# Gene expression

# A note on the false discovery rate of novel peptides in proteogenomics

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Received on February 2, 2015; revised on May 13, 2015; accepted on May 27, 2015

### Abstract

**Motivation**: Proteogenomics has been well accepted as a tool to discover novel genes. In most conventional proteogenomic studies, a global false discovery rate is used to filter out false positives for identifying credible novel peptides. However, it has been found that the actual level of false positives in novel peptides is often out of control and behaves differently for different genomes.

**Results:** To quantitatively model this problem, we theoretically analyze the subgroup false discovery rates of annotated and novel peptides. Our analysis shows that the annotation completeness ratio of a genome is the dominant factor influencing the subgroup FDR of novel peptides. Experimental results on two real datasets of *Escherichia coli* and *Mycobacterium tuberculosis* support our conjecture.

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# **1** Introduction

Tandem mass spectrometry (MS/MS)-based proteogenomics (Jaffe *et al.*, 2004) has been applied to refinement of annotated genes, discovery of novel genes (Kim *et al.*, 2014), personal genomics and disease-related studies (Zhang *et al.*, 2014). Unlike traditional genomic annotation techniques, such as *in silico* (*ab initio* or comparative) or cDNA-seq-based methods, proteogenomics allows validating proteincoding genes directly at the protein level, which is more favorable (Renuse *et al.*, 2011). To identify novel genes, researchers usually search the experimental MS/MS spectra against a large protein database that is constructed from the genomic or transcriptomic sequences and filter the search results to control the false discovery rate (FDR). It has been observed previously that, under a fixed FDR, the inflated database generated by, e.g. six-open-reading-frame (6-ORF) translation of a whole

genome significantly decreases the sensitivity of peptide identification (Blakeley *et al.*, 2012). However, few studies probe into the effect of the large database on the estimated FDR, especially for the novel peptides.

Most proteogenomic studies estimate a global FDR for all peptide identifications (Borchert *et al.*, 2010; Chaerkady *et al.*, 2011; Merrihew *et al.*, 2008). That is, the identifications of annotated peptides and novel peptides are subject to FDR estimation in combination. Some researchers noted the high actual FDR of novel peptides and therefore employed more stringent filtering strategies, e.g. post error probability (Brosch *et al.*, 2011) or separate FDRs for annotated and novel peptides (Branca *et al.*, 2014). Recently, Krug *et al.* (2013) highlighted that for well-annotated genomes, such as the *Escherichia coli* genome, the post error probability distribution of

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novel peptide hits is almost identical to that of decoy hits, indicating that most novel peptides were false positives. Krug's work implied that the identification accuracy of novel peptides is greatly affected by the completeness of genome annotation.

In fact, the relationship between annotated and novel peptides is quite similar to that between unmodified and modified peptides. Recently, Fu has formally studied the factors that influence the subgroup FDRs of differently modified peptides (Fu, 2012; Fu and Qian, 2014). Here, we follow the same framework as in Fu's work to quantitatively investigate the subgroup FDRs of annotated and novel peptides identified by 6-ORF translation search.

### 2 Methods

Let subscript  $k \in \{\text{ann}, \text{new}\}\$  denote the subgroup of annotated (ann) and novel (new) peptide identifications, respectively. Here, the novel peptides are those from the previously unannotated region on a genome, excluding the peptide variants resulting from DNA mutation or mRNA alternative splicing. Then following Fu's formalization, we define (i) *T*, a true peptide identification; (ii) *F*, a false peptide identification; (iii) *I<sub>k</sub>*, a peptide identification belonging to subgroup *k*; (iv) FDR(*x*), the global FDR of peptide identifications that score better than *x*, where both annotated and novel peptides are included; (v) FDR<sub>*k*</sub>(*x*), the subgroup FDR, e.g. FDR<sub>ann</sub>(*x*) for annotated peptides and FDR<sub>new</sub>(*x*) for novel ones. Following the derivation by Fu and Qian (2014), FDR<sub>*k*</sub>(*x*) can be written as

$$FDR_k(x) = \frac{FDR(x)}{FDR(x) + \frac{P(I_k|T,X>x)}{P(I_k|F,X>x)} \left(1 - FDR(x)\right)},$$
(1)

where  $P(I_k|T, X > x)$  is the probability that an identification belongs to subgroup k under the condition that this identification is true and scores better than x, and  $P(I_k|F, X > x)$  is the probability that an identification belongs to subgroup k under the condition that this identification is false and scores better than x. Equation (1) implies that FDR<sub>k</sub>(x) is determined by three variables, i.e. FDR(x),  $P(I_k|T, X > x)$  and  $P(I_k|F, X > x)$ .

To make the relationship in Equation (1) computable, we need to evaluate  $P(I_k|T, X > x)$  and  $P(I_k|F, X > x)$ , for both annotated and novel peptides. Note that we assume FDR(x) can be readily estimated using some methods, e.g. the commonly used target-decoy search strategy (Elias and Gygi, 2007). For convenience of discussion, we introduce two quantities: (i)  $\theta$ , the annotation completeness ratio, defined as the length ratio of the currently annotated genes to all genes on the genome; (ii)  $\mu$ , the annotation length ratio, defined as the length ratio of currently annotated genes to the whole genome. Presuming that only one gene exists at any genomic locus, the value scope of  $\mu$  is [0, 1]. Actually,  $\mu$  varies across species even if their genomes are well annotated (for *E.coli* it is about 0.88 and for *Homo sapiens*, it is less than 0.02). However, for a poorly annotated genome,  $\mu$  is relatively small, and we have  $\mu = 0$  if no gene is annotated.

Suppose that the annotated and novel peptides could be equally likely retrieved by the search engine and their scores are identically distributed, then apparently, we have  $P(I_{ann}|T, X > x) = \theta$  and  $P(I_{new}|T, X > x) = 1 - \theta$ .  $P(I_k|F, X > x)$  depends on the sizes of the annotated database and the translated database. Given the genome length *L*, the summed length of annotated genes is  $\mu L$ . If falsely identified peptides distribute uniformly on the genome, we have  $P(I_{ann}|F, X > x) = \mu L/6L = \mu/6$  and  $P(I_{new}|F, X > x) =$  $(6 - \mu)/6$ . So far, we have obtained the probabilities that an identified peptide is an annotated or novel peptide given that this identification is true or false and scores better than *x*, as summarized in Table 1.

Now we first come to the formulation of  $FDR_{ann}(x)$ :

$$FDR_{ann}(x) = \frac{FDR(x)}{FDR(x) + \frac{6\theta}{\mu} \left(1 - FDR(x)\right)}.$$
 (2)

The value of  $\mu/\theta$  represents the length proportion of all genes on the genome and is a constant for a certain species. Therefore, we can conclude that FDR<sub>ann</sub>(*x*) depends only on FDR(*x*).

Similarly, we can write  $FDR_{new}(x)$  as

$$FDR_{new}(x) = \frac{FDR(x)}{FDR(x) + \frac{6(1-\theta)}{6-\mu} \left(1 - FDR(x)\right)}.$$
(3)

If a genome has never been annotated  $(\theta = 0, \mu = 0)$ , then no identification could be an annotated peptide and  $FDR_{new}(x) = FDR(x)$ , which is consistent with the assumption. If a genome is completely annotated ( $\theta = 1$ ), then FDR<sub>new</sub>(x) = 1, meaning that all novel peptide identifications are false, which is also consistent with the assumption; in this case, as FDR(x) and  $\mu$  are usually very small,  $FDR_{ann}(x)$  approximately equals  $\mu/6$  of FDR(x). If we take FDR(x) = 1%, the  $FDR_{ann}(x)$  is only 1.5% for *E.coli*  $(\mu = 0.88)$  and 0.03‰ for *H.sapiens* ( $\mu < 0.02$ ), much more conservative than FDR(x). On the other hand, if we assume  $\theta = 0.999$ ,  $\mu$ = 0.6 and FDR(x) = 1%, then we have  $P(I_{new}|T, X > x) = 1/1000$ and  $P(I_{\text{new}}|F, X > x) = 9/10$ . The calculated FDR<sub>new</sub>(x) is 90.1%, as large as 90 times of FDR(x). In contrast, the  $FDR_{ann}(x)$  is only 1‰. We can see that for well annotated genomes,  $FDR_{ann}(x)$  is overestimated, while  $FDR_{new}(x)$  is underestimated, if a global FDR is controlled.

Since  $0 \le \mu \le 1$ , we have  $5/6 \le P(I_{new}|F, X > x) \le 1$ . It is easy to deduce from Equation (3) that  $\mu$ , as a parameter quantitatively reflecting the length ratio of the annotated genes to the whole genome, has little influence on FDR<sub>new</sub>(*x*). Let us take FDR(*x*) = 1%, then for different  $\theta$ , the upper and lower bounds (occurring when  $\mu = 0$ and  $\mu = 1$ , respectively) of FDR<sub>new</sub>(*x*) can be calculated and are depicted by the dashed blue and solid red lines, respectively, in Figure 1. It is worth emphasizing that FDR<sub>new</sub>(*x*) is less than 10% if  $\theta$  does not exceed 90%. However, as  $\theta$  increases over 90%, FDR<sub>new</sub>(*x*) ramps up quickly to a much higher level. Thus, we conclude that  $\theta$ significantly affects FDR<sub>new</sub>(*x*). Nevertheless, given FDR(*x*) = 1%, the maximum difference between the upper and lower bounds of FDR<sub>new</sub>(*x*) is less than 4.6%, and thus  $\mu$  does not substantially change FDR<sub>new</sub>(*x*), just as we deduced above.

## **3 Results**

By removing some genes from a completely annotated database based on their summed length, we could perform numerical simulation of  $\theta$ . Then, experimental FDR<sub>ann</sub>(*x*), which is the ratio of the number of identified annotated decoys to the number of annotated targets, and FDR<sub>new</sub>(*x*), which is the ratio of the number of identified novel decoys to the number of novel targets, can be calculated and compared to the theoretical ones [computed by Equations (2) and (3)]. On the basis of this idea, we experimentally validated our theoretical model on two species, i.e. *E.coli* and *Mycobacterium tuberculosis*.

#### 3.1 Results on E.coli

Krug *et al.* (2013) concluded that the *E.coli* genome might have achieved a complete annotation. We downloaded one of these *E.coli*'s datasets from PeptideAtlas, which consisted of six raw files

Table 1. The probabilities and their estimates used in this article

Identification type	True positive	False positive
Annotated identification Novel identification	$\begin{split} P(I_{\text{ann}} T,X > \mathbf{x}) &= \theta \\ P(I_{\text{new}} T,X > \mathbf{x}) &= 1 - \theta \end{split}$	$\begin{split} P(I_{\text{ann}} F,X>x) &= \mu/6\\ P(I_{\text{new}} F,X>x) &= (6-\mu)/6 \end{split}$



Fig. 1. The upper and lower bounds of  $FDR_{new}(x)$  when FDR(x) = 1%

(trypsin digested, SAX\_01~SAX\_06), 300032 MS/MS spectra in total. The latest genome sequence and annotation data (NC\_000913.3) were downloaded from the NCBI website. First, a stop-to-stop 6-ORF translation was applied to the E.coli's genome, and a commonly used contaminant database containing porcine trypsin and human keratins was concatenated. The simply reversed form of each protein sequence in the combined database was added, resulting in a combined target-decoy database to facilitate FDR estimation (Elias and Gygi, 2007). Next, the MS/MS spectra were searched against the combined database using pFind studio (version 2.8). Peptides were digested in silico with up to two missed cleavages allowed, and carbamidomethylation on cysteine was set as the fix modification and oxidation on methionine as the variable modification. The precursor and fragment mass error tolerances were set to  $\pm$  20 ppm and  $\pm$  0.5 Da, respectively. A global peptide-level FDR of 1% was used for quality assessment, which allowed us to identify 12835 peptides. Among these peptides, 113 were contaminant ones, 12619 were annotated ones and 103 were novel ones. Since the E.coli's genome has been almost completely annotated, the 103 novel target identifications should be mostly false ones. Just as expected, among the 128 decoy identifications above the threshold of FDR < 1%, 97 were novel decoys, very close to the number of novel targets, indicating that the subgroup FDR of novel peptides was close to 1 (97/103 = 0.94).

To simulate  $\theta$ , we randomly removed some genes from the annotated database to vary the ratio of their summed length to all genes. Using the same global FDR threshold of 1%, we obtained the numbers of targets and decoys separately on annotated and novel peptides, allowing us to calculate the experimental FDR<sub>ann</sub>(*x*) and FDR<sub>new</sub>(*x*). Given  $\theta$  and  $\mu$ , the theoretical FDR<sub>ann</sub>(*x*) and FDR<sub>new</sub>(*x*) were also calculated through Equations (2) and (3). Our simulation showed that, the experimental FDR<sub>ann</sub>(*x*) were close to the theoretical value of 1.5‰, with a minimum of 2.1‰ and a maximum of 3.6‰. Moreover, the experimental FDR<sub>new</sub>(*x*) fits well with the theoretical counterpart, as shown in Figure 2A. On the other hand, we can deduce the value of  $\theta$  from the experimental FDR<sub>new</sub>(*x*) based on Equation (3). As shown in Figure 2, the pairs of sampled and deduced values of  $\theta$  distribute diagonally, indicating that



**Fig. 2.** Simulation results on the *E.coli* and *M.tuberculosis* datasets. To simulate partial annotation, we randomly removed some annotated genes from the database. Gene sampling was performed on the basis of  $\theta$ , with a step of 0.1 from 0 to 1, and in addition, 0.95 and 0.99 were also appended. (A) The experimental FDR<sub>new</sub>(*x*) obtained on the *E.coli* dataset as shown by red crosses fits well with the theoretical value (blue line). The deduced values for  $\theta$  were approximately identical to the sampled ones, as shown by magenta triangles on the diagonal line. (B) On the *M.tuberculosis* dataset, genes were sampled 10 times for each value of  $\theta$ . The experimental FDR<sub>new</sub>(*x*) values as shown by red boxes fit well with the theoretical values (blue line) when  $\theta$  is less than 0.9. As truly novel peptides may exist, the experimental FDR<sub>new</sub>(*x*) diverges from the theoretical counterpart. The experimental FDR<sub>new</sub>(*x*) is 0.69 when sampled  $\theta = 1$ , and the deduced  $\theta$  is 0.996 correspondingly. However, all deduced values for  $\theta$  still match the sampled ones (green box), since the annotation completeness ratio is very close to 1

the deduced  $\boldsymbol{\theta}$  could be used as an estimate of the real annotation completeness ratio.

We also found that if we remove the 'novel genes' from the annotated database and search the spectra of novel peptides (identified by 6-ORF translation search) against the partially annotated database, then these spectra will be assigned with false peptides and random scores (see Supplementary Materials S2 and S3 for more details).

### 3.2 Results on M.tuberculosis

*M.tuberculosis* is another organism that has undergone several proteogenomic studies (de Souza *et al.*, 2008; Kelkar *et al.*, 2011).

The annotation length ratio of *M.tuberculosis* is about 0.91, and its genome is featured by the high GC content. Therefore, we selected *M.tuberculosis* as the second organism to verify our model. A dataset of 503 933 MS/MS spectra was generated

(see Supplementary Method for details of the data) and were searched against the translated genome (NC\_018143.2) under the same parameter setting as for *E.coli*. The search resulted in 28 545 target peptides identified, including 682 contaminant ones, 27 528 annotated ones and 335 novel ones. Meanwhile, a total of 230 novel decoys were obtained above the peptide-level FDR of 1%, leading to an experimental FDR<sub>new</sub>(*x*) of 0.69 (=230/335) and a deduced  $\theta$  of 0.996, which was calculated through Equation (3). The disparity between the numbers of novel targets and decoys implies that a set of truly novel peptides may exist in *M.tuberculosis*. We performed a blast search for the 105 (=335 – 230) top-scoring novel peptides and found that 68 of them have been annotated in other mycobacterial species, meaning that they are conservative and reliable. The rest of them should be experimentally validated through further efforts.

The same simulation experiment of  $\theta$  as done on *E.coli* was also tested on *M.tuberculosis*. The deduced values of  $\theta$  are in line with the theoretical ones on differently sampled  $\theta$ , as shown in Figure 2B. The experimental FDR<sub>new</sub>(x) also fits well with the theoretical counterpart for smaller  $\theta$ . However, the experimental FDR<sub>new</sub>(x) apparently deviates from its theoretical value when  $\theta \ge 0.95$ , because of the existence of truly novel peptides. This result shows that *M.tuberculosis* is not so completely annotated as *E.coli*, and FDR<sub>new</sub>(x) is sensitive to the incomplete annotation, even when  $\theta$  approaches 1.

In some previous researches, a filter of protein length is applied to the translated database. To test the influence of this operation on our model, we used four length filters of 30, 50, 100 and 500 to modify the original translated database of *M.tuberculosis*. The search results upon these four modified databases show that, a small length filter ( $\leq 100$ ) causes minor effect on the theoretical estimation of FDR<sub>new</sub>(*x*) and the deduced  $\theta$  calculated by Equation (3). However, a large filter such as 500, which removes 80% of annotated genes in *M.tuberculosis*, greatly shrinks the sample space of novel peptides and biases the estimation. In this situation, Equation (3) should be modified to fit the experimental data consequently (Supplementary Fig. S2). Therefore, to appropriately use the estimation in Equation (3), a suitable length filter (e.g.  $\leq 100$ ) is necessary.

#### 4 Discussions

Above, we have assumed that the annotated and novel peptides distribute equally in the expressed and unexpressed proteins. Since not all proteins are expressed in a specific sample under a specific condition, estimation of  $P(I_k|T, X > x)$  becomes harder. In fact, novel peptides in nearly completely annotated organisms may have lower expression levels or worse scores, because more abundant and better scoring peptides are easier to annotate, and accordingly,  $P(I_{\text{new}}|T, X > x)$  is smaller. This can lead to a larger FDR<sub>new</sub>(x) and hence less credible novel peptide identifications.

The peptide variants resulted from DNA mutation or mRNA alternative splicing are sometimes also considered as novel peptides. However, these variants are much like protein modifications, the sample space of which is difficult to estimate explicitly. Definitely, great care should be taken when reporting these variants, because the search space of these peptides become even larger, and according to Fu's (2012) corollary, more false positives will appear if a global FDR is used.

In this article, we have revealed that the genome annotation completeness ratio is the dominant factor influencing the identification accuracy of novel peptides identified by 6-ORF translation search when a global FDR is used for quality assessment. The subgroup FDR of novel peptides will be seriously under-estimated if the genome has been well annotated (e.g. when the annotation completeness ratio exceeds 90%). For such well-annotated genomes, separate FDR control is very necessary as recently suggested by Nesvizhskii (2014).

However, with a stringent FDR control (e.g. 1%), many low scoring but true peptide identifications may be excluded along with false positives. To increase the sensitivity and specificity of novelgene discovery, one should reduce the size of searched database as much as possible (Nesvizhskii, 2014). For example, when the transcriptome information (especially from the strand-specific cDNAseq data) is available, it is apparently more favorable to search against the transcriptome as well than to search against the genome alone. If the transcriptome information is unavailable, it would be also helpful to reduce the 6-OFR translation database by removing sequences that are predicted to be hardly possible to be real proteins. From the point of view of data analysis, we believe that intelligent post-processing of search results is a promising resolution to sensitive discovery of novel peptides and genes. For example, machine learning techniques (Kall et al., 2007) can be used to discriminate true and false identifications of novel peptides and to re-score and re-rank the peptides using specific information in proteogenomics. Alternatively, the search results from multiple search engines can be combined properly to generate a set of reliable identifications (Kelkar et al., 2011).

#### Funding

This work was supported by the International S&T Cooperation Program of China (2014DFB30010), the Strategic Priority Research Program of Chinese Academy of Sciences (XDB13040600), the National Key Basic Research Program of China (2011CB910600, 2013CB911201, 2010CB912701, 2015CB554406), the National Natural Science Foundation of China (31170780, 31470809, 31400698), the National High-Tech Research and Development Program of China (SS2012AA020502, 2011AA02A114), the International Collaboration Program (2014DFB30020), the National Megaprojects for Key Infectious Diseases (2013zx10003002), and the NCMIS CAS.

Conflict of Interest: none declared.

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