

# On the origin of internal rotation in ammonia borane

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Received: 6 December 2013 / Accepted: 24 April 2014 / Published online: 27 May 2014  
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**Abstract** The internal rotation in ammonia borane (AB) was studied on the basis of natural orbitals for chemical valence (NOCV) and eigenvectors for Pauli repulsion (NOPR). We found that the total hyperconjugation stabilization (ca. 5 kcal mol<sup>-1</sup>), based on the charge transfer from the occupied  $\sigma$  (B–H) orbitals into the empty  $\sigma^*$ (N–H), slightly favors the staggered conformation over the eclipsed one; however, the barrier to internal rotation in ammonia borane can be understood predominantly in a ‘classical’ way, as originating from the steric (Pauli) repulsion contributions (of the kinetic origin) that act solely between N–H and B–H bonds. Repulsion between the lone pair of ammonia and the adjacent B–H bonds was found to be dominant in absolute terms; however, it does not determine the rotational barrier. Similar conclusions on the role of CH $\leftrightarrow$ HC repulsion appeared to be valid for isoelectronic ethane.

**Keywords** Ammonia borane · Steric repulsion · Hyperconjugation

## Introduction

One of the most important goals of theoretical chemistry is to understand the origin of conformational changes in molecules [1, 2]. In order to achieve this goal many methods can be

applied to the description of electronic structures: molecular orbitals (MOs) [3, 4], localized molecular orbitals (LMOs) [5–7], bond orders [8–17], atoms in molecules (AIM) [18], Fermi hole [19], kinetic energy and information theory based quantities [20–22], and various charge and energy decomposition schemes [23–28]. A useful and elegant approach suitable for description of energy profiles of chemical reactions was proposed by Torro-Labbe and coworkers [29] based on the reaction force concept. Bickelhaupt and Zeist [30] proposed the ‘activation strain model’, which also appears to be very useful in the analysis of chemical reactions.

Rotation around a single carbon–carbon bond is one of the most important conformational transitions in organic chemistry [31, 32]. A typical example is ethane, which exhibits staggered and eclipsed conformations; the former minimum energy structure is more stable than the transition state eclipsed structure by  $\sim 3.0$  kcal mol<sup>-1</sup> [33]. The classical and intuitive explanation of the barrier suggested in organic textbooks is based on the steric repulsion between C–H bonds, which is dominant in the eclipsed structure [34]. An alternative explanation is based on hyperconjugation stabilization, which is stronger in the staggered conformation [35–38]. However, as pointed out by Mulliken [35], hyperconjugation effect should have only a minor influence on the barrier. Bader et al. [39] stated that the barrier to rotation in ethane can be related to the polarization of charge density along the carbon–carbon bond. Goodman and coworkers [40] have shown, based on the natural bond orbitals (NBO) method, that ethane’s staggered conformation is the result of hyperconjugation. This point of view was also presented by Weinhold [41]. Goodman’s results based on the NBO method have been challenged by the work of Bickelhaupt and Baerends [42] based on the model of a chemical bond originating from fragmented molecular orbitals; according to these results the internal rotational barrier in ethane is due to Pauli repulsion acting

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This paper belongs to Topical Collection MIB 2013 (Modeling Interactions in Biomolecules VI)

**Electronic supplementary material** The online version of this article (doi:10.1007/s00894-014-2272-y) contains supplementary material, which is available to authorized users.

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between the CH bonds of opposite CH<sub>3</sub> units. Subsequent calculations by Mo and coworkers [44, 45] and then by Pendas et al. [43], confirmed the classical, steric-based interpretation of the barrier; in addition, the former authors have shown that hyperconjugation stabilizes the staggered conformer only by about 4 kJ mol<sup>-1</sup> relative to the eclipsed form [45]. A very elegant recent paper by Mo and Gao [46] provided a compact overview of the most important studies on this subject; the main conclusion is that the internal rotational barrier in ethane is due predominantly to steric effects acting between C–H bonds, with minor participation stemming from hyperconjugation.

We have recently developed the ETS-NOCV scheme [47–50] by combining the extended transition state (ETS) [25, 26] energy decomposition approach with the natural orbitals for chemical valence (NOCV) method [51–57]. ETS-NOCV has proved suitable for qualitative and quantitative description of the crucial components ( $\sigma$ ,  $\pi$ ,  $\delta$ , etc.) that constitute various types of chemical bonds [58–61]. In addition, the energy profiles of some chemical reactions can be also characterized [62, 63]. More importantly for this study, it was shown that NOCV representation allows for qualitative and quantitative description of hyperconjugation effects [47, 48]. Furthermore, the ETS energy decomposition scheme provides quantitative information on the Pauli repulsion effects [2, 25, 26].

Therefore, the main goal of this article was to apply for the first time the ETS-NOCV charge and energy decomposition scheme to analysis of the internal rotation in ammonia borane. Hyperconjugation and steric factors will be discussed in a detailed way. It should be noted that ammonia borane is considered nowadays as one of the most promising hydrogen storage materials. In addition, it was already proven that ammonia borane exhibits dissimilar features as compared to isoelectronic ethane [64]. Furthermore, the present study sheds additional qualitative and quantitative light on the steric repulsion in ammonia borane by decomposition of total Pauli repulsion into specific contributions stemming from different symmetry ( $\sigma$  and  $\pi$ ). In order to achieve this goal, we defined for the first time the eigenvectors for Pauli repulsion; in this representation, one can thus discuss the Pauli repulsion components originating from different symmetries. For comparison, similar analyses will be performed for ethane.

#### Computational details

All DFT calculations presented here were based on the Amsterdam Density Functional (ADF 2009.01) program [2, 65–68] in which the ETS-NOCV scheme was implemented [47–63]. The Becke-Perdew exchange-correlation functional

[69, 70] was applied (BP86). A standard triple-zeta STO basis containing two sets of polarization functions (TZ2P) was adopted for all atoms. The contours of deformation densities were plotted based on ADF-GUI interface [71].

#### Computational methods

Our analysis is based on the ETS-NOCV approach, which is a combination of the extended transition state (ETS) [25, 26] method with the natural orbitals for chemical valence (NOCV) scheme [51–57].

The basic concept of the ETS scheme involves partitioning of the total bonding energy  $\Delta E_{\text{total}}$  between interacting fragments into four components:

$$\Delta E_{\text{total}} = \Delta E_{\text{dist}} + \Delta E_{\text{elstat}} + \Delta E_{\text{Pauli}} + \Delta E_{\text{orb}} \quad (1)$$

The first component,  $\Delta E_{\text{dist}}$ , referred to as the distortion term, represents the amount of energy required to promote the separated fragments from their equilibrium geometry to the structure they will take up in the combined molecule; it can also be seen as strain energy. The second term,  $\Delta E_{\text{elstat}}$ , corresponds to the classical electrostatic interaction between the promoted fragments as they are brought to their positions in the final complex. The third term,  $\Delta E_{\text{Pauli}}$ , accounts for the repulsive Pauli interaction between occupied orbitals on the two fragments in the combined molecule. It is calculated as the difference between the energies of orthogonalized and non-orthogonalized fragments [2, 25]. Finally, the last stabilizing term,  $\Delta E_{\text{orb}}$ , represents the interactions between the occupied molecular orbitals of one fragment with the unoccupied molecular orbitals of the other fragment as well as the mixing of occupied and virtual orbitals within the same fragment (inner-fragment polarization). This energy term,  $\Delta E_{\text{orb}}$ , may be linked to the electronic bonding effect coming from the formation of a chemical bond (Eq. 2).

The NOCV are eigenvectors that diagonalize deformation density matrix  $\Delta P^{\text{orb}} = P_{\text{molecule}} - P_0$ , where  $P_0$  corresponds to the sum of density matrices for orthogonalized fragments; it has been shown that the natural orbitals for chemical valence pairs ( $\psi_{-k}, \psi_k$ ) decompose the deformation density  $\Delta \rho_{\text{orb}}$  into NOCV-contributions,  $\Delta \rho_{\text{orb}}^k$ :

$$\Delta \rho_{\text{orb}}(r) = \sum_{k=1}^{M/2} \nu_k \left[ -\psi_{-k}^2(r) + \psi_k^2(r) \right] = \sum_{k=1}^{M/2} \Delta \rho_{\text{orb}}^k \quad (1)$$

where  $\nu_k$  and  $M$  are the NOCV eigenvalues and the number of basis functions, respectively. Visual inspection of deformation density plots ( $\Delta \rho_{\text{orb}}^k$ ) helps to attribute symmetry and the direction of the charge flow. In addition, information gained from the analysis of deformation density plots can be enriched by providing the

energetic estimations,  $\Delta E_{\text{orb}}^k$ , for each  $\Delta \rho_{\text{orb}}^k$  within ETS-NOCV scheme:

$$\Delta E_{\text{orb}} = \sum_k \Delta E_{\text{orb}}^k = \sum_{k=1}^{M/2} v_k \left[ -F_{-k,-k}^{\text{TS}} + F_{k,k}^{\text{TS}} \right] \quad (2)$$

where  $F_{i,i}^{\text{TS}}$  are diagonal Kohn-Sham matrix elements defined over NOCV with respect to the transition state density (at the midpoint between density of the molecule and the sum of fragment densities). The above components  $\Delta E_{\text{orb}}^k$  provide the energetic estimation of  $\Delta \rho_{\text{orb}}^k$  that may be related to the importance of a particular electron flow channel for the bonding between the considered molecular fragments.

In the present study, in analogy to NOCVs, we defined for the first time the natural orbitals (eigenvectors) for Pauli repulsion,  $\phi_k$ , that diagonalize the Pauli deformation density matrix,  $\Delta \rho^{\text{Pauli}} = \text{P}0 - \text{P}_{\text{isolated}}$ , where  $\text{P}_{\text{isolated}}$  is the sum of density matrices for non-orthogonalized fragments, whereas  $\text{P}0$  correspond to the sum of density matrices for orthogonalized fragments. Such eigenvectors decompose the total Pauli deformation density,  $\Delta \rho^{\text{Pauli}} = \rho 0$  (orthogonalized-fragments)  $- \rho$  (non-orthogonalized-fragments), into the NOCV-like contributions ( $\Delta \rho_k^{\text{Pauli}}$ ) (in analogy to Eq. 1):

$$\Delta \rho^{\text{Pauli}}(r) = \sum_{k=1}^{N/2} v_k^{\text{Pauli}} \left[ -\phi_{-k}^2(r) + \phi_k^2(r) \right] = \sum_{k=1}^{N/2} \Delta \rho_k^{\text{Pauli}}(r) \quad (3)$$

The total charge transferred in this channel can be considered as:

$$\Delta q_k^{\text{Pauli}} = v_k^{\text{Pauli}} \quad (4)$$

The present study characterized not only the total values of Pauli repulsion ( $\Delta E_{\text{Pauli}}$ ) in ammonia borane based on the original ETS scheme (Eq. 1) but, in addition, provided a more detailed picture by analyses of both the Pauli repulsion contributions  $\Delta \rho_k^{\text{Pauli}}$  (Eq. 3) and the corresponding quantitative charge estimations  $\Delta q_k^{\text{Pauli}}$  (Eq. 4). This approach (Eqs. 3, 4) was implemented by one of us in the home version of ADF2009.01. At present, the energetic Pauli repulsion contributions ( $\Delta E_{\text{Pauli}}^k$ ) from  $\Delta \rho_k^{\text{Pauli}}$  (calculated in an analogous way to Eq. 2) are unavailable. Hence, we focused our attention on the quantitative measures of  $\Delta \rho_k^{\text{Pauli}}$  based on Eq. 4. Red areas of deformation density channels correspond to charge depletion, whereas blue indicates charge accumulation upon bond formation.

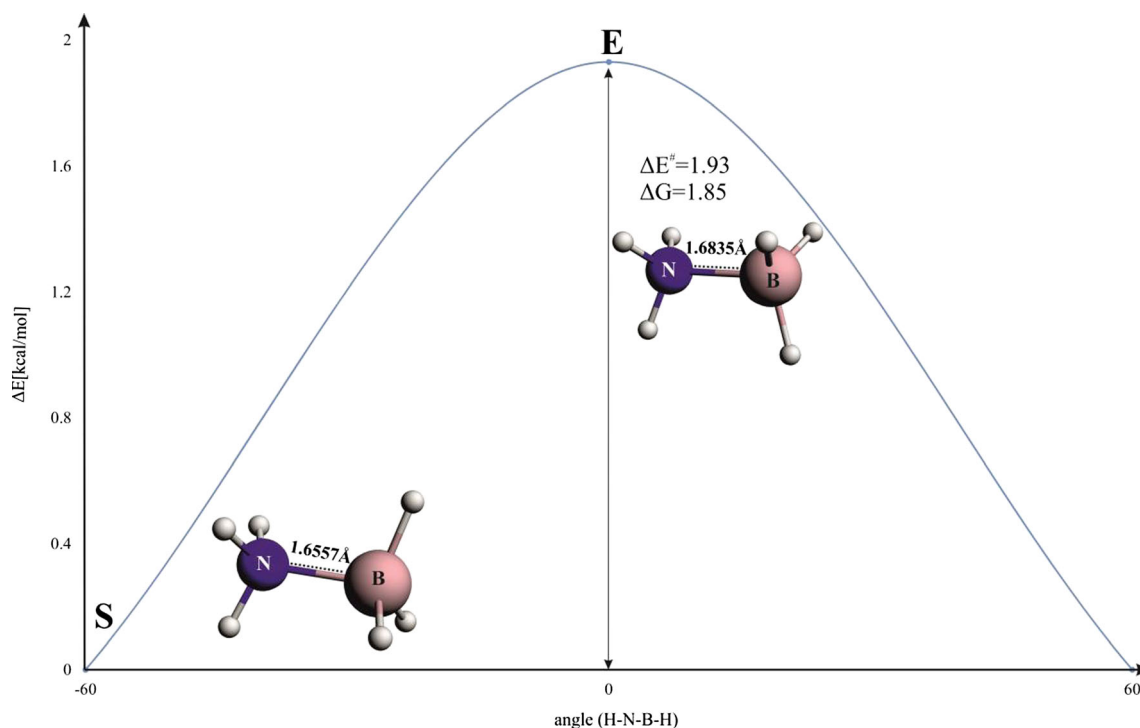
Due to the fact that the steric interaction, which is a non-observable quantity [72], is very often attributed in the literature to Pauli repulsion quantum effect [2, 43, 46], we use both terms interchangeably throughout the text. Finally, we should note that Pauli repulsion is one of the bonding components in various energy decomposition schemes; hence, we believe

that a more detailed description of this term based on Eqs. 3, 4, could be of wide interest. It is very important to point out that the main source of the Pauli repulsion is related to an increase in the kinetic energy contribution; so we could also refer to the Pauli repulsion term as kinetic repulsion due to the Pauli exclusion principle [2]. Such a concept, which relates the steric repulsion to the 'kinetic energy pressure' has already been put forward by various authors [73, 74]. In addition, the Pauli repulsion contribution appears to qualitatively correlate very well with the experimental Taft's steric parameters [75].

## Results and discussion

We will start with a brief description of the bonding situation in the most stable staggered conformation (S) of ammonia borane (Fig. 1). It can be seen from Table 1 that the bond dissociation energy ( $-\Delta E_{\text{total}}$ ) amounts to 31.94 kcal mol<sup>-1</sup> (BP86/TZ2P). This value fits well to the experimental enthalpy estimated by Haaland (31.1 ± 1 kcal mol<sup>-1</sup> [76, 77]) as well as to other theoretical estimations [48, 78–81]. In line with previous studies [48, 78, 82–85], we found a slight dominance (by ~0.7 kcal mol<sup>-1</sup>) of the electrostatic stabilization over the orbital interaction term (Table 1). Decomposition of the latter stabilizing term into NOCV-based deformation density channels leads to the conclusion that donation ( $\Delta \rho_{\text{orb}}^{\sigma}$ ) from the lone electron pair of ammonia to the lowest unoccupied orbital of BH<sub>3</sub> is by far most dominant ( $\Delta E_{\text{orb}}^{\sigma} = -66.32$  kcal mol<sup>-1</sup>) as compared to the two hyperconjugation contributions,  $\Delta \rho_{\text{orb}}^{\text{hyp}1}$ ,  $\Delta \rho_{\text{orb}}^{\text{hyp}2}$ ; the corresponding orbital interaction stabilizations are  $\Delta E_{\text{orb}}^{\text{hyp}1} = \Delta E_{\text{orb}}^{\text{hyp}2} = -2.30$  kcal mol<sup>-1</sup> (Fig. 2). The latter two degenerated contributions stem from charge transfer from the occupied  $\sigma$  (B–H) orbitals into the empty  $\sigma^*$ (N–H) (Fig. 2). It is noteworthy that, in the isoelectronic ethane, the sum of stabilization arising from the two orthogonal hyperconjugation components was found to be significantly stronger (~10 kcal mol<sup>-1</sup>) [46, 85].

It is clear from Fig. 1 that rotation from the staggered to the eclipsed form leads to a change in energy, by 1.93 kcal mol<sup>-1</sup>. This barrier agrees quite well with the experimental value of 2.07 kcal mol<sup>-1</sup> determined based on microwave spectra [86], and with other high level computations [87]. It is very important to point out that when going from the staggered (S) to the eclipsed isomer (E), one observes a notable stretch of the B–N bond, by ~0.03 Å. Such elongation leads expectedly to a significant decrease in Pauli repulsion, by 7.27 kcal mol<sup>-1</sup>; at the same time the electrostatic ( $\Delta E_{\text{elstat}}$ ) and orbital interaction ( $\Delta E_{\text{orb}}$ ) contributions become less stabilizing, by 4.14 kcal mol<sup>-1</sup> and 4.69 kcal mol<sup>-1</sup>, respectively (see Table 1 and the blue line in Fig. 3). From the examples of ethane [42] or biphenyl [88], it is known that this type of elongation when going from one isomer to the other is due to the steric (Pauli)



**Fig. 1** Energy profile for internal rotation in ammonia borane. B–N bond lengths (in Å) are indicated

repulsion. As indicated in a series of recent works [42–46, 88, 89], in order to estimate and characterize the forces leading to such elongation, one must first consider rigid rotation from the staggered to the eclipsed conformation; we have labeled such eclipsed conformation (in the staggered geometry) as  $E_s^{\text{geom}}$ . We can clearly see now from Table 1 and Fig. 3 (the orange curve), that an increase in the Pauli repulsion contribution, by  $2.11 \text{ kcal mol}^{-1}$ , is noted when going from  $S$  to  $E_s^{\text{geom}}$ ; it is important to note that the remaining bonding components are practically unchanged. A similar trend, i.e., the maximum Pauli repulsion in ammonia borane with the dihedral angle

$\angle(\text{H-B-N-H}) = 0.0$ , is noted when considering the rigid rotation from the geometry of the eclipsed structure to the staggered one ( $S_e^{\text{geom}}$ ) (gray curve in Fig. 3). Thus, the Pauli (steric) repulsion contribution is responsible for stretching of the B–N bond and, accordingly, for the rotational barrier in ammonia borane; the analogous situation holds true for the ethane molecule, as demonstrated first by Bickelhaupt et al. [42] and then by others [43–46]. An increased kinetic repulsion (the main source of the Pauli term) in the  $E_s^{\text{geom}}$  geometry is related through the virial theorem to the existence of repulsive forces acting predominantly on nitrogen and boron nuclei

**Table 1** Extended transition state (ETS)<sup>a,b</sup> energy decomposition results describing the  $\text{H}_3\text{N-BH}_3$  bond in various isomers of ammonia borane. Charge estimates for Pauli repulsion contributions are indicated<sup>c</sup>

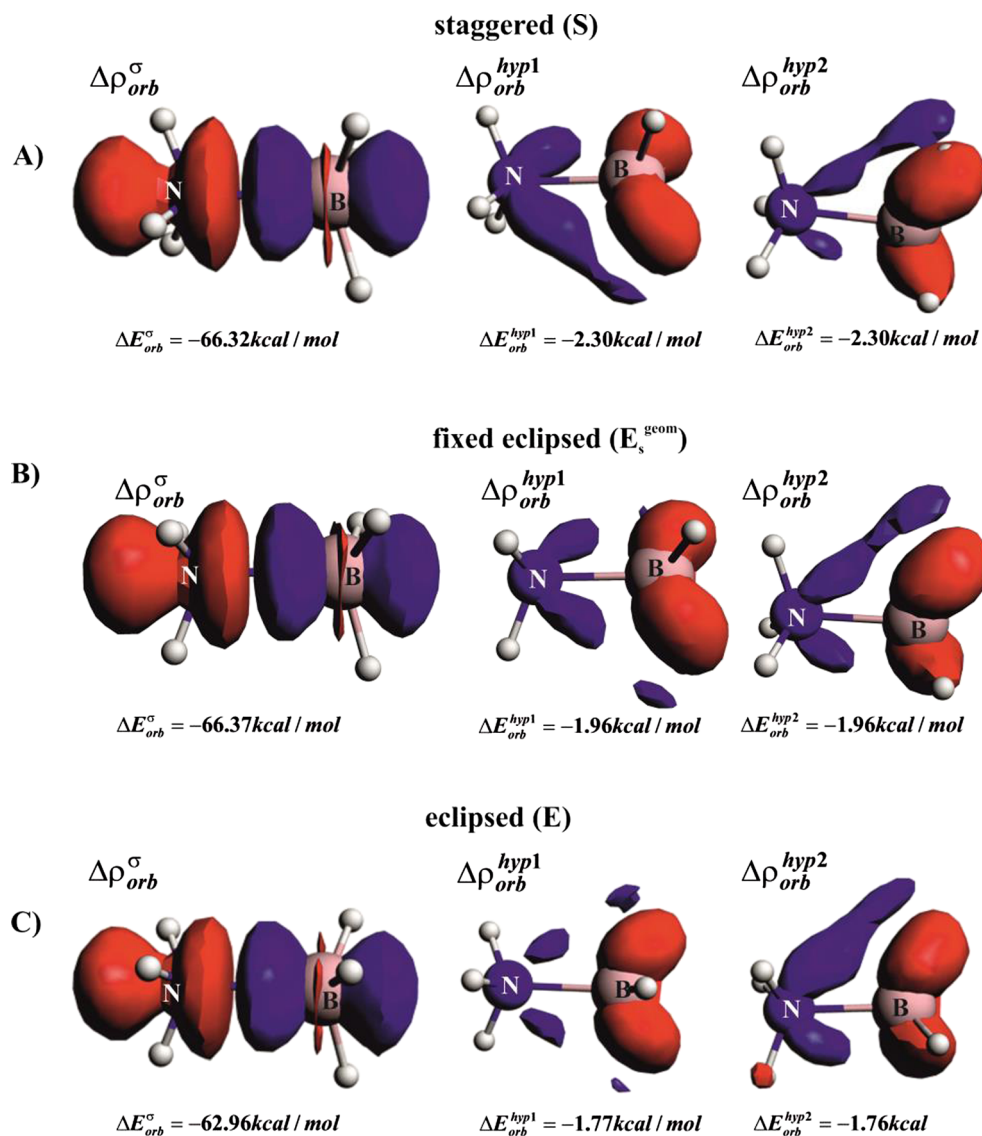
	<i>S</i>	<i>E</i>	<i>E-S</i>	$E_s^{\text{geom}}$
$\Delta E_{\text{total}}$	-31.94	-30.01	1.93	-29.87
$\Delta E_{\text{dist}}$	12.65	13.02	0.37	12.65
$\Delta E_{\text{elstat}}$	-77.32	-73.18	4.14	-77.8
$\Delta E_{\text{Pauli}}$	109.39	102.12	-7.27	111.5
$\Delta E_{\text{orb}}$	-76.66	-71.97	4.69	-76.22
$\Delta Q_{\text{global}}^{\text{Pauli}} (\Delta q_1^{\text{Pauli}} + \Delta q_2^{\text{Pauli}} + \Delta q_3^{\text{Pauli}})$	1.1833	1.1693	-0.014	1.2135
$\Delta q_1^{\text{Pauli}}$	0.7261	0.7049	-0.0212	0.7267
$\Delta q_2^{\text{Pauli}}$	0.2286	0.2325	0.0039	0.2434
$\Delta q_3^{\text{Pauli}}$	0.2286	0.2319	0.0033	0.2434

<sup>a</sup>  $\Delta E_{\text{total}} = \Delta E_{\text{orb}} + \Delta E_{\text{Pauli}} + \Delta E_{\text{elstat}} + \Delta E_{\text{dist}}$  [kcal mol<sup>-1</sup>]

<sup>b</sup> Labels assigned in Fig. 1;  $E_s^{\text{geom}}$  corresponds to the eclipsed structure in the staggered geometry

<sup>c</sup> See Eqs. 3, 4 in Computational Methods and Fig. 5

**Fig. 2** Dominant natural orbitals for chemical valence (NOCV)-based deformation density channels,  $\Delta\rho_{orb}^{\sigma}$ ,  $\Delta\rho_{orb}^{hyp1}$ ,  $\Delta\rho_{orb}^{hyp2}$ , with the corresponding orbital interaction energies for the alternative isomers of ammonia borane. The contour value is  $|\Delta\rho| = 0.005$  a.u. for  $\Delta\rho_{orb}^{\sigma}$ , whereas for remaining hyperconjugation contributions 0.001 a.u. was applied. Blue/red contours correspond to accumulation/depletion of electron density. *S* Fully optimized staggered isomer,  $E_s^{geom}$  eclipsed structure in the staggered geometry, *E* fully optimized eclipsed isomer

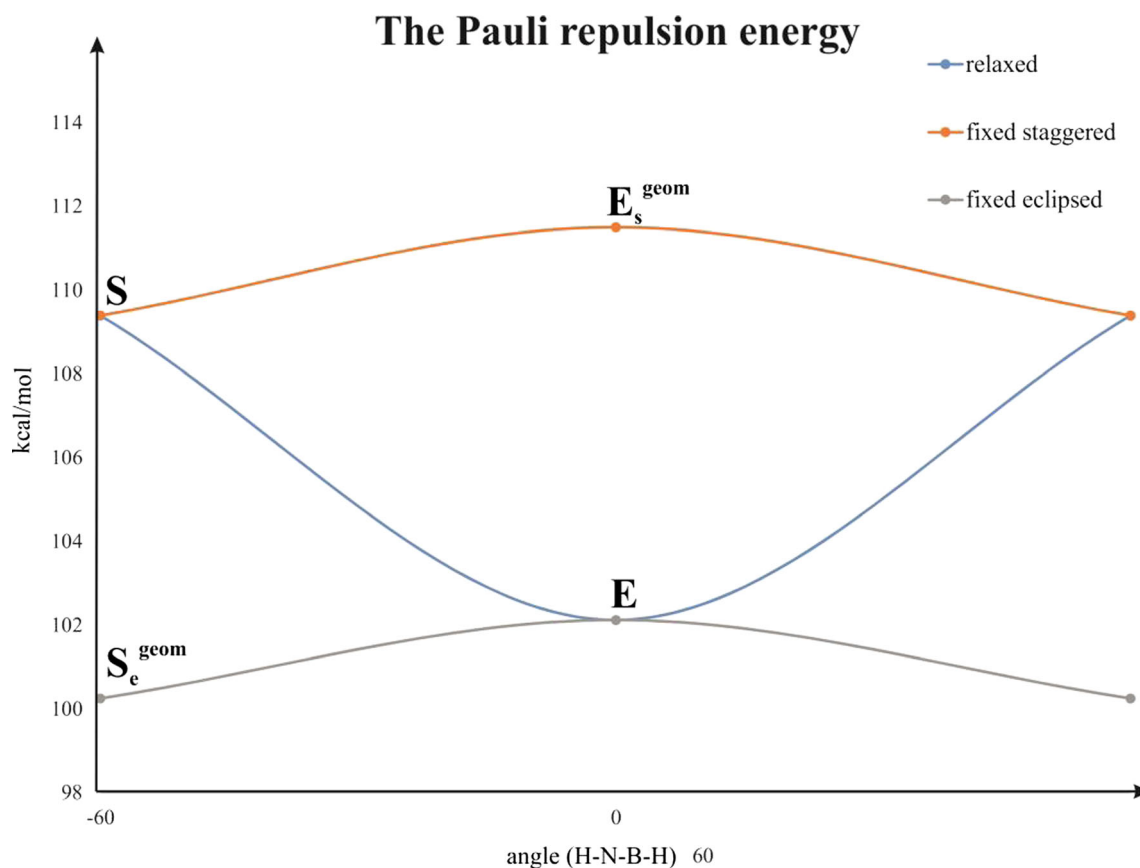


[18]. It must be added that hyperconjugation stabilizations stemming from the charge transfer from the occupied  $\sigma$  (B–H) orbitals into the empty  $\sigma^*$ (N–H) ( $\Delta\rho_{orb}^{hyp1}$ ,  $\Delta\rho_{orb}^{hyp2}$ ), favors the staggered conformation (Fig. 2), although the effect is minor ( $\sim 0.4 \text{ kcal mol}^{-1}$ ) compared to changes in the remaining bonding contributions (Table 1). A quantitatively similar effect is observed for the change in the energy distortion contribution ( $\Delta E_{dist}$ ) (Table 1).

Let us now focus our attention on detailed changes in the Pauli repulsion contributions in the three ammonia borane isomers, *S*,  $E_s^{geom}$  and *E*. Figure 4 presents the total Pauli deformation density contours ( $\Delta\rho^{Pauli}$ ) together with the corresponding energy values ( $\Delta E_{Pauli}$ ).

As already stated, the  $S \rightarrow E_s^{geom}$  transition leads to a jump in the Pauli term that it is then ‘relieved’ by elongation of the B–N bond in step  $E_s^{geom} \rightarrow E$ . The important question that arises at this point is how the total Pauli repulsion is

‘distributed’ between  $\text{NH}_3$  and  $\text{BH}_3$  fragments. An analysis of function  $\Delta\rho^{Pauli}$  leads to the observation that electrons are removed from the N–B binding region (in fact, it is a manifestation of the Pauli exclusion principle [2, 90]); although one can see that the red lobes extend also to the areas of  $\text{NH} \leftrightarrow \text{HB}$  interaction. However, such contours do not allow us to extract information on whether the total changes in Pauli repulsion are determined by the repulsive interaction between the lone electron pair of ammonia with the occupied  $\sigma$  (B–H) orbitals or directly by ‘classical’ N–H  $\leftrightarrow$  H–B repulsion [an interaction between the occupied  $\sigma$  (B–H) orbitals with the occupied  $\sigma$  (N–H)]. In order to obtain such separated information, we have decomposed total Pauli repulsion  $\Delta\rho^{Pauli}$  into the contributions ( $\Delta\rho_k^{Pauli}$ ) according to Eq. 3. The three leading Pauli deformation density channels,  $\Delta\rho_1^{Pauli}$ ,  $\Delta\rho_2^{Pauli}$ ,  $\Delta\rho_3^{Pauli}$ , together with the corresponding quantitative charge estimations (Eq. 4) are presented in Fig. 5. It should be noted that the total



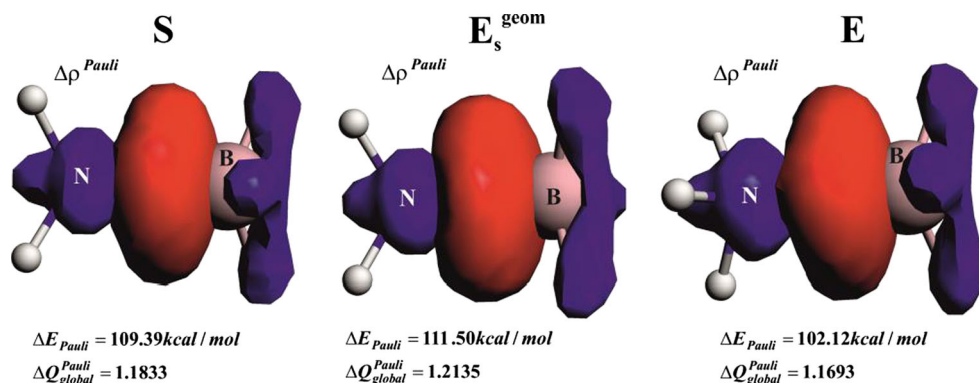
**Fig. 3** Pauli repulsion energies in the alternative isomers of ammonia borane. *Blue* Fully relaxed structures; *orange* staggered geometry; *gray* eclipsed geometry. *S* Fully optimized staggered isomer,  $E_s^{\text{geom}}$  eclipsed

structure in the staggered geometry,  $S_e^{\text{geom}}$  staggered structure in the eclipsed geometry, *E* fully optimized eclipsed isomer

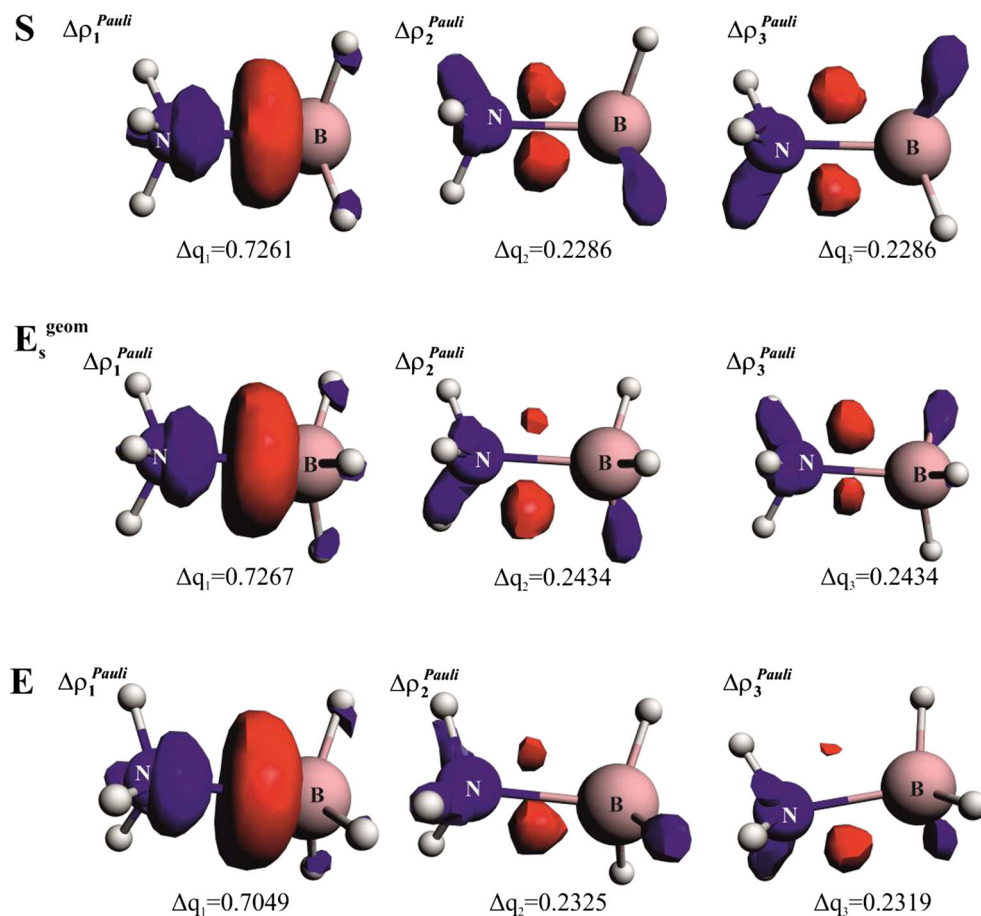
charge,  $\Delta Q_{\text{global}}^{\text{Pauli}} = \Delta q_1^{\text{Pauli}} + \Delta q_2^{\text{Pauli}} + \Delta q_3^{\text{Pauli}}$ , that is removed from the  $\text{H}_3\text{N}-\text{BH}_3$  binding region correlates well with the trend based on the Pauli repulsion energy (Table 1, Fig. 4). Qualitative inspection of the contours  $\Delta \rho_i^{\text{Pauli}}$  leads to the important observation that the first channel ( $\Delta \rho_1^{\text{Pauli}}$ ) corresponds solely to the interaction between the lone electron pair of ammonia with the B-H bonds, whereas the two latter orthogonal contributions ( $\Delta \rho_2^{\text{Pauli}}, \Delta \rho_3^{\text{Pauli}}$ ) show  $\text{NH} \leftrightarrow \text{HB}$  repulsion (Fig. 5). More importantly, quantitative analysis of the charge depletion, based on the eigenvalues (Eq. 3), leads to

the conclusion that, when going from  $S \rightarrow E_s^{\text{geom}}$ , the major changes (by 0.0148 a.u.) are within the second and third values of  $\Delta q_2^{\text{Pauli}}, \Delta q_3^{\text{Pauli}}$ . The repulsion  $\Delta \rho_1^{\text{Pauli}}$  characterized by  $\Delta q_1^{\text{Pauli}}$  remains unchanged. Once going to the relaxed eclipsed structure, the Pauli contribution is further 'relieved' ( $\Delta \rho_i^{\text{Pauli}}$  values decrease in line with  $\Delta E_{\text{Pauli}}$ ). These results show that an increase in the total repulsion in the eclipsed conformation compared to staggered ( $S \rightarrow E_s^{\text{geom}}$ ) is determined solely by the  $\text{NH} \leftrightarrow \text{HB}$  repulsion (of the kinetic origin) due to the Pauli exclusion principle (an interaction between

**Fig. 4** Contours of the total Pauli deformation density together with the corresponding energies. In addition, charge-based estimations are presented based on Eq. 4. The *blue/red* contours correspond to accumulation/depletion of electron density due to the Pauli exclusion principle



**Fig. 5** Dominant Pauli repulsion deformation density channels,  $\Delta\rho_1^{\text{Pauli}}$ ,  $\Delta\rho_2^{\text{Pauli}}$ ,  $\Delta\rho_3^{\text{Pauli}}$ , together with the corresponding charge estimations,  $\Delta q_1^{\text{Pauli}}$ ,  $\Delta q_2^{\text{Pauli}}$ ,  $\Delta q_3^{\text{Pauli}}$  in the selected ammonia borane conformations. The blue/red contours correspond to accumulation/depletion of electron density. *S* Fully optimized staggered isomer,  $E_s^{\text{geom}}$  eclipsed structure in the staggered geometry, *E* fully optimized eclipsed isomer



the electrons with the same spin as within the B–H and N–H bonds). The repulsive contribution from the interaction between the lone electron pair of ammonia with the electrons of B–H bonds ( $\Delta\rho_1^{\text{Pauli}}$ ) is dominating in absolute terms; however, it does not influence the barrier. These results confirm the ‘classical’ view that the internal rotational barrier in ammonia borane can be understood solely in terms of NH $\leftrightarrow$ HB steric (Pauli) effects, with minor participation stemming from the hyperconjugation (Fig. 2) and geometry distortion term. It must be further noted that we performed a detailed study of the changes in  $\Delta q_i^{\text{Pauli}}$  values (based on various sets of molecules) and have found that differences in the second decimal place are quantitatively meaningful.

Finally, we performed similar ETS-NOCV and Pauli repulsion analyses for ethane and found that CH $\leftrightarrow$ HC Pauli (kinetic) repulsion channels are responsible for the rotation of methyl groups (see [Supplementary electronic material](#)); this is in line with the conclusions reached first by Bickelhaupt and subsequently by other researchers [42–46]. It is important at this point to cite another important work in the field explaining the origin of rotation in ethane. It is possible to decompose the barrier into changes in the kinetic ( $\Delta T$ ) and potential energy contributions: nuclei–nuclei ( $\Delta V_{\text{nn}}$ ), nuclei–electrons ( $\Delta V_{\text{ne}}$ ) and electrons–electrons ( $\Delta V_{\text{ee}}$ ), as done by Bader

and others for ethane [18]. Such an approach, while very physical and compelling, does not allow, for example, separate discussion of the role of the hyperconjugation effect, which is well rooted in chemistry. It was shown that rigid rotation  $S \rightarrow E_s^{\text{geom}}$  leads to a rise in all of the destabilizing terms ( $\Delta T \sim +9 \text{ kcal mol}^{-1}$ ,  $\Delta V_{\text{nn}} + \Delta V_{\text{ee}} \sim +16 \text{ kcal mol}^{-1}$ ), whereas the electron–nuclei stabilization is  $\Delta V_{\text{ne}} \sim -22 \text{ kcal mol}^{-1}$ . (Fig. 6.11 in [18]). At this non-equilibrium geometry, the rise in kinetic energy is related, through the virial theorem, to the repulsion force acting on the nuclei. Accordingly, in the next step,  $E_s^{\text{geom}} \rightarrow E$ , the CC bond elongates, which leads to weakening of the attraction ( $\Delta V_{\text{ne}} \sim +207 \text{ kcal mol}^{-1}$ ) and decrease in the repulsion ( $\Delta V_{\text{nn}} + \Delta V_{\text{ee}} \sim -201 \text{ kcal mol}^{-1}$ ;  $\Delta T \sim -3 \text{ kcal mol}^{-1}$ , the values are provided with respect to ethane in staggered geometry). One should also note that various authors have combined the above contributions in different ways [31]. Finally, Liu and Govind [91], defined in an elegant way at DFT level, the steric contribution (equal to the kinetic Weizsäcker term) from a difference between the total electronic energy and the sum of electrostatic ( $\Delta V_{\text{ne}} + \Delta V_{\text{ee}} + \Delta V_{\text{nn}}$ ) and quantum energy terms  $\Delta E_{\text{q}}$  (comprising the sum  $\Delta E_{\text{xc}} + \Delta E_{\text{Pauli}}$ ); the change in the kinetic term due to the Pauli exclusion principle is incorporated in  $\Delta E_{\text{Pauli}}$ . It was shown that rigid rotation  $S \rightarrow E_s^{\text{geom}}$  results in

the appearance of destabilizing forces originating from the fermionic quantum contribution  $\Delta E_q$ ; closer inspection of the author's data shows that this change is due entirely to a rise in the kinetic energy term [91]. Finally, one should cite the separate work of Nagy [92], who discussed the Fisher information based on the kinetic term; the role of kinetic energy and the information origin of the chemical bonding have been studied by Nalewajski [22].

### Concluding remarks

The present work studied for the first time the internal rotation in ammonia borane based on our recently developed charge and energy decomposition scheme, ETS-NOCV, as well as the eigenvectors for Pauli repulsion. Detailed analyses of the electronic and the steric factors were performed in order to understand the origin of the barrier to rotation in ammonia borane.

We found that the barrier to rotation, staggered  $\leftrightarrow$  eclipsed, is only  $\sim 2$  kcal mol $^{-1}$ . It was demonstrated using the ETS-NOCV scheme that the hyperconjugation, originating from the charge transfer from the occupied  $\sigma$  (B–H) orbitals into the empty  $\sigma^*$ (N–H), favors the staggered isomer, although, quantitatively it leads to only a slight stabilization ( $\sim 5$  kcal mol $^{-1}$ ). For ethane, this stabilization was more pronounced,  $\sim 10$  kcal mol $^{-1}$ . We have found, based on our newly proposed scheme, the natural orbitals for Pauli repulsion, that rigid rotation from the staggered to the eclipsed conformation causes predominantly the enhancement of steric (Pauli) repulsion acting solely between N–H and B–H bonds; this is subsequently ‘relieved’, leading to elongation of the B–N bond in the fully optimized eclipsed structure. Analogous trends were found for ethane (Table S1). Accordingly, the barrier to rotation in ammonia borane can be understood in a classical way; namely, as originating from the steric (Pauli) repulsion contributions that act solely between N–H and B–H bonds. Repulsion between the lone pair of ammonia and the B–H bonds is dominant in absolute terms; however, it does not influence the barrier.

**Acknowledgments** M.P.M. greatly appreciates extremely valuable discussions with Dr. Chad McKee and Prof. von Rague Schleyer (University of Georgia) on the origin of rotational barriers in hydrocarbons. M.P.M. also acknowledges the financial support from the Polish Ministry of Science and Higher Education (“Outstanding Young Researchers” scholarships, 2010, 2011–2014 and for young researchers T-subsidy). M.Parafiniuk acknowledges the Polish Ministry of Science and Higher Education for the support of the project “Diamantowy Grant,” No. DI2011 010241. We are also grateful to Academic Computer Center CYFRONET (PL-Grid Infrastructure) for the computer time.

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### References

1. Frenking G, Frohlich N (2000) *Chem Rev* 100:717–774 (and references therein)
2. Bickelhaupt FM, Baerends EJ (2000) In: Lipkowitz KB, Boyd DB (eds) *Reviews in computational chemistry: Kohnsham density functional theory: predicting and understanding chemistry*, vol 15. Wiley, Hoboken, pp 1–86. doi: 10.1002/9780470125922.ch1
3. Hund F (1926) *Z Phys* 36:657–674
4. Mulliken RS (1927) *Phys Rev* 29:637–649
5. Boys SF (1960) *Mol Phys* 32:296–299
6. Edmiston C, Ruedenberg K (1963) *Rev Mod Phys* 35:457–464
7. Reed AE, Curtiss LA, Weinhold F (1998) *Chem Rev* 88:899–926
8. Wiberg K (1968) *Tetrahedron* 24:1083–1096
9. Gopinathan MS, Jug K (1983) *Theor Chim Acta* 63:497–509
10. Mayer I (1984) *Chem Phys Lett* 97:270–274
11. Nalewajski RF, Mrozek J (1994) *Int J Quantum Chem* 51:187–200
12. Nalewajski RF, Mrozek J, Formosinho SJ, Varandas AJC (1994) *Int J Quantum Chem* 52:1153–1176
13. Nalewajski RF, Mrozek J (1996) *Int J Quantum Chem* 57:377–389
14. Nalewajski RF, Mrozek J, Mazur G (1996) *Can J Chem* 74: 1121–1130
15. Nalewajski RF, Mrozek J, Michalak A (1997) *Int J Quantum Chem* 61:589–601
16. Nalewajski RF, Mrozek J, Michalak A (1998) *Polish J Chem* 72: 1779–1791
17. Michalak A, De Kock R, Ziegler T (2008) *J Phys Chem A* 112:7256–7263
18. Bader RF (1990) *Atoms in molecules. A quantum theory*. Oxford University Press, Oxford, and references therein
19. Ponec R (1997) *J Math Chem* 21:323–333
20. Jackobsen H (2010) *Dalton Trans* 39:5426–5428
21. Becke AD, Edgecombe KE (1990) *J Chem Phys* 92:5397–5403
22. Nalewajski RF (2010) *Information origins of chemical bond, chemistry research and applications series*. Nova Science, New York
23. Dapprich S, Frenking G (1995) *J Phys Chem* 99:9352–9362
24. Kitaura K, Morokuma K (1976) *Int J Quantum Chem* 10:325–340
25. Ziegler T, Rauk A (1977) *Theor Chim Acta* 46:1–10
26. Ziegler T, Rauk A (1979) *Inorg Chem* 18:1755–1759
27. Pendás AM, Blanco MA, Francisco E (2006) *J Chem Phys* 125: 184112–184120
28. Jeziorski B, Moszynski R, Szalewicz K (1994) *Chem Rev* 94: 1887–1930
29. Toro-Labbé A, Gutiérrez-Oliva S, Murray JS, Politzer P (2009) *J Mol Model* 15:707–710
30. Van Zeist WJ, Bickelhaupt FM (2010) *Org Biomol Chem* 8: 3118–3127
31. Payne PW, Allen LC (1977) In: Schaefer HF (ed) *Modern theoretical chemistry*. Plenum, New York, pp 29–108
32. Wiberg KB (1998) *Encyclopedia of computational chemistry*, Schleyer PvR. Wiley, Berlin, pp 2518–2525
33. Kemp JD, Pitzer KS (1936) *J Chem Phys* 4:749
34. Sovers OJ, Kern CW, Pitzer RM, Karplus M (1968) *J Chem Phys* 49: 2592–2599
35. Mulliken RS (1939) *J Chem Phys* 7:339–352
36. Lowe JP (1973) *Science* 179:527–532
37. England W, Gordon MS (1971) *J Am Chem Soc* 93:4649–4657



38. Epiotis ND, Cherry WR, Shaik S, Yates RL, Bernardi F (1977) Structural theory of organic chemistry. In: Topics in current chemistry, vol 70. Springer, Berlin
39. Bader RFW, Cheeseman JR, Laidig KE, Wiberg KB, Breneman C (1990) *J Am Chem Soc* 112:6530–6536
40. Pophristic V, Goodman L (2001) *Nature* 411:565–568
41. Weinhold F (2003) *Angew Chem Int Ed* 42:4188–4194
42. Bickelhaupt FM, Baerends EJ (2003) *Angew Chem Int Ed* 42: 4183–4188
43. Pendás AM, Blanco MA, Francisco E (2009) *J Comput Chem* 30:98–109
44. Mo Y (2010) *J Org Chem* 75:2733–2736
45. Mo Y, Wu W, Song L, Lin M, Zhang Q, Gao J (2004) *Angew Chem Int Ed* 43:1986–1990
46. Mo Y, Gao Y (2007) *Acc Chem Res* 40:113–119
47. Mitoraj M, Michalak A, Ziegler T (2009) *J Chem Theory Comput* 5: 962–975
48. Mitoraj M (2011) *J Phys Chem A* 115:14708–14716
49. Kurczab R, Mitoraj MP, Michalak A, Ziegler T (2010) *J Phys Chem A* 114:8581–8590
50. Mitoraj MP, Michalak A (2011) *Inorg Chem* 50:2168–2174
51. Michalak A, Mitoraj M, Ziegler T (2008) *J Phys Chem A* 112:1933–1939
52. Mitoraj M, Michalak A (2007) *J Mol Model* 13:347–355
53. Mitoraj MP, Zhu H, Michalak A, Ziegler T (2009) *Int J Quantum Chem* 109:3379–3386
54. Mitoraj M, Michalak A (2007) *Organometallics* 26:6576–6580
55. Mitoraj M, Michalak A (2008) *J Mol Model* 14:681–687
56. Srebro M, Mitoraj M (2009) *Organometallics* 28:3650–3655
57. Nalewajski RF (1993) Köster AM, Jug K. *Theor Chim Acta* 85:463–484
58. Parafiniuk M, Mitoraj MP (2013) *Organometallics* 32:4103–4113
59. Dyduch k, Mitoraj MP, Michalak A (2013) *J Mol Model* 19: 2747–2758.
60. Kozyra P, Broclawik E, Mitoraj MP, Datka J (2013) *J Phys Chem* 117:7511–7518
61. Mitoraj MP, Michalak A, Ziegler T (2009) *Organometallics* 28:3727–3733
62. Mitoraj MP, Parafiniuk M, Srebro M, Handzlik M, Buczek A, Michalak A (2011) *J Mol Model* 17:2337–2352
63. Piękoś Ł, Mitoraj MP (2013) *J Comput Chem* 34:294–304
64. Paul A, Musgrave CB (2007) *Angew Chem* 119:8301–8304
65. Baerends EJ, Autschbach J, Bashford D, Berger JA, Bérces A, Bickelhaupt FM, Bo C, de Boeij PL, Boerrigter PM, Cavallo L, Chong DP, Deng L, Dickson RM, Ellis DE, van Faassen M, Fan L, Fischer TH, Fonseca Guerra C, Giammona A, Ghysels A, van Gisbergen SJA, Götz AW, Groeneveld JA, Gritsenko OV, Grüning M, Harris FE, van den Hoek P, Jacob CR, Jacobsen H, Jensen L, Kadantsev ES, van Kessel G, Klooster R, Kootstra F, Krykunov MV, van Lenthe E, Louwen JN, McCormack DA, Michalak A, Mitoraj M, Neugebauer J, Nicu VP, Noodleman L, Osinga VP, Patchkovskii S, Philipsen PHT, Post D, Pye CC, Ravenek W, Rodriguez JI, Romaniello P, Ros P, Schipper PRT, Schreckenbach G, Seth M, Snijders JG, Solà M, Swart M, Swerhone D, te Velde G, Vernooijs P, Versluis L, Visscher L, Visser O, Wang F, Wesolowski TA, van Wezenbeek EM, Wiesenekker G, Wolff SK, Woo TK, Yakovlev AL, Ziegler T (2009) *ADF 2009.01 SCM*, Amsterdam, The Netherlands.
66. te Velde G, Bickelhaupt FM, Baerends EJ, Fonseca Guerra C, van Gisbergen SJA, Snijders JG, Ziegler T (2001) *J Comput Chem* 22: 931–967, and references therein
67. Baerends EJ, Ellis DE, Ros P (1973) *Chem Phys* 2:41–51
68. Boerrigter PM, te Velde G, Baerends E (1988) *J Int Quantum Chem* 33:87–113
69. Becke A (1988) *Phys Rev A* 38:3098–3100
70. Perdew JP (1986) *Phys Rev B* 34:7406–7406
71. Visser O, Leyronnas P, van Zeist WJ, Lupki M (2009) *ADF-GUI*, SCM, Amsterdam, The Netherlands, <http://www.scm.com>.
72. Schwarz WHE, Schmidbauer H (2012) *Chem Eur J* 18: 4470–4479, and references therein
73. Ruedenberg K (1962) *Rev Mod Phys* 34:326–352
74. Tokiwa H, Ichikawa H (1994) *Int J Quantum Chem* 50:109–112
75. Pinter B, Fievez T, Bickelhaupt FM, Geerlings P, De Proft F (2012) *Phys Chem* 14:9846–9854
76. Haaland A (1989) *Angew Chem Int Ed* 101:1017–1032
77. Haaland A (1989) *Angew Chem Int Ed* 28:992–1007
78. Jonas V, Frenking G, Reetz MT (1994) *J Am Chem Soc* 116: 8741–8753
79. Jagielska A, Moszynski R, Piela L (1999) *J Chem Phys* 110:947–954
80. Dixon DA, Gutowski M (2005) *J Phys Chem A* 109:5129–5135
81. Bauschlicher CW Jr, Ricca A (1995) *Chem Phys Lett* 237:14–19
82. Mo Y, Song L, Wu W, Zhang Q (2004) *J Am Chem Soc* 126: 3974–3982
83. Plumley JA, Evanseck JD (2007) *J Phys Chem A* 111:13472–13483, and references therein
84. Bessac F, Frenking G (2006) *Inorg Chem* 45:6956–6964
85. Fernández I, Frenking G (2006) *Chem Eur J* 12:3617–3629
86. Thome LR, Suenram RD, Lovas FJ (1982) *J Chem Phys* 78:167–171
87. Leboeuf M, Russo N, Salahub DR, Toscano M (1995) *J Chem Phys* 103:7408–7413
88. Poater J, Sola M, Bickelhaupt MF (2006) *Chem Eur J* 12:2889–2895
89. Goodman L, Hongbing G, Pophristic V (1999) *J Chem Phys* 110: 4268–4275
90. Bader RFW, Preston HJT (1966) *Can J Chem* 44:131–145, and references therein.
91. Liu S, Govind N (2008) *J Phys Chem A* 112:6690–6699
92. Nagy Á (2007) *Chem Phys Lett* 449:212–215