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Article

Reaction of Ta₃⁻ Clusters with Molecular Nitrogen: A Mechanism Investigation

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ABSTRACT: Because of the inertness of molecular nitrogen, its practicable activation under mild conditions is a fundamental challenge. Ta_3^- is an exceptionally small cluster that reacts with N₂ at room temperature, leading finally to $Ta_3N_2^-$; $Ta_3N_2^-$ also could react with N₂ at room temperature, leading finally to $Ta_3N_4^-$, a product of interest in its own right because of its potential as a nitrogen fixation medium. The mechanisms of the Ta_3^- and $Ta_3N_2^-$ -mediated activation of the N \equiv N triple bond have been investigated. Our extensive computations elucidate mechanisms for the ready reactions, leading to stepwise cleavage of the N \equiv N bond. Initial isomeric N₂/Ta₃⁻ complexes, N \equiv N elongation, undergo a N \equiv N split over generally low barriers in a highly exothermic process. The nitrogen-atom or molecular exchange reactions found in the Ta₃N₂⁻/N₂ system may be of paramount importance in both applied and fundamental studies.

1. INTRODUCTION

The atmospheric abundance, accessibility, and nontoxicity of N₂ make it particularly desirable for us to construct N-containing compounds,¹⁻⁴ such as typical synthetic ammonia reaction.⁵⁻⁹ However, the functionalization of N₂ represents a major challenge for modern chemistry due to its stability. The stability could be accounted for the lack of the dipole moment, the high bond dissociation energy (941 kJ mol⁻¹), high ionization energy (15.58 eV), the low proton and electron affinities (5.1 and -1.9 eV respectively),^{6,10-12} as well as the very low lying, completely filled σ - and π -molecular orbitals and substantial energy gap between the highest occupied molecular orbital (-15.6 eV) and the lowest unoccupied molecular orbital (7.3 eV).

Vol'Pin and Shur were the first to study nitrogen fixation with transition-metal complexes.¹³ Transition metals (M) could weaken or break the strong triple bond (N \equiv N) by donating electrons from d orbitals to empty antibonding π and σ orbitals of N₂ (Scheme 1a). In return, electron donation from fully filled π - and σ -orbitals of N₂ to vacant M orbitals could be found as well (Scheme 1b).^{14–16} The former donation is vital in enabling N₂ binding and reduction, following which metal–nitrogen formed and strengthened. However, the latter donation is relatively small. By extension, the complete splitting of the N \equiv N by metal clusters is essentially governed by combining the two donations.^{16,17}

Moreover, the $M-N_2$ binding mode strongly depends on the nature of the metal center. The different coordination modes generally show different orbital interaction modes and charge transfer and also different kinds of activation of the N \equiv N bond.^{19,20} There are four possible coordination modes (Scheme 2): (1) end-on (η^1 -N₂, $M-M-N\equiv$ N, Scheme 2a), N₂ gets

Scheme 1. Orbital Interactions between N_2 and Transition Metal $\left(M\right)$



activated upon η^1 -coordination to the first metal center, so the electron density in the antibonding orbitals in N₂ increases, rendering the coordinated molecule a better base for another metal center, (2) end-on bridging (Scheme 2b), μ - η^1 - η^1 -N₂, generally, M-M-N=N and M-N=N-M are more or less linear to allow for efficient orbital overlap. (3) Side-on mode (η^2 -N₂, Scheme 2c) and μ - η^2 - η^2 -N₂ bridging coordination mode

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Scheme 2. Possible Modes of N_2 Coordination to Transition Metal



(Scheme 2d) is not as usual as the end-on one. Compared to end-on mode involving two M–N π -bonds, there is only one π bond, while σ donation and backdonation (Scheme 1a,b) probably were not involved. Therefore, the end-on mode usually is energetically preferred than the side-on mode.²¹ (4) Side-onend-on (μ - η ¹: η ²-N₂) (Scheme 2e), exhibiting a side-on coordination of N₂ to one metal center and an end-on coordination to the other.

Metal clusters have been found to be able to react with N₂.²²⁻³¹ However, most of the studied clusters can only adsorb N₂, and a few of them can split the N \equiv N under moderate conditions such as Sc, Ti, Gd, Co, Fe, and Ta clusters.^{17,32-42} Among them, it was recognized that Ta clusters give outstanding performances to split the N \equiv N completely since the Ta-Ta center has enough reductivity to store electrons of N₂.^{43,44}

As shown by the recent investigations, the extent of N \equiv N elongation varies with the model cluster size.⁴⁵ Larger clusters are favorable for N₂ adsorption. However, it does not necessarily have higher activity towards N₂ activation. Studies predicted that N₂ molecule activation is accessible at ambient temperature by small Ta_n⁺ clusters (n = 2, 3, 4). The rate-limiting transition states is located at -55, -44, and -59 kJ mol⁻¹ for Ta₂⁺,¹⁶ Ta₃⁺, and Ta₄^{+,46} respectively, however it is located above the entrance asymptote for Ta₆^{+,35} Significantly, during N₂ activation by Ta₄⁺ and Ta₆⁺, the surface Ta–Ta–Ta acted as a protagonist, and the other Ta atoms were not directly involved or played only a minor role in N₂ cleavage. The Ta₃ moiety is the key structural unit of Ta series clusters and surfaces in N₂ cleavage. It is particularly important to study N₂ activation by Ta ternary clusters.

Moreover, our studies indicated that an anionic system can give better kinetic activity and thermodynamic stability of the product than cationic and neutral ones.^{47,48} V and Tanitride,^{37,49} V and Ta-carbide,^{36,50–52} and Co hydride⁵³ anion clusters are identified to be highly reactive toward N≡N bond cleavage by combining quantum chemistry calculations and experimental studies. Motivated by the vivid and splendid studies, we present detailed mechanisms of the first and second N₂ activation by anion cluster Ta₃[−] at a molecular level, which probably would be taken as a model in the cluster and surface reactions.

2. COMPUTATIONAL DETAILS

All calculations were carried out by using the Gaussian 09 package.⁵⁴ The high quality of the triple- ζ def2-TZVP basis set was confirmed in previous, rather extensive studies.^{55–57} For the Ta metal atoms, an effective core potential (ECP) is used for an approximate treatment of relativistic effects. We used the Becke-3-Lee–Yang–Parr (B3LYP) functional, which has already been successfully applied in the Ta₂⁺/N₂ and Ta₂N⁺/N₂ systems.^{16,17} Furthermore, Armentrout and co-workers reported that B3LYP provides bond energies for MO⁺ and MO₂⁺ (M = Ta, W), which correspond very well to experimental data.¹⁸

Harmonic vibrational frequencies were computed to verify the nature of the stationary points. To corroborate the correct link between the minima and the transition states (TSs), intrinsic reaction coordinate^{58–61} calculations were performed. Unscaled vibrational frequencies were used to calculate the zeropoint energy contributions; thermal corrections to the enthalpy (ΔH) within the ideal-gas, rigid-rotor, harmonic-oscillator approximation at a temperature of 298 K and a pressure of 1 atm have been applied.

To obtain possible low-energy structures on the landscapes of the Ta_3^{-}/N_2 and $Ta_3N_2^{-}/N_2$ couples, the ABCluster⁶² has been used to generate guess structures of $Ta_3N_2^{-}$ and $Ta_3N_4^{-}$ clusters. The def2-SVP basis set was adopted in the initial calculations, which produced more than 200 optimized structures. Subsequently, the lowest-lying isomers were reoptimized at the B3LYP/def2-TZVP level to obtain the global minimum structures of $Ta_3N_2^{-}$ and $Ta_3N_4^{-}$.



Figure 1. Simplified PES (ΔH_{298K} in kJ mol⁻¹) for Ta₃⁻/N₂ coupling at the B3LYP/def2-TZVP + ECP level of theory. Key structures including selected geometric parameters are also provided. Bond lengths are given in angstrom and relative energies are given with respect to the entrance asymptote. ΔG (kJ mol⁻¹) is behind the vertical line.



Figure 2. Simplified PES (ΔH_{298K} in kJ mol⁻¹) of Ta₃N₂^{-/}N₂ coupling at the B3LYP/def2-TZVP + ECP level of theory. Key structures including selected geometric parameters are also provided. Bond lengths are given in angstrom and relative energies are given with respect to the entrance asymptote. ΔG (kJ mol⁻¹) is behind the vertical line.

3. RESULTS AND DISCUSSION

3.1. Ta₃⁻ Mediates the N=N Bond to Form Ta₃N₂⁻. The optimal potential energy surface (PES) and structural parameters of key species for Ta₃⁻ mediates N=N activation at B3LYP/def2-TZVP are shown in Figure 1. Three possible spin states, singlet, triplet, and quintet, are invested (Figure S1). The left superscript 1/3/5 is used to represent the singlet/triplet/quintet state (e.g., $^{1/3/5}$ 1). The ground state of Ta₃⁻ is a quintet, which is 20 and 29 kJ mol⁻¹ lower than the triplet and singlet, respectively.

The Ta_3^{-}/N_2 coupling starts from either the quintet or triplet separated reactants, and it is subject to a two-state reactivity mechanistic scenario. The triplet/quintet PES crosses at the minimum energy crossing point (MECP, -60 kJ mol^{-1}), which could turn a spin flip from the quintet to the triplet surface and lead to obtaining the intermediate ³1, releasing -67 kJ mol⁻¹ of heat. The optimized structure indicates an end-on η^1 -N₂ coordination mode with the distances of $Ta^{a}-N^{a} = 2.05$ Å and $N^{a}-N^{b} = 1.15$ Å. Subsequently, the triplet dominates the PES, so the triplet mechanism is mainly discussed below. Ta^b attacks N≡N further in a side-on manner to obtain a well-known combining end-on/side-on mode ³2 (μ - η^{1} : η^{2} -N₂) releasing -118 kJ mol⁻¹ energy. In ³2, the end-on bond length between the terminal nitrogen atom (N^a) and Ta^a is 1.96 Å, and the side interaction between Ta^b and N^a-N^b forms Ta^b-N^a (2.12 Å) and Ta^b-N^b (2.00 Å) bonds. Compared with the separation reactant, the $N \equiv N$ bond is weakened, and the bond length of the N \equiv N bond is elongated by 0.20 Å. Meanwhile, the Ta^a–Ta^b bond is elongated from 2.47 to 2.58 Å. Note that from ³1 to ³2, no barrier is encountered. However, in the Ta_4^+/N_2 system studied by Fries et al., this step requires merely an activation of 5 kJ mol⁻¹.⁴

The N \equiv N bond is elongated to 1.41 Å by the interaction of N^b with the third Ta atom (Ta^c) through the transition state ³TS1 with an energy below the entrance asymptote of -92 kJ mol⁻¹ generating ³3 (-160 kJ mol⁻¹; C_s symmetry). N^b is changed from being interacted only with Ta^b in ³2 to being interacted with the three Ta atoms. That is, the geometric structure is transferred from a η^2 to η^3 coordination, and this transformation is the rate-limiting step which is called the across edge-above surface (AEAS) mechanism by Fries et al. The prediction that AEAS operates significantly more likely on small

clusters is confirmed.⁴⁶ Note that the rate-limiting transition state ³TS1 in Ta₃⁻/N₂ coupling has the lowest energy among those in Ta₂⁺, Ta₄⁺, and Ta₆⁺/N₂ couplings.^{16,35,46} Finally, N \equiv N is completely broken through the transition state ³TS2 with a low energy barrier of 10 kJ mol⁻¹, generating the lowest energy intermediate ³4 (-469 kJ mol⁻¹; C_s symmetry). In addition, there are other reaction paths for Ta₃⁻/N₂ coupling (Figure S2), but they are disadvantageous on PES.

3.2. $Ta_3N_2^{-}/N_2$ Coupling. $Ta_3N_2^{-}$ (4 in Figure 1)/ N_2 coupling is quite complicated (Figure S3). Only the optimal PES and structural parameters of key species are shown in Figure 2. The ground state of $Ta_3N_2^{-}$ is triplet, which is 32 and 67 kJ mol⁻¹ lower than singlet and quintet, respectively (Figure S1). Moreover, the triplet species along the PES have more thermodynamic stability than the other two states, and there is no crossing point on the PES. Therefore, only the triplet state is studied.

First, N_2 approaches the $Ta_3N_2^-$ through the end-on mode $(\mu - \eta^1)$ to form ³5 (-57 kJ mol⁻¹). Inspecting the geometric features of 3 5, the N^c-Ta^b bond length is 2.07 Å. Compared with the separated reactant, the N≡N bond is slightly weakened and the length is elongated by 0.05 Å. Then, N^c and N^d interact further with Ta^c in a side-on manner to obtain end-on/side-on mode ³6 (μ - η^1 : η^2 -N₂), releasing -144 kJ mol⁻¹ energy. The length of the N \equiv N bond in ³6 is elongated by 0.16 Å than that of ³5. The extension of the N \equiv N bond is similar to that in the Ta_3^{-}/N_2 coupling. At the same time, the three Ta atoms become detached and Ta and N become intimate in ³6, for instance, the Ta^{b} -Ta^c bond is elongated to 2.64 Å, the end-bonded Ta^{b} -N^c bond length is 1.96 Å, and the side-bonded $Ta^b - N^c$ and $Ta^b - N^d$ bond lengths are 2.07 and 2.00 Å, respectively. The transition state ³TS3 is located 10 kJ mol⁻¹ above that of ³5. However, in Ta_3^{-}/N_2 , this step is no barrier.

The N \equiv N bond is elongated for a third time similar to AEAS. N^d interacts with the third Ta atom (Ta^a) through ³TS4, which is located -88 kJ mol⁻¹ below the entrance asymptote to generate ³7 (-132 kJ mol⁻¹; C_s symmetry). In ³7, the N \equiv N bond is elongated to 1.40 Å, which is 0.10 Å longer than that of ³6. Subsequently, from ³7, the N \equiv N bond could also be a cleavage finally through one transition state (³TS17), generating ³18. However, the energy barrier (-6 kJ mol⁻¹ below the entrance) is much higher and ³18 is not the lowest energy structure on the landscapes. Surprisingly, a lower energy channel was detected, and it can lead to the lowest energy structure (³9, -418 kJ mol⁻¹) on the landscapes, which is one step more than Ta₃⁻/N₂ coupling. This path can be described in detail as follows. From ³⁷ to ³⁸, Ta and N become more intimate; for instance, the Ta^b-N^c bond is shortened from 2.09 to 1.93 Å, and Ta^c-N^d is shortened from 2.18 to 2.07 Å. Meanwhile, the Ta^b-Ta^c bond is elongated to 2.70 Å. In this process, the N≡N bond is only slightly elongated, from 1.40 to 1.41 Å, and only needs to pass through the transition state ³TS5 with an energy of -117 kJ mol⁻¹. However, the energy of the transition state ³TS6 (-54 kJ mol⁻¹) through which the N^c-N^d bond is completely destroyed is much higher than that of ³TS2 (-150 kJ mol⁻¹) in the Ta₃⁻/N₂ coupling. From the perspective of the activation energy barrier, the rate-determining transition state is ³TS6.

Incidentally, if the remaining intermediate ³9 is taken as the start of the PES, $Ta_3^{14}N^{15}N^- + {}^{14}N^{15}N$ or $Ta_3^{15}N_2^- + {}^{14}N_2$ would be the product. This scenario only could be presented when N is labeled; otherwise, N₂ activation may be hidden without being discovered. The scenarios that N atoms or N₂-ligand exchange reactions between ${}^{15}N_2$ and $Ta_3^{14}N_2$ revealed follow the Mars–van Krevelen (MVK) mechanism.¹⁷ The highly symmetrical structure of ³9 is the key to N exchange.

3.3. Crucial Properties. Density functional theory (DFT) calculations are further employed to probe the crucial properties including the electronic structures of the key complexes in Ta_3^{-}/N_2 and $Ta_3N_2^{-}/N_2$ couplings.

In Table 1, we present the natural bond orbital (NBO) charge and the energy of the d donating orbital of the Ta_3^- and $Ta_3N_2^-$

Table 1. NBO Charges and Orbital Energies (Unit: eV) of the Major π Backdonation Donor Orbital (π_b) of Ta₃⁻ and Ta₃N₂⁻ Clusters at the B3LYP/def2-TZVP + ECP Level

	nature			
clusters	Ta	Ta	$\pi_{ m b}$	
Ta ₃ -	-0.29	-0.42	1.25	
$Ta_3N_2^-$	0.06	0.22	0.90	

clusters. The detailed evolution of the electronic structure along the reaction coordinate is shown in Figure S4. The activation of N_2 by a metal cluster is the reduction of N_2^0 into $2N^{3-}$; therefore, the stronger the electron supply ability and oxidation of metal, the stronger its ability to activate N_2 . Compared with Ta_3^- , the metal oxidation state of $Ta_3N_2^-$ is increased, and its ability to donate electrons becomes weaker. Correspondingly, the activity of $Ta_3N_2^-$ is weaker than that of Ta_3^- . In addition, the orbital energy of π_b in $Ta_3N_2^-$ is also reduced, which makes it more difficult for the transfer of d electrons to the $\pi^*_{(N-N)}$ or $\sigma^*_{(N-N)}$ orbital.

The binding of N₂ to the Ta₃⁻ or Ta₃N₂⁻ cluster can occur in either the side-on (10 and 15) or end-on (5 and 10) configurations. IR spectra as a function of wavelength were calculated at the B3LYP/def2-TZVP + ECP level (Figure S5). This behavior is similar to that shown in $M^+-(N_2)_n$ systems.^{22,23} End-on binding reproduced its favorite. The end-on binding is more strongly bound by 29 and 26 kJ mol⁻¹ than the side-on binding for the triplet state for Ta₃⁻/N₂ and Ta₃N₂⁻/N₂, respectively.

In order to explore the effects of temperature and pressure on the reaction, the transition state ³TS1 of the rate-determining step in the Ta₃⁻/N₂ reaction was selected. Figure 3 shows the change of relative Gibbs free energy (ΔG , kJ mol⁻¹) along with temperature (K) at a pressure of 1 atm. One can see that ΔG



Figure 3. Change of relative Gibbs free energy (ΔG , kJ mol⁻¹) for ³TS1 with temperature (K) at a pressure of 1 atm using B3LYP/def2-TZVP + ECP.

increases linearly with the increase of temperature. However, ΔG decreases with increasing pressure at the temperature of 298 K although the change is small (Figure S6).

3.4. DFT Gauging. In previous studies, it was found that the structural factor plays a minor role in the single point energy (SPE) calculations, and reaction energy prediction is quite challenging for DFT methods. SPE calculations on the structures obtained at B3LYP/def2-TZVP + ECP were performed by using 13 density functionals (Table 2),⁶³⁻⁷⁷ and

Table 2. List of Density Functionals Used^a

	HF-exchange (%)	References
Pure Functionals		
PBE	0	62
tHCTH	0	63
M06L	0	64
B97D	0	65
M11L	0	66
MN15L	0	67
Hybrid Functionals		
TPSSh	10	68
tHCTHhyb	15	63
B3LYP	20	69-72
X3LYP	21.8	73
BMK	42	74
BH&HLYP	50	75
wB97	100	76

"The color codes are as follows: (a) pure functionals (gray) and (b) hybrid functionals (yellow).

the def2-QZVPP + ECP basis set was used. Table 3 displays the energy differences of the two spin states and the apparent barriers as computed by the 13 methods listed in Table 2. One can see that all these methods predict that the quintet state is the ground state of Ta_3^- except for M11 and most of the 13 methods could yield similar energy differences between the singlet or triplet and quintet states. Most hybrid functionals give higher results, while pure functionals give lower ones. In general, the apparent barriers increase with the increasing amount of Hartree–Fock (HF)-exchange. The highest value is twice as high as the lowest value, and some are even nearly 5 times higher.

Table 3. Apparent Barrier ΔE (kJ mol⁻¹) for the Transition States Obtained by Various Methods at the def2-QZVPP + ECP Level

³ Ta ₃	³ Ta ₃ ⁻ ¹ Ta ₃ ⁻		³ TS1		³ TS2		
M11L	-14	BH&HLYP	1 0	PBE	-156	BMK	-236
tHCTH	4	M06L	21	TPSSh	-155	TPSSh	-235
BH&HLYP	7	M15L	22	M06L	-151	M06L	-218
PBE	10	B3LYP	22	M11L	-147	PBE	-216
M06L	10	BMK	23	BMK	-141	M11L	-204
M15L	10	X3LYP	23	M15L	-127	M15L	-202
B97D	11	wB97	24	tHCTHhyb	-125	tHCTHhyb	-188
TPSSh	13	tHCTH	26	tHCTH	-113	wB97	-176
BMK	13	PBE	26	X3LYP	-103	X3LYP	-168
tHCTHhyb	13	TPSSh	27	B3LYP	-100	B3LYP	-163
B3LYP	14	tHCTHhyb	30	B97D	-83	tHCTH	-160
X3LYP	15	B97D	32	BH&HLYP	-75	BH&HLYP	-145
wB97	27	M11L	50	wB97	-72	B97D	-129
³ TS3							
³ TS3		³ TS4	1	³ TS5		³ TS	6
³ TS3 PBE	-89	³ TS4 PBE	1 -143	³ TS5 BMK	-203	³ TS TPSSh	6 -119
³ TS3 PBE M06L	-89 -80	³ TS4 PBE <mark>TPSSh</mark>	1 -143 -143	³ TS5 BMK TPSSh	-203 -185	³ TS TPSSh BMK	6 -119 -112
³ TS3 PBE M06L TPSSh	-89 -80 -77	³ TS4 PBE TPSSh M06L	-143 -143 -138	³ TS5 BMK TPSSh M11L	-203 -185 -172	³ TS TPSSh BMK PBE	6 -119 -112 -105
³ TS3 PBE M06L TPSSh tHCTH	-89 -80 -77 -68	³ TS4 PBE TPSSh M06L BMK	-143 -143 -138 -138	³ TS5 BMK TPSSh M11L PBE	-203 -185 -172 -163	³ TS TPSSh BMK PBE M06L	6 -119 -112 -105 -100
³ TS3 PBE M06L TPSSh tHCTH M15L	-89 -80 -77 -68 -59	³ TS4 PBE TPSSh M06L BMK M15L	-143 -143 -138 -138 -138 -127	³ TS5 BMK TPSSh M11L PBE M15L	-203 -185 -172 -163 -161	³ TS TPSSh BMK PBE M06L M15L	6 -119 -112 -105 -100 -91
³ TS3 PBE M06L TPSSh tHCTH M15L tHCTHhyb	-89 -80 -77 -68 -59 -58	³ TS4 PBE TPSSh M06L BMK M15L M11L	-143 -143 -138 -138 -127 -114	³ TS5 BMK TPSSh M11L PBE M15L wB97	-203 -185 -172 -163 -161 -158	³ TS TPSSh BMK PBE M06L M15L tHCTHhyb	6 -119 -112 -105 -100 -91 -75
³ TS3 PBE M06L TPSSh tHCTH M15L tHCTHhyb B97D	-89 -80 -77 -68 -59 -58 -58 -52	³ TS4 PBE TPSSh M06L BMK M15L M11L tHCTHhyb	-143 -143 -138 -138 -138 -127 -114 -113	³ TS5 BMK TPSSh M11L PBE M15L wB97 M06L	-203 -185 -172 -163 -161 -158 -145	³ TS TPSSh BMK PBE M06L M15L tHCTHhyb M11L	6 -119 -112 -105 -100 -91 -75 -71
³ TS3 PBE M06L TPSSh tHCTH M15L tHCTHhyb B97D M11L	-89 -80 -77 -68 -59 -58 -52 -52	³ TS4 PBE TPSSh M06L BMK M15L M11L tHCTHhyb tHCTH	-143 -143 -138 -138 -127 -114 -113 -108	³ TS5 BMK TPSSh M11L PBE M15L wB97 M06L tHCTHhyb	-203 -185 -172 -163 -161 -158 -145 -137	³ TS TPSSh BMK PBE M06L M15L tHCTHhyb M11L tHCTH	6 -119 -112 -105 -100 -91 -75 -71 -64
³ TS3 PBE M06L TPSSh tHCTH M15L tHCTHhyb B97D M11L X3LYP	-89 -80 -777 -68 -59 -58 -52 -52 -52 -52 -49	³ TS4 PBE TPSSh M06L BMK M15L M11L tHCTHhyb tHCTH X3LYP	-143 -143 -138 -138 -127 -114 -113 -108 -93	³ TS5 BMK TPSSh M11L PBE M15L wB97 M06L tHCTHhyb BH&HLYP	-203 -185 -172 -163 -161 -158 -145 -137 -137	³ TS TPSSh BMK PBE M06L M15L tHCTHhyb M11L tHCTH X3LYP	6 -119 -112 -105 -100 -91 -75 -71 -64 -57
³ TS3 PBE M06L TPSSh tHCTH M15L tHCTHhyb B97D M11L X3LYP B3LYP	-89 -80 -77 -68 -59 -58 -52 -52 -52 -49 -48	³ TS4 PBE TPSSh M06L BMK M15L M11L tHCTHhyb tHCTH X3LYP B3LYP	-143 -143 -138 -138 -127 -114 -113 -108 -93 -90	³ TSE BMK TPSSh M11L PBE M15L wB97 M06L tHCTHhyb BH&HLYP X3LYP	-203 -185 -172 -163 -161 -158 -145 -137 -137 -125	³ TS TPSSh BMK PBE M06L M15L tHCTHhyb M11L tHCTH X3LYP B3LYP	6 -119 -112 -105 -100 -91 -75 -71 -64 -57 -54
³ TS3 PBE M06L TPSSh tHCTH M15L tHCTHhyb B97D M11L X3LYP B3LYP BMK	-89 -80 -77 -68 -59 -58 -52 -52 -52 -52 -49 -48 -39	³ TS4 PBE TPSSh M06L BMK M15L M11L tHCTHhyb tHCTH X3LYP B3LYP B97D	-143 -143 -138 -138 -138 -127 -114 -113 -108 -93 -90 -80	³ TSE BMK TPSSh M11L PBE M15L wB97 M06L tHCTHhyb BH&HLYP X3LYP B3LYP	-203 -185 -172 -163 -161 -158 -145 -137 -137 -125 -120	³ TS TPSSh BMK PBE M06L M15L tHCTHhyb M11L tHCTH X3LYP B3LYP BH&HLYP	6 -119 -112 -105 -100 -91 -75 -71 -64 -57 -54 -54
³ TS3 PBE M06L TPSSh tHCTH M15L tHCTHhyb B97D M11L X3LYP B3LYP BMK BH&HLYP	-89 -80 -77 -68 -59 -58 -52 -52 -52 -49 -48 -39 -23	³ TS4 PBE TPSSh M06L BMK M15L M11L tHCTHhyb tHCTH X3LYP B3LYP B97D BH&HLYP	-143 -143 -138 -138 -127 -114 -113 -108 -93 -90 -80 -75	³ TSE BMK TPSSh M11L PBE M15L wB97 M06L tHCTHhyb BH&HLYP X3LYP B3LYP tHCTH	-203 -185 -172 -163 -161 -158 -145 -137 -137 -125 -120 -115	³ TS TPSSh BMK PBE M06L M15L tHCTHhyb M11L tHCTH X3LYP B3LYP BH&HLYP B97D	6 -119 -112 -105 -100 -91 -75 -71 -64 -57 -54 -54 -45 -40

The functional with an HF-exchange percentage of about 20% such as B3LYP gives more moderate results.

4. CONCLUSIONS

Detailed mechanisms of Ta_3^- and $Ta_3N_2^-$ clusters to activate N_2 have been explored with DFT. Thermodynamic analysis shows that Ta_3^- and $Ta_3N_2^-$ can adsorb N_2 at room temperature and cleave $N \equiv N$, and Ta_3^- has higher activity than Ta_2^+ , Ta_4^+ , and Ta_6^+/N_2 couplings to cleave $N \equiv N$.^{16,35,46} AEAS is operated significantly on this small cluster Ta_3^- . From the functionals selected in this paper, for the time being, the density functional with an HF percentage of 20% might be used as a suitable choice for the study of such anion transition-metal systems. In addition, in the rational design of the catalyst, increasing the energy of the π -donor orbital may be a constructive strategy to reduce the effective cracking of $N \equiv N$.

Nitrogen atoms or N_2 molecules' exchange in the $Ta_3N_2^{-}/N_2$ scenarios are revealed following the MVK mechanism. This constitutes a rare example of complete nitrogen balance during cluster-mediated gas phase activation and is of great significance in the development of N_2 fixation as well as activation catalysts.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acsomega.2c02138.

Simplified simplified potential energy surface and key structures including selected geometric parameters for the reactions of Ta_3^- with N_2 at the B3LYP/def2-TZVP + ECP level of theory; all structures and energies calculated for the reactions of $Ta_3N_2^-$ with N_2 at the B3LYP/def2-TZVP + ECP level of theory; schematic orbital diagrams

based on a frontier orbital analysis; IR spectra as a function of wavelength at the B3LYP/def2-TZVP + ECP level; and change of relative Gibbs free energy for ${}^{3}TS1$ along the pressure at a temperature of 298 K using B3LYP/def2-TZVP + ECP(PDF)

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Notes

The authors declare no competing financial interest.

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