

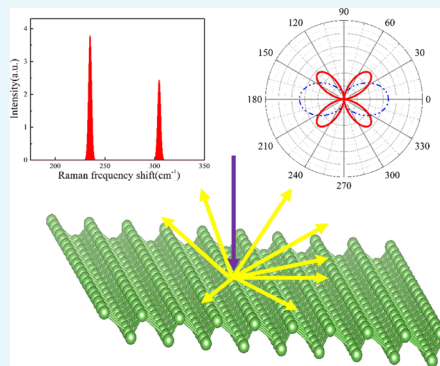
## $\beta$ -As Monolayer: Vibrational Properties and Raman Spectra

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**ABSTRACT:** Recently, semiconducting and other extraordinary properties of the monolayer of the V-group element have attracted a broad interest and attention. The success of experimentally growing antimonene and black phosphorus makes the arsenic monolayer a reasonable candidate for two-dimensional semiconductors. By using DFT calculation, we investigate the vibrational properties and Raman spectra of the buckled honeycomb monolayer of arsenic ( $\beta$ -As) for four commonly used laser lines. By calculating Raman tensor of each active modes of the  $\beta$ -As monolayer, we obtained polarization angle-dependent Raman intensities when the wave vector of incident light is parallel and perpendicular with the plane of the  $\beta$ -As monolayer. We found that the nonresonant Raman spectra have two peaks at 235 and 305  $\text{cm}^{-1}$  that correspond to the in-plane vibrating mode  $E_g$  and out-of-plane vibrating mode  $A_{1g}$ , which is similar to germanene, blue phosphorene, and  $\beta$ -Sb monolayer Raman spectra. There are two (four) minima and two (four) maxima when the polarization direction of scattered light is parallel (perpendicular) to that of the incident light and the wave vector of the incident light is parallel to the  $\beta$ -As monolayer. The Raman intensities of neither parallel polarization configuration nor perpendicular polarization configuration depend on the polarization direction when the wave vector of incident light is perpendicular to the  $\beta$ -As monolayer. The relation between shapes of the polar plots and relative values of Raman tensor elements is found. The Raman intensities decrease with increasing wavelength of incident laser lines in most cases. Our results will help experimentalists to identify the existence and the orientation of the  $\beta$ -As monolayer while they are growing the  $\beta$ -As monolayer.



### INTRODUCTION

Recently, few-layered structures of group-V element have attracted much attention in the nanoelectronic and optoelectronic fields. Black phosphorene, a monolayer of phosphorus atoms, is a popular member of this group because of having extraordinary properties such as direct moderate band gap,<sup>1</sup> high carrier mobility,<sup>2</sup> and anisotropic<sup>3</sup> transport properties. Blue phosphorene is another allotrope of phosphorene. The growth of blue phosphorene on Au(111) was reported by using a molecular beam epitaxial, in 2016.<sup>4</sup> The high thermal conductivity<sup>5,6</sup> and large band gap of blue phosphorene are one of the features that makes it a good suggestion for the electronic industry.<sup>7,8</sup> Lei et al. succeeded to experimentally grow antimonene, which is another member of group-V, on  $\text{Bi}_2\text{Te}_3$  and  $\text{Sb}_2\text{Te}_3$ .<sup>9</sup> Comparing with group IV (graphene,<sup>10</sup> silicene,<sup>11</sup> etc.), this group has a large band gap in their few layer structures, that is, an indispensable feature in electronic applications.

The gray arsenic, yellow arsenic, and black arsenic are the three common allotropes of arsenic.<sup>12</sup> The bulk of gray arsenic is semimetal. The existence of monolayer and bilayer of gray arsenic has been predicted because of its weak interlayer interaction.<sup>13–15</sup> The band gap of gray arsenic changes from  $\sim 0.175$  to  $\sim 2.49$  eV when its thickness decreases from bulk to

monolayer.<sup>16–18</sup> The buckled and puckered honeycomb structures are two stable monolayers of arsenic that are also called  $\beta$ -arsenene and  $\alpha$ -arsenene, respectively. The  $\alpha$ -arsenene was predicted<sup>13,19</sup> to be a semiconducting material with a direct band gap and has high carrier mobility<sup>20</sup> and strong anisotropy.<sup>20</sup> The structure of  $\beta$ -arsenene with an indirect band gap is similar to that of the layered blue phosphorus; this structure is a little more stable than that of  $\alpha$ -arsenene.<sup>13</sup> The investigated optical properties show that  $\beta$ -arsenene could be very useful in various photovoltaic and optoelectronic applications.<sup>14</sup>

Although few-layer arsenic has not been experimentally studied yet,<sup>13</sup> the success of growing antimonene,<sup>9</sup> black phosphorene,<sup>21</sup> and blue phosphorene<sup>4</sup> makes arsenic monolayers plausible candidates for two-dimensional (2D) semiconductors.

Up to now, there is not any study about vibrational properties and Raman spectra of the  $\beta$ -As monolayer, which is essential for the experimentalists to investigate the electronic and thermal properties of graphene and beyond,<sup>22</sup> and to

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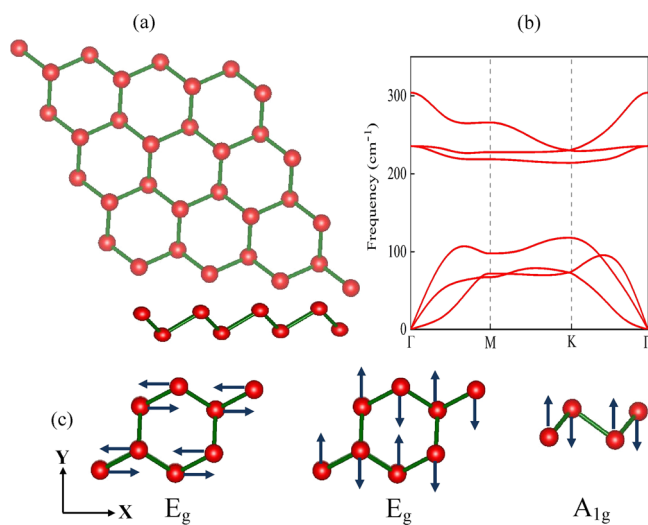
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identify the  $\beta$ -As monolayer when experimentalists are trying to grow it. Raman spectroscopy is also possible to determine the pressure by measuring the blue shift of Raman optical modes.<sup>23</sup> In this work, we investigated vibrational properties of the  $\beta$ -As monolayer, based on the density functional theory (DFT) calculation. We calculated Raman tensor and thus the polarization direction-dependent Raman intensities of the  $\beta$ -As monolayer with four commonly used laser lines (532, 633, 830, and 785 nm).

## RESULTS AND DISCUSSION

The phonon dispersion curve (Figure 1b) of the  $\beta$ -As monolayer (Figure 1a) shows that there is no imaginary



**Figure 1.** (a) Top and side view of  $3 \times 3 \times 1$   $\beta$ -As monolayer (buckled monolayer arsenic), (b) Phonon dispersions of  $\beta$ -As monolayer, and (c) Raman active modes  $A_{1g}$  (out-of-plane) and  $E_g$  (in-plane) at  $\Gamma$  point.

vibrating mode which means that the  $\beta$ -As monolayer has the dynamic stability. There are 3 optical modes. All of them are Raman active. The phonon dispersion is similar to those of blue phosphorene<sup>24</sup> and  $\beta$ -antimonene.<sup>25</sup> Our result also agrees with the previous work.<sup>19</sup>

The  $\beta$ -As monolayer belongs to the  $D_{3d}$  point group, whose Raman active modes are  $A_{1g}$  and  $E_g$  (doubly degenerate). The  $A_{1g}$  mode is out-of-plane vibration (Figure 1c) whose frequency is  $305 \text{ cm}^{-1}$ . The  $E_g$  (doubly degenerate) mode is in-plane vibration (Figure 1c) whose frequency is  $235 \text{ cm}^{-1}$ . Table 1 lists the Raman-active modes and the Raman shifts of  $\beta$ -As monolayer, germanene, blue phosphorene, and  $\beta$ -Sb monolayer. All of these four materials belong to space group  $P\bar{3}m1$  and point group  $D_{3d}$ .

**Table 1. Raman Active Modes and the Corresponding Raman Shifts (in  $\text{cm}^{-1}$  Unit) of  $\beta$ -As Monolayer, Germanene, Blue Phosphorene, and  $\beta$ -Sb Monolayer**

materials	$A_{1g}$	$E_g$
germanene <sup>24</sup>	160	310
blue phosphorene <sup>24</sup>	550	435
$\beta$ -As monolayer (present work)	305	235
$\beta$ -Sb monolayer <sup>25</sup>	195	150

We considered four commonly used laser lines with wavelengths 532, 633, 785, and 830 nm, corresponding to photon energies of 2.33, 1.96, 1.57, and 1.49 eV, respectively. Two of them are larger than the band gap of the  $\beta$ -As monolayer 1.59 eV,<sup>26</sup> two of them are smaller than the band gap. This band gap is underestimated by DFT and can be improved by hybrid exchange–correlation functional<sup>26</sup> or exchange–correlation energy whose derivative of the density (or density matrix) with respect to the number of electrons is discontinued at integers.<sup>27,28</sup>

After finding the Raman tensor, we calculated the Raman intensity; we considered that the  $\beta$ -As monolayer is in  $xy$  plane. Therefore, the incident light is parallel to the  $\beta$ -As monolayer plane when the incident light wave vector is along  $x$ -axis. The polarization direction of the incident light can be written as  $e_i = (0, \cos \theta, \sin \theta)$ ; it is a common practice to measure the parallel and perpendicular polarized scattered light whose polarization direction is  $e_s^{\parallel} = (0, \cos \theta, \sin \theta)$  and  $e_s^{\perp} = (0, -\sin \theta, \cos \theta)$ , respectively. These are called parallel polarization configuration and perpendicular polarization configuration, respectively.

The form of Raman tensors we obtained agrees with the group theory.  $\beta$ -As belongs to the  $D_{3d}$  point group. The Raman tensor of their Raman-active modes  $A_{1g}$  and  $E_g$  (doubly degenerate) modes has the form<sup>29</sup>

$$\begin{aligned} \tilde{R}(A_{1g}) &= \begin{pmatrix} a & 0 & 0 \\ 0 & a & 0 \\ 0 & 0 & b \end{pmatrix} \\ \tilde{R}(E_{g,1}) &= \begin{pmatrix} c & 0 & 0 \\ 0 & -c & d \\ 0 & d & 0 \end{pmatrix} \\ \tilde{R}(E_{g,2}) &= \begin{pmatrix} 0 & c & d \\ c & 0 & 0 \\ d & 0 & 0 \end{pmatrix} \end{aligned} \quad (1)$$

where  $a$ ,  $b$ ,  $c$ , and  $d$  are main terms, other elements are 0 because of the point group symmetry. By substituting the calculated Raman tensor for each modes and polarization vectors of the incident and scattered light into eq 11 in the Methods section, we have calculated the polarization angle-dependent Raman intensity for each mode. The Raman intensities for these two polarization settings are

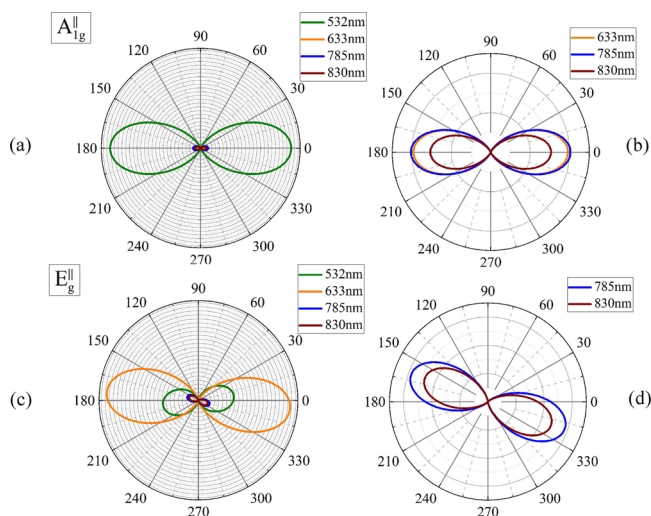
$$I^{\parallel}(A_{1g}) \propto |a|^2 \cos^4 \theta + |b|^2 \sin^4 \theta + 1/2 \text{Re}(a \cdot b^*) \sin^2(2\theta) \quad (2)$$

$$I^{\parallel}(E_g) \propto |c|^2 \cos^4 \theta + |d|^2 \sin^2(2\theta) - 2 \text{Re}(c \cdot d^*) \cos^2 \theta \sin(2\theta) \quad (3)$$

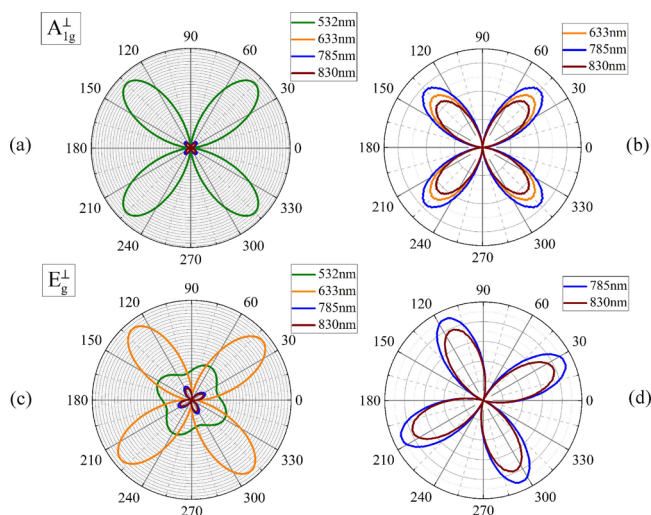
$$I^{\perp}(A_{1g}) \propto 1/4[|a|^2 + |b|^2 - 2 \text{Re}(a \cdot b^*)] \sin^2(2\theta) \quad (4)$$

$$I^{\perp}(E_g) \propto 1/4|c|^2 \sin^2(2\theta) + |d|^2 \cos^2(2\theta) + 1/2 \text{Re}(c \cdot d^*) \sin(4\theta) \quad (5)$$

The angular-dependent Raman intensities of different vibrating modes of the  $\beta$ -As monolayer for four laser lines 532, 633, 785, and 830 nm are shown in Figure 2 (parallel polarization configuration) and Figure 3 (perpendicular polarization configuration). The order of magnitude of



**Figure 2.** Polar plots of the angular-dependent Raman intensities,  $|\vec{e}_s \cdot \vec{R} \cdot \vec{e}_i|^2$ , of  $A_{1g}$  mode (a) and  $E_g$  mode (c) of the  $\beta$ -As monolayer for four laser lines 532 nm (green), 633 nm (orange), 785 nm (red), and 830 nm (wine). The plots corresponding to the latter three and two laser lines are enlarged in (b) for the  $A_{1g}$  mode and (d) for the  $E_g$  mode, respectively. The polarization direction of the scattered light is parallel to the polarization direction of the incident light. The incident and scattered light are in  $x$ -direction.



**Figure 3.** Polar plots of the angular-dependent Raman intensities,  $|\vec{e}_s \cdot \vec{R} \cdot \vec{e}_i|^2$ , of the  $A_{1g}$  mode (a) and  $E_g$  mode (c) of the  $\beta$ -As monolayer for 532 nm (green), 633 nm (orange), 785 nm (red), and 830 nm (wine). The plots corresponding to the latter three and two laser lines are enlarged in (b) for the  $A_{1g}$  mode and (d) for  $E_g$  mode, respectively. The polarization direction of the scattered light is perpendicular to the polarization direction of the incident light. The incident and scattered light are in  $x$ -direction.

Raman intensities is different because the Raman intensity is proportional to  $\omega_s^4$  (eq 11 in the Methods section). Therefore, we plot  $|\vec{e}_s \cdot \vec{R} \cdot \vec{e}_i|^2$  for clarity. Raman intensities of the  $A_{1g}$  and  $E_g$  modes in parallel polarization configurations have two maxima for all of the laser lines (Figure 2). The first term is dominant in eq 2 because  $|a| \gg |b|$ . Therefore, the maxima locate at  $\theta = 0^\circ$  and  $180^\circ$  for the  $A_{1g}$  mode; the minima intensities are zero at  $\theta = 90^\circ$  and  $270^\circ$  for the  $A_{1g}$  mode. The first term and the third term in eq 3 are dominant because  $|c| \approx 2|d|$ . Therefore, the common factor  $\cos^2 \theta$  of these two terms leads to the

similarity of the polar plots of the  $E_g$  mode and that of the  $A_{1g}$  mode. The remaining factors in eq 3 rotate the polar plots of the  $E_g$  mode with respect to that of the  $A_{1g}$  mode.

We did not find a configuration that has four maxima as blue phosphorene had in the parallel polarization configuration.<sup>24</sup>

In the perpendicular polarization configuration, both the  $A_{1g}$  and  $E_g$  modes have four maxima for all of the laser lines. The common factor  $\sin^2(2\theta)$  in eq 4 determines that the four maxima of all of the laser lines locate at  $\theta = 45^\circ + n 90^\circ$  for the  $A_{1g}$  mode; the minima intensities are zero at  $\theta = n 90^\circ$  for the  $A_{1g}$  mode, where  $n$  is an integer. This is not relevant to the relative value of  $a$  and  $b$ . The summary of the first two terms in eq 5 is approximately a constant  $|d|^2$  because  $|c| \approx 2|d|$  for laser lines 830, 785, and 532 nm. Therefore, the location of maxima and minima of polar plots of the  $E_g$  mode is determined by the third term. The minima (maxima) locate near  $67.5^\circ + n 90^\circ$  ( $22.5^\circ + n 90^\circ$ ) because the difference of argument of  $c$  and  $d$  is less than  $\pi/2$  for laser lines 830 and 785 nm. The minima (maxima) locate near  $22.5^\circ + n 90^\circ$  ( $67.5^\circ + n 90^\circ$ ) because the difference of argument of  $c$  and  $d$  is larger than  $\pi/2$  for the laser line 532 nm. The difference of argument of  $c$  and  $d$  is close to  $\pi/2$  for the laser line 532 nm. Therefore, the third term in eq 5 is small; thus, the minimal amplitude of the polar plots of the  $E_g$  mode is close to the maximal amplitude, which is distinctly different from other polar plots. For the laser line 633 nm, the first term in eq 5 is dominant because  $|c| \gg |d|$ . Therefore, the minima (maxima) locate near  $n 90^\circ$  ( $45^\circ + n 90^\circ$ ).

When the incident light is perpendicular to the plane of  $\beta$ -As, the polarization direction can be written as  $\vec{e}_i = (\cos \theta, \sin \theta, 0)$ . Then, the polarization direction of the parallel and perpendicular polarized scattered light is  $\vec{e}_s^{\parallel} = (\cos \theta, \sin \theta, 0)$  and  $\vec{e}_s^{\perp} = (-\sin \theta, \cos \theta, 0)$ , respectively. The Raman intensities of the parallel and perpendicular polarized scattered light are

$$I^{\parallel}(A_{1g}) \propto |a|^2 \quad (6)$$

$$I^{\parallel}(E_g) \propto |c|^2 \quad (7)$$

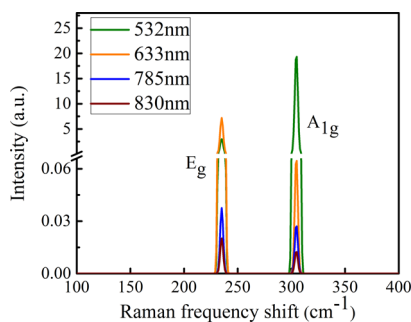
$$I^{\perp}(A_{1g}) = 0 \quad (8)$$

$$I^{\perp}(E_g) \propto |c|^2 \quad (9)$$

As one can see in the equations, only two elements of the Raman tensor ( $a$  and  $c$ ) play the role in the Raman intensity, whereas the Raman intensity depends on all elements of the Raman tensor when the incident light is parallel with the plane. In addition, the Raman intensity of the  $A_{1g}$  mode for parallel polarized scattered light depends only on  $a$ ; it is zero for perpendicular polarized scattered light. The Raman intensity of  $E_g$  mode depends only on  $c$ . None of the Raman intensities depend on the polarization angle  $\theta$ .

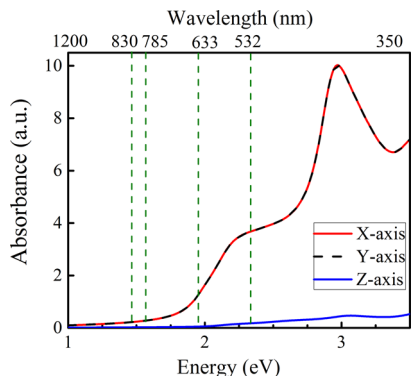
The phonon frequencies are 7.05 and 9.14 THz for the in-plane ( $E_g$ ) and out-of-plane ( $A_{1g}$ ) vibration modes at  $\Gamma$  point, respectively. Therefore, there are two peaks (235 and 305  $\text{cm}^{-1}$ ) in the nonresonant Raman spectra (Figure 4). As listed in Table 1, it is similar to germanene,<sup>30</sup> blue phosphorene,<sup>24</sup> and  $\beta$ -Sb monolayer.<sup>25</sup> The Raman intensity corresponding to the  $E_g$  mode is stronger than that corresponding to the  $A_{1g}$  mode for the  $\beta$ -As monolayer except for laser line 633 nm. The Raman intensity for different laser lines follows hierarchy  $I_{532} > I_{633} > I_{785} > I_{830}$  except  $I_{633}$  of the  $E_g$  mode.





**Figure 4.** Nonresonant Raman spectra of the  $\beta$ -As monolayer for four laser lines: 532 nm (green), 633 nm (orange), 785 nm (red), and 830 nm (blue). There are two peaks at 305  $\text{cm}^{-1}$  ( $A_{1g}$  mode) and 235  $\text{cm}^{-1}$  ( $E_g$  mode).

We also calculate the absorbance of the  $\beta$ -As monolayer (Figure 5). The absorbance is isotropic for lights with polarization direction in the  $x$ - $y$  plane. The absorbance increases with the photon energy for the four laser lines we concerned.



**Figure 5.** Absorbance spectra of the  $\beta$ -As monolayer for incident light with polarization direction in  $x$  (red),  $y$  (black dash), and  $z$  (blue) directions. The four vertical green dashed lines indicate the photon energy of four laser lines 830 nm (1.49 eV), 785 nm (1.57 eV), 633 nm (1.96 eV), and 532 nm (2.33 eV).

## CONCLUSIONS

In summary, we systematically investigated vibrational properties and Raman spectra of the buckled gray arsenic ( $\beta$ -As monolayer) for four commonly used laser lines 532, 633, 785, and 830 nm. There are not any imaginary vibrating modes, which mean the  $\beta$ -As monolayer has the dynamic stability. All of the optical modes are Raman active. The calculated Raman spectra show that there are two peaks at 235 and 305  $\text{cm}^{-1}$  where the former one corresponds to degenerate in-plane vibration modes  $E_g$  and the latter corresponds to the out-of-plane vibration mode  $A_{1g}$ . We calculated polarization angle-dependent Raman intensities when the wave vector of incident light is parallel and perpendicular to the plane of the  $\beta$ -As monolayer. There are two (four) minima and two (four) maxima when the polarization direction of scattered light is parallel (perpendicular) to that of incident light and the wave vector of the incident light is parallel to the  $\beta$ -As monolayer. The Raman intensities of neither parallel polarization configuration nor perpendicular polarization configuration depend on the polarization direction when the wave vector of incident light is perpendicular to the  $\beta$ -As monolayer. The

shapes of the polar plots are resulted from the argument difference between Raman tensor elements ( $c$  and  $d$ ) and relative amplitudes of Raman tensor elements ( $|a| \gg |b|$  and  $|c| \approx 2|d|$ ). The Raman intensities decrease with increasing wavelength of incident laser line except that of the  $E_g$  mode for laser line 633 nm.

## METHODS

Geometry optimization and dielectric tensor calculation are done with Vienna Ab initio Simulation Package.<sup>31</sup> Phonon frequency and phonon modes are obtained with Phonopy code.<sup>32</sup> The exchange–correlation potential is treated at the level of the generalized gradient approximation using Perdew–Burke–Ernzerhof.<sup>33</sup> For constructing basis set, the projected augmented wave method<sup>34,35</sup> is employed. Energy cutoff for all calculations is 500 eV. The Brillouin zone of the unit cell structure is sampled with a  $15 \times 15 \times 1$  and  $40 \times 40 \times 1$   $k$ -point grid for geometry optimization and static calculation, respectively. Vacuum slabs of 1.5 nm thick are inserted between neighboring 2D atom sheets. The convergence tolerance for the total energy and force calculations set to  $10^{-7}$  eV and 0.01 eV/Å, respectively.

The Raman tensor is obtained with a finite displacement method<sup>36–38</sup>

$$R_{\alpha\beta}(j) = V \sum_{\mu=1}^N \sum_{l=1}^3 \frac{\partial \chi_{\alpha\beta}}{\partial r_l(\mu)} \frac{e_l^j(\mu)}{\sqrt{M_\mu}} \quad (10)$$

where  $V$  is the volume of unit cell,  $M_\mu$  is the atomic mass of atom  $\mu$ , and  $\partial \chi_{\alpha\beta} / \partial r_l(\mu)$  is the first derivative of the electric polarizability tensor with respect to the atomic displacement. It equals with the derivative of dielectric tensor  $\epsilon_{\alpha\beta}$  divided by  $4\pi$  because  $\chi_{\alpha\beta}(\omega) = (\epsilon_{\alpha\beta}(\omega) - \delta_{\alpha\beta}) / 4\pi$ .  $\omega$  is the frequency of laser electric field.  $e_l^j(\mu)$  is the eigen vector of the  $j$ -th phonon mode at  $\Gamma$  point. The dielectric tensor of the structure with finite displacement can be obtained with DFT.

Then, the Raman intensity can be obtained<sup>36–38</sup>

$$I \propto \omega_s^4 |\vec{e}_s \cdot \vec{R} \cdot \vec{e}_i|^2 \quad (11)$$

where  $\omega_s$  is the frequency of scattered light,  $\vec{e}_i$  and  $\vec{e}_s$  are electric polarization vectors of incident and scattered light, respectively.

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### Notes

The authors declare no competing financial interest.

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