

Water-Mediated Proton Hopping Mechanisms at the SnO₂(110)/H₂O Interface from Ab Initio Deep Potential Molecular Dynamics

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ABSTRACT: The interfacial proton transfer (PT) reaction on the metal oxide surface is an important step in many chemical processes including photoelectrocatalytic water splitting, dehydrogenation, and hydrogen storage. The investigation of the PT process, in terms of thermodynamics and kinetics, has received considerable attention, but the individual free energy barriers and solvent effects for different PT pathways on rutile oxide are still lacking. Here, by applying a combination of ab initio and deep potential molecular dynamics methods, we have studied interfacial PT mechanisms by selecting the rutile $SnO_2(110)/H_2O$ interface as an example of an oxide with the characteristic of frequently interfacial PT processes. Three types of PT pathways among the interfacial groups are found, i.e., proton transfer from terminal adsorbed water to bridge oxygen directly (surface-PT) or via a solvent water (mediated-PT), and proton hopping between two terminal groups (adlayer PT). Our simulations reveal that the terminal water in mediated-PT prefers to point toward the solution and forms a shorter H-bond with the assisted solvent water, leading to the lowest energy barrier and the fastest relative PT rate. In particular, it is found that the full solvation environment plays a crucial role in water-mediated proton conduction, while having little effect on direct PT reactions. The PT mechanisms on aqueous rutile oxide interfaces are also discussed by comparing an oxide series composed of SnO_2 , TiO_2 , and IrO_2 . Consequently, this work provides valuable insights into the ability of a deep neural network to reproduce the ab initio potential energy surface, as well as the PT mechanisms at such oxide/liquid interfaces, which can help understand the important chemical processes in electrochemistry, photoelectrocatalysis, colloid science, and geochemistry.

KEYWORDS: Proton transfer mechanism, ab initio molecular dynamics, deep potential molecular dynamics, rutile oxide, machine learning, solvation effect, free energy

INTRODUCTION

Metal oxide electrode materials are ubiquitous in a number of applications, including electrochemistry,¹ photoelectrocatalysis,² geochemistry,³ biochemistry,⁴ and colloid science.^{5,6} When the electrode is exposed to humid environments or immersed in solution at working conditions, water species, i.e., protons and hydroxyl groups, are always adsorbed on the active functional sites of metal oxide surfaces.^{7–11} The interfacial proton transfer (PT) reaction among the water species is a key elementary step in many chemical processes,^{12–14} including photocatalytic¹⁵ or electrochemical water splitting,¹⁶ catalytic hydrogen evolution and reforming,¹⁷ photocatalytic dehydrogenation,¹⁸ and hydrogen storage.¹⁹ Therefore, the investigation of the PT process, in terms of kinetics and thermodynamics, has received considerable attention both from experiments and theoretical simulations in recent years.

Despite traditional approaches, i.e., vibrational spectroscopy²⁰ and X-ray scattering methods,²¹ which have been applied to explore the interfacial water, advanced experimental techniques such as in situ X-ray photoelectron spectroscopy (XPS),^{22,23} sum-frequency-generation spectroscopy

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Figure 1. (a) Molecular dynamics model of the $SnO_2(110)/H_2O$ interface. Three proton transfer pathways at the $SnO_2(110)/H_2O$ interface (b) surface-PT: proton transfer between terminal adsorbed water molecule O_aH_2 and bridging oxygen O_{br} , (c) adlayer-PT: proton hopping between terminal adsorbed $O_{a1}H_2$ and another terminal $O_{a2}H^-$, (d) mediated-PT: proton transfer between O_aH_2 and O_{br} via a solvent water H_2O_m .

(SFG),^{24–27} in situ Raman spectroscopy,^{28–30} and scanning tunneling microscopy $(STM)^{31–33}$ further provide the elemental composition, and structural and dynamical properties of oxide/liquid interfaces at the molecular level. However, it is still challenging to probe the microscopic structures and identify the dynamic interfacial proton hopping events with sufficient atomic resolution, especially in distinguishing the different pathways of PT reactions.

Alternatively, ab initio molecular dynamics (AIMD) can provide valuable interfacial information at the atomistic scale.^{34–41} Compared to static density functional theory (DFT) optimizations, implicit solvation model or other classical molecular dynamics simulations,^{42–44} AIMD simulations have one great advantage that they include the all-atom method, treating solute and solvent at the same level of electronic structure and computing the electronic structure from first-principles calculation.⁴⁵ Hence, it is appropriate to investigate interfacial PT events, which involve the breaking and forming of O–H bonds dynamically, with AIMD simulations.

However, it is difficult to reach the equilibration of PT dynamics among the interfacial species in the picosecond (ps) time scale from AIMD simulations, especially for the slow PT processes at the metal oxide surfaces.⁴⁶ Both the expensive computational cost of a heterogeneous supercell and the limitation of time scale for AIMD calculations make the study of interfacial PT events quite difficult. Fortunately, the fledged machine-learned (ML) potential techniques dramatically extend both the supercell size and time scale for the MD simulations.^{46–54} Assisted by the deep neural network (DNN), ML potentials are trained using configurations and corresponding energies and forces from DFT for potential energy surface (PES).^{38,47,51,52} The application of ML potentials significantly accelerates MD simulations and keeps ab initio accuracy.

In the case of large free-energy barriers related to slow and rare interfacial PT events, it calls for enhanced sampling techniques, such as umbrella sampling^{51,55} and metadynam-

ics,^{56–60} which increase the relative probability of rare configurations as well as accelerating the PT events more frequently. Currently, both the DNN based MD simulations and enhanced sampling MD simulations have been successfully applied to investigate various oxide/liquid interfaces, for example, Selloni and Cheng have reported aqueous rutile $TiO_2(110)$, (100), and (011),^{58,61} anatase $TiO_2(100)$, (101), and (110),^{51,58} and $IrO_2(110)$ interfaces,⁵⁹ Nakayama has studied aqueous $CeO_2(111)$ and (110) interfaces,⁶⁰ and Behler has reported the water-ZnO(1010) interface.^{38,62} The interfacial structural properties, dynamic behavior, H-bond networks, and proton transfer pathways, i.e., direct and indirect PT reactions between interfacial species, have been demonstrated in these works. However, individual free energy barriers and solvent effects of different PT pathways on rutile oxide are still lacking.

A previous work has shown that the surface groups $Sn_{5c}OH_2$ and Sn_2OH^+ on rutile $SnO_2(110)$ have close pK_a values, and the terminal adsorbed water dissociates spontaneously and frequently.⁶³ To explore the molecular picture of microscopic structure, PT pathways, and solvent effects on the rutile oxide surface, SnO_2 can serve as a model system with fast PT processes. Currently, SnO_2 -based materials have been widely applied for many technological fields such as solar batteries,⁶⁴ catalysis,⁶⁵ lithium-ion batteries,⁶⁶ and gas sensors,⁶⁷ due to their nontoxic nature, abundance in the Earth's crust, and low cost.

In this study, we train and validate deep potentials and then perform Deep Potential Molecular Dynamics (DPMD) simulations for the $SnO_2(110)/H_2O$ interface. We analyze the microscopic structure and find three types of PT pathways among the interfacial species at the $SnO_2(110)/H_2O$ interface. Additionally, we discuss the free energy landscapes and relative PT rates for these PT reactions. It is followed by the investigation of full solvation effects on interfacial PT reactions via comparing climbing image nudged elastic band (CI-NEB) calculations for a monolayer of adsorbed water. We also calculated the average degree of water dissociation and its associated free energy at the $SnO_2(110)/H_2O$ interface. Finally, we discuss the PT mechanisms on aqueous rutile oxide interfaces by comparing an oxide series composed of SnO_{22} , TiO₂₂, and IrO₂₂.

COMPUTATIONAL METHODS

AIMD Simulations

The SnO₂(110) surface was built up by a symmetric periodic slab of five O–Sn–O layers with lateral dimensions of a 4 × 2 surface cell (see Figure 1a). The symmetric slabs were separated by a solvent space of 25 Å, giving an orthorhombic supercell with dimensions 12.7 × 13.4 × 41.0 Å³, with the volume of bulk water in the supercell being approximately cubic. The solvent space between the SnO₂ slabs was made up of 143 water molecules, and the number of water molecules was confirmed by adjusting the density of water in the bulk solvent region to ~1 g/cm³.

AIMD simulations were performed with the freely available CP2K/ Quickstep package.^{68,69} The Perdew–Burke–Ernzerhof (PBE) functional was augmented with the D3 dispersion correction of Grimme⁷⁰ to properly simulate the SnO₂(110)/H₂O interface. The Goedecker-Teter-Hutter (GTH) pseudopotentials^{71,72} were employed to represent the core electrons. The atomic basis sets for the valence electrons (1s¹ for H; 2s² and 2p⁴ for O; 5s² and 5p² for Sn) were the standard short-ranged double- ζ basis functions with one set of polarization functions (DZVP).⁷³ The plane wave cutoff for the electron density expansion was set as 400 Ry. The target accuracy for the SCF convergence was 3×10^{-7} a.u. The NVT ensemble was used for MD propagation with a time step of 0.5 fs, and the equilibrium temperature for all the simulations was kept to 330 K by using the Nosé–Hoover thermostat.⁷⁴

Machine Learning Potential Training

The deep potentials were trained by the open source code DeePMDkit.^{75,76} The Deep Potential-Smooth Edition (DeepPot-SE) model⁷⁷ was used for the structural descriptor. The cutoff radius of the local environment was set to 6.0 Å, and the cutoff smooth (rcut_smth) was set as 0.5 Å. To train a practical deep potential, the concurrent learning as implemented in DP-GEN code^{78,79} was also applied to construct the data set. In the exploration stage, MD simulations are performed in parallel at the elevated temperatures of 330, 430, and 530 K (Figures S1–S3).

Our final data set contains 600 structures, which were randomly extracted from the 100 ps trajectory of the AIMD simulation, and 5400 structures were collected from concurrent learning. To ensure the quality of DPMD simulations, the final deep potentials in use were trained with 2000000 batch steps, which achieved the L2 energy error of 0.504 meV/atom and the force error of 66.3 meV/Å on the training set (see Figures S4 and S5). In addition, a number of structures were extracted from the trajectory for every 2000 time steps and computed by DFT to validate the accuracy of energies and forces predicted by the deep potentials. The error of energies and forces was 0.8 and 56.8 meV/Å, respectively (Figure S6). The details of deep potential training and the DP-GEN setup are given in the Supporting Information.

DPMD Simulations

The DPMD simulations of the $\text{SnO}_2(110)/\text{H}_2\text{O}$ interface were carried out using the molecular dynamics engine LAMMPS⁸⁰ with the same supercell model as AIMD simulations. All the DPMD simulations of the $\text{SnO}_2(110)/\text{H}_2\text{O}$ interface were performed under the canonical ensemble condition (constant volume and constant temperature). The temperature is controlled by the Nosé–Hoover thermostat and is set to 330 K. The MD time step is set to 0.5 fs, and the time scale of DPMD simulation is about 1–5 ns.

CI-NEB Calculations

For SnO_2 covered with a monolayer of adsorbed water, the transition state geometries and energy barriers were studied through the

climbing image nudged elastic band (CI-NEB) method^{81,82} as implemented in the CP2K code. The transition states were finally verified by the presence of a single imaginary frequency through harmonic vibrational analysis.

RESULTS AND DISCUSSION

Validation and Equilibrium of the SnO₂(110)/H₂O Interface

The radial distribution functions (RDFs) of selected interfacial groups from the 1 ns DPMD trajectory are in excellent agreement with RDFs predicted by 100 ps AIMD simulations for the $SnO_2(110)/H_2O$ interface (Figure 2a). Furthermore, DPMD simulations accurately predict the average water density profile (Figure 2b) and water dipole orientation (Figure 2c), which exhibit perfect symmetry around the center, reflecting the symmetric nature of the interface models. In addition, we find that the vibrational density of state (VDOS) of the O–H groups at the $SnO_2(110)$ surface calculated from AIMD (100 ps) and DPMD (final 100 ps) simulations coincides well, as depicted in Figure 2d. Both the length of simulation trajectories and the length of correlation time used to compute the VDOS from AIMD and DPMD simulations were set as 100 ps. These results indicate that the DPMD simulations have obtained the equilibrium density distribution of interfacial water species at the $SnO_2(110)/H_2O$ interface.

Structure and Proton Transfer at the SnO₂(110)/H₂O Interface

As mentioned in the Introduction, the interfacial groups $Sn_{5c}OH_2$ and Sn_2OH^+ on $SnO_2(110)$ surface have close pK_a values and release protons spontaneously and frequently.⁶³ In this work, three types of PT pathways are indeed found occurring at the $SnO_2(110)/H_2O$ interface based on AIMD and DPMD simulations (Figure 1b-d). It is worth noting that these three types of PT reactions are reversible due to the close pK_a values for each interfacial group.⁶³

The first pathway is proton transfer from terminal water molecule $Sn_{5c}O_aH_2$ to bridge oxygen Sn_2O_{br} directly, which is denoted as "surface-PT" here (Figure 1b):

$$\mathrm{Sn}_{\mathrm{5c}}\mathrm{O}_{\mathrm{a}}\mathrm{H}_{2}\mathrm{\cdots}\mathrm{Sn}_{2}\mathrm{O}_{\mathrm{br}} \rightleftharpoons \mathrm{Sn}_{\mathrm{5c}}\mathrm{O}_{\mathrm{a}}\mathrm{H}^{-}\mathrm{\cdots}\mathrm{Sn}_{2}\mathrm{O}_{\mathrm{br}}\mathrm{H}^{+}$$
(1)

The second pathway involves two terminal groups $Sn_{5c1}O_{a1}H_2$ and $Sn_{5c2}O_{a2}H^-$, which is denoted as "adlayer-PT" (Figure 1c):

$$Sn_{5c1}O_{a1}H_2\cdots Sn_{5c2}O_{a2}H^- \rightleftharpoons Sn_{5c1}O_{a1}H^-\cdots Sn_{5c2}O_{a2}H_2$$
(2)

The third type denoted as "mediated-PT" involves a solvent water molecule H_2O_m between terminal $Sn_{5c}O_aH_2$ and bridge oxygen Sn_2O_{br} (Figure 1d):

$$Sn_{5c}O_{a}H_{2}\cdots H_{2}O_{m}\cdots Sn_{2}O_{br}$$

$$\Rightarrow Sn_{5c}O_{a}H^{-}\cdots H_{2}O_{m}\cdots Sn_{2}O_{br}H^{+}$$
(3)

The three types of PT reactions can be viewed as the dissociation (forward reaction) or combination (backward reaction) of the adsorbed water molecule. Previous studies have shown that the pathway of water dissociation is determined by its orientation and the H-bond network.^{38,46} Thus, we first analyzed the probability distribution of the average angle θ between the dipole of terminal water and surface normal as demonstrated in Figure 3a.

It is found that the values of θ show three peaks from 0° to 105° (Figure 3a). The first peak is at 38° with both hydrogen atoms of the adsorbed water pointing toward the solution.



Figure 2. (a) Radial distribution function of selected atomic type pairs at the $\text{SnO}_2(110)/\text{H}_2\text{O}$ interface obtained from DPMD (lines) and AIMD (points). The definitions of $\text{Sn}_{5^{cr}} O_{a^r}$ and O_{br} are given in Figure 1, and O_w represents solvent water oxygen atoms. (b,c) Density profiles and dipole orientation of water confined between two SnO_2 surfaces as predicted by DPMD and AIMD simulations. (d) Vibrational density of state (VDOS) of O–H groups at $\text{SnO}_2(110)$ surface obtained from AIMD (100 ps) and DPMD (final 100 ps) simulations. We note here that the VDOS were obtained from the Fourier transform of the atomic velocity autocorrelation functions (VACF), and the Fourier transform was smoothed via a Savitzky-Golay filter;⁸³ a window length of 59 and a polynomial order of 1 were chosen for the filter.

Since the water molecule in this configuration forms two Hbonds with solvent water while donating no H-bond to the interfacial groups, it mainly consists of the mediated-PT as shown in the green box of Figure 3b. The second peak is at 60°, which is also the highest peak, with one hydrogen of the adsorbed water pointing toward the solution and the other parallel to the surface. The former hydrogen forms a hydrogen bond with solvent water, and the latter hydrogen forms a hydrogen bond with the interfacial groups. Note that this kind of terminal water molecule could undergo all three types of PT



Figure 3. (a) Probability distribution of the angle θ between adsorbed water dipole moment and surface normal for the SnO₂(110)/H₂O interface. (b) Proton transfer pathways correspond to the water orientation in (a) which are distinguished by box color.

reactions at $SnO_2(110)/H_2O$ interface (the black boxes in Figure 3b). The third peak is the smallest peak, which spreads over 87°, suggesting that the adsorbed water molecules are almost parallel to the surface. This water structure forms two H-bonds with interfacial species, and mainly contributes to the surface-PT and adlayer-PT (the blue boxes in Figure 3b).

Free Energy Landscapes of PT Reactions at the SnO₂(110)/H₂O Interface

To further investigate the thermodynamic and kinetic differences among the three types of PT reactions, the free energy landscapes at the $SnO_2(110)/H_2O$ interface are calculated in the following (see Figure 4). By applying the method introduced in ref 84, the free energy profiles of PT reactions are evaluated with the definition of a displacement coordinate δ . The values of δ are defined as $d_{\mathrm{O}_a\cdots\mathrm{H}_d}$ subtract $d_{O_d-H_d}$ where $d_{O_a\cdots H_d}$ and $d_{O_d-H_d}$ are the distances between the donated proton H_d and the two oxygens, i.e., the proton donor O_d and the proton acceptor O_a , in a PT reaction. The onedimensional PT coordinate δ_{min} is defined by selecting the "most active" H-bond with the minimum of δ , which is most likely to experience PT reactions. When the donated proton O_d is exactly in the middle of O_a and O_d , we can get the δ_{min} = 0 which corresponds to the transition state (TS). The Helmholtz free energy ΔF of a PT reaction can be described as³⁸

$$\Delta F(\delta_{\min}) = -k_{\rm B}T \ln W(\delta_{\min}) \tag{4}$$

where $W(\delta_{\min})$ denotes the counts for the corresponding configuration $HO_d \cdots H_d \cdots O_a H^-$ at a given δ_{\min} . The relative rates between two PT reactions *i* and *j* can be calculated by the ratio of $W(\delta_{\min})$ at the TS ($\delta_{\min} = 0$)



Figure 4. Free energy landscapes for surface-PT (a), adlayer-PT (b), and mediated-PT (c) from AIMD (dashed lines) and DPMD (solid lines) simulations, respectively. (d) Comparison of free energy landscapes for the three PT reactions from DPMD simulations. Note that the free energies ΔF of PT reaction in this figure are calculated from eq 4 and referenced to those of the reactant states for a quick comparison; the origin free energies profiles are shown in Figure S7.

$$\frac{r_i}{r_j} = \frac{W_i(\delta_{\min} = 0)}{W_j(\delta_{\min} = 0)}$$
(5)

To compare the differences between AIMD and DPMD simulations at the $SnO_2(110)/H_2O$ interface, the free energy profiles of the three types of PT reactions based 100 ps AIMD and 1 ns DPMD simulations are calculated using eq 4. As shown in Figure 4, it is found that the mediated-PT has reached equilibrium (Figure 4c) whereas the surface-PT (Figure 4a) and adlayer-PT (Figure 4b) have not reached equilibrium within the 100 ps of AIMD simulation, suggesting that the mediated-PT is the fastest PT reaction at the $SnO_2(110)/H_2O$ interface. The convergences for the free energy profiles of the three PT reactions from DPMD simulations are described in Figures S8-S10. What we observed demonstrates the necessity of employing DPMD simulations to investigate the large free-energy barriers related to slow PT reactions at the oxide/liquid interface.

The energy barriers for the three types of PT reactions from DPMD simulations are listed in Table 1. At the SnO₂(110)/ H_2O interface, proton transfer between Sn_{5c}O_aH₂ and Sn₂O_{br} sites can be either directly (surface-PT) or indirectly

Table 1. Comparison of Water Orientation θ , Length of H-Bonds $d_{\text{Oa}\text{--Hd}}$ (Å), Energy Barriers (eV), and Relative Rates for Surface-PT, Adlayer-PT, and Mediated-PT from DPMD Simulations

	surface-PT	adlayer-PT	mediated-PT
θ	60°, 87°	60°, 87°	38°, 60°
$d_{\mathrm{O}_{\mathrm{a}}\cdots\mathrm{H}_{\mathrm{d}}}$	1.66	1.56	1.46
energy barrier	0.10	0.07	0.05
relative PT rate	1	6.9	28.1

(mediated-PT). It is found that direct surface-PT has the highest energy barrier of 0.10 eV from DPMD simulations (Figure 4a). Interestingly, with the assistance of a solvent water molecule, the mediated-PT has the lowest energy barrier of 0.05 eV (Figure 4c), which is decreased by 50% as compared to surface-PT. For one thing, a smaller average length of Hbond $d_{O_a \cdots H_d}$ (1.46 Å) is observed for the mediated-PT groups along the PT coordinate, as compared to the $d_{O_a \cdots H_d}$ of surface-PT species (1.66 Å). In other words, the donated proton in mediated-PT has a shorter distance to travel (Table 1). For another, the two most abundant angles θ between the adsorbed water dipole and surface normal both at 38° and 60° contributed to mediated-PT (see Figure 3). Therefore, the shorter length of H-bond⁸⁵ and the specific orientation of terminal water molecule explain why the mediated-PT barrier is 50% smaller than the surface-PT barrier. Besides, the relative rates between the surface-PT and the mediated-PT can be calculated by eq 5 and given $\frac{r_{\text{mediated}-PT}}{2} = 28.1$, suggesting that r_{surface-PT} for every surface-PT event, there are 28.1 mediated-PT events.

Moreover, we find that the free energy landscapes for both the surface-PT and the mediated-PT are asymmetric. For the surface-PT, the backward barrier (0.11 eV) is slightly higher than the forward barrier (0.10 eV). Simultaneously, the backward barrier (0.09 eV) is also higher than the forward barrier (0.05 eV) for mediated-PT. Such results suggest that the proton donor group $Sn_{sc}O_aH_2$ is slightly more acidic than Sn_2O_{br} site, which is consistent with the previous calculation of surface acidity constant.⁶³

For the adlayer-PT, because the forward and backward PT reactions are equivalent, the free energy barriers are fully symmetric (Figure 4b). When comparing the two direct proton transfer reactions of surface-PT and adlayer-PT, the results

Full Solvation Effects on Interfacial PT Reactions

It has been known that the solvation environment plays an important role in the interfacial PT reaction.^{33,36,86} To further investigate the full solvation effects on interfacial PT reaction, a monolayer of adsorbed water on the $SnO_2(110)$ surface was studied by applying the CI-NEB method. The energy profiles of the three types of PT reactions are shown in Figure 5, and



Figure 5. Minimum energy pathway for surface-PT (a), adlayer-PT (b), and mediated-PT (c) reactions calculated by the CI-NEB method, respectively. The Sn, O, and H atoms are colored in yellow, red, and white, respectively. The oxygens and protons involved in the interfacial PT reaction are highlighted in purple and green.

the energy barriers are listed in Table 2. Note that the energy barriers obtained from DPMD simulations and CI-NEB calculations include different entropy effects as well as the definition of reaction coordinate; a rough comparison of energy barriers between the two methods is discussed below.

It is found that the energy barriers of direct surface-PT and adlayer-PT obtained from CI-NEB calculations (Table 2) are almost the same as the DPMD results (Table 1). Based on the

Table 2. Energy Barriers (eV) and Length of H-Bonds $d_{O_a \cdots H_d}$ (Å) Calculated from CI-NEB Calculations with a Monolayer Water Adsorption for Surface-PT, Adlayer-PT, and Mediated-PT^{*a*}

	surface-PT	adlayer-PT	mediated-PT
energy barrier (CI-NEB)	0.10	0.05	0.16
$d_{O_a \cdots H_d}$ (Monolayer)	1.69	1.61	1.58
$\Delta d_{\mathrm{O_a}\cdots\mathrm{H_d}}$	0.03	0.05	0.12

^{*a*}The difference of $d_{O_a \cdots H_d}$ between full solvation model and monolayer model is denoted as $\Delta d_{O_a \cdots H_d}$.

snapshots in the insets of Figure 5a and b, it is observed that the terminal water molecules of monolayer adsorption prefer to be parallel to the surface and form two H-bonds with interfacial species, which correspond to the orientation of the third peak (at 87°) for terminal water in Figure 3a. The differences of $d_{O_a \cdots H_d}$ between DPMD simulations and CI-NEB calculations are only 0.03 and 0.05 Å for surface-PT and adlayer-PT, respectively (see Table 2). In this case, the solvation from solvent water molecules, probably, has little effect on surface-PT and adlayer-PT, which leads to similar energy barriers between the full solvation of DPMD simulations and the monolayer water adsorption of CI-NEB calculations.

However, for the mediated-PT, the terminal water involved in the PT reaction prefers forming one H-bond with solvent water and another with surface species (Figure 5c), which corresponds to the second peak (at 60°) of terminal water orientation in Figure 3a. The difference of $d_{O_a \cdots H_d}$ between DPMD simulation and CI-NEB calculation is 0.12 Å (see Table 2). Without the assistance of the solvation environment, the hydrogen atom of the mediated-water H_2O_m above the SnO₂ surface, which points toward the vacuum, is unstable. This increases the instability of the model system. Therefore, the energy barrier of mediated-PT has increased to 0.16 eV, which is higher than the energy barrier obtained from DPMD simulation (0.05 eV). Through the above general comparison, it is clearly indicated that the solvent water molecules are helpful for the water-mediated proton conduction mechanism at the $SnO_2(110)/H_2O$ interface.

Degree α and Free Energy ΔA_{diss} of Water Dissociation at the SnO₂(110)/H₂O Interface

On the SnO₂(110)/H₂O interface model (Figure 1), there are 8 Sn_{5c} sites and 8 Sn₂O_{br} sites in total. Due to the dissociation of adsorbed water molecules on Sn_{5c} sites, the interfacial species at the SnO₂(110) surface are made up of a mixed state of Sn_{5c}O_aH₂, Sn₂O_{br}, Sn_{5c}O_aH⁻, and Sn₂O_{br}H⁺. The dissociation of terminal water, which corresponds to surface-PT and mediated-PT, is reversible. The degree of water dissociation α depends on the number of Sn_{5c}O_aH⁻ group when the SnO₂(110)/H₂O interface achieves dynamic equilibrium. The value of α can be calculated as the ratio of average number of Sn_{5c}O_aH⁻ group n(Sn_{5c}O_aH⁻) to total sites 8, and the values of n(Sn_{5c}O_aH⁻) are counted by setting the O–H bond length cutoff as 1.23 Å.

By averaging over the 100 ps AIMD trajectory, it is calculated that the average number of $n(Sn_{5c}O_aH^-)$ is 4.57, and the degree of water dissociation α is estimated to be 0.57 (Table 3). The time cumulative averages of α calculated from AIMD simulations are shown in Figure 6a (black dash line). It

Table 3. Comparison of the Average Number of $Sn_{5c}O_aH_2$ and $Sn_{5c}O_aH^-$ Groups, Degree α , and Free Energy of Water Dissociation ΔA_{diss} (Eq 6) from AIMD and DPMD Simulations



Figure 6. Time evolution of the degree of water dissociation α on the SnO₂(110)/H₂O interface obtained from AIMD (a) and DPMD (b) simulations. The black dashed line is the time average of α .

shows a slightly increasing trend, suggesting that the dynamics of the SnO₂(110)/H₂O interface have not yet obtained equilibrium within the 100 ps time scale. This calls for DPMD simulation, which has reached the equilibrium and validated in Section "Validation and Equilibrium of the SnO₂(110)/H₂O Interface". The value of α is given as 0.62 based on the 1 ns DPMD simulation.

Moreover, to further explore the convergence of α at $\text{SnO}_2(110)/\text{H}_2\text{O}$ interface, the time scale has been extended from 1 to 5 ns by DPMD simulation in this work. The average number of $n(\text{Sn}_{5c}\text{O}_{a}\text{H}^{-})$ is counted as 5.00, and the α is estimated as 0.63 (Table 3), which is consistent with the result of 1 ns (0.62), suggesting that the trajectory of 1 ns DPMD has reached the equilibrium. As shown in Figure 6b, the time cumulative averages of α (black dashed line) remain almost constant within the 5 ns time scale.

The free energy of water dissociation ΔA_{diss} can be linked to the degree of dissociation α

$$\Delta A_{\rm diss} = -k_{\rm B}T \ln \frac{\alpha^2}{(1-\alpha)^2} \tag{6}$$

The value of ΔA_{diss} is calculated as -0.03 eV based on the 5 ns DPMD simulation from eq 6 (Table 3). The corresponds to almost zero ΔA_{diss} suggests that the proton donor group $\text{Sn}_{\text{sc}}O_{a}\text{H}_{2}$ is slightly more acidic than $\text{Sn}_{2}O_{\text{br}}$ site, which is

consistent with the calculation of free energy landscapes for the fastest mediated-PT shown in Figure 4c.

Comparison of PT Mechanisms on Aqueous Rutile Oxide Interfaces

There are seven types of PT reactions including both direct and indirect pathways among interfacial species that have been reported on oxide surfaces (see Figure 7), i.e., rutile TiO_2 , ^{58,61,86} anatase TiO_2 , ^{51,58} CeO_2 , ⁶⁰ Al_2O_3 , ⁸⁹ ZnO, ^{38,62} ZrO_2 , ³⁶ IrO_2 , ⁵⁹ AlOOH, ⁹⁰ InP, ³⁵ and GaP; ³⁵ namely, proton transfer between terminal H_2O and surface oxygen O_s directly (Figure 7a, surface-PT) or via a solvent water molecule (Figure 7b, mediated-PT), proton transfer between two surface oxygens directly (Figure 7c, surface-O_s-PT) or assisted by a solvent water molecule (Figure 7d, solvent-assisted surface-O_s-PT), proton transfer between two terminal groups H_2O and OH^- directly (Figure 7f, solvent-assisted adlayer-PT-I) or via several solvent water molecules (Figure 7g, solvent-assisted adlayer-PT-II).

For the aqueous isostructural rutile oxide interfaces, one would wonder how adsorbed water would affect the proton hopping mechanisms. To further explore the difference of surface properties and PT pathways for rutile oxide systems, comparison of the $\Delta p K_a$, degree α , and free energy ΔA_{diss} of terminal water dissociation, the water adsorption energy E_{adst} and PT pathways of a series rutile oxides $(SnO_{2}, TiO_{2}, and$ IrO_2) are listed in Table 4. In the dilute limit, the dissociation of terminal water on the oxide surface is determined by the difference $\Delta p K_a$ between $p K_{a1}$ (acidity of terminal water) and $p K_{a2}$ (acidity of bridge oxygen).^{40,63} It is found the values of $\Delta p K_a$ for IrO₂ and SnO₂ are similar, and both are smaller than the TiO₂ surface. Accordingly, the values of α for IrO₂ (0.80⁵⁹) and SnO_2 (0.63) are significantly higher than that for TiO₂ (0.02^{52}) (Table 4). Meanwhile, it is found that a positive correlation exists between the water adsorption energy E_{ads} and the degree of terminal water dissociation α , as the IrO₂(110) surface has the highest E_{ads} (-1.92 eV⁸⁸) as well as the highest α (0.80⁵⁹) (Table 4).

For the PT pathways on aqueous rutile oxide interfaces, it is found that only mediated-PT occurs on the $IrO_2(110)$ surface while both surface-PT and mediated-PT go through at TiO_2 and SnO_2 systems. However, the energy barriers of each PT type on TiO_2 and IrO_2 surfaces have not been reported yet, though the overall energy barrier from molecular water to surface hydroxyl on $TiO_2(110)$ surface has been studied.⁵⁸ A plausible explanation can be provided based on what we observed on the SnO_2 surface, where the energy barrier of mediated-PT is significantly smaller than the surface-PT, leading to the preference of the mediated-PT pathway on IrO_2 surfaces.

CONCLUSIONS

In summary, by applying a combination of ab initio and deep potential molecular dynamics methods, we have studied the interfacial PT mechanisms by selecting the $SnO_2(110)/H_2O$ interface as an example of rutile oxide with the characteristic of fast PT processes. First, we found three types of PT pathways among the interfacial groups at the $SnO_2(110)/H_2O$ interface: (1) proton transfer from terminal adsorbed water to bridge oxygen directly (surface-PT) or (2) assisted by a solvent water molecule (mediated-PT), and (3) proton transfer between two terminal groups directly (adlayer PT). We calculated the free



Figure 7. Schematic mechanisms of proton transfer at oxide surfaces which are summarized from the reported literature: ${}^{38,51,58-62}$ proton transfer between terminal H₂O and surface oxygen O_s directly (a) or via a solvent water molecule (b); proton transfer between two surface oxygen atoms directly (c) or assisted by a solvent water molecule (d); proton transfer between two terminal groups H₂O and OH⁻ directly (e), via a solvent water molecule (f) or via several solvent water molecules (g). The proton donor/acceptor O_d/O_a, the transferred proton, and the H-bond are highlighted in red, blue, and green, respectively.

Table 4. Comparison of ΔpK_a (Acidity Difference between Adsorbed Terminal Water and Protonated Bridge Oxygen $O_{br}H^+$), Degree α , and Free Energy ΔA_{diss} (Obtained from eq 6, eV) of Terminal Water Dissociation, Water Adsorption Energy E_{ads} (eV), and PT Pathways on Rutile SnO₂(110), TiO₂(110), and IrO₂(110) Surfaces

system	$\Delta p K_a^{a}$	α^{a}	$\Delta A_{\rm diss}$	E_{ads}^{b}	PT pathways
SnO ₂ (110)/ H ₂ O	-0.3^{63}	0.63	-0.03	-1.5	surface-PT, mediated-PT, adlayer-PT
TiO ₂ (110)/ H ₂ O	3.9 ⁸⁷	0.020 ⁵²	0.22	-0.87 ⁴⁰	surface-PT, mediated-PT, adlayer-PT ⁶¹
$\frac{IrO_{2}(110)}{H_{2}O}/$	-0.4 ⁵⁹	0.80 ⁵⁹	-0.08	-1.92 ⁸⁸	adlayer-PT, water- assisted adlayer- PT, mediated- DT ⁵⁹

^{*a*}The results of ΔpK_a and α for SnO₂ and TiO₂ were computed using PBE functional, for IrO₂ was computed using SCAN functional. Note that pK_a 's of SnO₂ and TiO₂ were calculated using the free energy perturbation method while the pK_a of IrO₂ was obtained from an enhanced sampling method. ^{*b*}The E_{ads} of SnO₂, TiO₂ and IrO₂ were calculated by one monolayer of half dissociated water, molecular water and dissociated water with PBE functional, respectively.

energy landscapes for the three PT reactions and found that the mediated-PT has the lowest energy barrier and the fastest relative PT rate by the assistance of a solvent molecule with a shorter H-bond and a specific orientation of terminal water. Second, we found the full solvation environment plays a crucial role in the water-mediated proton conduction mechanism while having little effect on the direct PT reactions by comparing to the CI-NEB studies of a monolayer of adsorbed water on the SnO₂(110) surface. The average degree of water dissociation α is estimated as 0.63, and the free energy of water dissociation ΔA_{diss} is calculated as -0.03 eV. Finally, we discuss the PT mechanisms on aqueous rutile oxide interfaces by comparing an oxide series composed of SnO_2 , TiO_2 , and IrO_2 . We believe our work provides valuable molecular understanding for proton transfer mechanisms at such heterogeneous oxide interfaces, which is an important step in many chemical processes, including electrocatalysis, heterogeneous catalysis, or other energy production and storage.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/prechem.4c00056.

Machine learning potential training, comparison of free energy landscapes, and convergence of free energies (PDF)

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Author Contributions

[#]M.J. and Y.-B.Z. contributed equally to this work. J.C. and M.J. conceived and designed the project, M J. performed the AIMD calculations and analyzed the data, and Y.-B.Z. performed the DPMD calculations. The first draft of the manuscript was prepared by M.J. and Y.-B.Z., and the final draft was edited by all the authors.

Notes

The authors declare no competing financial interest.

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