

RESEARCH ARTICLE

# Fin Whale Sound Reception Mechanisms: Skull Vibration Enables Low-Frequency Hearing

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OPEN ACCESS

**Citation:** Cranford TW, Krysl P (2015) Fin Whale Sound Reception Mechanisms: Skull Vibration Enables Low-Frequency Hearing. PLoS ONE 10(1): e0116222. doi:10.1371/journal.pone.0116222

**Academic Editor:** Yan Ropert-Coudert, Institut Pluridisciplinaire Hubert Curien, FRANCE

**Received:** July 1, 2014

**Accepted:** December 3, 2014

**Published:** January 29, 2015

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**Data Availability Statement:** The relevant data is described in the manuscript, especially in the supplementary information.

**Funding:** TWC received funding from Michael Wiese and James Eckman, at the Office of Naval Research (N00014-12-1-0516); Frank Stone, Ernie Young, and Robert Gisinier at the Chief of Naval Operations Environmental Readiness Division as well as Curtis Collins and John Joseph at the Naval Postgraduate School (N00244-08-1-0025). The funders had no role in study design, data collection and analysis, decision to publish, or preparation of the manuscript.

## Abstract

Hearing mechanisms in baleen whales (Mysticeti) are essentially unknown but their vocalization frequencies overlap with anthropogenic sound sources. Synthetic audiograms were generated for a fin whale by applying finite element modeling tools to X-ray computed tomography (CT) scans. We CT scanned the head of a small fin whale (*Balaenoptera physalus*) in a scanner designed for solid-fuel rocket motors. Our computer (finite element) modeling toolkit allowed us to visualize what occurs when sounds interact with the anatomic geometry of the whale's head. Simulations reveal two mechanisms that excite both bony ear complexes, (1) the skull-vibration enabled bone conduction mechanism and (2) a pressure mechanism transmitted through soft tissues. Bone conduction is the predominant mechanism. The mass density of the bony ear complexes and their firmly embedded attachments to the skull are universal across the Mysticeti, suggesting that sound reception mechanisms are similar in all baleen whales. Interactions between incident sound waves and the skull cause deformations that induce motion in each bony ear complex, resulting in best hearing sensitivity for low-frequency sounds. This predominant low-frequency sensitivity has significant implications for assessing mysticete exposure levels to anthropogenic sounds. The din of man-made ocean noise has increased steadily over the past half century. Our results provide valuable data for U.S. regulatory agencies and concerned large-scale industrial users of the ocean environment. This study transforms our understanding of baleen whale hearing and provides a means to predict auditory sensitivity across a broad spectrum of sound frequencies.

## Introduction

Mysticete whales are the largest animals on Earth. The pelagic balaenopterids may reach 30 meters in length and produce low-frequency sounds in the range of 10–200 Hz [1, 2]. Most other mysticetes are primarily coastal species, less than 20 meters in length and produce sounds

**Competing Interests:** The authors have declared that no competing interests exist.

below 10 kHz. These acoustic frequency bands are presumably used for very long-range communication, managing social structure, and perhaps echo-navigation [3, 4].

The acoustic bandwidths used by mysticetes overlap with anthropogenic sound sources, raising concerns over potential deleterious effects from increasing trends in ocean noise [5, 6, 7, 8, 9]. Risk assessment is hampered by a lack of information about mysticete sound reception mechanisms and their sensitivity to various acoustic frequencies [10] [Science 10 January 2014, Vol. 343 no. 6167 p. 128. doi:10.1126/science.343.6167.128], [11].

To date, attempts to estimate the hearing parameters of baleen whales fall into three categories based on inferential methods: (A) the vocalizations of various species, based on the assumption that they can hear the sounds they generate [12, 13, 14, 15, 16]; (B) the anatomic structure of the ears, based on and compared to the functional morphology of the ears in well-known mammalian species [17, 18, 19, 20, 21, 22, 23]; and (C) behavioral reactions of wild mysticetes to playback experiments, based on the assumption that observations of behavioral reactions are interpretable in well-designed, controlled sound exposure experiments [24, 25, 26, 27, 28, 29]. Generally, these methods cannot predict mysticete sound reception mechanisms or reliably extract frequency sensitivity based on predicted sound exposure levels.

We constructed a finite element modeling system, based on serial CT scans, that allows us to predict low-frequency hearing sensitivity and identify sound reception mechanisms in cetaceans [30]. Recently, simulations from our vibroacoustic toolkit (VATk) have been validated [31, 32], used to study toothed whale bioacoustics [22, 33, 34], and hearing mechanisms in fish [35, 36]. This study shows that mysticete sound reception is primarily governed by bone conduction, as incident sound induces skull vibrations that are transmitted to both bony ear complexes.

## Materials and Methods

### Specimen

On 20 November 2003 a newborn male fin whale (*Balaenoptera physalus*) calf stranded alive on Sunset Beach in Orange County, California. Personnel from Sea World, San Diego and the California Marine Mammal Stranding Network attempted a rescue of this animal but it died during transport. This work was carried out in strict accordance with the Stranding Agreement, issued pursuant to Section 112(c) of the Marine Mammal Protection Act, between NOAA's National Marine Fisheries Service Southwest Region (NMFS-SWR) and SeaWorld San Diego (SeaWorld) (administrative reference number 151410SWR200900478:SMW).

This stranded fin whale was 550 cm long, weighed 1,165 kg, and was assigned a Field-ID (JEH520) by John E. Heyning at the Los Angeles County Museum of Natural History. The average length at birth for Northern Pacific fin whales is between 600–650 cm, while adults can reach 2400 cm in length [37]. The necropsy was performed by Dr. Judy St. Leger with help from additional personnel at SeaWorld San Diego, the Los Angeles County Museum of Natural History, and the California Marine Mammal Stranding Network. This specimen was shorter than average for a neonate, however there was evidence of expanded lungs but no evidence of gastric milk. The umbilicus was not yet closed but fetal folds were not appreciated. This suggests an animal of a few days of age. Poor development is reasonable based on the thin nutritional condition. This suggests (but cannot confirm) to either represent placental issues or a pre-term delivery of a live calf that did not thrive due to medical concerns (Judy St. Leger, personal communication). Tissue property measurements were made by Dr. John Hildebrand and his research team from the Scripps Institution of Oceanography. The intact head was removed for further study and frozen within 24 hours of death. After sufficient time to allow for complete freezing, the head was placed inside a 48 inch diameter fiber Sonotube, and a custom

container was constructed, as described previously [38]. The contained specimen was then transported to Hill Air Force Base in Utah and scanned in an industrial CT scanner. The CT data was processed into a three-dimensional image volume that provided the anatomic geometry of the animal used in our models.

After CT scanning, the head (in its container) was returned to a freezer until it was dissected on 21 August 2006. When the necropsy of the head was conducted, the tissue handling protocol was approved by the Graduate and Research Affairs, Institutional Animal Care and Use Committee at San Diego State University (APF#: 09-05-014B). Permission to possess the head was provided by a Letter of Authorization from the National Oceanic and Atmospheric Administration and the National Marine Fisheries Service Southwest Region (Administrative File: 151408SWR2013PROOO). The prepared skull was accessioned by the Museum of Biodiversity at San Diego State University. The specimen now resides there under Accession-ID S-970.

## Computational approach

Each bony ear complex in cetaceans is a conglomeration of various bones that comprise the *tympanoperiotic complex* (TPC), which can be modeled to some approximation as a collection of vibrating solids. For example, the work reported here uses a finite element model (a complete description of the finite element model and the input parameters used in this study can be found in the [S1 File](#)). The computational problem is the so-called forced harmonic vibration analysis, which can be readily solved [39], producing results (in terms of a transfer function) that transform the incident sound pressure into some measure of input to the cochlea. The cochlear input from the stapes can be transformed into an approximation of an audiogram. In order to exercise such simulations we need to determine the forcing applied to the model of the TPC.

An incident acoustic wave of a given pressure amplitude in the sea water surrounding an animal interacts with the tissues of its head to generate traction loads on the surface of the TPC. These loadings on the TPC can be calculated from the incident sound pressure because they are, to a good approximation, driven by the amplitudes of acoustic pressure. The TPC vibrates under the action of the loads, resulting in motion of the stapes within the oval window, which produces a velocity at the center of the stapes footplate. The resulting transfer function, the Stapes Velocity Transfer Function (SVTF), is the composite of *two* transfer functions: the first transfer function calculates the pressure on the surface of TPC given the amplitude of the incident sound pressure; the second transfer function calculates the velocity at the center of the stapes footplate given the pressure on the surface of the TPC. Correspondingly, we use these two models in series to calculate the two transfer functions.

We also consider the possibility that the ossicular chain may be set into motion by loading on the TPC that is analogous to bone conduction in humans [40]. In this case, we consider that loading of each TPC can be described by the motions of the periotic bones, which are firmly embedded in the skull. Each tympanic bone is forced to follow the vibration of the periotic bone, which is set into motion by the vibration of the skull, thereby exposing the ossicles to differential displacements.

We have quantified both means of loading the TPC, by pressure delivered through soft tissues and by “skull-bone conduction”, using our two-component series of finite element models specialized for propagating elastic waves through arbitrary geometries of combined fluids and solids in an acoustic medium. The CT scans were converted to a mesh of finite elements by mapping the voxel values to the material types (see [S2 Table](#)). For the simulations reported here, incident sound waves were directed toward the head, along a single axis from directly in front of the animal at selected frequencies. At each of the excitation frequencies, after the steady-state vibration was reached, the amplitude of the total pressure in the soft tissues and

the amplitudes and phase shifts of the displacement components of all tissues were extracted. These quantities were then used to define loads on the TPC as transfer functions from the sound pressure wave incident upon the animal and either the pressures acting on the TPC or the amplitudes and phase shifts of the displacements of the periotic bone.

The forced harmonic vibration analysis of the TPC then resulted in the combined transfer function between the incident acoustic pressure and the stapes footplate velocity. The stapes velocity transfer function (SVTF) was then used to estimate an audiogram, for each of the loading modalities separately and also for their combination. The audiogram curve was calibrated with respect to the minimum audible pressure using measurements and estimates from two previous studies of odontocetes [41, 42].

The sensitivity of the computed transfer functions to the input parameters was assessed by performing a series of forward/backward sensitivity analyses. The full details are provided in the [S1 File](#).

The mechanical response of the TPC and the vibrations of the tissues of the head, especially the skull, can be visualized with animations (as shown in the [S1 File](#)).

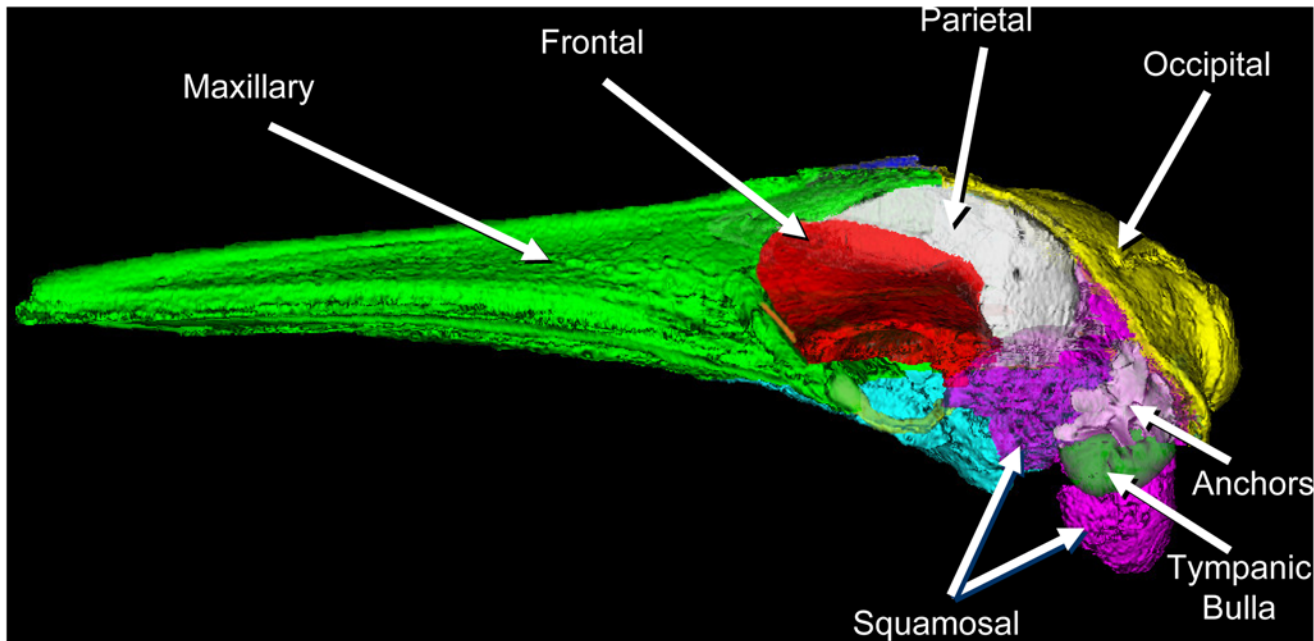
## Results

Synthetic audiograms were generated for a fin whale head using finite element modeling simulations derived from CT scans of a small *Balaenoptera physalus*. The simulations reveal two mechanisms that excite each bony tympanoperiotic complex (TPC), the **pressure mechanism** and the **bone conduction mechanism**. The **bone conduction mechanism** is the dominant of the two (this assertion will become clear with the figure at the end of this Results section).

The primary, or dominant, **bone conduction mechanism** is characterized by deformation of the whale's skull, as the acoustic pressure waves interact with it. During **bone conduction**, excitation of the hearing apparatus results from vibrations of the TPC induced by the motion of the skull. Secondarily, the **pressure mechanism** is the result of the acoustic pressure waves that reach the TPC through the seawater and various soft tissue pathways, resulting in direct pressure loading on the tympanic bulla.

Our assertion that mysticetes receive sound by a **bone conduction** mechanism is buttressed somewhat by the morphology of the skull and TPC, as noted by previous authors [43, 44]. In baleen whales the posterior process of the TPC is wedged between the squamosal and the exoccipital bones, while the anterior process is sandwiched between the squamosal and the pterygoid bones of the skull [45, 46, 47, 48]. In this fin whale, the CT scans reveal that there are also a series of dense bony ossifications within the squamosal bones of the cranium that appear to fan out from the junction with the adjacent periotic portion of each TPC (Figs. 1 and 2). Upon closer inspection these dense ossification components of the squamosal bones suggest that they may function to "anchor" or extend and reinforce the connection between the TPC and the cranium (Figs. 1 and 2).

By contrast, the TPCs of most odontocetes tend to be separated from the skull. Odontocete TPCs are suspended from the skull by numerous ligamentous fibers that originate from an approximately hemispherical distribution on the periotic fossa and peribullary fossa, sometimes crisscrossing, to insert upon the periotic bone of each TPC. It is generally considered that this suspension system functions to acoustically isolate the TPCs from skull vibrations in odontocetes. Instead, sounds apparently reach odontocete TPCs primarily through the mandibular fat bodies [22, 33, 34, 49, 50, 51, 52], probably by way of the gular pathway [53]. The Physeteridae and the Ziphiidae are exceptions to this exclusively ligamentous suspension system for odontocete TPCs. The sperm whales and beaked whales retain a bony connection to the skull through the pneumatized posterior process, where the vacuities in the posterior process may be filled



**Fig 1. Left lateral view of the skull bones in a fin whale (*Balaenoptera physalus*).** Some display transparency has been applied to the squamosal bone so that the tympanic bulla and the dense bony ossifications or “anchors” become visible. Bony skull components that are visible in this orientation are the: occipital (yellow), parietal (white), frontal (red), maxillary (green), squamosal (magenta), tympanic bullae (green), and the “anchors” (white). The dense bony anchors fan out dorsolaterally within the squamosal bones of the skull (see also Fig. 2). In this lateral view, the adjacent petriotic bones are not visible because they are obscured by the anchors and tympanic bulla.

doi:10.1371/journal.pone.0116222.g001

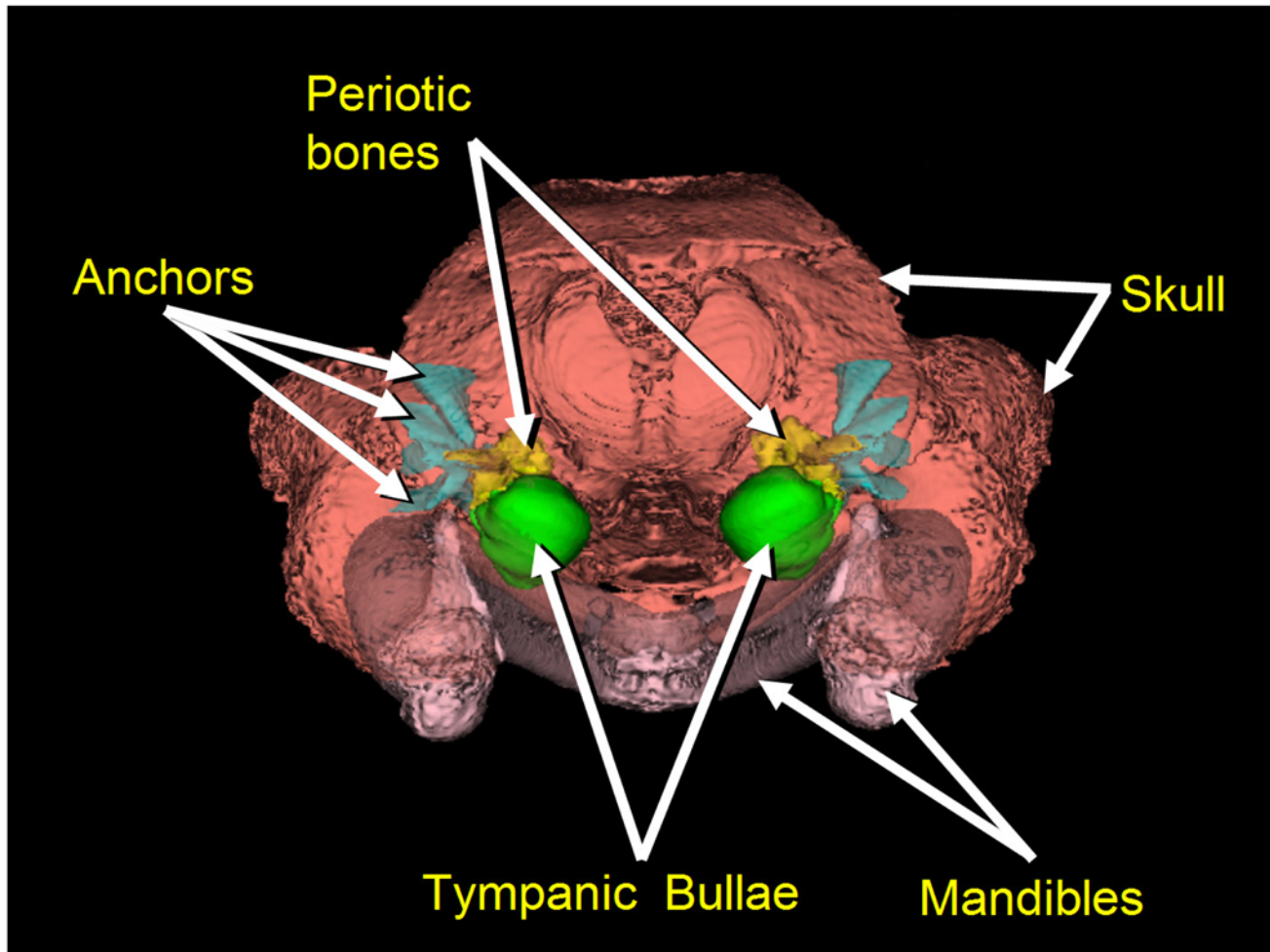
with lipids in life. This raises the possibility that a bone conduction mechanism may also exist in these two odontocete groups.

The results of our model have been applied to a fin whale, but the same firm connection between the TPC and the skull is common to all mysticetes [48]. This lends credence to the hypothesis that the same two sound reception mechanisms may be common to all baleen whales. However, vast differences in skull geometry between different Families of mysticetes (Balaenidae, Neobalaenidae, Eschrichtiidae, Balaenopteridae) suggest differences in the patterns of skull deformation and the resulting audiograms across these Families.

Two finite element models were required to cover the range of geometric resolution needed to accurately represent the relevant mechanisms. The first model (WP = Wave Propagation) simulated the traveling acoustic pressure waves through the water, from in front of the animal toward the head. The sound waves propagate through seawater, reach the head, continue along/within various soft tissue pathways (which have acoustic impedance values similar to water), and impinge upon the skull and the tympanic bone, the tympanic “bulla” of the TPC. The WP model could reasonably resolve the bone thicknesses of the TPC by employing cubic finite elements with dimensions of 2.7 mm on each side. This resolution was not sufficient to accurately represent the fine features of the middle ear ossicles. Therefore, the WP model was used to estimate the loading mechanisms acting on the TPC, and a second model with much higher resolution (0.684 mm) was used to compute the Forced Harmonic Vibration response of the TPC to these loads (hence the FHV model).

For the *pressure mechanism*, forces are exerted upon the tympanic bulla by the sound pressure waves that travel through seawater and various soft tissues. The extreme impedance mismatch between soft tissue and the dense tympanic bone causes significant force from the acoustic pressure waves to be exerted upon the tympanic bulla at the interface with soft tissue





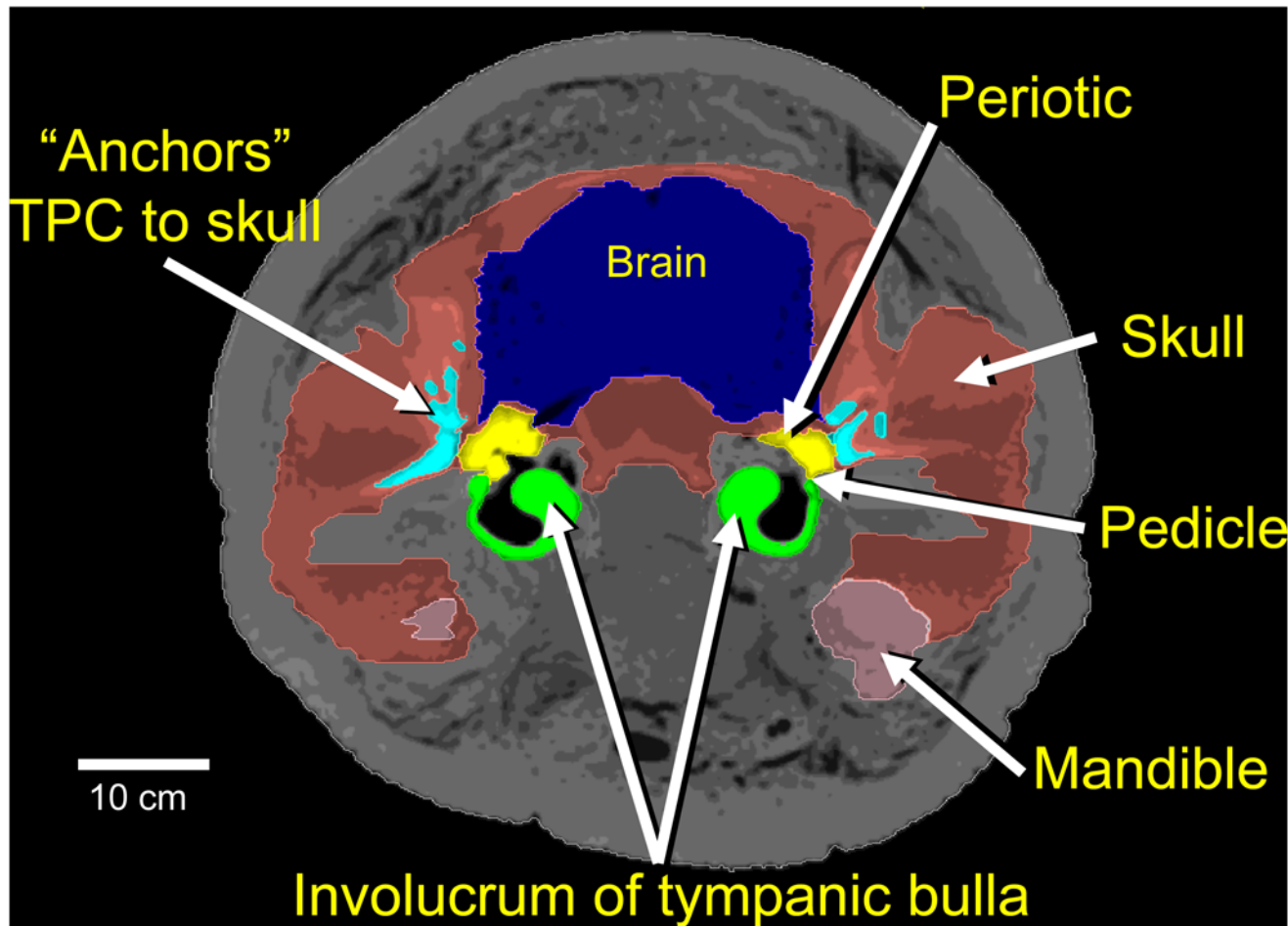
**Fig 2. Posterior view of both tympanoperiotic complexes in a fin whale (*Balaenoptera physalus*), with some display transparency applied.** The periotic bones (yellow) and tympanic bullae (green) are components of each TPC. The dense bony fan-like projections (cyan) are contained within the bones of the skull (salmon). Specifically, the anchors fan out as dense ossifications within the squamosal bone, from a locus at the junction with the juxtaposed periotic bones, and may function to stiffen the connection between the periotic and the skull. The mandibles (pink) are shown for context.

doi:10.1371/journal.pone.0116222.g002

[22]. Since the malleus is fused to the bulla, the force applied to the tympanic bulla will cause some motion in the ossicular chain, resulting in motion at the stapes footplate, which sits in the oval window of the cochlea. The pressure delivered to the surface of the tympanic bulla is the source of forcing for the *pressure mechanism* of sound reception.

The models that incorporate the *pressure mechanism* are essentially identical to those that we used to investigate sound reception in toothed whales [22, 33, 34]. That work led us to understand that the odontocete head works like an acoustic antenna; the entire surface of the animal's head receives sound, and the anatomy channels the sound toward the ears. This head-as-an-acoustic-antenna hypothesis probably applies to all mysticetes too.

The *bone conduction mechanism* was discovered by observing skull deformations that are associated with the elastic waves propagating through the head. Skull vibrations are apparently transmitted through the bony anchors to the periotic portion of the TPC (Figs. 1 and 2). Each tympanic bulla forms a lever arm that hangs from two thin bony struts (pedicles) (Fig. 3), and ends in the massive thickened rim at the distal tympanic bone, known as the involucrum [54]. The tympanic bone essentially “swings” on the pedicles [23], which function as the fulcrum of



**Fig 3. Transverse section through the otic region in the head of a fin whale calf.** The bony projections that “anchor” the tympanoperiotic complexes to the skull are cyan. The brain is blue, the skull is salmon colored, and the mandible is pink. The periotic portions of the TPC are yellow, and each tympanic bulla is green. Note that thin bony pedicles form a fulcrum for differential vibration between the periotic bones and the large hypermineralized masses of the tympanic bulla at the distal end of each involucrum.

doi:10.1371/journal.pone.0116222.g003

the lever arm. The flexing occurs in response to the differential motion between the periotic bones and the tympanic bulla, enhanced by the inertial properties of the hypermineralized [55] involucrum, causing it to lag behind the motions of the skull and periotic. The malleus is fused to the tympanic bone in all extant cetaceans, so any motion of the tympanic bone is transmitted through the middle ear ossicles that push on the oval window of the inner ear.

This lever arm construction is common to all cetacean TPCs (Archaeoceti, Odontoceti, and Mysticeti) [17, 23, 56], and is perhaps the single most innovative adaptation that allowed underwater hearing to evolve. The tympanic bullae in cetaceans develops precociously, such that it reaches adult size and shape very early in life [57, 58], attesting to its essential incipient functional prominence. The primary difference across the cetaceans is the degree to which the periotic is attached to the rest of the skull, and may be an indication of the relative importance of *bone-conduction* versus *pressure* mechanisms in sound reception and transduction across all cetacean groups [23, 59, 60, 61].

For the skull-vibration induced bone conduction, the WP model yielded the amplitude of the displacements of the periotic bone and relative phase shifts between the components of

displacement, while the FHV model simulated the response of the TPC to the forcing by prescribed harmonic-motion of the periotic bones.

For both the pressure and the bone conduction mechanisms, the result of the simulation was a transfer function (TF) between the amplitude of the incident sound pressure wave in the environment around the head and the magnitude of the velocity of the stapes footplate, the stapes-velocity transfer function (SVTF). Since two models were used to construct the SVTF for both loading mechanisms, the result is a composition of two TFs, WP-TF for the wave propagation model and FHV-TF for the forced vibration model.

**For the pressure mechanism**, the WP-TF describes the pressure acting on the tympanic bone as a function of the amplitude of the incident pressure wave, and the FHV-TF describes the velocity of the stapes footplate as a function of the pressure on the surface of the tympanic bone.

**For the bone conduction mechanism**, the WP-TF describes the motion of the periotic bone due to the vibration of the skull caused by a given amplitude of the incident pressure wave, and the FHV-TF describes the velocity of the stapes footplate as a function of the differential motions between the periotic bone and the bulla.

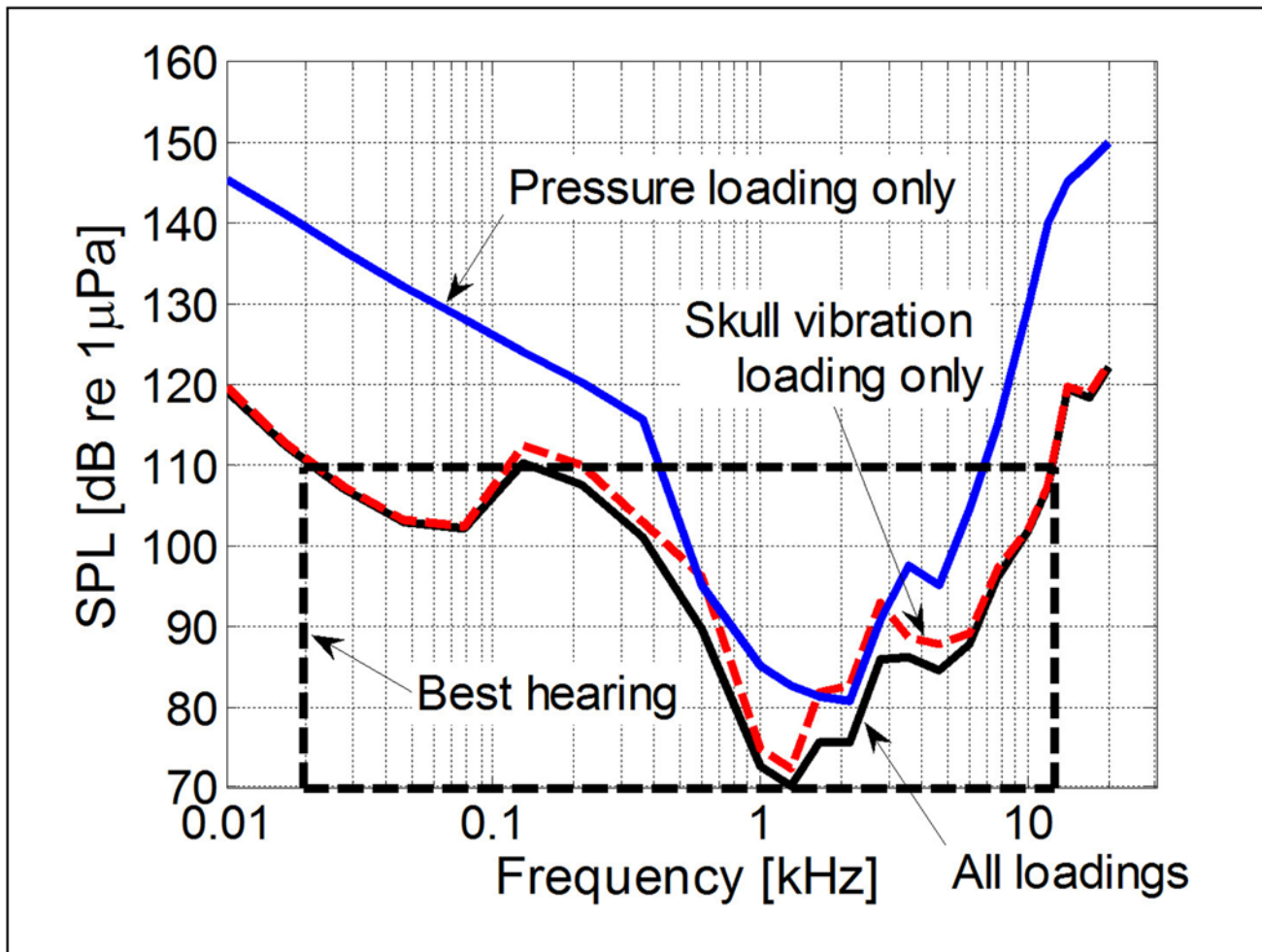
We note that Tubelli and colleagues [62] computed transfer functions for the minke whale middle ear that are analogous to the FHV-TF (for the pressure loading mechanism) in our two model series. Consequently, their results are only partial, as the wave propagation transfer function from the environment was not calculated. They considered two conjectural locations for application of loading by pressure, the tympanic bone and the tip of the glove finger. They did not consider the possibility of skull bone conduction.

With the SVTF at hand, we can attempt to predict the audiogram. The audiogram curve needs to be calibrated with the respect to the minimum audible pressure. Since this value has never been measured for a baleen whale, our approach was to set the hearing threshold to be similar to that measured for toothed whales, the bottlenose dolphin [41], or the killer whale [42], i.e. around 70 dB re 1  $\mu$ Pa at one meter. Then, the minimum threshold pressure across all frequencies can be estimated and the stapes velocity at the threshold can be consequently expressed through the maximum of the SVTF (see [S1 File](#) for a detailed explanation). Finally, the threshold pressure amplitude curve can be predicted from the SVTF as a function of frequency as shown in [Fig. 4](#). The three curves correspond to the audiograms predicted from, (1) the pressure mechanism alone, (2) the bone conduction mechanism alone, and (3) from the sum of the effects of these two mechanisms.

Mysticete sound reception by the **bone conduction mechanism** is, according to [Fig. 4](#), considerably more sensitive, particularly at low frequencies, than by the **pressure mechanism**, indicating that the **bone conduction** mechanism is largely responsible for the mysticete whale's sensitivity to low-frequency sound. Note that within the box (dashed lines) around the region of best hearing in [Fig. 4](#), the curve drops by as much as 40 decibels, indicating better sensitivity in that range. Therefore, according to the synthetic audiograms generated by our finite element models ([Fig. 4](#)), the **bone conduction** audiogram is approximately four times more sensitive (lower threshold) between 1–2 kHz than the **pressure** audiogram. More significantly, [Fig. 4](#) predicts that the difference in auditory sensitivity over the range of the lowest frequencies used by fin whales (10 Hz to 130 Hz), is between 10 to 30 dB (i.e. up to 10 times) more sensitive for the **bone conduction** mechanism than for the **pressure** mechanism.

This study uses the only currently available method capable of predicting relative sensitivities for sound reception in a mysticete over a broad range of frequencies, between 10 Hz and 12 kHz. Note that the lower frequencies (~20 Hz) propagate well in the ocean and are relatively less attenuated by the environment, so there may be no need for the best sensitivity to be located at those frequencies. The **bone conduction mechanism** produces the lowest thresholds (red





**Fig 4. Predicted audiograms for the fin whale calf.** The solid blue line represents the audiogram for the *pressure mechanism*. The red dashed line represents the audiogram for the *bone conduction mechanism*. The solid black line shows the combined audiograms for the *pressure* and *bone conduction* mechanisms.

doi:10.1371/journal.pone.0116222.g004

dashed line in Fig. 4), when both mechanisms are considered in isolation. Therefore, the *bone conduction mechanism* is likely the dominant component in mysticete hearing.

### Discussion

Mysticete sound reception is enabled by the vibration of the relatively stiff and dense skull in response to the sound waves passing through the body of the whale. The advantage to mysticetes of using low-frequency (long-wavelength) sounds becomes evident when considering the motion or displacement of the scatterer (i.e. the skull), instead of the scattered pressure, as described by Rayleigh [63]. The scattered pressure from low-frequency acoustic waves becomes ineffective as an excitation mechanism, because the amplification of the scattered pressure on the surface of the TPC is negligible for waves longer than the body of the animal. Consider, for example, that the wave length for a 20 Hz sound in water is 75 m, which is at least three times longer than the bodies of largest fin whales [64]. At the same time, the amplitude of the oscillations (displacement) of the scatterer (skull) grows with the wavelength of the incident sound [65]. It is of interest to note that a similar vibration mechanism has been studied in fish, where

the otoliths respond to long-wavelength sound by moving relative to the soft tissues attached to them [66].

The air spaces associated with the TPCs play a minor role for the pressure forcing mechanism, but only for high frequencies (above 5 kHz). At those frequencies, the air spaces helped to establish a “resonant cavity” for the sound waves propagating through the soft tissues towards the ears. The waves in the soft tissues are much too long below 5 kHz for the air spaces to be significant contributors to the pressure-distribution calculation. The most important function for these interconnected air spaces may be to maintain sufficient air volume in the tympanic cavity around the ossicular chain to allow the ossicles to vibrate free of damping or interference by nearby soft tissues. A similar mechanism has also been proposed for the enlarged pterygoid sinuses in *Ziphius cavirostris* [38].

Although these simulations were conducted with the skull geometry of a fin whale calf, the two basic mechanisms will not change significantly for the adult skull. The reasoning here is twofold. First, the tympanic bullae develop precociously [58]. Second, the firm connection between the TPC and the cranium is common to all mysticetes.

Adult fin whale skulls are approximately twice as long as they are wide [64], nearly the same length/width proportions as in our fin whale calf. According to True [64] the absolute dimensions of an adult fin whale skull are approximately four times longer and wider than our neonate skull. In order to understand the potential implication of adult skull size, we generated an artificial geometry by uniformly scaling the voxel dimensions by a factor of 4.0. This resulted in a skull of ~5 m in length, which we modeled with the WP model as for the neonate, but currently only for a 200 Hz incident sound. The displacement amplitudes of the periotic bone were slightly larger (1.1 to 2.0 times greater) than those calculated for the neonate at a similar frequency. Therefore, the WP+FHV model prediction for an adult is likely to result in an audiogram similar to those reported here for the neonate, and our preliminary result suggests that with an increase in skull size the frequency of best sensitivity may be shifted towards lower frequencies.

The audiogram is understood to be shaped by the external, middle, and inner ear connected in series [67]. Experimental data and models discussed therein point to the external and middle ear as the main contributors to low and mid frequency regions of the audiogram, and the cochlea is believed to contribute to the shape of the audiogram around the limit of high-frequency hearing. The graphs in Fig. 4 probably rise less sharply for the very high frequencies than would be observed experimentally, because in our transfer function we consider the effect of the cochlea only through a fluid load. Our predicted audiogram curves are certainly only approximations, but these approximations should be rather good for low and mid frequencies, until we begin to predict what happens at the high-frequency limit. For the fin whale, that high-frequency limit would probably begin around 10 kHz. We contend that our predictions are likely quite robust below 10 kHz, for the low and mid frequencies of concern with anthropogenic sound exposure.

Understanding the potential effects of anthropogenic noise on mysticetes is a subject that has long plagued U.S. regulatory agencies and concerned large-scale industrial users of the ocean environment. The results reported here provide a new tool for assessing these acoustic interactions.

## Supporting Information

**S1 File. This supporting information file contains a description of the modeling process and additional visualizations of the results, including animations, figures, and tables.**  
(DOC)

**S1 Fig. Schematic of the two models that extract the cochlear input from the incident wave.** (PNG)

**S2 Fig. (A) Finite element mesh 4, and (B) Close-up of the ossicular chain.** (A) Finite element mesh 4 (approximately 41,000 nodes, 230,000 elements). The periotic bone is trimmed off, and the red markers at the top-right of the mesh indicate nodes with prescribed displacements (as dictated by the motion or the lack of the motion of the squamosal bone of the skull). (B) Close-up of the ossicular chain and the sigmoidal process in the foreground. The joints between the ossicles are shown in color: the annular ligament between the stapes and the oval window is yellow; the incudostapedial ligament is green, and a small portion of the malleoincudal ligament is blue (most of this ligament and the malleus are obscured by the sigmoidal process).

(TIF)

**S3 Fig. The damping ratio for the Rayleigh proportional damping model as a function of the frequency for the parameters shown in the text.**

(PNG)

**S4 Fig. Surface of the tympanic bone with applied damping condition to account for the interaction with the soft tissues during skull bone-conduction loading is indicated by dark red color.** Mesh 4 as in [S2 Fig.](#)

(PNG)

**S5 Fig. Distribution of the total sound pressure in the head of the fin whale for a 4 kHz incident signal.** Sound Pressure Levels (SPL) between -3 dB (pressure diminished with the respect to incident) and +6 dB (pressure amplified with respect to incident) are shown. The pressure is not displayed in the volume of the bones (gray regions) or in the volume of the air spaces or sinuses (black regions). (A) is a transverse section through the TPC with labels indicating the involucra (i) of the tympanic bulla and the expanded portion of the squamosal (sq); (B) is a coronal (horizontal) section through the TPC, at the level of the tympanic bullae (tb). Note the amplified pressure amplitude near the dorsal surface of the tympanic bullae (tb) from a reflection off of the squamosal bones (sq).

(PNG)

**S6 Fig. Transformation of the incident pressure to pressure at the TPC near the sigmoidal process (TPTF).** Note that close to 1–2 kHz the incident pressure is magnified to arrive at the surface of the TPC almost doubled in amplitude.

(PNG)

**S7 Fig. Periotic-bone displacement transfer function (PDTF).** (A) Amplitudes of the displacements, and (B) phase shift with respect to the dorsal-ventral displacement.

(TIF)

**S8 Fig. Stapes Velocity Transfer Function (SVTF) and approximate error.** (A) SVTF(P) for two meshes: mesh 3, with 62,000 nodes, in solid line, and mesh 6, with 20,600 nodes, in dashed line. (B) Approximate error vs. the number of nodes in the model, where the smallest error is  $E_{a,4} = 0.061$ . The errors are for meshes 4, . . . ,9 (right to left).

(TIF)

**S9 Fig. Deformations and motion of the skull for 100 Hz incident wave.** Amplitude magnified 20,000 times. (Animated visualization link with displacements magnified by 20,000 times).

(GIF)

**S10 Fig. Deformations and motion of the skull for 250 Hz incident wave.** Amplitude magnified 20,000 times. (Animated visualization link with displacements magnified by 20,000 times). (GIF)

**S11 Fig. Deformations and motion of the skull for 1.0 kHz incident wave.** Amplitude magnified 20,000 times. (Animated visualization link with displacements magnified by 20,000 times). (GIF)

**S12 Fig. Deformations and motion of the skull for 2.0 kHz incident wave.** Amplitude magnified 20,000 times. (Animated visualization link with displacements magnified by 20,000 times). (GIF)

**S13 Fig. Motion of the TPC for pressure loading at 10 Hz.** (Animated visualization link with displacements magnified by 5,000 times). (GIF)

**S14 Fig. Motion of the TPC for pressure loading at 599 Hz.** (Animated visualization link with displacements magnified by 5,000 times). (GIF)

**S15 Fig. Motion of the TPC for pressure loading at 1 kHz.** (Animated visualization link with displacements magnified by 5,000 times). (GIF)

**S16 Fig. Motion of the TPC for pressure loading at 2.7 kHz.** (Animated visualization link with displacements magnified by 5,000 times). (GIF)

**S17 Fig. Motion of the TPC for pressure loading at 14.1 kHz.** (Animated visualization link with displacements magnified by 5,000 times). (GIF)

**S18 Fig. Motion of the TPC for skull-vibration loading at 129 Hz.** (Animated visualization link with displacements magnified by 5,000 times). (GIF)

**S19 Fig. Motion of the TPC for skull-vibration loading at 359 Hz.** (Animated visualization link with displacements magnified by 5,000 times). (GIF)

**S20 Fig. Motion of the TPC for skull-vibration loading at 1 kHz (Animated visualization link with displacements magnified by 5,000 times).** (GIF)

**S21 Fig. Motion of the TPC for skull-vibration loading at 5.99 kHz (Animated visualization link with displacements magnified by 5,000 times).** (GIF)

**S22 Fig. Motion of the TPC for skull-vibration loading at 20 kHz (Animated visualization link with displacements magnified by 5,000 times).** (GIF)

**S23 Fig. Change of the SVTF(P) due to a change in the cochlear impedance.** Dotted line: decrease by a factor of  $\frac{1}{2}$ ,  $\Delta = 0.159$ ; dashed line: increase by a factor of 2,  $\Delta = 0.084$ .  
(PNG)

**S24 Fig. Change of the SVTF(P) due to a change in the elastic modulus of the joints in the ossicular chain.** Dotted line: decrease by a factor of  $\frac{1}{2}$ ,  $\Delta = 0.65$ ; dashed line: increase by a factor of 2,  $\Delta = 0.85$ .  
(PNG)

**S25 Fig. Change of the SVTF(P) due to a change in the Rayleigh system damping.** Dotted line: decrease of  $\zeta_{\min}$  by a factor of  $\frac{1}{2}$ ,  $\Delta = 0.25$ ; dashed line: increase of  $\zeta_{\min}$  by a factor of 2,  $\Delta = 0.24$ .  
(PNG)

**S26 Fig. Change of the SVTF(P) due to a change in the Rayleigh system damping.** Dotted line: decrease of  $\omega_{\min}$  by a factor of  $\frac{1}{2}$ ,  $\Delta = 0.21$ ; dashed line: increase of  $\omega_{\min}$  by a factor of 2,  $\Delta = 0.22$ .  
(PNG)

**S27 Fig. Change of the SVTF(U) due to a change in the surface impedance on the tympanic bone.** Dotted line: decrease by a factor of  $\frac{1}{2}$ ,  $\Delta = 0.139$ ; dashed line: increase by a factor of 2,  $\Delta = 0.144$ .  
(PNG)

**S28 Fig. (A) The SVTF(P). (B) The audiogram predicted from the SVTF(P).**  
(TIF)

**S29 Fig. (A) The SVTF(U). (B) The audiogram predicted from the SVTF(U).**  
(TIF)

**S1 Table. Properties of materials used in the TPC simulations.**  
(DOCX)

**S2 Table. Properties of materials used in the VATk simulations.**  
(DOCX)

## Acknowledgments

This project included multiple daunting logistical challenges that were eventually solved by an array of individuals with diverse skill sets. We thank the following people for their support on various aspects of this project. Michael Wiese, James Eckman, and Dana Belden at the Office of Naval Research (N00014-12-1-0516); Frank Stone, Ernie Young, and Robert Gisiner at the Chief of Naval Operations (CNO45) along with Curtis Collins and John Joseph at the Naval Postgraduate School (N00244-08-1-0025). We appreciate assistance with specimen acquisition from: Judy St. Leger and Erika Nilson (Sea World, San Diego), John Heyning, David Janiger, and Jim Dines (Los Angeles County Museum of Natural History); James Mead, and Charles Potter (National Museum of Natural History, Smithsonian Institution); David Casper and Robin Dunkin (UC Santa Cruz); Joseph G. Cordaro and Sarah Wilkin, Jennifer L. Skidmore, Blair Maise, Susan Chivers, Kerri Danil, Wayne Perryman, and Debra Losey (NOAA); Eric Ekdale, Tom Deméré, and Philip Unitt (San Diego Natural History Museum). We also thank several other individuals, Jim Christmann and Dave Jablonski, Winston C. Lancaster, Jennifer Jeffress, Maureen Flannery, Kristi West, Michele Berman, Carl Schilt, William Ary, and A. Todd Newberry. Staff at the San Diego State University Research Foundation and



Department of Biology provided essential logistical assistance: Frank Sweeney, Thomas Scott, Michele Goetz, Maria Ortega, Eugene Stein, Jennie Amison, Danielle Arellano-Rieger, Mary Perl, (SDSURF) Terry Frey, Medora Bratlien, Christopher Glembotski, Annalisa Berta, Bob Mangen, and Mike Van Patten (Biology). Individuals from the Scripps Institution of Oceanography were also instrumental by helping encase the specimen in a specialized container for scanning at Hill AFB: John Hildebrand, Sean Wiggins, Megan McKenna, and Jeremy Goldbogen. Michael Philcock at Analyze Direct also made valuable contributions. The staff at Hill Air Force Base provided expertise with specimen CT scanning using their industrial scanner: Sal Juarez, Barry Gould, Randy Huber, Sam Samuelson, and Art McCarty. This manuscript was improved considerably from reviews by Mats Amundin, Olav Sand, Wim Verboom, James Mead, and one anonymous reviewer.

## Author Contributions

Conceived and designed the experiments: TWC PK. Performed the experiments: TWC PK. Analyzed the data: TWC PK. Contributed reagents/materials/analysis tools: TWC PK. Wrote the paper: TWC PK.

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