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# Polaron Formation in Conducting Polymers: A Novel Approach to Designing Materials with a Larger NLO Response

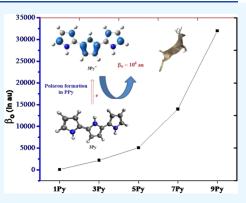
Atazaz Ahsin,<sup>#</sup> Iqra Ejaz,<sup>#</sup> Sehrish Sarfaraz, Khurshid Ayub,\* and Haitao Ma\*



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**ABSTRACT:** Substantial efforts have been made to design and investigate new approaches for high-performance nonlinear optical (NLO) materials. Herein, we report polaron formation in conducting polymers as a new approach to designing materials with a large NLO response. A comparative study of polypyrrole and polypyrrole-based polaron (nPy<sup>+</sup> where n = 1, 3, 5, 7, and 9) is carried out for optoelectronic and NLO properties. The studied polarons (PPy<sup>+</sup>) show excellent electronic properties and have reduced ionization potential (IP) as compared to neutral PPy, and a monotonic decrease is observed with increased chain lengths (**1Py** to **9Py**). Interesting trends of global reactivity descriptors can be seen; the softness (S) increases with an increase in the chain length of PPy, while the hardness ( $\eta$ ) decreases in the same fashion. The E<sub>H-L</sub> gaps for the PPy<sup>+</sup> polaronic state are significantly lower than their corresponding neutral PPy. In the polaronic model (PPy<sup>+</sup>), radicals decisively reduce the crucial excitation energy, reminiscent



of excess electrons (alkali metals). The performed TDOS spectral analysis further justifies the better conductive and electronic properties of polarons (PPy<sup>+</sup>) with increased chain lengths (conjugation). The static hyperpolarizability response ( $\beta_o$ ) is recorded up to  $1.3 \times 10^2$  au for **9Py**, while for polaron 9Py<sup>+</sup>, it has increased up to  $3.2 \times 10^4$  au. The static hyperpolarizability of the 9Py<sup>+</sup> polaronic state is 246 times higher than that of the corresponding neutral analogue, **9Py**. It is observed that the values of  $\beta_o$  obtained at the CAM-B3LYP/6-311+G(d,p) level of theory are comparable to those obtained at the LC-BLYP and  $\omega$ B97XD functionals. The  $\beta_{vec}$  values show a strong correlation with the total hyperpolarizability ( $\beta_o$ ). Furthermore, the calculated second harmonic generation (SHG) values are up to  $4.0 \times 10^6$  au at 532 nm, whereas electro-optic Pockel's effect (EOPE) is much more pronounced at the smaller dispersion frequency (1064 nm). The TD-DFT study reveal the red-shifted absorption maxima ( $\lambda_{max}$ ) with an increased length of PPy<sup>+</sup>. A significant reduction in excitation energy ( $\Delta E$ ) is observed with increased length of PPy and PPy<sup>+</sup>, which also favors the improved NLO response. Hence, the studied thermally conducting polypyrrole-based polarons (PPy<sup>+</sup>) are new entries into NLO materials with better electrical and optical features.

# INTRODUCTION

Materials possessing nonlinear optical (NLO) properties change the propagation characteristics (polarization, phase, frequency, amplitude, etc.) of light.<sup>1</sup> Nonlinear optics has found many applications in the communications, photonics industries, data storage, and computer display technology.<sup>2–6</sup> The early examples of NLO materials were based on inorganic materials; however, organic NLO materials have gained much interest recently due to their chemical flexibility and variety of synthetic strategies.<sup>7,8</sup> Several strategies have been proposed to enhance the nonlinear optical (NLO) response, which include the electron push–pull mechanism,<sup>9</sup> donor–acceptor- $\pi$ conjugation (D- $\pi$ –A) strategy,<sup>10</sup> bond length alternation (BLA),<sup>11</sup> multidecker sandwich complexes,<sup>12</sup> diradical character,<sup>13</sup> octupolar molecules,<sup>14</sup> and the excess electron system via doping.<sup>15,16</sup>

The doping of metals (1st and second groups) to inject excess electrons into materials is a quick approach to enhance NLO response in both (inorganic and organic) systems.<sup>17,18</sup> A

metal atom is doped on the substrate (doped material), where its excess electrons are diffused into the system and reduce the excitation energy of the system, which ultimately increases the first hyperpolarizability ( $\beta_{\rm o}$ ).<sup>19</sup> Several systems containing electropositive metals as external dopants on the homo and heteroatomic inorganic nanocages<sup>20</sup> and fullerenes have been reported.<sup>21</sup> Kosar et al. have investigated the effect of doping single and multialkali metal@C<sub>24</sub> complexes for NLO applications, where the Na<sub>3</sub>@C<sub>20</sub> complex has the highest  $\beta_{\rm o}$  value of 2.74 × 10<sup>5</sup> au.<sup>18</sup> Similarly, Maria et al. explored alkali metal-doped boron and aluminum phosphide nanocages for

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NLO properties, where hyperpolarizability shows dependence on the size of alkali metals.<sup>17</sup> Very recently, our group proposed single alkali metal-containing nonconventional alkalides based on M@[12-crown4] and M@[12-crown-5] for electronic and NLO properties.<sup>22</sup> In this study, a noticeable hyperpolarizability value ( $\beta_o = up$  to  $1.2 \times 10^7$  au) was reported for Li@[15-crown-5], which is attributed to the presence of loosely bound excess electrons.<sup>22</sup> A large number of studies were presented which demonstrate that excess electrons are crucial in promoting the static and dynamic NLO responses of clusters and molecules<sup>23,24</sup>.<sup>25</sup>

Excess electron compounds, or clusters, are those which contain extra transferable (excitable) electrons, which just look like Rydberg orbitals.<sup>26</sup> These excess electrons are the type of unique anions with dispersivity, loose binding, and other intriguing properties that play a critical role in decreasing the excitation energies (during crucial transition).<sup>27</sup> The reduction in HOMO–LUMO gaps is the driving force that makes excitation easier in the crucial transition.<sup>28</sup> In earlier research, Dye's group succeeded in providing the first experimental evidence of excess electron compounds in 1983 for the synthesized Cs<sup>+</sup>(18-crown-6)2e compound, which has characteristics of electride (alkali metal bearing a negative charge).<sup>29</sup>

Unpaired electrons (single radicals) behave in a similar way to alkali metals, and one expects an enhancement in the NLO properties of such radical species. Recent studies have demonstrated that unpaired electrons in orbitals (lying in the plane) and their spin multiplicity might be responsible for electronic and NLO properties.<sup>30,31</sup> These unpaired electrons are known as radical systems, and they function similarly to excess electrons inside molecules. For a variety of organic radical systems, Nakano et al. investigated the impacts of spin multiplicity, basis set, and electron correlation, which affect the NLO coefficients.<sup>32</sup>

Theoretically, polarons carry a spin  $(\pm 1/2)$  and are radical cations that can be designed by removing an electron from the conducting polymers. Also, it was investigated that increasing the size of the polarons (chain length) would improve the electrical and conductive properties. The unpaired electrons (radicals) in conducting polymers are responsible for the tunable electronic and conducting properties. Introducing a single cation charge in conjugated polymers would form polarons, whereas the bicationic state is described as bipolarons. Polarons have a very low excitation energy, as evidenced by the reported UV-visible spectra. The low excitation energy can result in a remarkable NLO response due to a nonlinear electric field interaction. This prompted us to explore polarons for the NLO properties. We became interested in studying the polaronic state of polypyrrole for its hyperpolarizability response.

Polypyrroles (PPy) are one of the most intensively studied conducting polymers due to their simple and inexpensive preparation, along with their widely admitted character as good sensors, actuators, and solar cell materials.<sup>33,34</sup> Conducting polymers are characterized by alternate double and single bonds and have tremendous applications in interdisciplinary science.<sup>35</sup> Since neutral polypyrrole has a broadband gap and makes it difficult to move electrons from the valence band to the conduction band, it is considered to be an insulator. Due to their radical nature, PPy<sup>+</sup> carries an unpaired electron, which might play a crucial role in evaluating electronic, optical, and NLO properties. Therefore, theoretical modeling of polypyrrole-based polarons (PPy<sup>+</sup>) can be interesting for

investigating electronic and NLO properties. Using polaronbased PPy (which resembles excess electrons) compounds reduces the excitation energy significantly, enhancing electronic and NLO properties. We performed a comparative study to investigate the role of polarons in improving the intrinsic properties of polypyrrole (PPy). Using DFT, we considered nPy (n = 1, 3, 5, 7, and 9) in neutral and cation (polarons). We mainly focused on the role of polarons in the conjugated polymer (PPy) and the change in their properties from the intrinsic to the polaronic state. The NLO properties of PPy are evaluated through polarizabilities ( $\alpha$ ), hyperpolarizabilities ( $\beta_{\alpha}$ ), and dynamic hyperpolarizabilities  $\beta(\omega)$ .

Computational Details. All the quantum chemical calculations were performed using the CAM-B3LYP method with a 6-31+G (d,p) basis set using the g09 software.<sup>36</sup> First, we considered the 1 to 9 units of pyrrole rings, and optimization was performed at CAM-B3LYP without any symmetry constraints. CAM-B3LYP is a hybrid exchangecorrelation function that includes the hybrid properties of the B3LYP functional and the long-range corrected Coulomb attenuating method (CAM) parameter. B3LYP is a hybrid part of the above method that contains Beckes 3-parameters for the exchange functional and Lee- Yang-parr- correlation functional (LYP). The performance of CAM-B3LYP is reliable for atomization energies and charge transfer-excitation.<sup>37</sup> It is also demonstrated by Limacher et al.,<sup>38</sup> that CAM-B3LYP provides accurate results for molecular geometry, much closer to experimental results.

After optimization, frequency calculations are performed to confirm that these structures are true minima on the potential energy surface (PES). Dipole moment, FMO analysis, and HOMO–LUMO ( $E_{H-L}$ ) gaps are calculated at the same level of theory. Furthermore, we have calculated electronic properties and global reactivity of the studied nPy, which include the ionization potential (IP), electronic affinity (EA), chemical hardness ( $\eta$ ), chemical softness (S), and chemical potential ( $\chi$ ) given by the following relations.

ionization potential (IP) =  $-E_{\text{HOMO}}$  (1)

electron affinity (EA) = 
$$-E_{LUMO}$$
 (2)

chemical hardness 
$$(\eta) = \frac{1}{2}(IP - EA)$$
 (3)

chemical softness (S) = 
$$\frac{1}{2\eta}$$
 (4)

chemical potential 
$$(\chi) = -(IP + EA)/2$$
 (5)

Nonlinear optical properties are induced by asymmetric charge displacements that are generated under the influence of light. The energy of the perturbed system is described by the Taylor expansion

$$E = E^{O} - \mu_{I}F_{i} - \left[\frac{1}{2!}\right]\alpha_{ij}F_{i}F_{j} - \left[\frac{1}{3!}\right]\beta_{ijk}F_{i}F_{j}F_{k} - \left[\frac{1}{4!}\right]\gamma_{ijkl}F_{i}F_{j}F_{k}F_{l}$$

$$(6)$$

Polarizability ( $\alpha_o$ ) and first hyperpolarizability ( $\beta_o$ ) values of PPy and polaron (PPy<sup>+</sup>) are studied at the same level of theory with the 6-31+G(d,p) basis set. This level of theory is reliable for the estimation of polarizability ( $\alpha_o$ ), first hyperpolarizability ( $\beta_o$ ), and other electronic parameters.<sup>39,40</sup> In the previous

studies, several types of hyperpolarizability values, such as  $\beta_{vec}$ ,  $\beta_{o_i}$  and  $\beta_{HRS}$ , were computed through this approach. We adopted the coupled-perturbed Kohn–Sham (CPKS) method to calculate the hyperpolarizability.

$$\mu = \sqrt{\mu_X^2 + \mu_Y^2 + \mu_Z^2} \tag{7}$$

$$\alpha_{ij} = \left(\frac{\delta\mu_i}{\delta F_j}\right)_{E_{\rightarrow 0}} \tag{8}$$

$$\alpha_{tot} = \frac{1}{3}(\alpha_{xx} + \alpha_{yy} + \alpha_{zz}) \tag{9}$$

The magnitude of hyperpolarizability can be defined as

$$\beta_x = \beta_{xxx} + \beta_{xyy} + \beta_{xzz}$$

$$\beta_y = \beta_{yyy} + \beta_{yxx} + \beta_{yzz}$$

$$\beta_x = \beta_{zzz} + \beta_{zxx} + \beta_{zyy}$$

$$\beta_{tot} = \sqrt{\beta_x^2 + \beta_y^2 + \beta_z^2}$$
(10)

The frequency-dependent NLO response is also calculated by the same method at applied frequencies of 532 and 1064 nm. In this regard, we estimated electro-optical Pockel's effect (EOPE) and second harmonic generation (SHG) phenomena. Time-dependent density functional theory (TD-DFT) simulations were considered at TD-CAM-B3LYP for getting excited state parameters. We considered 40 excited states (singlet and triplet), and a crucial excited state (highest oscillator strength) was adopted to determine absorbance ( $\lambda_{max}$ ), excitation energies ( $\Delta E$ ), and oscillator strength), which is used to get the values of oscillator strength ( $f_o$ ) and excitation energies ( $\Delta E$ ). To get a clear picture of the electronic properties of the studied PPy, we performed a total density of state (TDOS) analysis by using GaussSum software.<sup>41</sup>

#### RESULTS AND DISCUSSION

**Optimized Geometries of (PPy and PPy<sup>+</sup>).** Initially, optimized geometries of polypyrrole (PPy) at the CAM-B3LYP/6-31+G (d,p) functional are shown in Figure 2. We

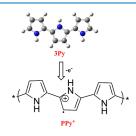
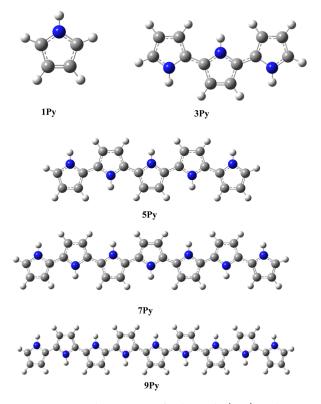


Figure 1. Representation of 3Py and 3Py<sup>+</sup>.

have considered the odd number of nPy (up to 9 units) for our investigation. The largest oligomers up to nine units (9Py) and their corresponding polarons (9Py<sup>+</sup>), which represent the structural properties of polypyrrole (PPy), are considered. The optimized geometries of neutral PPy are depicted in Figure 2. Figure 1 shows the neutral and radical generation of the **3Py** unit. All the neutral nPy have the  $C_1$  point group symmetry with planar structures. On the other hand, the optimized structures of polypyrrole-based polarons (PPy<sup>+</sup>) are almost



**Figure 2.** Optimized geometries of polypyrrole (PPy) at the CAM-B3LYP/6-31+G(d,p) level of theory; blue color indicates the N atom, while gray one for carbon atoms.

planar, and no distortions in the geometries were seen. The obtained point group symmetry for PPy<sup>+</sup> is  $C_{I_i}$  the same as that for their corresponding neutral PPy. Several important geometric parameters (bond angle, bond length, and dihedral angles) are computed for PPy<sup>+</sup>, and values are given in Table 1.

Table 1. Symmetries, Average Bond Lengths (in Å), and Bond Angles ( $\angle C-N-C/C-C-C/H-C-C/H-N-C$  in Degree) of Polypyrrole-Based Polarons (PPy<sup>+</sup>)

nPy	L <sub>C-C</sub>	L <sub>C-N</sub>	L <sub>C-H</sub>	$(\angle C-N-C)$	(∠C−C− C)	(∠H−C− C)
$1 Py^+$	1.43	1.36	1.08	109.07	107.15	128.06
$3Py^+$	1.42	1.38	1.08	109.07	107.15	128.06
$5Py^+$	1.43	1.38	1.08	109.07	107.15	128.06
$7Py^+$	1.44	1.38	1.08	109.07	107.15	128.06
9Py <sup>+</sup>	1.45	1.38	1.08	109.07	107.15	128.06

In the studied PPy<sup>+</sup>, 4-types of bond lengths are present, namely: C–C, C–H, N–C, and N–H. The C–C bond length lies in the range of 1.43 to 1.39 Å, while the computed C–N bond length ( $L_{C-N}$ ) ranges from 1.36 to 1.39 Å in these polarons. The measured carbon and hydrogen bond distances ( $L_{H-C}$ ) are identical to those for neutral PPy and range from 1.09 to 1.07 Å. The C–N bond lengths ( $L_{C-N}$ ) slightly increased with an increase in conjugation and chain lengths ( $1Py^+$  to  $9Py^+$ ). Vibrational frequency analysis of polarons and neutral PPy reveals that they are true minima on the potential energy surface, since no negative frequency is associated. For polarons, the measured average bond angles of C–N–C, C– C–C, and H–C–C are 109.07°, 107.15°, and 128.06°, respectively. On the other hand, the average bond angle of H–N–C is 125.47°. The computed average dihedral angles in

	1Py <sup>+</sup>	3	3Py <sup>+</sup>	5	SPy <sup>+</sup>	7	∕′Py⁺	ç	PPy <sup>+</sup>
C1	0.555	C2	0.14	C1	0.16	C1	0.13	C1	0.12
C2	0.555	C1	0.22	C2	0.12	C2	0.10	C2	0.08
Ν	-0.129	C3	0.21	C3	0.13	C3	0.11	C3	0.09
		C4	0.21	C4	0.13	C4	0.10	C4	0.05
		N5	-0.07	N5	-0.06	C5	0.10	C5	0.06
		C6	0.14	C6	0.12	C6	0.13	C6	0.09
		C7	0.22	C7	0.17	N1	-0.05	C7	0.08
						N2	-0.03	C8	0.12
								N1	-0.05
								N2	-0.03

Table 2. Spin Densities of the Studied Polypyrrole-Based Polarons (nPy<sup>+</sup>)

 $PPy^+$  for N-C-C-N and C-C-C-C are 177.92° and -168.87°, respectively (Table 1).

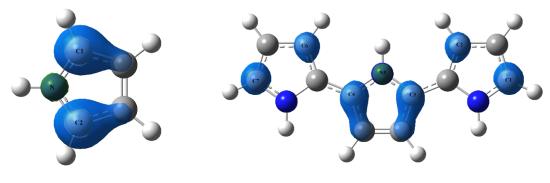
Spin Densities of Polypyrrole-Based Polarons (PPy<sup>+</sup>). The distribution of the unpaired spin density is crucial for determining the electronic properties of our studied PPy and PPy<sup>+</sup>. The calculated spin densities are listed in Table 2 and Figure 3. One can observe the reduction in spin densities with an increased chain length of PPy<sup>+</sup>. The obtained spin densities for 1Py<sup>+</sup> are higher and lie on the carbon atom of the PPy<sup>+</sup> ring. The higher value of spin density is obtained for 1Py<sup>+</sup>. It can be observed that the spin density decreases over the larger PPy<sup>+</sup> rings, and spin densities are dramatically reduced for corner rings. For 1Py<sup>+</sup>, the radical (unpaired) electrons are lying at C1 and C2, whereas for 3Py<sup>+</sup>, the spin densities are higher at the middle ring and are slightly reduced for terminal rings. Likewise, thesities for 5Py<sup>+</sup> are also higher in the case of the central Py-ring, and radicals (unpaired electrons) are associated with C3 and C4 for 5Py<sup>+</sup>. Likewise, the spin density on 7Py<sup>+</sup> was reduced to 0.10, and the maximum for the central ring was reduced to C3 and C4 (Figure 3). For 9Py<sup>+</sup>, the values of spin densities are further reduced to 0.05, and overall, density is higher at the middle ring and becomes negligible for the terminal Py<sup>+</sup>-rings. The performed spin density analysis concludes that the highest spin density is in the middle of these polypyrrole rings. Radical (unpaired electron) formation can be seen to be delocalized over the central PPy<sup>+</sup> rings, and its delocalization rises with greater conjugation (chain length), where values of spin densities also decrease.

Electronic Properties and Global Reactivity. The electronic stability of the studied PPy and polarons (PPy<sup>+</sup>) is verified by the calculated ionization potential (IP) and vertical electron affinity (EA). The ionization potential and electron affinity are calculated by using Koopman's theorem approximation.<sup>42</sup> The negative HOMO is taken as the ionization potential (IP), whereas the negative LUMO energy is considered the electron affinity (EA). The calculated values of IP and EA of neutral and polaronic PPy are given in Table 3. From the given values (Table 3), the IP values for neutral PPy are smaller than those of polaronic PPy<sup>+</sup> and lie in the range of 7.36 to 5.67 eV. The values decreased with an increased chain length of PPy. On the contrary, for polarons (PPy<sup>+</sup>), the values are significantly increased and lie in the range of 14.75 to 7.83 eV, where the lowest value was observed for 9PPy<sup>+</sup>. Similarly, the EAs values for neutral PPy range from -0.77 to -0.24 eV, whereas for polaronic PPy<sup>+</sup>, these values are quite higher and range from 4.98 to 2.98 eV. In the polaronic state, there is a significant reduction in EA values with the increased chain length and conjugation of polypyrrole. PPy<sup>+</sup> shows positive electron affinity and might be an electron acceptor undergoing charge transfer reactions, whereas negative electron affinity values are associated with neutral PPy.

The reactivity and stability of these structures were also evaluated through global reactivity descriptors. In this regard, we computed the chemical hardness  $(\eta)$ , chemical potential  $(\chi)$ , and softness (s). The computed results of the global reactivity descriptors are given in Table 3. The resistance of a molecule's electron distribution to change is assessed by its hardness ( $\eta$ ). For neutral PPy, the  $\eta$  values decreased with increasing chain length, where the lowest value (2.17 eV) accounts for 9Py. For the PPy<sup>+</sup>, a slightly increased chemical hardness ( $\eta$ ) can be seen, ranging from 4.89 to 2.43 eV. The chemical softness of neutral PPy ranges from 0.15 to 0.23 eV, and values slightly increased for 1P to 9Py. The softness of polaron (PPy<sup>+</sup>) is slightly smaller than that of neutral PPy, and there is a monotonic increase in softness with the increased chain length of polypyrrole. Moreover, we have calculated the chemical potential ( $\chi$ ) of PPy and PPy<sup>+</sup>, and the values are given in Table 3. The chemical potential  $(\mu)$  outlines the escaping tendency of electrons from an equilibrium system. The values of  $\chi$  are calculated by eq 5, which is given in the methodology section. The stability of polypyrrole (PPy) is shown by the negative chemical potential values; nPy are stable and do not spontaneously split. The values of  $\chi$  for neutral nPy range from -3.29 to -2.66 eV, and there is a gradual decrease in values from 1Py to 5Py and then slightly increased to -2.71eV for 9Py. On the other hand, the  $\chi$  values for polypyrrole polarons (PPy<sup>+</sup>) are higher and range from -9.86 to -5.41 eV. Hence, PPy<sup>+</sup> offers better chemical stability based on their chemical potential values.

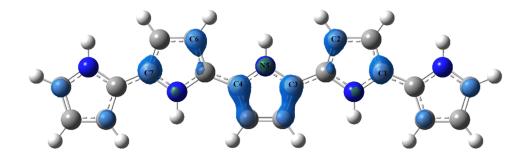
Orbital Analysis of PPy and PPy<sup>+</sup>. The frontier orbital gap helps to characterize the chemical reactivity, kinetic stability, and optical polarizability of molecules. We carried out frontier molecular orbital analysis (FMOs) at the UCAM-B3LYP/6-31+G (d,p) level of theory. Additionally, the FMO study is used to predict the spread of the electronic density of the orbitals in the studied polypyrrole. The energies of the highest occupied molecular orbitals (HOMO) and lowest unoccupied molecular orbitals (LUMO) energies and their corresponding HOMO–LUMO gaps  $(E_{H-L})$  are given in Table 4 for the neutral and polaronic states. In the neutral state, the HOMO-LUMO (E<sub>H-L</sub>) gaps range from 8.13 to 5.91 eV, where the lowest  $E_{H-L}$  value is recorded for 9Py, and the highest value is observed for 1Py. The significant reduction in the E<sub>H-L</sub> gaps may be attributed to the increased conjugation in PPy.

On the other hand, the HOMO–LUMO gaps for polarons  $PPy^+$  are slightly higher than the neutral polymers (PPy), and values range from 9.77 to 4.85 eV (Table 4). These values are

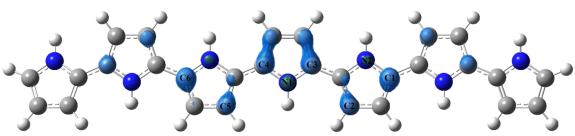












7PPy<sup>+</sup>



9PPy<sup>+</sup>

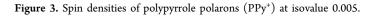


Table 3. Ionization Potential (IP in eV), Electron Affinity (VEA in eV), Chemical Hardness ( $\eta$  in eV), Chemical Softness (S in eV), and Chemical Potential ( $\chi$  in eV) of PPy and PPy<sup>+</sup>

	Neutral state (PPy)					Polaronic state (PPy <sup>+</sup> )				
nPy	IP	EA	η	S	χ	IP	EA	η	S	χ
1Py	7.36	-0.77	3.29	0.15	-3.29	14.75	4.98	4.89	0.10	-9.86
ЗРу	5.98	-0.52	2.73	0.18	-2.91	10.12	3.92	3.13	0.16	-7.02
5Py	5.84	-0.42	2.71	0.18	-2.66	8.84	3.40	2.72	0.18	-6.15
7Py	5.74	-0.31	2.71	0.18	-2.71	8.24	3.12	2.56	0.19	-5.68
9Py	5.67	-0.24	2.17	0.23	-2.71	7.83	2.98	2.43	0.20	-5.41

Table 4. HOMO and LUMO Energies and HOMO – LUMO ( $E_{H-L}$ ) Gaps (in eV) for Neutral and Polaronic PPy

	Neut	ral state (Pl	Py)	Polaronic state (PPy <sup>+</sup> )			
Polymer	НОМО	LUMO	$E_{H-L}$	НОМО	LUMO	E <sub>H-L</sub>	
1Py	-7.36	0.77	8.13	-14.75	-4.98	9.77	
ЗРу	-5.98	0.52	6.54	-10.12	-3.92	6.21	
5Py	-5.84	0.42	6.26	-8.84	-3.406	5.43	
7Py	-5.74	0.31	6.05	-8.24	-3.12	5.12	
9Ру	-5.67	0.24	5.91	-7.83	-2.98	4.85	

monotonically decreased from 1Py + to 9Py+, guaranteeing excellent electronic and conductive properties. From 1Py<sup>+</sup> to  $3Py^{+}$ , the  $E_{H-L}$  value dramatically decreases, and  $9Py^{+}$  displays a smaller gap than the corresponding 9Py. For the polypyrrolebased polaronic model (PPy<sup>+</sup>), the decreasing sequence of HOMO-LUMO gaps is  $1Py^+ > 3Py^+ > 5Py^+ > 7Py^+ > 9Py^+$ . Furthermore, 9Py's substantial HOMO energy (-7.83 eV) makes it possible to observe the reduced E<sub>H-L</sub>. The increased chain length of  $9Py^+$  has a radical (unpaired electron), which can be excited easily from HOMO to LUMO and would result in improved electrical and conductive properties. The higher degree of conjugation would also result in a drastic increase in the conductivity and reactivity of polypyrrole-based polarons. The density of the HOMO and LUMO orbitals is shown in Figure 4. The HOMO density cloud lies on the entire rings of PPy, whereas the LUMO is shifted into the middle of the rings, which shows the presence of unpaired electrons (radical). The correlation between the spin density and the existence of electronic density on the central rings in PPy<sup>+</sup> justifies the availability of radicals.

**Static Nonlinear Optical (NLO) Properties.** The literature is rich in describing different materials' NLO responses based on their hyperpolarizability values. Several studies were presented, which unfold the crucial role of excess electrons in triggering the NLO properties of molecules and clusters<sup>25,43</sup>.<sup>16,15</sup> For the first time, we studied the role of unpaired electrons (single radical) in conducting NLO-response polymers.

On the other hand, the formation of polarons in polypyrrole (oligomers) and their effect on electronic and NLO properties have still not been explored. Hence, the presence of radicals (polarons) shows a resemblance to excess electrons in determining the optical and NLO properties. The polarizability ( $\alpha_o$ ) of neutral PPy lies in the range of 50 to  $6.0 \times 10^2$  au, where the highest value is obtained for **9Py**, while the lowest value is for **1Py**. The polarizability (linear response) values increase gradually from **1Py** to **9Py** with an increased chain length of the polypyrrole. Likewise, the  $\alpha_o$  values for polarons (PPy<sup>+</sup>) are quite higher and range from 42 to  $2.7 \times 10^3$  au (Table 5). The presence of polaron-doped polypyrrole significantly increases the polarizability of PPy. The 9Py<sup>+</sup> complex is 4.5 times more polarizable than the neutral **9Py**.

To further explore the NLO response of polypyrrole, we calculated the hyperpolarizability ( $\beta_o$ ) values for second-order electric susceptibility ( $\chi^2$ ). The  $\beta_o$  values for neutral PPy range from 57 to  $1.3 \times 10^2$  au, where the highest hyperpolarizability is found for **9Py**, while the lowest value is observed for **1Py** (Table 5). The increased chain length and conjugation result in a drastic increase in  $\beta_o$  values for PPy.

On the other hand, interesting increased  $\beta_o$  values are observed for polarons (PPy<sup>+</sup>), and the value increased up to  $3.2 \times 10^4$  au for 9Py<sup>+</sup>. Strikingly, the  $\beta_o$  response for polaronic

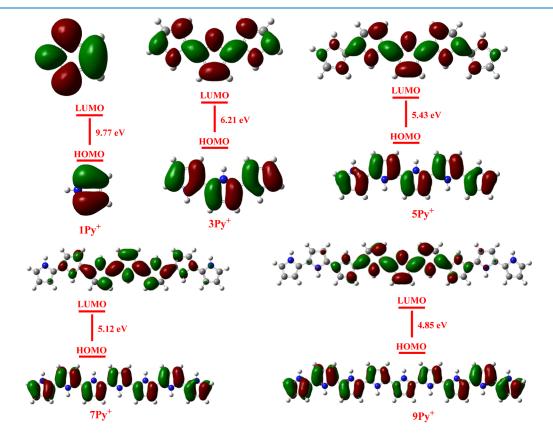


Figure 4. HOMO and LUMO densities of polarons (PPy<sup>+</sup>) at the CAM-B3LYP (isovalue = 0.025).

Table 5. Static Polarizability ( $\alpha_0$ in au), Static First Hyperpolarizability ( $\beta_0$ in au), Static Second Hyperpolarizability ( $\gamma_0$ in au),	
and $\beta_{vec}$ and Dipole Moment ( $\mu$ ) of PPy and PPy <sup>+</sup>	

		Neutral state (PPy)		Polaronic State (PPy <sup>+</sup> )			
РРу	$\alpha_{o}$	$\beta_{o}$	$\beta_{ m vec}$	$\alpha_{o}$	$\beta_{o}$	$eta_{ m vec}$	
1Py	50	57	57	42	$6.1 \times 10^{1}$	$6.1 \times 10^{1}$	
ЗРу	$1.7 \times 10^{2}$	$1.0 \times 10^{2}$	$1.0 \times 10^{2}$	$2.4 \times 10^{2}$	$2.2 \times 10^{3}$	$2.6 \times 10^{3}$	
5Py	$3.1 \times 10^{2}$	$3.4 \times 10^{2}$	$2.3 \times 10^{2}$	$6.6 \times 10^{2}$	$5.1 \times 10^{3}$	$4.2 \times 10^{3}$	
7Py	$4.5 \times 10^{2}$	$2.0 \times 10^{2}$	$2.0 \times 10^{2}$	$1.5 \times 10^{3}$	$1.4 \times 10^{4}$	$1.4 \times 10^{4}$	
9Ру	$6.0 \times 10^{2}$	$1.3 \times 10^{2}$	$1.3 \times 10^{2}$	$2.7 \times 10^{3}$	$3.2 \times 10^{4}$	$3.1 \times 10^{4}$	

Table 6. Calculated Mean Polarizabilities,  $\alpha_o$  (au) and Mean First Hyperpolarizabilities,  $\beta_o$  (au) on CAM-B3LYP, LC-BLYP, and WB97XD of Polypyrrole-Based Polarons (PPy<sup>+</sup>) as Well as for Alkyl Polypyrrole-Based Polarons (R-PPy<sup>+</sup>)

+	CAM-B3LYP		LC-BLYP		wB97XD			CAM-	CAM-B3LYP	
nPPy	$\alpha_{o}$	$\beta_o$	a	$\beta_o$	$\alpha_{o}$	$\alpha_{o}$	R-nPPy <sup>+</sup>	a	$\beta_o$	
1PPy <sup>+</sup>	42	$6.1 \times 10^{1}$	38	$1.2 \times 10^{1}$	38	$8.7 \times 10^{1}$	R-1PPy <sup>+</sup>	71	$8.8 \times 10^1$	
3PPy <sup>+</sup>	$2.4 \times 10^{2}$	$2.2 \times 10^{3}$	$2.3 \times 10^{2}$	$3.8 \times 10^{3}$	$2.2 \times 10^{2}$	$2.6 \times 10^{3}$	R-3PPy <sup>+</sup>	$3.0 \times 10^{2}$	$2.6 \times 10^{3}$	
5PPy <sup>+</sup>	$6.6 \times 10^{2}$	$5.1 \times 10^{3}$	$7.1 \times 10^{2}$	$3.4 \times 10^{3}$	$6.7 \times 10^{2}$	$5.3 \times 10^{3}$	R-5PPy <sup>+</sup>	$7.7 \times 10^{2}$	$8.7 \times 10^{3}$	
$7PPy^+$	$1.5 \times 10^{3}$	$1.4 \times 10^{4}$	$1.5 \times 10^{3}$	$2.4 \times 10^{4}$	$1.5 \times 10^{3}$	$1.5 \times 10^{4}$	R-7PPy <sup>+</sup>	$1.5 \times 10^{3}$	$9.3 \times 10^{3}$	
9PPy <sup>+</sup>	$2.7 \times 10^{3}$	$3.2 \times 10^{4}$	$2.4 \times 10^{3}$	$3.1 \times 10^{4}$	$2.6 \times 10^{3}$	$3.0 \times 10^{4}$	R-9PPy <sup>+</sup>	$2.7 \times 10^{3}$	$1.4 \times 10^{4}$	

Table 7. Static Hyperpolarizability ( $\beta_0$  in au), Frequency-dependent Hyperpolarizability  $\beta(\omega)$  in Terms of Electro-Optic Pockel's Effect (EOPE)  $\beta$  (- $\omega$ ;  $\omega$ , 0) in au, and Electric Field-Induced Second Harmonic Generation  $\beta(-2\omega;\omega,\omega)$  in au at  $\omega = 532$  and 1064 nm of PPy<sup>+</sup>

	$\omega = 0$	$\omega = 532 \text{ nm}$		$\omega = 1064 \text{ nm}$		
$nPy^+$	eta (0; 0,0)	$\beta$ (- $\omega$ ; $\omega$ ,0)	$\beta(-2\omega; \omega, \omega)$	$\beta$ (- $\omega$ ; $\omega$ ,0)	$\beta (-2\omega; \omega, \omega)$	
$1Py^+$	$6.2 \times 10^{1}$	$2.1 \times 10^{1}$	$7.0 \times 10^{1}$	$1.7 \times 10^{2}$	$1.9 \times 10^{1}$	
3Py <sup>+</sup>	$2.8 \times 10^{3}$	$2.4 \times 10^{3}$	$3.4 \times 10^{4}$	$5.4 \times 10^{3}$	$1.7 \times 10^{3}$	
5Py <sup>+</sup>	$6.1 \times 10^{3}$	$1.4 \times 10^{4}$	$7.7 \times 10^{4}$	$4.8 \times 10^{5}$	$1.0 \times 10^{6}$	
$7Py^+$	$1.4 \times 10^{4}$	$5.8 \times 10^{4}$	$4.0 \times 10^{6}$	$6.1 \times 10^{3}$	$1.3 \times 10^{4}$	
9Py <sup>+</sup>	$3.2 \times 10^4$	$5.5 \times 10^{4}$	$1.8 \times 10^{5}$	$1.3 \times 10^{4}$	$1.7 \times 10^{4}$	

9Py<sup>+</sup> is 24.6 times higher than that of neutral **9Py**, which might be attributed to the presence of a radical (unpaired electron) in polypyrrole-based polarons. Hyperpolarizability ( $\beta_0$ ) increases with the chain lengths in these polarons. Electronic properties can be correlated with hyperpolarizability responses, where a reduced ionization potential favors improved NLO properties as chain length grows. Similarly, the correlation of the electronic properties of PPy+ with the electronic parameters can be seen by analyzing IP, HOMO – LUMO  $(E_{H-L})$  gaps, and chemical hardness ( $\eta$ ). The decreased values of IPs and  $E_{H-L}$  would result in a significant enhancement in the  $\beta_{o}$ response. Hence, based on the thermal stability of PPy, a drastic change in their electronic properties can be seen by introducing the polaron model. The designed polypyrrolebased polarons are the new candidate in NLO materials based on their superb electronic and static hyperpolarizability response.

Additionally, to further explore the NLO properties, we estimated the projection of hyperpolarizability on the dipole moment ( $\beta_{vec}$ ). The values of the vector part of hyperpolarizability are given in Table 5. An identical trend of  $\beta_{vec}$  with  $\beta_o$  can be seen in the studied polypyrrole and their corresponding polarons (PPy<sup>+</sup>), which suggests the projection of hyperpolarizability on the dipole moment vector in one direction. A nice correlation is observed between  $\beta_o$  and  $\beta_{vec}$  indicating that hyperpolarizability lies mainly on the dipole moment axis in the unidirection.

Moreover, polarizability and hyperpolarizability values are also calculated on other DFT functionals for comparison (LC-

BLYP and WB97XD functional) with the 6-31+G(d,p) basis set (see Table 6). The obtained results are compared with results observed at the CAM-B3LYP/6-31+G(d,p) level of theory. Overall, it is observed that the values of  $\beta_o$  obtained at the CAM-B3LYP/6-311+G(d,p) level of theory are comparable to those obtained at the LC-BLYP and WB97XD functionals. These additionally computed results support and validate our results computed initially at the CAM-B3LYP/6-311+G(d,p) level of theory. Moreover, we introduced the alkyl (propyl) chain at the N-H groups of pyrrole rings and calculated their NLO response. The calculated values for polypyrrole-based polarons with an alkyl chain (R-PPy+) are reported in Table 6. The comparison of the obtained mean polarizabilities ( $\alpha_o$ ) and mean first hyperpolarizabilities ( $\beta_o$ ) of polypyrrole-based polarons with an alkyl chain (R-PPy+) with the polypyrrole-based polarons (PPy<sup>+</sup>) reveals that the NLO response is almost comparable. The polarizabilities and first hyperpolarizabilities values in both cases vary by  $\pm 0.1$  au.

**Dynamic NLO Properties of Polarons.** As polarons (PPy<sup>+</sup>) have excellent static NLO properties, we extended our study to frequency-dependent NLO properties. The dynamic hyperpolarizability  $\beta(\omega)$  values have been reported with incident frequencies of 532 and 1064 nm. The molecular design of highly active dynamic nonlinear optical (NLO) materials has been a hot topic in materials science because of their future applications in photonics and optoelectronics. The  $\beta(\omega)$  is estimated through electro-optical Pockel's effect (EOPE)  $\beta$  (- $\omega$ ;  $\omega$ ,  $\omega$ ) and second harmonic generation (SHG)  $\beta(-2\omega; \omega, \omega)$  phenomenon. The frequency-depend-

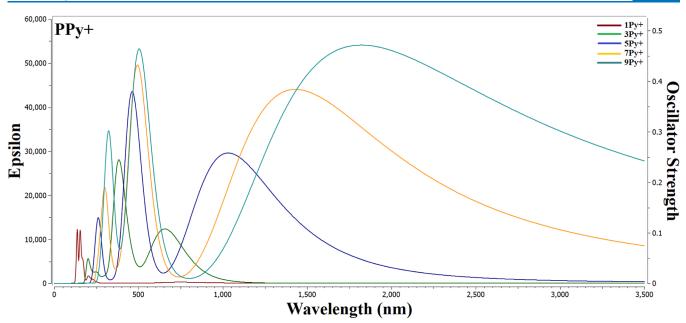


Figure 5. Absorption spectra of polypyrrole-based polarons ( $PPy^+$ ) at the TD-CAM-B3LYP/6-31 + g(d,P) method.

ent NLO parameters are given in Table 7. The light with specific wavelengths of 532 nm ( $\omega$  = 0.0856 au) and 1064 nm ( $\omega = 0.0428$  au) was adopted for simulations. Overall, the simulated frequency-dependent first hyperpolarizabilities  $\beta(\omega)$ are quite higher than that of static hyperpolarizability ( $\beta_0$ ). The increased  $\beta(\omega)$  response indicates external frequency's role in polypyrrole's nonlinearity. The determined EOPE and SHG values are significant at smaller dispersion frequency of 1064 nm (0.0428 au), whereas the values are slightly reduced at the frequency of 532 nm (Table 7). The calculated  $\beta$  (- $\omega$ ,  $\omega$ , 0) value of  $5.5 \times 10^4$  au is the highest for **9Py**<sup>+</sup> at 532 nm, while it increased up to  $4.8 \times 10^5$  au for 5Py<sup>+</sup> with reduced external frequency (1064 nm). Likewise, the calculated significant SHG value of  $4.0 \times 10^6$  au is recorded for 7Py<sup>+</sup> at 532 nm, while it became  $1.0 \times 10^6$  au for **5Py**<sup>+</sup> at the dispersion frequency of 1064 nm.

**UV–visible Study of Polarons.** The NLO materials are unique because they have a second harmonic generation (SHG) doubling frequency. Materials with the highest NLO qualities must be transparent in the presence of a functioning laser. The UV–visible properties of polypyrrole-based polarons (PPy<sup>+</sup>) are evaluated using TD-DFT calculations, and the spectra are shown in Figure 5. Table 8 shows the results of absorption wavelengths, total energy, and maximal oscillator strengths (during the crucial transition). In polarons (PPy<sup>+</sup>), the absorbance spectra are red-shifted, and band gaps are reduced. The absorption maxima of PPy appear in the range of

Table 8. Transition Energies ( $\Delta E$ ) in au, Oscillator Strength ( $f_o$  in au), and Absorption Wavelengths ( $\lambda$ max in nm, Dipole Moments ( $\mu$  in au) for all Polypyrrole-Based Polarons

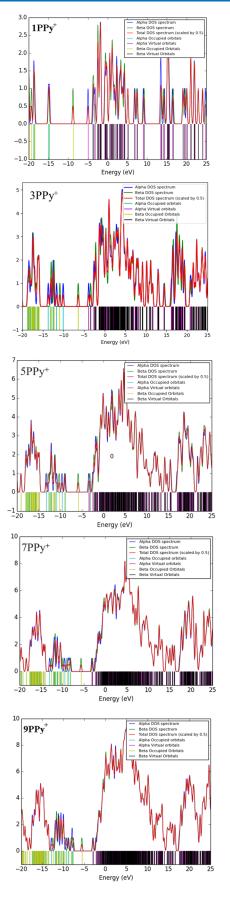
$nPy^+$	$\Delta E$	$f_o$	$\lambda_{ m max}$	μ
1Py <sup>+</sup>	8.29	0.29	149	0.73
3Py <sup>+</sup>	3.28	0.59	377	0.76
5Py <sup>+</sup>	2.67	1.07	463	0.74
$7Py^+$	0.88	1.08	1430	0.75
9Py <sup>+</sup>	0.68	1.34	1821	0.76

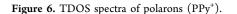
200 to 1800 nm, whereas the highest absorption of 9Py<sup>+</sup> was recorded at 1821 nm. The calculated absorption maxima ( $\lambda$ max) values for 1Py<sup>+</sup>, 3Py<sup>+</sup>, 5Py<sup>+</sup>, and 7Py<sup>+</sup> are 149, 377, 463, and 1430 nm, respectively. The modest absorption in the UV–visible region is observed in these maximums, demonstrating appropriate transparency under a generally practical laser. The 1Py<sup>+</sup>, in particular, is transparent in the deep UV region of (200 nm). As a result, these findings show that these polymers can serve as crucial building blocks for deep-violet NLO materials.

Density of States (DOS) Analysis of Polarons (PPy<sup>+</sup>). Total density of states analysis (TDOS) was used to get further insights into the studied polarons' electronic properties and orbital energies. The density of states (DOS) is the number of different states that electrons can occupy at a particular energy level. The formation of new energy states and alterations in the intensity of their peaks in the density of states (DOS) spectra are crucial for understanding the interaction mechanism and conductive properties of these polymers. The plotted TDOS spectra are shown in Figure 6. From the plotted spectra, one can observe that an increased number of PPy<sup>+</sup> rings would increase the number of states that appeared. The newly born energy states are also shifted to higher energy, which is also responsible for the significant reduction in HOMO-LUMO gaps. For  $1PPy^+$  the HOMO line appears near -10 eV, and for higher 9PPy<sup>+</sup>, the HOMO energy line rose to near 5 eV. Hence, the increased conjugation and chain length of PPy<sup>+</sup> would result in enhanced electrical and conductive properties. Thus, the larger-sized polarons (PPy<sup>+</sup>) show better conductive and nonlinear optical properties.

#### CONCLUSIONS

We presented a new approach to designing PPy-based polarons with remarkable electronic and NLO properties. The formation of polarons in thermally conducting polymers (PPy) has significantly reduced excitation energies ( $\Delta E$ ), which would result in a drastic enhancement in static first hyperpolarizability ( $\beta_o$ ). The studied polarons (PPy<sup>+</sup>) show excellent electronic properties and have reduced ionization





potential (IP) as compared to neutral PPy, and values decrease further with increased chain lengths (1Py to 9Py). The global reactivity descriptors show an interesting trend where softness (S) grows with the PPy chain length but hardness  $(\eta)$ decreases in the same fashion. The E<sub>H-L</sub> gaps for the PPy<sup>+</sup> polaronic state are significantly lower than their corresponding neutral PPy. In the polaronic model (PPy<sup>+</sup>), radicals decisively reduce the crucial excitation energy reminiscent of excess electrons (alkali metals). The static hyperpolarizability response ( $\beta_0$ ) is recorded up to  $1.3 \times 10^2$  au for **9Py**, while for polaron 9Py<sup>+</sup>, it has risen up to  $3.2 \times 10^4$  au. The static hyperpolarizability of the 9Py<sup>+</sup> polaronic state is 246 times higher than the corresponding neutral analogue, **9Py**. The  $\beta_{vec}$ values show a strong correlation with the total hyperpolarizability ( $\beta_0$ ). The performed TDOS spectral analysis further justifies the better conductive and electronic properties of polarons (PPy<sup>+</sup>) with increased chain lengths (conjugation). Furthermore, the calculated second harmonic generation (SHG) values are up to  $4.0 \times 10^6$  au at 532 nm, whereas electro-optic Pockel's effect (EOPE) is much more pronounced at a higher dispersion frequency (1064 nm). The TD-DFT study further shows the increased absorption maxima  $(\lambda_{\text{max}})$  with the increased size of PPy<sup>+</sup>. With increased length, a significant reduction in excitation energies ( $\Delta E$ ) is observed; PPy also favors the improved NLO response. Due to their improved thermal and electronic properties, the studied polypyrrole-based polarons (PPy<sup>+</sup>) are novel additions to the NLO material family.

# ASSOCIATED CONTENT

#### Data Availability Statement

The author affirms that the article's Supporting Information and the data used to support the study's findings are included. Upon a reasonable request, raw data from the corresponding sources are accessible to support the findings of this study.

#### AUTHOR INFORMATION

#### **Corresponding Authors**

- Khurshid Ayub Department of Chemistry, COMSATS University Islamabad, Abbottabad Campus, Abbottabad KPK, 22060, Pakistan; orcid.org/0000-0003-0990-1860; Email: khurshid@cuiatd.edu.pk
- Haitao Ma Beijing National Laboratory for Molecular Sciences, Institute of Chemistry, Chinese Academy of Sciences, Beijing 100190, China; orcid.org/0000-0002-2506-5498; Email: mht@iccas.ac.cn

### Authors

- Atazaz Ahsin Beijing National Laboratory for Molecular Sciences, Institute of Chemistry, Chinese Academy of Sciences, Beijing 100190, China; School of Chemical Sciences, University of Chinese Academy of Sciences, Beijing 100049, China
- **Iqra Ejaz** Department of Chemistry, COMSATS University Islamabad, Abbottabad Campus, Abbottabad KPK, 22060, Pakistan
- Sehrish Sarfaraz Department of Chemistry, COMSATS University Islamabad, Abbottabad Campus, Abbottabad KPK, 22060, Pakistan

Complete contact information is available at: https://pubs.acs.org/10.1021/acsomega.3c09468

# Author Contributions

<sup>#</sup>These authors contributed equally to this work.

## Notes

The authors declare no competing financial interest.

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