Monte Carlo-based Investigation of Absorbed-dose Energy Dependence of Thermoluminescent Dosimeters in Therapeutic Proton and Carbon Ion Beams

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Abstract

Background: The present study is aimed at calculating relative absorbed-dose energy response correction (*R*) of commonly used thermoluminescent dosimeters (TLDs) such as LiF, $Li_2B_4O_7$, and Al_2O_3 as a function of depth in water for protons (50–250 MeV/n) and carbon ion (80–480 MeV/n) beams using Monte Carlo-based FLUKA code. **Materials and Methods:** On-axis depth-dose profiles in water are calculated for protons (50–250 MeV/n) and carbon ion (80–480 MeV/n) beams using FLUKA code. For the calculation of *R*, selective depths are chosen based on the depth-dose profiles. In the simulations, the TLDs of dimensions 1 mm × 1 mm × 1 mm are positioned at the flat, dose gradient, and Bragg peak regions of the depth-dose profile. Absorbed dose to detector was calculated within the TLD material. In the second step, TLD voxels were replaced by water voxel of similar dimension and absorbed dose to water was scored. **Results:** The study reveals that for both proton and carbon ion beams, the value of *R* differs from unity significantly at the Bragg peak position and is close to unity at the flat region for the investigated TLDs. The calculated *R* value is sensitive to depth in water, beam energy, type of ion beam, and type of TLD. **Discussion:** For accurate dosimetry of protons and carbon ion beams using TLDs, the response of the TLD should be corrected to account for its absorbed-dose energy dependence.

Keywords: Carbon ions, Monte Carlo, protons, thermoluminescent dosimeter response

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INTRODUCTION

Radiotherapy utilizing proton and carbon ion beams offers improved dose confirmation as compared to photons and electrons due to their capability to deliver high doses precisely at a well-defined depth (Bragg peak) and rapid dose falloff beyond the peak.^[1,2] Various detectors, such as ionization chambers, silicon detectors, scintillation detectors, and thermoluminescent dosimeters (TLDs), are employed for dosimetry in this context.^[3-15] Ionization chambers are often considered the most precise dosimeters and are commonly used for routine dosimetry. TLDs such as LiF, Li₂B₄O₇, and Al₂O₃ are employed for dose mapping and absolute dose measurements in radiation therapy, including proton and carbon ion beams.^[8,16,17] The availability of TLDs in smaller dimensions and in various forms, such as powder, small extruded chips or ribbons, and thin Teflon-impregnated discs, makes the handling of these

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detectors relatively more convenient. In certain scenarios, TLDs are preferred over ionization chambers as they minimally perturb the radiation field. However, it is essential to note that the nonlinear dose-response curve of TLDs represents a limitation in proton and heavy-ion beam dosimetry.^[5] This results in a dependence of the detector's response on the radiation beam quality and the particle's linear energy transfer (LET). Hence, special care is required when using TLDs in proton and heavy-ion beams to achieve a precision of ±3%.^[18,19]

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Several studies have been conducted to examine the responses of various detectors in proton and heavy ion beams,[3-15] employing various approaches, including track structure theory, analytical algorithms, measurements, and Monte Carlo methods. McMahan^[10] conducted measurements to assess the response of different scintillator detectors to ions with atomic numbers ranging from 1 to 84 and energies in the range of 5-30 MeV/n. Pereyra et al.[11] investigated the response of nuclear track detectors to energetic heavy ions, such as ⁴He (150 MeV/n), ¹²C (390 MeV/n), and ⁵⁶Fe (465 MeV/n), particularly in the relatively low-dose range of less than or equal to 1 mGy. Yasuda^[14,15] conducted a study on the response of a direct ion storage dosimeter (DIS-1) when exposed to ⁴He, ¹²C, ⁴⁰Ar, and ⁵⁶Fe ion beams. Boscolo et al.^[5] presented an analytical algorithm designed to calculate the relative thermoluminescence efficiency (TL-efficiency) with respect to ion charge (Z) and energy (E). Massillon-Jl et al.^[9] irradiated LiF: Mg, Ti with ¹H (1, 3, 25, and 40 MeV),⁴He (25 and 40 MeV/n), ¹²C (15, 25, and 40 MeV/n), ¹⁶O (25 MeV/n), and ²⁰Ne (40 MeV/n) to investigate the response of the TLD as a function of LET. The majority of the mentioned studies are based on measurements^[3-15] and limited studies involved TLDs.[5,9]

Monte Carlo-based studies on the determination of energy dependence of TLDs such as LiF, Li₂B₄O₂, and Al₂O₂ TLDs in proton and carbon ion beams are not available in the literature. The energy dependence of a detector, such as TLDs in this case, is a product of its intrinsic energy dependence and the absorbed-dose energy dependence.^[20-22] The intrinsic energy dependence relates the TLD light output to the dose received by the TLD for a given beam quality, and it cannot be calculated using Monte Carlo methods but can be determined through measurement. On the other hand, the absorbed-dose energy dependence of a detector relates the TLD response to the dose in the medium and can be calculated using Monte Carlo simulations. The present study is focused on determining the relative absorbed-dose energy response correction for commonly used TL detectors, namely LiF, Li₂B₄O₇, and Al₂O₃. This correction factor is calculated as a function of depth in a water phantom for nonmodulated proton (50-250 MeV/n) and carbon ion (80-480 MeV/n) beams. The investigation employs the Monte Carlo-based FLUKA code^[23,24] for these calculations.

MATERIALS AND METHODS

Ion beams and detectors

The present study considered (a) proton beams of energy ranging from 50 to 250 MeV/n (with an increment of 50 MeV/n), which correspond to the projected range of 2.2–37 g/cm² in water medium, and (b) carbon ion beams with energy ranging from 80 to 480 MeV/n (with varying intervals), which correspond to the projected range of 1.8–37 g/cm², in water medium. LiF, Li₂B₄O₇, and Al₂O₃ TLDs having dimension of 1 mm × 1 mm × 1 mm are considered in this study. Note that 1 mm x 1 mm x 1mm TLD cubes are

commercially available. Elemental composition, mass fraction, effective atomic number (Z_{eff}) , electron density ($\langle Z/A \rangle$), and mass density (ρ) of these detectors are presented in Table 1.

Energy dependence of the detector

Absorbed-dose energy dependence, f(Q), of a detector for a given beam quality Q is the ratio of the dose to the medium (water in the present study) at the point of measurement in the absence of the detector, D_{wat} , to the dose to the detector, D_{dar} .^[20-22] It can be written as:

$$f(Q) = \left[\frac{D_{wat}}{D_{det}}\right]_{Q} \tag{1}$$

The detectors are generally calibrated against a reference beam, which is ⁶⁰Co in the present study. Thus, for a given TLD and beam quality Q, relative absorbed-dose energy response correction factor $R^{[20-22]}$ can be written as:

$$R = \frac{\frac{1}{f(Q)}}{\frac{1}{f(Q_0)}} = \frac{\left\lfloor \frac{D_{det}}{D_{wat}} \right\rfloor_Q}{\left\lfloor \frac{D_{det}}{D_{wat}} \right\rfloor_{Q_0}}$$
(2)

where Q_0 is ⁶⁰Co beam in the present study. The beam quality, Q, denotes the proton and carbon ion beams of different energy.

FLUKA Monte Carlo code

Monte Carlo-based FLUKA code^[23,24] (version 4.0, 2020) combined with FLAIR^[25] (version 3.0.10) is used in the present study. Note that FLAIR is advanced graphical user interface for FLUKA. FLUKA is a general-purpose Monte Carlo code capable of transporting about 60 different particles in matter.[26] FLUKA is well benchmarked for the dosimetry of proton and carbon ions in the therapeutic energy range.^[27,28] It has the capability to handle complex geometries using an improved version of the combinatorial geometry package. FLUKA treats elastic scattering through parameterized nucleon-nucleon cross sections and tabulated nucleon-nucleus cross sections. Inelastic cross sections for hadron-hadron interactions are represented by parameterized fits of the available experimental data. For hadron-nucleus interactions, a mixture of tabulated data and parameterized fits are used. The PEANUT package includes a very detailed generalized intranuclear cascade and a preequilibrium stage. This module is followed by equilibrium processes, evaporation, fission, Fermi breakup, and gamma de-excitation. Light residual nuclei are not evaporated but fragmented into a maximum of 6 bodies, according to a Fermi breakup model. Nuclear interactions generated by ions are treated through interfaces to external event generators. For example, modified Relativistic Quantum Molecular Dynamics (RQMD) is used between 0.1 and 5 GeV per nucleon. In the present study, RQMD-2.4 is linked by *ldpmqmd* script.

Monte Carlo calculations

The Monte Carlo simulations are carried out in two steps.

Step 1

A parallel ion beam of given kinetic energy (proton or carbon) having a field size of 5 cm \times 5 cm is incident on the front surface of a cubical water phantom of dimensions 50 cm \times 50 cm \times 50 cm. The absorbed dose is calculated as a function of depth along the central axis in the water phantom using USRBIN scoring card. The voxel size used for scoring the absorbed dose is 2 mm \times 2 mm \times 0.25 mm. From the depth-dose profile, position of the Bragg peak for a given energy of ion beam (proton or carbon) is obtained. Percentage depth-dose (PDD) profile is calculated by normalizing the absorbed-dose value at each voxel with respect to the dose value at the Bragg peak position.

Step 2

Simulations are carried out to obtain detector-specific absorbed-dose energy response correction factor (R) at different depths along the central axis of the beam. The on-axis depths considered for proton beams above 50 MeV/n and carbon beams above 80 MeV/n are d₁ (Bragg peak position), d_2 (dose gradient region), and d_3 and d_4 (flat region), as shown in Figure 1. Because of smaller range of 50 MeV/n proton and 80 MeV/n carbon beams, depths considered are d_1 (Bragg peak position) and d_4 (flat region). The considered values of d_1 , d_2 , d_3 , and d_4 for 50–250 MeV/n proton beams are shown in Table 2 and those for 80-480 MeV/n carbon ion beams are shown in Table 3. In the Monte Carlo simulations, cubical TL detectors (LiF or Li₂B₄O₂ or Al₂O₂) of dimensions $1 \text{ mm} \times 1 \text{ mm} \times 1 \text{ mm}$ are positioned at the above-described depths in the water phantom. Absorbed dose to detector (D_{def}) is scored on a region basis using USRBIN scoring card. Similar simulation is carried out to obtain absorbed dose to water (D_{wat}) by replacing the detector material as water. Note that for a given beam, placing of TLDs at all the depths in a single simulation will alter the water-equivalent depth of calculation which will affect the calculated value of R. Hence, in the present



Figure 1: Schematic depiction of the positions of thermoluminescent dosimeters (d_1, d_4) on the depth-dose profile. d_1 represents Bragg peak, d_2 represents dose gradient region, and d_3, d_4 represent flat region of the depth-dose profile

study, for a given beam, separate simulation was carried out for each investigated depth in water. Detector-to-water dose ratio for a given beam quality Q (numerator of equation 2) was calculated by taking the ratio of D_{det} and D_{wat} . The value of

$$\frac{1}{f(Q_0)} = \left\lfloor \frac{D_{det}}{D_{med}} \right\rfloor_{Q_0}$$
(denominator of equation 2) is taken from

a previously published study^[29] for LiF, Li₂B₄O₇, and Al₂O₃ detectors. It was demonstrated by Selvam and Keshavkumar^[30] that the detector-to-water dose ratio calculated for ⁶⁰Co beam in water phantom is independent of detector thickness ranging from 0.1 to 5 mm.

In the Monte Carlo calculations, PRECISIOn default card was used where both particle transport threshold and delta-ray production threshold were set at 100 keV. EVAPORAT and COALESCE PHYSICS cards were activated. Total 10⁸ primary particles were simulated to achieve 1 σ level statistical uncertainty in absorbed dose below 1%. As per the recommendations of AAPM Task Group 268,^[31] Table 4 summarizes all the Monte Carlo parameters used in this study.

Results and Discussion

Analysis of percentage depth dose

PDDs for the investigated energies of proton and carbon ion beams for field size of 5 cm \times 5 cm are presented in Figures 2 and 3, respectively. The positions of the Bragg peaks in the water phantom for proton beams of energies 50, 100, 150, 200, and 250 MeV/n are at 2.1, 7.6, 15.6, 25.6, and 37.6 cm, respectively. Similarly, for carbon ion beams of energies 80, 130, 200, 300, 400, and 480 MeV/n, Bragg peaks occur at depths of 1.6, 4.1, 8.6, 17.1, 27.3, and 36.3 cm, respectively. The positions of the Bragg peaks are consistent with the calculated projected range of the proton and carbon ion beams in water using SRIM code.^[32] In the depth-dose profiles of protons and carbon ions, as shown in Figures 2 and 3: (a)



Figure 2: FLUKA-calculated percentage depth-dose profiles of the investigated energies of proton beams in water for a field size of 5 cm \times 5 cm

density (p)	lensity (ρ) of Lif, Li ₂ B ₄ U ₇ , and Ai ₂ U ₃ detectors											
Detector	Н	Li	В	0	F	AI	Z _{eff}	<z a=""> (mol/g)</z>	ρ (g/cm³)			
LiF	-	0.268	-	-	0.732	-	8.27	0.462	2.635			
$Li_2B_4O_7$	-	0.082	0.257	0.661	-	-	7.4	0.485	2.44			
Al ₂ O ₃	-	-	-	0.471	-	0.529	10.2	0.491	3.97			
H ₂ O	0.112	-	-	0.888	-	-	7.4	0.555	1			

Table 1: Elemental composition, mass fraction, effective atomic number (Z_{eff}), electron density (<Z/A>), and mass density (ρ) of LiF, Li₂B₄O₇, and Al₂O₃ detectors

Table 2: On-axis depths in water considered for the calculation of R of LiF, Li_2B_407 , and Al_2O_3 detectors for monoenergetic proton beams

E (MeV/n)	d ₁ (cm)	d ₂ (cm)	d ₃ (cm)	d_4 (cm)
50	2.125	-	-	1.125
100	7.625	6.625	5.0	3.0
150	15.625	14.625	10.0	5.0
200	25.625	24.625	20	10
250	37.625	36.625	20	10

Table 3: On-axis depths in water considered for the calculation of R of LiF, $\text{Li}_2\text{B}_4\text{O}_7$, and Al_2O_3 detectors for monoenergetic carbon ion beams

E (MeV/n)	d ₁ (cm)	d ₂ (cm)	d ₃ (cm)	d_4 (cm)
80	1.625	-	-	0.625
130	4.125	3.625	2.625	0.625
200	8.625	8.375	4.625	0.625
300	17.125	16.625	8.875	0.625
400	27.375	26.875	13.875	0.625
480	36.375	35.875	18.125	0.625

rapid dose falloff is observed beyond the Bragg peak region for protons and (b) in the case of carbon ions, a tail is observed beyond the Bragg peak region of the depth-dose profile and the magnitude of this tail part increases with increase in carbon ion beam energy. As an example, for 80 MeV/n, 200 MeV/n, and 480 MeV/n carbon ion beams, beyond few mm of the Bragg peak positions, doses fall down to about 1%, 5%, and 17% of the peak dose, respectively. This is because primary carbon ions undergo nuclear interactions and fragment into lower atomic number particles such as protons and alpha producing a fragmentation tail beyond the Bragg peak.^[33-35]

Relative absorbed-dose energy response correction

The Monte Carlo-calculated values of *R* for LiF, Li₂B₄O₇, and Al₂O₃ detectors are presented in Tables 5 and 6 for depths d₁-d₄ in water phantom for proton and carbon beams, respectively. For a given detector, *R* values are independent of energy of the proton beams at the depths, d₂-d₄, in the water phantom. At these depths (d₂-d₄), *R* values are close to unity for LiF and Li₂B₄O₇ detectors. However, for Al₂O₃ detector at depths (d₂-d₄), *R* values are about 6%–9% lesser than unity depending on the beam energy and detector position. At the Bragg peak (d₁), *R* is sensitive to the energy of proton beam and the type of detector. For example, depending on kinetic energy



Figure 3: FLUKA-calculated percentage depth-dose profiles of the investigated energies of carbon ion beams in water for a field size of $5 \text{ cm} \times 5 \text{ cm}$

of proton beams, the value of *R* at the Bragg peak positions ranges from 0.817 to 0.971, 0.824 to 0.955, and 0.565 to 0.858 for LiF, $\text{Li}_2\text{B}_4\text{O}_7$, and Al_2O_3 detectors, respectively. Note that at a given energy of proton beam and depth in water, the values of *R* are comparable for LiF and $\text{Li}_2\text{B}_4\text{O}_7$ detectors (within 2%).

R values for carbon ion beams follow a similar trend as that of proton beams. For example, for LiF and $\text{Li}_2\text{B}_4\text{O}_7$ detectors, *R* values are close to unity (within 5%) at depths d₂-d₄ for all the investigated energies of Carbon ion. Whereas, in the case of Al₂O₃, the maximum deviation of *R* from unity is about 10% for 300 MeV/n at d₃ depth. However, at d₁, depending on the energy of the carbon ion beam, *R* values lie in the range of (a) 0.484–1.092 for LiF, (b) 0.489–1.147 for Li₂B₄O₇, and (c) 0.309–0.924 for Al₂O₃ detector.

Note that for a given energy of proton or carbon ion beam, R depends on the detector-to-water dose ratio (numerator of equation 2) and the detector-to-water dose ratio at reference beam, ⁶⁰Co (denominator of equation 2). For a given detector, $\begin{bmatrix} p \\ - \end{array}$

 $\left[\frac{de_{i}}{D_{wat}}\right]_{Q_{0}}$ is independent of depth in the water. For example,

$$\left\lfloor \frac{D_{det}}{D_{wat}} \right\rfloor_{Q_0} = 0.833, 0.873, \text{ and } 0.882 \text{ respectively, for LiF,}$$

 $Li_2B_4O_7$, and Al_2O_3 detectors.^[29] This is because at ⁶⁰Co energies, the interaction mechanism of photons with water

or detector material at various depths is predominantly by Compton scattering and therefore energy transferred to secondary electrons is proportional to electron density. In the case of ion beams, significant difference in the values of

 $\left\lfloor \frac{D_{det}}{D_{wat}} \right\rfloor$ is observed as a function of depth in water. Hence,

R values of a given energy (Q) of ion beam mostly follow

the behavior of
$$\left\lfloor \frac{D_{det}}{D_{wat}} \right\rfloor_Q$$
. Variation in $\left\lfloor \frac{D_{det}}{D_{wat}} \right\rfloor_Q$ with depth in

water and energy of the ion beam is due to the contributions from primary ion beam as well as secondaries generated. However, secondaries such as deuterons and other heavier ions collectively comprise about 1% or less of the total absorbed dose^[33,36] and hence have least importance in dosimetry. Thus,

 $\left\lfloor \frac{D_{det}}{D_{wat}} \right\rfloor_{Q}$ value depends mostly on the energy deposited by the

primary particles through ionization process.

Electronic mass collision stopping power
$$(S/\rho)_{e}$$
 values play
a major role in the determination of $\left[\frac{D_{det}}{D_{wat}}\right]_{Q}$. For better

understanding of the results, calculations of $(S/\rho)_{e}$ in water as a function of kinetic energy of protons and carbon ions are carried out using SRIM code.^[32] Figures 4 and 5 present the ratio of $(S/\rho)_{e}$ of the investigated TLD materials to that of water as a function of kinetic energy of proton and carbon ion beams, respectively. For example, $(S/\rho)_{e}$ in water varies in the range of 12.6–3.95 MeV-cm²/g and 298–98.5 MeV-cm²/g for proton beams of energy 50–250 MeV/n and carbon beams of energy 80-480 MeV/n, respectively.^[32] As the depth increases, kinetic energy of the beam decreases and therefore $(S/\rho)_{e}$ increases

with depth. It is observed that $\left[\frac{D_{det}}{D_{wat}}\right]_{Q}$ compares well with

the detector-to-water ratio of $(S/\rho)_{e}$ with a maximum deviation



Figure 4: SRIM^[32] calculated ratio of electronic mass stopping power of LiF, $\text{Li}_2\text{B}_4\text{O}_7$, and Al_2O_3 thermoluminescent dosimeter materials to water as a function of kinetic energy of protons

of 4% at the flat region (depths d_2 and d_4). However, at Bragg

peak, $\left[\frac{D_{det}}{D_{wat}}\right]_{Q}$ does not follow the detector-to-water $(S/\rho)_{e}$

ratio. The variation of R with depth can be explained as follows:

At depths
$$d_2 - d_4$$

values of $\left[\frac{D_{det}}{D_{wat}}\right]_Q$ for a given energy of ion beams are
comparable to detector-to-water ratio of $(S/\rho)_e$. This is because
at these depths the particle (proton or carbon ion) has sufficient
kinetic energy to cross the 1 mm-thick TLD voxel by depositing
energy which is dictated by $(S/\rho)_e$ of the detector material. As
calculated using SRIM code,^[32] the minimum kinetic energy
required to cross 1 mm thick water, LiF, Li₂B₄O₇, and Al₂O₃
voxel are 9, 14, 14, and 17 MeV/n, respectively, for protons.
Similarly, these values of kinetic energy for carbon ions are
17, 25, 24, and 31 MeV/n, respectively. Note that the kinetic
energy of the primary particles (protons and carbons) is greater
than the minimum required energy to cross the TLD voxel.

A difference of about 3% between the values of
$$\left\lfloor \frac{D_{det}}{D_{wat}} \right\rfloor_{Q}$$
 and

detector-to-water ratio of $(S/\rho)_{e}$ may be mainly due to the associated statistical uncertainties on the calculated $\left[\frac{D_{det}}{D_{wat}}\right]_{Q}$

values which is about 1.5%.

At d, depth (Bragg peak)

For a given energy of proton or carbon ion beams, kinetic energy of the incident ion beam decreases at Bragg peak significantly. As a result, the particles will not have sufficient kinetic energy to cross the TLD voxel and stop within the

voxel depositing their entire energy, and hence,
$$\left\lfloor \frac{D_{det}}{D_{wat}} \right\rfloor_Q$$
 does not follow detector-to-water ratio of (S/q)



Figure 5: SRIM^[32] calculated ratio of electronic mass stopping power of LiF, $Li_2B_4O_7$, and Al_2O_3 thermoluminescent dosimeter materials to water as a function of kinetic energy of carbon ions

Item name	Descriptions	References
Code, version/release date	FLUKA code (version 4.0)/26.11.2020	[23,24]
Validation	Validated for high-energy proton and carbon ion beams for medical applications	[26,27]
Timing	About 2160 total CPU hours on Intel (R) Xeon (R) 15 CPUs with clock speeds of 2.6 GHz	
Source description	Nonmodulated proton beam energy ranges from 50 to 250 MeV/n (with an increment of 50 MeV)	
	Nonmodulated carbon beam energy ranges from 80 to 480 MeV/n (with varying intervals)	
Cross sections	Elastic scattering through parameterized nucleon-nucleon cross sections and tabulated nucleon-nucleus cross sections	
	Inelastic scattering for hadron-hadron interactions is from parameterized fits of the available experimental data. For hadron-nucleus interactions a mixture of tabulated data and parameterized fits are used	
Transport parameters	PRECISIOn default card is used where both the particle transport threshold and delta-ray production threshold are set at 100 keV. EVAPORAT and COALESCE PHYSICS cards are activated. RQMD-2.4 is linked by <i>ldpmqmd</i> script	
VRT and AEIT	No variance reduction technique is used in this study	
Scored quantities	Dose to detector is scored using USRBIN card	
Number of histories/ statistical uncertainties	Up to 10 ⁸ histories are simulated/1 σ statistical uncertainties on the calculated values are <1%	
Statistical methods	Uncertainties are calculated with the default history-by-history method	
Postprocessing	Results are reported without using any kind of filtration	

Table 4: Summary of parameters used for Monte Carlo calculations as per the recommendations of AAPM Task Group-286^[31]

CPU: Central processing unit, RQMD: Relativistic Quantum Molecular Dynamics, VRT: Variance Reduction Technique, USRBIN: Expansion not required. It is technical term of FLUKA Monte Carlo code, AAPM: American Association of Physicists in Medicine, AEIT: Approximate Efficiency Improvement Technique

Table 5: Relative absorbed-dose energy response correction, R, presented for LiF, $Li_2B_4O_7$, and Al_2O_3 detectors for proton beams at different depths in the water phantom

Energy (MeV/n)	LiF					Li ₂ B ₄ O ₇				Al ₂ O ₃			
	d ₁	d ₂	d ₃	d ₄	d ₁	d ₂	d ₃	d ₄	d ₁	d ₂	d ₃	\mathbf{d}_4	
50	0.926	-	-	1.004	0.949	-	-	0.992	0.592	-	-	0.942	
100	0.817	1.010	0.990	0.991	0.824	1.004	0.983	0.985	0.565	0.939	0.908	0.929	
150	0.905	1.013	0.992	0.997	0.903	1.001	0.982	0.985	0.730	0.942	0.913	0.924	
200	0.971	1.003	0.988	1.007	0.955	0.989	0.980	0.991	0.858	0.937	0.913	0.929	
250	0.948	1.013	1.006	1.005	0.937	0.992	0.992	0.998	0.830	0.942	0.927	0.930	

Table 6: Relative absorbed-dose energy response correction, R, presented for LiF, Li₂B₄O₇, and Al₂O₃ detectors for carbon ion beams at different depths in the water phantom

Energy (MeV/n)	LiF				Li ₂ B ₄ O ₇				Al ₂ O ₃			
	d ₁	d ₂	d ₃	d ₄	d ₁	d ₂	d ₃	d ₄	d ₁	d ₂	d ₃	d ₄
80	1.092	-	-	1.030	1.147	-	-	1.008	0.705	-	-	0.969
130	0.484	1.011	1.003	1.013	0.489	1.009	0.984	0.976	0.309	1.000	0.971	0.940
200	0.512	1.055	0.984	0.989	0.590	1.054	0.961	0.970	0.370	1.054	0.917	0.931
300	0.643	1.045	0.956	1.005	0.661	1.024	0.979	1.002	0.427	1.013	0.898	0.940
400	0.604	1.017	0.975	0.991	0.764	0.997	0.977	0.962	0.508	1.007	0.914	0.930
480	1.059	1.022	1.007	0.972	1.038	1.004	1.021	0.960	0.924	0.994	0.947	0.936

The width of the Bragg peak for monoenergetic ion beams is so narrow that it may be considered to occur at a point, and due to the positioning of high density 1 mm thick TLD, the position of the Bragg peak will be shifted toward the smaller depth (as compared to position in water). As a result of this, a portion of TLD will lie at the distal end of the Bragg peak where kinetic energy of the residual particles (protons or carbon ions) is less as compared to the remaining portion of TLD. However, when the TLD is replaced with water medium, this effect is not significant. For investigating the effect of TLD thickness on the calculated R values, auxiliary simulations were carried out for Al_2O_3 TLD of thickness 0.1 mm placed at the Bragg peak locations of 50 and 250 MeV/n protons as well as 80 and 480 MeV/n carbon ions. The R values obtained for 0.1 mm thick Al_2O_3 TLD are: (a) 0.922 and 0.879 for 50 and 250 MeV/n protons, respectively, and (b) 0.941 and 0.907 for 80 and 480 MeV/n carbon ions, respectively. Thus, for thin detector positioned at the Bragg peak location, R approaches unity when the energy of the ion is smaller (for example, 50 MeV/n proton and 80 MeV/n carbon ions). Whereas,

for high energy ions (for example, 250 MeV/n proton and 480 MeV/n carbon ions), the response is less sensitive to the thickness of TLD. This suggests the importance of establishing detector thickness-specific R values for the ion beams.

CONCLUSION

The present study calculated R values for LiF, $Li_{2}B_{4}O_{7}$, and Al₂O₃ detectors as a function of depth in water for $5 \text{ cm} \times 5 \text{ cm}$ nonmodulated proton (50-250 MeV/n) and carbon ion (80-480 MeV/n) beams using FLUKA Monte Carlo code. This study shows that the calculated R values for LiF, $Li_2B_4O_7$, and Al_2O_2 detectors are insensitive to depth in water in the flat region of depth-dose profile and sensitive in the dose gradient region including at Bragg peak. The study also reveals that, for both the proton and carbon ion beams, the values of R differ from unity significantly at the Bragg peak position (d_1) and the degree of deviation from unity depends on the energy, type of ion beam, type of detector, and its thickness. The values of Rare close to unity (maximum deviation of about 7% for Al₂O₂ detector) at the flat region for the investigated detectors. The degree of deviation of R from unity reduces for thinner detector when the beam energy is smaller. The study suggests that for accurate dosimetry of protons and carbon ion beams using TLDs, the response of the TLD should be corrected to account for the beam-specific absorbed-dose energy dependence.

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Conflicts of interest

There are no conflicts of interest.

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