25 October 2016).
- Praisner, T.J.; Chen, J.S.; Tseng, A.A. An experimental study of process behavior in planar flow melt spinning. *Metall. Mater. Trans. B* 1995, 26, 1199–1208. [CrossRef]
- 14. Jones, H. A perspective on the development of rapid solidification and nonequilibrium processing and its future. *Mater. Sci. Eng. A* **2001**, *304*, 11–19. [CrossRef]
- 15. Chen, H.S.; Miller, C.E. A Rapid Quenching Technique for the Preparation of Thin Uniform Films of Amorphous Solids. *Rev. Sci. Instrum.* **1970**, *41*, 1237–1238. [CrossRef]
- Suzuki, T.; Anthony, A.M. Rapid quenching on the binary systems of high temperature oxides. *Mater. Res. Bull.* 1974, 9, 745–753. [CrossRef]
- 17. Lee, J.G.; Park, S.S.; Lee, S.B.; Chung, H.T.; Kim, N.J. Sheet fabrication of bulk amorphous alloys by twin-roll strip casting. *Scr. Mater.* **2005**, *53*, 693–697. [CrossRef]
- Lee, J.G.; Lee, H.; Oh, Y.S.; Lee, S.; Kim, N.J. Continuous fabrication of bulk amorphous alloy sheets by twin-roll strip casting. *Intermetallics* 2006, 14, 987–993. [CrossRef]
- Oh, Y.S.; Lee, H.; Lee, J.G.; Kim, N.J. Twin-Roll Strip Casting of Iron-Base Amorphous Alloys. *Mater. Trans.* 2007, 48, 1584–1588. [CrossRef]
- 20. Urata, A.; Nishiyama, N.; Amiya, K.; Inoue, A. Continuous casting of thick Fe-base glassy plates by twin-roller melt-spinning. *Mater. Sci. Eng. A* 2007, 449, 269–272. [CrossRef]
- 21. Hofmann, D.C.; Roberts, S.N.; Johnson, W.L. Twin Roll Sheet Casting of Bulk Metallic Glasses and Composites in an Inert Environment. Patent US20130025746 A1, 31 January 2013.
- 22. East, D.R.; Kellam, M.; Gibson, M.A.; Seeber, A.; Liang, D.; Nie, J.F. Amorphous magnesium sheet produced by twin roll casting. *Mater. Sci. Forum* **2010**, *654*, 1078–1081. [CrossRef]
- 23. Park, Y.S.; Lee, S.B.; Kim, N.J. Microstructure and Mechanical Properties of Strip Cast Al-Mg-Si-X Alloys. *Mater. Trans.* 2003, 44, 2617–2624. [CrossRef]
- 24. Ding, P.D.; Pan, F.S.; Jiang, B.; Wang, J.; Li, H.L.; Wu, J.C.; Wen, Y. Twin-roll strip casting of magnesium alloys in China. *Trans. Nonferr. Met. Soci. China* 2008, *18*, s7–s11. [CrossRef]
- 25. Hu, X.D.; Ju, D.Y.; Zhao, H. Y. Thermal flow simulation of twin-roll casting magnesium alloy. *J. Shanghai Jiaotong Univ. Sci.* **2012**, *17*, 479–483. [CrossRef]
- 26. Haga, T.; Suzuki, S. Melt ejection twin roll caster for the strip casting of aluminum alloy. *J. Mater. Process. Technol.* **2003**, *137*, 92–95. [CrossRef]
- 27. Sun, B.A.; Pan, M.X.; Zhao, D.Q.; Wang, W.H.; Xi, X.K.; Sandor, M.T.; Wu, Y. Aluminum-rich bulk metallic glasses. *Scr. Mater.* **2008**, *59*, 1159–1162. [CrossRef]
- 28. Chen, Z.P.; Gao, J.E.; Wu, Y.; Wang, H.; Liu, X.J.; Lu, Z.P. Designing novel bulk metallic glass composites with a high aluminum content. *Sci. Rep.* **2013**, *3*. [CrossRef] [PubMed]
- 29. Takeuchi, A.; Inoue, A. Evaluation of Glass-Forming Ability for Metallic Glasses from Time-Reduced Temperature-Transformation Diagram. *Mater. Trans.* **2001**, *42*, 2374–2381. [CrossRef]
- 30. Uhlmann, D.R. A kinetic treatment of glass formation. J. Non-Cryst. Solids 1972, 7, 337–348. [CrossRef]
- 31. Lee, S.B.; Kim, N.J. Kinetics of crystallization in continuously cooled BMG. *Mater. Sci. Eng. A* 2005, 404, 153–158. [CrossRef]

- 32. Takeuchi, A.; Inoue, A. Quantitative evaluation of critical cooling rate for metallic glasses. *Mater. Sci. Eng. A* **2001**, *304*, 446–451. [CrossRef]
- Inoue, A.; Nakamura, T.; Sugita, T.; Zhang, T.; Masumoto, T. Bulky La-Al-TM (TM=Transition Metal) Amorphous Alloys with High Tensile Strength Produced by a High-Pressure Die Casting Method. *Mater. Trans. JIM* 1993, 34, 351–358. [CrossRef]
- 34. Yang, G.N.; Shao, Y.; Yao, K.F.; Chen, S.Q. A study of cooling process in bulk metallic glasses fabrication. *AIP Adv.* **2015**, *5*. [CrossRef]
- 35. Xu, K.; Wang, Y.; Li, J.; Li, Q. Critical cooling rate for the glass formation of ferromagnetic Fe₈₀P₁₃C₇ alloy. *Acta Metall. Sin.* **2013**, *26*, 56–62. [CrossRef]
- 36. Umemoto, M.; Horiuchi, K.; Tamura, I. Pearlite Transformation during Continuous Cooling and Its Relation to Isothermal Transformation. *Trans. Iron Steel Inst. Jpn.* **1983**, *23*, 690–695. [CrossRef]
- 37. Busch, R.; Liu, W.; Johnson, W.L. Thermodynamics and kinetics of the Mg₆₅Cu₂₅Y₁₀ bulk metallic glass forming liquid. *J. Appl. Phys.* **1998**, *83*, 4134–4141. [CrossRef]
- Inoue, T.; Ju, D.Y.; Yosihara, N. Temperature and Viscoplastic Stresses During Vertical Semi-Continuous Direct Chill Casting of Aluminum Alloy. In *International Conference on Residual Stresses (ICRS2)*; Beck, G., Denis, S., Simon, A., Eds.; Springer: Dordrecht, The Netherlands, 1989; pp. 523–528.



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