# OPEN ACCESS International Journal of Molecular Sciences

ISSN 1422-0067 www.mdpi.com/journal/ijms

Article

# Prediction of Radical Scavenging Activities of Anthocyanins Applying Adaptive Neuro-Fuzzy Inference System (ANFIS) with Quantum Chemical Descriptors

Changho Jhin and Keum Taek Hwang \*

Department of Food and Nutrition, Research Institute of Human Ecology, Seoul National University, Seoul 151-742, Korea; E-Mail: changho@jhin.kr

\* Author to whom correspondence should be addressed; E-Mail: keum@snu.ac.kr; Tel.: +82-2-880-2531; Fax: +82-2-884-0305.

Received: 15 May 2014; in revised form: 24 July 2014 / Accepted: 11 August 2014 /

Published: 22 August 2014

Abstract: Radical scavenging activity of anthocyanins is well known, but only a few studies have been conducted by quantum chemical approach. The adaptive neuro-fuzzy inference system (ANFIS) is an effective technique for solving problems with uncertainty. The purpose of this study was to construct and evaluate quantitative structure-activity relationship (QSAR) models for predicting radical scavenging activities of anthocyanins with good prediction efficiency. ANFIS-applied QSAR models were developed by using quantum chemical descriptors of anthocyanins calculated by semi-empirical PM6 and PM7 methods. Electron affinity (A) and electronegativity ( $\chi$ ) of flavylium cation, and ionization potential (I) of quinoidal base were significantly correlated with radical scavenging activities of anthocyanins. These descriptors were used as independent variables for QSAR models. ANFIS models with two triangular-shaped input fuzzy functions for each independent variable were constructed and optimized by 100 learning epochs. The constructed models using descriptors calculated by both PM6 and PM7 had good prediction efficiency with Q-square of 0.82 and 0.86, respectively.

Keywords: QSAR; anthocyanin; semi-empirical; ANFIS; quantum chemical calculation

#### 1. Introduction

As constituents of flavonoid group, anthocyanins and their aglycones, anthocyanidins, are color pigments originated from plants. Anthocyanins basically have flavylium ion skeleton attached with different side groups including hydrogen atom, hydroxyl group, and methoxy group. Anthocyanins are classified by the position and type of the side groups (Figure 1 and Table 4).

Radical scavenging activity is one of the characteristics of anthocyanins and other flavonoids. These compounds can reduce reactive oxygen species (ROS), resulting in relieving oxidative stress [1,2]. The radical scavenging activities can be explained by two suggested mechanisms: One is hydrogen atom transfer (HAT) and the other is single electron transfer (SET) [3]. HAT-based radical scavenging activity is explained by hydrogen donation as following equation:

$$X \cdot + AH \rightarrow XH + A \cdot$$
 (1)

where X is a free radical, such as ROS, and AH is a molecule of antioxidant. Free radicals are scavenged by hydrogen atoms donated from an antioxidant. SET-based radical scavenging activity can be explained by the scheme below:

$$X \cdot + AH \to X^{-} + AH \cdot^{+} \tag{2}$$

An electron from antioxidant transfers to a radical, and consequently the electron pairs up with unpaired electron of the radical. 2,2'-Azino-bis(3-ethylbenzothiazoline-6-sulphonic acid) (ABTS), a stable radical, is mainly reduced by SET mechanism [3,4], while 1,1-diphenyl-2-picryl hydrazyl (DPPH) radical is mainly reduced by HAT mechanism [5]. Until now, it has been considered that quantum chemical descriptors of ionization potential and bond dissociation energy are related with SET and HAT-based radical scavenging activities, respectively [6].

The relationship between molecular descriptors (e.g., number of hydroxyl group, presence of double bond on flavonoid C ring, and bond dissociation energy of hydrogen) of flavonoids and radical scavenging activities has been studied [6]. These prediction models can be applied to estimate and design novel radical scavenging bio-materials. However, the relationship between radical scavenging activities and molecular descriptors of anthocyanins has been poorly understood. Unlike other flavonoids, the structures of anthocyanins vary depending on pH [2,7]. At low pH (<2), flavylium cation (FC) is dominant with red and purple color. At higher pH, FC decreases while quinoidal base (QB), carbinol pseudobase (CP), and chalcone (Ch) forms of anthocyanins increase [7]. The change of the structure leads to the change of molecular descriptors of an anthocyanin molecule. For better understanding of the relationship between molecular descriptors of anthocyanin and radical scavenging activities, therefore, molecular descriptors of various anthocyanin forms should be considered.

To establish quantitative structure-activity relationship (QSAR) model, linear combination of variables have been generally used in previous studies [6,8]. The linear combination equation could be constructed easily through regression analysis. However, the interaction effect between variables is ignored, and nonlinear relationship between variables cannot be explained easily by linear combination. These kinds of defects may affect reliability of prediction model. Therefore, another prediction model is necessary for explaining the relationship between variables. Adaptive neuro-fuzzy inference system (ANFIS) is an artificial neural network (ANN)—applied fuzzy inference system

(FIS). By using ANFIS, multi-variable related ambiguous relationship can be quantified by defuzzification process of FIS, and error is adjusted by backpropagation algorithm with hidden layer of ANN for reliable prediction [9]. Therefore, ANFIS is an effective technique for solving problems which cannot be easily solved by linear regression analysis. The aim of this study was to establish a QSAR model for predicting radical scavenging activities of anthocyanins by ANFIS using quantum chemical descriptors.

**Figure 1.** (A) Flavylium cation; (B–D) quinoidal bases; (E) carbinol pseudo base; (F) chalcone structure of anthocyanidin.

## 2. Results and Discussion

## 2.1. Correlation Analysis

The result of correlation analysis between DPPH radical scavenging activities and calculated Quantum chemical descriptors; which are ionization potential (I), electron affinity (A), chemical hardness ( $\eta$ ), softness (S), electronegativity ( $\chi$ ), chemical potential ( $\mu$ ), electrophilicity ( $\omega$ ); of anthocyanin structures is presented in Table 1. Since 4 out of 21 tested anthocyanins had a glycosidic bond on 5-position, QB5 forms could not be generated. Thus, QB5 structures were excluded for further analysis. The  $\chi$  and  $\mu$  of FC, and I of QB7 calculated by both of PM6 and PM7 methods were significantly correlated with DPPH radical scavenging activities (p < 0.01). A calculated by PM6 and PM7 methods were also significant at p < 0.01 and p < 0.05, respectively. Some of the other quantum chemical descriptors of FC, QB7, and CP, calculated by PM6 and PM7 methods, were significant (p < 0.05). However, none of the quantum chemical descriptors of QB4' nor Ch was significantly correlated with radical scavenging activities. This result suggests that FC and QB7 forms are main contributors for radical

scavenging characteristics of anthocyanins, rather than CP and Ch. Since the radical scavenging experiment by Kähkönen and Heinonen [10], of which data was adapted to this study, was not conducted on highly acidic condition nor on highly basic condition, QB and FC seemed to exist abundantly at experimental condition. The structural change affects quantum chemical descriptors and redox properties of molecules [8,11]. Borkowski, *et al.* [12] also reported that radical scavenging activities of anthocyanins were influenced by pH. In the case of QB, QB7 was suggested as a primary contributor for radical scavenging activities, because higher correlation was observed between quantum chemical descriptors of QB7 and radical scavenging activities compared with QB4'.

**Table 1.** Correlation coefficient between 1,1-diphenyl-2-picryl hydrazyl (DPPH) radical scavenging activities and quantum chemical descriptors of flavylium cation, quinoidal base, chalcone and carbinol pseudobase.

Descriptors			PM6			PM7					
	FC	QB4'	QB7	CP	Ch	FC	QB4'	QB7	CP	Ch	
I	0.554 **	0.343	0.674 **	0.233	0.121	0.504 *	0.355	0.708 **	0.269	0.251	
$\boldsymbol{A}$	0.673 **	-0.166	-0.256	-0.473 *	-0.052	0.538 *	-0.206	-0.037	-0.289	-0.199	
η	0.124	0.288	0.523 *	0.530 *	0.121	0.263	0.310	0.418	0.378	0.298	
$\boldsymbol{S}$	-0.153	-0.171	-0.503 *	-0.535 *	-0.138	-0.238	-0.132	-0.398	-0.411	-0.284	
ω	0.328	-0.127	-0.305	-0.470 *	-0.054	0.202	-0.112	-0.085	-0.326	-0.212	
χ	0.701 **	0.194	0.282	-0.344	0.009	0.567 **	0.087	0.551 **	-0.149	0.020	
μ	-0.701 **	-0.194	-0.282	0.344	-0.009	-0.567 **	-0.087	-0.551 **	0.149	-0.020	

FC: flavylium cation; QB7 and QB4': quinoidal bases (Figure 1B,D, respectively); CP: carbinol pseudobase; Ch: chalcone; I: ionization potential; A: electron affinity;  $\eta$ : chemical hardness; S: chemical softness;  $\omega$ : electrophilicity;  $\chi$ : electronegativity; and  $\omega$ : chemical potential. \*, \*\* significance (p < 0.05 or p < 0.01).

For further investigation, hydrogen atom bond dissociation energies (BDE) of FC and QB7 were calculated and compared. Some previous studies reported that negative relationship was observed between the lowest BDE (BDE<sub>min</sub>) and radical scavenging activities [6,8]. Physicochemically, hydrogen abstraction reaction is more favoured at the position with a lower BDE, because a hydroxyl group with a lower BDE needs less energy to dissociate hydrogen. In addition, the dissociated hydrogen pairs up with a free radical to scavenge it. For this reason, BDE<sub>min</sub> represents the radical scavenging activity by HAT mechanism. Average BDE of FC and QB7 structures were lowest at the hydroxyl group on 4'-position (Table 2). This tendency was also observed in a previous study by density function theory method [13–15]. It has been reported that BDE<sub>min</sub> of flavonoid was negatively correlated with radical scavenging activities by Amić and Lučić [8]. In this study, however, BDE<sub>min</sub> of FC and QB7 calculated by PM6 and PM7 were not significantly correlated with DPPH radical scavenging activities (p > 0.05). This result was probably caused by conformational difference between anthocyanins, of which conformation changes depending on pH, and flavonoids. Thus, BDE was excluded for establishing QSAR model.

**Table 2.** Hydrogen atom dissociation energy of flavylium cations and quinoidal pseudo bases calculated by semi-empirical methods.

C 1	M 41 1	(1) BDE of FL					BDE of QB7					
Compounds	Method	3	5	7	3'	4'	5'	3	5	3'	4'	5'
	PM6	80.98	84.8	90.2	82.06	83.34	-	67.08	75.5	76.04	72.44	-
cyanidin	PM7	81.77	81.77	91.41	83.43	84.78	-	68.98	75.72	75.54	7 5.16	-
delphinidin	PM6	78.15	84.24	90.53	83.16	75.61	78.55	65.65	74.8	79.17	68.74	74.47
deipiiindiii	PM7	82.55	85.75	92.2	85.58	77.6	82.08	68.2	75.42	78.74	71.29	75.13
malvidin	PM6	77.33	82.05	87.19	-	73.9	-	65.49	74.83	-	68.04	-
marvium	PM7	81.19	85.22	90.98	-	75.21	-	71.31	78.69	-	73.36	-
	PM	8	8	9	_	8		6	7	_	7	_
pelargonidin	6	1.01	4.79	0.39	_	9.53	_	8.45	5.5	_	4.43	_
	PM7	81.86	85.71	91.51	-	90.6	-	69.68	75.89	-	76.87	-
peonidin	PM6	80.86	84.58	90.45	-	77.37	-	68.38	76.99	-	69.2	-
peomani	PM7	81.86	85.71	91.51	-	90.6	-	71.53	78.3	-	73.51	-
cyanidin-3-coumaroyl-	PM6	-	-	88.15	80.05	82.17	-	-	-	74.12	75.16	-
sambubioside-5- galactoside	PM7	-	-	86.57	77.29	78.88	-	-	-	76.74	77.52	-
cyanidin-3-	PM6	-	-	89.15	80.07	82.15	-	-	-	74.12	75.23	-
sambubioside-5- galactoside	PM7	-	-	98.43	88.66	90.97	-	-	-	76.74	78.07	-
cyanidin-3,5-	PM6	-	-	91.23	80.23	83.08	-	-	_	74.85	75.92	-
diglucoside	PM7	_	85.22	_	80.39	82.39	-	-	-	77.19	78.28	-
	PM6	-	86.49	91.25	80.53	82.61	-	-	77.32	76.27	73.99	-
cyanidin-3-arabinoside	PM7	-	88.14	92.69	82.63	85.54	-	-	77.87	77.09	77.48	-
:1: 2 1 4 11	PM6	-	93.17	93.58	81.03	83.71	-	-	76.74	74.76	75.55	-
cyanidin-3-galactoside	PM7	-	96.62	96.76	84.86	85.8	-	-	81.26	80.34	79.3	-
:1: 2 1 :1	PM6	-	86.87	92.58	81.78	84.4	-	-	76.07	74.91	75.63	-
cyanidin-3-glucoside	PM7	-	87.79	82.92	82.92	85.51	-	-	77.07	77.52	77.99	-
ovanidin 2 mutinasida	PM6	-	88.51	94.22	80.41	83.25	-	-	76.6	74.72	76.12	-
cyanidin-3-rutinoside	PM7	-	90.49	94.22	81.73	84.65	-	-	80.23	77.36	78.9	-
delphinidin-3-	PM6	-	86.92	91.58	82.36	75.31	77.35	-	76.9	78.53	69.28	74.42
glucoside	PM7	-	89.94	92.99	84.51	77.89	80.94	-	80.64	80.53	77.06	80.23
delphinidin-3-	PM6	-	88.23	91.05	82.52	75.93	75.74	-	75.22	77.2	70.95	72.55
rutinoside	PM7	-	84.54	92.68	84.59	77.79	76.34	-	72.62	80.15	73.79	73.62
malvidin-3,5-	PM6	-	-	86.32	-	73.67	-	-	-	-	71.07	-
diglucoside	PM7	-	-	91.84	-	76.05	-	-	-	-	72.45	-
molyidin 2 colootooida	PM6	-	87.49	89.43	-	73.81	-	-	74.52	-	69.57	-
malvidin-3-galactoside	PM7	-	88.43	91.56	-	75.73	-	-	78.65	-	72.45	-
molyidin 2 alyansida	PM6	-	85.75	89.51	-	73.89	-	-	76.84	-	68.59	-
malvidin-3-glucoside	PM7	-	88.63	94.26	-	78.17	-	-	73.52	-	71.67	-
pelargonidin-3-	PM6	-	87.13	91.13	-	86.79	-	-	71.66	-	75.48	-
glucoside	PM7	-	86.20	93.35	-	89.08	-	-	72.61	-	78.55	-

C	Method -	(1) BDE of FL					BDE of QB7					
Compounds		3	5	7	3'	4'	5'	3	5	3'	4'	5'
:1: 2 1 :1	PM6	-	88.79	98.46	-	76.39	-	-	79.56	-	68.31	-
peonidin-3-galactoside	PM7	-	88.94	92.01		78.78	-	-	77.10	-	72.78	
	PM6	-	88.80	90.97	-	76.38	-	-	74.66	-	67.51	-
peonidin-3-glucoside	D) 47		- 88.57	91.51	-	<b>50.5</b> 4	78.74 -		7		7	
	PM7	-				/8./4		-	8.95	-	2.74	-
	PM6	-	86.34	90.85	82.33	74.17	-	-	76.79	79.31	68.40	-
petunidin-3-glucoside	PM7	-	88.62	94.78	87.69	78.51	-	-	73.73	80.33	71.51	-

Table 2. Cont.

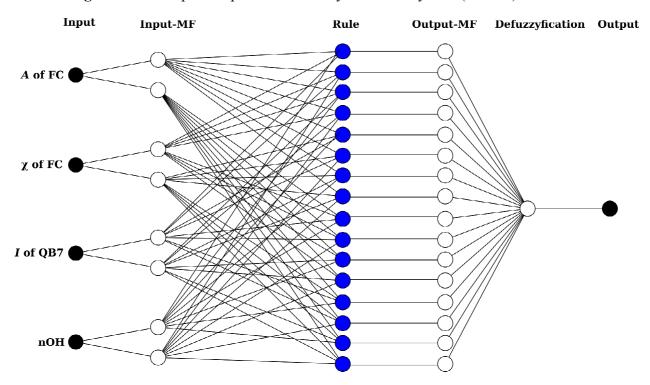
The possible mechanism for DPPH radical scavenging activities could be suggested by these results. Since BDE<sub>min</sub> was not significantly correlated with radical scavenging activities, the hydrogen atom transfer directly from anthocyanin to DPPH radical might not be a main mechanism for radical scavenging. Osman [16] suggested that DPPH radical and polyphenol compounds form a complex as an intermediate. For anthocyanin, as polyphenol, intermediate forming reaction could be occurred. Furthermore, the hydrazyl moiety of DPPH radical has nucleophilic characteristic and FC has high A and  $\chi$ . The intermediate forming step was suggested as reaction barrier, and this could explain why the DPPH radical scavenging activities were highly correlated with A and  $\chi$  of FC. On the other hand, from the positive correlation with I of QB7 and radical scavenging activity, electron transfer from QB7 to other molecules possibly lowers radical scavenging activities. The possible mechanism is single electron transfer from QB7 to FC. It is easy for a QB7 molecule with low I to transfer an electron to other molecules. Single electron addition to FC neutralizes net charge of the molecule to zero, and this will lower the A and  $\chi$  of the molecule. The required energy for intermediate forming reaction between anthocyanin and DPPH radical tends to be increased, consequently, total radical scavenging activity is decreased. Matsufuji, et al. [17] reported that the DPPH radical scavenging activities of anthocyanins were higher in acidic condition (pH 3) than in neutral condition (pH 7), and this tendency could also be explained by our suggested mechanism. Since electron transfer from QB7 to FC is suggested as decreasing total radical scavenging activities, low occurrence of QB7 and high occurrence of FC in acidic condition contribute to high DPPH radical scavenging activity.

# 2.2. Prediction of Radical Scavenging Activities of Anthocyanins

Through correlation analysis, four quantum chemical descriptors of A,  $\chi$  and  $\mu$  of FC, and I of QB7 were most highly correlated with radical scavenging activities. Among these descriptors, both  $\chi$  and  $\mu$  were drawn by the Equation (7), the correlation coefficient ( $R^2$ ) between these two variables was exactly 1. Hence, using both descriptors was unnecessary, and  $\chi$ , one of the two descriptors, was used for establishing the QSAR model. Previous studies also reported that  $\chi$  and  $\mu$  were reliable descriptors correlated with biological activities [11,18]. In addition, it has been reported that nOH was significantly correlated with radical scavenging activities of flavonoids and anthocyanins [6,8]. Therefore, nOH was chosen as an independent variable. Consequently, A and  $\chi$  of FC, I of QB7, and nOH were used as

<sup>&</sup>lt;sup>(1)</sup> BDE: hydrogen atom bond dissociation energy (kcal/mol); FL: flavylium cation; and QB7: quinoidal base (Figure 1D). The lowest BDE is presented in bold.

independent variables for establishing QSAR model. The calculated A and  $\chi$  of FC, I of QB7, nOH, and experimental DPPH radical scavenging activities were used as training data set for ANFIS model training. Structure of established ANFIS models is illustrated in Figure 2.



**Figure 2.** Developed adaptive neuro-fuzzy inference system (ANFIS) structure.

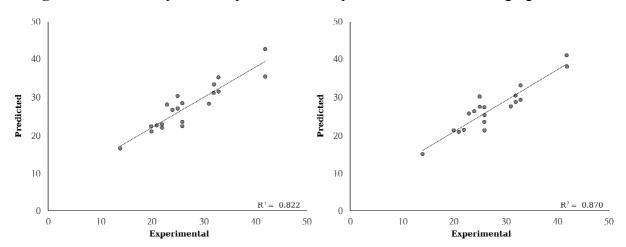
The experimental and predicted radical scavenging activities are presented in Table 3 and Figure 3. Since the number of naturally occurred and commercially available anthocyanins was limited, the test set with a relatively small number of compounds were only available to analyze. For small data set, cross validation with dividing data set into training set and test set might not be valid. Previous studies suggested a bootstrap validation method for small sample validation rather than cross validation [19,20]. Thus, bootstrap validation was performed in this study. The mean absolute error (MAE) and Q-square resulted by bootstrap validation were presented on Table 3. The ANFIS models with quantum chemical descriptors calculated by both of PM6 and PM7 semi-empirical methods had high prediction efficiency (p < 0.01). The error of the model continually decreased on every learning epoch (data not shown). After 100 learning epochs, the MAE of models with quantum chemical descriptors calculated by PM6 and PM7 were 2.44 and 2.06, respectively. Average DPPH radical scavenging activity of the tested compounds was 26.6. Thus, the prediction efficiency of established models was over 90%. Previous studies applied linear regression analysis for establishing QSAR models [6,11,18,19]. However, interaction between the variables was ignored in linear equations; therefore, a linear regression technique may not be suitable for multivariable analysis. Because four different independent variables were used in this study, linear regression analysis was not suitable for correcting interaction between variables. ANN has been applied on scientific studies because ANN can solve problems and predict problems practically as an adaptive intelligent system [9,20,21]. FIS can also solve non-linearly correlated variables by managing uncertainty of functions [22,23]. This explains the reason why ANFIS, an ANN applied problem-solving technique, was applied in this study. As a result, the established model showed high prediction efficiency and the ANFIS model fitted well with experimental data.

Table 3. Experimental and predicted DPPH radical scavenging activities.

Compounds	(1) Experimental	Predicted Radical Scavenging Activity		
•	Radical Scavenging Activity	PM6	PM7	
cyanidin	33	35.3	33.2	
delphinidin	42	42.6	41.0	
malvidin	24	26.6	26.1	
pelargonidin	31	28.3	27.6	
peonidin	33	31.4	29.3	
cyanidin-3-coumaroylsambubiose-5-galactoside	26	22.4	25.2	
cyanidin-3,5-diglucoside	21	22.6	20.9	
cyanidin-3-arabinoside	26	28.5	27.3	
cyanidin-3-sambubiose-5-galactoside	22	22.1	21.5	
cyanidin-3-galactoside	25	30.3	30.2	
cyanidin-3-glucoside	32	31.1	28.8	
cyanidin-3-rutinoside	25	27.0	27.5	
delphinidin-3-glucoside	42	35.4	38.1	
delphinidin-3-rutinoside	32	33.4	30.4	
malvidin-3,5-diglucoside	14	16.6	14.9	
malvidin-3-galactoside	22	22.9	21.3	
malvidin-3-glucoside	26	22.6	21.2	
pelargonidin-3-glucoside	20	21.0	21.2	
peonidin-3-galactoside	20	22.2	21.1	
peonidin-3-glucoside	26	23.6	23.5	
petunidin-3-glucoside	23	28.0	25.7	
(2) Mean absolute error		$2.43 \pm 0.35$	$2.06 \pm 0.32$	
<sup>(2)</sup> Q-square		$0.82 \pm 0.08$	$0.86 \pm 0.08$	

<sup>(1)</sup> Experimental radical scavenging activity data was adapted from a previous study by Kähkönen and Heinonen (2003), percentage of scavenged DPPH radical; (2) Mean absolute error and Q-squre are resulted from bootstrap validation, presented as mean ± standard deviation.

Figure 3. Relationship between predicted and experimental radical scavenging activities.



# 3. Experimental Section

# 3.1. DPPH Radical Scavenging Activity

DPPH radical scavenging activity data of 5 anthocyanidins and 16 anthocyanins were adapted from a previous study, which are listed in Table 4 [10].

Family	Compounds	(1) <b>nOH</b>	R1	R2	(2) <b>R3</b>	(2) <b>R4</b>				
	cyanidin	5	ОН	Н	OH	OH				
	delphinidin	6	ОН	ОН	OH	OH				
anthocyanidin	malvidin	4	$OCH_3$	$OCH_3$	OH	OH				
	pelargonidin	4	Н	Н	OH	OH				
	peonidin	4	OCH <sub>3</sub>	Н	OH	OH				
	cyanidin-3-coumaroyl-sambubioside-5-galactoside	3	ОН	Н	coumaroyl -sam	gal				
	cyanidin-3-sambubioside-5-galactoside	3	ОН	Н	sam	gal				
	cyanidin-3-arabinoside	4	ОН	Н	ara	OH				
	cyanidin-3-galactoside	4	ОН	Н	gal	OH				
	cyanidin-3-glucoside	4	ОН	Н	glc	OH				
	cyanidin-3-rutinoside	4	ОН	Н	rut	OH				
	cyanidin-3,5-diglucoside	3	ОН	Н	glc	glc				
anthocyanin	delphinidin-3-glucoside	5	ОН	ОН	glc	OH				
	delphinidin-3-rutinoside	5	ОН	ОН	rut	OH				
	malvidin-3-galactoside	3	$OCH_3$	$OCH_3$	gal	OH				
	malvidin-3-glucoside	3	$OCH_3$	$OCH_3$	glc	OH				
	malvidin-3,5-diglucoside	2	$OCH_3$	$OCH_3$	glc	glc				
	pelargonidin-3-glucoside	3	Н	Н	glc	OH				
	peonidin-3-galactoside	3	$OCH_3$	Н	gal	OH				
	peonidin-3-glucoside	3	$OCH_3$	Н	glc	OH				

**Table 4.** Evaluated anthocyanidins and anthocyanins.

petunidin-3-glucoside

# 3.2. Quantum Chemical Descriptors

# 3.2.1. Molecular Structure Preparation

Figure 1 presents various structures of anthocyanidins and anthocyanins. (**A**)–(**F**) are FC, quinoidal bases (QB4', QB5, and QB7), CP, and Ch, respectively. The structures of 21 anthocyanidins and anthocyanins were prepared using Gabedit 2.4.3 [24].

# 3.2.2. Calculation of Quantum Chemical Descriptors

Geometrical optimization of molecular structures was performed by semi-empirical methods of PM6 [25] and PM7 [26] using MOPAC2012 [27]. Quantum chemical descriptors of I, A,  $\eta$ , S,  $\chi$ ,  $\mu$ ,  $\omega$ , and BDE were calculated to establish QSAR models.

<sup>(1)</sup> *n*-OH: number of hydroxyl groups on flavonoid core; (2) sam: sambubioside; gal: galactoside; ara: arabinoside; glc: glucoside; and rut: rutinoside.

I was calculated as the following equation:

$$I = E(N-1) - E(N)$$
 (3)

where E(N-1) is energy of an anthocyanin radical generated after electron abstraction and E(N) is energy of an anthocyanin molecule. A was calculated as the following equation:

$$A = E(N) - E(N+1) (4)$$

where E(N+1) is energy of an anthocyanin radical generated after addition of an electron.

η was calculated from the following equation:

$$\eta = (I - A)/2 \tag{5}$$

S was calculated from the following equation:

$$S = 1/2\eta \tag{6}$$

 $\chi$  and  $\mu$  were calculated from the following equation:

$$\chi = -\mu = (I + A)/2 \tag{7}$$

 $\omega$  was calculated from the following equation:

$$\omega = \mu^2 / 2\eta \tag{8}$$

Hydrogen atom dissociation energy (BDE) was calculated from the following equation:

$$BDE = E(A-O\cdot) + E(H) - E(A-OH)$$
(9)

where  $E(A-O\cdot)$  is energy of a hydrogen abstracted anthocyanin phenoxyl radical, E(H) is the energy of a hydrogen atom, and E(A-OH) is energy of anthocyanin molecule.

# 3.3. QSAR Model Development

# 3.3.1. Correlation Analysis

Pearson's correlation analysis was conducted to examine the relationship between the DPPH radical scavenging activities and the quantum chemical descriptors using GNU R 3.0.1 [28]. The quantum chemical descriptors which were highly correlated with radical scavenging activities were chosen as independent variables for QSAR models.

# 3.3.2. ANFIS

ANFIS models were made using a fuzzy logic toolbox of Matlab 8.2 (Mathworks, Natick, MA, USA). Previous studies reported that the number of phenolic OH groups of flavonoid core (*n*-OH) was correlated with radical scavenging activities of flavonoids [8] and anthocyanins [19]. Therefore, *n*-OH, as well as quantum chemical descriptors, was used for establish OSAR model development.

For development of ANFIS models, A, and  $\chi$  of FC, I of QB7, and nOH were used as independent variables. DPPH radical scavenging activities of anthocyanins were used as a dependent variable. Two triangular-shaped membership functions for each independent variable, 16 if-then rules and 16

linear type output membership functions were developed (Figure 2). The ANFIS models were optimized by backpropagation method with 100 learning epochs.

To validate the constructed ANFIS models, bootstrap validation procedure was repeated 1000 times. Mean absolute error (MAE) was calculated and compared by bootstrapping. MAE was calculated from the following equation:

$$MAE = \frac{1}{n} \sum_{i=1}^{n} |y'_{i} - y_{i}|$$
 (10)

where  $y'_{i}$  is predicted DPPH radical scavenging activity and  $y_{i}$  is experimental one.

Also, Q-square between predicted radical scavenging activities and experimental ones was calculated and validated by bootstrap validation.

#### 4. Conclusions

Semi-empirical quantum chemical calculations of anthocyanins were done by PM6 and PM7 methods using MOPAC2012. PM7 is the most recently distributed semi-empirical calculation method. This is the first study regarding anthocyanins using PM7 method. This study suggests that PM7, as well as PM6, is a useful method for calculating quantum chemical descriptors for QSAR analysis. In addition, in this study, structural change of an anthocyanin was considered on semi-empirical quantum chemistry calculation. This study revealed that quantum chemical descriptors of flavylium cation and quinoidal base affect radical scavenging activities of anthocyanins. It suggests that the molecular conformation should be modified depending on surrounding condition before quantum chemical calculation. Established QSAR models by ANFIS showed good prediction efficiency with a statistical significance. Therefore, applying the ANFIS technique could improve the accuracy of QSAR models. However, the QSAR analysis of this study was limited to radical scavenging activities of anthocyanins. Further study is needed to verify the correlation between quantum chemical descriptors and biological activities of anthocyanins.

# Acknowledgments

This work (20110010846) was supported by the Mid-career Researcher Program through a National Research Foundation grant funded by Korea Ministry of Education, Science and Technology.

## **Author Contributions**

Changho Jhin designed the study, performed calculation processes, analysed results, and wrote the manuscript. Keum Taek Hwang gave advices to study and helped for editing the manuscript.

## **Conflicts of Interest**

The authors declare no conflict of interest.

## References

- 1. Tsuda, T.; Shiga, K.; Ohshima, K.; Kawakishi, S.; Osawa, T. Inhibition of lipid peroxidation and the active oxygen radical scavenging effect of anthocyanin pigments isolated from *Phaseolus vulgaris* L. *Biochem. Pharmacol.* **1996**, *52*, 1033–1039.
- 2. Kong, J.-M.; Chia, L.-S.; Goh, N.-K.; Chia, T.-F. Brouillard, R. Analysis and biological activities of anthocyanins. *Phytochemistry* **2003**, *64*, 923–933.
- 3. Ronald, L.; Wu, X.; Schaich, K. Standardized methods for the determination of antioxidant capacity and phenolics in foods and dietary supplements. *J. Agric. Food Chem.* **2005**, *53*, 4290–4302.
- 4. Scott, S.L.; Chen, W.J.; Bakac, A.; Espenson, J.H. Spectroscopic parameters, electrode potentials, acid ionization constants, and electron exchange rates of the 2,2'-azinobis (3-ethylbenzothiazoline-6-sulfonate) radicals and ions. *J. Phys. Chem.* **1993**, *97*, 6710–6714.
- 5. Bondet, V.; Brand-Williams, W.; Berset, C. Kinetics and mechanisms of antioxidant activity using the DPPH free radical method. *LWT-Food Sci. Technol.* **1997**, *30*, 609–615.
- 6. Amić, D.; Davidovic-Amic, D.; Beslo, D.; Rastija, V.; Lucic, B.; Trinajstic, N. SAR and QSAR of the antioxidant activity of flavonoids. *Curr. Med. Chem.* **2007**, *14*, 827–845.
- 7. Mazza, G.; Brouillard, R. Recent developments in the stabilization of anthocyanins in food products. *Food Chem.* **1987**, *25*, 207–225.
- 8. Amić, D.; Lučić, B. Reliability of bond dissociation enthalpy calculated by the PM6 method and experimental teac values in antiradical QSAR of flavonoids. *Bioorg. Med. Chem.* **2010**, *18*, 28–35.
- 9. Buyukbingol, E.; Sisman, A.; Akyildiz, M.; Alparslan, F.N.; Adejare, A. Adaptive neuro-fuzzy inference system (ANFIS): A new approach to predictive modeling in QSAR applications: A study of neuro-fuzzy modeling of pcp-based NMDA receptor antagonists. *Bioorg. Med. Chem.* **2007**, *15*, 4265–4282.
- 10. Kähkönen, M.P.; Heinonen, M. Antioxidant activity of anthocyanins and their aglycons. *J. Agric. Food Chem.* **2003**, *51*, 628–633.
- 11. Karelson, M.; Lobanov, V.S.; Katritzky, A.R. Quantum-chemical descriptors in QSAR/QSPR studies. *Chem. Rev.* **1996**, *96*, 1027–1044.
- 12. Borkowski, T.; Szymusiak, H.; Gliszczynska-Swiglo, A.; Rietjens, I.M.C.M.; Tyrakowska, B. Radical scavenging capacity of wine anthocyanins is strongly pH-dependent. *J. Agric. Food Chem.* **2005**, *53*, 5526–5534.
- 13. Trouillas, P.; Marsal, P.; Siri, D.; Lazzaroni, R.; Duroux, J.-L. A DFT study of the reactivity of OH groups in quercetin and taxifolin antioxidants: The specificity of the 3-OH site. *Food Chem.* **2006**, *97*, 679–688.
- 14. Kozlowski, D.; Marsal, P.; Steel, M.; Mokrini, R.; Duroux, J.-L.; Lazzaroni, R.; Trouillas, P. Theoretical investigation of the formation of a new series of antioxidant depsides from the radiolysis of flavonoid compounds. *Radiat. Res.* **2007**, *168*, 243–252.
- 15. Mendoza-Wilson, A.M.; Lardizabal-Gutiérrez, D.; Torres-Moye, E.; Fuentes-Cobas, L.; Balandrán-Quintana, R.R.; Camacho-Dávila, A.; Quintero-Ramos, A.; Glossman-Mitnik, D. Optimized structure and thermochemical properties of flavonoids determined by the chih (medium)–DFT model chemistry *versus* experimental techniques. *J. Mol. Struct.* **2007**, *871*, 114–130.

- 16. Osman, A. Multiple pathways of the reaction of 2,2-diphenyl-1-picrylhydrazyl radical (DPPH') with (+)-catechin: Evidence for the formation of a covalent adduct between DPPH' and the oxidized form of the polyphenol. *Biochem. Biophys. Res. Commun.* **2011**, *412*, 473–478.
- 17. Matsufuji, H.; Kido, H.; Misawa, H.; Yaguchi, J.; Otsuki, T.; Chino, M.; Takeda, M.; Yamagata, K. Stability to light, heat, and hydrogen peroxide at different pH values and DPPH radical scavenging activity of acylated anthocyanins from red radish extract. *J. Agric. Food Chem.* **2007**, *55*, 3692–3701.
- 18. Pasha, F.; Srivastava, H.; Singh, P. Comparative QSAR study of phenol derivatives with the help of density functional theory. *Bioorg. Med. Chem.* **2005**, *13*, 6823–6829.
- 19. Chang, H.-J.; Choi, E.H.; Chun, H.S. Quantitative structure-activity relationship (QSAR) of antioxidative anthocyanidins and their glycosides. *Food Sci. Biotechnol.* **2008**, *17*, 501–507.
- 20. Ghoush, M.A.; Samhouri, M.; Al-Holy, M.; Herald, T. Formulation and fuzzy modeling of emulsion stability and viscosity of a gum-protein emulsifier in a model mayonnaise system. *J. Food Eng.* **2008**, *84*, 348–357.
- 21. Amiryousefi, M.R.; Mohebbi, M.; Khodaiyan, F.; Asadi, S. An empowered adaptive neuro-fuzzy inference system using self-organizing map clustering to predict mass transfer kinetics in deep-fat frying of ostrich meat plates. *Comput. Electron. Agric.* **2011**, *76*, 89–95.
- 22. Lin, T.-C.; Liu, H.-L.; Kuo, M.-J. Direct adaptive interval type-2 fuzzy control of multivariable nonlinear systems. *Eng. Appl. Artif. Intell.* **2009**, *22*, 420–430.
- 23. Jang, J.; Sun, C.; Mizutani, E. Fuzzy inference systems. In *Neuro-Fuzzy and Soft Computing: A Computational Approach to Learning and Machine Intelligence*; Prentice-Hall: Upper Saddle River, NJ, USA, 1997; pp. 73–91.
- 24. Allouche, A.R. Gabedit—A graphical user interface for computational chemistry softwares. *J. Comput. Chem.* **2010**, *32*, 174–182.
- 25. Stewart, J.J.P. Optimization of parameters for semiempirical methods V: Modification of NDDO approximations and application to 70 elements. *J. Mol. Model.* **2007**, *13*, 1173–1213.
- 26. Stewart, J.J. Optimization of parameters for semiempirical methods VI: More modifications to the NDDO approximations and re-optimization of parameters. *J. Mol. Model.* **2013**, *19*, 1–32.
- 27. Stewart, J.J.P. Mopac2012. Available online: http://OpenMOPAC.net (accessed on 12 April 2014).
- 28. The R Core Team. *R: A Language and Environment for Statistical Computing*; R Foundation for Statistical Computing: Vienna, Austria, 2008.
- © 2014 by the authors; licensee MDPI, Basel, Switzerland. This article is an open access article distributed under the terms and conditions of the Creative Commons Attribution license (http://creativecommons.org/licenses/by/3.0/).