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# Experimental study of hemodynamics in the circle of willis

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## Abstract

**Background:** The Circle of Willis (CoW) is an important collateral pathway of the cerebral blood flow. An experimental study of the cerebral blood flow (CBF) distribution in different anatomical variations may help to a better understanding of the collateral mechanism of the CoW.

**Methods:** An *in-vitro* test rig was developed to simulate the physiological cerebral blood flow in the CoW. Ten anatomical variations were considered in this study, include a set of different degrees of stenosis in L-ICA and L-ICA occlusion coexist with common anatomical variations. Volume flow rates of efferent arteries and pressure signals at the end of communicating arteries of each case were recorded. Physiological pressure waveforms were applied as inlet boundary condition.

**Results:** In the development of L-ICA stenosis, the total CBF decreases with the increase of stenosis degree. The blood supply of ipsilateral middle cerebral artery (MCA) was affected most by the stenosis of L-ICA. Anterior communicating artery (ACoA) and ipsilateral posterior communicating artery (PCoA) function as important collateral pathways of cerebral collateral circulation when unilateral stenosis occurred. The blood supply of anterior cerebral circulation was compensated by the posterior cerebral circulation through ipsilateral PCoA when L-ICA stenosis degree is greater than 40% and the affected side was compensated immediately by the unaffected side through ACoA. Blood flow of the anterior circulation and the total CBF reached the minimum among all cases studied when L-ICA occlusion coexist with the absence of PCoA.

**Conclusion:** The results demonstrated the flow distribution patterns of the CoW under anatomical variations and clarified the collateral mechanism of the CoW. The flow ACoA is the most sensitive indexes to the morphology change of ipsilateral ICA. The relative independence of the circulation in anterior and posterior sections of the CoW is not broken and the function of ipsilateral PCoA is not activated until a severe stenosis of unilateral ICA occurs. PCoA is the most important collateral pathway of the collateral circulation and the missing of PCoA has the highest risk of stroke when the ipsilateral ICA has severe stenosis. These findings may provide the basis for future therapeutic and diagnosis applications.

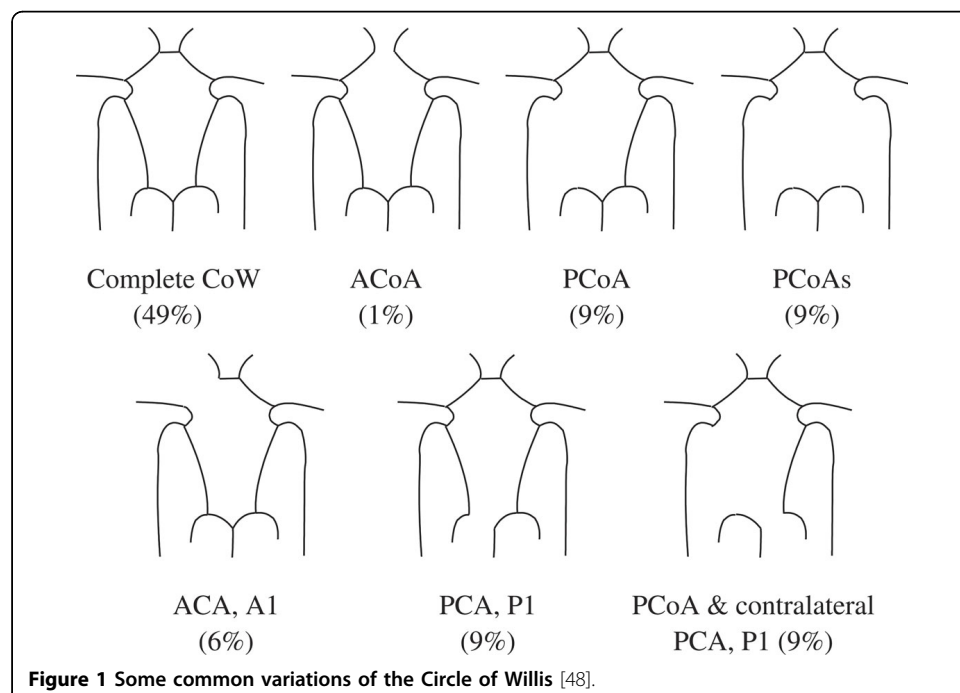
## Background

The Circle of Willis (CoW) is a ring like artery structure located at the bottom of brain. This structure provides important collateral circulation paths to maintain the sufficient blood supply, especially when stenosis or surgical clamping of the cerebral arteries happens. These collaterals consist of cross-flow through the anterior communicating artery toward the ipsilateral sphere of the ICA lesion, posterior to anterior flow through the ipsilateral posterior communicating artery, or both these systems [1-4].

Unfortunately, congenital incompleteness of CoW, such as the lack of anterior communicating artery, unilateral or bilateral PCoA, is found in 50%-60% of the population [5-7]. Other anatomical variations, including fused vessels, string-like vessels and the presence of extra vessels, are also not uncommon (Figure 1)[8]. Such variations undermine the compensational capability of the artery, and can cause undesirable clinical consequences, including ischemia stroke and transient ischemia attack (TIA). When either anatomical variations coexist with ICA stenosis or surgical clamping, the risk would be even higher. Therefore, it is important to be able to assess the blood distribution and collateral flow patterns of the CoW under various anatomical and pathological situations to help understanding the mechanism of stroke, planning the clinical surgery and diagnosis of early stage stroke.

In the literature, there are many papers proposing various methods for identifying the collateral flow patterns in complete and incomplete CoW. Clinically, the using of Transcranial Doppler (TCD) [9-20], Magnetic Resonance Angiography (MRA) [13,15,17,19,21-26] and Computed Tomography Angiography (CTA)[22,27-29] provide the *in-vivo* perspective of the role of the CoW in the collateral flow in anatomical variations. Numerically, one-dimensional [30-36], two-dimensional [37,38] and three-dimensional [31,34,39-43] models of the CoW were developed, flows in the CoW with common anatomical variations were investigated.

In contrast to a host of clinical and numerical studies, however, only limited *in-vitro* experimental studies were reported in open literature. Cieslicki et al [44] carried out *in-vitro* investigation of flow distribution in the CoW under four extreme cases, including complete CoW, unilateral ICA occlusion, complete occlusion of the vertebral-basilar system and bilateral ICA occlusion. Fahy et al [45] observed the flow distribution in three different patient specific model of CoW and assessed the risk factor brought by anatomical variations, including missing of unilateral PCoA, unilateral pre-communicating part of the



posterior cerebral artery, unilateral pre-communicating part of the anterior cerebral artery, bilateral PCoAs. In addition to limited quantity, there is a lack of *in-vitro* investigation that reveals the flow distribution in the development of ICA stenosis and ICA occlusion coexist with anatomical variations.

Moreover, details of the collateral mechanism of complete circle and incomplete circle are remaining debatable. Conflicting results have been reported on the flow patterns in the communicating arteries and importance of the collateral pathways. For the complete CoW, some *in-vitro* [46] and *in-vivo* [17] studies mentioned there are no flow across ACoA in a complete CoW, this phenomenon was also supported by numerical simulations [32,33,47]; Other numerical [48,49] and *in-vitro* [45] studies, in contrast, suggested flow across ACoA observed in complete circle of Willis under symmetrical boundary conditions. When unilateral ICA stenosis or occlusion occurred, Hartamp et al.[50], Miralles et al.[51] and Hoksbergen et al. [16] concluded that ACoA plays a more important role than PCoA in patients with severe ICA stenosis; Results from other studies suggested the fetal type or missing of ipsilateral PCoA is the only risk factor for ischemic cerebral symbols [4,38,51].

Motivated by the lacking of extensive *in-vitro* experimental studies and the conflicting research findings, an *in-vitro* experimental study focus on the collateral flow patterns in the CoW was carried out. A series of different degree of stenosis in unilateral ICA and unilateral ICA occlusion coexist with anatomical variations were simulated in this study. The CBF distributions in efferent arteries, cross flow in communicating arteries and collateral circulation mechanism of the CoW were investigated.

## Methods

### Model preparation

In previous studies, various techniques were used to measure the geometry of the CoW, including CTA imaging, MRI and direct measure of cerebral vessels. Due to individual differences, the dimensions of each artery segment are varied from case to case. In this study, average length and diameter from previous studies were used in this study to achieve a universal model [33,36,44,47,52]. The dimensions of each segment are listed in Table 1 and a physical model based on these dimensions was constructed. To simplify the model, each vessel is represented by a single silicon tube of constant radius. This simplification is acceptable because the length of every segment is relatively short and the conicity index is relatively small at cerebral artery site.

To simulate the different degrees of ICA stenosis, a set of connectors with different flow tunnel diameter was prepared. All connectors were made by copper cylinders of a length of 20 mm and an outer diameter of 4.5 mm. Flow tunnels with different diameters were drilled at the centre of the cross section along the axial direction to simulate different degrees of stenosis of ICA. The degree of stenosis is defined as the ratio of inner diameter of stenosed artery over original inner diameter. L-ICA occlusion was simulated by clamping the tube using a hemostat.

### Physiological flow system

The schematic diagram of the patented (ZL 200910021375.5) test rig is shown in Figure 2. A linear actuator (LMS 50, PBA System Pte. Ltd., Singapore) controlled by a programmable servo (Cornet COR 5/230, Elmo Motion Control Ltd., Israel) was used to drive the piston to generate pulsatile pressure waveforms. Function as mitral valve and aortic valve to

**Table 1 Diameters and length of vessels**

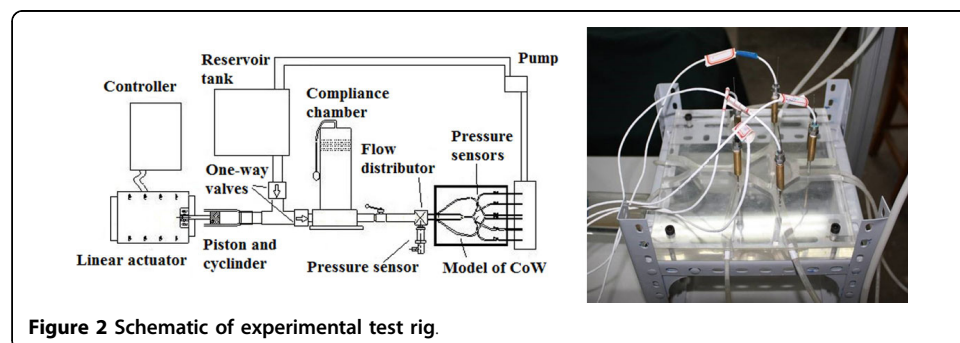
	Segment Name	Diameter (mm)	Length (mm)
ACA-A1	Proximal Anterior Cerebral Artery	2.5	20
ACA-A2	Distal Anterior Cerebral Artery	3.0	250
ACoA	Anterior Communicating Artery	2.0	3
BA	Basilar Artery	5.0	30
ICA	Internal Carotid Artery	4.5	250
PCA	Posterior Cerebral Artery	3.0	250
PCoA	Posterior Communicating Artery	1.8	20
VA	Vertebral Artery	3.0	250

prevent back flow, two one-way valves were connected to reservoir tank and compliance chamber, respectively. The effect of artery compliance was simulated by imposing an air chamber which air volume is adjustable. A flow distributor after the compliance chamber separated the flow into four branches and connected to the four afferent arteries of the CoW model.

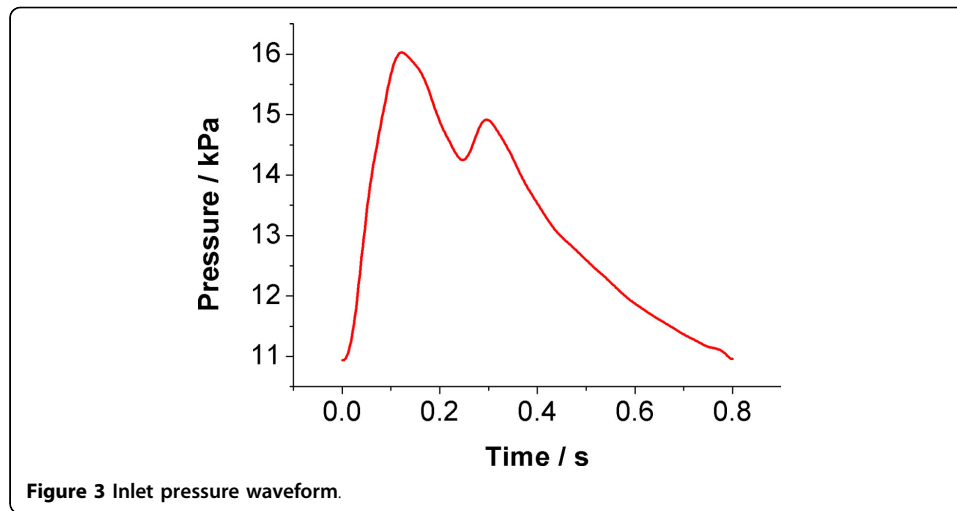
A physiological pulsatile pressure waveform for the bilateral ICA and VA were applied as inlet boundary condition (Figure 3). The systolic pressure, diastolic pressure and average pressure are 16.1 kPa (120.7 mmHg), 10.97 kPa (82 mmHg) and 12.7 kPa (95 mmHg), respectively [44,45,53]. The inlet pressure was measured by using dynamic pressure transducer (ATM231, Sensoren Transmitter Systeme GmbH, Sindelfingen, Germany). Six micro pressure transducers (XCQ-062, Kulite Semiconductor Products Inc., Ridgefield, NJ, USA) were installed at six bifurcation sites of the model, include the the bifurcation at the junction of bilateral PCA and PCoA, the bifurcation at the junction of bilateral MCA and PCoA and the bifurcation at the junction of bilateral ACA and ACoA. Pressure signals at these sites were recorded by a data acquisition system (Vision XP, LDS Test and Measurement GmbH, Ismaning, Germany).

Adjustable resistors were connected to the end of efferent arteries. Six beakers were placed at ends of the efferent arteries, and volume of fluid flows out from each efferent artery was measured periodically, to calculate the total mean volume flow rates and the flow rate of each efferent artery. The fluid collecting system simultaneously collected outflows from the CoW and distributes the fluid into six beakers so that the mean flow rate can be measured. The total flow rate of the complete CoW was set at physiological level of 760 ml·min<sup>-1</sup>, and the flow rate ratio between VAs and ICAs was 30:70. The cardiac cycle was set to 0.8 s (75 beats·min<sup>-1</sup>).

All devices were turned on 30 minutes before data collection for warm up and reach a stable condition. Measurements were collected for 100 consecutive cardiac cycles,



**Figure 2 Schematic of experimental test rig.**



and were repeated three times for each cases mentioned above. In the complete CoW, the pressure waveforms measured over 100 cycles in L-ICA was within 0.1% for peak systolic pressure and peak diastolic pressure respectively, shows an excellent repeatability between cycles. The average pressure difference between L-ICA and R-ICA of the complete CoW at systolic peak is less than 0.8%.

#### Working fluid

Blood is a non-Newtonian multiphase fluid with shear thinning properties. However, most researchers have considered blood as a Newtonian fluid except when they study the blood flow in medium to large arteries [54,55]. In this study, blood was assumed as Newtonian fluid. The working fluid applied here is a 40% aqueous solution of glycerin (volume ratio), the viscosity and density of which is 3.5 mPa·s (DV-III+, Brookfield, USA) and 1056 kg·m<sup>-3</sup>, respectively.

#### Experimental methods

To investigate the blood flow distribution in the CoW under different ICA stenosis degrees, a series of pathological variations were considered, including:

- 1) Complete circle;
- 2) Different stenosis degrees of L-ICA (40%, 50%, 60%, 75%, and 87.5%) and L-ICA complete occlusion;
- 3) L-ICA occlusion coexist with the absence of communication arteries (R-PCoA, ACoA and L-PCoA).

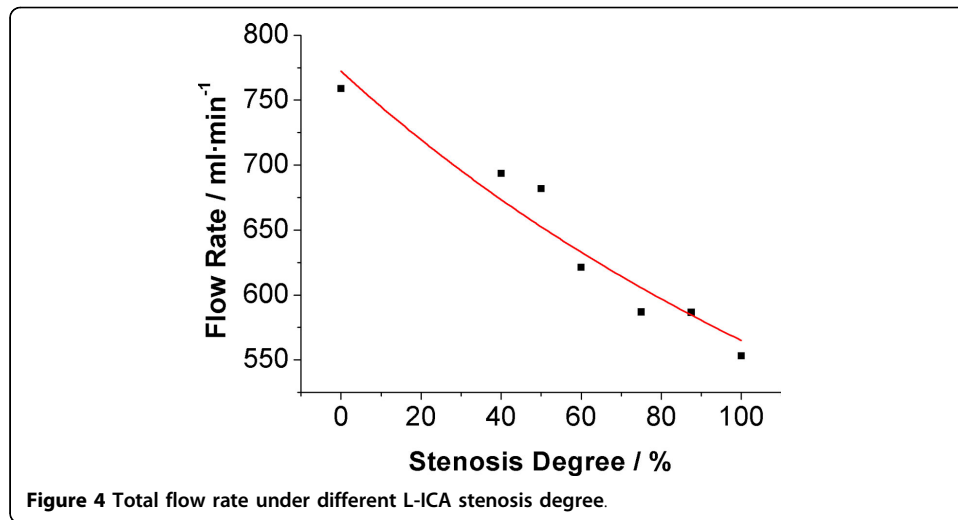
Flow rates of above conditions were recorded and analysed.

To investigate the collateral mechanism of the CoW, pressure at both ends of each communicating artery (ACoA, L-PCoA and R-PCoA) under different L-ICA stenosis degrees was recorded, and this also provide indication of the flow direction.

#### Results

##### Stenosis at L-ICA versus volume flow rate

The total volume flow rates of CoW under different L-ICA stenosis degrees are illustrated in Figure 4. Detailed data were shown in Table 2. When a stenosis was introduced to the L-ICA, the total flow rate was directly affected. As the stenosis degree



increased, the flow rate decreased continuously. When L-ICA was completely occluded, the total flow rate decreased by about 205 ml·min<sup>-1</sup>. This is about 27% of the normal flow rate. In complete CoW, the distribution of flow to anterior, middle and posterior cerebral artery was accounts for 21.19%, 51.49% and 27.27% of total flow rate, respectively.

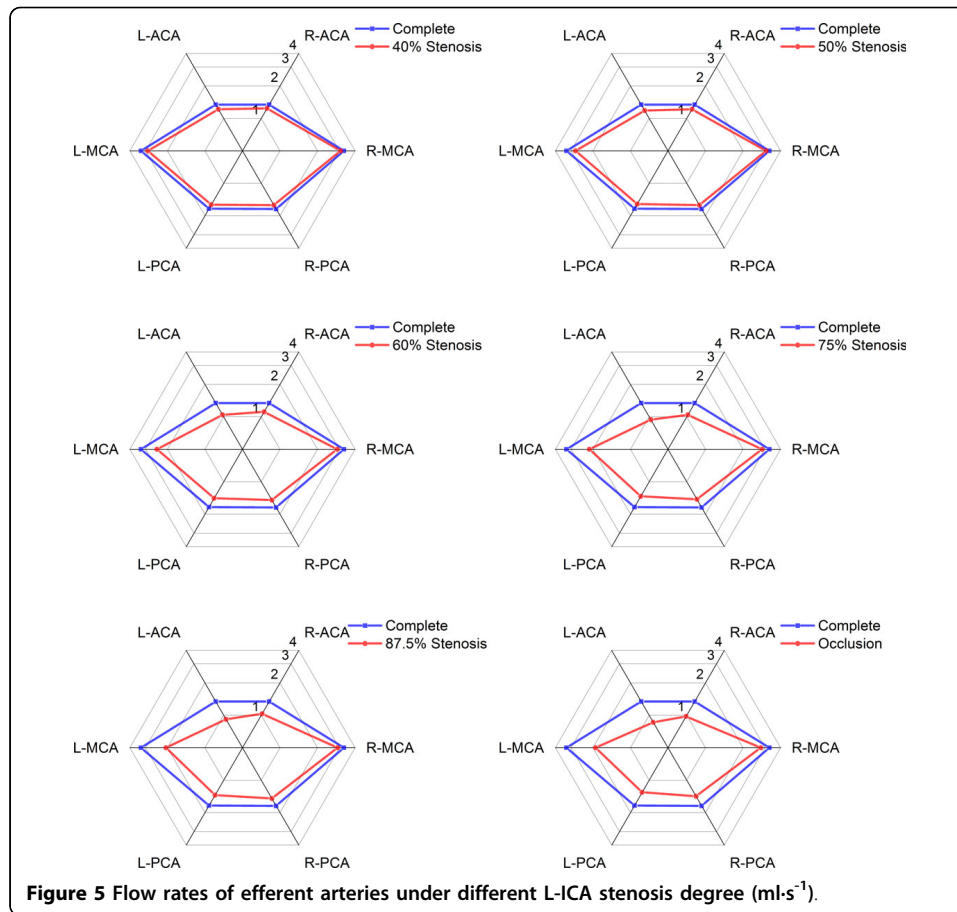
Figure 5 is a schematic illustrating the change of flow rates in efferent arteries (ACA, MCA and PCA) under different L-ICA stenosis degrees. The specific flow rates of efferent arteries are shown in Table 3.

There was an immediate reduction in blood flow through all of the efferent arteries when stenosis occurred, and the flow rates of all efferent arteries were decreased with the increasing of the stenosis degree of L-ICA. The three efferent arteries ipsilateral to the stenosis show the greatest relative reduction. When L-ICA was occluded, flow rate in the affected side of the ACA, MCA and PCA was 36.0%, 40.7% and 24.8% lower than normal conditions, respectively. The flow rate in the healthy side of the ACA, MCA and PCA was only 27.3%, 13.3% and 17.3% lower than normal conditions, respectively. This observation suggests that the L-MCA is affected most by the stenosis of L-ICA.

Under mild to medium degree of stenosis (<50%), the volume flow rates in the ACA and PCA were decreased synchronously, and no obvious differences between bilateral branches were observed. When the stenosis degree is greater than 75%, the result shows that the flow rates in bilateral ACA and PCA to become off-balance. This is an

**Table 2** Total flow rates under different stenosis degree of L-ICA

Stenosis degree (%)	Total flow rate (ml·min <sup>-1</sup> )	Percentage change (%)
0	758.93	0
40	693.58	-8.61
50	681.89	-10.15
60	621.32	-18.13
75	586.92	-22.66
87.5	585.56	-22.84
100	553.21	-27.10



**Figure 5** Flow rates of efferent arteries under different L-ICA stenosis degree (ml·s<sup>-1</sup>).

indication that the symmetry of the CoW is compromised. Compare with the ACA and PCA, the MCA is more sensitive to the morphology change of the ICA, see Table 3 and 4. The imbalanced flow between the bilateral MCA that appeared under mild stenosis and the difference in flow rates between the L-MCA and R-MCA increases continuously with the degree of stenosis.

The percentage change in flow rate of efferent arteries under different stenosis degree in Table 4 consistently shows the highest percentage change occurring in the L-MAC.

#### Flow direction in communicating arteries

To investigate the flow direction in communicating arteries, pressure signals were recorded at both ends of each communicating artery. Figure 6 shows the pressure difference between the upper end and lower end of L-PCoA and R-PCoA. Here, the upper end of PCoA is defined as the junction with MCA, and the lower end is the junction with PCA; the pressure difference of PCoA is the pressure at the upper end minus the pressure at the lower end. When no stenosis occurred, the pressure difference at both ends of the PCoA is near zero. Blood from VAs and ICAs just supply their own perfusion area and there is no blood flow through the PCoA. The pressure difference at the L-PCoA is found decreased sharply when the L-ICA stenosis degree is greater than 40%. This phenomenon can be explained as blood flow was drawing away

**Table 3 Flow rates of efferent arteries under different stenosis degree of L-ICA**

Stenosis degree (%)	Flow rate in efferent arteries (ml·s <sup>-1</sup> )					
	R-ACA	R-MCA	R-PCA	L-PCA	L-MCA	L-ACA
0	1.34	3.26	1.73	1.72	3.26	1.34
40	1.24	3.06	1.59	1.58	2.87	1.22
50	1.22	3.06	1.59	1.56	2.75	1.18
60	1.11	2.88	1.48	1.42	2.42	1.04
75	1.04	2.84	1.46	1.36	2.13	0.94
87.5	1.03	2.90	1.48	1.38	2.05	0.92
100	0.97	2.78	1.41	1.30	1.90	0.86

from the PCA, and flows from posterior to anterior. In contrast, contralateral PCoA is virtually unaffected, the pressure difference at R-PCoA increases slightly during the increase of L-ICA stenosis rate.

Figure 7 shows the pressure difference of ACoA. This is the pressure at the right end of the ACoA minus the pressure at the left end of the ACoA. Under normal conditions, the pressure difference is near zero, which means no blood flow through ACoA. As the increase of L-ICA stenosis increases, the pressure difference also increases, the blood flow through ACoA from right to left.

#### Flow distribution versus anatomical variations

In addition to 1) the complete CoW and 2) L-ICA occlusion, three anatomical variations were also investigated:

- 3) L-ICA occlusion coexist with absence of contralateral PCoA,
- 4) L-ICA occlusion coexist with absence of ACoA,
- 5) L-ICA occlusion coexist with absence of ipsilateral PCoA.

The total volume flow rate of case (3) to (5) was 31.3%, 31.3%, 31.4% lower than normal flow rate (case (1)) respectively, and about 7.1% lower than in case (2) where only occlusion occurred at the L-ICA (Figure 8).

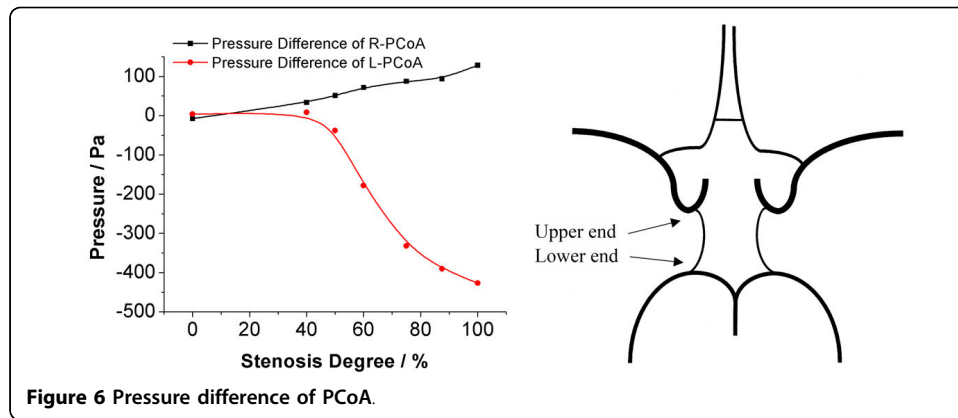
The volume flow rates of efferent arteries are shown in Figure 9, detailed data are listed in Table 5. When contralateral PCoA absent, no obvious change of flow rate in efferent arteries were observed except R-PCA, which decreased 10% compare with case (2).

Absence of ACoA coexist with occlusion of L-ICA is the most critical situation to ipsilateral ACA among all cases investigated. The flow rate in ACA ipsilateral to

**Table 4 Percentage change in flow rates of efferent arteries under different stenosis degree of L-ICA**

Stenosis degree (%)	Percentage change in flow rate (%)					
	R-ACA	R-MCA	R-PCA	L-PCA	L-MCA	L-ACA
0	0.00	0.00	0.00	0.00	0.00	0.00
40	-7.69	-5.98	-7.95	-8.00	-11.97	-9.39
50	-9.39	-5.98	-7.95	-9.33	-15.49	-11.96
60	-17.09	-11.62	-14.57	-17.33	-25.70	-22.22
75	-22.22	-12.68	-15.89	-20.66	-34.51	-29.91
87.5	-23.07	-10.92	-14.57	-20.00	-36.97	-31.61
100	-27.34	-14.79	-18.55	-24.67	-41.55	-35.89





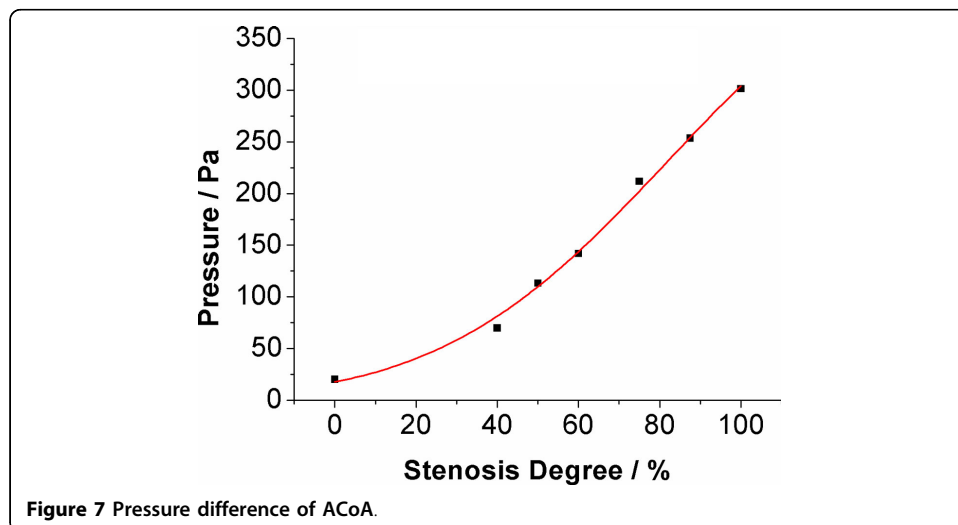
**Figure 6** Pressure difference of PCoA.

L-ICA is 28.1% lower than that in case (2). The absence of ACoA also decreasing the flow through ipsilateral MCA, which is 21.5% lower compare with case (2). Meanwhile, flow rate of MCA and PCA contralateral to L-ICA have no significant change compare with case (2). Flow rate in contralateral ACA increased 18.6% compare with case (2) and only 14.18% lower than complete CoW (case (1)).

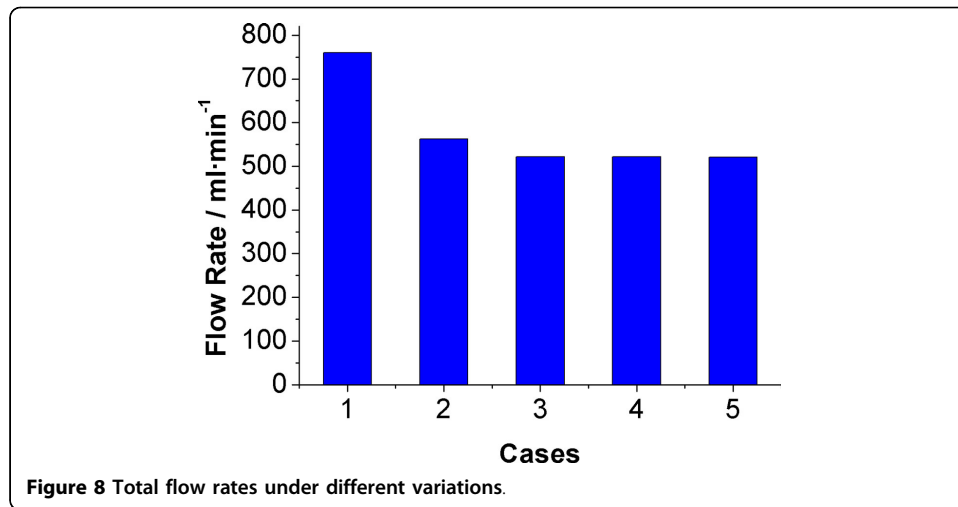
In case (5), total CBF, flow rate in L-MCA and flow rate in R-ACA reached their lowest value compare with that of all cases. The flow rate in L-MCA and R-ACA is 23.43% and 9.28% lower than case (2), respectively. Flow rates in bilateral PCA are highest among case (2) to (5).

## Discussion

*In-vitro* experimental study were carried out in present study to investigate the CBF distributions in efferent arteries, cross flow in communicating arteries and collateral circulation mechanism of the CoW. There are many factors that can influence the distributions of flow rates in the CoW. In the present study, neither the auto-regulation mechanism of peripheral arterial beds nor the vessel elastic was considered. As mentioned, the aim of this study is not to create a model of the CoW that can simulate all physiological factors of a real circulation system, but simply to investigate the impact



**Figure 7** Pressure difference of ACoA.

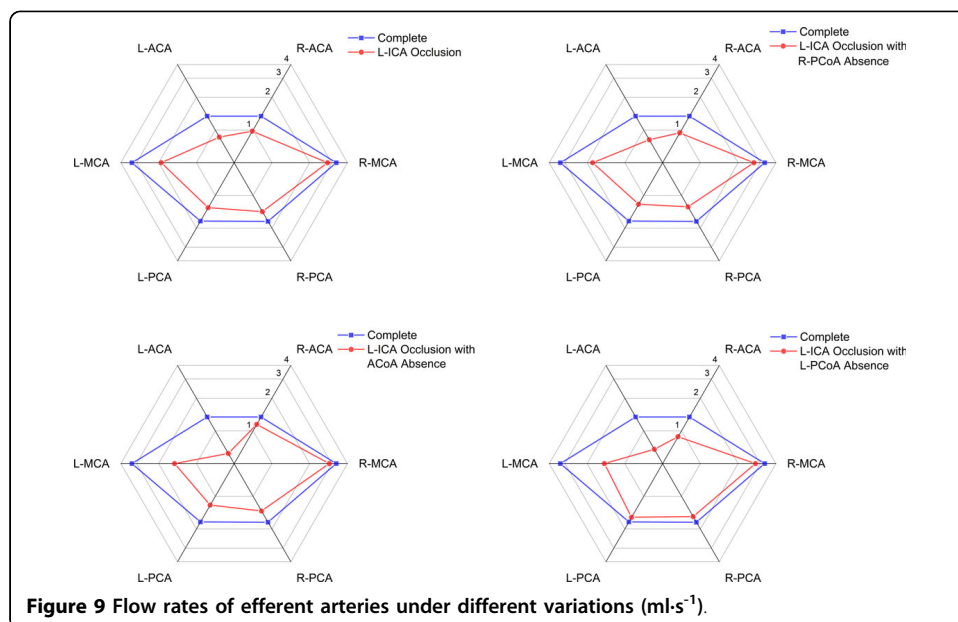


of structural variation on the flow distribution in the CoW and the basic collateral circulation mechanism.

In developing the model of the CoW, validation is of the utmost importance if the model results are to be trusted. Due to the lack of clinical data that cover all cases studied in this paper, a comparison based on the complete CoW was considered. The flow rates of efferent arteries were compared between this study and previous clinical measurements.

Table 6 listed the results from phase-contrast MRI measurements.

The flow rates in ICAs and ACAs agree well with *in-vivo* measurements data. The flow rates in MCAs, BA and most noticeably the PCAs, however, appear to slightly larger than *in-vivo* measurements. According to the simplify of current model, this phenomenon could be explained as the absence of branch arteries of ICAs and BA, include the ophthalmic and anterior choroidal arteries, may cause the raise of flow



**Table 5 Flow rates of efferent arteries under the absence of communicating arteries**

Case	Flow rate in efferent arteries (ml·s <sup>-1</sup> )					
	R-ACA	R-MCA	R-PCA	L-PCA	L-MCA	L-ACA
1	1.34	3.26	1.73	1.72	3.26	1.34
2	0.97	2.78	1.41	1.30	1.90	0.86
3	0.94	2.67	1.27	1.20	1.80	0.81
4	1.15	2.87	1.36	1.20	1.49	0.62
5	0.88	2.75	1.54	1.56	1.45	0.68

through MCAs and PCAs [47]. Further comparison was made between current results and previous numerical model [47] and *in-vitro* study [44], specific data were listed in Table 7.

These data presented in previous *in-vivo*, numerical and *in-vitro* studies are useful validations to show current *in-vitro* results are within acceptable physiological ranges. Therefore, the results in the study were convincing to provide information of CBF distribution and collateral circulation mechanism under such situations.

Notable decrease of flow rate in ACA and MCA was observed in the results, which indicate that the anterior circulation was affected most by ICA stenosis. When the stenosis degree of unilateral ICA increased from 0% to 100%, the flow rate in ipsilateral ACA and MCA decreased 35.89% and 41.55% respectively. These values can be validated in the numerical study of Zhang et al [32]. Flow rates in PCA is less affected by unilateral ICA stenosis. This may due to the blood flow of posterior circulation are mainly provided by VA-BA system.

The pressure signal provides more information about the collateral compensation mechanism of the CoW. In complete CoW, the pressure difference between both ends of ACoA is almost zero, which indicated there is no blood flow through ACoA and the left and right circulation is relatively independent when the CoW is complete. This finding was in contrast to some numerical [48,49] and *in-vitro* [45] studies, but it was in agreement other *in-vitro* [46], *in-vivo* [17] and numerical [30,47] studies. Uni-directional cross-flows occurs simultaneously in ACoA when stenosis induced to L-ICA. The blood flows through ACoA from the healthy side of the CoW to the affected side. As PCoA, the pressure difference of both PCoAs were near zero, which suggest there are almost no flow through PCoA in the complete CoW. When stenosis in unilateral ICA occurred, the pressure signals indicate that ipsilateral PCoA provides an important

**Table 6 Comparison of flow rates of efferent arteries with previous *in-vivo* measurements**

Study	Volume flow rate (ml·s <sup>-1</sup> )		
	ACAs	MCAs	PCAs
Current model (Complete CoW)	2.68	6.52	3.45
Enzmann et al. [57]	2.72 ± 0.35	3.92 ± 0.24	1.73 ± 0.14
Ooij et al. [58] <sup>1*</sup>	3.0 ± 0.80	6.2 ± 1.60	2.0 ± 0.60
Ooij et al. [58] <sup>2*</sup>	3.0 ± 0.80	4.8 ± 0.80	2.0 ± 0.60
Zhao et al. [59]	2.75 ± 0.90	4.92 ± 0.97	2.15 ± 0.47

\*The data provided in original paper was flow rates in unilateral arteries. For comparison, data presented here were doubled.

1. Results from 7T scanning, 0.8 mm resolution

2. Results from 7T scanning, 0.5 mm resolution

**Table 7 Comparison of flow rates of efferent arteries with previous numerical and in-vitro studies**

Study	Volume flow rate (ml·s <sup>-1</sup> )		
	ACAs	MCAs	PCAs
Current model (Complete CoW)	2.68	6.52	3.45
Moore et al. [47]	2.78	5.56	4.16
Cieslicki et al. [44]	3.1	4.85	3.76

collateral pathway in which the blood flow toward anterior circulation. This observation is supported by clinical TCD measurement [17]. The collateral compensation function of ipsilateral PCoA will be fully activated when the stenosis degree at L-ICA is greater than 40%. Contralateral PCoA, however, only provides limited support to the compensation blood supply as the pressure difference is very small even L-ICA was complete occlude.

The role of PCoA and ACoA in collateral circulation was further revealed when take the anatomical variations into consideration. When the L-ICA occlusion coexist with the absence of ACoA, minimum flow rate in L-ACA was observed among all cases studied. This observation indicate that ACoA is an utmost important collateral path for ACA at affected side. For the whole anterior circulation and the total CBF supply, however, PCoA ipsilateral to stenosed ICA plays a more important role than ACoA in the collateral circulation. This conclusion is based on the observation that the flow rates in anterior circulation and the total CBF supply reached their minimum value when L-ICA occlusion coexist with the absence of ipsilateral PCoA. These observations are well agreed with clinical results [56].

This study had several limitations. Some vessels of the CoW, include ophthalmic artery, choroidal arteries and superior cerebellar arteries were simplified. As discussed before, the simplification would influence the flow distribution in the CoW. Moreover, flow visualization in current model is impossible. This drawback prevent us from access more detailed flow parameters, such as flow pattern and wall shear stress, which may help us have a further understanding of the hemodynamics of the CoW under different anatomical configurations. To access the wave propagation in the CoW, the vessel elasticity also need to be considered in future work.

## Conclusions

Flow distribution patterns of the CoW under anatomical variations and the collateral mechanism of the CoW were investigated and clarified in present work. Experiment showed that PCoA is the most important collateral pathway in cerebral collateral circulation. The anatomical variation missing PCoA has the highest risk of TIA and cerebral stroke when the ipsilateral ICA has severe stenosis. In addition, the anterior circulation and posterior circulation of the CoW was found to be independent to each other until the ICA stenosis become severe. Moreover, we found that the collateral capacity of PCoA won't be fully activated until ICA stenosis degree is greater than 40%. Further more, the results indicate that the flow in ACoA might be used as a criterion of morphology change of ICA. These findings may potentially be used to enhance our understanding of the hemodynamics in the CoW and eventually lead to future therapeutic and diagnosis applications.

#### Competing interests

The authors declare that they have no competing interests.

#### Authors' contributions

GYZ carried out the experimental study, participated in the sequence alignment and drafted the manuscript. QY participated in the design of this study and sequence alignment as supervisor. JY participated in the sequence alignment. JHY participated in the design of the study and helped to draft the manuscript.

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#### Declarations

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