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Crystal structure of TiBi₂

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Black granular single crystals of monotitanium dibismuth, TiBi₂, were synthesized by slow cooling of a mixture of Bi and Ti from 693 K. The title compound is isostructural with $CuMg_2$ (orthorhombic *Fddd* symmetry). Ti atoms are located in square antiprisms of Bi atoms. The network of one type of Bi atom spirals along the *a*-axis direction while honeycomb layers of the other type of Bi atom spreading in the *ab* plane interlace one another.

1. Chemical context

TiBi₂ was first reported in the study of the Ti–Bi binary phase diagram by Vassilev (2006). Maruyama *et al.* (2013) confirmed the presence of TiBi₂ in their phase-diagram study and showed that the powder X-ray diffraction (XRD) pattern was consistent with that of a Ti–Bi film prepared by RF sputtering (Simić & Marinković, 1990). However, the crystal system, lattice parameters and structure of TiBi₂ were not reported.

In the present study, we prepared single crystals of TiBi₂ to clarify the structure. The pellet of the starting mixture maintained the original shape after heating at 693 K. The powder XRD pattern of the sample showed that a mixture of TiBi₂, Bi, and Ti had been obtained. Single crystals of TiBi₂ approximately 120 μ m in size were picked up from the fractured sample. TiBi₂ is unstable and decomposes in air. When the mixture was heated at 703 K, the obtained sample was a mixture of Bi and Ti₈Bi₉. This temperature was above the peritectic temperature of TiBi₂ (698 K) reported in the phase diagram by Maruyama *et al.* (2013).

2. Structural commentary

TiBi₂ is isotypic with CuMg₂ (Schubert & Anderko, 1951; Gingl *et al.*, 1993), NbSn₂, VSn₂, CrSn₂ (Wölpl & Jeitschko, 1994; Larsson & Lidin, 1995), and IrIn₂ (Zumdick *et al.*, 2000). TiSnSb is the only reported compound which contains Ti and crystallizes in the CuMg₂-type structure (Malaman & Steinmetz, 1979; Dashjav & Kleinke, 2003). The crystal structure of TiSb₂ adopts the CuAl₂ type, while that of TiSn₂ is not known. TiBi₂ is the first binary compound that is composed of Ti and a group 15 element and has the CuMg₂-type structure.

Fig. 1 shows the crystal structure of TiBi₂ while the coordination environments of the Ti1, Bi1, and Bi2 atoms are illustrated in Fig. 2. The Ti1 site is located in a square antiprism of Bi atoms. The Bi square antiprisms are aligned alternately along the a + b and a - b directions by sharing the square planes. Bi—Ti bond lengths in the Bi square antiprism and the Ti—Ti distance of the inter-antiprisms are 2.9382 (16)– 3.0825 (6) and 2.9546 (2) Å, respectively, which are in the



Figure 1

Crystal structure of $TiBi_2$ illustrated with Ti-centered Bi1–Bi2 square antiprisms and Bi1–Bi1 and Bi2–Bi2 bonds.

ranges reported for Ti_8Bi_9 [Bi-Ti = 2.818 (4)-3.144 (6) Å and Ti-Ti = 2.934 (6)-3.715 (5) Å; Richter & Jeitschko, 1997].

The Bi1–Bi1 bond lengths in the Bi1 spiral-like network are 3.0730 (8) Å in the *c*-axis direction and 3.4589 (4) Å in the other direction. The Bi2–Bi2 bond lengths in the Bi2 honeycomb layers in the *ab* plane are 3.4639 (8) Å in the *b*-axis direction and 3.3435 (4) Å in the other direction. The Bi–Bi bond lengths in the spiral rings and honeycomb layers in TiBi₂ are in the range of those in Bi metal (3.071 and 3.529 Å; Cucka & Barrett, 1962). The interatomic distances between the Bi atoms of the spiral network and the honey-



Figure 2

The atomic arrangement around Ti and Bi atoms in the structure of TiBi₂. Displacement ellipsoids are drawn at 99% probability. [Symmetry codes: (i) $x, -y + \frac{1}{4}, -z + \frac{1}{4}$; (ii) -x, -y, -z; (iii) $x + \frac{1}{4}, y + \frac{1}{4}, -z$; (iv) $x - \frac{3}{4}, y + \frac{1}{4}, -z$; (v) $-x - \frac{1}{4}, -y + \frac{3}{4}, z$; (vi) x, y - 1, z; (vii) $-x + \frac{3}{4}, y - \frac{1}{2}, -z + \frac{1}{4}$; (viii) $-x + \frac{3}{4}, -y + \frac{3}{4}, z$; (ix) $-x - \frac{1}{4}, y - \frac{1}{2}, -z + \frac{1}{4}$; (x) -x, -y + 1, -z; (xi) $-x, y - \frac{1}{4}, z - \frac{1}{4}$; (xii) $x, -y - \frac{1}{4}, -z + \frac{3}{4}$; (xiii) $x, y - \frac{1}{2}, z - \frac{1}{2}$; (xv) $x + \frac{1}{4}, y - \frac{1}{4}, -z + \frac{1}{2}$; (xv) $-x + \frac{3}{4}, -y + \frac{1}{4}, z - \frac{1}{2}$; (xvi) $-x, -y + \frac{1}{2}, -z + \frac{1}{2}$]

Table 1	
Experimental details.	
Crystal data	
Chemical formula	TiBi ₂
M _r	465.86
Crystal system, space group	Orthorhombic, Fddd
Temperature (K)	298
<i>a</i> , <i>b</i> , <i>c</i> (Å)	5.7654 (4), 10.3155 (6), 19.4879 (12)
$V(Å^3)$	1159.00 (13)
Z	16
Radiation type	Μο Κα
$\mu \text{ (mm}^{-1})$	123.50
Crystal size (mm)	$0.14 \times 0.09 \times 0.06$
Data collection	
Diffractometer	Bruker D8 goniometer
Absorption correction	Numerical (<i>SADABS</i> ; Bruker, 2014)
T_{\min}, T_{\max}	0.016, 0.102
No. of measured, independent and observed $[I > 2\sigma(I)]$ reflections	3881, 339, 309
R _{int}	0.048
$(\sin \theta / \lambda)_{\max} (\text{\AA}^{-1})$	0.649
Refinement	
$R[F^2 > 2\sigma(F^2)], wR(F^2), S$	0.024, 0.062, 1.31
No. of reflections	339
No. of parameters	17
$\Delta \rho_{\rm max}, \Delta \rho_{\rm min} \ ({ m e} \ { m \AA}^{-3})$	2.54, -3.80

Computer programs: Instrument Service, APEX2 and SAINT-Plus (Bruker, 2014), SHELXL2014 (Sheldrick, 2015) and VESTA (Momma & Izumi, 2011).

comb layers (Bi1-Bi2) are 3.6974(3), 3.7309(4) and 3.7546(4) Å, which are longer than the Bi-Bi bond lengths in Bi metal.

3. Synthesis and crystallization

Starting powders of Bi (1 mmol, Mitsuwa Chemicals Co., Ltd, 99.999%) and Ti (0.5 mmol, Mitsuwa Chemicals Co., Ltd, 99.99%) were weighed, mixed in an alumina mortar with a pestle and formed into a pellet by uniaxial pressing in an Ar gas-filled glove box (O_2 and $H_2O < 1$ p.p.m.). The pellet was put in a tantalum boat (Nilaco Corp., 99.95%). The boat was sealed in a stainless-steel (SUS 316) tube. The sample was heated to 693 K in an electric furnace with a heating rate of 3.5 K min⁻¹. This temperature was kept for 10 h, and then lowered to 473 K with a cooling rate of 5 K h⁻¹. After cooling to room temperature by shutting off the electrical power to the furnace, the stainless-steel tube was cut and opened in the glove box. To identify the crystalline phases, powder XRD (Cu $K\alpha$, Bruker, D2 phaser) was carried out for a portion of the sample which was ground in the alumina mortar and sealed under an Ar atmosphere in a holder with a kapton film window. The chemical compositions of TiBi2 single crystals placed on a carbon tape were determined with an electron probe microanalyzer (EPMA, JEOL, JXA-8200). Bi and TiO₂ (Japan Electronics Co., Ltd) were used as standard samples. The analyzed composition ratio of Ti:Bi in the crystals was 1.0 (1):2.0 (1). A single crystal of TiBi₂ was sealed in a glass

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capillary with Ar gas in the glove box for the single-crystal XRD experiment.

4. Refinement

Crystal data, data collection and structure refinement details are summarized in Table 1.

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Computing details

Data collection: *Instrument Service* (Bruker, 2014); cell refinement: *APEX2* (Bruker, 2014); data reduction: *SAINT-Plus* (Bruker, 2014); program(s) used to solve structure: *APEX2* (Bruker, 2014); program(s) used to refine structure: *SHELXL2014* (Sheldrick, 2015); molecular graphics: *VESTA* (Momma & Izumi, 2011).

Titanium dibismuth

Crystal data TiBi₂ $M_r = 465.86$ Orthorhombic, *Fddd* a = 5.7654 (4) Å b = 10.3155 (6) Å c = 19.4879 (12) Å V = 1159.00 (13) Å³ Z = 16F(000) = 3008

Data collection

Bruker D8 goniometer diffractometer Radiation source: micro focus sealed tube Detector resolution: 10.4167 pixels mm⁻¹ ω , φ scans Absorption correction: numerical (SADABS; Bruker, 2014) $T_{\min} = 0.016$, $T_{\max} = 0.102$

Refinement

Refinement on F^2 Least-squares matrix: full $R[F^2 > 2\sigma(F^2)] = 0.024$ $wR(F^2) = 0.062$ S = 1.31339 reflections 17 parameters 0 restraints Primary atom site location: dual $D_x = 10.679 \text{ Mg m}^{-3}$ Mo $K\alpha$ radiation, $\lambda = 0.71073 \text{ Å}$ Cell parameters from 4528 reflections $\theta = 4.2-31.4^{\circ}$ $\mu = 123.50 \text{ mm}^{-1}$ T = 298 KGranule, black $0.14 \times 0.09 \times 0.06 \text{ mm}$

3881 measured reflections 339 independent reflections 309 reflections with $I > 2\sigma(I)$ $R_{int} = 0.048$ $\theta_{max} = 27.5^{\circ}, \ \theta_{min} = 4.2^{\circ}$ $h = -7 \rightarrow 7$ $k = -13 \rightarrow 13$ $l = -25 \rightarrow 25$

Secondary atom site location: difference Fourier map $w = 1/[\sigma^2(F_o^2) + (0.0275P)^2 + 47.1241P]$ where $P = (F_o^2 + 2F_c^2)/3$ $(\Delta/\sigma)_{max} < 0.001$ $\Delta\rho_{max} = 2.54 \text{ e } \text{Å}^{-3}$ $\Delta\rho_{min} = -3.80 \text{ e } \text{Å}^{-3}$ Extinction correction: SHELXL2014 (Sheldrick, 2015), Fc*=kFc[1+0.001xFc^2\lambda^3/sin(2\theta)]^{-1/4} Extinction coefficient: 0.00038 (3)

Special details

Geometry. All esds (except the esd in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell esds are taken into account individually in the estimation of esds in distances, angles and torsion angles; correlations between esds in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell esds is used for estimating esds involving l.s. planes.

	x	у	Ζ	$U_{ m iso}$ */ $U_{ m eq}$	
Bi1	0.1250	0.1250	0.04615 (2)	0.0064 (2)	
Bi2	0.1250	0.45710 (4)	0.1250	0.0066 (2)	
Ti1	0.1250	0.1250	0.49898 (10)	0.0050 (4)	

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\mathring{A}^2)

Atomic displacement parameters $(Å^2)$

	U^{11}	U ²²	U ³³	U^{12}	U^{13}	U^{23}
Bi1	0.0035 (3)	0.0076 (3)	0.0082 (3)	0.00176 (15)	0.000	0.000
Bi2	0.0058 (3)	0.0080 (3)	0.0060 (3)	0.000	-0.00212 (15)	0.000
Ti1	0.0039 (9)	0.0060 (9)	0.0051 (8)	0.0005 (8)	0.000	0.000

Geometric parameters (Å, °)

Ti1—Bi2 ⁱ	2.9382 (16)	Bi1—Bi2 ^{xix}	3.7546 (4)
Ti1—Bi2 ⁱⁱ	2.9382 (16)	Bi1—Bi2	3.7546 (4)
Ti1—Bi2 ⁱⁱⁱ	3.0051 (16)	Bi1—Ti1 ^{xx}	3.0257 (6)
Ti1—Bi2 ^{iv}	3.0051 (16)	Bi1—Ti1 ^{xxi}	3.0257 (6)
Ti1—Bi1 ^v	3.0257 (6)	Bi1—Ti1 ^{vii}	3.0825 (6)
Ti1—Bi1 ^{vi}	3.0257 (6)	Bi1—Ti1 ⁱ	3.0825 (6)
Ti1—Bi1 ^{vii}	3.0825 (6)	Bi1—Ti1 ^{xxii}	4.9243 (16)
Ti1—Bi1 ⁱ	3.0825 (6)	Bi1—Ti1 ^{xxiii}	4.9243 (16)
Ti1—Ti1 ^{viii}	2.9546 (2)	Bi1—Ti1 ^{xxiv}	4.9348 (16)
Ti1—Ti1 ^{ix}	2.9546 (2)	Bi1—Ti1 ^{xxv}	4.9348 (16)
Bi1—Bi1 ^x	3.0730 (8)	Bi1—Ti1 ^{xxvi}	5.1110 (4)
Bi1—Bi1 ^{xi}	3.4589 (4)	Bi2—Ti1 ⁱ	2.9382 (16)
Bi1—Bi1 ^{xii}	3.4589 (4)	Bi2—Ti1 ^{xxiv}	2.9382 (16)
Bi2—Bi2 ^{xiii}	3.3435 (4)	Bi2—Ti1 ^{xxvii}	3.0051 (16)
Bi2—Bi2 ^{xiv}	3.3435 (4)	Bi2—Ti1 ^{xxviii}	3.0051 (16)
Bi2—Bi2 ^{xv}	3.4639 (8)	Bi2—Bi1 ^{xxix}	3.6974 (3)
Bi1—Bi2 ^{xiv}	3.6974 (3)	Bi2—Bi1 ^{xxx}	3.6974 (3)
Bi1—Bi2 ^{xvi}	3.6974 (3)	Bi2—Bi1 ^{xxxi}	3.6974 (3)
Bi1—Bi2 ^{xvii}	3.6974 (3)	Bi2—Bi1 ^{xxxii}	3.6974 (3)
Bi1—Bi2 ^{xiii}	3.6974 (3)	Bi2—Bi1 ^{xii}	3.7310 (4)
Bi1—Bi2 ^{xviii}	3.7309 (4)	Ti1—Bi1 ^{xxii}	4.9242 (16)
Bi1—Bi2 ^{xii}	3.7309 (4)	Ti1—Bi1 ^{xxiii}	4.9242 (16)
Ti1 ⁱ —Bi2—Bi1 ^{xxx}	100.12 (2)	Bi2 ^{xiv} —Bi1—Ti1 ^{xxiv}	36.352 (10)
Bi1 ^{xxix} —Bi2—Bi1 ^{xii}	100.174 (6)	Bi2—Bi1—Ti1 ^{xxiv}	36.426 (10)
Bi2 ^{xvi} —Bi1—Bi2 ^{xviii}	100.175 (5)	Bi1 ^v —Ti1—Bi1 ^{xxii}	36.48 (2)

Bi1 ^{xii} —Bi1—Ti1 ^{xxii}	100.237 (12)	Bi1 ^x —Bi1—Ti1 ^{xxiv}	36.775 (14)
Bi1 ^{xii} —Bi1—Bi2 ^{xiii}	101.056 (6)	Bi2 ^{xiv} —Bi1—Ti1 ^{xxii}	37.501 (10)
Bi1 ^{xi} —Bi1—Bi2 ^{xvii}	101.056 (7)	Bi2 ⁱⁱⁱ —Ti1—Bi1 ^{xxii}	48.51 (2)
Bi2 ^{xvi} —Bi1—Bi2 ^{xvii}	102.459 (10)	Bi1 ^{xxix} —Bi2—Bi1 ^{xxx}	49.109 (12)
Bi1 ^{xxix} —Bi2—Bi1 ^{xxxii}	102.460 (10)	Ti1 ^{vii} —Bi1—Bi2 ^{xix}	49.72 (3)
Bi1 ^{xxx} —Bi2—Bi1 ^{xxxi}	102.460 (11)	Ti1 ^{xx} —Bi1—Bi2 ^{xviii}	50.23 (3)
Bi2 ^{xiii} —Bi2—Bi1 ^{xii}	102.596 (8)	$Ti1^{vii}$ — $Bi1$ — $Bi2^{xvii}$	50.37 (3)
$Bi2^{xv}$ — $Bi2$ — $Bi1^{xii}$	103.120 (6)	Ti1 ⁱ —Bi1—Bi2 ^{xviii}	51.27 (3)
$Ti1^{xxi} Bi1 Bi1^{xi}$	103.83(2)	$Ti1^{xxi} Bi1 Bi2^{xiv}$	51.93 (3)
Bi1 ^{xii} —Bi1—Bi2 ^{xvii}	103 916 (6)	$Ti1^{i}$ $Bi2$ $Bi1^{xii}$	52 331 (19)
$Bi2^{xiv}$ $Bi1$ $Bi2^{xix}$	104.912(8)	$Ti1^{xxvii} Bi2 Bi1^{xxix}$	52.551 (1)) 52.441 (7)
$Ti1^{ix} Ti1 Bi1^{xii}$	104.912(0) 105.95(7)	$Ti1^{xxviii} Bi2 Bi1^{xii}$	53 148 (19)
Ti1 - Ti1 - Di1 $Ti1xiv Pi2 Pi2xiii$	105.95(7) 106.077(14)	\mathbf{P}_{i}^{2}	53.140(19)
$\mathbf{T}_{\mathbf{i}}^{\mathbf{i}} \mathbf{D}_{\mathbf{i}}^{\mathbf{i}} \mathbf{D}_{\mathbf{i}}^{\mathbf{i}} \mathbf{D}_{\mathbf{i}}^{\mathbf{i}} \mathbf{D}_{\mathbf{i}}^{\mathbf{i}}$	100.077(14) 106.20(3)	$\mathbf{D}_{12} = -\mathbf{D}_{11} - \mathbf{D}_{12}$ $\mathbf{D}_{12} = \mathbf{D}_{12}$	53.241(9)
$\begin{array}{cccc} \Pi &D \Pi \\ D \\ \Pi & $	100.29(3)	$\begin{array}{c} \mathbf{D}\mathbf{I}\mathbf{Z} \mathbf{D}\mathbf{I}\mathbf{I} \\ \mathbf{T}\mathbf{I}1\mathbf{x}\mathbf{x}\mathbf{y} \mathbf{D}\mathbf{I}2 \mathbf{D}\mathbf{I}1\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x} \\ \mathbf{T}\mathbf{H}\mathbf{x}\mathbf{x}\mathbf{y} \mathbf{D}\mathbf{I}2 \mathbf{D}\mathbf{I}\mathbf{X}\mathbf{x}\mathbf{x}\mathbf{x} \\ \mathbf{T}\mathbf{H}\mathbf{x}\mathbf{x}\mathbf{y} \mathbf{D}\mathbf{I}\mathbf{X}\mathbf{x}\mathbf{x}\mathbf{x} \\ \mathbf{T}\mathbf{X}\mathbf{X}\mathbf{x}\mathbf{y} \mathbf{D}\mathbf{I}\mathbf{X}\mathbf{x}\mathbf{x}\mathbf{x} \\ \mathbf{T}\mathbf{X}\mathbf{X}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x} \\ \mathbf{T}\mathbf{X}\mathbf{X}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x} \\ \mathbf{T}\mathbf{X}\mathbf{X}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x} \\ \mathbf{T}\mathbf{X}\mathbf{X}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x}\mathbf{x}x$	52.001 (6)
$\begin{array}{c} \mathbf{D}\mathbf{I}\mathbf{I}^{\text{m}} \longrightarrow \mathbf{D}\mathbf{I}\mathbf{I} \longrightarrow \mathbf{I}\mathbf{I}\mathbf{I}^{\text{m}} \\ \mathbf{T}_{1}\mathbf{I}_{1} \longrightarrow \mathbf{D}_{2} \longrightarrow \mathbf{D}_{2}\mathbf{X}\mathbf{Y} \end{array}$	100.38(4) 106.752(12)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	55.901(0)
$\mathbf{H}^{\mathbf{H}} = \mathbf{H}^{\mathbf{H}} \mathbf{H}^{\mathbf{H}} = \mathbf{H}^{\mathbf{H}} \mathbf{H}^{\mathbf{H}}$	106.755(12)	$\frac{111^{\text{M}}-B11}{B11} = \frac{B11^{\text{M}}}{B11}$	54.737 (17)
111^{AVH} B12—B12 ^{AH}	106.976 (10)	$H_{11} = H_{12} = H_{12}$	54.81 (2)
111^{xx} $B11$ $B11^{x}$	107.69 (4)	$111 - B12 - B12^{\text{min}}$	55.32 (2)
$B_1 I^{v_1} - T_1 I - B_1 I^{xx_1}$	108.14 (5)	B_{11} xxx B_{12} B_{11} xn	55.502 (6)
Ti1 ^{xxvn} —Bi2—Ti1 ^{xxvm}	109.61 (4)	Bi2 ^{xiv} —Bi1—Bi2 ^{xvn}	55.865 (12)
Ti1 ^{xx} —Bi1—Ti1 ^{vn}	111.026 (7)	Ti1 ^{xx} —Bi1—Bi1 ^{x1}	56.289 (16)
Bi1 ^{xi} —Bi1—Bi1 ^{xii}	117.32 (2)	Ti1 ^{xxi} —Bi1—Ti1 ^{vii}	57.847 (3)
Ti1 ^{ix} —Ti1—Bi1 ^v	117.43 (3)	Ti1 ^{viii} —Ti1—Bi2 ⁱⁱⁱ	59.07 (5)
Ti1 ^{xxiv} —Bi2—Bi1 ^{xii}	118.70 (2)	Ti1 ^{xxiv} —Bi2—Ti1 ^{xxvii}	59.609 (4)
Bi2 ^{xiii} —Bi2—Bi2 ^{xiv}	119.12 (2)	Ti1 ^{ix} —Ti1—Bi1 ^{vii}	60.113 (19)
Ti1 ^{ix} —Ti1—Bi2 ⁱⁱⁱ	119.48 (9)	Bi2 ⁱⁱ —Ti1—Ti1 ^{viii}	61.32 (5)
Bi2 ^{xvii} —Bi1—Ti1 ^{xxvi}	119.656 (11)	Ti1 ^{xxiii} —Bi1—Ti1 ^{xxiv}	61.418 (6)
Bi2 ^{xii} —Bi1—Ti1 ^{xxii}	119.910 (14)	Bi1 ^{xii} —Bi1—Bi2 ^{xviii}	61.757 (12)
Bi2 ⁱ —Ti1—Ti1 ^{viii}	120.13 (9)	Ti1 ^{viii} —Ti1—Bi1 ^v	62.04 (2)
Ti1 ⁱ —Bi1—Ti1 ^{xxii}	120.34 (3)	Bi2 ^{xv} —Bi2—Bi1 ^{xxix}	62.067 (6)
Bi1 ⁱ —Ti1—Bi1 ^{xxii}	120.34 (3)	Bi2 ^{xv} —Bi2—Bi1 ^{xxx}	62.067 (6)
Ti1 ^{viii} —Ti1—Bi1 ^{vii}	120.39 (3)	Bi1 ^{xi} —Bi1—Bi2 ^{xix}	62.132 (6)
Bi2 ⁱⁱ —Ti1—Bi2 ⁱⁱⁱ	120.391 (4)	Bi1 ^{xii} —Bi1—Bi2 ^{xiv}	62.742 (7)
Bi2 ^{xiii} —Bi2—Bi2 ^{xv}	120.438 (12)	Bi1 ^{xi} —Bi1—Bi2 ^{xviii}	62.826 (12)
Bi1 ^x —Bi1—Bi1 ^{xi}	121.338 (11)	Bi2 ^{xiv} —Bi2—Bi1 ^{xii}	63.380 (4)
Ti1 ^{xx} —Bi1—Ti1 ^{xxiv}	121.44 (3)	Bi2 ^{xiv} —Bi2—Bi1 ^{xxix}	64.221 (7)
$Ti1^{vii}$ Bi1 $Ti1^{xxiv}$	121.95 (3)	Bi2 ^{xiii} —Bi2—Bi1 ^{xxxi}	64.221 (7)
Bi2—Bi1—Ti1 ^{xxvi}	122.061 (9)	Bi1 ^x —Bi1—Bi2 ^{xiv}	65 444 (6)
$Bi1^{vi}$ $Ti1 Bi1^{vii}$	122.001(9) 122.154(4)	Bi1 ^x —Bi1—Bi2 ^{xix}	65 843 (6)
Bi1 ^{xxix} Bi2Bi1 ^{xxxi}	122.131(1) 124135(12)	$Bi2^{xix}$ $Bi1$ $Ti1^{xxvi}$	67.048(12)
$Bi2^{xiy}$ $Bi1$ $Bi2^{xviii}$	124.133 (12)	$Ti1^{xxy}$ $Bi1$ $Ti1^{xxyi}$	68 10 (3)
$\mathbf{p}_{12} - \mathbf{p}_{11} - \mathbf{p}_{12}$	124.499(0) 124.058(7)		68.52(2)
$\mathbf{T}_{\mathbf{T}}_{\mathbf{T}_{\mathbf{T}}_{\mathbf{T}}_{\mathbf{T}}}}}}}}}}$	124.936(7) 120.41(2)	$D_{12} - D_{11} - D_{11}$ $D_{11} - T_{11} - D_{11}$	68.52(2)
$\begin{array}{cccc} \Pi \Pi & \longrightarrow & \Pi \Pi \\ \Pi & \longrightarrow & \Pi & \Pi \\ \Pi & \Pi & \Pi & \Pi & \Pi \\ \Pi & \Pi & \Pi$	129.41(3) 120.72(2)	$DII \longrightarrow DII \longrightarrow DII$ $T; 1xxiii D; 1 T; 1xxvi$	00.973(7)
$\mathbf{D}_{11} = \mathbf{D}_{11} = 11^{\text{min}}$ $\mathbf{T}_{11} \mathbf{x}_{\mathbf{x}\mathbf{y}\mathbf{y}} = \mathbf{D}_{11} = \mathbf{T}_{11} \mathbf{x}_{\mathbf{x}\mathbf{y}\mathbf{y}\mathbf{y}\mathbf{y}\mathbf{y}\mathbf{y}\mathbf{y}\mathbf{y}\mathbf{y}y$	127.73(2) 120.440(11)	$\begin{array}{cccccccccccccccccccccccccccccccccccc$	60.26(10)
	130.440 (11)	$D12^{}III^{}B12^{}$	09.30 (4)
$B12^{AVI}$ $B11$ $B12^{AVI}$	130.889 (12)	$\mathbf{D}_{12}^{\text{AAA}} = \mathbf{D}_{11}^{\text{AAAA}} = \mathbf{D}_{11}^{\text{AAAAA}}$	09.40/(12)
B12 B11B12	131.685 (13)	$B12^{AII} - B11 - 111^{AAIV}$	69.516 (7)
$B_{11} - B_{11} - T_{11} x_{11}$	131.728 (9)	B_{12}^{m} —T11—B12 ^w	70.39 (4)

$\begin{array}{l} Bi2^{iii} \hline Ti1 \hline Bi1^{vii} \\ Bi2^{i} \hline Ti1 \hline Bi1^{v} \\ Bi2^{xii} \hline Bi1 \hline Ti1^{xxiv} \end{array}$	135.68 (5) 135.83 (5) 136.209 (11) 138.917 (11)	Bi 2^{xvii} —Bi 1 —Ti 1^{xxiv} Ti 1^{xxii} —Bi 1 —Ti 1^{xxiii} Bi 1^{xxii} —Ti 1 —Bi 1^{xxiii}	71.591 (8) 71.66 (3)
$\begin{array}{l} Bi2^{i} \hline Ti1 \hline Bi1^{v} \\ Bi2^{xii} \hline Bi1 \hline Ti1^{xxiv} \end{array}$	135.83 (5) 136.209 (11) 138 917 (11)	Ti1 ^{xxii} —Bi1—Ti1 ^{xxiii} Bi1 ^{xxii} —Ti1—Bi1 ^{xxiii}	71.66 (3)
Bi2 ^{xii} —Bi1—Ti1 ^{xxiv}	136.209 (11) 138 917 (11)	Bi1 ^{xxii} —Ti1—Bi1 ^{xxiii}	
	138 917 (11)	Dii 111 Dii	71.66 (3)
Ti1 ^{xxi} —Bi1—Ti1 ^{xxvi}	130.717 (11)	Ti1 ^{xxi} —Bi1—Ti1 ^{xxii}	71.85 (5)
Bi1 ^{xxxii} —Bi2—Bi1 ^{xii}	141.173 (9)	Ti1 ^{viii} —Ti1—Bi1 ^{xxii}	72.76 (6)
Bi2 ^{xvii} —Bi1—Bi2 ^{xviii}	141.174 (9)	Ti1 ^{xxiv} —Bi1—Ti1 ^{xxv}	73.55 (3)
Ti1 ^{xx} —Bi1—Ti1 ^{xxii}	143.52 (2)	Bi2 ^{iv} —Ti1—Bi1 ^{vii}	75.584 (18)
Bi1 ^v —Ti1—Bi1 ^{vi}	144.62 (7)	Bi2 ⁱⁱⁱ —Ti1—Bi1 ^v	75.62 (3)
Ti1 ^{xx} —Bi1—Ti1 ^{xxi}	144.63 (7)	Bi2 ⁱ —Ti1—Bi1 ^{vii}	75.73 (3)
Ti1 ⁱ —Bi2—Ti1 ^{xxiv}	146.49 (2)	Bi2 ⁱⁱ —Ti1—Bi1 ^{vii}	77.12 (3)
Ti1 ^{vii} —Bi1—Ti1 ⁱ	146.84 (7)	Bi2 ⁱⁱ —Ti1—Bi1 ^v	77.437 (16)
Bi1 ^{vii} —Ti1—Bi1 ⁱ	146.84 (7)	Bi1 ^{xii} —Bi1—Ti1 ^{xxiv}	84.563 (17)
Ti1 ⁱ —Bi2—Ti1 ^{xxvii}	146.946 (8)	Ti1 ^{vii} —Bi1—Ti1 ^{xxvi}	85.661 (13)
Bi2 ⁱ —Ti1—Bi2 ⁱⁱⁱ	146.946 (8)	Ti1 ⁱ —Bi1—Ti1 ^{xxiv}	85.87 (4)
Ti1 ⁱ —Bi2—Bi1 ^{xxix}	149.23 (2)	Ti1 ^{vii} —Bi1—Ti1 ^{xxii}	87.57 (2)
Ti1 ^{xxvii} —Bi2—Bi1 ^{xii}	149.475 (16)	Bi1 ^{vii} —Ti1—Bi1 ^{xxii}	87.57 (2)
Ti1 ^{xx} —Bi1—Bi2 ^{xiv}	150.350 (13)	Bi2 ^{xiii} —Bi1—Bi2 ^{xviii}	87.936 (5)
Ti1 ⁱ —Bi1—Bi2 ^{xvii}	151.051 (14)	Ti1 ^{xxi} —Bi1—Ti1 ^{xxiv}	88.00 (2)
Ti1 ⁱ —Bi1—Bi2 ^{xix}	151.659 (13)	Ti1 ⁱ —Bi1—Ti1 ^{xxvi}	88.706 (13)
Bi1 ^{xi} —Bi1—Bi2 ^{xiv}	152.907 (6)	Bi1 ^{xxxi} —Bi2—Bi1 ^{xii}	92.064 (5)
Bi1 ^{xii} —Bi1—Bi2 ^{xix}	153.267 (4)	Bi2 ^{xii} —Bi1—Ti1 ^{xxvi}	93.35 (2)
Bi1 ^x —Bi1—Bi2 ^{xviii}	153.380 (4)	Ti1 ^{xxviii} —Bi2—Bi1 ^{xxix}	93.992 (16)
Bi2 ^{xiii} —Bi2—Bi1 ^{xxix}	155.439 (6)	Ti1 ⁱ —Bi1—Bi2 ^{xiv}	95.236 (16)
Bi1 ^{xi} —Bi1—Ti1 ^{xxiv}	158.113 (19)	Ti1 ^{xxiv} —Bi2—Bi1 ^{xxx}	95.410 (14)
Bi2 ^{xviii} —Bi1—Ti1 ^{xxii}	161.981 (11)	Ti1 ^{xxi} —Bi1—Bi2 ^{xviii}	95.54 (4)
Bi2 ⁱ —Ti1—Bi1 ^{xxii}	162.533 (7)	Ti1 ^{vii} —Bi1—Bi2 ^{xviii}	96.63 (4)
Bi2 ^{xiv} —Bi1—Ti1 ^{xxvi}	165.35 (2)	Bi2 ^{xvi} —Bi1—Ti1 ^{xxii}	96.863 (15)
Ti1 ^{viii} —Ti1—Ti1 ^{ix}	178.47 (15)	Ti1 ^{xx} —Bi1—Bi2 ^{xix}	97.142 (14)
Ti1 ^{xx} —Bi1—Ti1 ^{xxvi}	30.870 (13)	Bi2 ^{xvi} —Bi1—Ti1 ^{xxiv}	98.027 (15)
Bi2 ^{xvi} —Bi1—Ti1 ^{xxvi}	34.47 (2)	Ti1 ^{vii} —Bi1—Bi2 ^{xiv}	98.391 (15)
Ti1 ^{xxii} —Bi1—Ti1 ^{xxiv}	34.877 (3)	Bi2 ^{xix} —Bi1—Ti1 ^{xxiv}	98.570 (15)
Bi1 ^{xi} —Bi1—Ti1 ^{xxvi}	35.089 (15)	Bi2 ^{xii} —Bi1—Bi2 ^{xix}	99.134 (9)
Bi1 ^x —Bi1—Ti1 ^{xxii}	35.832 (14)	Bi1 ^x —Bi1—Ti1 ^{xxvi}	99.91 (2)

Symmetry codes: (i) -x, -y+1/2, -z+1/2; (ii) x+1/4, y-1/4, -z+1/2; (iii) -x+1/4, -y+3/4, z+1/2; (iv) x, y-1/2, z+1/2; (v) x+1/2, y, z+1/2; (vi) x-1/2, y, z+1/2; (vii) -x+1/2, -y-1/2, z+1/2; (viii) -x+1/2, -y-1/2, z+1/2; (viii) -x+1/2, -y-1/2, z; (xiii) -x+1/2, -y+1/2, -z+1; (ix) -x, -y, -z+1; (ix) -x-1/4, y, -z+1/4; (ix) -x, -y, -z; (iii) -x+1/2, -y+1/2, -z; (xiii) -x-1/4, -y+3/4, z; (xiv) -x+3/4, -y+3/4, z; (xiv) -x+3/4, -y+3/4, z; (xiv) -x+3/4, -y+5/4, z; (xvi) x-1/2, y-1/2, z; (xviii) x-1/4, y-1/4, -z; (xix) -x+1/4, -y+1/4, -z; (xix) x+1/2, y, z-1/2; (xxi) x+1/2, y, z-1/2; (xxii) -x+1/4, y-1/2, z-1/4; (xxv) x-1/4, -y+1/2, z-1/4; (xxv) x-1/4, -y+1/2, -z+1/4; (xxv) x+1/2, -y+1/2, z; (xxvii) -x-1/4, y+1/2, -z+1/4; (xxv) x+1/2, y+1/2, z; (xxvi) x-1/4, y+1/2, -z+1/4.