



# Article A Density Functional Theory and Microkinetic Study of Acetylene Partial Oxidation on the Perfect and Defective Cu<sub>2</sub>O (111) Surface Models

Ling-Nan Wu <sup>1,2,\*</sup>, Zhen-Yu Tian <sup>1,2,\*</sup> and Wu Qin <sup>3</sup>

- <sup>1</sup> Institute of Engineering Thermophysics, Chinese Academy of Sciences, Beijing 100190, China
- <sup>2</sup> University of Chinese Academy of Sciences, Beijing 100049, China
- <sup>3</sup> Engineering Laboratory for Biomass Generation Equipment, North China Electric Power University, Beijing 102206, China
- \* Correspondence: wulingnan@iet.cn (L.-N.W.); tianzhenyu@iet.cn (Z.-Y.T.); Tel.: +86-10-82543305 (Z.-Y.T.)

Abstract: The catalytic removal of  $C_2H_2$  by  $Cu_2O$  was studied by investigating the adsorption and partial oxidation mechanism of C<sub>2</sub>H<sub>2</sub> on both perfect (stoichiometric) and Cu<sub>CUS</sub>-defective Cu<sub>2</sub>O (111) surface models using density functional theory calculations. The chemisorption of  $C_2H_2$  on perfect and defective surface models needs to overcome the energy barrier of 0.70 and 0.81 eV at 0 K. The direct decomposition of  $C_2H_2$  on both surface models is energy demanding with the energy barrier of 1.92 and 1.62 eV for the perfect and defective surface models, respectively. The H-abstractions of the chemisorbed C<sub>2</sub>H<sub>2</sub> by a series of radicals including H, OH, HO<sub>2</sub>, CH<sub>3</sub>, O, and O<sub>2</sub> following the Langmuir–Hinshelwood mechanism have been compared. On the perfect Cu<sub>2</sub>O (111) surface model, the activity order of the adsorbed radicals toward H-abstraction of  $C_2H_2$  is:  $OH > O_2 > HO_2 > O >$  $CH_3 > H$ , while on the defective  $Cu_2O$  (111) surface model, the activity follows the sequence: O > $OH > O_2 > HO_2 > H > CH_3$ . The Cu<sub>CUS</sub> defect could remarkably facilitate the H-abstraction of  $C_2H_2$ by  $O_2$ . The partial oxidation of  $C_2H_2$  on the  $Cu_2O$  (111) surface model tends to proceed with the chemisorption process and the following H-abstraction process rather than the direct decomposition process. The reaction of  $C_2H_2$  H-abstraction by  $O_2$  dictates the  $C_2H_2$  overall reaction rate on the perfect  $Cu_2O(111)$  surface model and the chemisorption of  $C_2H_2$  is the rate-determining step on the defective Cu<sub>2</sub>O (111) surface model. The results of this work could benefit the understanding of the C<sub>2</sub>H<sub>2</sub> reaction on the Cu<sub>2</sub>O (111) surface and future heterogeneous modeling.

Keywords: acetylene; partial oxidation; density functional theory calculations; Cu<sub>2</sub>O (111) surface; defects

# 1. Introduction

Acetylene ( $C_2H_2$ ) is a kind of important industrial raw materials used for various purposes, including oxyacetylene welding, cutting, illuminant, soldering metals, signaling, precipitating metals, particularly copper, manufacture of acetaldehyde, acetic acid, etc. [1].  $C_2H_2$  is a significant intermediate formed during the combustion of hydrocarbons, especially under fuel-rich conditions, which is responsible for the soot formation during combustion processes via the H-abstraction- $C_2H_2$ -addition (HACA) mechanism [2,3]. The production of  $C_2H_2$  during combustion could endanger the safety and efficiency of combustors, etc.  $C_2H_2$  is also a component of volatile organic compounds (VOCs), and it gains increasing attention due to its toxicity to the environment and human health. Exposure to high concentrations of  $C_2H_2$  may cause loss of consciousness or even death, and it is a serious fire and explosion hazard.  $C_2H_2$  is an undesirable by-product of the petroleum cracking process, and it causes damage to the catalyst for the ethylene polymerization process [4]. To address the problems caused by  $C_2H_2$  formation and emission, the efficient removal of  $C_2H_2$  during combustion and industrial processes is of great interest. To the best of our knowledge, much attention has been paid to the study of  $C_2H_2$ /hydrocarbons



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**Copyright:** © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). homogeneous kinetics under pyrolysis [5,6], oxidation [3,7], and flame conditions [2], and kinetic models predicting the reaction characteristics under these conditions have been proposed [3,7], while relatively less attention has been paid to the heterogeneous processes of  $C_2H_2$ .

Catalytic removal is an important technique in exhaust gas purification, and the activity of catalysts plays a crucial role in the catalytic process. Previous studies have shown that Cu<sub>2</sub>O thin film catalysts prepared by the pulsed-spray evaporation chemical vapor deposition (PSE-CVD) method are effective for the catalytic removal of C<sub>2</sub>H<sub>2</sub> [8], but the oxidation mechanism of  $C_2H_2$  on the  $Cu_2O$  surface remains unclear. Theoretical studies based on density functional theory (DFT) calculations have been widely used as an effective tool in revealing the gas-surface heterogeneous reaction mechanisms on Cu-based oxide surfaces [9-26]. DFT studies regarding the C<sub>2</sub>H<sub>2</sub> hydrogenation process have been reported previously. Zhang et al. [27,28] have studied  $C_2H_2$  hydrogenation to ethylene using DFT calculations, and it is found that the valence state of the surface Cu site has an important impact on the surface catalytic ability toward the  $C_2H_2$  hydrogenation to ethylene. Good command of the surface oxidation mechanism could be beneficial for the development of high-performance catalysts. Experiments could provide useful information by studying the dependency of catalysts' performance on the preparation methods and macroscopic parameters, such as temperature, pressure, PH, etc. Proper characterizing techniques, such as SEM, XPS, XRD, etc., could also throw light upon the surface morphology and surface properties, which could help better understand the nature of the catalytic process. In addition, theoretical studies based on DFT calculations could also reveal the intrinsic surface reaction mechanism, and the effect of surface sites and vacancies on the catalytic performance is still needed. The establishment of a proper surface model is of importance for the theoretical investigation of the  $C_2H_2$  partial oxidation process on the  $Cu_2O$  surface. The  $Cu_2O(111)$  plane is the most widely used surface model to reveal the heterogeneous reaction mechanism on the Cu<sub>2</sub>O surface due to its thermodynamic stability, while many of them used the bulk-terminated models (the stoichiometric surface model or the perfect surface model) [13,16,29–31] but not the more stable Cu<sub>2</sub>O (111)–Cu<sub>CUS</sub> surface model as proposed by Soon et al. [32], and the importance of the Cu<sub>CUS</sub> vacancy has also been confirmed by Onsten et al. [33] experimentally. Our previous study also found that the defective Cu<sub>2</sub>O (111)–Cu<sub>CUS</sub> surface model could improve the surface activity toward CO oxidation [34] than the perfect one. Therefore, it is of significance to consider the surface defects when studying Cu<sub>2</sub>O surface chemistry.

To provide a better understanding of the reaction mechanism of  $C_2H_2$  on the  $Cu_2O$  surface, the adsorption and reaction processes of  $C_2H_2$  on the  $Cu_2O$  surface models were studied based on DFT calculations in this study. The reaction processes of  $C_2H_2$  on the  $Cu_2O$  surface models, including the adsorption process, decomposition process, and H-abstraction reactions, by a variety of radicals and  $O_2$  have been studied. The effect of the surface defect on the  $C_2H_2$  elementary reaction steps has been explored by studying the  $C_2H_2$  conversion on both the stoichiometric perfect  $Cu_2O$  (111) surface model and the  $Cu_2O$  (111)- $Cu_{CUS}$  defective surface model. The rate constants have been calculated and the parameters are provided in the Arrhenius form, which could be helpful for heterogeneous kinetic modeling studies.

#### 2. Computational Details

DFT calculations were performed using the DMol<sup>3</sup> code [35,36]. The generalized gradient approximation (GGA) functional of Perdew–Burke–Ernzerhof (PBE) [37] was used for exchange and correlation potential. The double numerical basis set plus the polarization (DNP) basis set was used for all the calculations. The DFT semi-core pseudopots (DSPP) core treatment was used for inner core pseudopotential treatment, which introduces relativistic correction into the cores. Transition state structures were preliminarily searched by the combination of linear synchronous transit (LST) and quadratic synchronous transit (QST) method and then optimized using the eigenvector following (EF) method to validate

only one imaginary vibrational mode, which corresponds to a first-order saddle point on the potential energy surface and correctly connects the reactant and the product of each elementary reaction.

A higher computational accuracy has been used in the current work compared with our previous works [29,34]. The orbital cut-off has increased from 4.0 to 4.4 Å, and the convergence threshold of the self-consistent field (SCF) has increased to  $1.0 \times 10^{-6}$  from  $1.0 \times 10^{-5}$ . The convergence criteria of energy, maximum force, and maximum displacement are  $1.0 \times 10^{-5}$  Ha, 0.002 Ha/Å, and 0.005 Å, respectively. For the crystal optimization, a  $4 \times 4 \times 4$  Monkhorst–Pack k-point grid was used. The surface planes were built by cleaving the Cu<sub>2</sub>O (111) surface from the optimized Cu<sub>2</sub>O crystal. A sheet of 10 Å vacuum layer was placed over the surface slab to avoid interference from imaging surface planes due to the periodic boundary conditions. The defective surface model was established by removing the top and bottom layer unsaturated Cu<sub>CUS</sub> sites. A  $3 \times 3 \times 1$  Monkhorst–Pack k-point grid was used for the energy calculations of the succeeding surface reactions.

Adsorption energy ( $E_{ad}$ ) is used to evaluate the interaction between the surface and the adsorbate, which is defined as:

$$E_{\rm ad} = E_{\rm sys} - E_{\rm ads} - E_{\rm sur} \tag{1}$$

where  $E_{sys}$  is the energy of the system after adsorption;  $E_{ads}$  is the energy of the adsorbate before adsorption;  $E_{sur}$  is the energy of the clean surface before adsorption.

The Gibbs free energy of activation was calculated by combining zero-point energy (ZPE), the electronic energies calculated at 0 K, and the thermal corrections at elevated temperatures. For surface species, the translations and rotations were converted into frustrated oscillation modes and were included in the vibration analysis [38]. Reaction rate constants of elementary reaction steps were calculated based on harmonic transition-state theory (HTST) [29,34,38,39], which is  $k = \frac{k_{\rm B}T}{h} \left(\frac{-\Delta G_a}{RT}\right)$ , where *k* is reaction rate constant,  $k_{\rm B}$  is the Boltzmann constant, *T* is temperature, *h* is the Planck constant, *R* is the universal gas constant, and  $\Delta G_a$  is the Gibbs free energy of activation. Detailed calculation processes can be found elsewhere [34,40].

## 3. Results and Discussion

#### 3.1. Perfect and Defective $Cu_2O$ (111) Surface Models and $C_2H_2$ Adsorption

The (111) surface plane of Cu<sub>2</sub>O crystal has been used throughout this study as it is the most thermodynamically stable and, therefore, dominantly exposed low-index surface plane [29,34,41,42]. The perfect and the Cu<sub>CUS</sub>-defective Cu<sub>2</sub>O (111) surface models have been established, as shown in Figure 1. The lattice constant of the perfect Cu<sub>2</sub>O (111) crystal after geometric optimization is 4.33 Å as a result of the improved convergence accuracy, which is close to the previously reported values (4.32 Å [43]) and experimental values (4.27 Å [23]). The perfect Cu<sub>2</sub>O (111) surface model is stoichiometric with the Cu/O ratio to be exactly two, and it contains four kinds of surface top-sites on the top layer, including the saturated copper (Cu<sub>CSS</sub>) site, the saturated oxygen (O<sub>CSS</sub>) site, the unsaturated copper (Cu<sub>CUS</sub>), and the unsaturated oxygen (O<sub>CUS</sub>) site, while the defective Cu<sub>2</sub>O (111) surface model only comprises the Cu<sub>CSS</sub>, O<sub>CSS</sub>, and O<sub>CUS</sub> sites, as the top and bottom Cu<sub>CUS</sub> sites are missing. The Cu<sub>CUS</sub> sites are active in absorbing the molecules, but the strong covalent bond between the adsorbate and the Cu<sub>CUS</sub> sites may hinder the following surface reactions.

The stable adsorption structure of  $C_2H_2$  on the  $Cu_2O$  (111) surface was explored by comparing the adsorption energies of  $C_2H_2$  on different surface sites of the  $Cu_2O$  (111) surface models. One  $C_2H_2$  molecule was placed on different surface sites, including the surface  $Cu_{CUS}$  site, the  $Cu_{CSS}$  site, the  $O_{CUS}$  site, and the  $O_{CSS}$  site, and the adsorption energies were obtained after the geometric optimization process. Only the most stable adsorption structure corresponding to the largest adsorption energy is presented.



Figure 1. Structures of the perfect and the defective Cu<sub>2</sub>O (111) surface models.

The adsorption processes of C<sub>2</sub>H<sub>2</sub> on the perfect and defective Cu<sub>2</sub>O (111) surface models are shown in Figure 2. For the adsorption on the perfect Cu<sub>2</sub>O (111) surface model, a  $C_2H_2$  molecule will first adsorb over the surface unsaturated  $Cu_{CUS}$  site with the energy release of 1.13 eV, and the linear structure of  $C_2H_2$  is slightly distorted with the O–C–C angles decreasing from both  $180^{\circ}$  to  $162^{\circ}$  and  $169^{\circ}$ . The C–C bond length of C<sub>2</sub>H<sub>2</sub> increases to 1.242 from 1.211 Å in the gas phase and the C-H bond length also increases to 1.077 and 1.081 from 1.071 Å. The activated  $C_2H_2$  molecule will then overcome the energy barrier of 0.70 eV and interacts with one surface lattice O<sub>CUS</sub> site and its neighboring Cu<sub>CUS</sub> site and one Cu<sub>CSS</sub> site, forming a chemisorbed structure depicted as FS in Figure 2a with the heat release of 1.78 eV in total. For the same process on the defective Cu<sub>2</sub>O (111) surface model. One  $C_2H_2$  molecule will first undergo a physisorption process releasing 0.20 eV. The bond length of the C–H bond close to the surface increases to 1.076 Å, while the bond lengths of the other C–H bond and the C–C bond are almost unchanged after physisorption. The physisorbed  $C_2H_2$  will then overcome the energy barrier of 0.81 eV and react with the surface O<sub>CUS</sub> site to form an adsorbed CHCHO\* species, which is bonded to three surface Cu<sub>CSS</sub> sites. The whole reaction process on the defective Cu<sub>2</sub>O (111) surface model releases 1.26 eV. By comparison, the perfect  $Cu_2O$  (111) surface model is more favorable for the  $C_2H_2$  adsorption at 0 K with a lower energy barrier and larger energy release, which is due to the existence of the active  $Cu_{CUS}$  site in activating the  $C_2H_2$  bond.



**Figure 2.** Energy profile of  $C_2H_2$  chemisorption on the (**a**) perfect  $Cu_2O$  (111) and (**b**) defective surface models.

# 3.2. Decomposition of $C_2H_2$ on the Perfect and the Defective $Cu_2O$ (111) Surface Models

The direct decomposition processes of the chemisorbed  $C_2H_2^*$  molecule undergoing the cleavage of the C-H bond on the Cu<sub>2</sub>O (111) surface models are first investigated, which represents the surface activity toward  $C_2H_2$  direct decomposition when there are no other adsorbates on the surface. Reaction energy profiles and the structures of the initial states, transition states, and final states are provided in Figure 3. The energy barrier of the reaction process on the perfect  $Cu_2O$  (111) surface model is 1.92 eV, and the reaction is an exothermic process releasing 0.21 eV. The adsorbed  $C_2H_2$  molecule will undergo an H-abstraction process, and the H atom will shift to the surface  $Cu_{CUS}$  site after the H-abstraction process. The  $C_2H$  part will react with the lattice  $O_{CUS}$  site and form an adsorbed HCCO\* species on the surface after the reaction. The H-C-C part of the formed HCCO<sup>\*</sup> species has a nearly linear structure with the H-C-C angle to be 177°. As for the direct decomposition of  $C_2H_2$  on the defective  $Cu_2O(111)$  surface model, the energy barrier has increased to 2.46 eV, and the reaction is an endothermic process adsorbing 0.36 eV. Therefore, the decomposition of the chemisorbed  $C_2H_2$  on both the perfect and the defective  $Cu_2O(111)$  surface models is hard to happen in terms of the reaction energy barrier, and the perfect Cu<sub>2</sub>O (111) surface model is more favorable than the defective one comparatively, which is due to the existence of the neighboring active Cu<sub>CUS</sub> site.



Figure 3. Energy profile of C<sub>2</sub>H<sub>2</sub> direct decomposition on the Cu<sub>2</sub>O (111) surface models.

## 3.3. H-Abstraction Reactions of Chemisorbed $C_2H_2$ by $O_2$ on the $Cu_2O$ (111) Surface Models

The H-abstraction reactions are important in the consumption of  $C_2H_2$ , hence the H-abstraction of the chemisorbed  $C_2H_2$  by  $O_2$  was studied in this section. The Langmuir–Hinshelwood reaction mechanism featuring the reaction between two adsorbed molecules on the perfect and defective  $Cu_2O$  (111) surface models is studied. The left part of Figure 4 shows the H-abstraction process on the perfect  $Cu_2O$  (111) surface model. The surface unsaturated  $Cu_{CUS}$  site is active for  $O_2$  adsorption, and an  $O_2$  molecule will adsorb on the  $Cu_{CUS}$  site close to the chemisorbed  $C_2H_2$  molecule, releasing 1.09 eV. Then, one H atom of the chemisorbed  $C_2H_2$  will transfer to the adsorbed  $O_2$  forming an adsorbed HO<sub>2</sub> molecule by overcoming the energy barrier of 1.43 eV. The reaction releases 0.23 eV with the formation of an adsorbed HO<sub>2</sub> and an adsorbed HCCO species on the surface.



**Figure 4.** Energy profile of  $C_2H_2$  H-abstraction by  $O_2$  on the perfect and defective  $Cu_2O$  (111) surface models.

The energy profile of  $C_2H_2$  H-abstraction by  $O_2$  on the defective  $Cu_2O$  (111) surface model is shown in the right part of Figure 4. An  $O_2$  molecule will first adsorb on the surface hollow site, and the chemisorbed  $C_2H_2$  needs to overcome the energy barrier of 0.97 eV to react with the adsorbed  $O_2$  and form an HO<sub>2</sub> on the hollow site with an energy release of 0.86 eV. An adsorbed HCCO species is formed after the reaction on top of three  $Cu_{CSS}$  sites. Compared with the perfect surface model, the H-abstraction of  $C_2H_2$  by  $O_2$  on the defective  $Cu_2O$  (111) surface is easier with a lower energy barrier and a larger energy release. The homogeneous H-abstraction of  $C_2H_2$  by  $O_2$  is also calculated for comparison purposes, and the reaction is a strong endothermic process adsorbing 3.59 eV. Therefore, both the perfect and the defective  $Cu_2O$  (111) surface models are favorable for the H-abstraction process of  $C_2H_2$  by  $O_2$  from the thermodynamic point of view, and the  $Cu_{CUS}$  defect will be beneficial for the H-abstraction of  $C_2H_2$  by  $O_2$ .

#### 3.4. H-Abstraction and H-Addition of Chemisorbed $C_2H_2$ by Atomic H

The reaction between a chemisorbed  $C_2H_2$  and an adsorbed atomic H via the LH mechanism is further studied in this section. The neighboring adsorbed atomic H, as shown in Figure 5, is bonded to the surface unsaturated  $Cu_{CUS}$  site, and it could attack the chemisorbed  $C_2H_2$  and form an adsorbed H<sub>2</sub> and an adsorbed HCCO species together with a lattice  $O_{CUS}$ . The reaction process is endothermic with energy adsorption of 0.78 eV, and the energy barrier is 2.75 eV. The chemisorbed  $C_2H_2$  could also react with an adsorbed H together with the lattice O to form a CH<sub>2</sub>CHO species, as shown in the right part of Figure 5, on the perfect Cu<sub>2</sub>O (111) surface model. The energy barrier of the reaction process is 1.78 eV, which is lower than that of the H-abstraction reaction of the adsorbed  $C_2H_2$  with an energy barrier of 2.75 eV. In terms of the reaction energy, the formation of CH<sub>2</sub>CHO needs to adsorb 0.67 eV, while the H-abstraction process adsorbs 0.78 eV. Therefore, the adsorbed  $C_2H_2$  is more likely to be converted to CH<sub>2</sub>CHO when reacting with an adjacent adsorbed H together with a lattice  $O_{CSS}$  site on the perfect Cu<sub>2</sub>O (111) surface model.



**Figure 5.** Energy profile of chemisorbed  $C_2H_2$  reaction with atomic H into  $CH_2CHO$  and HCCO on the perfect  $Cu_2O$  (111) surface model.

## 3.5. A Comparison of H-Abstraction Reactions of Chemisorbed C<sub>2</sub>H<sub>2</sub> by Different Radicals

The energy profile of the interaction between the chemisorbed  $C_2H_2$  species and the pre-adsorbed oxygen molecule and radicals, including H, OH, O, HO<sub>2</sub>, and CH<sub>3</sub>, on the perfect Cu<sub>2</sub>O (111) surface model are compared in Figure 6. The IS state also incorporates the energy release of various radicals on the surface unsaturated Cu<sub>CUS</sub> site after adsorption. The interaction between the O radical and the surface releases the largest amount of energy (-4.56 eV after adsorption), followed by HO<sub>2</sub>, OH, H, CH<sub>3</sub> radicals, and O<sub>2</sub> with the adsorption energy of -3.79, -3.61, -3.07, -2.21, and -1.09 eV, respectively. The energy barriers have been listed in the left corner of Figure 6. The H-abstraction of the chemisorbed  $C_2H_2$  by OH and O<sub>2</sub> have similar barriers, which are 1.39 and 1.43 eV, while the H-abstraction reactions by adsorbed HO<sub>2</sub>, H, CH<sub>3</sub>, and O radicals need to overcome higher energy barriers, which are 1.64, 2.75, 2.15, and 2.07 eV. The H-abstraction reactions by all the adsorbed radicals considered are exothermic except for H radical, indicating that the H-abstraction reactions on the perfect Cu<sub>2</sub>O (111) surface model is thermodynamically favorable.



**Figure 6.** Energy profiles of  $C_2H_2$  H-abstraction by various radicals on the perfect  $Cu_2O$  (111) surface model.

The energy profile of the interaction between the chemisorbed  $C_2H_2$  species and the pre-adsorbed oxygen and radicals, including H, OH, O, HO<sub>2</sub>, and CH<sub>3</sub> on the defective

Cu<sub>2</sub>O (111) surface model are compared in Figure 7. In general, the energy release of the radicals on the defective surface is lower than those on the perfect Cu<sub>2</sub>O (111) surface model, which is due to the absence of the unsaturated surface Cu<sub>CUS</sub> site. The adsorption of an atomic O on the defective Cu<sub>2</sub>O (111) surface model releases the highest amount of energy (-3.22 eV), which is located at the bridge site of two surface Cu<sub>CSS</sub> sites. The H-abstraction of the chemisorbed C<sub>2</sub>H<sub>2</sub> by the adsorbed O radical need to get over the 0.52 eV energy barrier, which is the lowest among all the considered radicals and O<sub>2</sub>, and it is also lower than that on the perfect Cu<sub>2</sub>O (111) surface model. The bridge site of two neighboring Cu<sub>CSS</sub> sites is also the adsorption site for OH radicals, and the energy barrier of the H-abstraction process by OH is 0.91 eV. The energy barriers of the H-abstraction by other adsorbed radicals, including O<sub>2</sub>, HO<sub>2</sub>, and H radicals are 0.97, 0.98, and 1.17 eV, respectively, which are more active than the same processes on the perfect Cu<sub>2</sub>O (111) surface activity toward the H-abstraction of C<sub>2</sub>H<sub>2</sub> via the LH mechanism.



Reaction pathway

**Figure 7.** Energy profiles of  $C_2H_2$  H-abstraction by various radicals on the defective  $Cu_2O$  (111) surface model.

## 3.6. Temperature Dependence of Elementary Reaction Rate Constants

The above-mentioned discussions are based on the DFT calculation results at 0 K, and the rate constants at elevated temperatures are more relevant to the real circumstances, and the temperate dependence of elementary reaction rates is discussed in this section. The Gibbs free energy of activation ( $\Delta G$ ) of the elementary reactions, including the C<sub>2</sub>H<sub>2</sub> chemisorption, C<sub>2</sub>H<sub>2</sub> direct decomposition, and H-abstraction of C<sub>2</sub>H<sub>2</sub> by O<sub>2</sub>, are shown in Figure 8.  $\Delta G$  denotes the Gibbs energy difference between the transition state and the initial state, and a larger  $\Delta G$  corresponds to a smaller reaction rate constant at a given temperature according to the transition state theory. Except for the reaction of H-abstraction by O<sub>2</sub> on the defective Cu<sub>2</sub>O (111) surface model, the  $\Delta G$  of all the considered reactions are positively correlated to the temperature. For the reactions of C<sub>2</sub>H<sub>2</sub> chemisorption and the direct decomposition of the chemisorbed C<sub>2</sub>H<sub>2</sub> into an adsorbed C<sub>2</sub>H and an atomic H species, the perfect Cu<sub>2</sub>O (111) surface model shows better performance over the defective Cu<sub>2</sub>O (111) surface model than the perfect one, so the defective surface could facilitate the H-abstraction process of C<sub>2</sub>H<sub>2</sub> by O<sub>2</sub>.



Figure 8. Gibbs free energy of activation of elementary reactions.

The reaction rate constants of elementary reaction steps are further calculated based on transition state theory, and the rate constants including  $C_2H_2$  chemisorption,  $C_2H_2$ direct decomposition, and the H-abstraction of  $C_2H_2$  by  $O_2$  are presented in Figure 9. The  $C_2H_2$  chemisorption process is more active on the perfect  $Cu_2O$  (111) surface model than on the defective Cu<sub>2</sub>O (111) surface model, and the reaction rate is about one order of magnitude higher. The  $C_2H_2$  direct decomposition rate constants are the slowest regardless of the perfect or the defective Cu<sub>2</sub>O (111) surface models compared with other elementary reaction steps considered in Figure 9, and the rate on the defective surface model is slower than on the perfect surface. The rate constant of H-abstraction by  $O_2$  on the defective surface model is remarkably higher than on the perfect one, and the rate constant is faster by about 4.4 orders of magnitudes at 1000 K. Therefore, the perfect Cu<sub>2</sub>O (111) surface model is more favorable for the C<sub>2</sub>H<sub>2</sub> chemisorption process, while the defective surface model could be beneficial for the H-abstraction reaction of  $C_2H_2$  by  $O_2$  over the considered temperature range from room temperature to 1000 K. In terms of the reaction rate constants, the direct decomposition of  $C_2H_2$  is less likely to proceed compared with the H-abstraction process. Therefore, the chemisorption and the succeeding H-abstraction process by  $O_2$ could be the possible partial oxidation reaction pathway of  $C_2H_2$  on the  $Cu_2O$  (111) surface model. The chemisorption of  $C_2H_2$  is the rate-determining step on the defective  $Cu_2O$  (111) surface model, and the H-abstraction by the O<sub>2</sub> process is the rate-determining step on the perfect Cu<sub>2</sub>O (111) surface model.



Figure 9. Reaction rate constants of  $C_2H_2$  chemisorption, decomposition, and H-abstraction processes.

The calculated rate constants are then converted into the Arrhenius form with the *A*, *n*, and *E* parameters provided in Table 1 for future heterogeneous kinetic modeling works.

**Table 1.** Calculated rate constants of  $C_2H_2$  elementary reactions on the perfect and defective  $Cu_2O$  (111) surface models, units are in K, kcal, mol, s, and cm.

No.	Elementary Reactions	A	п	Ε
R1	$C_2H_2$ chemisorption on the perfect $Cu_2O$ (111) surface	$5.11  imes 10^{13}$	-0.687	15.117
R2	$C_2H_2$ decomposition on the perfect $Cu_2O$ (111) surface	$1.15 imes10^{10}$	0.906	40.193
R3	$C_2H_2$ H-abstraction on the perfect $Cu_2O$ (111) surface by $O_2$	$3.16 imes10^{10}$	0.689	29.443
R4	$C_2H_2$ chemisorption on the defective $Cu_2O$ (111) surface	$1.98 imes10^{11}$	-0.021	18.130
R5	$C_2H_2$ decomposition on the defective $Cu_2O$ (111) surface	$5.13 imes10^7$	1.656	51.245
R6	$C_2H_2$ H-abstraction on the defective $Cu_2O$ (111) surface by $O_2$	$8.15  imes 10^{12}$	0.588	18.679

# 4. Conclusions

The adsorption and oxidation of  $C_2H_2$  on the perfect stoichiometric and Cu<sub>CUS</sub>defective Cu<sub>2</sub>O (111) surface models are studied using DFT calculations. The perfect  $Cu_2O$  (111) surface model is active in adsorbing the  $C_2H_2$  molecule with 1.13 eV adsorption energy and an energy barrier of 0.70 eV to form the chemisorption, while the adsorption of  $C_2H_2$  on the defective  $Cu_2O$  (111) surface model only releases 0.20 eV. The energy barrier of the  $C_2H_2$  chemisorption on the defective surface model is 0.81 eV which is close to that of the perfect model. The reaction rate of H-abstraction of the chemisorbed  $C_2H_2$  on the defective surface model is much faster than on the perfect surface model with the energy barrier decreasing from 1.43 to 0.97 eV at 0 K. The H-abstraction of  $C_2H_2$  by  $O_2$  is about 4.4 orders of magnitudes faster at 1000 K on the defective  $Cu_2O(111)$  surface model than on the defective Cu<sub>2</sub>O (111) model. Therefore, the surface defect featuring the absence of surface unsaturated  $Cu_{CUS}$  sites significantly facilitates the H-abstraction of  $C_2H_2$  by  $O_2$  process. The partial oxidation of  $C_2H_2$  on the Cu<sub>2</sub>O (111) surface model is likely to proceed by the chemisorption of  $C_2H_2$  and a succeeding H-abstraction process by  $O_2$ .  $C_2H_2$ chemisorption is the rate-determining step on the defective Cu<sub>2</sub>O (111) surface model and the H-abstraction process is the rate-determining step on the perfect  $Cu_2O$  (111) surface model. The activity of H-abstractions of  $C_2H_2$  via the LH mechanism by various radicals follows the order of  $OH > O_2 > HO_2 > O > CH_3 > H$  from high to low on the perfect Cu<sub>2</sub>O (111) surface model. On the defective Cu<sub>2</sub>O (111) surface model, the activity follows the order:  $O > OH > O_2 > HO_2 > H > CH_3$ .

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