



The neural signature of numerosity by separating numerical and continuous magnitude extraction in visual cortex with frequency-tagged EEG

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The ability to handle approximate quantities, or number sense, has been recurrently linked to mathematical skills, although the nature of the mechanism allowing to extract numerical information (i.e., numerosity) from environmental stimuli is still debated. A set of objects is indeed not only characterized by its numerosity but also by other features, such as the summed area occupied by the elements, which often covary with numerosity. These intrinsic relations between numerosity and nonnumerical magnitudes led some authors to argue that numerosity is not independently processed but extracted through a weighting of continuous magnitudes. This view cannot be properly tested through classic behavioral and neuroimaging approaches due to these intrinsic correlations. The current study used a frequency-tagging EEG approach to separately measure responses to numerosity as well as to continuous magnitudes. We recorded occipital responses to numerosity, total area, and convex hull changes but not to density and dot size. We additionally applied a model predicting primary visual cortex responses to the set of stimuli. The model output was closely aligned with our electrophysiological data, since it predicted discrimination only for numerosity, total area, and convex hull. Our findings thus demonstrate that numerosity can be independently processed at an early stage in the visual cortex, even when completely isolated from other magnitude changes. The similar implicit discrimination for numerosity as for some continuous magnitudes, which correspond to basic visual percepts, shows that both can be extracted independently, hence substantiating the nature of numerosity as a primary feature of the visual scene.

numerical cognition | numerosity extraction | fast periodic visual stimulation | quantities | nonsymbolic mathematical abilities

When it comes to sets of more than five objects, we can rapidly figure out an approximation of the number of items, the numerosity, without counting (1). Humans share with other animal species an intuition for numerical quantities (2). The nature of the cognitive mechanism behind this ability to approximate large numerosities is still vividly debated. Researchers largely assume that we possess an approximate number system (ANS), a specific system that extracts numerosity and builds a mental representation of the discrete numerical magnitude from the visual scene (3). However, a set of objects is characterized not only by numerosity, but also by several continuous visual features, including the individual object sizes and the extent of the set. These continuous magnitude dimensions are intrinsically related to numerosity (e.g., a more numerous set naturally occupies a larger area) and may serve as critical visual cues to access numerosity. This has led some authors to suggest that there is no specific cognitive mechanism devoted to number processing and that numerosity is either processed by general magnitude mechanisms or emerges from a combination of continuous dimensions (4). No consensus has been reached thus far on how continuous magnitudes contribute to numerosity processing, and a large body of evidence has demonstrated that they can either facilitate or

interfere with numerosity judgments (5). The current study capitalized on a frequency-tagging electrophysiological approach to isolate numerosity from continuous magnitude dimensions and to measure the specific cerebral responses driven by both.

The ability to discriminate sets of objects based on numerosity is thought to be shared with other animal species and to be present in infants long before the development of language (6–8). There is substantial behavioral and neuroimaging evidence of this numerical ability. For instance, recent experiments highlighted a spontaneous bias in favor of numerosity against continuous magnitudes when participants had to choose the odd one of three collections of dots or to categorize collections as “large” or “small” (9, 10): In both cases, numerosity was spontaneously selected as the decision criterion. Further, some studies identified populations of neurons that are specifically tuned to numerosity in the parietal cortex of humans and monkeys (11, 12). Theoretical models postulate that the mechanism behind this numerical ability consists in a transformation of sensory input into an abstract estimate of the number of elements present in a visual scene (2, 13). Nevertheless, existing empirical evidence of such mechanisms remains problematic due to the inherent correlation of continuous magnitude changes with

Significance

Approximating large quantities has been identified as a building block of mathematical cognition. Despite its importance from both a fundamental and an educational perspective, the mechanism behind this ability is still not fully understood. The remaining gap comes from the fact that a set is not only characterized by its number of objects but additionally by non-numerical features naturally correlating with numerosity (e.g., a more numerous set occupies a larger surface). The current frequency-tagging EEG paradigm isolates specific responses to number and to nonnumerical dimensions. We demonstrate that when numerosity and the other dimensions are totally decorrelated in stimulus sequences, changes of each are automatically discriminated in early visual cortex, highlighting the status of numerosity as a primary visual feature.

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numerosity changes. Continuous magnitudes rather than numerosity itself could account for the observed results (14). It is an open question whether the cognitive system is able to rapidly extract numerosity information necessary to build up a representation independent of continuous magnitude variations—and if the system has that ability, what happens to the covarying continuous magnitude information as numerosity is processed? The ANS theory proposes that all continuous magnitudes are filtered out during a normalization stage (2), but there is not much evidence about this filtering stage since continuous magnitudes substantially affect numerosity judgments (15).

Alternative theories have proposed that numerosity is yoked to continuous magnitude processing. Among these, a Theory of Magnitude (ATOM) describes the relationship between continuous magnitudes and numerosity in terms of a unique system that is capable of representing any kind of discrete and continuous magnitude, including numerosity, time (duration), and space (extension) (16). Some authors proposed a general sense of magnitude for both continuous and discrete quantities, in which size perception is developmentally and evolutionarily more primitive than numerosity, and continuous magnitude plays a key role in the development of numerical magnitude processing (17, 18). There is substantial empirical evidence supporting both common and separate neural areas for numerical and continuous magnitudes (e.g., refs. 19–22). Partially overlapping topographical maps for numerosity and continuous magnitude extraction were identified within the human parietal cortex, although distinct neural tuning and organization within the maps suggested distinct processing mechanisms (23, 24). Within these overlapping areas, the right parietal lobe was identified as a likely anatomical location of the generalized magnitude processing system, according to a recent functional (fMRI) meta-analysis (25). Further, some authors argued that numerosity is only an abstract cognitive construct resulting from the weighting of all continuous magnitude features present in the visual stimulus, and that numerosity is extracted through adaptive recombination of lower-level sensory information according to the needs of a particular context (4). Such Sensory Integration (SI) theory assumes that all existing evidence of numerosity extraction can be explained by cognitive control mechanisms handling the integration of continuous magnitudes.

The major challenge in disentangling these hypotheses and in understanding the mechanism of numerosity processing is to isolate numerosity from continuous magnitudes. Several elegant ways to control for continuous dimensions have been developed for behavioral tasks (26–29), but they control for all magnitude changes across the stimulus set, although each stimulus still contains information about both numerosity and continuous dimensions. Indeed, any visual stimulus carries information about both numerosity and continuous magnitudes. These methods are thus incapable of disentangling numerosity from nonnumerical magnitude processing in any strict sense. Importantly, this limitation applies to almost all evidence provided so far in favor of the ANS theory.

The current study used a frequency-tagging approach, which consists in recording steady-state visual evoked potentials (SSVEP) corresponding to the neural responses that are specific to periodic stimulus changes in a single given dimension (30). SSVEP have already been successfully recorded in response to numerosity variations (31), but the present study systematically isolates the discrimination of numerosity and of continuous magnitudes with a frequency-tagged experimental paradigm that requires no explicit task (and thus no decision nor judgment): Visual stimulation followed an oddball paradigm in which a deviant stimulus was periodically introduced within a stream of standard stimuli (32). Critically, we strictly manipulated the nature of the periodic change, so that only the dimension under consideration periodically fluctuated (33). This manipulation allows for the recording of the neural responses synchronized to changes in the target dimension, since only that particular dimension was updated periodically. The current

design allows to track neural discrimination of changes in numerosity as well as in each of the continuous dimensions, by assigning each dimension to be the periodic deviant in separate experimental conditions. If the visual system is sensitive to periodic changes relative to the fluctuating dimension, the brain should produce responses synchronized to the deviant frequency and its harmonics (34). We are thus able to record brain activity specifically related to the discrimination of numerosity and of each continuous dimension.

Experimental Design

Sequences of dot arrays were presented, updating at a base rate of 10 Hz (i.e., 10 dot arrays per second). Each presented stimulus was characterized by five dimensions: number of dots, dot size, total occupied area, convex hull (i.e., the smallest contour enclosing all dots of the collection), and density. The dot arrays were made to vary randomly along all dimensions except one, which changed systematically at a rate of 1.25 Hz (i.e., one deviation every eight items). On each 44-s block, the periodic dimension was made to be either numerosity or one of the four continuous magnitudes (i.e., dot size, total area, convex hull, and density), see Fig. 1. The ratio by which the deviant dimension varied from the standards could be 1.1, 1.2, 1.3, 1.4, or 1.5, leading to a design consisting of five dimensions and five ratios. Each of the 25 conditions was repeated in three blocks. Additionally, we were interested in assessing whether variability along each of these dimensions could be expected to elicit responses at the early stages of the visual processing hierarchy. As the current electrophysiological recordings did not allow to precisely identify the exact location where the discrimination occurs, we ran our stimuli through a relatively simple model of early visual processing that has previously been shown to predict responses in four topographically organized areas of visual cortex (35). This provides an a priori, assumption-free estimate of how visual cortex might respond to our stimuli. Those estimates are then compared to our electrophysiological results and used to relate the current study to general information processing capabilities of the human visual system.

Results

To measure the neural responses corresponding to the discrimination of each dimension, we summed the baseline-corrected amplitudes of the target frequency (1.25 Hz) and its harmonics up to the 18th (i.e., the highest harmonic with a significant response, *Methods*), excluding harmonics of the base rate frequency (i.e., 10 and 20 Hz, as in previous studies; ref. 36). The Sums of Baseline-corrected Amplitudes (SBA) were computed per participant and per condition, and then averaged at the group level. We found a clear response to the deviant stimulus at the group level for the largest ratio of three visual dimensions: Total Area, Convex Hull, and Numerosity (Fig. 2). The strongest SBA peaks were recorded around medial occipital electrode Oz, which is consistent with previous results on number discrimination (32). The mean values of the SBA for the highest ratio (1.5) averaged across the whole posterior scalp and their corresponding 95% confidence intervals (CI) were, respectively, 0.27 μ V [0.23, 0.31] for Total Area, 0.25 μ V [0.21, 0.28] for Numerosity, 0.23 μ V [0.19, 0.27] for Convex Hull, 0.12 μ V [0.08, 0.15] for Density, and 0.02 μ V [0.00, 0.05] for Item Size. To get a clearer picture of these results, we considered four posterior regions of interest for further analyses: the medial occipital, medial occipito-parietal, left occipito-parietal, and right occipito-parietal regions (*Methods*).

To evaluate the effect of the ratio manipulation, we constructed a linear mixed model, with the ratio and the regions as fixed predictors of the SBA and participants as random factor. Visual inspection of residual plots did not reveal any obvious deviations from homoscedasticity or normality. We compared the full model to two reduced models that did not include the ratio and region predictor, respectively, using χ^2 tests on the log-likelihood values. For Numerosity, the full model had a better fit than both reduced models, $\chi^2(1) = 21.60$, $P < 0.001$, and $\chi^2(3) = 10.874$, $P = 0.01$, respectively without ratio and without regions. A similar result was

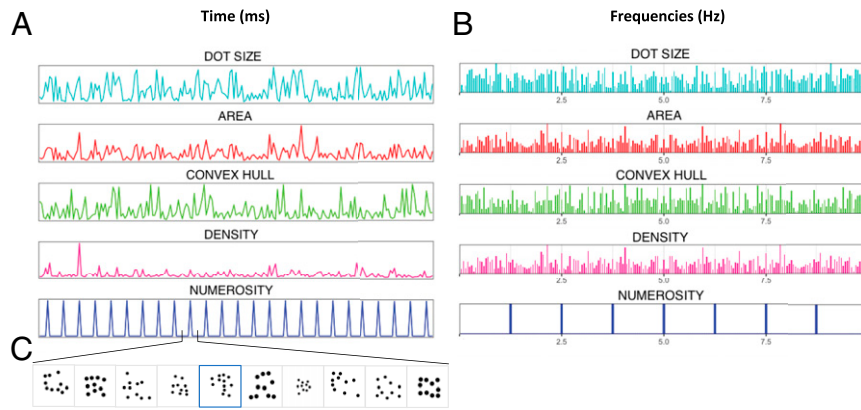


Fig. 1. Illustration of the experimental design, example with numerosity as the periodic deviant. (A) Sequences of dot patterns were characterized by five dimensions: dot size, total area, convex hull, density, and numerosity. Time series of values for the five dimensions during the first 20 s of a trial (200 stimuli) are plotted. In this example, numerosity is the deviant that varies periodically at 1.25 Hz while the continuous magnitude dimensions vary randomly. (B) Frequency spectra of the corresponding time series after Fourier transformation. Only the periodic varying dimension, in this example numerosity, produces clear spectral power at 1.25 Hz and higher harmonics. (C) Illustration of a subset of the stimuli.

observed for Total Area where the full model had a better fit than both reduced models, $\chi^2(1) = 23.915$, $P < 0.001$, and $\chi^2(3) = 31.077$, $P < 0.001$, respectively, without ratio and without regions. We thus observed a significant ratio effect in both conditions. The strongest responses to periodic changes in Numerosity and in Total Area were recorded in the medial occipital electrodes. For Convex Hull, the full model had a better fit than the reduced models without ratio, $\chi^2(1) = 35.53$, $P < 0.001$, but not better than the reduced model without regions, $\chi^2(3) = 2.66$, $P = 0.45$. For Density, the full model had a barely significantly better fit than the model without ratio, $\chi^2(1) = 4.07$, $P = 0.04$, but not than the one without regions, $\chi^2(3) = 0.171$, $P > 0.10$. Finally, for Size, the full model did not have a significantly better fit than either reduced models, $\chi^2(1) = 0.171$, $P > 0.10$, and $\chi^2(3) = 4.55$, $P = 0.21$.

The linear mixed models thus showed that the brain response to the periodic change of Numerosity and Total Area was significantly affected by both the ratio between deviant and standard and by the location of the electrodes (Fig. 2). The effect was

largely driven by responses in the medial occipital region: At the group level, the medial occipital region produced a clear SBA response to periodic changes in Area when the ratio was 1.3 or more (mean SBA for ratio 1.3 = 0.43 μV ; 95% CI [0.24, 0.62]). Periodic changes in Numerosity also produced clear SBA responses in the medial occipital region, although only for the largest ratio of 1.5 (mean SBA = 0.53 μV ; 95% CI [0.30, 0.74]). Convex Hull and Density both yielded significant effects of ratio, but not of region, but in both conditions the medial occipital region produced the strongest responses. For Convex Hull, only ratio 1.5 reached significance (mean SBA = 0.43 μV ; 95% CI [0.19, 0.61]), while ratio 1.4 of Density (mean SBA = 0.19 μV ; 95% CI [0.05, 0.33]) was just at the limit of significance. However, there was no significant brain response to periodic changes of Item Size (mean SBA = 0.11 μV ; 95% CI [-0.02, 0.25]), consistent with the lack of region or ratio effect in the linear mixed effect model.

To enrich our interpretation of the electrophysiological measurements, we ran an additional analysis that was aimed at testing

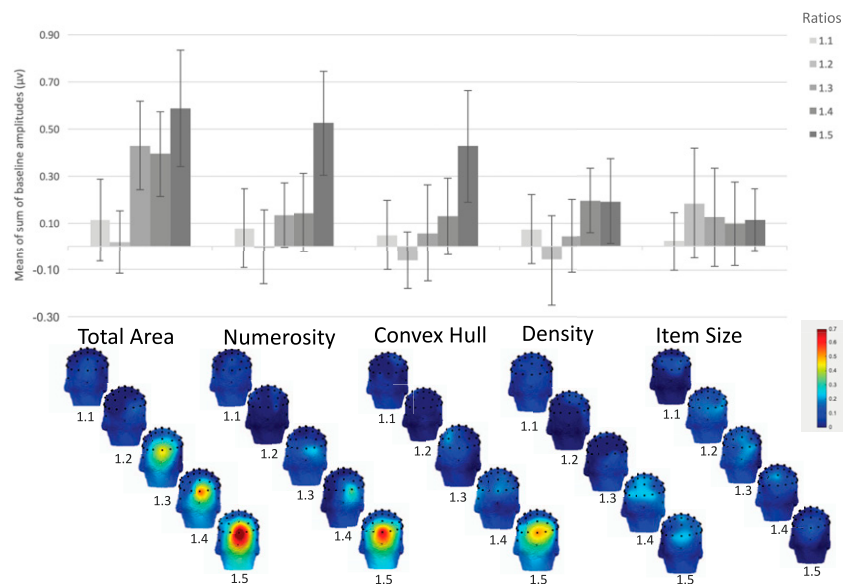


Fig. 2. (Upper) Average of the sums of the baseline-corrected amplitudes (SBA, in microvolts) for every condition, as a function of the change ratio. The SBA is the sum of the target frequency (1.25 Hz) and its harmonics, excluding the base rate (see text). Error bars depict 95% CI. (Lower) Scalp topographies of the SBAs (in microvolts) for every condition, as a function of the ratio.

whether a relatively simple model of early visual processing, which was not designed to account for number processing, would predict the results we observed. To that end, we applied a second-order contrast (SOC) model (*Methods*) to the images used in the experiments. We plot the model output in Fig. 3, along with the variability of the standard and deviant images on the five dimensions. The model output was closely aligned with our SSVEP data: For three dimensions that elicited significant synchronized brain responses, Numerosity, Total Area, and Convex Hull, the deviant images tended to elicit stronger model responses than standard images, as evidenced by nonoverlapping boxplots in Fig. 3 (the median and 25th and 75th percentiles represented by the boxplots are reported in *SI Appendix, Table S2*). For Numerosity and Total Area, this effect was weaker when modeling visual areas beyond V1, whereas for convex hull, the strongest effect was seen in V4. For Dot Size and Density, the two dimensions that did not elicit synchronized brain responses, every deviant image produced model responses that were within the 25th and 75th percentile of the standard responses, indicating that the model was unable to distinguish standard and deviant responses. It is important to note that the model was designed to capture activity elicited in the visual cortex by simple gratings, textures, and natural scenes and fit to fMRI data, a different neuroimaging modality from the one we used. The fact that the output of such a model is so well-aligned with our measured data are good news both for the model and for our approach. The model's ability to approximate our measured electrophysiological responses to numerosity, despite not being designed to capture or account for numerosity, is especially compelling, and may indicate that the initial stages of numerosity processing rely on relatively simple computations taking place in early visual cortex.

Discussion

The objective of the current study was to isolate and contrast the specific cerebral responses to changes of numerosity and four continuous visual magnitudes. We observed clear electrophysiological responses that were synchronized to the frequency of a periodically occurring deviant stimulus, when that deviant encompassed a change of numerosity similarly as for some visual features. These synchronized responses support the view that the human brain can spontaneously discriminate periodic changes in numerosity. The observed effect of region of interest and the results from the model approach further suggest that this ability is primarily driven in the occipital cortex. The frequency-tagging approach taken in the current study allows us to overcome the issue of correlations between numerosity and continuous magnitudes, which means that we could choose natural dimensions as a strong comparison point in terms of low-level changes in visual features. Indeed, we demonstrated that when numerosity was the only parameter varying periodically without periodic variation of continuous magnitudes at the sequence level, its changes could still be discriminated as automatically as changes in Total Area and Convex Hull.

These findings are in line with recent studies that have identified rapid electrophysiological responses to numerosity (75 ms after stimulus presentation) (37) and with evidence that encoding of numerosity occurs very early in the visual processing stream: Tuning for numerosity has been demonstrated in early visual regions of occipital cortex (V1, V2, and V3) (31, 33, 38, 39). Crucially, as our experimental design ensured that only a single dimension varied periodically over a given stimulus sequence, the current observed responses can be uniquely associated with numerosity, and contributions from any of the continuous dimensions in isolation can be ruled out. It is worth noting that our study involved passive viewing only. Hence, our findings do not preclude the existence of later interactions between the dimensions, such as those that have been recurrently reported behaviorally in nonsymbolic comparison tasks involving decision-making and cognitive control. The current frequency-tagging paradigm was not designed to capture the latter kind of processes, nor the relative contribution

of parietal or frontal regions to the subsequent processing stages. It is thus still possible that a weighting (4) or normalization of the various magnitude information (2) occurs at later processing stages while performing a numerosity task (e.g., nonsymbolic estimation or comparison tasks). Recent studies support the view that such interactions are deliberate, and strategic, rather than perceptual (40). In other words, the current results do not support the hypothesis that the number of items in a visual scene is initially processed through an active weighting of continuous magnitudes at that early processing stage.

The results of the conditions in which continuous magnitudes were manipulated revealed synchronized responses that could be uniquely associated with the total area occupied by the dots and the extent of the convex hull. On the contrary, no such synchronizations were observed for periodic variations of density and dot size. This pattern of results indicates that the brain can spontaneously discriminate total area and convex hull, but not density and dot size: Total Area and Convex Hull are both directly related to low-level visual features: Total Area is confounded with stimulus luminance, a primary property of the visual scene (41) to which the visual system responds in a nearly veridical manner (42). Convex Hull is confounded with the size of the space taken in the visual scene and, thus, with the width and height of the visual angle sustained by the entire stimulus, properties that are known to influence the brain response to the stimulation (43, 44). Human vision thus seems to be provided with an early discrimination mechanism for numerosity that operates in an equivalent way to the mechanisms involved with decoding low-level visual features, suggesting that numerosity may also be considered a primary visual feature (45). The topological invariance of numerosity has been proposed as a key visual attribute distinguishing numerosity from continuous magnitudes (46, 47). This unique aspect of numerosity might be key to its utility as a primary feature of visual scenes.

The SOC model was designed to capture activity elicited in visual cortex by relatively simple image stimuli and fit to fMRI data. The responses predicted by the model are well-aligned with our electrophysiological data, so that variability over dimensions that produced synchronized brain responses also produced systematically different predicted model responses. This indicates that the synchronized brain responses could plausibly be elicited by the mechanisms in early visual cortex that the model was designed to capture. It is perhaps not surprising that early visual cortex would be sensitive to Total Area and Convex Hull, as indicated by the model. However, stimuli that are made to vary along the numerosity, but not the other dimensions, also elicit systematically different predicted model responses. This finding is more remarkable as the model was not designed to detect that kind of change. It thus offers support for the idea that numerosity is a primary visual feature that, at least at initial processing stages, relies on relatively simple computations taking place in early visual cortex.

It is worth noting that the observed discrepancies across dimensions suggests that the observed synchronized electrophysiological responses do not reflect a general mechanism of response to any periodic deviant, but rather depend critically on the brain's sensitivity to the change (34). The results indicate that the brain is sensitive to Numerosity, Total Area, and Convex Hull, while we found no evidence of sensitivity to periodic changes in Dot Size or Density. The lack of a density effect might be due to the range of number of dots used in the present experiment. Indeed, some authors have argued that the density of a dot array becomes salient only when the number of dots is much larger than the range we used (i.e., over hundreds of dots) (48). According to their results, electrophysiological responses to density changes would not occur with arrays with less than 50 dots, which is consistent with our observations. The lack of a dot size effect could be explained by attention being allocated to the global visual scene rather than to its individual parts. The visual system can segment a scene to extract relevant information, and previous research suggests that there would be no encoding of individual dots but rather

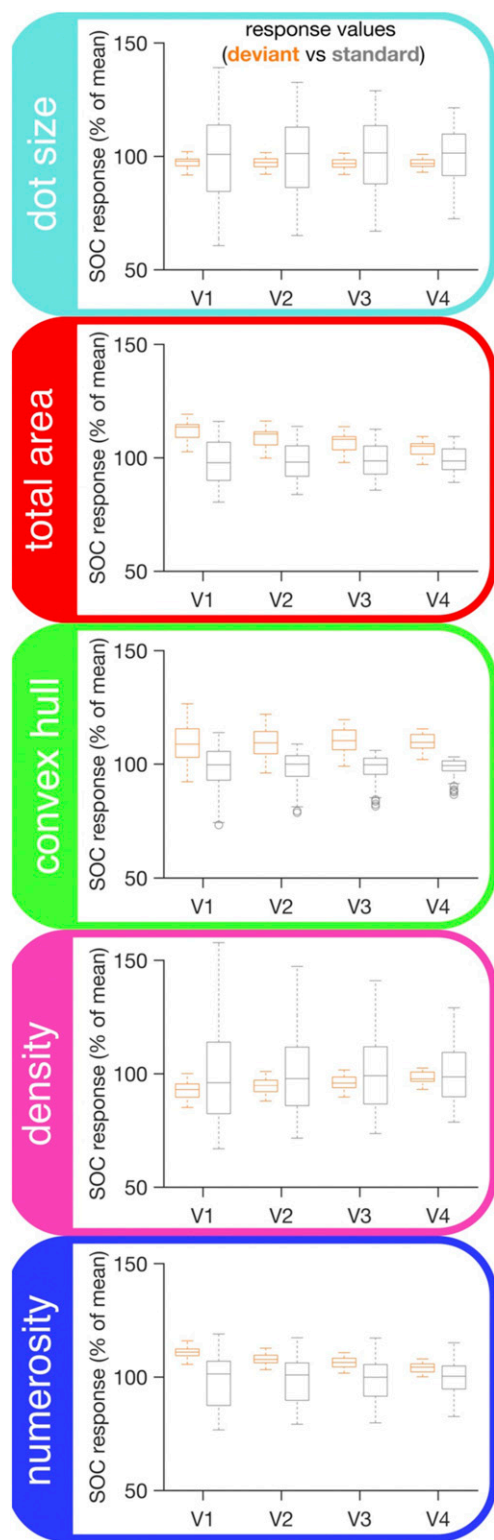


Fig. 3. For each periodic deviant dimension, the graphs depict the responses predicted by the SOC model in four topographically organized areas in the human visual cortex (V1 [primary visual cortex], V2, V3, and V4). Each row represents a dimension assigned as periodic deviant, as indicated on the left, with each plot describing the set of images associated. The predicted responses are plotted as percent of the overall average response across all images (standard and deviant) within each condition. The predicted responses are the result of passing the stimuli through four different iterations of the SOC model, using model parameters derived previously by fitting the model to fMRI BOLD responses in each of the four areas. For every boxplot,

an efficient general description of the scene (45). Thus, although we did not observe specific responses to variations in dot size and density, these properties may be measurable under different experimental settings, including larger ratios or longer presentation times, with the latter manipulation possibly allowing for directed attention toward individual scene parts.

Taken together, the current results provide evidence in favor of the Visual Number Sense idea proposed by Burr and Ross (49), which considers numerosity a primary visual property that can be extracted from the visual scene. Further support comes from recent evidence highlighting a specific neural sensitivity to numerosity very early in the visual stream, which was interpreted as direct and automatic encoding of numerosity information (37, 39). The seminal ANS theory proposed that lower-level visual features related to continuous magnitudes must be neutralized in a so-called normalization stage, which precedes the extraction of number in an abstract, modality-free manner (i.e., the “abstract numerosity” as described by Gebuis; ref. 4). Recent findings of neural sensitivity to numerosity both in early and late ERP components were interpreted as neural evidence of this normalization stage occurring in primary visual cortex prior to later summation stage (31). The data presented here can also be considered as evidence of an early summation stage in primary visual cortex (39). The current results demonstrate that a specific discrimination based on numerosity and some continuous magnitudes is possible similarly and very early in the visual stream. It is important to note that in a natural context, where the dimensions are not isolated as in the current experimental paradigm and, thus, strongly correlate with each other, early stage visual discrimination would likely be much stronger. Indeed, recent neuroimaging evidence supports a numerosity representation both in parietal and occipital areas, with an increasing sensitivity to numerosity along the dorsal stream especially when the numerosity is related to a task (50, 51).

Conclusion. The current study reports isolated measures of the brain’s ability to detect changes in both numerosity and continuous magnitudes, without the confounds that usually arise due to the correlation between these dimensions. The results show that numerosity can be rapidly discriminated in the visual stream independently of other visual features, supporting the hypothesis of an early visual number sense. We further suggest that numerosity is a primary attribute that can be directly extracted from the visual scene. Future research is needed to determine whether the ability to extract numerosity directly is an innate ability or is learned over the course of visual development.

Methods

Participants. Twenty-five undergraduate students participated in the study. Volunteers suffering from or with a history of suffering from any neurological or neuropsychological disease, from any learning disability such as dyscalculia, or from any uncorrected visual impairment were not allowed to participate. We excluded four participants due to the presence of substantial noise in their EEG signal (e.g., noise due to transpiration or movements). The final sample thus consisted of 21 participants, with a mean age of 23.5 y (SD = 2.7, 9 females). Due to the length of the experiment, some participants failed to respond to the color change task (see below) and were excluded for some of the conditions, resulting in a final sample of 19 for Area, 18 for Convex hull, 18 for Numerosity, 19 for Size, and 20 for Density. No participant was excluded for more than two conditions. We followed American Psychological Association (APA) ethical standards to conduct the present study. The Faculty Ethics Committee approved the methodology and the implementation of the experiment before the start of data collection (Comité d’Avis Ethique de la Faculté des Sciences Psychologiques et de l’Education). All participants provided their written informed consent prior to taking part in the study. The experiment lasted 2 h in total, and participants received 20 euros for their participation.

the central mark is the median, the edges of the box are the 25th and 75th percentiles, the whiskers extend to the most extreme data points not considered outliers, and the outliers are indicated with dots.

Fast Periodic Visual Stimulation.

Stimuli. To create the dot arrays, we used a preliminary version of the NASCO software (52). NASCO is an open and freely usable MATLAB application that allows the generation of dot arrays while keeping a given dimension constant. Critically for the purpose of our study, for every condition, we generated 400 standard pictures in which only one dimension (determined by the condition under consideration) was kept constant while other features stochastically varied. We then created 100 deviant arrays for each condition with a similar approach, by using the ratio of the given condition to determine the value of the only manipulated fluctuating dimension. All pictures were squares of 850 × 850 pixels. After the creation of the pictures, we generated multiple sequences of 440 of these (since the whole stimulation sequence had 10 pictures per second during 44 s), including 385 frequent and 55 deviant stimuli. In order to statistically verify that stochastic fluctuations related to irrelevant dimensions were not periodic within these sequences, we computed the Fast-Fourier Transform (FFT) of the values taken by each dimension over time. We transformed the spectra into Z-scores, and we averaged the values of the deviant frequency rate and its harmonics up to the seventh (1.25, 2.50, 3.75, 5.00, 6.25, 7.50, 8.75 Hz). We then iteratively selected for each condition one sequence in which the averaged periodicity of the dimension of interest was larger than the 99% probability unilateral threshold of a standard normal distribution (i.e., 2.32), and in which the averaged periodicity of the other four dimensions were less than this threshold. The exact same sequence was used thrice within a given condition to avoid any periodic artifact when averaging the repetitions (see *SI Appendix* for further details about stimulus construction).

Apparatus. We used MATLAB (The MathWorks) with the Psychophysics Toolbox extensions (53, 54) to display the stimuli and record behavioral data. The electroencephalography (EEG) recording took place in a shielded Faraday cage (275 cm × 195 cm × 280 cm). Participants were comfortably seated at 1 m from the screen, with their gaze in front to the center of the screen (24-inch LED monitor, 100-Hz refresh rate, 1-ms response time). Screen resolution was 1,024 × 768 pixels. The order of the conditions during the EEG recording session was counterbalanced across participants.

Procedure. Participants were instructed to look at the entire screen by keeping their gaze on a small fixation diamond that was continuously displayed at the center of the screen. The fixation randomly changed color from blue to red four to six times during a sequence and participants were instructed to press a button with their right forefinger each time they detected the color change. Their responses were recorded to quantify compliance with the instructions. Participants' mean response rates to the color change of the fixation diamond was 96%. No participant missed the color change more than once during a 44-s block. Such high detection rate indicates that participants followed the instructions and kept their gaze on the center of the screen during EEG acquisition. Stimuli subtended a maximal visual angle of 9°. Stimulus presentation followed a sinusoidal contrast modulation from 0 to 100% (55, 56). The base frequency rate was 10 Hz, so that 10 stimuli were displayed per second (and consequently each stimulus lasted 100 ms in total from onset to total offset). Every stimulation sequence lasted 48 s, including 44 s of recording and 2 s of fade-in and fade-out, which were not analyzed.

During each sequence, dot arrays entailed one specific feature that was kept constant, and a periodic deviation from this constant every eight items. In other words, deviant stimuli were periodically displayed within a stream of standard dot arrays at the frequency rate of 1.25 Hz (see Fig. 1, and for all conditions see *SI Appendix, Figs. S1–S5*). We manipulated two factors: the nature of the dimension that periodically fluctuated and the ratio of the fluctuation from the standard to the deviant arrays. As for the dimension, we manipulated the Number (N) of dots, the individual dot Size (S), the total Area (A) occupied by the dots, the area of the Convex Hull (CH), and finally the Density (D) of the array. As for the ratio, we created dot arrays that deviated from the standard with five different ratios (1.1, 1.2, 1.3, 1.4, and 1.5). The manipulated dimension and the deviation ratio were fixed during a block. Therefore, by the combination of both factors we obtained 25 different conditions. Each condition was repeated three times, for a total of 75 44-s stimulation sequences. When debriefed at the end of the experiment,

participants reported changes of the dot arrays but no participant noticed periodic changes in any dimension.

EEG recording. EEG data were acquired at 1,024 Hz using a 64-channel BioSemi ActiveTwo system (BioSemi B. V.). The electrodes were positioned on the cap according to the standard 10–20 system locations (for exact position coordinates, see <http://www.biosemi.com>). Two additional electrodes, the Common Mode Sense (CMS) active electrode and the Driven Right Leg passive electrode, were respectively used as reference and ground electrodes. Offsets of the electrodes, referenced to the CMS, were held below 40 mV. Eye movements were monitored with four flat-type electrodes; two were placed above and below participant's right eye, the other two were positioned lateral to the external canthi.

Data analyses. Analyses were conducted with the help of Letswave 6 (<https://github.com/NOCIONS/letswave6>). Data files were down-sampled from 1,024 Hz to 512 Hz for faster processing. Data were filtered with a four-order band-pass Butterworth filter (0.1–100 Hz) and referenced to the common average.

The fade-in and fade-out periods were excluded from the analyses leading to the segmentation of an EEG signal of 44 s (corresponding to the display of 440 stimuli). The three repetitions were averaged per condition and per participant. A FFT was applied on the signal to extract amplitude spectra for the 64 channels with a frequency resolution (the size of the frequency bins) of 0.016 Hz.

Based on the frequency spectra, we computed two measures to determine whether and how the brain specifically responded to the deviant frequency in the five conditions: Sum of baseline-corrected amplitudes, and Z-scores. The SBA is expressed in microvolts and can thus quantify changes within the EEG signal (32, 34). We computed the baseline-corrected amplitudes by subtracting from the bin of interest (i.e., 1.25 Hz) the mean amplitude of 20 surrounding frequency bins and the latter's 20 surrounding bins (10 on each side, excluding the one immediately adjacent to the bin of interest), which constitutes the baseline amplitude (57). We calculated similarly the baseline-corrected amplitude of the harmonics of the frequency of interest relative to their neighbors (i.e., up the 18th harmonic). Then, we summed the baseline-corrected amplitudes obtained for the frequency of interest and its harmonics.

We grouped electrodes of interest in four posterior regions of interest for further analyses: the medial occipital (O1, O2, Oz, Iz), medial occipito-parietal (Pz, POz, P1, P2, P3, P4, PO3, PO4), left occipito-parietal (P5, P7, P9, PO7), and right occipito-parietal (P6, P8, P10, PO8) regions (58).

Visual Cortex Response Predictions. We applied a cascaded, feed-forward model of BOLD responses to visual stimuli, the second-order contrast (SOC) model to the images used in the conditions with the largest ratio (1.5). This model first passed the image through a bank of contrast-normalized, localized, V1-like filters, and then reprocessed the output in a second stage that, among other things, measured the contrast variability in the output of the first stage (35). The SOC model has been fit to data for V1, V2, V3, and V4, and is effective at predicting how these areas respond to simple visual stimuli, including gratings and textures, while also capturing increased sensitivity to the structure of natural scenes in extrastriate visual areas. These features make it a reasonable model for estimating the activity that our dot images would elicit in early visual cortex. We applied the SOC model separately to each image, using model parameters for V1, V2, V3, and V4 provided in the original publication. We then summed the model output across each image to get a predicted average response of each brain area to each image update. This allowed us to compare the predicted average responses to the standard and deviant image updates and use the comparison as an estimate of how strongly the deviants would be expected to drive synchronized brain responses in early visual cortex, according to the SOC model.

Data availability. Data related to this work are available on the Open Science Framework (https://osf.io/9z5jb/?view_only=3266699943a54b28aa30cc7ea8177ef3).

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1. E. L. Kaufman, M. W. Lord, T. W. Reese, J. Volkman, The discrimination of visual number. *Am. J. Psychol.* **62**, 498–525 (1949).
2. S. Dehaene, J.-P. Changeux, Development of elementary numerical abilities: A neuronal model. *J. Cogn. Neurosci.* **5**, 390–407 (1993).
3. L. Feigenson, S. Dehaene, E. Spelke, Core systems of number. *Trends Cognit. Sci.* **8**, 307–314 (2004).
4. T. Gebuis, R. Cohen Kadosh, W. Gevers, Sensory-integration system rather than approximate number system underlies numerosity processing: A critical review. *Acta Psychol. (Amst.)* **171**, 17–35 (2016).
5. A. Henik, *Continuous Issues in Numerical Cognition: How Many or How Much* (Academic Press, 2016).

6. A. Nieder, S. Dehaene, Representation of number in the brain. *Annu. Rev. Neurosci.* **32**, 185–208 (2009).
7. J. F. Cantlon, M. L. Platt, E. M. Brannon, Beyond the number domain. *Trends Cognit. Sci.* **13**, 83–91 (2009).
8. G. Anobile, G. M. Cicchini, D. C. Burr, Number as a primary perceptual attribute: A review. *Perception* **45**, 5–31 (2016).
9. G. M. Cicchini, G. Anobile, D. C. Burr, Spontaneous perception of numerosity in humans. *Nat. Commun.* **7**, 12536 (2016).
10. S. Ferrigno, J. Jara-Ettinger, S. T. Piantadosi, J. F. Cantlon, Universal and uniquely human factors in spontaneous number perception. *Nat. Commun.* **8**, 13968 (2017).

11. M. Piazza, V. Izard, P. Pinel, D. Le Bihan, S. Dehaene, Tuning curves for approximate numerosity in the human intraparietal sulcus. *Neuron* **44**, 547–555 (2004).
12. A. Nieder, D. J. Freedman, E. K. Miller, Representation of the quantity of visual items in the primate prefrontal cortex. *Science* **297**, 1708–1711 (2002).
13. T. Verguts, W. Fias, Representation of number in animals and humans: A neural model. *J. Cogn. Neurosci.* **16**, 1493–1504 (2004).
14. K. S. Mix, J. Huttenlocher, S. C. Levine, Multiple cues for quantification in infancy: Is number one of them? *Psychol. Bull.* **128**, 278–294 (2002).
15. J. Nys, A. Content, Judgement of discrete and continuous quantity in adults: Number counts! *Q J Exp Psychol (Hove)* **65**, 675–690 (2012).
16. V. Walsh, A theory of magnitude: Common cortical metrics of time, space and quantity. *Trends Cognit. Sci.* **7**, 483–488 (2003).
17. T. Leibovich, N. Katzin, M. Harel, A. Henik, From “sense of number” to “sense of magnitude”: The role of continuous magnitudes in numerical cognition. *Behav. Brain Sci.* **40**, e164 (2017).
18. A. Henik, Y. Gilksman, A. Kallai, T. Leibovich, Size perception and the foundation of numerical processing. *Curr. Dir. Psychol. Sci.* **26**, 45–51 (2017).
19. V. Dormal, M. Andres, M. Pesenti, Dissociation of numerosity and duration processing in the left intraparietal sulcus: A transcranial magnetic stimulation study. *Cortex* **44**, 462–469 (2008).
20. D. Bueti, V. Walsh, The parietal cortex and the representation of time, space, number and other magnitudes. *Philos. Trans. R. Soc. Lond. B Biol. Sci.* **364**, 1831–1840 (2009).
21. S. F. Lourenco, M. R. Longo, General magnitude representation in human infants. *Psychol. Sci.* **21**, 873–881 (2010).
22. O. Tudusciuc, A. Nieder, Neuronal population coding of continuous and discrete quantity in the primate posterior parietal cortex. *Proc. Natl. Acad. Sci. U.S.A.* **104**, 14513–14518 (2007).
23. B. M. Harvey, A. Fracasso, N. Petridou, S. O. Dumoulin, Topographic representations of object size and relationships with numerosity reveal generalized quantity processing in human parietal cortex. *Proc. Natl. Acad. Sci. U.S.A.* **112**, 13525–13530 (2015).
24. B. M. Harvey, S. O. Dumoulin, A network of topographic numerosity maps in human association cortex. *Nat. Hum. Behav.* **1**, 0036 (2017).
25. H. M. Sokolowski, W. Fias, C. Bosah Ononye, D. Ansari, Are numbers grounded in a general magnitude processing system? A functional neuroimaging meta-analysis. *Neuropsychologia* **105**, 50–69 (2017).
26. C. Mussolin, S. Mejias, M.-P. Noël, Symbolic and nonsymbolic number comparison in children with and without dyscalculia. *Cognition* **115**, 10–25 (2010).
27. M. Piazza, Neurocognitive start-up tools for symbolic number representations. *Trends Cognit. Sci.* **14**, 542–551 (2010).
28. M. M. M. Mazzocco, L. Feigenson, J. Halberda, Preschoolers’ precision of the approximate number system predicts later school mathematics performance. *PLoS One* **6**, e23749 (2011).
29. N. K. DeWind, G. K. Adams, M. L. Platt, E. M. Brannon, Modeling the approximate number system to quantify the contribution of visual stimulus features. *Cognition* **142**, 247–265 (2015).
30. D. Regan, Steady-state evoked potentials. *J. Opt. Soc. Am.* **67**, 1475–1489 (1977).
31. J. Park, A neural basis for the visual sense of number and its development: A steady-state visual evoked potential study in children and adults. *Dev. Cogn. Neurosci.* **30**, 333–343 (2018).
32. S. P. Heinrich, D. Mell, M. Bach, Frequency-domain analysis of fast oddball responses to visual stimuli: A feasibility study. *Int. J. Psychophysiol.* **73**, 287–293 (2009).
33. M. Guillaume, S. Mejias, B. Rossion, M. Dzhelyova, C. Schiltz, A rapid, objective and implicit measure of visual quantity discrimination. *Neuropsychologia* **111**, 180–189 (2018).
34. A. M. Norcia, L. G. Appelbaum, J. M. Ales, B. R. Cottareau, B. Rossion, The steady-state visual evoked potential in vision research: A review. *J. Vis.* **15**, 4 (2015).
35. K. N. Kay, J. Winawer, A. Rokem, A. Mezer, B. A. Wandell, A two-stage cascade model of BOLD responses in human visual cortex. *PLoS Comput. Biol.* **9**, e1003079 (2013).
36. M. Dzhelyova, C. Jacques, B. Rossion, At a single glance: Fast periodic visual stimulation uncovers the spatio-temporal dynamics of brief facial expression changes in the human brain. *Cereb. Cortex* **27**, 4106–4123 (2017).
37. J. Park, N. K. DeWind, M. G. Woldorff, E. M. Brannon, Rapid and direct encoding of numerosity in the visual stream. *Cereb. Cortex* **26**, 748–763 (2016).
38. M. Fornaciai, E. M. Brannon, M. G. Woldorff, J. Park, Numerosity processing in early visual cortex. *Neuroimage* **157**, 429–438 (2017).
39. N. K. DeWind, J. Park, M. G. Woldorff, E. M. Brannon, Numerical encoding in early visual cortex. *Cortex* **114**, 76–89 (2019).
40. A. Roquet, P. Lemaire, Strategy variability in numerosity comparison task: A study in young and older adults. *Open Psychol.* **1**, 152–167 (2019).
41. S. S. Stevens, Duration, luminance, and the brightness exponent. *Percept. Psychophys.* **1**, 96–100 (1966).
42. J.-H. Nam, C. Chubb, Texture luminance judgments are approximately veridical. *Vision Res.* **40**, 1695–1709 (2000).
43. O. Katsumi, T. Hirose, T. Tsukada, Effect of number of elements and size of stimulus field on recordability of pattern reversal visual evoked response. *Invest. Ophthalmol. Vis. Sci.* **29**, 922–927 (1988).
44. A. E. Kertesz, Effect of stimulus size on fusion and vergence. *J. Opt. Soc. Am.* **71**, 289–293 (1981).
45. D. C. Burr, G. Anobile, R. Arrighi, Psychophysical evidence for the number sense. *Philos. Trans. R. Soc. B* **373**, 20170045 (2017).
46. L. He, K. Zhou, T. Zhou, S. He, L. Chen, Topology-defined units in numerosity perception. *Proc. Natl. Acad. Sci. U.S.A.* **112**, E5647–E5655 (2015).
47. T. Kluth, C. Zetzsche, Numerosity as a topological invariant. *J. Vis.* **16**, 30 (2016).
48. G. Anobile, M. Turi, G. M. Cicchini, D. C. Burr, Mechanisms for perception of numerosity or texture-density are governed by crowding-like effects. *J. Vis.* **15**, 4 (2015).
49. D. Burr, J. Ross, A visual sense of number. *Curr. Biol.* **18**, 425–428 (2008).
50. S. Cavdaroglu, A. Knops, Evidence for a posterior parietal cortex contribution to spatial but not temporal numerosity perception. *Cereb. Cortex* **29**, 2965–2977 (2019).
51. E. Castaldi, M. Piazza, S. Dehaene, A. Vignaud, E. Eger, Attentional amplification of neural codes for number independent of other quantities along the dorsal visual stream. *eLife* **8**, e45160 (2019).
52. M. Guillaume, C. Schiltz, A. Van Rinsveld, NASCO: A new method and program to generate dot arrays for non-symbolic number comparison tasks. *J. Numer. Cogn.* (2020), in press.
53. D. H. Brainard, The psychophysics toolbox. *Spat. Vis.* **10**, 433–436 (1997).
54. M. Kleiner et al., What’s new in Psychtoolbox-3? *Perception* **36**, 1–16 (2007).
55. A. Lochy, A. de Heering, B. Rossion, The non-linear development of the right hemispheric specialization for human face perception. *Neuropsychologia* **126**, 10–19 (2019).
56. R. De Keyser, A. Mouraux, G. L. Quek, D. M. Torta, V. Legrain, Fast periodic visual stimulation to study tool-selective processing in the human brain. *Exp. Brain Res.* **236**, 2751–2763 (2018).
57. T. Meigen, M. Bach, On the statistical significance of electrophysiological steady-state responses. *Doc. Ophthalmol.* **98**, 207–232 (1999).
58. J. Liu-Shuang, A. M. Norcia, B. Rossion, An objective index of individual face discrimination in the right occipito-temporal cortex by means of fast periodic oddball stimulation. *Neuropsychologia* **52**, 57–72 (2014).