

Finding correct protein–protein docking models using ProQDock

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Abstract

Motivation: Protein–protein interactions are a key in virtually all biological processes. For a detailed understanding of the biological processes, the structure of the protein complex is essential. Given the current experimental techniques for structure determination, the vast majority of all protein complexes will never be solved by experimental techniques. In lack of experimental data, computational docking methods can be used to predict the structure of the protein complex. A common strategy is to generate many alternative docking solutions (atomic models) and then use a scoring function to select the best. The success of the computational docking technique is, to a large degree, dependent on the ability of the scoring function to accurately rank and score the many alternative docking models.

Results: Here, we present ProQDock, a scoring function that predicts the absolute quality of docking model measured by a novel protein docking quality score (DockQ). ProQDock uses support vector machines trained to predict the quality of protein docking models using features that can be calculated from the docking model itself. By combining different types of features describing both the protein–protein interface and the overall physical chemistry, it was possible to improve the correlation with DockQ from 0.25 for the best individual feature (electrostatic complementarity) to 0.49 for the final version of ProQDock. ProQDock performed better than the state-of-the-art methods ZRANK and ZRANK2 in terms of correlations, ranking and finding correct models on an independent test set. Finally, we also demonstrate that it is possible to combine ProQDock with ZRANK and ZRANK2 to improve performance even further.

Availability and implementation: <http://bioinfo.ifm.liu.se/ProQDock>

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Supplementary information: [Supplementary data](#) are available at *Bioinformatics* online.

1 Introduction

Protein–protein interactions are crucial in almost all biological processes. To understand the mechanism of protein–protein interaction, the structure of the protein complex is essential. Despite massive efforts in structure determination the majority of protein complexes are not and will never be available in the PDB (Berman *et al.*, 2000). Thus, there is a great need for computational methods that are able to build models of protein complexes using docking.

Constructing models of protein complexes is a fundamental challenge in structural biology and despite years of investigation is still unsolved. The problem can be divided into sampling and scoring, where sampling is the problem of generating realistic docking models, and scoring is the problem of identifying the correct docking models among many incorrect ones. A number of different approaches have been applied to this problem ranging from

composite scoring describing the physics (Dominguez *et al.*, 2003; Cheng *et al.*, 2007; Lyskov and Gray, 2008; Pierce and Weng, 2007, 2008) to methods derived from the statistics of structural databases (Geppert *et al.*, 2010; Liu and Vakser, 2011; Pons *et al.*, 2011), methods based on interface composition and geometry (Chang *et al.*, 2008; Khashan *et al.*, 2012; Mitra and Pal, 2010) or complementarity (Gabb *et al.*, 1997; Lawrence and Colman, 1993; McCoy *et al.*, 1997) and methods based on machine learning (Bordner and Gorin, 2007; Chae *et al.*, 2010). The different approaches provide different aspects of docking model quality and could potentially result in higher performance when combined together (Moal *et al.*, 2013).

The multitude of approaches applied to the scoring problem highlights the difficulty in scoring protein docking models. At one end there are features that serve as critical filters for complex

formation, like shape complementarity (Lawrence and Colman, 1993) while on the other end, there could be features that might largely vary even among good-quality models. It is, for instance, fairly easy to generate completely incorrect docking models with good shape complementarity, as the van der Waals interactions contribute favorably to the scoring function used in sampling. Another problem in scoring docking models in general occurs when the docking models have been generated using different force fields, which is often the case, in particular in the scoring part of CAPRI (Lensink and Wodak, 2014). In this case, an almost perfectly correct model scoring well in one force field, might contain some small clashes in some other force field. Of course, it might be possible to refine the docking models and remove the clash. However, this is time-consuming and it might be worthy only if the model is correct, and as most docking models are incorrect it would be better if promising cases could be quickly detected without the need for extensive calculations. For instance, the use of coarse-grained scoring function, which are less sensitive to local errors than all-atom scoring functions (Viswanath *et al.*, 2013) is one such example. However, it is likely that other features such as electrostatic balance at the interface, solvation, amino acid composition at the interface, etc. are also important to discriminate incorrect and correct docking models and finding the right balance between features is a highly non-trivial task.

In this study, we present the development of an algorithm, ProQDock, that predicts the quality of docking models using structural information, scoring functions and the predicted features were combined using a support vector machine (SVM). The method is optimized on realistic docking models to predict the DockQ score (Basu and Wallner, 2016), of the corresponding model. DockQ is a score between 0 and 1, which is similar to IS-score (Gao and Skolnick, 2011) in its design, but optimized to reproduce the CAPRI classification (Lensink *et al.*, 2007).

2 Methods

2.1 Training set

To train ProQDock, two benchmark sets of protein–protein docking models were used, the ‘CAPRI’ set (Lensink and Wodak, 2014), which contains 19 013 models from 15 targets submitted to the CAPRI scoring experiment, and the ‘MOAL’ set (Moal *et al.*, 2013) containing 56 015 models for 118 targets from the docking Benchmark 4.0 (Hwang *et al.*, 2010) using SwarmDock (Torchala *et al.*, 2013) to generate the models (generously provided by authors of Moal *et al.*). The targets T36 (PDB ID: 2W5F) and T38 (3FM8) from the CAPRI set were discarded because they lacked at least a single acceptable (or better) model, resulting in 17 777 models from 13 targets.

The constructions of the two benchmark sets are completely different: the CAPRI set is based on docking model submitted to CAPRI, which contains predictions from *many different* methods, while the MOAL set contains models generated with only *one* method. In that respect, the CAPRI set is probably more realistic, as it contains models made with a variety of methods. On the other hand, the number of models and in particular the number of targets are small in the CAPRI set. Thus, to achieve a larger and more balanced set, the CAPRI set and MOAL set were combined into one set, ‘CnM’ (CAPRI and MOAL), to be used in training ProQDock using cross-validation (see below). The combined data set contained 73 792 docking models from 131 targets and is available at <http://bioinfo.ifm.liu.se/ProQDock/>.

2.2 Independent test set, BM5

Although, training of the machine learning algorithm was performed using a cross-validation procedure, the efficacy of ProQDock was independently tested on a dataset based on 55 new docking targets added to the Benchmark 4.0 in its updated version, Benchmark 5.0 (Vreven *et al.*, 2015). In total, 25 985 docking models generated with SwarmDock (Torchala *et al.*, 2013) for these 55 targets were again kindly provided by the authors of Vreven *et al.* (2015).

2.3 Native structures test set

To test the ability of ProQDock on native structure and to suggest a range of predicted values characteristic of native protein–protein complexes. A set consisting of 1879 co-crystallized interacting native structures with resolution better than 2 Å, and no missing backbone atoms were assembled using the ‘Build Database’ option from Dockground (Anishchenko *et al.*, 2014).

2.4 Cross-validation test sets

Five-fold cross-validation was used for training and assessing performance. To this end the training set targets were divided in five parts (cross-validation test sets) with no homologous proteins between them, four were used for training while testing the remaining one. This was performed for each of the five parts to get predictions for the whole set. All homologous proteins were placed in the same cross-validation test set, to ensure that the training and testing data for the same round of cross-validation did not contain any homologous between them. Blastclust (Altschul *et al.*, 1990) was used to cluster homologous sequences from all complexes using a strict criteria 20% sequence similarity over at least 50% sequence coverage (-L 0.5 -S 20). Two complexes were considered homologous if at least one of the partners was homologous and placed in the same cluster. Finally, all clusters were grouped into five with approximately the same number of targets, with the total number of models spanning from 13 058 to 15 227 and the ratio of acceptable (or better) to incorrect models, spanning a range of 0.016 to 0.14. Neither different groupings (5-fold) nor jack-knifing (leave-one-out) did affect the performance (data not shown). A similar cross-validation strategy was used in the related problem of binding affinity predictions (Marillet *et al.*, 2016) having similar number of high-level features (11 compared to 13 in the current study) and similar number of available native target complexes (144 compared to 131).

2.5 Target function

The target function should ideally reflect the true quality of a given protein–protein docking model. The state-of-the-art quality measure in docking, established by the CAPRI community, is to use three distinct though related measures, F_{nat} , LRMS and iRMS (Méndez *et al.*, 2003). F_{nat} is the fraction of native interfacial contacts preserved in the model, LRMS the root mean square deviation for the smaller chain (ligand) after superposition of the larger chain (receptor) and iRMS is the RMS deviation of the interfacial atoms. By applying various *ad hoc* cutoffs on these three measures, protein–protein docking models are classified as ‘incorrect’, ‘acceptable’, ‘medium’ or ‘high’ quality. To avoid this classification scheme, we recently developed DockQ (Basu and Wallner, 2016), which combines F_{nat} , LRMS and iRMS into a continuous score between [0,1], reflecting no similarity (0) to perfect similarity (1). It was demonstrated that the continuous DockQ score can almost completely recapitulate the CAPRI classification into incorrect, acceptable, medium and high quality (94% average PPV at 90% Recall) using

the following cutoffs: incorrect <0.23, acceptable [0.23,0.49), medium [0.49,0.8), high >0.8. Thus, DockQ is essentially a higher resolution version of the already established state of the art in the docking field and used as the target function to train ProQDock.

2.6 SVM Training

The Support Vector Regression module in the SVM^{light} package (Joachims, 2002) was used to train ProQDock using 5-fold cross-validation with radial basis function (RBF) kernel. The trade-off between training error and margin, C , and the RBF γ parameter were optimized using a grid search in the ranges; C from 2^{-15} to 2^{10} , and γ from 2^{-10} to 2^{10} , in \log_2 steps, maximizing the cross-validated Pearson's correlation coefficient. The epsilon width of tube for regression was kept at 0.1 (default). Because there were large imbalances in the number of acceptable (positive example) and incorrect (negative) models, the cost factor (-j flag) option of SVM_{learn} was set to the ratio of 'incorrect-to-acceptable' models, so that the training errors on negative examples could be outweighed by errors on positive examples (Morik *et al.*, 1999). Rosetta energy terms and CPM were scaled between 0 and 1 to improve convergence using logistic scaling: $Scaled(E) = 1/(1 + \exp(-k(E-E_0)))$, where E_0 is the midpoint of the sigmoid and k the steepness of the sigmoid curve. E_0 and k were optimized by estimating the cumulative distribution function, $cdf(E)$, for a given training feature using the kernel smoothing function $ksdensity$ in MATLAB. E_0 was chosen as the midpoint of the data, i.e. $cdf(E_0) = 0.5$, and k to cover at least 99% of the data, by selecting the lowest k (largest coverage) that made the Scaled(E) pass through the points (E_1 , 0.01) or (E_2 , 0.99) where $cdf(E_1) = 0.01$ and $cdf(E_2) = 0.99$.

2.7 Training features

A number of different features that describe either some specific structural properties of protein-protein interfaces or the overall protein structural integrity and quality were calculated and used for training ProQDock. The features are described in detail below.

2.7.1 Shape complementarity

The complementary in shape of protein-protein interface is a necessary condition for binding. Shape complementarity (Sc) of a protein-protein interface (Lawrence and Colman, 1993) was calculated using the program Sc part of CCP4 package (Winn *et al.*, 2011). Sc is defined in a range from -1 to 1 corresponding to anti- and perfectly correlated surfaces, respectively.

2.7.2 Electrostatic complementarity

The electrostatic character of native protein-protein interfaces is generally associated with anti-correlated surface electrostatic potentials (McCoy *et al.*, 1997), reflected in positive values of the term, electrostatic complementarity (EC). First, the molecular surface (Connolly, 1983) was generated individually for both the partner molecules using the software EDTSurf (Xu and Zhang, 2009), with the scale factor for the optimum fit of the molecule in a bounding box set to 1.0. The protein-protein interface atoms were defined as atoms having a net (non-zero) change in solvent accessible surface area calculated for the bound and unbound state by NACCESS (Hubbard and Thornton, 1993). Hydrogen atoms were geometrically fitted by REDUCE (Word *et al.*, 1999), partial charges and atomic radii were assigned by the AMBER94 all-atom molecular-mechanics force field (Cornell *et al.*, 1995). DelPhi (Li *et al.*, 2012) was used to compute the electrostatic potential for each surface point (buried on association) at the interface, iteratively solving the

linearized version of the Poisson-Boltzman equation. From the electrostatic surface potentials generated at both interfaces, EC was calculated precisely according to the original methodology (McCoy *et al.*, 1997), which was also used to probe electrostatic complementarity (E_m) within protein interiors (Basu *et al.*, 2012). The internal dielectric within the interior and buried interfaces of proteins were generally considered to be low ($\epsilon = 2$), although, the more advanced multi-dielectric Gaussian smoothing method (Li *et al.*, 2013) was also adapted in a trial calculation in all native structures (DB3). Both methods (single and multi-dielectric) resulted in similar EC values (rmsd: 0.15, Pearson's Correlation: 0.94). Similar to Sc, EC is defined from -1 to 1, and it approaches 1 with increasing matching (anti-correlation) of surface electrostatic potential generated on the same surface, owing to two complementary set of atoms, whereas a negative EC reflects unbalanced electric fields at the interface.

2.7.3 Relative size of the interface (nBSA, Fintres)

Neither the shape (Sc) nor EC, described above, takes the size of the interface into account. Native complexes have been found to exist spanning a wide range from small (< 10 amino acids) to large interfaces (Basu *et al.*, 2014b). Also, only a few atoms at the interface can give rise to very high Sc (Lawrence and Colman, 1993) depending on how good their shapes correlate (e.g. 2FPE: 39 atoms, Sc: 0.83, 1D2Z: 14 atoms, Sc: 0.57). Thus, both Sc and EC should be coupled with additional features measuring the size of the interface. Following similar formulations to that of the 'Overlap' parameter (Banerjee *et al.*, 2003) introduced for protein interiors, here, two related yet independent measures were calculated to account for the size of the interface: (i) the normalized buried surface area (nBSA), which measures the fraction of exposed surface area buried upon association, and (ii) the fraction of residues buried at the interface (Fintres).

2.7.4 Joint conditional probability of Sc, EC given nBSA

The joint conditional probability of Sc and EC given the actual size of the interface obtained from native protein-protein interactions (PPI) complexes was added as a separate feature. A similar function was shown to be successful in fold-recognition (Basu *et al.*, 2012). To this end, nBSA, Sc and EC were computed in a database containing 1879 native structures from DOCKGROUND (see Section 2). Based on the distribution of nBSA, interfaces were classified as small ($nBSA \leq 0.05$), medium ($0.05 < nBSA \leq 0.10$) and large ($nBSA > 0.10$). Distributions of Sc and EC were divided into intervals of 0.05 and their normalized frequencies calculated. For a given complex, CPM is the joint conditional probability of finding its interface within a certain range of Sc and EC given its size (nBSA), i.e. $CPM = \log(P(Sc|nBSA)) + \log(P(EC|nBSA))$, where $P(Sc|nBSA)$ and $P(EC|nBSA)$ are the probabilities of finding an interface within a certain range of Sc and EC values conditioned by its relative size, nBSA. CPM was set to 0 if $P(Sc|nBSA)$ or $P(EC|nBSA)$ was 0 to avoid the log score being undefined.

2.7.5 Link density

To capture the density of atomic contacts at the interface, the link density (Ld) measure was implemented (Basu *et al.*, 2011). Ld is defined as the ratio of the actual number of links at the interface to the theoretical maximum number of links, where a link is pair of interacting residues from two chains defined as having at least one pair of heavy atoms within 6Å. If M and N residues are found to be at the interface from chain A and B, respectively, then the maximum number of links is $M \times N$.

2.7.6 Interface contact preference score

It is well known that particular inter-residue contacts are preferred at protein interfaces (Lo Conte *et al.*, 1999). To account for this fact, a Contact Preference Score (CPscore) was derived by training a SVM to predict DockQ using inter-residue contact information alone. The training was performed using the 5-fold cross-validation sets, as described above, but before the training of ProQDock. The inter-residue contact information was encoded as the fraction of any residue-residue contact, weighted by a contact preference weight available in the literature (Glaser *et al.*, 2001). All possible combinations of amino acid pairs comprise 210 residue-residue contacts. Inter-residue contacts were defined as any two side-chain heavy atoms (CA for Glycine) within 10Å between the two molecules. This cutoff was deliberately kept somewhat relaxed in consistency with the measure iRMS (Méndez *et al.*, 2003), to account for all possible combination of residue pairs at the interface.

2.7.7 Accessibility score

The expected distribution of amino acid residues with respect to burial was estimated by the accessibility score (*rGb—residue Given burial*) as detailed in an earlier publication (Basu *et al.*, 2014a). *rGb* measures the propensity of a particular amino acid residue given a specific solvent accessibility. First, the burial of solvent exposure for individual residues were estimated by the ratio of ASA of the amino acid X in the polypeptide chain to that of an identical residue located in a Gly-X-Gly peptide fragment with a fully extended conformation. The hydrophobic burial profile for a given PPI model was then compared with an equivalent native profile. The *rGb* values for native PPI complexes are in the range of 0.059 (± 0.022) (Basu *et al.*, 2014b), where values 2σ below the mean (here 0.011) correspond to partially unfolded structures with hydrophobic residues being completely exposed to the solvent (Basu *et al.*, 2014a). The consideration of *rGb* as an all-atom feature was also motivated by recent studies, emphasizing the plausible role of the non-interacting protein surface in modulating the binding affinity of potential protein-protein interactions (Visscher *et al.*, 2015), primarily owing to solvation effect.

2.7.8 Protein model accuracy (ProQ2)

The overall structural quality of the whole complex, taken to be a folded pseudo-unimolecule, was estimated by the protein quality predictor ProQ2 (Uziela and Wallner, 2016) shown to be one of the best protein quality predictors in CASP11 quality assessment category (Kryshtafovich *et al.*, 2015).

2.7.9 Rosetta energy terms (*rTs*, *Isc*, E_{rep} , E_{tmr})

The structure integrity and quality of packing was assessed by scoring each protein-protein docking model using Rosetta all-atom energy function with the 'talaris2013' weight set (O'Meara *et al.*, 2015). Before scoring, the side chains of each protein-protein docking model were rebuild. Ideally, each model should have been subjected to a full Rosetta relax or at least a short minimization to relieve potential backbone clashes. However, it turned out that even only side chain rebuild and minimization was too time-consuming (>5 min per model in some cases), given that the aim of the current study is to develop a tool that should be able to score thousands of models.

The Rosetta total score (*rTs*), the interface energy (*Isc*), the van der Waals repulsive term (E_{rep}) and the total score minus the repulsive term (E_{tmr}) were used. The reason to separate the repulsive term was that even a small clash might give high contributions to the total

energy, obfuscating potential good energy terms. Because all terms except *Isc* depend on the chain length (the probability of higher number of interactions increases with chain length), before SVM training all terms except *Isc* were normalized by the length of the target complex. *Isc* was not normalized because stability in terms of binding energy is not necessarily a function of the interface size, and there might be instances where a small but stable interface could be energetically more favorable than a larger (unstable) interface.

2.8 ZRANK and ZRANK2

The knowledge-based all atom energy terms ZRANK (Pierce and Weng, 2007) and ZRANK2 (Pierce and Weng, 2008) were also computed, primarily for comparing the SVM results, but also for use in the hybrid method ProQDockQZ. Both ZRANK and ZRANK2 include van der Waals, electrostatics (Coulomb, using distance dependent dielectric) and desolvation energy terms. In addition, ZRANK2 includes the IFACE term, an interface statistical potential (Mintseris *et al.*, 2007). ZRANK was primarily designed to re-rank initial docking predictions from ZDOCK, while ZRANK2 was designed toward refinement of protein docking models, in conjunction with RosettaDock (Gray *et al.*, 2003). Besides the IFACE potential, the weight for the repulsive van der Waals is significantly smaller for ZRANK, making it less sensitive to small clashes compared with ZRANK2.

2.9 Evaluation Measures

Apart from calculating direct correlation (Pearson's) between scoring function and the quality measure (DockQ) used as target function, performance was also measured by Receiver Operating Characteristic (ROC) curves and ability to correctly rank models.

2.9.1 ROC curves

Performance of classifying protein-protein docking models as acceptable or better according to the CAPRI classification was evaluated based on true-positive rate (TPR, also known as recall), and false-positive rate (FPR)

$$TRP = Recall = \frac{TP}{\sum TP} = \frac{TP}{TP + FN}$$

$$FRP = \frac{FP}{\sum FP} = \frac{FP}{FP + TN}$$

where TP is the number of protein-protein docking models with a CAPRI classification *acceptable or better* correctly predicted as positive (true positives); FP is the number of misclassified negative cases (false positive); TN is the number of correctly predicted negatives (true negatives); FN is the number of misclassified positive cases (false negative). For any prediction method, ROC curves (TPR versus FPR) were constructed by sorting the prediction from good to bad and calculate TP, FP, FN, TN for all possible cutoffs for positive prediction. The area under the curve (AUC) was calculated using the trapezoidal numerical integration function `trapz` in MATLAB.

2.9.2 Ranking ability

The ability to properly rank models was measured by counting the number of correct models, defined as acceptable or better, ranked at top 1; within top 5, top 10 and top 100 by any given method. This measure is identical to the measure in a recent benchmark of scoring metrics for docking (Moal *et al.*, 2013).

3 Results and Discussion

The aim of this study was to develop a method, ProQDock, that is capable of predicting the absolute quality of protein–protein docking models. The main idea is to calculate high-level features (Table 1) from each protein–protein docking model and use these features to predict the correctness of the protein–protein docking model as measured by the DockQ score (see Section 2).

3.1 Development of ProQDock

SVM training was performed using 5-fold cross-validation using different subsets of features in Table 1 to predict the DockQ score on the combined CnM dataset and the performances were primarily evaluated by their Pearson's Correlation values (versus DockQ). Best individual correlations were obtained for EC (0.24) and nBSA (0.17) (Fig. 1). Features were then categorized into interface (Int1, Int2) and all-atom (All1, All2) features according to their physico-chemical description, finally leading into four groups—Int1: size and packing of the interface {nBSA, Fintres, Sc, Ld}; Int2: electrostatics, binding energy and composition of the interface {EC, CPM, CPscore, ISc}; All1: solvation and overall quality of the whole complex {rGb, ProQ2}; All2: the Rosetta all-atom energy terms {rTs, Erep, Etmr}. Each group had better correlations than any of their constituting features (Fig. 1). Merging the interface and the all atom

Table 1. Description of ProQDock training features

Features	Feature description
nBSA	Normalized buried surface area
Fintres	Fraction of residues at the interface
rGb	Accessibility score
CPscore	Contact Preference score
Ld	Link Density at the interface
Sc	Shape Complementarity at the interface
EC	Electrostatic Complementarity at the interface
CPM	Joint Conditional Probability of Sc, EC given nBSA
ProQ2	Protein model quality prediction
ISc ^a	Rosetta interface energy
rTs ^a	Rosetta total energy
Erep ^a	Rosetta repulsive term
Etmr ^a	Rosetta total energy minus repulsive

^aEnergy terms, lower scores are better.

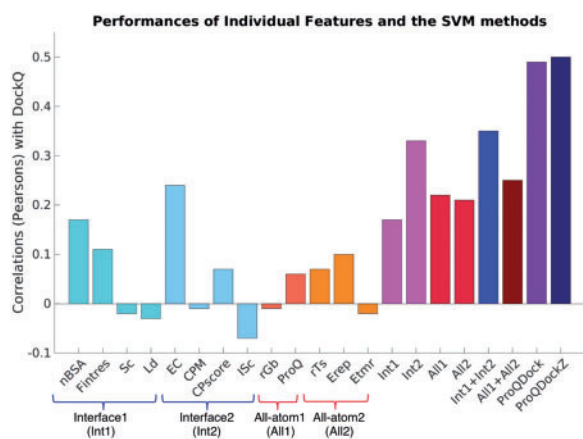


Fig. 1. Correlations with DockQ for different training features and their combinations

features, correlations were further improved to 0.35 for {Int1 + Int2} and 0.25 for {All1 + All2}, respectively. Finally, combining all features, it was possible to improve the performance to 0.49 for ProQDock (Fig. 1). The correlations indicate that the interface features are more influential though the all atom features are also necessary to improve the overall performance.

In addition, ProQDock was combined with the external energy terms, ZRANK (Pierce and Weng, 2007) and ZRANK2 (Pierce and Weng, 2008) (ProQDockZ), using a linear weighted sum optimized on the CnM set. ZRANK2 and ZRANK were chosen primarily as independent methods to benchmark the performance of ProQDock because ZRANK2 was one of the best methods in a recent benchmark of docking scoring functions (Moal *et al.*, 2013). To analyze if combining different complementary scoring functions would yield better performance, the hybrid method, ProQDockZ, was also included in the benchmark as a comparison. Indeed, the combined method further improved the correlation slightly from 0.49 for ProQDock to 0.50 for ProQDockZ (Fig. 1 and Table 2).

3.2 Benchmark on cross-validated data

The performances of ProQDock and ProQDockZ were compared with ZRANK and ZRANK2 on the CnM set by analyzing correlations (Table 2) as well as the ranking ability of each method and ROC curves (Fig. 2). Out of 131 targets, ProQDockZ, ProQDock, ZRANK2 and ZRANK could detect a correct (acceptable or better) model in 36, 33, 32 and 23 cases at the top rank, respectively, while, in 65, 61, 60 and 40 cases, at least one correct model was detected within top 10 ranks. Thus, the ranking ability are similar for ProQDock and ZRANK2, whereas the combined method ProQDockZ is slightly better than both methods (Fig. 2A). A more detailed analysis using ROC curves revealed that ProQDock (AUC = 0.87) in fact performed significantly better than both ZRANK (AUC = 0.71) and ZRANK2 (AUC = 0.75). By using a ProQDock score of 0.23 for correct predictions, ProQDock is able to find 80% of the correct models (TPR = 0.8 in Fig. 2B) at 20% FPR. The combined method, ProQDockZ, further enhanced the overall prediction ability (AUC = 0.88), finding slightly more true positives for all FPRs (Fig. 2B).

Both ProQDock and ProQDockZ correlate significantly better than ZRANK and ZRANK2 with the true quality measure DockQ (Table 2). ProQDockZ has a small but significantly better correlation than ProQDock. ZRANK has a better correlation than ZRANK2 despite the fact that ZRANK2 has been reported to have the better performance (Moal *et al.*, 2013). To explain the reason for this, correlations were calculated separately for the CAPRI and MOAL part of the CnM set (Table 2). This shows that ZRANK2 has a better correlation than ZRANK on MOAL but worse on CAPRI. This is because the CAPRI set contains docking models created using different methods, where many of the models have not been energy minimized and hence will contain more clashes, as opposed to the models in the MOAL set, where all models were energy

Table 2. Correlations with DockQ on different datasets

Methods	CnM <i>n</i> = 73 792	CAPRI <i>n</i> = 17 777	MOAL <i>n</i> = 56 015	BM5 <i>n</i> = 25 985
ProQDock	0.49 ± 0.01	0.55 ± 0.01	0.34 ± 0.01	0.37 ± 0.01
ProQDockZ	0.50 ± 0.01	0.57 ± 0.01	0.36 ± 0.01	0.38 ± 0.01
ZRANK	−0.31 ± 0.01	−0.39 ± 0.02	−0.21 ± 0.01	−0.22 ± 0.02
ZRANK2	−0.20 ± 0.01	−0.25 ± 0.02	−0.31 ± 0.01	−0.33 ± 0.01

Confidence intervals are at 99% level.

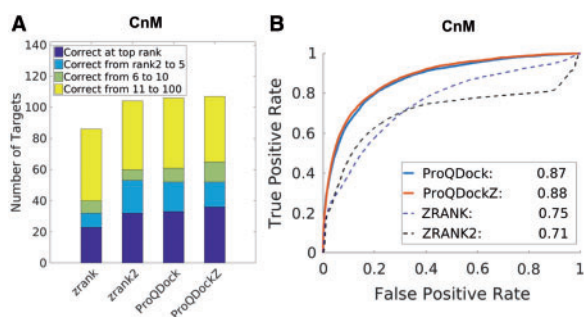


Fig. 2. CnM performance measured by (A) the ability to rank a model with quality acceptable or better among top 1, 5, 10 and 100 and (B) ROC curves; the AUC values are given in the legend

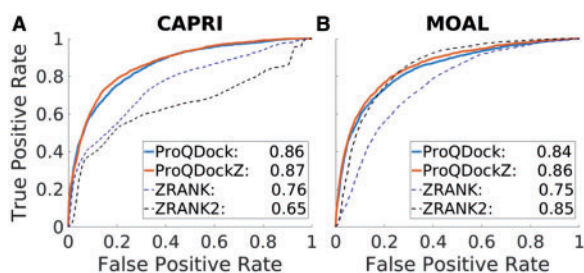


Fig. 3. ROC curves for the (A) CAPRI part and (B) MOAL part of the CnM set. AUC values in the legend

minimized using SwarmDock (Torchala *et al.*, 2013) (see Erep term for MOAL and CAPRI in Supplementary Figs S1 and S2). A major difference between ZRANK and ZRANK2 is that ZRANK2 has a harder repulsive term, which makes it more sensitive for models without clashes but obviously less sensitive on models with clashes. ROC curves for CAPRI and MOAL also illustrate this behavior (Fig. 3). ZRANK is better than ZRANK2 on CAPRI and vice versa on MOAL, while ProQDock performs much better than both on CAPRI; similar to ZRANK2 and much better than ZRANK on MOAL. Demonstrating that ProQDock can capture both coarse-grained and full-atom detail needed to perform well on both sets. As shown on the combined set, CnM, ProQDockZ is marginally better than both ProQDock and ZRANK2 on both subsets. The *P*-values corresponding to the difference in correlations (versus DockQ) between both ProQDock and ProQDockZ are <0.01 over both ZRANK and ZRANK2, suggesting that the correlations are significantly better at 99% confidence level implying definite improvement in performance (Table 2). This is true for both, the cross-validated (CnM) and the independent benchmark (BM5).

3.3 Performance on independent test set BM5

The performance of the different scoring functions was further tested on the independent dataset, BM5, consisting of 25 985 models from 55 targets. In ranking, ProQDock and ProQDockZ could detect a correct (acceptable or better) model in 8 and 8 targets at the top rank, respectively; while, ZRANK and ZRANK2 could detect 4 and 10 (Fig. 4A). Looking at the top 10 rank, ZRANK2 has a correct model for 16 targets, ZRANK has 17, ProQDock has 20 and ProQDockZ have 23. Thus, in terms of ranking, ProQDock is better than ZRANK and ZRANK2, and their (hybrid) combination, ProQDockZ, is slightly better than both. This is also reflected in the correlation values against DockQ where a slight increase was observed from ProQDock (0.37) to ProQDockZ (0.38), while both

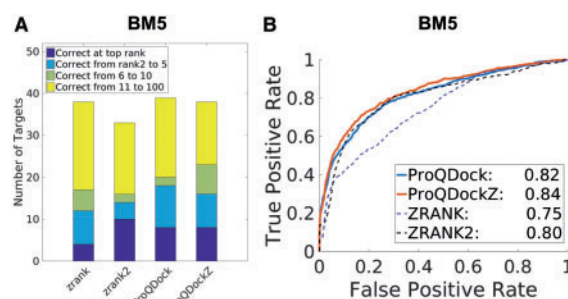


Fig. 4. BM5 performance measured by (A) the ability to rank a model with quality acceptable or better among top 1, 5, 10 and 100 and (B) ROC curves; the AUC values are given in the legend

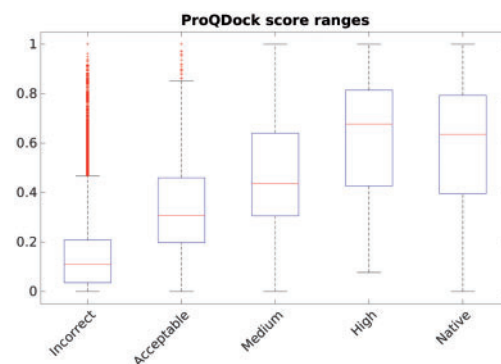


Fig. 5. ProQDock score for native structure and incorrect, acceptable, medium and high-quality models from the CnM set

ZRANK2 (−0.33) and ZRANK (−0.22) obtained lower correlations (Table 2). AUC values of the TPR versus FPR plots also follow the same overall trends, with gradual improvements observed from ZRANK (0.75), ZRANK2 (0.80) to ProQDock (0.82) and the hybrid method ProQDockZ (0.84). Thus, the cross-validated performance observed above is maintained on an independent benchmark set.

3.4 Test on native structure

Obviously, ProQDock was designed to predict the quality of protein docking models. However, it is also interesting to investigate how they perform on native structures, like a reality check. To this end, ProQDock was calculated for a set of high-resolution native structures in the database DB3 (see Section 2). Indeed, the ProQDock scores for native structures are much higher than the scores obtained for the docking models (with the exception of ‘High’ quality models) from CnM included as reference (Fig. 5). The median ProQDock for native structures is 0.64 compared with 0.11, 0.31, 0.44 and 0.68 for incorrect, acceptable, medium and high docking model quality, respectively. The high-quality docking models have scores similar to the score for native structures, which makes sense because high-quality models are close to the native structure.

3.5 Complementary of ProQDock and ZRANK2 in ranking correct models

To analyze what features were characteristic to the complementarity behavior of ProQDock and ZRANK2, which resulted in slight but still improved prediction ability of the combined method ProQDockZ, a statistical analysis of features for correct docking

models ranked high by ProQDock and not by ZRANK2 (set1) and vice versa (set2) was performed. The sets were constructed by considering the correct models in the MOAL set, up to the point (Fig. 3B) where ProQDock and ZRANK2 intersects corresponding to TPR of 70%, ensuring equal number top correct models before applying the criteria above. ZRANK2 has a fairly strict van der Waals repulsive term and will not be able to rank models with clashes, so the MOAL set was chosen over CnM, as these models have fewer clashes.

Statistics for individual features were calculated as mean and standard deviation of the mean (standard error) for three sets constructed above (Table 3) and feature distributions for correct and incorrect models were calculated (Supplementary Fig. S1). From the statistics, two groups of features can be distinguished based on the set of models selected by ProQDock and ZRANK2, one group (i) with features that are significantly different both in Table 3 as well as from the overall distributions of features of correct models (Supplementary Fig. S1), i.e. a feature has to be significantly different in Table 3 and significantly different from the mean of the overall distribution of correct models, and another group (ii) where features that are invariant.

The features for which ProQDock and ZRANK2 select models with significantly different ranges of values are ($\log_{10}(\text{Pval}) < -3$): nBSA, Fintres, EC, ProQ, Isc, CPM, Ld and CPscore (Table 3). In all cases, except for Ld, at least one of the values is also significantly different from the mean of distribution of correct models (Supplementary Fig. S1, *P* values not shown). Thus, features in group (i) are EC (0.26 for ProQDock versus 0.01 for ZRANK2), Isc (0.27 versus 0.52, raw unscaled energy term corresponding to -11.6 versus -8.0 in Rosetta Energy Units), CPscore (0.36 versus 0.22), Fintres (0.162 versus 0.239), nBSA (0.047 versus 0.060, note that the scale for nBSA goes from 0 to 0.1), CPM (0.79 versus 0.71) and ProQ2 (0.84 versus 0.80). A common trait to all features in this group (i) is that they all (with the exception of ProQ2) describe the protein–protein interface. nBSA and Fintres measures the relative size of the interface using buried surface area and contacts, respectively; EC describes the electrostatic complementarity of the interface, Isc is the interface energy term in Rosetta, CPscore is an SVM-based measure capturing the composition and contact preferences of different amino acid residues at the interface, and CPM is a composite function of EC, Sc and nBSA (see Section 2). Although, ZRANK2 includes the IFACE potential (which is similar to CPscore) that describe the interface, it is not nearly as detailed as the set of all features listed above. Furthermore, ZRANK2 does not contain an advanced electrostatic term like EC, modeled on fine-grid Poisson–Boltzman continuum electrostatics, which is advantageous over explicit electrostatic models for intrinsically providing equilibrium solutions (Li *et al.*, 2013). This is most likely the reason why many correct models are missed by ZRANK2. On the other hand, it is also possible that ProQDock focus too much on interface features and EC in particular, so it misses many of the correct models with low EC (Supplementary Fig. S1) that ZRANK2 is able to pick up. In fact, a large fraction (21%) of correct models have $\text{EC} < 0$, meaning that they have correlated surface electrostatic potentials (or in other words, unbalanced electric fields) at their interface most likely compensated by stronger constraints of shape complementarity. This is also true for native PPI models (from DB3) where a similar fraction ($\sim 20\%$) of interfaces had a negative EC, suggesting that EC has much more relaxed thresholds to satisfy compared with Sc (packing), which is a more well-established necessary condition for oligomer formation (Tsuchiya *et al.*, 2006).

The second group (ii) with features that are similar in values attained by models selected by both ProQDock and ZRANK2 (Table 3) are physico-chemical features: rGb, Sc, Erep, rTs, Etmr; all of

Table 3. Feature statistics for highly ranked correct models

Features	ProQDock (set1) 247 models 50 targets	ZRANK2 (set2) 240 models 39 targets	$\log_{10}(\text{Pval})$
rGb	0.031 (± 0.001)	0.031 (± 0.002)	−0.3
nBSA	0.047 (± 0.001)	0.060 (± 0.001)	−23.3
Fintres	0.162 (± 0.004)	0.239 (± 0.006)	−26.1
Sc	0.648 (± 0.004)	0.645 (± 0.004)	−0.5
EC	0.264 (± 0.014)	0.012 (± 0.016)	−28.8
ProQ2	0.836 (± 0.004)	0.799 (± 0.006)	−6.5
Isc	0.270 (± 0.019)	0.520 (± 0.016)	−21.4
rTs	0.469 (± 0.011)	0.459 (± 0.012)	−0.6
Erep	0.491 (± 0.007)	0.515 (± 0.004)	−2.6
Etmr	0.495 (± 0.009)	0.464 (± 0.011)	−1.9
CPM	0.787 (± 0.008)	0.705 (± 0.010)	−9.8
Ld	0.110 (± 0.003)	0.126 (± 0.002)	−4.7
CPscore	0.359 (± 0.018)	0.224 (± 0.009)	−10.4
DockQ	0.548 (± 0.013)	0.456 (± 0.010)	−8.1

Descriptive statistics, mean and standard errors of features for set1: correct models ranked by ProQDock and not by ZRANK2; set2: correct models ranked by ZRANK2 and not by ProQDock; from the MOAL set. *P*-values are calculated using *t*-test for the difference in mean between set1 and set2. Features in **bold** are the set of features for which ProQDock and ZRANK2 have significantly different values as defined in group (i) in the text.

which have their equivalent representative terms in ZRANK2: rGb is a solvation term, Sc is to some extent captured by the van der Waal's attractive term, Erep is the van der Waal's repulsive term, rTs is the total all-atom Rosetta energy (including Erep), Etmr is the rTs excluding the Erep term. Thus, it makes sense that they are not different between the correct models selected by ProQDock or ZRANK2. However, the fact that they are invariant (or stable) suggests that they provide a necessary but not sufficient condition for correct (native like) interaction between two proteins. Hence, they should be treated more as filters, which need to be satisfied. On the other hand, the discriminative (variable) features in group (i) measure specific structural attributes that differ between different sets of correct protein–protein docking models. Finally, it is noteworthy that the overall docking model quality, DockQ, is in fact also markedly better ($P < 10^{-8}$) for models selected only by ProQDock (0.548 ± 0.013) than those selected only by ZRANK2 (0.456 ± 0.010). This is consistent with the observed trends in the discriminative features in both sets.

3.6 A case study of contrasting interface properties by models ranked by ProQDock and ZRANK2

The complementary behavior of ProQDock and ZRANK2 in ranking correct models is further illustrated by two models with contrasting interface properties belonging to the two sets, the first is model *a7d* from target 1K4C, ranked by ProQDock and not by ZRANK2, and the second is model *a1b* from target 4CPA, ranked by ZRANK2 and not by ProQDock. Both models were ranked by the combined method ProQDockZ. The models have almost identical overall structural qualities with DockQ score of 0.59 and 0.55, respectively, medium quality according to CAPRI classification. However, they have vastly different values for several features, in particular at the interface. EC, for instance, is completely different (0.76 for ranked by ProQDock versus -0.69 for ranked by ZRANK2) illustrated by the electric fields induced by the different chains on the surfaces (Fig. 6). Also, the Rosetta interface score, Isc, is far better for the model ranked by ProQDock (-21.2 and -4.5 Rosetta Energy

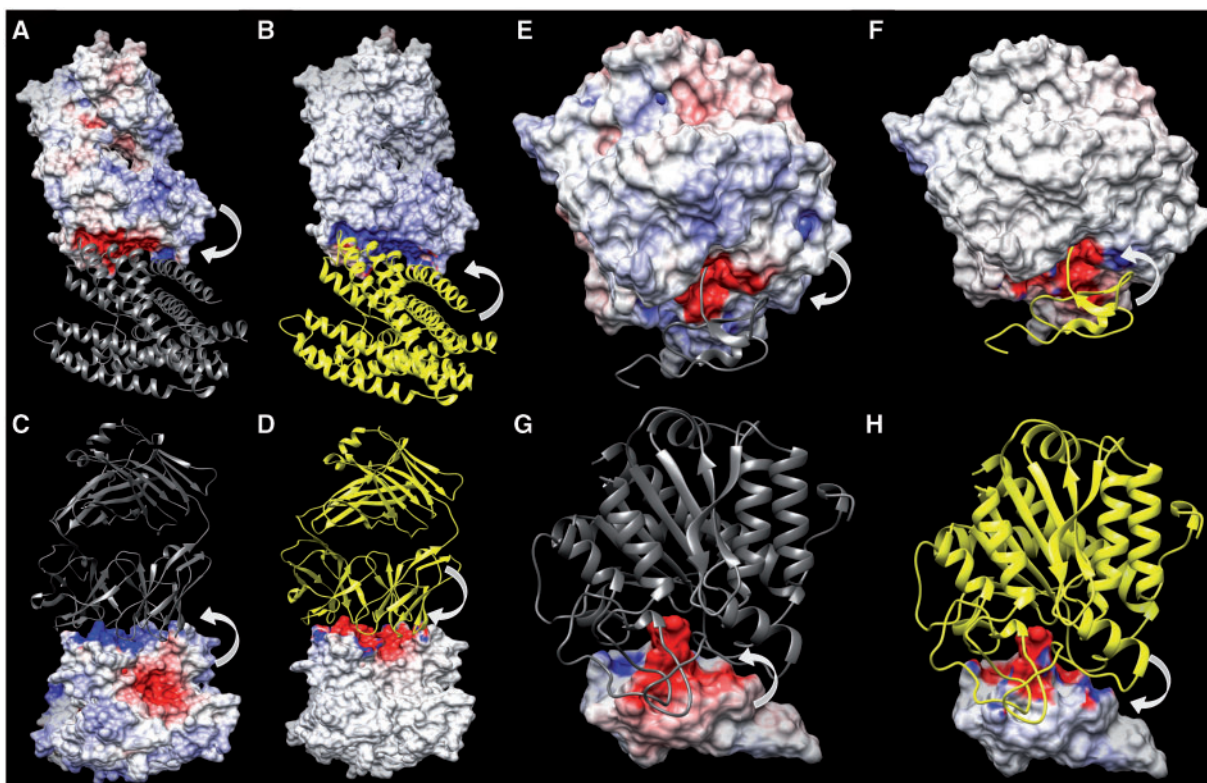


Fig. 6. Electrostatic Potentials (ESP) mapped onto the molecular interfaces of the model 1K4C-a7d ranked by ProQDock and not by ZRANK2 (A–D), and model 4CPA-a1b ranked by ZRANK2 and not by ProQDock (E–H). In each figure panel (A–H), only one of the two molecular interfaces have been displayed, colored according to its ESP, either owing to the charged atoms of the molecule itself or owing to the partner molecule, while the other partners have been drawn in ribbon. The arrows pointing from a molecule to the surface illustrate from which molecule the ESP is generated. Surface coloring follows deep blue for high positive (10 kT/e) to deep red for high negative (–10 kT/e) ESPs. Ribbons are colored in yellow if the corresponding atoms are charged and dark gray if uncharged (dummy). The high anti-correlated ESP reflected in their contrasting ESP surface coloring leads to a high EC value (0.76) at the interface (compare A-B and C-D). The high correlated ESP reflected in their similar ESP surface coloring leads to a high negative EC value (–0.69) at the interface (compare E-F and G-H). (A and E) ESP mapped onto the interface of the receptor chain, owing to its own charged atoms. (B and F) ESP on the interface of the receptor chain, owing to the charged atoms of the ligand. (C and G) ESP mapped onto the interface of the ligand chain, owing to its own charged atoms. (D and H) ESP on the interface of the ligand chain, owing to the charged atoms of the receptor

Units), which can partly but not fully be explained by the slightly larger interface (56 versus 42 residues) in the two models. In contrast, CPscore is better for the model ranked by ZRANK2 (0.32 versus 0.44) possibly because of the similarity with IFACE term in ZRANK2. Finally, Ld is much higher in the model ranked by ZRANK2 (0.10 versus 0.15) (Note, the Ld distribution is narrow, see [Supplementary Fig. S1](#)), revealing that the interface is more connected for the latter (ranked by ZRANK2). However, both models have good shape complementarity at the interface (0.68 in both cases), which, as discussed earlier, is a more necessary condition for inter-protein association, than the electrostatic balance at their interface.

This example highlights the difficulty in scoring protein docking models. At one end there are features that serve as critical filters for complex formation, like shape complementarity. On the other hand, there are variations with regard to features like EC, which probably describes the diverse plethora of biological interactions.

4 Conclusions

The aim of this study was to develop a method that could improve the detection of correct docking models in a set of many incorrect docking models. This was done by training SVMs to predict the quality of protein docking models as measured by DockQ using features that

can be calculated from the docking model itself. By combining different types of features describing both the protein–protein interface and the overall physical chemistry, it was possible to improve the correlation to DockQ from 0.25 for the best individual features to 0.49. The final version of ProQDock performed better than the state-of-the-art methods ZRANK and ZRANK2 in terms of correlations, ranking and finding correct models on independent test set. Finally, we also demonstrate that it is possible to combine ProQDock with ZRANK and ZRANK2 to improve the overall performance even further. In fact, based on the results described in Sections 3.5 and 3.6, the hybrid method, ProQDockZ should be considered as a better choice over both ProQDock and ZRANK to cover the diverse repertoire of plausible correct protein–protein docking models.

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