Structured demographic buffering: A framework to explore the environment drivers and demographic mechanisms underlying demographic buffering

Supplementary online materials

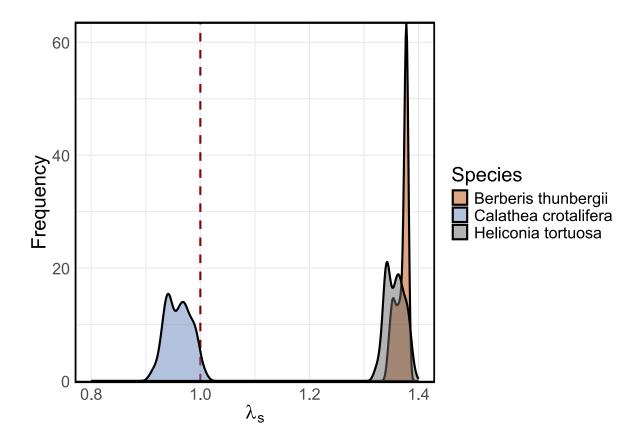
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Table of Contents

Supplementary Figure 1. Distribution of λs from simulations across the environment autocorrelation – variance parameter space
Supplementary Table 1. Formulas, regressions and parameters used to construct the IPMs for <i>Berberis thunbergii</i>
Supplementary Table 2. Formulas, regressions and parameters used to construct the IPMs for <i>Calathea crotalifera.</i>
Supplementary Table 3. Formulas, regressions and parameters used to construct the IPMs for <i>Heliconia tortuosa</i> .
Standardised analysis pipeline
Supplementary Table 4. Model selection to quantify the effects of environmental autocorrelation and variance on demographic buffering (DB) in <i>Berberis thunbergii</i>
Supplementary Table 5. Model selection to quantify the effects of environmental autocorrelation and variance on demographic buffering (DB) in <i>Calathea crotalifera</i>
Supplementary Table 6. Model selection to quantify the effects of environmental autocorrelation and variance on demographic buffering (DB) in <i>Heliconia tortuosa</i>
Supplementary Table 7. Model selection to quantify the effects of environmental autocorrelation and variance on the differences of
Supplementary Table 8. Model selection to quantify the effects of environmental autocorrelation and variance on the differences of
Supplementary Table 9. Model selection to quantify the effects of environmental autocorrelation and variance on the differences of
Supplementary Table 10. Model selection to quantify the effects of environmental autocorrelation and variance on the mean buffered size in <i>Berberis thunbergii</i>
Supplementary Table 11. Model selection to quantify the effects of environmental autocorrelation and variance on the mean buffered size in <i>Calathea crotalifera</i>
Supplementary Table 12. Model selection to quantify the effects of environmental autocorrelation and variance on the mean buffered size in <i>Heliconia tortuosa</i>
Supplementary Table 13. Model selection to quantify the effects of environmental autocorrelation and variance on the P-F contribution in <i>Berberis thunbergii</i>
Supplementary Table 14. Model selection to quantify the effects of environmental autocorrelation and variance on the P-F contribution in <i>Calathea crotalifera</i>
Supplementary Table 15. Model selection to quantify the effects of environmental autocorrelation and variance on the P-F contribution in <i>Heliconia tortuosa</i>



Supplementary Figure 1. Distribution of λ_s from simulations across the environment autocorrelation – variance parameter space. The red dashed line represents a population that stays stable when projected across time steps (*i.e.*, $\lambda_s = 1$). Values distributed to the left of the red dashed line represent populations who will asymptotically decline in number across time steps (*i.e.*, $\lambda_s < 1$), whilst values distributed to the right of the red dashed line represent populations that will asymptotically increase across time steps (*i.e.*, $\lambda_s > 1$).

Supplementary Table 1. Formulas, regressions and parameters used to construct the IPMs for *Berberis thunbergii*.

Cor	nstruction	Model	Parameter
Density-independent environmentally stochastic IPM		$n(z',t+1) = \int_{\alpha}^{\omega} K(z',z,\psi_t) n(z,t) dz$ $\psi_t = \{T_t, P_t, PAR_t, N_t, pH_t\}$	$\alpha = 2$ $\omega = 25$ $z = \log(\text{plant area})$ $\psi = \text{an array containing}$ climate values
<u> </u>	K -kernel	$K(z',z,\psi_t) = P(z',z,\psi_t) + F(z',z,\psi_t)$	
	P -subkernel	$P(z', z, \psi_t) = s(z, \psi_t) * g(z', z, \psi_t)$	
Sub-kernels	<i>F</i> -subkernel	$F(z', z, \psi_t) = f_s(z) * fl_p(z) * germ_p(\psi_t)$ $* sdl_s(z')$	
	Survival	$logit(s(z, \psi_t)) = s_i + s_z * z + s_T * T_t + s_P * P_t$ $+ s_{PAR} * PAR_t + s_N * N_t + s_{pH}$ $* pH_t$	$s_i = -11.8$ $s_z = 1.05$ $s_T = 1.11$ $s_P = 0.22$ $s_{PAR} = -0.52$ $s_N = -0.1$ $s_{pH} = 0.11$
Demographic functions	Growth	$g(z', z, \psi_t) = \operatorname{dnorm}(z', g_{\mu}(z, \psi_t), g_{sd})$ $g_{\mu}(z, \psi_t) = g_z * z + g_T * T_t + g_P * P_t + g_{PAR}$ $* PAR_t + g_N * N_t + g_{pH} * pH_t$	$g_{sd} = 1.48$ $g_z = 1.02$ $g_T = 0.65$ $g_P = 0.02$ $g_{PAR} = 0.59$ $g_N = -0.04$ $g_{pH} = 0.4$
	Reproduction	$f_s(z) = \exp(seed_i + seed_z * z)$ $\log \operatorname{logit}(fl_p(z)) = fl_i + fl_z * z$	$seed_i = -23.01$ $seed_z = 1.32$ $fl_i = -33.43$ $fl_z = 1.68$

		$logit(germ_p(\psi_t)) = germ_i + germ_T * T_t$	$germ_i = -11.8$
		$+ germ_P * P_t + germ_{PAR}$ $* (PAR_t/0.018) + germ_{pH}$	$germ_T = 0.51$ $germ_P = -0.02$
		$*pH_t$	$germ_{PAR} = -0.02$
			$germ_{pH} = 0.26$
		$sdl_s(z') = dnorm(z', sdl_{\mu}, sdl_{sd})$	$sdl_{\mu} = 10.23$
			$sdl_{sd} = 1.581$
	Mean temperature in	$T \sim N(0, 1.5)$	
	warmest month		
Envisonment	Mean May	$P \sim N(0, 1.5)$	
Environment values	precipitation		
	PAR	<i>PAR</i> ~ N(0, 1.5)	
	Soil Nitrogen	$N \sim N(0, 1.5)$	
	Soil pH	$pH \sim N(0, 1.5)$	

Supplementary Table 2. Formulas, regressions and parameters used to construct the IPMs for *Calathea crotalifera*.

for Calathea Cor	nstruction	Model	Parameter
Density-independent environmentally		$n(z',t+1) = \int_{\alpha}^{\omega} K(z',z,\psi_t) n(z,t) dz$	$\alpha = 0.57$ $\omega = 11.9$ $z = \text{leaf area}$
stoc	chastic IPM	$\psi_t = \{j_t, A_t\}$	ψ = an array containing climate values
1	K -kernel	$K(z',z,\psi_t) = P(z',z,j_t,A_t) + F(z',z,j_t)$	
	P -kernel	$P(z', z, j_t, A_t) = s(z, j_t) * g(z', z, j_t, A_t)$	
Sub-kernels		$F(z', z, j_t) = r_p(z, j_t) * r_o(z, j_t) * n_f * n_s * s_s(j_t)$	$n_f = 23$
Suo-kerners	<i>F</i> -kernel	$* sdl_s(j_t) * sdl_{size}(z', j_t)$	$n_s=3$
		$\log i(s(z, \psi_t)) = s_i + s_z * z + s_j * j_t + s_{z*j} * z * j_t$	$s_i = -2.74$
			$s_z = 0.95$
	Survival		$s_j = 0.07$
			$s_{z*j} = -0.02$
		$g(z', z, j_t, A_t) = \operatorname{dnorm}(z', g_{\mu}(z, j_t, A_t), g_{sd})$	$g_{sd} = 1.53$
		$g_{\mu}(z,j_t,A_t) = g_i + g_z * z + g_j * j_t + g_A * A_t$	$g_i = 0.76$
		$+g_{z*j}*z*j_t+g_{z*A}*z*A_t$	$g_z = 0.9$
		$+g_{j*A}*j_t*A_t+g_{z*j*A}*z*j_t$	$g_j = 0.03$
Demographic	Growth	$*A_t$	$g_A = 0.006$
functions			$g_{z*j} = -0.001$
runctions			$g_{z*A} = 0.00045$ $g_{j*A} = -0.0052$
			$g_{j*A} = -0.0052$
			$g_{z*j*A} = 0.00035$
		$logit(r_p(z, j_t)) = r_{p,i} + r_{p,z} * z + r_{p,j} * j_t + r_{p,z*j} * z$	$r_{p,i} = -13.23$
	D ow J'	$*j_t$	$r_{p,z} = 1.401$
	Reproduction		$r_{p,j} = -0.213$
			$r_{p,z*j} = 0.043$
		$r_o(z, j_t) = \exp(r_{o,i} + r_{o,z} * z + r_{o,j} * j_t + r_{o,z*j} * z)$	$r_{o,i} = -6.673$
		$*j_t)$	$r_{o,z} = 0.829$

			$r_{o,j} = 0.067$
			$r_{o,j} = 0.067$ $r_{o,z*j} = -0.007$
		$s_s(j_t < 6) = 0.29$	
		$s_s(j_t \ge 6) = 0.32$	
		$sdl_s(j_t < 6) = 0.14$	
		$sdl_s(j_t \ge 6) = 0.95$	
		$sdl_{size}(z', j_t < 6) = dnorm(z', 3.08, 0.54)$	
		$sdl_{size}(z', j_t \ge 6) = dnorm(z', 2.88, 1.4)$	
Environment	Canopy openness*	$j \sim N(3, 1.4)$	
values	Photosynthetic rate*	$A \sim N(6, 0.8)$	

^{*} In Westerband and Horvitz (2016), canopy openness (j) and photosynthetic rate (A) were modelled as random samples from a sequence of values or draws from a uniform distribution. Specifically canopy openness was realized at time t as random draws from the sequence $\{1, 2, 3, 4, 5\}$ whilst photosynthetic rate was realized at time t as random draws from a uniform distruction (i.e., $A \sim U(5,7)$). However, since our manipulation of the environment involves explicitly changing the temporal variance of a series, we coerced the distributions into normal distributions with the same mean and reported variance of the original sampling distributions reported in Westerband and Horvitz (2016).

Supplementary Table 3. Formulas, regressions and parameters used to construct the IPMs for *Heliconia tortuosa*.

Cor	nstruction	Model	Parameter
Density-independent environmentally		$n(z',t+1) = \int_{\alpha}^{\omega} K(z',z,\psi_t) n(z,t) dz$	$\alpha = 0.78$ $\omega = 11.07$
stoc	chastic IPM		z = leaf area
		$\psi_t = \{j_t, A_t\}$	ψ = an array containing climate values
1	K -kernel	$K(z',z,\psi_t) = P(z',z,j_t,A_t) + F(z',z,j_t)$	
	P -kernel	$P(z', z, j_t, A_t) = s(z, j_t) * g(z', z, j_t, A_t)$	
		$F(z', z, j_t) = r_p(z, j_t) * r_o(z, j_t) * n_f * n_s * s_s(j_t)$	$n_f = 37$
Sub-kernels	F -kernel	$* sdl_s(j_t) * sdl_{size}(z', j_t)$	$n_s = 2.5$
		$logit(s(z, \psi_t)) = s_i + s_z * z + s_j * j_t + s_{z*j} * z * j_t$	$s_i = -2.05$
	Survival		$s_z = 0.78$
			$s_z = 0.78$ $s_j = -0.22$
			$s_{z*j} = 0.05$
		$g(z', z, j_t, A_t) = \operatorname{dnorm}(z', g_{\mu}(z, j_t, A_t), g_{sd})$	$g_{sd} = 0.71$
		$g_{\mu}(z, j_t, A_t) = g_i + g_z * z + g_j * j_t + g_A * A_t$	$g_i = 2.6$
		$+ g_{z*j} * z * j_t + g_{z*A} * z * A_t$	$g_z = 0.56$
		$+ g_{j*A} * j_t * A_t + g_{z*j*A} * z * j_t$	$g_j = -1.55$
Demographic	Growth	$*A_t$	$g_A=0.44$
functions			$g_{z*j} = 0.18$
ranctions			$g_{z*A} = -0.034$ $g_{j*A} = 0.014$
			$g_{j*A} = 0.014$
			$g_{z*j*A} = -0.0014$
		$logit(r_p(z, j_t)) = r_{p,i} + r_{p,z} * z + r_{p,j} * j_t + r_{p,z*j} * z$	$r_{p,i} = -12.55$
	Reproduction	$*j_t$	$r_{p,z} = 1.527$ $r_{p,j} = 0.154$ $r_{p,z*j} = -0.013$
			$r_{p,j}=0.154$
			$r_{p,z*j} = -0.013$
		$r_o(z, j_t) = \exp(r_{o,i} + r_{o,z} * z + r_{o,j} * j_t + r_{o,z*j} * z$	$r_{o,i} = -1.009$
		$*j_t)$	$r_{o,z} = 0.157$

			$r_{o,j} = -0.382$
			$r_{o,z*j} = 0.048$
		$s_s(j_t < 6) = 0.15$	
		$s_s(j_t \ge 6) = 0.2$	
		$sdl_s(j_t < 6) = 0.26$	
		$sdl_s(j_t \ge 6) = 0.33$	
		$sdl_{size}(z', j_t < 6) = dnorm(z', 2.73, 0.71)$	
		$sdl_{size}(z', j_t \ge 6) = dnorm(z', 2.34, 1.17)$	
Environment	Canopy openness	$j \sim N(3, 1.4)$	
values	Photosynthetic rate	$A \sim N(6.5, 0.8654937)$	

^{*} In Westerband and Horvitz (2016), canopy openness (j) and photosynthetic rate (A) were modelled as random samples from a sequence of values or draws from a uniform distribution. Specifically canopy openness was realized at time t as random draws from the sequence $\{1, 2, 3, 4, 5\}$ whilst photosynthetic rate was realized at time t as random draws from a uniform distruction (i.e., $A \sim U(5,8)$). However, since our manipulation of the environment involves explicitly changing the temporal variance of a series, we coerced the distributions into normal distributions with the same mean and reported variance of the original sampling distributions reported in Westerband and Horvitz (2016).

Standardised analysis pipeline.

To investigate the roles of environmental autocorrelation and variance on demographic buffering, we used a standardised analysis pipeline to reproducibly model the linear and nonlinear impacts of environment components (*i.e.*, environment autocorrelation and variance).

The standardised analysis pipeline has two phases. First, a suite of pre-defined statistical models were used to model the specified response variable (e.g., **P-F** contribution). These models were classified as a priori (see below).

A priori models:

- 1. response variable $\sim \sigma^2 + \varphi + \sigma^2 * \varphi$
- 2. response variable $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$
- 3. response variable $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$
- 4. response variable $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$
- 5. response variable $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$
- 6. response variable $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$
- 7. response variable $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$
- 8. response variable $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$
- 9. response variable $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$

We chose this list of statistical models as they (1) contain linear and linear-interaction terms of environment autocorrelation (φ) and environment variance (σ^2) (see the first three terms of each model), (2) they sequentially add combinations of environment autocorrelation and variance up to a cubic term and (3) simplifies the combination of possible models generate from 7 predictors (127 possible combinations).

Supplementary Table 4. Model selection to quantify the effects of environmental autocorrelation and variance on demographic buffering (DB) in *Berberis thunbergii*. This model selection corresponds to the data show in Figure 2A in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-1333.377	
	2	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-1566.159	
	3	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-1681.584	
	4	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-1349.455	
	5	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-1619.828	
	6	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-1783.319	SELECTED
	7	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-1347.510	
	8	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-1618.012	
	9	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-1781.704	
Complete f	formula	$DB \sim -0.48626 + 1.2427383 * [\sigma^2] + 0.0004573 * [\varphi] + 0.0256003 * [\varphi]$	$\sigma^2 * \varphi$] - 1.003696	$8 * [(\sigma^2)^2]$
		$-\ 0.0454271*[\varphi^2] - 0.0501562*[\varphi^3]$			

Supplementary Table 5. Model selection to quantify the effects of environmental autocorrelation and variance on demographic buffering (DB) in *Calathea crotalifera*. This model selection corresponds to the data show in Figure 2B in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-925.2545	
	2	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-953.4019	
	3	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-980.3957	
	4	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-927.4461	
	5	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-956.2009	
	6	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-983.8628	SELECTED
	7	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-925.4511	
	8	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-954.2067	
	9	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-981.8694	
Complete for	rmula	$DB \sim -0.26329 + 1.224845 * [\sigma^2] - 0.027656 * [\varphi] + 0.059247 * [\alpha]$	$\sigma^2 * \varphi$	- 1.215454 ×	$*[(\sigma^2)^2]$
		$+\ 0.049503 \ * [\varphi^2] - 0.1.6741 * [\varphi^3]$			

Supplementary Table 6. Model selection to quantify the effects of environmental autocorrelation and variance on demographic buffering (DB) in *Heliconia tortuosa*. This model selection corresponds to the data show in Figure 2C in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-1891.832	
	2	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-1913.937	
	3	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-1930.921	
	4	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-1895.561	
	5	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-1918.323	
	6	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-1935.878	SELECTED
	7	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-1893.568	
	8	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-1916.330	
	9	$DB \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-1933.886	
Complete for	rmula	$DB \sim -0.05349 + 0.1897 * [\sigma^2] + [6.797e - 04] * [\varphi] - [9.386e - 05]$	$*[\sigma^2]$	$* \varphi] - 0.1656$	$6*[(\sigma^2)^2]$
		$+ 0.005201 * [\varphi^2] - 0.01033 * [\varphi^3]$			

Supplementary Table 7. Model selection to quantify the effects of environmental autocorrelation and variance on the differences of $\sum E_{a_{ij}}^{\sigma^2}$ and $\sum E_{a_{ij}}^{\sigma^2} | \text{ASD}$ in *Berberis thunbergii*. This model selection corresponds to the data show in Figure 3B in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-741.7773	
	2	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-769.6791	
	3	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-890.4373	
	4	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-744.6596	
	5	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-773.2640	
	6	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-898.1634	SELECTED
	7	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-742.7117	
	8	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-771.3237	
	9	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-896.2684	
Complete for	rmula	$differences \sim -1.969071 + 3.965287 * [\sigma^2] - 0.512308 * [$	φ] + 0.3	$64988 * [\sigma^2 >$	* \varphi]
		$-1.970633*[(\sigma^2)^2] - 0.074138*[\varphi^2] + 0.2$	199437 *	$[\varphi^3]$	

Supplementary Table 8. Model selection to quantify the effects of environmental autocorrelation and variance on the differences of $\sum E_{a_{ij}}^{\sigma^2}$ and $\sum E_{a_{ij}}^{\sigma^2} | \text{ASD}$ in *Calathea crotalifera*. This model selection corresponds to the data show in Figure 3E in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-1718.857	
	2	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-1756.217	
	3	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-1784.586	
	4	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-1759.530	
	5	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-1806.057	
	6	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-1843.012	SELECTED
	7	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-1757.962	
	8	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-1804.593	
	9	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-1841.650	
Complete for	rmula	$differences \sim 0.638800 - 1.276380 * [\sigma^2] - 0.019216 * [\varphi] + 0.02904$	$41 * [\sigma^2]$	$* \varphi] + 0.637$	$492 * [(\sigma^2)^2]$
		$-\ 0.009601 \ * [arphi^2] - 0.018321 \ * [arphi^3]$			

Supplementary Table 9. Model selection to quantify the effects of environmental autocorrelation and variance on the differences of $\sum E_{a_{ij}}^{\sigma^2}$ and $\sum E_{a_{ij}}^{\sigma^2} | \text{ASD}$ in *Heliconia tortuosa*. This model selection corresponds to the data show in Figure 3H in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-1380.828	
	2	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-1386.508	
	3	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-1473.794	
	4	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-1392.269	
	5	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-1398.431	
	6	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-1492.824	SELECTED
	7	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-1391.522	
	8	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-1397.730	
	9	$differences \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-1492.822	
Complete for	rmula	$differences \sim -0.804339 + 1.592423 * [\sigma^2] - 0.017227 * [\varphi] - 0.0499$	$0087 * [\sigma^2]$	$[2*\varphi] - 0.782$	$2833 * [(\sigma^2)^2]$
		$-\ 0.009305*[arphi^2] + 0.067106*[arphi^3]$			

Supplementary Table 10. Model selection to quantify the effects of environmental autocorrelation and variance on the mean buffered size in *Berberis thunbergii*. This model selection corresponds to the data show in Figure 3C in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-1808.928	
	2	mean buffered size \sim $\sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-2170.820	
	3	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-2291.923	SELECTED
	4	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-1807.061	
	5	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-2169.493	
	6	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-2291.086	
	7	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-1805.061	
	8	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-2167.493	
	9	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-2289.087	
Complete for	rmula	mean buffered size \sim 0.6679336 $-$ 0.0313268 $*$ [σ^2] $-$ 0.0051673	$* [\varphi] -$	0.0019560 *	$[\sigma^2 * \varphi]$
		$-\ 0.0175639*[\varphi^2] + 0.0133206*[\varphi^3]$			

Supplementary Table 11. Model selection to quantify the effects of environmental autocorrelation and variance on the mean buffered size in *Calathea crotalifera*. This model selection corresponds to the data show in Figure 3F in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-3226.940	
	2	mean buffered size \sim $\sigma^2+\varphi+\sigma^2*\varphi+\varphi^2$	6	-3241.007	
	3	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-3261.367	SELECTED
	4	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-3225.148	
	5	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-3239.230	
	6	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-3259.614	
	7	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-3223.159	
	8	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-3237.243	
	9	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-3257.628	
Complete for	rmula	mean buffered size \sim 0.8956762 + 0.0007139 * $[\sigma^2]$ + 0.0009980	$* [\varphi] -$	0.0011847 *	$[\sigma^2 * \varphi]$
		$+\ 0.0002204*[\varphi^2] + 0.0005852*[\varphi^3]$			

Supplementary Table 12. Model selection to quantify the effects of environmental autocorrelation and variance on the mean buffered size in *Heliconia tortuosa*. This model selection corresponds to the data show in Figure 3I in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-1971.458	
	2	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-2090.884	
	3	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-2119.626	SELECTED
	4	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-1970.073	
	5	mean buffered size \sim $\sigma^2+\varphi+\sigma^2*\varphi+(\sigma^2)^2+\varphi^2$	7	-2089.940	
	6	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-2118.838	
	7	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-1968.075	
	8	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-2087.944	
	9	mean buffered size $\sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-2116.842	
Complete for	mula	mean buffered size \sim 0.8411429 + 0.0082338 * $[\sigma^2]$ - 0.1178307	* [\varphi] +	0.0912694 *	$[\sigma^2 * \varphi]$
		$+ 0.0088286 * [\varphi^2] + 0.0087587 * [\varphi^3]$			

Supplementary Table 13. Model selection to quantify the effects of environmental autocorrelation and variance on the **P-F** contribution in *Berberis thunbergii*. This model selection corresponds to the data show in Figure 4B in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-8282.140	
	2	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-8747.482	
	3	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-8783.395	
	4	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-8286.741	
	5	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-8804.515	
	6	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-8853.171	SELECTED
	7	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-8284.763	
	8	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-8802.731	
	9	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-8851.442	
Complete for	rmula	$\mathbf{P} - \mathbf{F} \ contribution \sim [5.943e - 08] - [1.541e - 07] * [\sigma^2] + [1.951e - 0]$	9] * [φ]	- [6.017 <i>e</i> -	$09] * [\sigma^2 * \varphi]$
		+ $[1.208e - 07] * [(\sigma^2)^2] + [1.038e - 08] * [\varphi^2] + [3.633]$	3e – 09]	$ *[\varphi^3]$	

Supplementary Table 14. Model selection to quantify the effects of environmental autocorrelation and variance on the **P-F** contribution in *Calathea crotalifera*. This model selection corresponds to the data show in Figure 4C in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection	
A priori	1	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-8011.995		
	2	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-8040.051		
	3	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-8067.034		
	4	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-8014.190		
	5	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-8042.851		
	6	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-8070.503	SELECTED	
	7	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-8012.195		
	8	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-8040.857		
	9	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-8068.509		
Complete for	rmula	$\mathbf{P} - \mathbf{F} \ contribution \sim -\left[3.810e - 08\right] + \left[1.773e - 07\right] * \left[\sigma^{2}\right] - \left[4.000e - 09\right] * \left[\varphi\right] + \left[8.580e - 09\right]$				
		$* [\sigma^2 * \varphi] - [1.760 - 07] * [(\sigma^2)^2] + [7.155e - 09] * $	$[\varphi^2]$ – [1	.545 <i>e</i> – 08] *	$*[\varphi^3]$	

Supplementary Table 15. Model selection to quantify the effects of environmental autocorrelation and variance on the **P-F** contribution in *Heliconia tortuosa*. This model selection corresponds to the data show in Figure 4D in the main text. Environmental autocorrelation is denoted as φ whilst environmental variance is denoted as σ^2 .

Model type	Model number	Model	DF	AIC	Selection
A priori	1	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi$	5	-8958.788	
	2	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2$	6	-8986.418	
	3	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + \varphi^2 + \varphi^3$	7	-9010.538	
	4	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2$	6	-8962.007	
	5	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2$	7	-8990.381	
	6	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + \varphi^2 + \varphi^3$	8	-9015.246	SELECTED
	7	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3$	7	-8960.023	
	8	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2$	8	-8988.399	
	9	$\mathbf{P} - \mathbf{F} \ contribution \sim \sigma^2 + \varphi + \sigma^2 * \varphi + (\sigma^2)^2 + (\sigma^2)^3 + \varphi^2 + \varphi^3$	9	-9013.267	
Complete for	rmula	$P - F contribution \sim -[6.997e - 09] + [2.657e - 08] * [\sigma^2] - [4.22]$	5e – 11	$[]*[\varphi]+[7.5]$	92e - 10]
		* $[\sigma^2 * \varphi] - [2.392e - 08] * [(\sigma^2)^2] + [8.669e - 10] *$	$\langle [arphi^2] - [$	[1.796e – 09]	$*[\varphi^3]$