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Entorhinal velocity signals reflect environmental geometry

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Summary

The entorhinal cortex contains neurons that represent self-location, including grid cells that fire in periodic locations and velocity signals that encode running speed and head direction. While the size and shape of the environment influences grid patterns, whether entorhinal velocity signals are equally influenced or provide a universal metric for self-motion across environments remains unknown. Here, we report that speed cells rescale after changes to the size and shape of the environment. Moreover, head direction cells re-organize in an experience-dependent manner to align with the axis of environmental change. A knockout mouse model allows a dissociation of the coordination between cell types, with grid and speed, but not head direction, cells responding in concert to environmental change. These results point to malleability in the coding features of multiple entorhinal cell types and have implications for which cell types contribute to the velocity signal used by computational models of grid cells.

Introduction

Navigation is a complex cognitive process requiring the integration of multi-sensory cues to form a unified percept of an animal's position in space. The neural substrates for generating this position estimate are thought to reside in the medial entorhinal cortex (MEC) and include grid cells, which fire in multiple spatial locations arranged in a hexagonal lattice¹. The emergence of periodicity in grid cell firing patterns despite frequent changes in an animal's running speed and direction led to the proposal that grid cells actively use self-motion cues to build a metric representation of the local spatial environment^{1,2}. This self-motion information may be derived from MEC velocity signals, including speed cells that

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Conflicts of Interest:

The authors declare no competing interests.

Data Availability

Data that support the findings of this study are available from corresponding authors on reasonable request.

Code Availability

Code used in the analyses described in this manuscript can be accessed at: https://github.com/GiocomoLab/Munn_et_al_2019. The code used in the Inp model can be accessed at: <https://github.com/GiocomoLab/In-model-of-mec-neurons>

change their firing rate as a function of running speed and head direction cells, which fire maximally when an animal faces a particular direction^{3–6}. However, recent work revealed that grid cells do not provide an invariant spatial metric across all environments and instead grid patterns deform, distort, and rescale in response to the geometric shape of local environments^{7–10}. Sensory landmark cues, such as environmental boundaries, play a key role in driving such structural changes to grid patterns^{11–13}. It remains unknown, however, whether velocity signals show flexibility in their coding in response to metric changes to the environment or contribute to environmentally driven changes in grid patterns. For example, MEC speed cells have been proposed to invariantly code for running speed across spatial contexts³ but these signals have not been broadly considered under conditions in which the geometric size and shape of an environment is altered^{3,9,10}.

Many computational models of grid cells use translational speed and movement direction to generate the velocity input that drives and updates grid cell firing patterns^{2,14–21}. These models provide frameworks for predictions regarding how velocity signals may respond to environmental perturbations. In attractor network models, grid cell firing results from the invariant translation of periodic activity bumps across a neuronal lattice^{2,14,16}. Inputs that reflect the running speed and direction of the animal drive the translation of the activity bumps and thus, determine the spatial scale and structure of the resulting grid firing patterns. Faster translation of the activity bumps, driven by stronger velocity inputs, results in smaller grid spatial scales^{2,16,17,22}. In oscillatory interference models, grid cells arise from multiple velocity-controlled oscillators (VCO), with changes in frequency driven by the animal's running speed and direction of movement relative to the preferred direction of each VCO. The degree to which velocity inputs change the frequency of the VCO can determine grid spatial scale^{19–21,23–25}. Both classes of models generate the untested prediction that if velocity input controls grid spatial scale, the grid rescaling observed after a parametric decrease in the size of an open arena^{9,10} should occur in concert with rescaling in the velocity input to the grid network^{16,25}. Whether this occurs experimentally however, remains unknown.

Here, we use single-cell in vivo electrophysiology to record from grid, head direction and speed cells in MEC as mice explore familiar and transiently compressed or expanded open arenas. We examine whether speed and head direction signals provide invariant self-motion signals across environments or change their coding in response to metric changes to the environment. To then more directly assess whether speed or head direction signals contribute to the rescaling observed in grid cells, we take advantage of the altered MEC speed signals observed after the loss of HCN channels in mutant mice²⁶.

Results

Behavioral paradigm

To examine how the firing patterns of MEC cells change after local environmental perturbations in mice, we recorded neurons in the superficial layers of MEC as mice foraged for randomly scattered food rewards in open arenas (see Methods). Mice explored either a familiar square followed by a compressed rectangle (compression condition: mouse $n = 25$, cell $n = 193$) or a familiar rectangle followed by an expanded square (expansion condition:

mouse $n = 16$, cell $n = 282$). Neuron matching between environments was determined by cluster matching and determination of cluster center of mass (Supplementary Figure 1). We identified cells as encoding position (P), head direction (H), or running speed (S) in their firing pattern using a statistical model based approach^{5,27} (see Methods). Quantifications of tuning curve features were then used for additional classification, such as identifying P-encoding grid and border cells.

Grid spacing in mice distorts after local environmental perturbation

We first considered grid cell patterns after local environmental perturbations (compression mouse $n = 14$, grid cell $n = 31$; expansion mouse $n = 5$, grid cell $n = 28$). We created a rescaled map by iteratively stretching (compression condition) or compressing (expansion condition) and translating (up to 20 cm in the vertical and horizontal axes) the rate maps observed in the rectangular arena (Figure 1a–b, Supplementary Figure 2). We then quantified the amount of stretching or compressing (λ rescaling factor) and translation needed to best correlate the baseline map with the rescaled map (Figure 1c, Supplementary Figure 3). Consistent with observations in rats^{9,10}, the grid pattern rescaled in response to changes in the local geometry of the environment (Figure 1c–d). In the compression condition, grid cells rescaled asymmetrically. Compared to baseline, the grid pattern was more elliptical in the modified environment, with grid spacing decreasing in the axis of compression but remaining unchanged in the static axis (Figure 1e–f). We observed the same result when using the autocorrelations of the rate maps (Supplementary Figure 3). In the expansion condition, grid cells rescaled symmetrically. Grid spacing was larger in both the expanded and the static axes (Figure 1h, Supplementary Figure 3), and the ellipticity of the grid pattern decreased (Figure 1e, h). In both conditions the spatial phase of grid maps also translated and the orientation of the grid pattern rotated, but this did not occur in a systematic direction (Figure 1g, Supplementary Figure 4). As in rats, grid rescaling was more pronounced for larger compared to smaller grid scales (Pearson correlation coefficient, rescaling factor (λ) and baseline grid node spacing (cm): compression $r = 0.47$, $p = 0.008$; expansion $r = 0.40$, $p = 0.03$) (Figure 1i–j, Supplementary Figure 5)¹⁰. Critically, the extent of rescaling was unrelated to running speed, average coverage (Supplementary Figure 6), number of exposures (< 13 per animal, Supplementary Figure 7A) or dorsal-ventral recording depth (Supplementary Figure 7B). These data demonstrate that grid firing patterns rescale in mice after systematic perturbations in the geometric shape of the spatial environment.

Speed coding and grid spacing rescale in concert

We next sought to determine if MEC velocity signals respond to environmental perturbations. We began by considering MEC speed cells that increase their firing rate with running speed³. We fit a linear function to the model-derived tuning curves of the firing rate by running speed (FR/RS) relationship in S-encoding cells (mouse n compression = 11, expansion = 8; S-encoding cell n , positive slope in baseline, compression = 21; expansion = 30). We observed a similar proportion of stable S-encoding cells between the compression and expansion condition ($X^2 = 0.007$, $p = 0.933$). Indicating that environmental perturbations impact speed coding, the FR/RS slope and intercept increased after environmental compression and decreased after expansion (Figure 2a–d). We then examined

whether there was axis specificity in the slope changes we observed after environmental perturbation. We considered the spike rate tuning curves of S-encoding cells relative to the animal's running speed in the compressed/expanded versus static axis (S-encoding cell n , positive slope in compressed/expanded or static axis in baseline, compression = 26, expansion = 36) (Figure 2e, 2g). After the environment was compressed, the slope was greater in the compressed compared to static axis, matching the asymmetry in grid spacing observed in the same condition (mean slope Hz/(cm/s) \pm SEM: compressed axis = 0.11 ± 0.02 , static axis = 0.05 ± 0.01 , $Z = 3.33$, $p < 0.001$) (Figure 2e and Supplementary Figures 8 and 9). In contrast, there was no difference in slope between the expanded and static axes in the expansion, matching the lack of asymmetry in the grid pattern in the same condition (mean slope Hz/(cm/s) \pm SEM: expanded axis = 0.05 ± 0.01 , static axis = 0.03 ± 0.01 , $Z = 1.24$, $p = 0.21$) (Figure 2f, 2h). The changes we observe in speed cell slope occurred independent of any systematic changes in running speed between environments (Supplementary Figure 10). These results reveal that speed cells are not invariant across all spatial contexts and instead, like grid cell firing patterns, show non-uniform changes in their coding features in response to changes in environmental geometry.

Providing an additional readout of speed coding, EEG measured theta-band activity (5 – 11 Hz) in MEC increases in frequency as a function of running speed^{26,28}. Consistent with the increase in speed cell slope in the compression condition, the mean frequency of theta and intercept of theta frequency by running speed increased in the modified compared to baseline environment ($n = 23$ mice, $n = 67$ sessions, mean frequency (Hz) \pm SEM: baseline = 8.66 ± 0.042 , modified = 8.77 ± 0.039 , $Z = 4.12$, $p < 0.001$; intercept (Hz) \pm SEM: baseline = 8.33 ± 0.037 , modified = 8.39 ± 0.041 , $Z = 2.89$, $p = 0.004$). Moreover, the slope of the frequency/running speed relationship increased in the compression, and decreased in the expansion (mean slope (Hz/(cm/s)) \pm SEM: baseline = $0.0011 \pm 1 \times 10^{-3}$, modified = $-0.0023 \pm 9.1 \times 10^{-4}$, $Z = 0.0096$, Figure 3 and Supplementary Figure 11). Likewise, consistent with the decrease in speed cell slope in the expansion condition, the mean frequency of theta and intercept of theta frequency by running speed decreased in the modified compared to baseline environment ($n = 11$ mice, $n = 74$ sessions, mean frequency (Hz) \pm SEM: baseline = 8.55 ± 0.024 , modified = 8.49 ± 0.031 , $Z = 2.67$, $p = 0.007$; intercept (Hz) \pm SEM: baseline = 8.19 ± 0.036 , modified = 8.13 ± 0.042 , $Z = 2.06$, $p = 0.039$) (Figure 3 and Supplementary Figure 11). These results, together with our observations of non-uniform changes in speed cell coding, point to environmental perturbations modifying MEC speed signals at several levels of granularity.

Experience-dependent asymmetry in head direction tuning

As a velocity signal consists of both speed and direction information, we next examined how head direction (HD) cells respond to environmental perturbations (compression mouse $n = 17$, H-encoding cell $n = 49$, expansion mouse $n = 9$, H-encoding cell $n = 103$) (Figure 4a). We observed a bias in the preferred firing direction of H-encoding cells along the compressed/expanded axis only in the asymmetric rectangular environment, regardless of whether this served as the modified environment for compression sessions or the baseline environment for expansion sessions. In the compression condition, the preferred firing directions of HD cells sampled all phase angles equally in the baseline square, but the

preferred direction of these cells clustered along the modified axis in the compressed rectangle (Kuiper test: baseline; $V = 0.20$, $p = 0.23$, modified: $V = 0.35$, $p < 0.001$). In the expansion condition, the preferred phase angles of HD cells aligned with the to-be-modified axis in the baseline rectangle, but redistributed their preferred phase angles to evenly cover the environment in the expanded square (Kuiper test: Baseline; $V = 0.26$, $p < 0.001$, Modified; $V = 0.14$, $p = 0.19$). Moreover, the distribution of preferred phase angles differed between baseline and modified environments for both conditions, demonstrating a remapping of directional preference between baseline and modified environments (Watson-Williams test: compression $F(1,96) = 10.41$, $p = 0.002$; expansion $F(1,204) = 15.01$, $p < 0.001$). In the compression, this directional bias appeared attributable to many cells that aligned with the compressed axis in the baseline environment (preferred angle $45^\circ - 135^\circ$ and $225^\circ - 315^\circ$) retaining their preferred direction in the modified environment (change in angle ($^\circ$) \pm SEM: baseline compressed axis aligned = 48.81 ± 9.45 , baseline static axis aligned = 86.32 ± 10.32 , $Z = 2.76$, $p = 0.006$) (Figure 4b–e). While many H-encoding cells changed their preferred directions, this did not occur with any systematic directional bias (change in angle ($^\circ$) \pm SEM: baseline expanded axis aligned = 76.94 ± 5.68 , baseline static axis aligned = 76.83 ± 8.72 , $Z = 0.02$, $p = 0.98$) (Figure 4b–d).

Firing rates were also greatest in the asymmetric, rectangular environment, regardless of whether this environment served as the baseline or modified environment (Figure 4e). In the compression, firing rates increased between baseline (square) and modified (rectangular) environments (mean FR \pm SEM: baseline = 1.06 ± 0.19 Hz, modified = 2.28 ± 0.38 Hz, $Z = 4.82$, $p < 0.001$). In the expansion, firing rates decreased between baseline (rectangular) and modified (square) environments (mean FR (Hz) \pm SEM: baseline = 3.19 ± 0.81 , modified = 1.77 ± 0.59 , $Z = 5.50$, $p < 0.001$) (Figure 4e). Unlike the bidirectional changes in preferred direction, the changes in firing rate appeared to be largely unidirectional, and primarily explained by changes in the directional bins that aligned with the moveable wall (Figure 4h–i, Supplementary Figure 12 and 13).

The development of the directional bias in H-encoding cells depended on experience. There was no significant bias in directional preference in the modified compression or baseline expansion condition during the first, or first three, environmental perturbation sessions (Kuiper test, first exposure: compression modified, $n = 12$, $V = 0.36$, $p = 0.36$; expansion baseline, $n = 7$, $V = 0.42$, $p = 0.48$; Kuiper test, first three exposures: compression modified, $n = 24$, $V = 0.33$, $p = 0.08$; expansion baseline $n = 23$, $V = 0.27$, $p = 0.28$) (Figure 4f–g). Starting with the fourth exposure however, the bimodal bias appeared in the modified compression and baseline expansion condition (Kuiper test, compression modified, $n = 25$, $V = 0.34$, $p = 0.04$, expansion baseline, $n = 80$, $V = 0.30$, $p < 0.001$) (Figure 4f–g). By contrast, the change in firing rate between environments was present on the first exposure to the modified environment (mean FR (Hz) \pm SEM: compression baseline = 1.19 ± 0.43 , modified = 2.31 ± 1.01 , $p = 0.01$; expansion baseline = 1.90 ± 0.36 , modified = 1.00 ± 0.19 , $p = 0.03$) and persisted on three and more exposures (mean FR (Hz) \pm SEM: compression baseline = 1.08 ± 0.25 , modified = 2.46 ± 0.55 , $Z = 3.38$, $p < 0.001$; expansion baseline = 4.03 ± 1.09 , modified = 2.00 ± 0.76 , $Z = 5.37$, $p < 0.001$). This experience dependent development of directional bias in the head direction signal contrasts with grid rescaling, which does not vary with session number (Supplementary Figure 7). Combined, these data

suggest a dissociation between speed and directional signals, and that MEC head direction cells may not serve as the directional component of a velocity signal. Rather, head direction signals may reflect a learned signal regarding the direction in which the environment will change or learned knowledge of asymmetry in environmental geometry.

HCN-channel auxiliary subunit TRIP8b deletion reduces grid rescaling

One challenge to examining how MEC velocity signals influence grid cells is the heterogeneous nature of speed coding in MEC, with running speed encoded by both putative excitatory and inhibitory cells, as well as in the frequency of EEG measured oscillatory activity^{3-5,28}. To more directly dissociate the contribution of speed and head direction to grid cell rescaling after environmental perturbations, we next took advantage of the altered speed signals previously observed after the loss of forebrain HCN channels^{26,29,30}. Here, we considered grid, head direction and speed cells in Pex51 knockout mice lacking tetratricopeptide repeat-containing Rab8b-interacting protein (TRIP8b), an accessory subunit necessary for the insertion of HCN channels into the post-synaptic membrane, the loss of which significantly attenuates the HCN conducted hyperpolarization-activated current³¹.

First, we examined grid cells in TRIP8b knockout (KO) mice in the compression condition (mouse $n = 9$, grid cell $n = 27$). Consistent with previous work²⁶, we observed larger grid spacing in TRIP8b compared to WT grid cells at equivalent dorsal-ventral depths (Supplementary Figure 5). Compared to wildtype (WT) mice, grid cells in KO mice showed significantly less rescaling (mean λ rescaling factor \pm SEM: WT = 0.34 ± 0.057 , KO = 0.21 ± 0.065 , KS = 0.44, $p = 0.0047$, Figure 5a–b) and did not change in ellipticity between baseline and modified environments (mean ellipticity \pm SEM: baseline = 1.55 ± 0.15 , modified = 1.49 ± 0.07 , Z = 0.40, $n = 19$, $p = 0.69$) (Figure 5c). Moreover, unlike grid cells in WT mice, there was no difference in grid spacing in either the compressed or static axis between baseline and modified environments (mean spacing (cm) \pm SEM: compressed axis baseline = 50.32 ± 2.02 , modified = 49.16 ± 2.16 , Z = 0.29, $p = 0.77$; static axis baseline = 40.67 ± 2.13 , modified = 36.79 ± 1.78 cm, Z = 1.66, $p = 0.097$) (Figure 5d–e). The difference in grid rescaling between WT and KO mice did not reflect differences in baseline spatial stability, overall poorer peak correlations between baseline and rescaled rate maps or larger amounts of translation in the spatial phase of grid maps (mean spatial stability \pm SEM: WT = 0.35 ± 0.037 , KO = 0.28 ± 0.035 , KS = 0.29, $p = 0.145$) (Figure 5f–g). Together, these results indicate that the loss of HCN channels via TRIP8b KO renders grid cells less sensitive to environmental deformation.

Speed coding remains stable after environmental perturbation in TRIP8b KO mice

To assess the relationship between speed coding and grid rescaling after environmental perturbation, we examined the coding features of speed cells in TRIP8b KO animals in the compression condition (mouse $n = 11$, S-encoding cells $n = 76$) (Figure 6a). Similar proportions of cells encoded speed in WT and KO mice in baseline (WT = 27.46 %, $n = 53/193$, KO = 21.05 %, $n = 16/76$, $X^2 = 1.09$, $p = 0.30$). However, compared to WT mice, very few KO S-encoding cells retained their speed coding in the compressed environment (WT = 12.04%, $n = 23$, KO = 3.94% $n = 3$, $X^2 = 3.97$ $p = 0.046$, Figure 6b). This loss in S-

encoding cells was significantly more than would be predicted based on the proportion of S-encoding cells observed in the WT compression group (TRIP8b KO $n = 4/104$ cells, WT compression $n = 21/193$ cells, $X^2 = 4.34$, $p = 0.04$). Given the small number of stable S-encoding cells in the KO group, we also considered speed coding using a traditional score-based approach (speed score $P95 = 0.045$, speed cell $n = 12$; see Methods). However, even when considering this more broadly defined speed cell population, there was no difference in the FR/RS slope between baseline and modified environments in KO mice (mean slope (Hz/(cm/s)) \pm SEM: baseline = 0.034 ± 0.007 , modified = 0.027 ± 0.007 , $p = 0.73$) (Figure 6c–d). This contrasted with a significant increase in slope in WT mice when using the same cell classification criterion (speed cell $n = 58$, mean slope (Hz/(cm/s)) \pm SEM: baseline = 0.042 ± 0.006 , modified = 0.057 ± 0.009 , $Z = 2.31$, $p = 0.02$, Supplementary Figure 9).

A comparable lack of change in speed coding was also observed for oscillatory activity in the theta-band (5 – 11 Hz) in MEC. As expected from previous work, theta frequency was lower in KO compared to WT mice in baseline (session $n = 53$, mean frequency \pm SEM: WT = 8.33 ± 0.037 Hz, KO = 7.87 ± 0.029 Hz, $Z = 7.79$, $p = 6.717^{-15}$) (Figure 6e–g)^{29,30}. In contrast to WT animals, there was no difference in theta frequency between the baseline and modified environment (mean frequency \pm SEM: baseline = 7.87 ± 0.029 Hz, modified = 7.91 ± 0.033 Hz, $Z = 1.72$, $p = 0.086$). There also was no difference in the slope of the running speed/frequency relationship in KO animals between baseline and modified environments (mean slope (Hz/(cm/s)) \pm SEM: baseline = 0.0069 ± 0.0012 , modified = 0.0076 ± 0.0010 , $Z = 0.35$, $p = 0.73$) (Figure 6f–g). Together, these results point to coupled responses of speed and grid cells to changes in environmental structure and raise the possibility that MEC speed inputs are necessary to update grid cell estimates of position.

Bias in head direction coding after environmental perturbation in TRIP8b mice

Unlike the relative inflexibility of the grid and speed code to environmental perturbations, head direction cells (mouse $n = 12$, H-encoding cell $n = 47$) in KO mice showed signatures of re-organization in line with those observed in WT mice (Figure 6h). Unlike the speed signal, there was no difference between WT and KO in the proportion of cells that retained their directional coding between baseline and modified environments (WT = 25.65%, KO = 25%, $X^2 = 0.012$, $p = 0.91$) and, as in WT mice, the mean firing rate of HD cells significantly increased between environments (mean firing rate (Hz) \pm SEM: baseline = 1.19 ± 0.19 , modified = 2.31 ± 0.48 , $Z = 2.05$, $p < 0.04$). Moreover, as in WT animals, there was a reorganization of preferred directions in the modified environment compared to baseline (Figure 6i–m). As in WT, in the baseline square, the preferred directions of KO HD cells were distributed around all headings, but there was pronounced bidirectional anisotropy in the preferred direction of HD cells in the compressed rectangle (Kuiper test; baseline: $V = 0.19$, $p = 0.38$, modified: $V = 0.30$, $p = 0.005$) (Figure 6l). As in WT HD coding cells, the reorganization of phase angles in KO HD coding cells was experience dependent. There was no apparent clustering of phase preferences on the first exposure to the modified environment, but there was apparent clustering after this initial exposure (Kuiper test: modified environment, first exposure, $n = 10$, $V = 0.37$, $p = 0.39$; modified environment, more than one exposure, $n = 37$, $V = 0.32$, $p = 0.011$). These changes in the KO head direction cell population contrast with the insensitivity of grid cells and MEC speed codes to

environmental perturbation, pointing to head direction cells in MEC contributing a directional signal that can be uncoupled from grid and speed signals.

Discussion

We observed changes in the MEC speed signal that closely matched the changes in grid cells after environmental deformation. Critically, when there was an asymmetric change in grid spacing, there was a matching asymmetric change in the speed cell signal. Complementary to this, expanding the environment from an asymmetric rectangle to a symmetric square caused a symmetric change in grid spacing and a matching symmetric change in the speed cell signal. These results contrast with the previous proposal that speed cell coding is context-invariant³.

Attractor-network and oscillatory interference based models of grid cells assume a velocity input to the grid network composed of translational speed and movement direction^{2,14–21}. The observation of analogous changes in the slope of speed signals (Figures 2 and 3) and grid rescaling (Figure 1) in both the compression and expansion condition is broadly consistent with predictions of both classes of model (Supplementary Figure 14). On the other hand, HD cells re-organize over a longer time scale (~3 days of exposure) than grid rescaling (Supplementary Figure 4). Moreover, HD firing directions show bi-modality in the asymmetric rectangle environment (Figure 4), regardless of whether it served as the modified or baseline condition, and in KO mice grid cells do not rescale even though HD cells show strong re-organization (Figures 5 and 6). These observations are inconsistent with predictions of both attractor-network and oscillatory interference based grid cell models (Supplementary Figure 14). First, many attractor models use grid by head direction cells to provide the movement direction signal to the grid cell population^{2,14–17}. Second, the generation of the grid cell firing patterns in many oscillatory interference models depends on VCO inputs with preferred directions offset by 60°^{18,20,23,24}, with computational work suggesting that unsupervised Hebbian learning can establish such connections^{18,32}. Thus, the reorganization observed in head direction signals between baseline and modified environments would require re-learning these connections and, until the proper connections were re-established, resulting in distortions and disorganization in the grid pattern^{23,24} (Supplementary Figure 14) which we do not observe in our data. However, combining features of oscillatory interference models with network dynamics, which has been shown to improve the robustness of the grid pattern to perturbations in directional inputs, could be an avenue for future computational work^{24,33}.

While the changes in head direction signals we observed after environmental perturbation suggest MEC head direction cells may not serve as the movement-direction signal required by grid cell models³⁴, our findings do not rule out that the directional component of a velocity signal may be represented by a small subset of MEC cells, or derive from head direction signals originating in another region^{34–38}. A complementary influence on grid rescaling could come also from landmark-driven or boundary-tethered shifts in grid phase^{7,8,11,13,24,39,40}. Future computational work could thus also further consider networks in which the speed component of the velocity input combined with sensory-driven adjustments to the phase of the grid network drive the grid rescaling observed after environmental

perturbations^{12,24,25,40}. Finally, the bimodal nature of the head direction organization we observed raises the possibility that MEC head direction cells provide directional information that is relative to an internal reference frame⁴¹. This type of code is reminiscent of head direction signals in retrosplenial cortex, a brain region with strong reciprocal MEC connections, and that contains bidirectional head direction cells that anchor their preferred firing angle to local landmarks⁴².

The mechanism by which speed signals asymmetrically rescale to reflect changes in environmental geometry remains unknown. Previous work has found that speed cells determine a component of their movement estimates from visual cues^{12,43}, which could involve optic flow information derived from movement relative to static visual landmarks or visual features on the ground plane^{25,44}. Thus, one possible mechanism for the observed speed cell asymmetry is that MEC speed cells use learned visual angles of landmarks to estimate the relative motion between the animal and environment^{25,44}. Regardless of the mechanism however, our data indicate that speed cells are not static across environmental conditions as previously suggested³ but rather, can rescale in a manner similar to grid patterns to reflect changes in the geometry of the spatial environment^{9,10}.

Finally, the loss of rescaling in spatial and speed codes after KO of TRIP8b sheds light on the potential mechanisms underlying these phenomena. HCN channel expression controls membrane integration kinetics and thus, the loss of HCN channels could impact the sensitivity of MEC grid and speed cell responses to changes in self-motion cues⁴⁵. HCN channels also play a key role in generating rhythmic activity in the medial septum^{29,30}, which contains MEC projecting neurons that encode running speed in their firing rate⁴⁶. As the MEC grid network likely depends on multiple inputs to estimate a speed signal¹³, the loss of HCN channels in the medial septum could impair speed coding at the level of both rate-coded speed inputs to MEC and the frequency modulation of theta oscillations by running speed. It also remains unknown if the loss of HCN impacts processing in higher-order visual cortices, which encode differences in movement speed and the spatial frequency of stimuli^{47,48}, as well as running speed⁴⁹. The loss of TRIP8b also reduces the expression of HCN1 in the retina, which may result in visual features carrying less information regarding the animal's velocity⁵⁰. However, determining precisely what intrinsic or network properties result in the loss of grid and speed rescaling in TRIP8b KO animals awaits the development of approaches that can specifically target these cell-types.

Methods

Subjects

All procedures were approved by the Institutional Animal Care and use Committee at Stanford University School of Medicine. Male C57BL/6 (WT, n = 31) and TRIP8b knockout (KO) mice (n = 16; donated by D. Chetkovich, Department of Neurology, Vanderbilt University) were housed in groups of between one and five same-sex littermates. TRIP8b mice were generated from a C57BL/6 background, as previously described³¹, and bred at Stanford University School of Medicine. After surgical implantation, mice were housed singly in transparent cages on a 12-hour light/dark schedule. All experiments were conducted during the light phase. Animals were between 1 and 6 months old at time of

surgery (18–30 grams). Prior to surgery, animals had *ad libitum* access to food and water. After three days had elapsed post-surgery, animals were food-restricted to maintain ~ 80% of their free-feeding weight. All animals continued to have free access to water. Fifteen WT mice were recorded in the environmental compression condition, and 16 WT mice were recorded in the environmental expansion condition. Data collection was not performed blind to the conditions of the experiments; the experimenter was not blind to the condition of the mice (either genotype or recording geometry) during the experiments. During analysis, the same procedures were run on all data in batch format, and the results then segregated into experimental groups post hoc. Wildtype animals were randomly assigned to either compression or expansion groups, TRIP8b KO animals were manually assigned to compression.

Surgery

Animals were given prophylactic and initial anesthesia by intra-peritoneal injection of buprenorphine (0.1 mg/kg) and were then maintained under anesthesia via inhalation of a mixture of oxygen and between 0.5 – 3% Isoflurane. Mice were implanted unilaterally with a two tetrode, 8-channel Microdrive (Axona Ltd.) connected to 17 μ m polyimide-coated 90% platinum 10% iridium wire tetrodes cut flat. Just prior to implantation, the tips of the electrodes were electroplated with platinum until their measured impedance ranged between 150–200 k Ω . During surgery the skull was thinned over the putative target site at between 3.2–3.3 mm from the midline and 0.5 mm posterior to lambda until the transverse sinus was visualized. Electrodes were then implanted 0.5 mm anterior to the sinus at an angle of between 2–6 degrees caudal in the sagittal plane. Six stainless steel jeweler's screws were threaded into the skull at intervals around the incision site, and the Microdrive assembly was affixed to the skull using acrylic dental cement. One of the anterior skull screws was soldered to a ground wire, which was then connected to the Microdrive ground pin. After surgery, animals were continuously monitored until they recovered, then monitored on an hourly basis for the first six hours, and on a 12 hour basis for the first three days post-surgery. During the 3 post-surgery days, animals were administered Carprofen analgesia as required. After at least 3 days post-surgery, animals were habituated to the baseline recording environment that corresponded to their assigned group (i.e. a rectangular or square environment see "In vivo single-unit data collection"). Recordings began 7 days post-surgery.

In vivo single-unit data collection

Animals in the compression condition were screened for single units in a 1 \times 1 m square box, while animals in the expansion condition were screened in a 0.5 \times 1 m rectangular box, created by the insertion of a removable wall 0.5 m into the 1 \times 1 m environment. The environments were constructed of black polycarbonate, and each environment featured a white paper cue card affixed to the static wall on the opposite side from the movable wall. The moveable wall itself was constructed of the same material as the rest of the environment and was the same height as all the walls (0.5 m). Black curtains surrounded the perimeter of the recording environment. During recordings, mice were connected to an eight channel headstage that consisted of AC-coupled unity-gain operational amplifiers and connected through a counterbalanced cable to a DACQUSB pre-amplifier and system unit (Axona Ltd).

Acquired signals were amplified between 5,000 and 20,000 times, and then band-pass filtered between 800 and 6,700 Hz. A threshold for signals was manually selected and the resultant spikes were stored at a sampling rate of 48 kHz. One of the channels was manually selected to be simultaneously used for recording EEG. This channel was digitally amplified 3,000–10,000 times and lowpass filtered at 500 Hz with a notch filter at 60 Hz. This channel was simultaneously recorded at high resolution at 48 kHz and lower resolution at 250 Hz. The EEG trace was saved continuously to disk. Animal position was stored alongside the electrophysiological recordings through means of tracking two groups of light-emitting diodes (LEDs); one “large” consisting of four individual LEDs and one “small” consisting of two individual LEDs. These LEDs were recorded by a camera mounted over the recording environment.

Each animal underwent no more than one condition (baseline and modified environments) per day before being returned to its home cage and then to the vivarium. During the recordings, animals were free to explore the environment and were encouraged to free forage with randomly scattered crumbled chocolate cereal. Animals were screened in the baseline environment for the presence of single units. All baseline recording sessions lasted at least 10 minutes and continued until the animal had covered more than 70% of the recording environment, or 60 minutes had elapsed. If 60 minutes elapsed and animals failed to cover 70% of the recording environment, they were removed from the baseline environment, returned to their home cages, and screened again the next day. If cells of interest were isolated during the baseline recording session, animals were immediately transferred to a modified environment (for WT mice in the compression experiments and TRIP8b KO mice, this was a 1 m x 0.5 m rectangle; for mice in the expansion experiments this was a 1 m x 1 m square). Animals were recorded in the modified environment for at least 10 minutes and until they had covered at least 70 % of the environment, or 60 minutes had elapsed. If the animal had not covered > 70 % of the environment after 60 minutes it was removed from the modified environment, returned to its home cage, and the data was not used except to determine the number of exposures each animal had to the modified environment. If no units of interest were uncovered or all data had been collected at a given recording depth, the tetrodes were advanced between 25 and 100 μm at the end of the recording in the baseline environment and the animal was returned to its home cage until the following day. The recording environments were cleaned immediately after each recording by spray-on and wipe-down application of Nature’s Miracle stain and odor eliminator (Spectrum Brands Inc.)

Spike sorting and 2-D position estimation

Spikes were analyzed offline using a vendor-specific cluster-cutting software (TINT, Axona Ltd). Initial clustering was performed manually by examining spikes one dimension at a time in multidimensional feature space. Initial clustering was done using amplitude comparison of each channel on a given tetrode against all other channels. Spikes and positions recorded from epochs during which animals ran < 2 cm/s or > 100 cm/s were excluded. Only clusters with more than 100 spikes remaining after this exclusion were used for further analysis. Cluster quality and separation distance was calculated for each putative cell post-hoc. Cluster separation was calculated by determining the distance, in Mahalanobis

space, between the putative spikes belonging to one cells from spikes belonging to all other cells recorded on the same tetrode⁵¹. Cluster matching between baseline and compressed environments was performed manually using cluster location and waveform comparison. The center of mass of each resulting cluster in voltage space was then determined. The center of mass of each cluster in the baseline and modified environments was used to determine drift in the center of mass between the recording sessions (See Supplementary Figure 1). Putative interneurons were separated from putative excitatory cells by examining spike rate and spike width. Digitized position data was binned into 2.5×2.5 cm bins and smoothed using a 21-sample boxcar filter using a 400 ms window, with ten samples on each side. A 5×5 bin quasi-Gaussian kernel was used to filter time and spiking maps. The firing rate of each cell was calculated from these smoothed maps by dividing the number of spikes in each bin by time spent in the respective bin. The peak rate was determined from the bin with the highest firing rate. To calculate scores (i.e. grid, speed, and mean vector length) maps were adaptively smoothed⁵².

Histology and determination of recording positions

Data collection ceased when the signal to noise ratio precluded the successful isolation of spikes or the animal was exposed to the modified environment for more than 13 sessions – whichever came sooner. Due to the angle of implantation of the tetrodes, the development of noise on many channels typically indicated that the electrodes had passed through MEC and into the extracortical space. Mice were given an acute intraperitoneal overdose of sodium pentobarbitone and transcardially perfused with 0.9% saline to remove blood from the circulatory system, and then with 4% paraformaldehyde to fix the tissue. Animals were decapitated and left for several minutes to allow for shrinkage of the brain tissue. The tetrodes were then wound as far up their travel allowed, and then the skull was removed allowing the brain to be removed. Brains were then stored in 4% paraformaldehyde solution until sectioning. In all cases, an attempt was made to electrolytically lesion the final position of the electrodes. The lesions were made after overdose by passing 20- μ A current for 10–15 seconds through two of the channels on each tetrode. In animals for which the electrodes had exited the brain, no lesion was evident, and the electrode tracks were used to determine the sites of recording.

For sectioning, brains were removed from the fixation solution, the hemisphere of interest was isolated by hemispheric transection of the brain in the sagittal plane, and the brains were rapidly frozen. Brains were sagittally sectioned into 40 μ m sections using a ThermoFisher HM 550 cryostat, mounted, and stained with Cresyl violet. Mounted stained sections were then manually inspected microscopically to visualize the electrode tracks and determine the path of the electrodes. In cases where the electrode track ran to the edge of the slice, the edge of cortex where the track terminated was used as the final electrode position. In mice for which a lesion was evident, the center of the lesion was determined to be the final position of the electrodes. The border of MEC was determined from the lateral position of the electrodes which was determined primarily by the cytoarchitecture of the nearby hippocampus and cross-referenced with a stereotaxic atlas⁵³.

Shuffling

For each cell in the dataset of 555 cells that were recorded in the baseline and modified environments, 100 shuffles of the spike trains were produced, and each shuffled spike train was used to compute a grid score, a speed score, a directional mean vector length, and a speed stability score. These variables were calculated in the same way as the original datasets. Each cell's spike train was shuffled by transposing each spike a random interval from 20 seconds prior to its true position, or up to 20 seconds ahead of its position. From the resulting arrays of 55,500 shuffles, the 95th percentile was determined using the *prctile* function in the statistics toolbox of MATLAB 2017b. Spatial shuffling of grid cells was achieved by randomly re-distributing the spikes recorded over the session to a random point on the animal's trajectory. For each cell, 500 shuffles of the modified ratemap were made, and the 95th percentile of each cell's 500 shuffles was determined using the *prctile* function.

Tuning curve classification and thresholding

As we limited the number of times an animal could experience the modified environment, we first screened cells in the baseline to identify cells of interest to be recorded in the modified environment. This screening process used score methods to classify functionally-defined cell types^{54,3}. Spatial maps were produced from all recordings such that the location of the animal was divided into 2 cm x 2 cm bins, and the mean spikes/bin for the recording was determined. Gridness scores were calculated from the autocorrelation of the rate map at 60 and 120 degrees compared to 30 and 90 degrees, as previously described^{54,55}. Speed scores were calculated as the Pearson correlation between the smoothed instantaneous firing rate of the cell and the running speed of the animal in 20 ms time bins, as previously described³. The stability of the firing rate/running speed relationship was calculated as in Kropff, et al³; briefly, each recording session was divided into equal quarters, and the mean firing rate for each 2 cm/s speed bin from 5–50 cm/s was calculated. Stability was calculated as the mean correlation coefficient over each tuning curve. Directionality was determined from the mean vector length of a cell's firing over all directions; more unidirectionally specific cells produced a greater mean vector length, and vice versa. Briefly, mean vector length was calculated from the mean firing rate in each 0.5 degree directional bin that was then smoothed using a 14.5 degree mean window filter as in Mallory et.al²⁷. For the purposes of determining whether cells were of interest for inclusion in the environmental manipulation sessions, we used conservative score-based cutoffs informed from shuffled score distributions from previous similar experiments^{26,27}. Specifically, cells were classified as of interest if they had a grid score > 0.35, speed score > 0.05, or a mean vector length over 0.2.

Cell classification using the linear-non-linear Poisson spiking (LNP) model

After data collection, we employed a statistical model based approach to identify which neurons carried significant information about position (P), head direction (H), and running speed (S)^{5,27}. Following previous work, we determined the minimum set of variables encoded by each neuron by using a greedy forward-search feature selection method in combination with 10-fold cross-validation⁵. In short, variables were added to the model if they significantly improved model-fit (quantified through log-likelihood increase from a

baseline model) on held out data. Models were fit by minimizing the negative Poisson log-likelihood of the observed data (spike-trains) given the model prediction using MATLAB's `fminunc` function. Models that did not significantly encode any variables (e.g. model performance was not above a baseline mean-firing rate model) were labeled “unclassified.” Regressors for each variable (e.g. position) were computed based on spline interpolation between set control points (position $n = 144$, head direction $n = 12$, speed $n = 21$). After the model-fitting procedure, we computed model-derived tuning curves for each encoded variable using the set of learned parameters. To distinguish different types of speed-encoding, we fit an additional model that split speed into its directional components; e.g. the model considered position (P), head direction (H), speed in the x-direction (Sx), and speed in the y-direction (Sy) as external covariates that could predict cell spiking. Model selection and model-fitting were otherwise identical.

Analysis of grid cells

Grid scores were calculated from the rate maps of each cell. Cells were classified as grid cells if their score exceeded the 95th percentile of the distribution of grid scores produced from the entire shuffled data set (55500 shuffles). We considered only those cells with a threshold-crossing grid score ($P95 = 0.35$) that also significantly encoded position (P) according to the LNP model. Specifically, grid cells were only included if the LNP model determined that the grid cell coded for position in the baseline condition, and continued to be detected as coding position in the modified condition. The distance from the center of each autocorrelogram to each of the surrounding six autocorrelation nodes was used to compute the grid spacing; the pair of nodes closest to the axis that was modified (i.e. compressed or expanded) was used to determine node spacing in the “modified” axis, and the set of nodes closest to the orthogonal axis were used to determine the spacing in the “static” direction (mean node orientation (degrees) \pm SEM: WT compressed orientation = 57.04 ± 3.78 , static orientation = 4.11 ± 5.94). In order to determine the ellipticity of the grid pattern, local maxima in the autocorrelation maps were determined using the `imextendedmax` function in the image processing toolbox of MATLAB (2017b). An ellipse was then fit to these identified maxima using a least-squares method^{10,56}. This procedure occasionally failed to fit an ellipse to the identified maxima, reducing the overall number of grid cells in this analysis. For the grid cells to which an ellipse was successfully fit, the ellipticity (ϵ) of each cell was then computed as a ratio between the semi-major (α) and semi-minor (β) axes of this fitted ellipse.

$$\epsilon = \frac{\alpha}{\beta}$$

This produced an ellipticity value between 1 (a perfect circle) and infinity (∞ , the point at which the ellipse becomes parabolic). From this ellipse, the semi-minor and semi-major axes, and hence the ellipse ellipticity and eccentricity were determined.

In order to determine the amount of deformation of the grid pattern in the modified environments compared to the baseline environments, we expanded the rectangular map using the `imresize` function in MATLAB 2017b. This procedure produced a stretched (re-

scaled) version the rectangular environment map over an array of values that each differed by a single spatial bin width (2 cm). This rescaling was only performed in the direction of environmental change. Each re-scaled map was also translated in 1 cm increments (up to 40 cm, 20cm in each direction of each cardinal axis) in both the x and y dimensions. Each re-scaled and translated map was then correlated against the corresponding square map. From the resultant matrix of correlations (Supplementary Figure 2), the combination of re-scaling and x and y translation that produced the optimum correlation (Rho) was selected to derive the proportion of deformation of the modified environment map at this point. This value (λ) was a value ranging between 0 (best correlation when the rectangular map was not resized) and 1 (the best correlation was achieved when the rectangular map was resized such that it matched the dimensions of the corresponding square map). In order to validate this procedure, the spatial autocorrelation maps produced from each grid cell's baseline and modified environments were compared in a similar way. First, to control for changes in orientation and remapping that may have occurred between environments, at each rescaling of the rectangular autocorrelation map, it was also rotated in 1 degree increments from -45 to 45 degrees and correlated against the corresponding section of the modified map (see Supplementary Figure 3) until the best correlation between these maps was found.

Analysis of direction-encoding cells

During initial screening in the baseline experiments, cells of interest were determined based on their head direction mean vector length score, as previously described. Directionality in all of the 555 cells in the dataset was determined post-hoc using the LNP model. This method captured cells that were considered traditionally "directional" using the score-based criterion (All model directional cells ($n = 171$): mean vector length \pm SEM, baseline = 0.29 ± 0.02 , modified = 0.25 ± 0.02), but also uncovered cells with unconventional tuning curves that nevertheless still encoded direction. The LNP model produced a direction-conditioned tuning curve for each cell, which was divided into 60 bins of 0.1047 radians (6 degrees). The "preferred" direction of each directional cell was therefore determined from these tuning curves for each recording as the direction of maximal firing. The mean firing rate of each neuron for each recording was determined as the average over the firing rate in each of the 60 equally-sized directional bins for each recording.

Analysis of speed-encoding cells

During initial screening in the baseline experiments, cells of interest were determined based on their tuning curve-based speed score, as previously described. Cells that coded speed were identified post-hoc by the LNP model. As with H-encoding cells, these model-identified cells often included cells that had a super-threshold speed score, but also included some cells that would ordinarily have been overlooked by traditional shuffling methods (All S-encoding cells ($n = 55$) speed score \pm SEM: baseline = 0.162 ± 0.018 , modified = 0.105 ± 0.018) The speed-conditioned spike tuning curves of these cells was derived from the model; and provided the speed/firing rate relationship. The overall slope and intercept of this relationship was determined for each speed encoding cell by the fitting of first-degree (linear) polynomial through these data by using the *polyfit* function in MATLAB. In order to determine the speed/firing rate relationship of these cells in each individual axis, the 2D speed-conditioned tuning curve in the initial LNP model was reduced to two 1D curves, each

conditioned on speed in only the x or y axis. Slope and intercept of these relationships was determined as for the overall 2D model. During recording, cells identified as interneurons were deliberately excluded from the recording sessions, so all speed cells were putative excitatory cells. We restricted our analyses to those cells that positively encoded speed in the baseline environment (that is, the slope of their firing rate/running speed relationship was positive).

Analysis of theta-band EEG

EEG was recorded in baseline and modified environments simultaneously with single units. Sessions were included in analysis if both baseline and modified recording sessions met the same criteria as single units (> 70% coverage of the environment after epochs at which the movement of the animal was less than 2 cm/s or over 100 cm/s were excluded). Analyses of theta band EEG were carried out using data sampled at 250 Hz. EEG was bandpass filtered between 5 and 11 Hz and subjected to a Fourier transform in order to produce a power spectrum. The frequency at which the power peak occurred was determined for both the baseline and modified recording sessions. Instantaneous power, phase, and frequency were derived using a Hilbert transform. We determined the slope and intercept of the running speed/theta frequency relationship by linearly regressing these data using a least-squares method.

Simulations of the attractor network models of grid cells

The attractor model was implemented following the model described in Fiete et al., 2009 and was simulated using the code available from <http://clm.utexas.edu/fietelab/code.html>. To match the 2-dimensional open field recordings, we ran the 2-dimensional spiking attractor model (with periodic boundary conditions). In brief, this model simulates the activity of 128^2 recurrently connected neurons, where each neuron inhibits its neighboring neurons when arranged on a 2-d ‘neural sheet’ and receives broad-field excitation. This connectivity pattern results in a grid pattern of activity across the neural sheet. When each neuron receives directionally-sensitive velocity input, and has a corresponding offset in its outgoing connections, the grid pattern on the neural sheet moves in tandem with the animal’s velocity and generates a single-cell grid pattern of activity in an open environment. The scale of the grid pattern in the open field is determined by how ‘fast’ the grid pattern on the neural sheet moves in relation to the animal. To probe the relationship between grid scale and the velocity signal, we altered a parameter that controls this relationship (alpha). Increasing this parameter could correspond to increasing the slope of the speed signal, or increasing the gain of the input from head direction cells. By changing this parameter in a direction-dependent manner (i.e. changing this parameter only for cells that receive north-south or east-west inputs), we can mimic the direction-dependent changes we observed in the speed cells.

Simulations of the oscillatory interference models of grid cells

Simulations were implemented following a slightly modified version of the model presented in Burgess and O’Keefe, 2005. In brief, this model simulates the activity of a single grid cell, where the grid cell receives three directionally-sensitive, oscillatory inputs offset by 60 degrees, of the grid pattern occurs as a result of interference between these oscillations. Grid

cells also receive input corresponding to the speed of the animal; similar to the attractor network model, altering the gain of this input can alter the scale of the resulting grid pattern. To probe the relationship between grid scale and the slope of the speed signal, we altered this input in a direction-dependent manner. To probe the relationship between grid scale and remapping head direction cells, we altered the directional preference of the three directionally-sensitive inputs.

Statistical Analyses

Sample sizes were chosen based on similar studies recording *in vivo* single units using tetrodes.^{8,12,9,27} All the statistical tests were two-sided, with the exception of the LN model determination of variable coding, which used a one-sided rank test. All comparisons were tested for parametricity using a Lilliefors test. In all cases for which the compared data did not conform to a normal distribution, nonparametric tests were used to assess differences between groups. Wilcoxon sign-rank tests were used for paired data, and Wilcoxon rank-sum tests were used for non-paired data. When comparing differences between distributions, a two-sided Kolmogorov-Smirnov test was used. Directional data was analyzed using the *CircStat* toolbox for MATLAB⁵⁷. To determine whether directional data was uniformly distributed around the orientation space or not, a one-sample Kuiper test was performed. This test is a circular analog to Kolmogorov-Smirnov, but the equal sensitivity at the tails of the distribution as at the median renders it ideal for detecting departures from circular uniformity in both unimodal and bimodal distributions. Watson-Williams tests were used to determine whether directional distributions differed. While this test assumes a von Mises distribution, it has been demonstrated to be robust to departures from this assumption⁵⁸.

Supplementary Material

Refer to Web version on PubMed Central for supplementary material.

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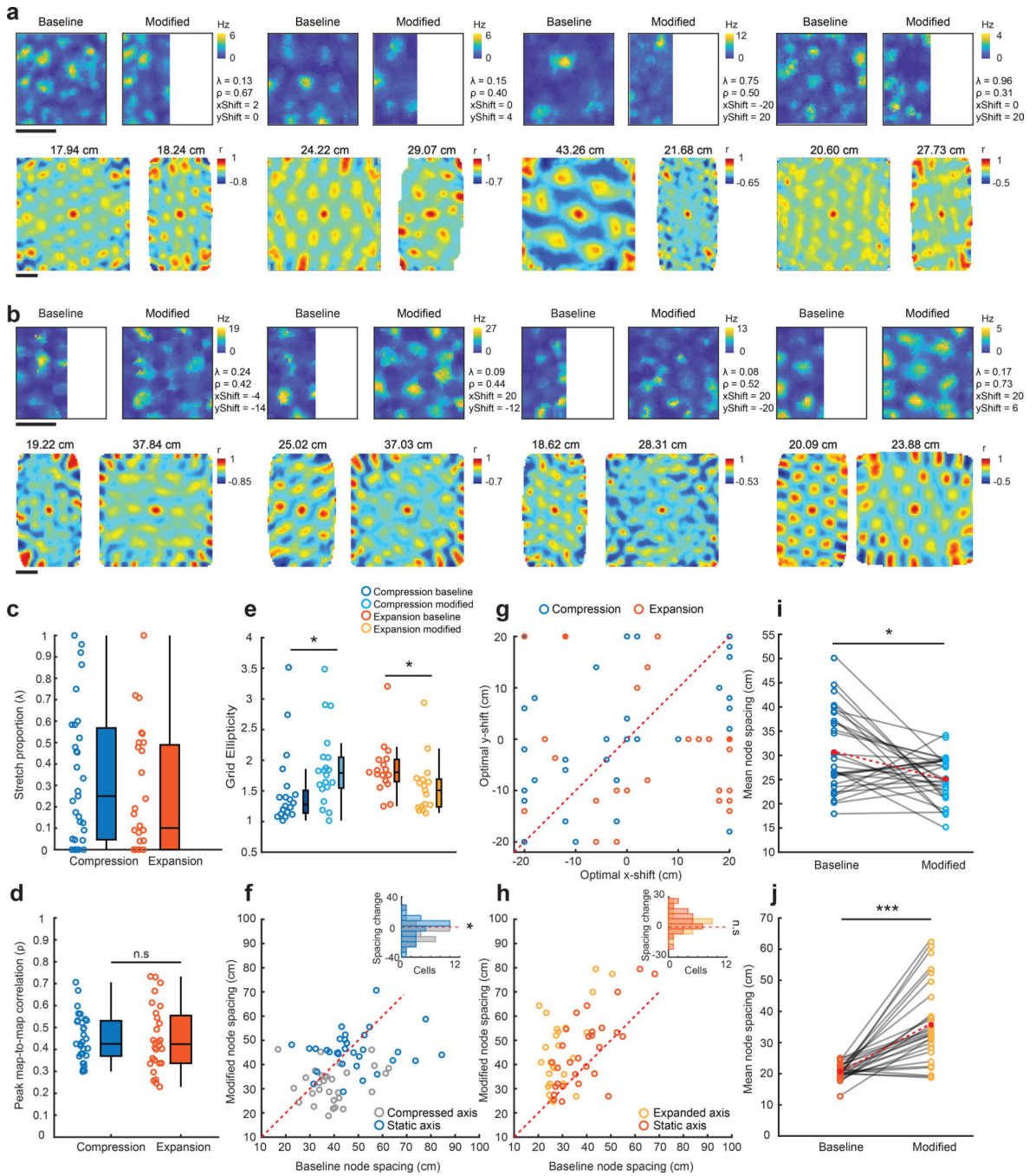


Figure 1. Environmental perturbation distorts grid spacing.

a, Firing rate maps (top row) and spatial autocorrelations (bottom row) of grid cells in the baseline (left panels) and modified (right panels) environment for the compression condition. Maps are color coded for maximum (red) and minimum (blue) values. Scale bar indicates 50 cm. Rescaling factor (λ), magnitude of the peak correlation between baseline and rescaled maps (ρ) and optimal shift in X (xShift) and Y (yShift) at peak correlation are shown to the right of each rate map. Mean node spacing values are reported above the autocorrelation. Scale bars show the range of firing rates (Hz, top rows) and correlation

values (r , bottom rows). **b**, Examples of grid cells labeled as in (a) for the expansion condition. **c**, Rescaling factor (λ) for grid cells in the compression (blue, $n = 31$) and expansion condition (orange, $n = 28$) (mean $\lambda \pm \text{SEM}$; compression = 0.34 ± 0.057 ; expansion = 0.37 ± 0.065). Box illustrates median $\pm 25^{\text{th}}$ and 75^{th} percentiles and whiskers $1.5\times$ the interquartile range. **d**, The magnitude of the peak correlation (ρ) between baseline and rescaled maps is the same between compression (blue, $n = 31$ grid cells) and expansion (orange $n = 28$ grid cells) conditions (Wilcoxon rank-sum test; mean Pearson correlation coefficient between baseline and rescaled map $\pm \text{SEM}$; compression = 0.45 ± 0.02 , expansion = 0.47 ± 0.03 , $Z = 0.77$, $p = 0.44$). Data presented as in (c). **e**, Environmental compression caused an increase in grid ellipticity for those grid cells successfully fit with an ellipse (mean $\pm \text{SEM}$: compression baseline = 1.52 ± 0.14 , modified = 1.85 ± 0.14 , two-sided Wilcoxon sign-rank test; $Z = 2.20$, $n = 20$ grid cells, $p = 0.028$), while environmental expansion resulted in a decrease in grid ellipticity (expansion baseline = 1.86 ± 0.10 , modified = 1.57 ± 0.11 ; two-sided Wilcoxon sign-rank test; $Z = 2.01$, $n = 17$ grid cells, $p = 0.044$). Data presented as in (c) **f**, In the compression condition, grid spacing decreased in the compressed but not the static axis (mean spacing $\pm \text{SEM}$: compressed axis baseline = 38.97 ± 1.90 cm, modified = 32.56 ± 1.40 cm, $n = 31$ grid cells, two-sided Wilcoxon sign-rank test: $Z = 2.78$, $p = 0.005$; static axis baseline = 48.66 ± 2.48 cm, modified = 45.63 ± 1.49 cm, $n = 28$ grid cells, two-sided Wilcoxon sign-rank test: $Z = 0.49$, $p = 0.62$). Unity between conditions is illustrated by a dotted red line. Inset histogram: distribution of spacing changes in each axis (two-sided KS test = 0.36 , $p = 0.03$). **g**, Amount of shift (cm) in the X and Y direction needed to produce the optimal map-to-map correlation between baseline and rescaled maps (mean shift $\pm \text{SEM}$: compression, x-shift = -1.55 ± 2.71 cm, y-shift = 0.90 ± 2.26 cm, $n = 31$ grid cells, two-sided Wilcoxon sign-rank test: $Z = 0.85$, $p = 0.39$; expansion, x-shift = 0.43 ± 1.19 cm, y-shift = -2.29 ± 1.01 cm, $n = 31$ grid cells, two-sided Wilcoxon sign-rank test $Z = 1.48$, $p = 0.14$). Overlapping data points denoted with a small square symbol. **h**, In the expansion condition, grid spacing increased in the compressed and static axis (mean spacing $\pm \text{SEM}$: expanded axis baseline = 29.71 ± 1.44 cm, modified = 33.22 ± 1.92 cm, $n = 28$ grid cells, two-sided Wilcoxon sign-rank test: $Z = 2.25$, $p = 0.024$; static axis baseline = 39.26 ± 2.15 cm, modified = 45.44 ± 2.90 cm, $n = 28$ grid cells, two-sided Wilcoxon sign-rank test: $Z = 2.85$, $p = 0.004$). Inset histogram: distribution of spacing changes in each axis (two-sided KS test = 0.26 , $p = 0.17$). **i,j**, Mean grid spacing of the central six autocorrelation nodes in the baseline and modified compression (i) and expansion (j) condition. The overall mean is shown in red. Spacing decreased in compression (mean spacing (cm) $\pm \text{SEM}$: baseline = 30.66 ± 1.48 , modified = 25.24 ± 0.84 , $n = 31$ grid cells, two-sided Wilcoxon sign-rank test: $Z = 2.45$, $p = 0.014$) and increased in expansion (mean spacing (cm) $\pm \text{SEM}$: baseline = 20.85 ± 0.47 , modified = 35.73 ± 2.40 , $n = 28$ grid cells, two-sided Wilcoxon sign-rank test $Z = 4.42$, $p < 0.001$). All panels: * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$, n.s., not significant ($p > 0.05$).

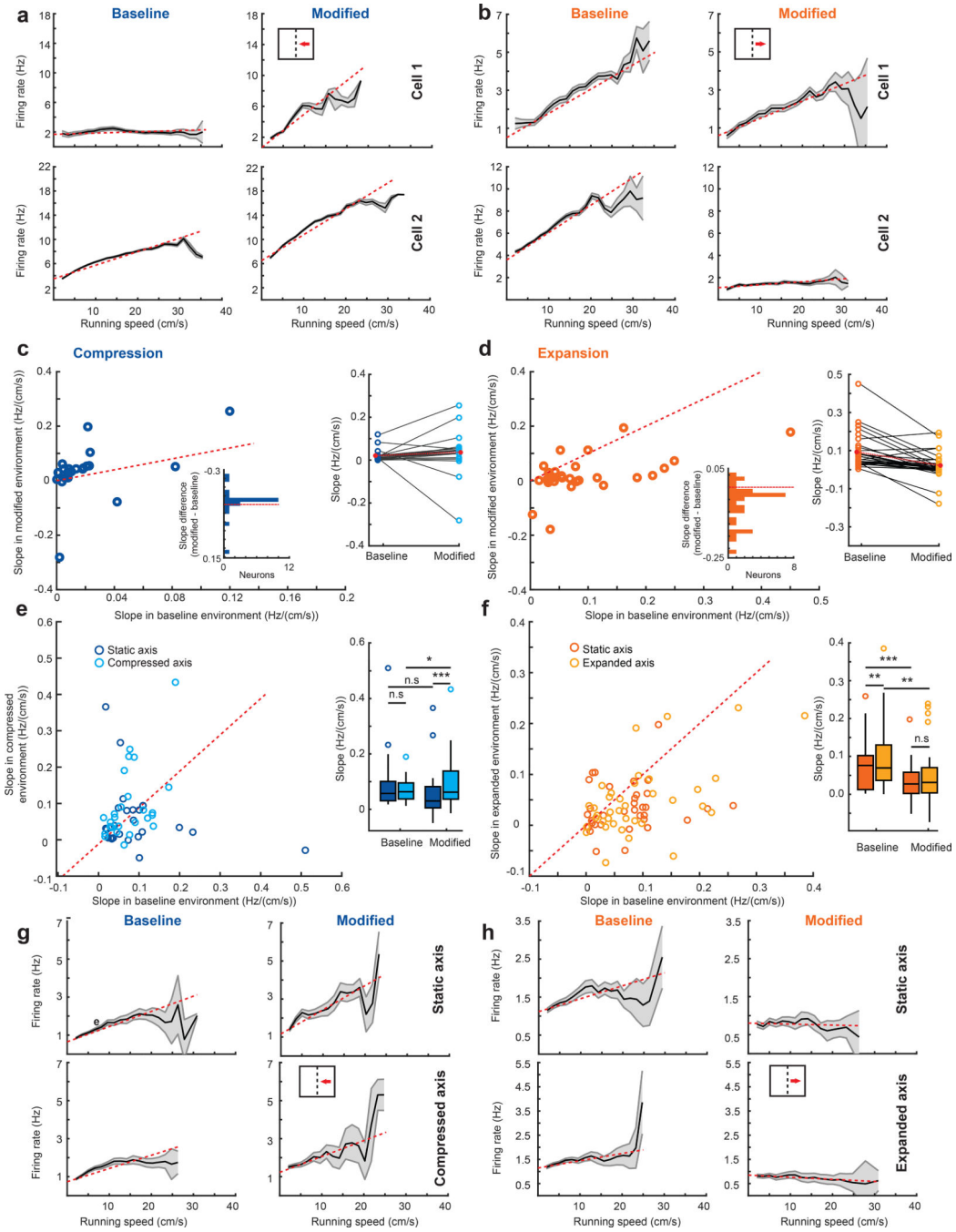


Figure 2. S-encoding cells rescale in response to environmental perturbation.

a, Two example S-encoding cells in the baseline ($n = 2$ independent speed coding cells, left panels) and modified (right panels) environment for the compression condition. Dotted red line indicates the linear function fit through the data. Solid black line indicates the mean response, with gray denoting \pm SEM. **b**, Two example S-encoding cells labeled as in (a) for the expansion condition ($n = 2$ independent speed coding cells). **c**, Scatterplot of the slope (left) of S-encoding cells ($n = 21$ independent speed cells) in the baseline and modified environment for the compression condition. The red dotted line illustrates unity between the

baseline and modified environments. Inset: histogram of the difference in slope (modified – baseline). Red dotted line indicates zero. Right panel shows the change in slope between environments for each cell. The overall mean slope in each environment is shown in red, with a red dotted line illustrating the mean change in slope between environments (slope Hz/(cm/s) \pm SEM: compression baseline = 0.011 ± 0.003 , modified = 0.021 ± 0.007 , $n = 21$ speed coding cells, two-sided Wilcoxon sign-rank test: $Z = 2.14$, $p = 0.033$). **d**, As in (c) for S-encoding cells recorded in the expansion condition (slope Hz/(cm/s) \pm SEM expansion baseline = 0.010 ± 0.002 , modified = 0.003 ± 0.001 , $n = 30$ speed coding cells, two-sided Wilcoxon sign-rank test: $Z = 4.00$, $p = 8.91 \times 10^{-5}$). **e**, Left: Slope of S-encoding cells ($n = 26$ speed cells) in the static and compressed axis in the baseline versus modified environment. Asymmetry between axes is apparent in the modified but not baseline environment. Right: Boxplot illustrates median \pm 25th and 75th percentiles and whiskers 1.5x the interquartile range. Single points beyond this range are plotted individually two-sided Wilcoxon sign-rank tests: Baseline static axis – Modified static axis; $Z = 1.917$, $p = 0.0552$; Baseline modified axis – Modified modified axis; $Z = 2.425$, $p = 0.0153$, Baseline environment between axes; $Z = 0.241$, $p = 0.809$, Modified environment between axes; $Z = 3.695$, $p = 2.195 \times 10^{-4}$. **f**, As in (e) for speed cells recorded in the expansion condition ($n = 36$ speed cells; individually two-sided Wilcoxon sign-rank tests: Baseline static axis – Modified static axis; $Z = 2.624$, $p = 0.0087$; Baseline modified axis – Modified modified axis; $Z = 3.551$, $p = 3.84 \times 10^{-4}$, Baseline environment between axes; $Z = 2.639$, $p = 0.0083$, Modified environment between axes; $Z = 1.241$, $p = 0.2146$). All panels: * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$, n.s., not significant ($p > 0.05$). **g,h**, Axis-specific firing rate by running speed responses for two example S-encoding cells ($n = 2$ independent speed cells), one in the compression (g) and one in the expansion (h) condition (static axis, top row; modified axis, bottom row). Labeled as in (a).

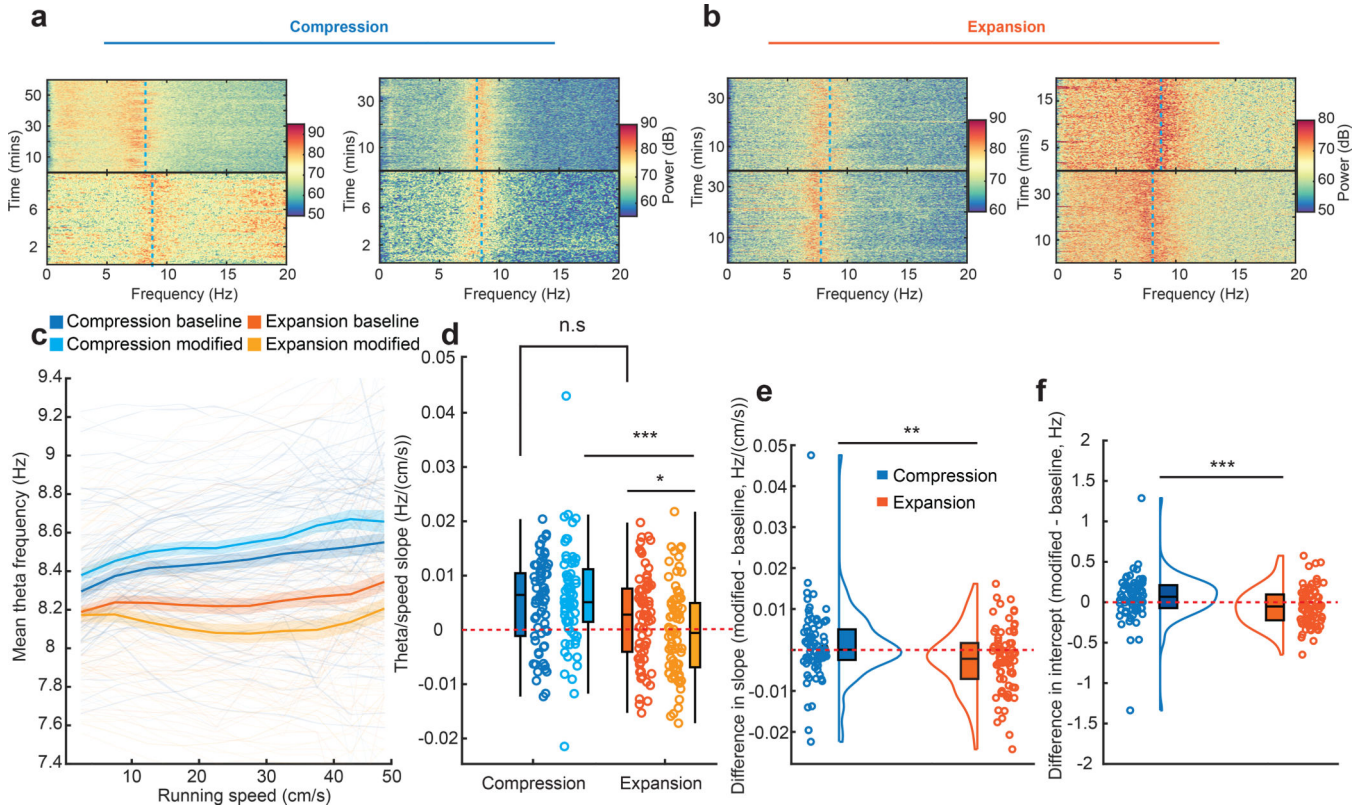


Figure 3. The gain of theta increases in compression and decreases in expansion conditions. **a**, Two example spectrograms showing LFP power in the 0–20 Hz frequency band for a recording session in the baseline (top panels) and modified (bottom panels) environments in the compression condition. A dotted blue line shows the mean theta frequency for that session. **b**, As in (a), but for two sessions (baseline, top and modified, bottom) in the expansion condition. **c**, Mean theta frequency by running speed for compression (n = 75 independent sessions) and expansion (n = 74 independent sessions) conditions. Solid lines show the mean, shaded region is \pm SEM. Individual sessions are shown as faint lines. **d**, The slope of linear fits through the frequency/speed relationship (compression, blues, n = 75 independent sessions; expansion, oranges, n = 74 independent sessions). Boxplots illustrate the medians \pm 25th and 75th percentiles and whiskers 1.5x the interquartile range. There was no difference in slope between compression and expansion baseline sessions (two sided Wilcoxon rank-sum test, Z = 1.528, p = 0.1265), but the slope was greater in the modified environment in compression compared to the modified environment in expansion (two sided Wilcoxon rank-sum test, Z = 3.738, p = 1.856⁻⁴). In the expansion, theta slope was smaller in the modified compared to baseline environments (two sided Wilcoxon sign-rank test, Z = 2.481, p = 0.0131). **e**, The difference in the slope of linear regressions through the running speed/theta frequency relationship between the baseline and modified environments for the compression (blue, n = 75 independent sessions) and expansion (orange, n = 74 independent sessions) groups. Half violin plots show the distribution of values, while inset boxes illustrate the median, upper quartile and lower quartile boundaries. Slope increased between environments in compression, and decreased in expansion (slope difference, modified – baseline (Hz/(cm/s)) \pm SEM: compression = 0.0011 \pm 0.001, expansion = -0.0023 \pm 9.14⁻⁴,

two-sided Wilcoxon rank-sum test, $Z = 2.59$, $p = 0.0096$). **f**, As in e, but for the difference in intercept of linear regressions through the running speed/frequency data between baseline and modified environments. As with slope, the intercept increased in compression (intercept difference, modified – baseline, (Hz) \pm SEM: compression = 0.063 ± 0.033 , expansion = -0.052 ± 0.028 , two-sided Wilcoxon rank-sum test, $Z = 3.362$, $p = 7.740^{-4}$). All panels: * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$, n.s., not significant ($p > 0.05$).

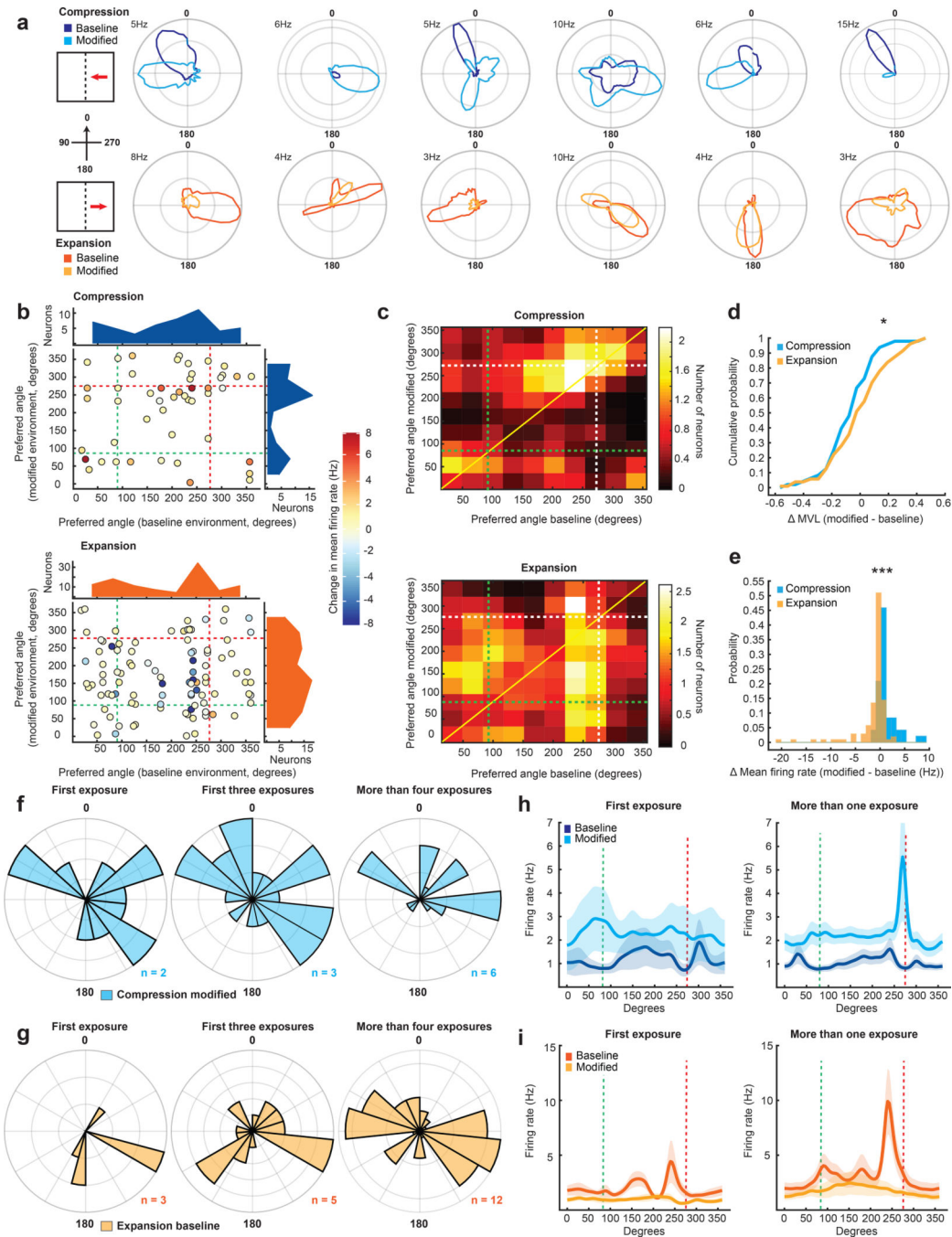


Figure 4. A directionally specific asymmetric bias develops after multiple exposures to modified environments.

a, Polar plots of H-encoding cells in the compression ($n = 6$ directional cells, top row) and expansion ($n = 6$ directional cells, bottom row) condition. Top left numbers show the firing rate indicated by the outermost ring. **b**, Scatterplot of preferred phase angle (degrees) of H-encoding cells between baseline and modified environments in compression (top) and expansion (bottom) conditions. The change in firing rate between baseline and modified environments is indicated by colors coded for minimum (blue) and maximum (red) values.

Marginal density plots (blue, compression, top; orange, expansion, bottom) indicate the distribution of phase angles. The wall axes are indicated by dotted lines (green, static wall; red, moved wall). **c**, The number of neurons falling in each 33° directional bin in the baseline and modified environments in the compression (top) and expansion (bottom) condition. A 2-bin Gaussian filter is applied to the data. The wall axes are indicated by dotted lines (green, static wall; white, moved wall). A solid yellow line demarks the bins in which there was no change in direction. **d**, The cumulative probability of change in mean vector length (MVL) between environments for the compression (blue, H-encoding cell $n = 49$) and expansion (orange, H-encoding cell $n = 103$) condition (mean change in MVL \pm SEM: compression = -0.06 ± 0.025 , expansion = 0.013 ± 0.021 , two-sided Wilcoxon rank sum test: $Z = 2.21$, $p = 0.027$) **e**, The probability distribution of the change in mean firing rate between environments for the compression (blue, H-encoding cell $n = 49$) and expansion (orange, H-encoding cell $n = 103$) condition (Firing rate change (Hz) \pm SEM: compression = 1.22 ± 0.29 , expansion = -1.41 ± 0.35 , two-sided Wilcoxon rank-sum test, $Z = 7.07$, $p = 1.52 \times 10^{-12}$). **f,g**, A bidirectional bias develops in H-encoding cells after multiple exposures to the modified environments. Polar histograms show the number of cells with a given preferred phase angle, with scale (n) indicated by the number on the top left. In the compression experiments (blue bars, (f)) no phase angle bias is evident on the first exposure to the compressed environment (left panel, $n = 12$) or over the first three exposures ($n = 24$). Cells recorded on sessions after the fourth exposure ($n = 25$; right panel) cluster bimodally. (g) shows the same as (f) but for cells recorded in the expansion condition (expansion left panel $n = 7$, middle $n = 23$ right $n = 80$). **h,i**, The directionally specific unimodal bias in firing rate develops with experience. H and I show the mean firing rate for all H-encoding cells in the compression (h) and expansion (i) conditions on the first exposure (left panels) and subsequent exposures (right panels). Solid lines are mean firing rates, \pm SEM is shown as a shaded region. The wall axes are indicated by dotted lines (green, static wall; red, moved wall). All panels: * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$, n.s., not significant ($p > 0.05$).

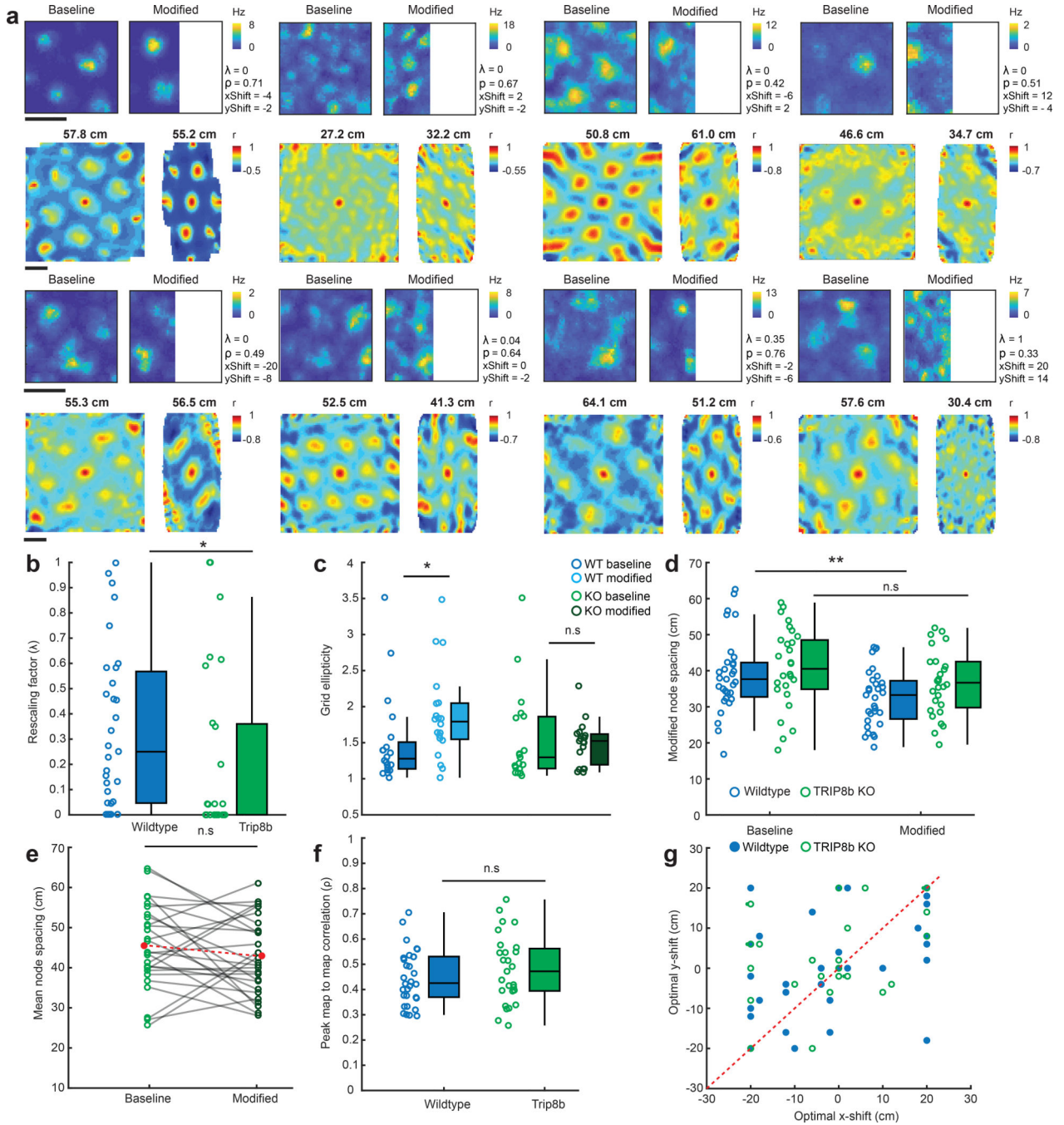


Figure 5. TRIP8b KO grid spacing is less sensitive to environmental perturbation.

a, Firing rate maps (top rows) and spatial autocorrelations (bottom rows) of KO grid cells in the baseline (left panels) and modified (right panels) environment for the compression condition. Maps are color coded for maximum (red) and minimum (blue) values. Scale bar indicates 50 cm. The rescaling factor (λ), magnitude of the peak correlation between baseline and rescaled maps (ρ) and optimal shift in X (xShift) and Y (yShift) at peak correlation are shown to the right of each rate map. Mean node spacing \ values are reported above the autocorrelation. Scale bars show the range of firing rates (Hz, top rows) and

correlation values (r , bottom rows). **b.** Rescaling factor (λ) at optimum correlation. WT grid cells (blue, $n = 31$ grid cells) required more stretching than KO grid cells (green, $n = 27$) (mean $\lambda \pm \text{SEM}$: WT = 0.34 ± 0.06 , KO = 0.21 ± 0.06 , two-sided Wilcoxon rank sum test; $Z = 2.15$, $p = 0.031$). Box illustrates median $\pm 25^{\text{th}}$ and 75^{th} percentiles and whiskers 1.5x the interquartile range. **c.** WT grid cells ($n = 31$ grid cells) became significantly more elliptical compared to KO grid cells ($n = 27$ grid cells) in the modified environment (two-sided Wilcoxon rank sum test; $Z = 2.50$, $p = 0.013$). There was no difference in the ellipticity of KO grid cells between environments (mean $\pm \text{SEM}$: KO baseline = 1.54 ± 0.15 , modified = 1.43 ± 0.07 , two-sided Wilcoxon sign rank test; $Z = 0.40$, $n = 19$, $p = 0.6687$, n.s.). Data are presented as in (b). **d.** In the compression condition, grid spacing in the compressed axis decreased in WT ($n = 31$ grid cells) but not in KO ($n = 27$ grid cells, WT baseline = $39.0 \pm 1.90\text{cm}$, WT modified = $32.56 \pm 1.40\text{cm}$, $Z = 2.78$, $p = 0.005$; KO baseline = $40.67 \pm 2.13\text{cm}$, KO modified = $36.80 \pm 1.78\text{cm}$, two-sided Wilcoxon rank sum test; $Z = 1.66$, $p = 0.10$ n.s.). Data are presented as in (b). **e.** Mean grid spacing for cells in the baseline and modified environments for the compression condition. The overall mean is shown in red. There is no difference in spacing between environments (KO baseline = 45.50 ± 2.01 cm, KO modified = 42.97 ± 1.84 cm, $Z = 1.20$, $p = 0.23$). **f.** There was no difference in the peak map-to-map correlations between WT ($n = 31$ grid cells) and KO ($n = 27$ grid cells, mean $\pm \text{SEM}$: WT = 0.45 ± 0.02 , KO = 0.50 ± 0.03 , two-sided Wilcoxon rank sum test; $Z = 0.89$, $p = 0.37$, n.s.). Data are presented as in (b). **g.** There was no difference between WT ($n = 31$ grid cells) and KO ($n = 27$ grid cells) in the amount of shift in the X or Y direction needed to produce the optimal map-to-map correlation between baseline and rescaled maps (mean $\pm \text{SEM}$: x-shift, WT = -1.55 ± 2.71 cm, KO = -2.67 ± 2.67 cm, two-sided Wilcoxon rank sum test; $Z = 0.14$, $p = 0.89$, n.s.; y-shift, WT = 0.90 ± 2.26 cm, KO = 3.33 ± 2.16 cm, two-sided Wilcoxon rank sum test; $Z = 0.69$, $p = 0.49$, n.s.). Overlapping points denoted with a smaller circular symbol. All panels: * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$, n.s., not significant ($p > 0.05$).

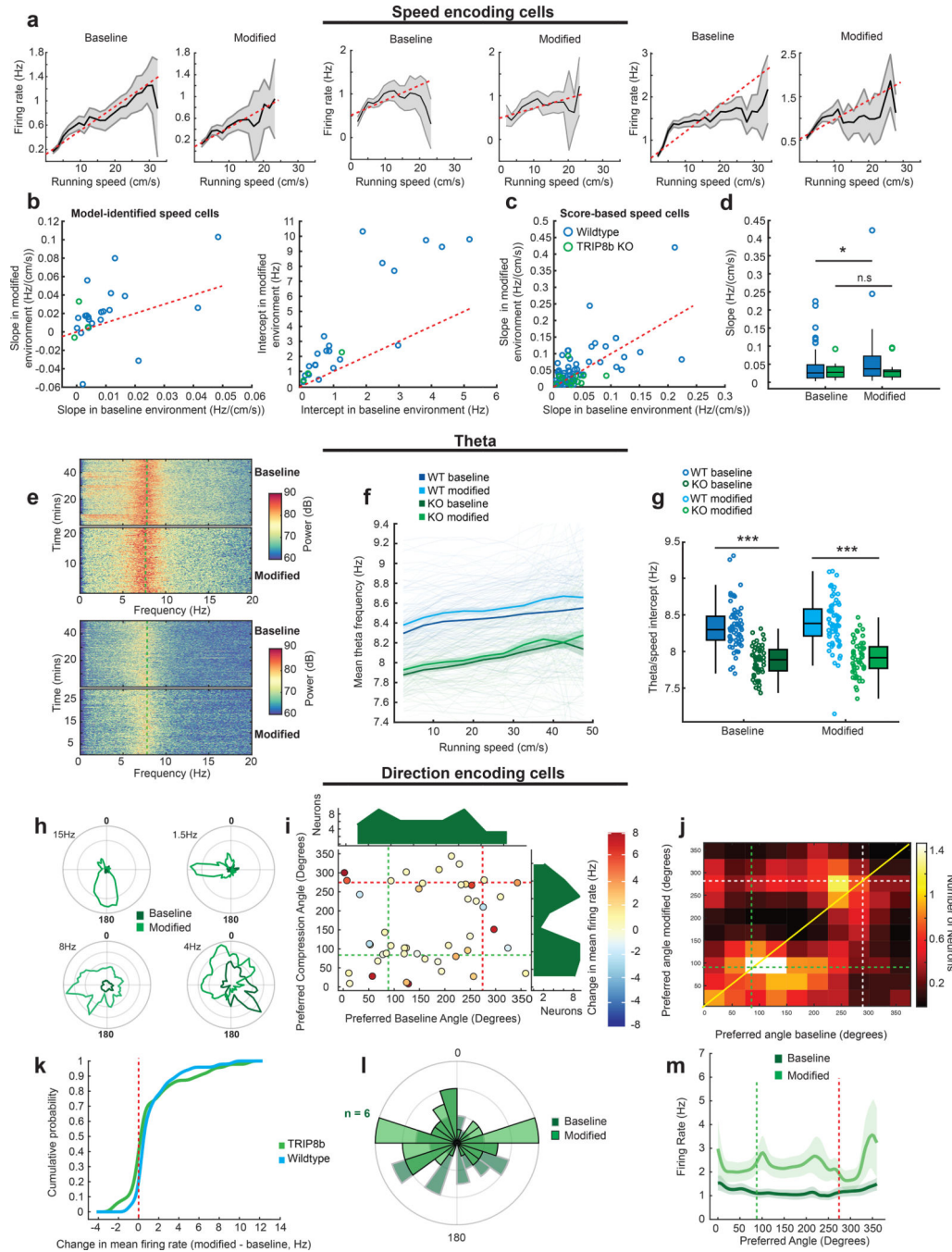


Figure 6. TRIP8b KO speed signals are less sensitive to environmental perturbation while directional signals remain malleable.

a, Three example S-encoding cells in the baseline (left panels) and modified (right panels) environment for the compression condition (n = 3 speed cells). Dotted red line indicates the linear function fit through the data. Solid black line indicates the mean response, with gray denoting \pm SEM. **b**, Scatterplot of the slope (left) and intercept (right) of KO S-encoding cells (n = 3) in the baseline and modified environment for the compression condition. S-encoding cells from the WT compression experiments shown in blue for comparison. **c**,

Scatterplot of the of KO and WT speed cells defined using traditional speed scores. There was no significant difference in the slope of score-identified KO speed cells between baseline and modified environments. **d**, Boxplots of the slope of KO (green, $n = 12$ speed cells) and WT (blue, $n = 58$ speed cells) score-identified speed cells in the baseline and modified (compressed) environment. Box illustrates median $\pm 25^{\text{th}}$ and 75^{th} percentiles and whiskers $1.5\times$ the interquartile range. Slopes beyond this range are illustrated as individual points. There was no difference in the slope of KO speed cells between environments (mean slope (Hz/(cm/s)) \pm SEM: baseline = 0.034 ± 0.007 , modified = 0.027 ± 0.007 , two-sided Wilcoxon sign rank test; $p = 0.73$, n.s.) WT speed cells increased slope between baseline and modified environments (mean slope (Hz/(cm/s)) \pm SEM: baseline = 0.042 ± 0.006 , modified = 0.057 ± 0.009 , two-sided Wilcoxon sign rank test; $Z = 2.31$, $p = 0.02$). **e**, Example spectrograms showing LFP power in the 0–20Hz range in two sessions recorded from TRIP8b KO animals in the baseline (top panels) and modified (bottom panels) environments. The mean theta frequency over each session is shown as a superimposed dotted green line. **f**, Mean theta frequency by running speed for KO (greens, $n = 53$ independent sessions) and WT (blues, $n = 67$ independent sessions) animals in the baseline and modified (compressed) environments. Solid lines show the mean, shaded region is \pm SEM. Individual sessions are shown as faint lines. **g**, The intercept of linear regressions of the running speed/theta frequency relationships for sessions recorded from WT animals (blues, $n = 67$ independent sessions) and KO animals (greens, $n = 53$ independent sessions) in the baseline and modified (compressed) environments. There was no difference in the intercept between baseline and modified environments in KO animals (KO intercept \pm SEM (Hz): baseline = 7.87 ± 0.03 , modified = 7.91 ± 0.03 , two-sided Wilcoxon sign rank test $Z = 1.72$, $p = 0.086$). WT theta intercept was greater than KO theta intercept in both baseline (two-sided Wilcoxon rank sum test; $Z = 7.79$, $p = 6.717^{-15}$) and modified (two sided Wilcoxon rank sum test; $Z = 7.34$, $p = 2.063^{-13}$) environments. Data are presented as jittered scatterplots and summarized as boxplots. Box illustrates median $\pm 25^{\text{th}}$ and 75^{th} percentiles and whiskers $1.5\times$ the interquartile range. **h**, Polar plots of KO H-encoding cells in the compression condition. Top left numbers show the firing rate indicated by the outermost ring. **i**, Scatterplot of preferred phase angle (degrees) of KO H-encoding cells between baseline and modified environments in the compression condition. The change in firing rate is indicated by colors coded for minimum (blue) and maximum (red) values. Marginal density plots (green) indicate the distribution of phase angles. The wall axes are indicated by dotted lines (green, static wall; red, moved wall). **j**, Number of KO neurons falling in each 33° directional bin in the baseline and modified environments in the compression condition. A 2-bin Gaussian filter is applied to the data. The wall axes are indicated by dotted lines (green, static wall; white, moved wall). A solid yellow line demarks the bins in which there was no change in direction. **k**, Cumulative probability of the change in mean firing rate between baseline and modified environments for direction encoding cells from the WT compression (blue) and TRIP8b KO (green) group. The vertical dotted line illustrates the point at which firing rates change from decreasing to increasing between environments. As in the WT group, direction encoding cells in the TRIP8b KO ($n = 47$ cells) group generally increased in mean firing rate in the modified environment compared to baseline. **l**, Polar histograms show the number of cells with a given preferred phase angle in baseline (dark green) and modified (light green) environments, with scale (n) indicated by the number on

the top left. **m**, Mean firing rates for all H-encoding cells in the compression condition over all exposures ($n = 47$). Solid lines are mean firing rates, \pm SEM is shown as a shaded region. The wall axes are indicated by dotted lines (green, static wall; red, moved wall). All panels: * $p < 0.05$, ** $p < 0.01$, *** $p < 0.001$, n.s., not significant.