REGULAR ARTICLE



The Epistemology of a Positive SARS-CoV-2 Test

Rainer Johannes Klement¹ · Prasanta S. Bandyopadhyay²

Received: 10 April 2020 / Accepted: 19 August 2020 / Published online: 4 September 2020 © Springer Nature B.V. 2020

Abstract

We investigate the epistemological consequences of a positive polymerase chain reaction SARS-CoV test for two relevant hypotheses: (i) V is the hypothesis that an individual has been infected with SARS-CoV-2; (ii) C is the hypothesis that SARS-CoV-2 is the cause of flu-like symptoms in a given patient. We ask two fundamental epistemological questions regarding each hypothesis: First, how much confirmation does a positive test lend to each hypothesis? Second, how much evidence does a positive test provide for each hypothesis against its negation? We respond to each question within a formal Bayesian framework. We construe degree of confirmation as the difference between the posterior probability of the hypothesis and its prior, and the strength of evidence for a hypothesis against its alternative in terms of their likelihood ratio. We find that test specificity-and coinfection probabilities when making inferences about C-were key determinants of confirmation and evidence. Tests with < 87% specificity could not provide strong evidence (likelihood ratio > 8) for V against \neg V regardless of sensitivity. Accordingly, low specificity tests could not provide strong evidence in favor of C in all plausible scenarios modeled. We also show how a positive influenza A test disconfirms C and provides weak evidence against C in dependence on the probability that the patient is influenza A infected given that his/her symptoms are not caused by SARS-CoV-2. Our analysis points out some caveats that should be considered when attributing symptoms or death of a positively tested patient to SARS-CoV-2.

Keywords Bayesianism · Confirmation · COVID-19 · Evidence · RT-qPCR

Rainer Johannes Klement rainer_klement@gmx.de http://www.rainerklement.com

¹ Department of Radiotherapy and Radiation Oncology, Leopoldina Hospital Schweinfurt, Robert-Koch-Straße 10, 97422 Schweinfurt, Germany

² Department of History & Philosophy, Montana State University, Bozeman, MT, USA

1 Introduction

Currently, the world is a state of emergency caused by the new virus called severe acute respiratory syndrome-corona virus-2, or short SARS-CoV-2. Coronavirus disease 2019 (COVID-19) is the term used to describe the disease symptoms caused by the SARS-CoV-2. Symptoms of COVID-19 are typically flu-like symptoms such as fever and cough and in severe cases pneumonia, which however predominantly occurs in frail patients with other comorbidities. In general, SARS-CoV-2 appears to cause similar symptoms as other coronaviruses or influenza strains (Guan et al. 2020; Shi et al. 2020).

To prevent the virus from spreading and causing symptoms and deaths, policy makers at the helm of affairs had taken dramatic measures which included the closure of kindergartens, schools and universities, restaurants, museums and shops, prohibition of gatherings, cancellation of public events and the prohibition to leave the house without good reason. These measures were justified under the premise that SARS-CoV-2 is extremely virulent. However, the validity of this premise itself is rarely investigated. In particular, which data justify this premise? It appears that the positive testing of patients and its reporting in the media play a central role in sustaining the belief in a high virulence of SARS-CoV-2 and the notion of a pandemic. Our goal here is therefore to conduct a critical analysis of the SARS-CoV-2 testing and the conclusions that can be drawn from it based on a Bayesian account of evidence and confirmation.

2 Evidence, Confirmation, and Diagnostic Testing

A comprehensive understanding of scientific hypotheses requires an understanding of scientific inference, broadly construed. However, several epistemological issues need to be distinguished in order to appreciate the proper relationship between the tenability of scientific hypotheses and inference. We will discuss the significance of these issues/questions by borrowing an insight from Richard Royall (Royall 1997, 2004). Our approach provides a unified Bayesian response to three questions posed by Royall.

Consider two hypotheses: V, stating that a patient is infected with the SARS-CoV-2, and \neg V, its denial. Assume that a SARS-CoV-2 test comes out positive. Based on this simple scenario, one could pose at least three types of question that underline the epistemological issues at stake, following an insight from Royall (1997):

- (i) Given the positive test result, what should we *believe* about V and to what degree?
- (ii) Does the positive test result provide strong *evidence* for V against its alternative $\neg V$?
- (iii) Given the positive test result, what should we do?

We call the first question the belief or confirmation question, the second the evidence question and the third the decision question. These three questions are pretheoretical and statistical paradigm-neutral; yet they require some statistical/probabilistic tools for their articulation. Here, we will confine ourselves to the first two questions and just briefly touch upon the decision question in the Discussion section.

We have developed two distinct accounts to answer the first two types of questions (Bandyopadhyay and Brittan 2006; Bandyopadhyay et al. 2016). The first is an account of belief/confirmation, the second of evidence. Our two accounts of belief/ confirmation and evidence naturally fulfill the need to have both notions of degreesof-belief and degrees-of-support pointed out by Hawthorne (2005), which not only avoids the old evidence problem but also resolves a number of other philosophical paradoxes (Bandyopadhyay et al. 2016).

For Bayesians, degrees of belief need to be finegrained (Ramsey 1926). A satisfactory Bayesian account of confirmation, according to us, should be able to capture this notion of degree of belief. In formal terms:

D confirms H to a greater degree if and only if
$$P(H|D) > P(H)$$
, (1)

where D denotes the data and H the hypothesis. Confirmation becomes strong or weak depending on how great the difference is between the posterior probability, P(HID), and the prior probability of the hypothesis, P(H). P(HID) represents an agent's degree of belief in the hypothesis after the data are accumulated. P(H) stands for an agent's degree of belief in the hypothesis before the data for the hypothesis have been acquired.

While the account of confirmation is concerned with belief in a single hypothesis, our account of evidence compares the merits of two simple statistical hypotheses, H1 and H2 (or \neg H1) relative to the data D, some auxiliaries, and background information¹. Bayesians use the Bayes factor to make this comparison, while others use the likelihood ratio (LR) or other functions designed to measure evidence. For simple statistical hypotheses/models with no free parameters², as is the case in diagnostic testing that is treated here, the Bayes factor and the LR are identical, and capture the bare essentials of an account of evidence without any appeal to prior probability. The LR in favor of H1 over H2 is

$$LR=P(D|H1)/P(D|H2)$$
(2)

The data D constitute evidence for H1 against H2 if and only if their LR is greater than one. Note that, if $1 < LR \leq 8$, then D is often said to provide weak to moderate evidence for H1 against H2, while when LR ≥ 8 , D provides strong evidence (Kass and Raftery 1995; Bandyopadhyay et al. 2016). This is also the cut-off and characterization of evidence we use in this work.

¹ The dependence on auxiliaries and background information will not be explicitly stated in the equations.

 $^{^2}$ See Bandyopadhyay et al. (1996) for a general model selection case when models have adjustable parameters.

3 Sensitivity and Specificity

In the following, we assume that testing for SARS-CoV-2 is based on reverse transcriptase-quantitative polymerase chain reaction (RT-qPCR), a biomedical testing procedure that is routinely applied for detecting and quantifying RNA. Such tests are able to detect very few numbers of nucleic acid molecules—in this case RNA—by amplifying a target nucleic acid sequence several million fold. Because RNA cannot serve as a template for PCR, the RNA template is first reversely transcribed (RT) into complementary DNA (cDNA)³ which is then exponentially amplified in a PCR over many cycles (Bustin 2000). In quantitative (also called real time) PCR one can calculate the number of DNA molecules of the amplified sequence that were initially present in the sample (Kubista et al. 2006, 96). However, for such a calculation to be reliable several operating standards should be followed closely, else sensitivity (true positive rate) and specificity (true negative rate) may be compromised (Raymaekers et al. 2009).

Upon the spread of the SARS-CoV-2 in Wuhan, China, new RT-qPCR tests have been rapidly developed. For example, Corman et al. created a test based on the closely related SARS-CoV from 2003 and got their paper published in January 2020 only two days after submission (Corman et al. 2020). Nowadays, a multitude of more or less defined commercial and laboratory "in house" tests are used, often without mandatory guidelines and adequate validation. While some of these tests have shown 100% specificity in independent validation studies (Nalla et al. 2020), others have been found to yield a significant percentage of false-negative results. For example, an early validation study of Chinese SARS-CoV-2 RT-qPCR tests revealed a false positive rate of almost 50% or higher (Zhuang et al. 2020)—however, the study was retracted for unknown reasons soon after ahead-of-print publication. In a German inter-laboratory validation study ("Ringversuch") of many commercially available and in-house RT-qPCR tests, a total of 67 out of 983 SARS-CoV-2-negative samples containing the human coronavirus HCoV 229E were classified as "positive", yielding an average false-positive rate of 6.8% (Zeichhardt and Kammel 2020). Another German laboratory found some commercial primers and probes to be contaminated with nucleotides, resulting in up to 7.3% false positive results from SARS-CoV-2-negative human throat swabs and up to 17% false positive results from swabs taken from cattle (Wernike et al. 2020). Finally, the test used by the US Center for Disease Control appears to have specificity problems, as 3/10 reference samples classified as positive by RT-qPCR did not contain SARS-CoV-2 (Lee 2020).

SARS-CoV-2 RT-qPCR tests may also have problems with sensitivity in clinical routine application. The reason is that sensitivity depends on both the site from which a sample is obtained and the time relative to symptom onset (Sethuraman et al. 2020). Xie et al. (2020) reported on five patients presenting with flu-like symptoms and radiological diagnosis of COVID-19 pneumonia, but negative RT-qPCR test

³ To provide RT enzymes a starting point for synthesis, specific primers flanking the RNA sequence to be amplified are used. Their choice is crucial for estimating the RNA copy number (Bustin 2000).

results; in these patients it took multiple re-tests to obtain a positive SARS-CoV-2 detection. Similar findings were reported by Li et al. (2020) who conducted multiple tests on the same patients diagnosed with COVID-19 but observed highly variable results. Here, 13.5% (48/355) of symptomatic patients who had initially tested negative were SARS-CoV-2 positive at the second test, and 18 patients had a positive test after two consecutive negative ones. In particular, tests based on the frequently taken nasopharyngeal swabs appear to be not very sensitive (Wu et al. 2020a). In a Chinese study on patients with confirmed COVID-19, sensitivity was only 32% (126/398) for pharyngeal swabs and 63% (5/8) for nasal swabs compared to 93% (14/15) for bron-choalveolar lavage fluid (Wang et al. 2020). This is consistent with the percentage of positive test results from nasopharyngeal swabs of COVID-19 patients by Guo et al. (2020) (51.9%) and the observations of Liu et al. (2020).

In summary we conclude that both the sensitivity and specificity of SARS-CoV-2 tests are context-dependent⁴. We therefore investigate how test inferences depend on various sensitivities and specificities for which we adopt specificity $\geq 80\%$ and sensitivity $\geq 30\%$ as realistic ranges.

4 The Base Rate

Due to the novelty of the SARS-CoV-2 and the fact that most infections remain undetected the base rates are still very uncertain. The base rate is also populationspecific and space-time-dependent. In Table 1 we have compiled several infection rate estimates from various contexts. While taking these as base rate estimates assumes perfect tests, we are not so much interested in the exact values, but in a crude realistic range for our modeling study. We see that in asymptomatic persons, most studies support a base rate between 0 and 5%, while high-risk populations range somewhere between 5% and 20% (counting the 37.9% obtained by Folgueira et al. (2020) as an outlier). Therefore, realistic base rates are somewhere in the range 0–20% which we account for by plotting base rate on a log scale in order to better visualize test inferences for low base rates.

5 The Two Questions Revisited

5.1 Basic Inferences from a Positive SARS-CoV-2 Test

Let us now assume that a person⁵ has been tested positive for SARS-CoV-2. We are interested in the following hypotheses:

V: The person is infected with the SARS-CoV-2.

 \neg V: The person is not infected with the SARS-CoV-2.

⁴ Context-dependence of test performances is not restricted to the new SARS-CoV-2 tests. The reason is that such tests are not experiments within closed systems, but are conducted on open systems that are highly responsive to their environment or the given context (Klement and Bandyopadhyay 2019).

⁵ It does not necessarily have to be a patient with symptoms.

Table 1 SARS-CoV-2 infection rates based on positive RT-qPCR test results from various settings in chronological order	n positive RT-qPCR test results	from various settings in chronological order		
Population	Time	Specimen	Infection rate	Reference
161 hospitalized children in Wuhan, China	December 1, 2019–January 16	Nasopharyngeal swab, sputum or bronchoalveolar lavage fluid	1.2%	Jian et al. (2020)
151 close household contacts of COVID-19 patients in Taiwan	January 15-March 18, 2020	NA	4.6%	Cheng et al. (2020)
32 suspected SARS- CoV-2 cases and 337 people repatriated from China	January–February, 2020	NA	%0	Colson et al. (2020)
9199 inhabitants of Iceland with high risk of infection	January 31–March 31, 2020	Nasopharyngeal and oropharyngeal swabs	13.3%	Gudbjartsson et al. (2020)
1911 symptomatic health care workers from Madrid, Spain	February 24–April 30	Nasopharyngeal swab	11.1% ^a	Suárez-García (2020)
2085 hospital healthcare workers in Madrid, Spain	March 1-29, 2020	Nasopharyngeal and oropharyngeal swabs	37.9% ^a	Folgueira et al. (2020)
131 patients with mild influenza-like illness from a Los Angeles medical center, USA	March 12–16, 2020	Nasopharyngeal swabs	5.3%	Spellberg et al. (2020)
783 asymptomatic repatriation passengers arriving in Greece	March 20–25, 2020	Oropharyngeal swabs	3.6–6.3%	Lytras et al. (2020)
210 asymptomatic pregnant women from New York, USA	March 22–April 4, 2020	Nasopharyngeal swabs	13.7%	Sutton et al. (2020)
400 asymptomatic health care workers in London hospital, UK	March 23–April 26, 2020	Nasal swabs	1.1%-7.1% (decreasing every week)	Treibel et al. (2020)
919 randomly chosen individuals from Gangelt, Germany	March 31–April 6, 2020	Pharyngeal swabs	3.59%	Streeck et al. (2020)
2283 randomly chosen asymptomatic inhabit- ants of Iceland	March 31–April 4, 2020	Nasopharyngeal and oropharyngeal swabs	0.6%	Gudbjartsson et al. (2020)
381 hospitalized patients in Wuhan, China	April 3–15, 2020	Nasopharyngeal swabs	0.3%	Wu et al. (2020b)
1021 asymptomatic resuming patients in Wuhan, China	April 3–15, 2020	Nasopharyngeal swabs	%0	Wu et al. (2020b)

We do not provide uncertainties on these estimates stemming from binomial statistics or test imperfection, since we are only interested in a crude range that the infection rates occupy

^aSome persons were tested more than once

Given the positive test result, what should we believe about the infection status of the person and to which degree? This question can be answered by calculating the posterior probability of V and comparing it to its prior probability.

Given T, the positive test result, we can derive the posterior probability of V from Bayes' theorem:

$$P(V|T) = [P(T|V) \times P(V)]/P(T)$$
(3)

$$P(T) = P(T|V) \times P(V) + P(T|\neg V) \times P(\neg V)$$
(4)

The left panel of Fig. 1 shows the degree of confirmation of the hypothesis that the person is infected as a function of the base rate plotted on a log scale and five different assumptions for test sensitivity and specificity. Even for tests with 90% sensitivity and 95% specificity, the base rate would have to exceed 5.6% in order to raise our degrees of belief in V to more than 50%, while for tests with only 30% sensitivity and 80% specificity, a base rate >40% would be required.

The right panel of Fig. 1 shows the LR as a function of the test sensitivity for two assumed test specificities (=1–P(T \neg V)). For 80% specificity, one would not be justified to speak of a positive test result as providing strong evidence in favor of V, regardless of test sensitivity; more generally, this holds for any specificity falling below 87%. If test specificity is 95%, however, evidence for V would become strong for sensitivity >40%.

5.2 COVID-19 and a Positive SARS-CoV-2 Test

Imagine now a patient presenting with flu-like symptoms. Borghetti et al. (2020) have pointed out that patients being tested positive for SARS-CoV-2 could have co-infection with other pathogens, and listed several other viruses and bacteria that are able to cause symptoms similar to COVID-19⁶. By now, several case reports (Borghetti et al. 2020; Cuadrado-Payán et al. 2020; Wu et al. 2020a) and cohort studies (Jian et al. 2020; Kim et al. 2020; Lin et al. 2020) have revealed that co-infections between SARS-CoV-2 and other respiratory pathogens occur. Being aware of the fact, we therefore pose the following hypothesis:

C: SARS-CoV-2 infection has caused the flu-like symptoms of the patient.⁷

Implicit in this notion of causation is a presupposition that there exists at least one biological mechanism explaining how the virus can cause flu-like symptoms (Russo and Williamson 2007). This we take as our background knowledge that we do not explicitly state in the following equations. Given that COVID-19 has many symptoms in common with other viruses or common hospital bacteria, the negation of C could be conceived as the catch-all hypothesis for all these other possible causes:

 \neg C: A pathogen other than SARS-CoV-2 has caused the flu-like symptoms of the patient.

⁶ Among them are adenovirus, bocavirus, other coronaviruses, influenza viruses, rhinovirus or the bacteria Chlamydophila pneumoniae and Mycoplasma pneumoniae.

⁷ This is what some media reports implicitly assume to be true given a positive test.

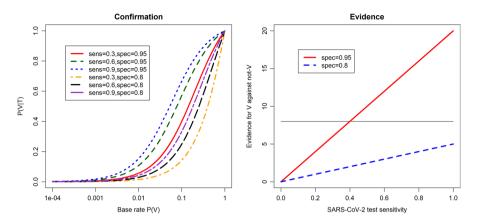


Fig. 1 Left: Posterior probability for the hypothesis V ("The tested patient is infected with the SARS-CoV-2") as a function of the prior probability or base rate P(V) plotted on a log scale. Right: Evidence measured by the likelihood ratio as a function of the test sensitivity with specificity fixed at 0.95 or 0.9, respectively. The black straight line denotes the threshold of a likelihood of 8 above which we speak of strong evidence for the hypothesis V

Therefore:

 \neg C &V: SARS-CoV-2 infection is associated with but has not caused the symptoms of the patient. ⁸

Now imagine a SARS-CoV-2 test is conducted and turns out positive. We can then ask to what degree the positive test result confirms hypothesis C. To this end, we construct the simple Bayesian network model depicted in Fig. 2. The SARS-CoV-2 test assesses the truth of the hypothesis V, that the patient has the SARS-CoV-2 infection. As above, T stands for a positive test result. We conceive of V as a testable consequence of the hypothesis C. The truth of C is both a necessary and sufficient condition for the truth of V, because if C is true for a given patient it deductively follows that he/she must be infected with SARS-CoV-2.

From this it follows that

$$P(V|C) \equiv p = 1 > P(V|\neg C) \equiv q$$
(5)

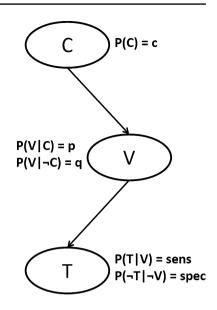
$$P(C|\neg V) = (P\neg V|C) = 0$$
(6)

$$P(T|C) = P(T|V) = sens$$
(7)

To calculate the degree of confirmation given to C by a positive test report, we need to calculate

⁸ In principle, we can let \neg C include the case that both SARS-CoV-2 and another pathogen cause the symptoms together, so that \neg C &V means "SARS-CoV-2 infection is associated with but has not *solely* caused the symptoms of the patient". For simplicity, however, we continue by assuming the mono-causal scenario.

Fig. 2 Bayesian network model of the relationship between a positive test T and hypothesis C



$$P(C|T) = P(T|C) \times P(C)/P(T) = \frac{P(T|C)P(C)}{P(T|C)P(C) + P(T|\neg C)P(\neg C)}$$
(8)

Defining $c \equiv P(C)$, Eq. (8) becomes

$$P(C|T) = \frac{c}{c + (1 - c) \frac{P(T|\neg C)}{P(T|C)}}$$
(9)

To calculate the LR in the denominator of Eq. (9) in terms of sensitivity and specificity, we re-express the likelihood $P(T \mid \neg C)$ using the definition of conditional probability:

$$P(T|\neg C) = \frac{P(T\&\neg C)}{P(\neg C)}$$
(10)

Furthermore, according to the law of total probability (Pearl et al. 2016):

$$P(T\&\neg C) = P(T\&\neg C\&V) + P(T\&\neg C\&\neg V)$$
(11)

We apply the product rules (Pearl et al. 2016) for the Bayesian network structure shown in Fig. 2 to calculate the total probabilities in Eq. (11):

$$P(T\&\neg C) = P(\neg C) P(V|\neg C) P(T|V) + P(\neg C) P(\neg V|\neg C) P(T|\neg V),$$
(12)

By inserting Eq. (12) into (10), we obtain

$$P(T|\neg C) = P(V|\neg C) P(T|V) + P(\neg V|\neg C) P(T|\neg V)$$
(13)

or, using the notations given in Fig. 2:

Deringer

$$P(T|\neg C) = q \cdot \text{sens} + (1-q)(1-\text{spec})$$
(14)

We define the LR \equiv x and use Equations (7) and (14):

$$x = \frac{P(T \mid \neg C)}{P(T \mid C)} = \frac{q \cdot \text{sens} + (1 - q)(1 - \text{spec})}{\text{sens}}$$
(15)

Inserting (15) into (9) we get

$$P(C|T) = \frac{c}{c + (1 - c)x}$$
(16)

Note that $q \equiv P(V \mid \neg C)$ in Eq. (15) is the proportion among symptomatic cases not caused by SARS-CoV-2 which in addition to the symptom-causing pathogen carry the SARS-CoV-2. To obtain a reference point and upper limit for the magnitude of q, we therefore look at percentages of symptomatic patients with confirmed non-SARS-CoV-2 respiratory pathogen infection who additionally were tested positive for SARS-CoV-2. Such co-infection rates were found to vary from 0/3380 in French patients tested since January 1 2020 (Colson et al. 2020) to 2/239 (0.8%) in Chinese children (Jian et al. 2020), 6/186 (3.2%) in Chinese adults (Lin et al. 2020) and 24/318 (7.5%) in Californian patients (Kim et al. 2020). Based on these data, we set an upper limit of q at 10%.

In Fig. 3 we plot the posterior P(C|T) against the prior probability P(C), adopting four different values for q: 0.5%, 2.5%, 5% and 10%. It can be seen that the confirmation we gain in the hypothesis C depends on its prior, the value for q and more on the specificity of the test than its sensitivity. As q increases, the confirmation of C provided by a positive test result becomes weaker and less dependent on the test performance, in particular specificity. However, even in the scenario where 10% of patients having symptoms not caused by SARS-CoV-2 are co-infected with SARS-CoV-2, a positive test would raise our degrees of belief in C to more than 50% if the prior probability c would exceed 29%. This may be a reasonable assumption during the height of the COVID-19 transmission curve in a given country.

In Fig. 4 we have plotted the evidence provided by a positive test result for the hypothesis C against \neg C as a function of the test sensitivity for different fixed values of specificity and q. Note that in the depicted situations a positive test always constitutes evidence for C (likelihood ratio > 1). This is consistent with the theorem that data constitute evidence for a hypothesis against its mutually exclusive and jointly exhaustive alternative if and only if the data confirm the hypothesis to a certain degree (Bandyopadhyay et al. 2016). Figure 4 shows that the evidence for C against \neg C is moderate to weak if test specificity is only 80%, even for 100% sensitive tests and very low q. For q=10%, this is also the case for highly specific (95%) tests. In scenarios with small probability of co-infection with SARS-CoV-2 (q=0.5%–5%) a positive test is able to provide strong evidence for C. Note however, that even for q=0.5%, the evidence for C against \neg C is not strong if sensitivity ranges below 40%; such low sensitivity may be characteristic of RT-qPCR tests on pharyngeal swabs (Wang et al. 2020), so that tests using these specimen may generally be considered to allow no strong evidential inferences.

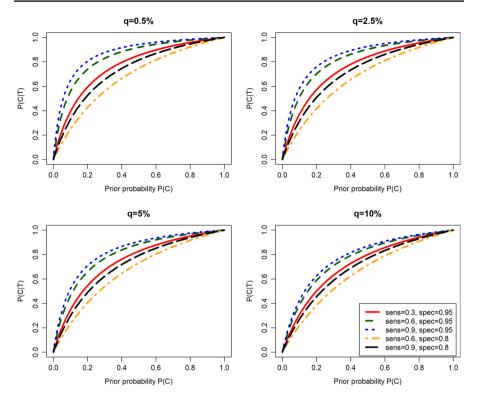


Fig.3 Confirmation of the hypothesis C (that SARS-CoV-2 caused the COVID-19-like symptoms of a patient) by a positive test as a function of the prior probability for C, $q \equiv P(V|\neg C)$ and different test performances

5.3 COVID-19 and a Positive Test for Influenza A

Influenza A is one of the dominating respiratory viruses responsible for causing flu-like symptoms (Nickbakhsh et al. 2019). Coinfection of influenza A and SARS-CoV-2 has been documented (Cuadrado-Payán et al. 2020; Kim et al. 2020; Nowak et al. 2020; Wu et al. 2020a). Imagine now that instead of a SARS-CoV-2 test, a test for influenza A has been performed in a patient with flu-like symptoms and came out positive. How does this affect an agent's degree of belief in C and the evidence for C against its alternative? Using a model with the same structure as Fig. 2 and similar notation as above, let T' denote the positive test result (now for influenza A) and V' the hypothesis that an influenza A infection is present. However, now we do not have a deductive relationship between C and V' as was the case in the SARS-CoV-2 test example. Instead, V' can be conceived as a testable consequence of C in the sense that $P(V'|C) < P(V'|\neg C)$.

⁹ We thereby apply a similar definition of the testable consequence as Bovens and Hartmann (2003) in their chapter on confirmation (page 90), the difference being that the probability of the consequence given that the hypothesis is false is greater than the probability of the consequence given that the hypothesis is true in our case, while it is the other way around in Bovens and Hartmann (2003).

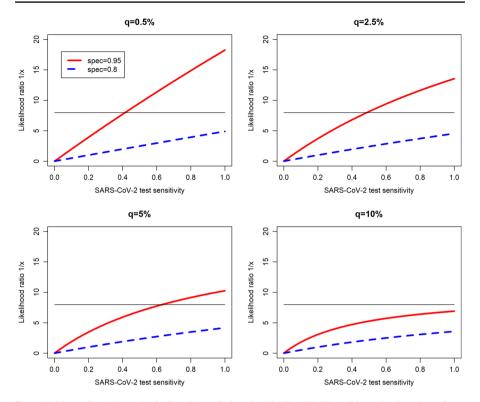


Fig. 4 Evidence for the hypothesis C against \neg C given by 1/x (Eq. 15). The evidence is plotted as a function of the test sensitivity for fixed specificity of 80% and 95%, respectively, and different values of q, the probability that a patient who has symptoms caused by a pathogen other than SARS-CoV-2 additionally has SARS-CoV-2 coinfection. The black solid line denotes the threshold of strong evidence (1/x = 8)

assume q'>p' because if C is true, it follows deductively that the patient must have SARS-CoV-2, so that p' is the probability of a co-infection of SARS-CoV-2 with influenza A which appears to be $\approx 1\%$ (Kim et al. 2020). In contrast, if \neg C is true, the symptoms are caused by a pathogen other than SARS-CoV-2, so q' represents the sum of (i) the probability of a single influenza A infection plus (ii) the probability of co-infection of a non-SARS-CoV-2 pathogen with influenza A plus (iii) the probability of SARS-CoV-2 infection not causing the symptoms with influenza A causing the symptoms. The prevalence of influenza A infection among symptomatic patients testing negative for SARS-CoV-2 ranges from 10/845 (1.2%) (Nowak et al. 2020) over 29/1101 (2.6%) (Kim et al. 2020) to 794/3380 (23.5%) (Colson et al. 2020). In these patients, because SARS-CoV-2 was not detected, we assume that \neg C was true. We also neglect any imperfections of the influenza A tests so that these fractions give us a crude lower limit for realistic estimates of q' and show that the assumption q'>p' is justified. Accordingly, we set p'=1% and vary q' from 1.2–25%.

The LR for the case of a positive influenza A test is

$$\mathbf{x}' = \frac{\mathbf{P}(\mathbf{T}'|\neg \mathbf{C})}{\mathbf{P}(\mathbf{T}'|\mathbf{C})} \tag{17}$$

The numerator in the LR can be re-formulated analogous to Eq. (14). A similar derivation of the denominator gives

$$P(T'|C) = \frac{P(T'\&C)}{P(C)} = \frac{P(T'\&C\&V') + P(T'\&C\&\neg V')}{P(C)} = P(V'|C)P(T'|V') + P(\neg V'|C)P(T'|\neg V')$$
(18)

Using q' > p', we thus obtain

$$x' = \frac{q' \cdot \text{sens}' + (1 - q')(1 - \text{spec}')}{p' \cdot \text{sens}' + (1 - p')(1 - \text{spec}')} = \frac{(\text{sens}' + \text{spec}' - 1)q' + 1 - \text{spec}'}{(\text{sens}' + \text{spec}' - 1)p' + 1 - \text{spec}'} > 1$$
(19)

Hereby, sens' and spec' denote the sensitivity and specificity, respectively, of the influenza A test. These are better known than for the new SARS-CoV-2 test. We adopt the values derived by López Roa et al. (2011) for the influenza A RTqPCR test which were obtained by comparison to conventional cell culture as the gold standard. These are sens'=95.6%, spec'=82.3%. Figure 5 plots the disconfirmation of C constituted by a positive influenza A test for five different values of q' (left panel) as well as the evidence for \neg C against C as a function of q' (right panel). Two results can be read off the graph: First, the smaller the chance of having infection with influenza A given that the symptoms are not caused by SARS-CoV-2, the stronger a positive influenza A test for influenza A would only constitute weak evidence for the hypothesis that the symptoms are caused by a pathogen other than SARS-CoV-2 (\neg C) against C.

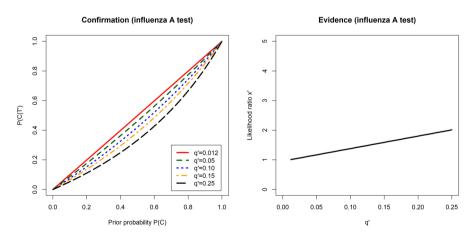


Fig. 5 (Dis-)confirmation of C and evidence of \neg C against C (Eq. 19) constituted by a positive influenza A test in dependence of q', the probability of having an influenza A infection when the symptoms are not caused by SARS-CoV-2

6 Discussion

We here provided a critical investigation of the inferences that can be drawn from a positive SARS-CoV-2 RT-qPCR test result for two main hypotheses: One is that a person is infected with SARS-CoV-2 (hypothesis V), the second that the flu-like symptoms of a patient are caused by this virus (C) and not any other pathogen (\neg C). The two epistemological questions we posed are: Given a positive SARS-CoV-2 test result (i) what should we believe about each hypothesis to what degree? (ii) What is the evidence for each hypothesis compared to its negation?

We found that even for tests with 90% sensitivity and 95% specificity, the base rate would have to exceed 5.6% in order to raise our degrees of believe in V to more than 50%, while for tests with only 30% sensitivity and 80% specificity, a base rate > 40% would be required. Since base rates > 40% are probably unrealistic (Table 1), but sensitivity around 30% has been reported for pharyngeal swabs (Wang et al. 2020), tests based on pharyngeal swab specimen would not convince a rational agent that the tested person is infected with SARS-CoV-2. In addition, if the test would only have 80% specificity, positive tests cannot provide strong evidence (LR > 8) in favor of V against \neg V (Fig. 1, right panel). Qualitatively, the same result was obtained regarding hypothesis C (Fig. 4). Thus, sample handling and contamination that might compromise specificity become crucial.

The degree of confirmation for C was found to highly depend on the test specificity and in addition on the probability that a patient has asymptomatic SARS-CoV-2 coinfection when in fact his or her symptoms are caused by another pathogen. If this probability (that we denoted as q) is low, the degree of confirmation becomes high, and vice versa, *ceteris paribus*.

Finally, we showed that a positive influenza A test would disconfirm C to a degree depending on the probability that the patient has influenza A infection given that his or her symptoms are not caused by SARS-CoV-2. As this probability, denoted q', increases, the degree of disconfirmation also increases, *ceteris paribus*. However, a positive influenza A test provides only weak evidence against C for the realistic ranges of q' considered. This is mainly because (i) we adopted a realistic assumption about the prevalence of influenza A infections that, despite being a very frequent pathogen causing flu-like symptoms, is less than about 25%, and (ii) because the test specificity for influenza A was only 82.3%.

Our analysis points out that one should be careful in ascribing the symptoms or death of a positively tested patient to COVID-19, if the possibility exists that the disease has been caused by another pathogen. To rule out the second possibility, one would have to test for all other possible symptom causes, which in practice is rarely attempted, and complicated by the fact that such tests are also not 100% sensitive.

Since COVID-19 is a novel disease and most tests used in practice have not been adequately validated, there are still many uncertainties associated with basic statistical quantities that we used in our modeling. We tried to account for these uncertainties by assuming several plausible values for the variables in our modeling. Yet, these uncertainties pose the major limitation of this work. In particular, the probability of having coinfection with SARS-CoV-2 when in fact the symptoms are caused by another pathogen is crucial to the inference that can be made from a positive SARS-CoV-2 test and should be investigated in future studies.

We now briefly turn to the third epistemological question that we posed in the beginning, but so far have neglected: Given a positive test result, what should we do? We can conclude that unless one is certain that the test has a high specificity, clinical decision making should not be based solely on such tests. To test specificity, Wernike et al. (2020) recommended to pre-test each batch of PCR reagents at least 50 times with negative control samples. Furthermore, given that COVID-19 might show a seasonality similar to other human coronaviruses (Olofsson et al. 2011; Nickbakhsh et al. 2019; Monto et al. 2020) and that similar symptoms might be caused by certain bacteria (Lin et al. 2020), the possibility of other viral or bacterial infections should always be considered. That this approach is feasible has been shown by initial studies (Jian et al. 2020; Kim et al. 2020; Lin et al. 2020; Nowak et al. 2020). In general, policy makers and the media should recognize the limitations of the new SARS-CoV-2 tests and consider the possibility that deceased patients who were tested positive for this virus might only have died with but not because of it.

Acknowledgements We thank Prof. Dr. Ulrike Kämmerer for helpful discussions of the RT-qPCR method and constructive comments. We also thank Prof. Gordon Brittan Jr., Prof. Palash Sarkar and an anonymous reviewer for helpful comments on a previous version of this paper.

Author contribution RJK conceived of the presented idea and wrote the manuscript; PSB developed the theoretical conceptions and supervised the project. Both authors discussed the results and contributed to the final manuscript.

Funding This research received no external funding.

Compliance with Ethical Standards

Conflicts of interest The authors declare that they have no competing interests relevant to this research.

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