



# *Article* **Insights on Substitution Preference of Pb Ions in Sulfoaluminate Cement Clinker Phases**

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**Abstract:** The doping behaviors of Pb in sulfoaluminate cement (SAC) clinker phases were systematically studied combined with density functional theoretical simulations and experiments. The results present that, in the three composed minerals of  $C_4A_3\overline{S}$ ,  $C_2S$ , and  $C_4AF$ , Pb ions prefer to incorporate into  $C_4A_3\overline{S}$  by substituting Ca ions. Further analyses from partial density of states, electron density difference, and local distortions show that such doping preference can be attributed to the small distortions as Pb introduced at Ca sites of  $C_4A_3\overline{S}$ . The results and clear understandings on the doping behaviors of Pb ions may provide valuable information in guiding the synthesis of Pb-bearing SAC clinker, thus should draw broad interests in fields from sustainable production of cement and environmental protection.

**Keywords:** sulfoaluminate cement clinker; solid waste; first-principles; Pb; electronic structure



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#### **1. Introduction**

In recent years, with the urbanization, population growth, and industrialization, the amounts of solid waste are increasing sharply. It is estimated that 1.3 billion tons of waste is produced worldwide every year, and will increase to 3.4 billion tons by 2050 [\[1\]](#page-8-0). Solid waste, especially industrial by-product, contains many heavy metal elements, halogens, and other substances that are harmful to human beings. As a toxic heavy metal, plumbum (Pb), which exists broadly in fly ash (416.6 mg/g), sludge (92.5 mg/g), and coal dust  $(20.41 \text{ mg/g})$  [\[2\]](#page-8-1), is extremely harmful to human health. How to effectively treat such industrial solid waste has become an essential issue of environmental protection.

Cement is the most widely used artificial product, which can be classified into various types according to the main composed phases, such as Portland cement (PC), sulfoaluminate cement (SAC), and magnesium phosphate cement (MPC) [\[3,](#page-8-2)[4\]](#page-8-3). PC clinker mainly consists of C<sub>3</sub>S (3CaO·SiO<sub>2</sub>), C<sub>2</sub>S (2CaO·SiO<sub>2</sub>), C<sub>3</sub>A (3CaO·Al<sub>2</sub>O<sub>3</sub>), and C<sub>4</sub>AF  $(4CaO·Al<sub>2</sub>O<sub>3</sub>·Fe<sub>2</sub>O<sub>3</sub>)$  [\[5\]](#page-8-4). SAC clinker is composed of  $C<sub>4</sub>A<sub>3</sub>$  $\overline{S}$  (4CaO·3Al<sub>2</sub>O<sub>3</sub>·SO<sub>3</sub>), C<sub>2</sub>S, and  $C_4$ AF [\[6\]](#page-8-5). The latter has high early strength, frost resistance, alkali resistance, and other excellent properties [\[7\]](#page-8-6). Therefore, SAC clinker may play key role in cement-related materials in future. It is reported that SAC clinker can be produced by utilizing solid waste as raw materials [\[8](#page-8-7)[,9\]](#page-8-8). The co-processing of solid waste by cement kilns is an efficient way for safe disposal of heavy metals [\[10\]](#page-8-9), and it is also the direction of sustainable development of the cement industry in the future. In the process of clinker formation, heavy metal ions can be solidified in clinker minerals by forming solid solutions, thus effectively avoid the formation of secondary pollution. Compared with Portland cement, heavy metal ions are more likely to dissolve into SAC clinker phases [\[11\]](#page-8-10). Moreover, the content of Pb in SAC clinkers produced by this technology is below the levels limited by the international standards [\[12\]](#page-9-0). Moreover, the firing temperature of SAC clinker could be reduced by 150 ◦C to 200  $\mathrm{^{\circ}C}$  [\[13](#page-9-1)[,14\]](#page-9-2), which can reduce carbon emissions [\[15](#page-9-3)[,16\]](#page-9-4).

Several researchers studied the effects of Pb on the properties of SAC clinker as well as its hydration products. For example, Mao, Y. et al. used solid waste as raw materials and found that Pb can be dissolved in SAC clinker phases [\[17\]](#page-9-5). Ma, B. et al. reported that the solidification of Pb ions can increase the hydration rate of SAC clinker and the jelling time can be reduced 72% by introducing 2 wt%  $Pb(NO_3)$  [\[18\]](#page-9-6). Wang. L. et al. reported the carbonation and water washing can effectively reduce the volatilization of Pb in the calcination process [\[19\]](#page-9-7). To better utilize Pb-bearing raw materials as well as SAC-based materials, it is essential to learn the existing state, the possible substitution preference, and the factors influencing doping behaviors of Pb ions in SAC clinker phases.

Besides the progress from experimental researchers, it also intrigued great interests of theorists. Especially in recent years, with the rapid development of parallel computing and simulation methods, it has become possible to simulate the complicated system of various cements [\[20–](#page-9-8)[24\]](#page-9-9). Zhu, J. et al. studied the doping behaviors of Zn ions in PC clinker with density functional theoretical (DFT) simulations and experiments [\[20\]](#page-9-8). They found that Zn ions prefer to substitute Fe in  $C_4$ AF and the extracted Fe will react with another phase,  $C_3$ A. Zhao, R. et al. reported the doping preference of Mg ions in  $C_4$ AF by substituting Fe, while in the other three minerals of PC clinker, they prefer to replace Ca ions and the solubility follows the sequence of  $C_3S \approx C_3A > C_2S$  [\[21\]](#page-9-10). Zhu, J. et al. studied the substituting behaviors of Ba in SAC clinker, the extinct Ba atoms prefer to incorporate into  $C_4A_3S$  by substituting Ca atoms while little enters the other two minerals, C2S and C4AF [\[22\]](#page-9-11). Li, N. et al. revealed the doping preference of Mn and Cu in PC clinker combined with DFT simulations and experiments [\[23,](#page-9-12)[24\]](#page-9-9). In this work, we attempt to unveil the doping behaviors and existing form of Pb in SAC clinker phases, and based on these understandings to further evaluate the possibility of producing SAC clinker by utilizing Pb-bearing industrial solid waste.

## **2. Simulations and Experiments**

## *2.1. Simulations*

The mineral  $C_4A_3\overline{S}$ , which accounts for about 55–75 wt% of SAC clinker, has cubic, tetragonal, and orthorhombic forms. Here, the cubic form was used to model  $C_4A_3\overline{S}$  [\[25\]](#page-9-13). C2S also possesses several crystal structures and the β-form was used as the matrix to model  $C_2S$  as it can be retained at room temperature. [\[26](#page-9-14)[,27\]](#page-9-15). Considering the complexity and poor symmetry of  $\beta$ -C<sub>2</sub>S, the Ca ions with 6- and 8- fold coordination numbers are denoted as CaI and CaII, respectively. The ferrite phase usually exists as continuous solid solutions, and the one with equal molar aluminum and iron,  $C_4AF$ , is used to model tetracalcium aluminoferrite [\[28\]](#page-9-16). To reduce the influence between adjacent doping atoms and ensure the comparability of clinker with similar content, primitive cell  $(C_4A_3\overline{S})$  and the supercells of  $2 \times 2 \times 1$  (for  $\beta$ -C<sub>2</sub>S) and  $2 \times 1 \times 2$  (for C<sub>4</sub>AF) were used to model doping behaviors of Pb in SAC clinker phases. The detailed schematic structure models of three minerals are shown in Figure [1.](#page-2-0)

DFT simulations were performed with the Vienna Ab-initio Simulation Package (VASP) in this work [\[29](#page-9-17)[,30\]](#page-9-18), and the generalized gradient approximation (GGA) within Perdew–Burke–Ernzerhof (PBE) functionals were adopted as the exchange-correlation potential [\[31\]](#page-9-19). The energy cutoff was 500 eV. The K-points were sampled with Gammacentered scheme in the first Brillouin zone [\[32\]](#page-9-20). The K-point meshes with density of 0.02 and 0.01 were used for configuration relax and calculations of partial density of states (PDOS), respectively. The detailed K-points are summarized in Appendix [A](#page-8-11) Table [A1.](#page-8-12) The convergence criteria of 10<sup>-5</sup> eV/atom and 0.01 eV/Å were used for the energy and force, respectively. The electron density difference (EDD) was calculated by CASTEP [\[33\]](#page-9-21). The models and results were visualized by VESTA.

<span id="page-2-0"></span>

Figure 1. Schematic structures of SAC clinker phases: (a)  $C_4A_3\bar{S}$ , (b)  $C_2S$ , and (c)  $C_4$ AF. The doping sites are highlighted with bigger bicolored balls in each panel. One color (the red one) represents Pb and the other one stands for the atoms been substituted. The green, blue, purple, yellow, grey, orange, and red balls represent six-fold Ca, eight-fold Ca, Al, S, Si, Fe, and Pb, respectively.

The normalized defect formation energy (*E<sup>f</sup>* ) was used to characterize the possibility of substitution, which can be defined as [\[34](#page-9-22)[,35\]](#page-9-23):

$$
\overline{E}_f = \frac{E - E_0 + \mu_{\rm Pb} - \mu_{\rm X}}{\omega} \tag{1}
$$

where  $E$  and  $E_0$  are the energies of the doped and original clinker phases, respectively;  $\mu_{\text{Pb}}$  and  $\mu_X$  are the chemical potentials of Pb and the atoms, X (X = Ca, Al, S, Si and Fe), respectively. The values of  $\mu_{\text{Pb}}$  and  $\mu_X$  can be calculated from corresponding bulk materials [\[36\]](#page-9-24). More details about the bulk materials and their chemical potentials are summarized in Table  $A2$ .  $\omega$  is the mass concentration of Pb in each phase.

#### *2.2. Experiments*

behaviors of Pb ions. The analytical grade materials CaCO<sub>3</sub>, CaSO<sub>4</sub>, SiO<sub>2</sub>, Al<sub>2</sub>O<sub>3</sub> and<br>F. C. Cassos defined the construction of the construction of the construction of the construction of the constr Fe<sub>2</sub>O<sub>3</sub> were used as raw materials. The mass of these materials was set as constants to  $Fe<sub>2</sub>O<sub>3</sub>$  were used as raw materials. The mass of these materials was set as constants to ensure the compositions of each mineral of SAC clinker. The potential mineral compositions ensure the compositions of each mineral of SAC clinker. The potential mineral compositions *37* calculated from Bogue equations  $[37]$  are  $C_4A_3S$  (56 wt%),  $C_2S$  (29 wt%) and  $C_4AF$  (15 wt%), samples of pristine and Pb-doped  $C_4A_3\overline{S}$  were also prepared. The detailed ratios of raw  $\frac{1}{2}$  materials are summarized in Table [1.](#page-2-1) Both pristine and Pb-doped SAC clinker samples were prepared to learn the doping respectively. Different amounts of  $PbO<sub>2</sub>$  were added as Pb source. For comparison, the

<span id="page-2-1"></span>Table 1. The ratios of materials used to prepare pristine and Pb-doped SAC clinker and the mincal  $C_4A_3\bar{S}$ . The distribution regions of  $C_4A_3\bar{S}$ . eral  $C_4A_3\overline{S}$ .

| <b>Samples</b>       |                | Ratio of Materials (wt%) |                          |           |                   |                                |                      |  |  |
|----------------------|----------------|--------------------------|--------------------------|-----------|-------------------|--------------------------------|----------------------|--|--|
|                      |                | CaCO <sub>3</sub>        | SiO <sub>2</sub>         | $Al_2O_3$ | CaSO <sub>4</sub> | Fe <sub>2</sub> O <sub>3</sub> | $PbO_2$ <sup>*</sup> |  |  |
| <b>SAC</b>           | A1             | 54.56                    | 7.66                     | 23.58     | 10.46             | 3.74                           | 0                    |  |  |
|                      | A <sub>2</sub> | 54.56                    | 7.66                     | 23.58     | 10.46             | 3.74                           | 11.82                |  |  |
|                      | A3             | 54.56                    | 7.66                     | 23.58     | 10.46             | 3.74                           | 17.74                |  |  |
|                      | A4             | 54.56                    | 7.66                     | 23.58     | 10.46             | 3.74                           | 23.65                |  |  |
| $C_4A_3\overline{S}$ | S <sub>1</sub> | 40.47                    | -                        | 40.80     | 18.73             | $\overline{\phantom{0}}$       | $\Omega$             |  |  |
|                      | S <sub>2</sub> | 40.47                    | $\overline{\phantom{0}}$ | 40.80     | 18.73             | $\overline{\phantom{0}}$       | 16.86                |  |  |
|                      | S <sub>3</sub> | 40.47                    | $\overline{\phantom{0}}$ | 40.80     | 18.73             | $\overline{\phantom{0}}$       | 25.29                |  |  |
|                      | S4             | 40.47                    |                          | 40.80     | 18.73             | $\overline{\phantom{0}}$       | 33.71                |  |  |

 $*$  Notes: The dosage of PbO<sub>2</sub> is calculated based on the masses of products after calcination.

The mixture of all materials used to prepare each sample was grinded for 1 h in agate mortar and pressed into pellets (height, ~10 mm; diameter, ~30 mm) at a pressure of 30 MPa. The obtained pellets were put in alumina crucibles and sintered for 30 min at 0.000 for all all all the higher possibilities of reaction. Figure 2 shows means of  $\sim 2000$  for all all the higher possibilities of 900 °C and 3 h at 1350 °C with a heating rate of 10 °C/min. All samples were quenched for the diate of the theoretic which a neating rate of to the phase were quentified to room temperature in air. The obtained samples were crushed into small pieces. Some to room temperature in unit. The obtained samples were erashed mic small precess some were polished and sputter-coated with gold for backscattered electron (BSE) measurement. were poilshed and sputter-coated with gold for backscattered electron (b5E) measurement.<br>The other parts and the  $C_4A_3\overline{S}$  pellets were ground until passing 200 mesh sieves for X-ray The other parts and the  $C_4A_3$ <sub>2</sub> pe<br>diffraction (XRD) measurements. o room tempe<br>vare reliebed e  $\begin{array}{ccc} \circ & \bullet & \bullet & \bullet & \bullet \\ \text{hence} & \bullet & \bullet & \bullet & \bullet \end{array}$ 

BSE measurements were performed with the scanning electron microscopy (SEM, Merlin Compact, Carl Zeiss NTS GmbH, Oberkochen, Germany) coupled with the energydispersive spectroscopy (EDS, Oxford, UK) at 15 kV. XRD measurements were carried out using Rigaku diffractometer (XRD, Smart lab, Rigaku, Tokyo, Japan). The data were collected from  $5°$  to  $80°$  with a step size of  $5°/$ min and the counting time of  $0.02°$  per step under 40 kV and 150 mA.

#### **3. Results and Discussion**

## *3.1. Defect Formation Energies*

The configurations of three minerals with Pb ions introduced at different sites are shown in Figure [1.](#page-2-0) The doping sites were highlighted by bigger bicolored balls. The values of  $\overline{E}_f$  can be used to characterize the possibility of forming solid solutions. Generally, the smaller values mean the higher possibilities of reaction. Figure [2](#page-3-0) shows  $\overline{E}_f$  of all configurations of SAC clinker phases (see Figure [1](#page-2-0) for detailed geometries). It can be seen that the values of all  $\overline{E}_f$  are positive. Additionally, the configuration with Pb introduced at Ca site of C<sub>4</sub>A<sub>3</sub>S has the lowest  $E_f$ , indicating that Pb tends to incorporate into C<sub>4</sub>A<sub>3</sub>S by substituting Ca. The positive  $\overline{E}_f$  implies that extra energy is required to overcome the reaction barrier. As SAC clinker was prepared at 1350 °C, such barrier may be easily  $\frac{1}{1}$  overcome under the above synthetic conditions.

<span id="page-3-0"></span>

**Figure 2.** The normalized defect formation energies  $(\overline{E}_f)$  of configurations with Pb introduced at different sites. different sites.

## *3.2. Experimental Analyses 3.2. Experimental Analyses*

In order to confirm the doping preference of Pb in the SAC clinker, several samples In order to confirm the doping preference of Pb in the SAC clinker, several samples with Pb content of 0 wt%, 11.82 wt%, 17.74 wt%, and 23.65 wt% were prepared, respec-with Pb content of 0 wt%, 11.82 wt%, 17.74 wt%, and 23.65 wt% were prepared, respectively. The SEM-EDS of elements including Ca, S, Si, and Fe of the sample A4 are shown tively. The SEM-EDS of elements including Ca, S, Si, and Fe of the sample A4 are shown in Figur[e 3](#page-4-0)a–d, respectively. The brighter regions represent those with high content of in Figure 3a–d, respectively. The brighter regions represent those with high content of corresponding elements. The distribution regions of Ca are contributed by all composed corresponding elements. The distribution regions of Ca are contributed by all composed minerals of SAC clinker while those of S, Si, and Fe are solely originated from the mineral minerals of SAC clinker while those of S, Si, and Fe are solely originated from the mineral  $C_4A_3S$ ,  $C_2S$  and  $C_4AF$ , respectively. Therefore, the regions of S, Si, and Fe represent the zones of corresponding minerals. To clearly show the possible doping preference of Pb in three minerals, the distributions of Pb were overlapped with those of Ca, S, Si, and Fe, respectively. The obtained figures are shown in Figure [3e](#page-4-0)–h, respectively. It can be seen from Figure [3e](#page-4-0) that the regions of Ca are larger than that of Pb, indicating that Pb ions from Figure 3e that the regions of Ca are larger than that of Pb, indicating that Pb ions prefer to locate in certain phases. Careful examinations of panels Figure [3f](#page-4-0)–h present that prefer to locate in certain phases. Careful examinations of panels Figure 3f–h present that the distributions of Pb consist almost exactly with that of S (see panel b and f) while present the distributions of Pb consist almost exactly with that of S (see panel b and f) while present poor overlap with those bright regions of Si (panel c and g) and Fe (panel d and h). There-<br>fore Philippe developments in comparate into the mineral G  $\Lambda \bar{E}$ . Developments in it is not of fore, Pb ions should mainly incorporate into the mineral  $C_4A_3S$ . Due to the limitations of EDS, it is hard to judge which element is the one that Pb ions tend to substitute. Thus, we analyzed the YPD recults in the following neath analyzed the XRD results in the following part.

<span id="page-4-0"></span>

Figure 3. (a–d) The element distributions of Ca (a), S (b), Si (c), Fe (d), and (e–h) overlaps of Pb with the above four elements in SAC clinker samples. in SAC clinker samples.

The full ranged XRD patterns of SAC clinker with different dosages of  $PbO<sub>2</sub>$  are shown in Figure 4a. All diffractions were assigned according to the standard diffraction shown in Figure [4a](#page-5-0). All diffractions were assigned according to the standard diffraction  $p$ atterns of  $C_4A_3\overline{S}$  (PDF#-71-0969),  $C_2S$  (PDF#-33-0302), and  $C_4AF$  (PDF#-71-0607). The peaks belonging to the same phase are identified with identical symbols. From Figure 4a, peaks belonging to the same phase are identified with identical symbols. From Figure [4a](#page-5-0), we can see that the peaks belonging to  $C_4A_3\overline{S}$  are much higher than those of  $C_2S$  and  $C_4AF$ , which can be attributed to the predominant content of  $C_4A_3\overline{S}$  in the prepared SAC clinker. The Miller indices of three main peaks of  $C_4A_3\overline{S}$  are also labelled in Figure [4a](#page-5-0). To present  $\overline{S}$ the variations as Pb introduced, the enlarged parts of these three main peaks are shown the variations as Pb introduced, the enlarged parts of these three main peaks are shown in Figure 4b. It clearly presents that these three peaks continuously shift towards left as in Figure [4b](#page-5-0). It clearly presents that these three peaks continuously shift towards left as the dosage of Pb increases, indicating that Pb ions successfully incorporate into  $C_4A_3\overline{S}$ . According to Bragg equation, the decrease in Bragg angles means the increase in lattice According to Bragg equation, the decrease in Bragg angles means the increase in lattice constant as Pb is introduced in SAC clinker.

To further verify the incorporation possibility of Pb ions in the mineral  $C_4A_3\overline{S}$ , both pristine and Pb-doped  $C_4A_3S$  were also prepared. The full ranged and enlarged XRD patterns of  $C_4A_3\overline{S}$  are shown in Figure [4c](#page-5-0),d, respectively. The peaks as well as the Miller indices of the three main peaks are also presented in Figure [4c](#page-5-0),d. The left shifts observed in the single mineral  $C_4A_3\overline{S}$  is consistent with those from XRD patterns of SAC clinker.

Both the above element distributions and XRD patterns show that Pb ions prefer to incorporate into the mineral  $C_4A_3\overline{S}$ . However, more quantitative experiments and further analyses are needed to determine the exact solubility of Pb ions in SAC clinker in the future. Besides that, there are several sites, such as those occupied by Ca, Al, and/or S, can host Pb ions. As shown in Table [A3,](#page-8-14) the ionic radius of these ions is smaller than that of Pb ions. In other words, the incorporation of Pb in the above sites can result in increase in lattice parameters. The exact sites of Pb in  $C_4A_3\overline{S}$  cannot be determined from experiments. To further figure out the exact doping sites, we analyzed the partial density of states and electron density difference of all minerals before/after Pb is introduced.

<span id="page-5-0"></span>

Figure 4. The full ranged and enlarged XRD patterns of SAC clinker (a,b) and the single mineral  $C_4A_3\overline{S}$  (c,d). The Miller indices of three main peaks of  $C_4A_3\overline{S}$  are also presented in each panel.

# 3.3. Partial Density of States and Electron Density Difference

 $\sigma$ . The process of points and  $\mathbb{R}$ , denoted  $\overline{C}$   $\overline{C}$   $\overline{C}$   $\overline{C}$  and  $\overline{C}$   $\overline{A}$   $\overline{D}$  and  $\overline{D}$ The PDOS of pristine and Pb-doped C<sub>4</sub>A<sub>3</sub>S, C<sub>2</sub>S and C<sub>4</sub>AF are shown in Figure [5.](#page-6-0)<br>Converged with pristine  $C_A \overline{S}$  in explication with Ph introduced at  $C_B$ , the perverse  $t_{\rm{m}}$  are also presented in Figure 4c and d. The single-singlet shifts observed in the single-single-single-single-single-single-single-single-single-single-single-single-single-single-single-single-single-single-sing formed Pb-O bonds are mainly contributed by the overlaps of electron density on Pb-6*s*,<br>Rh fo and O 2n orbitals. For configurations with Ph introduced at Al and S, the electron density of states of Pb-6*s* possess higher energies and present little overlaps with that of density of states of 19-0s possess higher energies and present fittle overlaps with that of<br>O-2*p* orbitals, indicating weaker Pb-O bonds in configurations with Pb introduced at Al and S. For the minerals  $C_2S$  and  $C_4AF$ , all the newly formed Pb-O bonds present much less  $\frac{1}{2}$  are setween  $\frac{1}{2}$  best  $\frac{1}{2}$  by Ca,  $\frac{1}{2}$  and  $\frac{1}{2}$ ,  $\frac{1}{2}$  are  $\frac{1}{2}$  by Ca,  $\frac{1}{2}$  and  $\frac{1}{2}$  are  $\frac{1}{2}$  by Ca,  $\frac{1}{2}$  and  $\frac{1}{2}$  are  $\frac{1}{2}$  are  $\frac{1}{2}$  are  $\frac{1}{2}$  overlaps between Pb-6*s,* Pb-6*p* and O-2*p* orbitals. Thus, Pb should prefer to substitute the<br>Ca atom in C+4.5 S Compared with pristine  $C_4A_3\overline{S}$ , in configuration with Pb introduced at Ca, the newly Pb-6*p* and O-2*p* orbitals. For configurations with Pb introduced at Al and S, the electron Ca atom in  $C_4A_3S$ .

 $EDD$  can visually show the electron redistributions between adjacent atoms, thus can be used to determine the strength of bonds. The EDD results of pristine and Pb-doped C<sub>4</sub>A<sub>3</sub>S, C<sub>2</sub>S, and C<sub>4</sub>AF are shown in Figure [6a](#page-6-1)–c, respectively. The central ions and partial oxygen atoms are also presented in each panel. The red and blue regions stand for around O present red due to its most strong electronegativity. The regions around Al and Si present similar electron distributions due to their similar electronegativity, while the regions with S and Fe as centered atoms present obviously blue, which can be attributed to their predominant numbers in valent electrons. For regions centered with Ca and Pb, they present light blue, indicating much less electron transfer occurs from Ca/Pb to O. In configurations with Pb introduced at Al, S, Si, and Fe, the Pb-centered regions present lighter blue than those in pristine minerals. For the configurations with Pb introduced at Ca, the one in C $_4$ A3S present a little deeper blue than that in C2S and C $_4$ AF. Thus, Pb ions should prefer to occupy the sites of Ca in  $C_4A_3S$ , well consistent with the results obtained from PDOS. accumulation and reduction of electrons, respectively. In all configurations, the regions

<span id="page-6-0"></span>

Figure 5. The partial density of states (PDOS) of pure and Pb-doped SAC clinker Phases: (a)  $C_4A_3\overline{S}$ , (b)  $C_2S$ , and (c)  $C_4AF$ . The Fermi energy was set to zero eV. The Fermi energy was set to zero eV. should prefer to occupy the sites of Ca in C4A3Sത, well consistent with the results obtained

<span id="page-6-1"></span>

**Figure 6.** Electron density difference (EDD) of pristine and Pb-doped minerals of SAC clinker: (a)  $C_4A_3\overline{S}$ , (b)  $C_2S$  and (c)  $C_4$ AF. The blue and red isosurfaces stand for electron accumulation and reduction, respectively.

#### $\mathfrak{so}(3)$  in Ca in Ca in Casino of Ca in Casino with the results obtained with the result  $f(x, 2)$ *3.4. Local Structural Distortions 3.4. Local Structural Distortions*

The above results present that, although all three minerals contain Ca atoms, Pb ions The above results present that, although all three minerals contain Ca atoms, Pb ions prefer to substitute the Ca atoms in  $C_4A_3\overline{S}$  To further determine the preferred incorporation, the local distortions of Pb-centered polyhedrons were carefully analyzed. Here, we use the relative bond length  $\Delta R$ , ( $\Delta R = (R - R_0)/R_0 \times 100\%$ ; *R* and *R*<sub>0</sub> represent the bond length of Pb-O and Ca-O, respectively) to characterize the local distortions. The results are shown in Figure [7.](#page-7-0) The values of  $\Delta R$  fall in a large range of ~−2–10% in three minerals. For a reference, the averaged ∆*R* is also presented as red lines in Figure [7.](#page-7-0) Among these configurations, the mineral  $C_4A_3\overline{S}$  presents the smallest distortions as Pb is introduced. The small distortions in  $C_4A_3\overline{S}$  may also play positive roles in hosting Pb ions.

<span id="page-7-0"></span>



configurations, the mineral C4A3Sത presents the smallest distortions as Pb is introduced.

# **4. Conclusions 4. Conclusions**

In this work, we systematically studied the possibility and doping preference of Pb In this work, we systematically studied the possibility and doping preference of Pb in SAC clinker phases by DFT simulations and experiments. Our results show that Pb ions can incorporate into SAC clinker by forming solid solutions. Such incorporation probably can incorporate into SAC clinker by forming solid solutions. Such incorporation probably can be attributed to the preferred substitution of Pb at Ca sites of  $C_4A_3\overline{S}$ . The preferred substitution can be attributed to the small structure distortions between Pb-O and Ca-O as Pb ions are introduced. The understandings on the existing state and the doping preference of Pb could provide valuable information in the synthesis of SAC clinker by utilizing ing Pb-bearing solid waste, thus is very meaningful both in sustainable development of Pb-bearing solid waste, thus is very meaningful both in sustainable development of SAC industry and environment protections.

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## <span id="page-8-11"></span>**Appendix A**

<span id="page-8-12"></span>**Table A1.** Minerals, supercells, lattice parameters, and detailed k point meshes used for relax and partial density of states (PDOS).

| <b>Minerals</b>                | <b>Supercells</b>     | Lattice Parameters/Å                    | Relax                 | <b>PDOS</b>           |
|--------------------------------|-----------------------|---|-----------------------|-----------------------|
| $C_4A_3\overline{S}$ [25]      | $1 \times 1 \times 1$ | $a = b = c = 9.19$                      | $3 \times 3 \times 3$ | $5 \times 5 \times 5$ |
| $\beta$ -C <sub>2</sub> S [26] | $2 \times 2 \times 1$ | $a = 11.01$ , $b = 13.51$ , $c = 9.31$  | $2 \times 2 \times 3$ | $5 \times 4 \times 5$ |
| $C_4AF$ [28]                   | $2 \times 1 \times 2$ | $a = 11.17$ , $b = 14.60$ , $c = 10.75$ | $2 \times 2 \times 2$ | $5 \times 3 \times 5$ |

<span id="page-8-13"></span>**Table A2.** Phases, space group, ICSD IDs, lattice parameters [\[36\]](#page-9-24), and chemical potentials (µ) of Pb and the atoms that have been replaced by Pb.

| Phase       | <b>Space</b><br>Group | <b>ICSD</b><br><b>IDs</b> | <b>Lattice Parameters</b> |      |         |                    |            |             |           |
|-------------|-----------------------|---------------------------|---------------------------|------|---------|--------------------|------------|-------------|-----------|
|             |                       |                           | a/Å                       | b/Å  | $c/\AA$ | $\alpha l^{\circ}$ | $\beta$ /° | $\gamma$ /° | $\mu$ /eV |
| $\alpha$ Pb | Fm3m                  | 648.343                   | 0.50                      | 0.50 | 0.50    | 90                 | 90         | 90          | $-3.56$   |
| $\alpha$ Ca | Fm3m                  | 426,932                   | 5.59                      | 5.59 | 5.59    | 90                 | 90         | 90          | $-1.92$   |
| $\alpha$ Al | Fm3m                  | 53,774                    | 4.05                      | 4.05 | 4.05    | 90                 | 90         | 90          | $-3.75$   |
| $\alpha S$  | P2/c                  | 82,372                    | 13.64                     | 9.25 | 10.90   | 57                 | 90         | 90          | $-4.12$   |
| $\alpha$ Si | Fd3m                  | 181,356                   | 5.43                      | 5.43 | 5.43    | 90                 | 90         | 90          | $-5.43$   |
| $\alpha$ Fe | Im3m                  | 631,729                   | 2.87                      | 2.87 | 2.87    | 90                 | 90         | 90          | $-8.24$   |

<span id="page-8-14"></span>**Table A3.** Ions, coordination number, electronegativity, and ionic radius [\[38\]](#page-9-26) of Pb and other ions that have been substituted.



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