



Article Enhancing Thermoelectric Properties of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x Composites by Optimizing Carrier Concentration

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Abstract: Because of the high carrier concentration, copper telluride (Cu₂Te) has a relatively low Seebeck coefficient and high thermal conductivity, which are not good for its thermoelectric performance. To simultaneously optimize carrier concentration, lower thermal conductivity and improve the stability, BiCuTeO, an oxygen containing compound with lower carrier concentration, is in situ formed in Cu₂Te by a method of combining self-propagating high-temperature synthesis (SHS) with spark plasma sintering (SPS). With the incorporation of BiCuTeO, the carrier concentration decreased from 8.1×10^{20} to 3.8×10^{20} cm⁻³, bringing the increase of power factor from ~1.91 to ~2.97 μ W cm⁻¹ K⁻² at normal temperature. At the same time, thermal conductivity reduced from 2.61 to 1.48 W m⁻¹ K⁻¹ at 623 K. Consequently, (Cu₂Te)_{0.95}-(BiCuTeO)_{0.05} composite sample reached a relatively high *ZT* value of 0.13 at 723 K, which is 41% higher than that of Cu₂Te.

Keywords: thermoelectric materials; Cu2Te-BiCuTeO composites; carrier concentration

1. Introduction

With the capability of direct conversion from thermal energy to electrical energy through the movement of internal phonons and charge carriers, thermoelectric (TE) materials are widely researched and used in cogeneration, electronic refrigeration and thermal sensors [1–7]. Thus, TE materials play an increasingly crucial part in sustainable development. The energy conversion efficiency of a TE material is mainly depicted by its dimensionless figure of merit $ZT = \sigma S^2 T / \kappa$, where σ , *S*, *T* and κ are the electrical conductivity, Seebeck coefficient, absolute temperature and thermal conductivity, respectively [8,9]. Therefore, TE materials with high power factor (PF), which is defined as PF = σS^2 , but low thermal conductivity, are suitable for thermoelectric applications. To get the ideal thermoelectric performance, the PF of materials can be raised by band engineering, quantum confinement effects and electron energy barrier filtering [10–16]. Besides, κ can be reduced by nanostructures all-scale hierarchical architecture engineering, which is able to increase the scattering of short, medium and long wavelength phonons, and entropy engineering [17–22].

Among the TE materials, transition-metal chalcogenides, especially tellurides, such as PbTe [17,23], Bi₂Te₃ [24,25] and AgSbTe₂ [26,27], have been widely studied because of their high carrier mobilities and remarkably low thermal conductivities. In recent years, copper telluride (Cu₂Te) [28,29], along with copper selenide (Cu₂Se) [30] and copper sulfide (Cu₂S) [31], have emerged as promising thermoelectric materials. This kind of material has exhibited great thermoelectric performance due to its low thermal conductivity and electrical resistivity. Compared to Cu₂Se and Cu₂S, Cu₂Te should have more appealing thermoelectric performance owing to the lower ionicity of chemical bonds between Cu and



Citation: Zhang, W.; Zhou, Z.; Yang, Y.; Zheng, Y.; Xu, Y.; Zou, M.; Nan, C.-W.; Lin, Y.-H. Enhancing Thermoelectric Properties of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x Composites by Optimizing Carrier Concentration. *Materials* **2022**, *15*, 2096. https:// doi.org/10.3390/ma15062096

Academic Editor: Andres Sotelo

Received: 21 January 2022 Accepted: 2 March 2022 Published: 11 March 2022

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Copyright: © 2022 by the authors. Licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution (CC BY) license (https:// creativecommons.org/licenses/by/ 4.0/). Te due to the lower electronegativity of Te in comparison to Se or S, which is beneficial for obtaining large carrier mobility (μ) and improving its carrier conductivity. Besides, the lattice thermal conductivity (κ_L) of Cu₂Te is expected to be lower than that of Cu₂S and Cu₂Se because tellurium is much heavier than sulfur and selenium. These two points make Cu₂Te a theoretical potential TE material with high *ZT* [32]. However, an abnormality has been found ascribed to two aspects. One of them is that the hole concentration (pH) of Cu₂Te is too high because of its severe copper deficiency, which easily forms nonstoichiometric Cu_{2- δ}Te compound [33]. The other is that the phase diagram of Cu₂Te is too complex, especially, it has at least five phase transitions from room temperature to its melting point [34].

Several researches have been made to improve the thermoelectric property of Cu_2Te in recent years. Dabin Park, et al. [28] synthesized Te/Cu_2Te nanorod composites with 1D nanostructure through a solution phase mixing process by using Cu_2Te with different properties and polyvinylpyrrolidone (PVP) in 2018. Sayan Sarkar, et al. [29] synthesized Ga-doped Cu_2Te , $Cu_{1.97}Ga_{0.03}Te$, to improve the electrical conductivity and Seebeck coefficients of Cu_2Te in 2019. However, the way of incorporating with oxide to optimize the thermoelectric properties of Cu_2Te is rarely reported.

BiCuXO (X = S, Se and Te) oxychalcogenides have a layered structure that is made up of $(Bi_2O_2)^{2+}$ insulating layers alternately stacked with $(Cu_2X_2)^{2-}$ conductive layers as a charge reservoir along the *c*-axis [35–37]. With regard to the thermoelectric properties of BiCuXO, most previous studies focus on BiCuSeO due to the high Seebeck coefficient and low thermal conductivity, but low conductivity [38]. Besides, oxide-containing compounds have better chemical and thermal stability [39]. Based on the above, we planned to combine Cu₂Te with BiCuTeO to lower the thermal conductivity and improve the Seebeck coefficient of Cu₂Te by optimizing the carrier concentration.

Herein, we synthesized $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x composites by self-propagating hightemperature synthesis (SHS) and spark plasma sintering (SPS) process to optimize carrier concentration (*n*) and decrease the total thermal conductivity. As a result, the PF was raised from ~1.91 to ~2.97 μ W cm⁻¹ K⁻² at normal temperature, and the (Cu₂Te)_{0.95}-(BiCuTeO)_{0.05} composite sample reached a relatively high *ZT* value of 0.13 at 723 K, which is 41% higher than that of pristine Cu₂Te.

2. Materials and Methods

 $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x (x = 0, 0.05, 0.1, 0.2, 0.3, 0.4) samples were prepared by selfpropagating high-temperature synthesis (SHS) and spark plasma sintering (SPS) process. Commercial high-purity powders of Bi (4N, Innochem, Meerhout, Belgium), Cu (AR, Meryer, Shanghai, China), Te (4N, Aladdin, Shanghai, China) and Bi₂O₃ (3N, Meryer) were weighed with a stoichiometry of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x (x = 0, 0.05, 0.1, 0.2, 0.3, 0.4), and then mixed uniformly in an agate mortar in air. The mixed powders were cold-pressed into a pellet using a steel die under 6 MPa in air and the bulk was put in an alumina crucible. The SHS process was started by heating the bottom of the crucible to the ignition temperature with an alcohol lamp in air. Once the reaction began, we put the lid on the cauldron and moved the alcohol lamp away. The combustion wave was persisted by the energy released by the initial reaction and it spread to the whole bulk in a few seconds. The product after SHS was crushed into powders and the obtained powders were densified by SPS furnace (Sumitomo SPS-1050T, Fuji, Japan) for 10 min at 773 K under axial pressure of 40 MPa.

The micro-structure of all prepared bulks was characterized by the X-ray diffraction (XRD; D/max-2500/PC, Rigaku, Japan). The fractured surface morphology of the samples was studied by field emission scanning electron microscopy (FESEM; ZEISS-MERLIN, Germany), equipped with energy dispersive spectrometer (EDS). The morphology and chemical composition of the nano-powders (prepared by grounding bulks into powders and ball milling following by ultrasonic treatment into nano-powders) were characterized by high-resolution transmission electron microscopy (TEM; JEM-2100F, JEOL, Tokyo,

Japan) with an integrated energy dispersive spectrometer (EDS), and the corresponding fast Fourier transform (FFT) patterns are obtained by RADIUS software. The electrical conductivity (σ) and Seebeck coefficient (*S*) were simultaneously measured by using a ZEM-3 instrument (ULVAC-RIKO, Yokohama, Japan). Thermal conductivity (κ) was measured indirectly according to the equation $\kappa = DC_P\rho$, where *D* is thermal diffusivity as measured by the LFA 457 MicroFlash (Netzsch, Weimar, Germany), ρ is the mass density of samples determined according to the Archimedes method and C_P is the specific heat capacity calculated according to the Neumann–Kopp rule [40]. The Hall coefficients were investigated at room temperature and a magnetic field of 0.7 T, from which the carrier concentration and mobility of all samples was able to be determined.

3. Results and Discussion

Cu₂Te, along with its nonstoichiometric compound Cu_{2- δ}Te, has a very complicated crystal structure among all the copper chalcogenides [33]. The crystal structure at room-temperature for prepared (Cu₂Te)_{1-x}-(BiCuTeO)_x bulk samples, as presented in Figure 1, is very complicated as well, and consists of different phases. As x = 0, the Cu₂Te is composed of Cu₂Te (PDF#06-0649), Cu_{2- δ}Te (PDF#10-0421) and Cu_{0.664}Te_{0.336} (PDF#37-1027), similar to the previous study [33]. When x = 0.1, the peaks of BiCuTeO are detected at 33°, and become more and more pronounced with the content of BiCuTeO growing. Since x = 0.2, the peaks of Cu₂Te (PDF#06-0649) start to decrease, because the Cu and Te reacted with Bi and O to form BiCuTeO. The standard Powder Diffraction File (PDF) card is calculated according to the literature data [41].



Figure 1. Bulk XRD patterns for $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x (x = 0, 0.05, 0.1, 0.2, 0.3, 0.4).

To prove structure evolution of the $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x and the in situ formation of BiCuTeO, detailed microscopic investigations were made on the prepared Cu₂Te samples. Two phases with obviously different contrast were presented in the cross-sectional microstructures of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x shown in Figure 2a,b. It can be easily seen that there are a large number of tiny dispersive particles homogeneously clung or embedded to each layer. Due to the intrinsic layered feature of Cu₂Te, and the gathering of Bi which was revealed in Figure 2b through the energy dispersive spectrometer (EDS), the powders with lower contrast should be BiCuTeO and the slices with higher contrast are Cu₂Te.

TEM investigation was performed on $(Cu_2Te)_{0.9}$ -(BiCuTeO)_{0.1} sample to research microstructure information, as revealed in Figure 3a,b. A few tinier nanocrystals of 50 nm could be observed in Figure 3a and was proved to be bismuth content clumping together by EDS analysis. Figure 3b shows the HRTEM image of $(Cu_2Te)_{0.9}$ -(BiCuTeO)_{0.1}. The lattice fringe space measured as 4.7 Å may correspond to the (002) plane of BiCuTeO, while differently oriented lattice spacing of about 7.2 Å, 3.3 Å and 2.9 Å may correspond to (003), (106) and (204) planes of $Cu_{2-\delta}$ Te, respectively. Actually, the lattice spacing of about 7.2 Å and 3.3 Å could also be assigned to the (031) and (162) planes of Cu_2 Te, because of their similar crystal structure.



Figure 2. (a) FESEM fractography for (Cu₂Te)_{0.9}-(BiCuTeO)_{0.1}; (b) EDS for (Cu₂Te)_{0.9}-(BiCuTeO)_{0.1}.



Figure 3. (a) TEM and EDS for $(Cu_2Te)_{0.9}$ -(BiCuTeO)_{0.1}. (b) HRTEM for $(Cu_2Te)_{0.9}$ -(BiCuTeO)_{0.1}. The insets are the corresponding fast Fourier transform (FFT) patterns for the areas marked in Figure 3b.

Since Cu₂Te has a complex phase diagram containing at least five phase transitions from room temperature to its melting point [34], the electrical performance of Cu₂Te is abnormal with temperature change. Figure 4 displays the electrical properties of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x as a function of temperature, where (a)–(c) are the in plane electrical conductivity, Seebeck coefficient and power factor, respectively. As presented in Figure 4a, the electrical conductivity reduces except for the phase transition regions as the temperature increases, behaving as a highly degenerate semiconductor. When x is less than 0.1 and more than 0.2, the electrical conductivity is decreased as the content of BiCuTeO increases, while the electrical conductivity increases from x = 0.1 to x = 0.2. The reason should be ascribed to the variable carrier concentration and mobility, as demonstrated in Table 1. Since x = 0.2, Cu₂Te (PDF#06-0649), one of the main phases, begins to decrease until it almost disappears, while the phase of BiCuTeO increases. That leads to the decrease of the carrier concentration and increase of the carrier mobility, as Cu₂Te has a high carrier concentration and BiCuTeO has a low carrier concentration but high mobility.



Figure 4. In plane electrical properties of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_{*x*}: (**a**) electrical conductivity, (**b**) Seebeck coefficient, (**c**) power factor. Electrical properties of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_{*x*}; out-of-plane electrical properties of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_{*x*}: (**d**) electrical conductivity, (**e**) Seebeck coefficient, (**f**) PF.

Samples	<i>n</i> (cm ⁻³)	μ (cm ² V ⁻¹ s ⁻¹)	$R_{ m H}$ (cm ³ C ⁻¹)	$m^{*}(m_{0})$
Cu ₂ Te	$8.085 imes10^{20}$	58.58	$7.819 imes10^{-3}$	0.663
(Cu2Te)0.95-(BiCuTeO)0.05	$4.459 imes 10^{20}$	54.71	$1.400 imes 10^{-2}$	0.785
(Cu ₂ Te) _{0.9} -(BiCuTeO) _{0.1}	$3.804 imes10^{20}$	58.47	$1.641 imes 10^{-2}$	0.716
(Cu2Te) _{0.8} -(BiCuTeO) _{0.2}	$1.691 imes10^{20}$	295.40	$3.692 imes 10^{-2}$	0.025
(Cu2Te)0.7-(BiCuTeO)0.3	2.289×10^{20}	151.50	$2.727 imes 10^{-2}$	0.052
(Cu ₂ Te) _{0.6} -(BiCuTeO) _{0.4}	2.379×10^{20}	102.90	2.627×10^{-2}	0.110

Table 1. Carrier concentration and mobility of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x. (R_H is Hall coefficient).

All the samples display p-type conducting within the measured temperature range on account of the intrinsic copper deficiencies in Cu₂Te, as shown in Figure 4b, which is proved by the positive Seebeck coefficient. The Seebeck coefficient for all samples is relatively low, even no more than 60 μ V K⁻¹ at 723 K. Such a low Seebeck coefficient is related to the high carrier concentration. Among all the samples, (Cu₂Te)_{0.95}-(BiCuTeO)_{0.05} and $(Cu_2Te)_{0.9}$ -(BiCuTeO)_{0.1} composites show the highest Seebeck coefficient values of 26.94 μ V K⁻¹ and 27.33 μ V K⁻¹ at room temperature, respectively. Besides the appropriate carrier concentration, the DOS effective mass (m^*) should be another reason. Thus, it is necessary to calculate the m^* . The calculations are based on assumption of acoustic phonon scattering and the single parabolic band (SPB) mode [19]. Although the calculation of a single parabolic band model in a complex system is not that accurate, especially after the content of BiCuTeO has increased, a trend could be observed according to the results. It can be seen from Table 1, that (Cu₂Te)_{0.95}-(BiCuTeO)_{0.05} and (Cu₂Te)_{0.9}-(BiCuTeO)_{0.1} composites have the highest m^* of 0.785 m_0 and 0.716 m_0 . The PF of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x as a function of temperature is displayed in Figure 4c. The variation in PF is very similar to that in Figure 4b, illustrating that Seebeck coefficient plays a decisive role in altering the PF of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x. The PF of pristine Cu₂Te is 4.05 μ W cm⁻¹ K⁻² at 723 K, and the PF of (Cu₂Te)_{0.95}-(BiCuTeO)_{0.05} and (Cu₂Te)_{0.9}-(BiCuTeO)_{0.1} composites increase to 4.49 μ W cm⁻¹ K⁻² and 4.43 μ W cm⁻¹ K⁻² at 723 K, respectively. The difference of PF at high temperature is not so obvious, but the improvement of PF is large at room temperature. The PF increased from 1.91 (for pristine Cu₂Te) to 2.97 μ W cm⁻¹ K⁻² (for the $(Cu_2Te)_{0.95}$ -(BiCuTeO)_{0.05} at normal temperature. Figure 4d–f display the out of plane electrical conductivity, Seebeck coefficient and power factor, and are similar to Figure 4a-c, indicating that $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x composites have nearly isotropic transports.

The total thermal conductivity (κ_{tot}) of (Cu₂Te)_{1-x}-(BiCuTeO)_x composites shown in Figure 5a is quite high, which are due to the inherent metallic property of Cu₂Te and the high hole concentration caused by unavoidable deviation from stoichiometry. They show complicated temperature dependencies in the temperature ranged from 300 to 723 K, first decreasing and then increasing as a whole over the entire temperature range, which is the effect of the phase transition of Cu_2Te [29]. $(Cu_2Te)_{0.95}$ -(BiCuTeO)_{0.05} and $(Cu_2Te)_{0.95}$ -(BiCuTeO)_{0.1} composites have the lowest thermal conductivity due to the lower carrier thermal conductivity (κ_e). As displayed in Figure 5b, the κ_e is dominant in the total thermal conductivity (κ_{tot}). The κ_e of (Cu₂Te)_{1-x}-(BiCuTeO)_x changes, affected by its electrical conductivity according to Wiedemann law, $\kappa_e = L\sigma T$, where L, σ and T are Lorentz coefficient, electrical conductivity and temperature, respectively. Besides, electrical conductivity could be calculated according to $\sigma = ne\mu$, where *n*, *e* and μ are carrier concentration, elementary charge and carrier mobility, respectively. As exhibited in Table 1, from x = 0 to x = 0.1, the carrier concentration of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x is decreased, which causes the reduction of the σ and further results in the depression of the κ_{e} . When the content of BiCuTeO changes from 0.1 to 0.2, the carrier mobility is improved a lot, bringing about a high σ and further causing the enhancement of κ_e . The reduction of the range from x = 0.2 to x = 0.4 is owing to the dropping of the μ . The κ_{tot} decreases to 1.48 W m⁻¹ K⁻¹ at 623 K with increasing BiCuTeO content, while the thermal conductivity of Cu₂Te is 2.61 W m⁻¹ K⁻¹ at 623 K.



Figure 5. (a) Thermal conductivity of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x as a function of temperature. (b) Lattice thermal conductivity (κ_L) and carrier thermal conductivity (κ_e) as a function of BiCuTeO content at room temperature.

Consequently, combining the results of the higher PF and lower κ_{tot} , the *ZT* values of $(Cu_2Te)_{0.95}$ -(BiCuTeO)_{0.05} and $(Cu_2Te)_{0.9}$ -(BiCuTeO)_{0.1} are higher than that of Cu_2Te , as illustrated in Figure 6. The *ZT* values of $(Cu_2Te)_{0.95}$ -(BiCuTeO)_{0.05} and $(Cu_2Te)_{0.9-}$ (BiCuTeO)_{0.1} are 0.13 and 0.12 at 723 K, respectively, while the *ZT* value of pristine Cu_2Te is 0.09 at 723 K.



Figure 6. *ZT* of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_x as a function of temperature.

4. Conclusions

In this study, we successfully synthesized $(Cu_2Te)_{1-x}$ - $(BiCuTeO)_x$ composites by SHS combined with SPS. The carrier concentration has been optimized with the incorporation of BiCuTeO, which increased the power factor of $(Cu_2Te)_{1-x}$ - $(BiCuTeO)_x$ and largely decreased carrier thermal conductivity resulting in a lower total thermal conductivity.

Consequently, the $(Cu_2Te)_{0.95}$ -(BiCuTeO)_{0.05} composite sample reached a relatively high *ZT* value of 0.13 at 723 K, which is 41% higher than that of pure Cu₂Te.

Although the *ZT* of $(Cu_2Te)_{1-x}$ -(BiCuTeO)_{*x*} is not high enough, this study lays a foundation for better performance system research.

Author Contributions: Conceptualization, W.Z. and Z.Z.; methodology, W.Z. and Y.Z.; software, W.Z. and Y.Y.; validation, Y.X.; formal analysis, W.Z. and Z.Z.; investigation, W.Z.; resources, Y.Z. and Y.Z.; data curation, W.Z. and Y.Y.; writing—original draft preparation, W.Z.; writing—review and editing, W.Z., Z.Z., M.Z. and Y.-H.L.; visualization, M.Z.; supervision, Y.-H.L.; project administration, Y.-H.L. and C.-W.N.; funding acquisition, Y.-H.L. and C.-W.N. All authors have read and agreed to the published version of the manuscript.

Funding: This work was financially supported by the Basic Science Center Project of the National Natural Science Foundation of China under grant No. 51788104, National Science Foundation of China (51729201, 52172211) and National Key Research Program of China under grant No. 2016YFA0201003.

Institutional Review Board Statement: Not applicable.

Informed Consent Statement: Not applicable.

Data Availability Statement: Data is contained within the article.

Conflicts of Interest: The authors declare no conflict of interest.

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