

Received 14 October 2013; revised 6 February 2014; accepted 3 March 2014. Date of publication 18 March 2014;  
date of current version 7 April 2014.

Digital Object Identifier 10.1109/JTEHM.2014.2312191

# A Method to Standardize Quantification of Left Atrial Scar From Delayed-Enhancement MR Images

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This work was supported in part by the Kings College London Centre, Excellence in Medical Engineering through the Wellcome Trust and EPSRC under Grant WT088641/Z/09/Z, and in part by the National Institute for Health Research, Biomedical Research Centre Award to Guy's and St Thomas' NHS Foundation Trust and King's College London.

**ABSTRACT** Delayed-enhancement magnetic resonance imaging (DE-MRI) is an effective technique for detecting left atrial (LA) fibrosis both pre and postradiofrequency ablation for the treatment of atrial fibrillation. Fixed thresholding models are frequently utilized clinically to segment and quantify scar in DE-MRI due to their simplicity. These methods fail to provide a standardized quantification due to inter-observer variability. Quantification of scar can be used as an endpoint in clinical studies and therefore standardization is important. In this paper, we propose a segmentation algorithm for LA fibrosis quantification and investigate its performance. The algorithm was validated using numerical phantoms and 15 clinical data sets from patients undergoing LA ablation. We demonstrate that the approach produces good concordance with expert manual delineations. The method offers a standardized quantification technique for evaluation and interpretation of DE-MRI scans.

**INDEX TERMS** Delayed-enhancement MRI, left atrium, image segmentation, fibrosis.

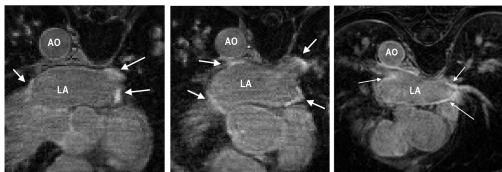
## I. INTRODUCTION

Atrial fibrillation (AF) affects approximately 2.3 million people in the USA with significant comorbidity and mortality [1], [2]. It is a condition that increases the risk of stroke by a factor of six-fold and doubles the mortality rate of patients when compared to age-matched controls. Since it was shown that ectopic beats from the pulmonary veins (PV) give rise to AF [3] the treatment of AF using radiofrequency catheter ablation (RFCA) has become an important and common procedure. In this procedure, ablation lesions are created in a circular fashion around the PV ostia to electrically isolate the PVs, and thus the ectopic focal points, from the rest of the left atrium (LA). This treatment can provide a cure for the majority of patients and prevent the requirement for long-term pharmacotherapy. However, for a high proportion of patients (15%–46%) [4]–[6], there is recurrence of AF. This normally

requires a second or third re-do ablation procedure and thus has a high burden on health care.

It is important to select patients who will respond better to RFCA to reduce recurrence rates. Several studies have shown that it is possible to predict the outcome of RFCA procedures from the fibrosis extent in LA [7]–[10]. A scoring system based on the degree of fibrosis has been developed, leading to treatment stratification [8]. Other recent studies have also highlighted the significance of the extent of fibrosis or scar in LA post-ablation for predicting outcome [11], evaluate effectiveness of ablation technologies [12] and helping to gain a better understanding of the left atrial substrate [13]. In this context, magnetic resonance imaging (MRI) has been shown to be effective for non-invasive imaging of the LA. In particular, Gadolinium delayed-enhancement (DE) MRI has the ability to detect changes that take place in the LA

both pre- and post-ablation and recent studies have shown that it could potentially be useful for selecting suitable candidates for RFCA [8]. DE-MRI is acquired with an inversion-recovery gradient echo sequence performed after administration of Gadolinium yielding an image at an inversion time which is chosen to null the signal from healthy myocardium. Due to the differential washout kinetics of Gadolinium, scar or fibrotic areas are differentiated from healthy tissue. Fibrotic or scar tissues in the myocardium appear with a signal intensity (SI) above normal myocardium. Fig. 1 shows some examples of DE-MRI with intensities significantly higher than myocardium.



**FIGURE 1.** DE-MRI images from three separate patients taken 3 months post-ablation. Arrows indicate areas of enhancement. Abbreviations: AO - aorta, LA - left atrium.

Quantification of scar or fibrosis from DE-MRI is challenging due to various reasons [14]. The thin myocardium of the LA wall leads to low signal-to-noise ratio. Contrast variation in these images can be an issue due to choice of inversion time. Also the complex geometry of the LA results in some transverse slices where a very small section of the anatomy is visible, making manual quantification in these areas highly observer-dependent. Finally, patients suffering from AF often have an irregular heart rate and breathing making it hard to acquire good quality respiratory- and cardiac-gated images. Quantification from such images become difficult to automate and manual quantification tends to be highly observer-dependent.

In this work, a scar quantification approach is proposed and investigated. The method exploits a well-known image segmentation approach known as graph-cuts [15]. Segmentation is achieved using a combination of scar intensity model priors and Gaussian-fitting to tissues in the unseen image to be segmented. The final labelling is achieved by optimizing a cost function using graph-cuts.

### A. PREVIOUS WORKS

Quantification and segmentation of ventricular scar from DE-MRI images have been studied in several investigations. Refer to Table 1 for a brief summary. A common method for detecting scar or fibrosis is to use a fixed model of thresholding between two and six standard deviations (SD) above the mean intensity of healthy myocardium [16]–[19]. This requires the user to manually outline remote or healthy myocardium. Another common method is the Full-Width-At-Half-Maximum (FWHM) which sets scar to be intensities greater than 50% of manually outlined hyper-enhanced myocardium [19]. Other approaches exist to compute the

threshold automatically [17] or by applying clustering [20], [21], or with graph-cuts [22].

The aforementioned works were primarily developed for the left ventricle. For the LA, methods have been proposed for endocardial surface-based segmentation [23] and threshold-based volumetric segmentation [7], [14], [24]. In [23], the maximum intensity projection (MIP) of the DE-MRI SI on the segmented LA shell is used to visualise enhancing intensities on the surface. This technique has an important drawback: it is only a visualisation of intensities and thus not a segmentation technique with no volumetric segmentation as output. In [7], a volumetric segmentation of pre-ablation LA fibrosis is proposed by obtaining suitable measurements from the intensity histogram within atrial wall. This has a disadvantage that the LA wall is thin and thus its manual segmentation can have significant inter-observer variation. Other methods have employed fixed models for pre-ablation fibrosis [24] and post-ablation scar [25] with variable thresholding.

In summary, a fixed thresholding model cannot handle all the different variabilities encountered in LA DE-MRI and these are both from the varied internal factors (size, distribution and heterogeneity of scar) and varied external factors (resolution, image noise, inversion time, surface coil intensity variation). The inversion time choice can generate the appearance of more or less scar, and change the appropriate scar threshold. Motion blurring also reduces the appearance of scar.

### B. CONTRIBUTIONS

In this work, we present a method for segmenting and thus quantifying LA fibrosis in DE-MRI. It is based on a probabilistic tissue intensity model of DE-MRI data, which is derived from both training and the unseen data. It offers two advantages: 1) It does not require manual outlining of base-line healthy myocardium, and 2) It provides greater accuracy than fixed models with no inter-observer variation. The algorithm was evaluated and compared with existing clinically-used methods using local pixel overlap measures. Performance was analyzed by exploring various scar contrast levels.

An abbreviated version of this work was published in [31] and [32]. In this current version, we present the approach with more details including additional experiments and validation. We also include an automated adaptive step that allows for variation in the scar signal level and avoids sub-optimal scar intensity models. Furthermore, we present a much more comprehensive validation of the algorithm on a larger clinical cohort. The algorithm was also used recently in a segmentation challenge [33], segmenting sixty DE-MRI datasets from three imaging centres.

## II. CLINICAL AND IMAGING PROTOCOLS

### A. PATIENTS

15 patients were followed up at 6 months following their first ablation for the treatment of paroxysmal AF. The procedures

**TABLE 1.** Overview of previously published methods for scar detection, quantification and segmentation.

	Reference	Model	$n$	Algorithm	Evaluation
LV	Kim et al. [16]	Canine	26	SD	Infarct size, <i>ex-vivo</i>
	Amado et al. [19]	Animal	13	SD, FWHM	Bland altman, Infarct volume
	Kolipaka et al. [17]	Human	23	SD	Percentage scar, Bland-Altman
	Positano et al. [20]	Human	15	Clustering	Percentage scar
	Yan et al. [26]	Human	144	SD	Percentage scar
	Schmidt et al. [18]	Human	47	SD	Infarct size
	Hennemuth et al. [27]	Human	21	EM fitting	Percentage scar, Bland-Altman
	Detsky et al. [21]	Human	15	Clustering	Infarct size
	Tao et al. [28]	Human	20	Otsu thresholding	Dice
Lu et al. [29]	Human	10	Graph-cuts	Infarct size and Bland-Altman	
LA	Oakes et al. [7]	Human	81	SD	Percentage scar
	Knowles et al. [23]	Human	7	MIP	Percentage scar
	Ravanelli et al. [30]	Human	10	SD, Skeletonization	Percentage scar, Bland-Altman

Methods were analysed on the type of data they were evaluated with and the structure of interest: left ventricle (LV) or left atrium (LA). The number of datasets ( $n$ ) is listed. Most methods employed simple standard deviation (SD) thresholding from a base healthy tissue intensity value. Others such as Full-Width-at-Half-Maximum (FWHM), Maximum Intensity Projection (MIP) and Expectation-Maximisation (EM) fitting have also been proposed. The evaluation measures used were compared.

were carried out in the cardiac catheterization laboratory at St. Thomas Hospital, London, U.K. All patients gave written permission to take part in this local ethics committee approved study.

### B. ABLATION PROCEDURE

A catheter was placed in the coronary sinus to provide a reference for electroanatomic mapping and to enable LA pacing. Two trans-septal punctures were made to access the LA using standard long sheaths (St. Jude Medical, MN, USA). A three-dimensional (3D) LA geometry was created using either Ensite NavX (St. Jude Medical, MN, USA) or CARTO (Biosense Webster, Diamond Bar, CA, USA). A circular mapping catheter was then placed in each PV in turn while the corresponding LA-PV ostium was targeted with wide area circumferential ablation. Energy was delivered through a 3.5 mm irrigated tip catheter with flow limited to 17 ml/min, power limited to 30 W on the anterior wall and 20 W on the posterior wall and temperature limited to 50°C. Ablation lesions were marked on the LA geometry when there had been an 80% reduction in the local electrogram voltage or after 30 seconds of energy delivery. The clinical endpoint was electrical isolation of all PVs.

### C. MRI SCANNING PROCEDURE

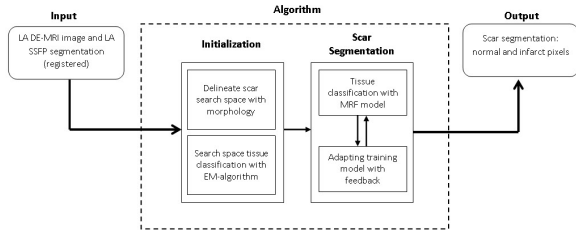
MRI scanning was performed before and after the ablation procedure. Pre-ablation scanning was performed 24 hours prior to the procedure and post-ablation scanning was performed 6 months after the procedure. The proposed algorithm in this work was developed and evaluated primarily for post-ablation images.

All scanning was performed on a 1.5T Achieva scanner (Philips Healthcare, The Netherlands). The examination began with a survey and reference scans, and an

interactive scan to determine the four-chamber orientation of the heart. For anatomical information, a 3D magnetic resonance angiography (MRA) scan with whole-heart coverage ( $1 \times 1 \times 2 \text{mm}^3$  acquired,  $1 \times 1 \times 1 \text{mm}^3$  reconstructed, 20 secs duration) was acquired following the injection of 0.4 ml/kg double dose of a gadolinium-diethylenetriaminepentaacetate (Gd-DTPA) contrast agent. This scan was not cardiac-gated. This scan was followed by a 3D respiratory navigated and cardiac-gated, 3D balanced steady-state free precession (b-SSFP) acquisition in a sagittal orientation with whole-heart coverage ( $1.3 \times 1.3 \times 2.6 \text{mm}^3$  acquired,  $1.3 \times 1.3 \times 1.3 \text{mm}^3$  reconstructed, 6 mins duration). The scan for the visualization of delayed-enhancement was a 3D ECG-triggered, free breathing inversion recovery (IR) turbo field echo (TFE) with respiratory-navigated and cardiac-gated with whole heart coverage ( $0.6 \times 0.6 \times 4 \text{mm}^3$  acquired,  $0.6 \times 0.6 \times 2 \text{mm}^3$  reconstructed, 3 mins duration). Data were acquired within a window of 150 ms every one RR interval, with a low-high k-space ordering and spatial pre-saturation with inversion recovery (SPIR) fat suppression. The IR time delay was determined from the Look-Locker sequence, and was set at an inversion time (TI) intermediate between the optimal TIs to null myocardium and blood. This scan was performed approximately 20 mins after contrast administration. The slices were set for complete coverage of both left and right atria. Slice orientation was in the four-chamber view for AF ablation to optimize visualization of the pulmonary veins. Note that the scan times quoted above are actual scan times. Typical respiratory gating efficiency is 50% but this varies considerably in this particular patient population.

### D. SEGMENTATION ALGORITHM

Fig. 2 shows an overview of the algorithm. The inputs were a DE-MRI image and a segmentation of the LA from an



**FIGURE 2.** An overview of the steps involved in the segmentation process. The pipeline takes as input MRI images and outputs binary segmentations (rounded boxes). The processing pipeline is illustrated here with each separate stage in the algorithm. Smaller boxes represent sub-steps. The scar segmentation stage is iterative as indicated by the bi-directional arrows.

anatomical scan. The LA segmentation was obtained from the b-SSFP whole-heart scan by an automatic approach based on a statistical shape model [34], and was followed where necessary by manual correction by a human rater (throughout this paper, the terms human rater or observer refer to someone who has experience viewing tomographic images and can correctly identify the LA endocardium and fibrosis in the LA myocardium). The b-SSFP image was chosen over MRA as it was acquired at the same phase in the cardiac cycle as the DE-MRI. The MRA, though it provides better anatomical visualization, was not cardiac gated and it can be difficult to resolve the differences between this and the DE-MRI with registration. The anatomical images were registered to the DE images using the DICOM header data, and then refined by rigid and affine registration steps [35]. Affine registration was necessary to account for the differing PV angles in the scans. This defined the endocardial LA boundary in the DE images.

### E. SCAR SEGMENTATION

Segmentation of scars from DE-MRI images can be defined as assigning a label  $f_p \in \{\text{non-scar}, \text{scar}\}$  for every voxel  $p$  in the search space of the image. The search space is defined as a region  $\pm 3$  mm from the endocardial border obtained from the atrial geometry extraction. This is within the limits of atrial wall [23]. Given the observed intensities in the atrial wall and prior knowledge of scars, the segmentation problem is solved using a probabilistic framework where the maximum *a posteriori* (MAP) estimate is computed using Bayes' theorem:

$$\arg \max_{\mathbf{f}} p(\mathbf{f}|\mathbf{I}) = \frac{p(\mathbf{I}|\mathbf{f})p(\mathbf{f})}{p(\mathbf{I})} \quad (1)$$

where  $\mathbf{f}$  is the total label configuration and  $\mathbf{I}$  are all observed intensities in the image. The image likelihood  $p(\mathbf{I}|\mathbf{f})$  describes how likely is the observed image given a label configuration  $\mathbf{f}$ . The prior  $p(\mathbf{f})$  encodes any prior knowledge of the healthy and scar tissue classes.

The MAP estimate allows to determine the most likely label configuration  $\mathbf{f}$  of the observed image  $\mathbf{I}$ . To make numerical computation more convenient, the MAP formulation is transformed to one involving only summations. This is

possible by taking the negative logarithm of Eq. 1:

$$\hat{\mathbf{f}} = \arg \min_{\mathbf{f}} \{-\ln p(\mathbf{I}|\mathbf{f}) - \ln p(\mathbf{f})\} \quad (2)$$

where  $\hat{\mathbf{f}}$  is the optimal labelling. The prior probability  $p(\mathbf{I})$  can be ignored as it is independent from the labelling  $\mathbf{f}$ . Note that the segmentation problem is now an energy minimization problem, following from (2):

$$\hat{\mathbf{f}} = \arg \min_{\mathbf{f}} \{\lambda E_{\text{data}}(\mathbf{f}) + E_{\text{prior}}(\mathbf{f})\} \quad (3)$$

where  $\lambda$  weights the influence of the two terms. The intensity energy  $E_{\text{data}}$  measures the disagreement between a probabilistic tissue model and the observed data, and  $E_{\text{prior}}$  is a smoothness term penalizing any discontinuities within a tissue class. In the following sections, the intensity models that contribute towards  $E_{\text{data}}$  and  $E_{\text{prior}}$  are described in the following sections.

### F. INTENSITY MODELS

The likelihood  $p(\mathbf{I}|\mathbf{f})$  of the observed intensities in the image can be estimated. Assuming that the voxel intensities are independent, the total likelihood for the image is given as:

$$p(\mathbf{I}|\mathbf{f}) = \prod_{p \in I} p(I_p | f_p) \quad (4)$$

The negative logarithm or the log-likelihood gives the total intensity energy contributed by each voxel:

$$E_{\text{data}} = - \sum_{p \in I} \ln p(I_p | f_p) \quad (5)$$

We first consider the intensity energy contribution from the scar tissue class, i.e. for the function  $p(\mathbf{I}|f_p = 1)$  and then for the non-scar class.

#### 1) INTENSITY MODEL FOR SCAR TISSUE

Enhancements in DE-MRI can vary greatly depending on a number of reasons: choice of inversion time, scanner vendor, protocol, operator experience, motion-blurring and patient breathing. Modelling variation in enhancement is thus important. When examining atrial DE-MRI images, the contrast-to-noise ratio (CNR) of scar to left atrial blood pool is often compared. This is simply due to the fact that normal atrial myocardium is not sufficiently visible to the naked eye in DE-MRI. Atrial blood pool is the single largest neighbouring tissue block sufficiently visible to the naked eye in the axial view. In this work, to exploit the nature of scar-blood CNR in DE-MRI, the scar to blood pool (SC-BP) intensity ratio is modelled and in the rest of paper we refer to *normalization* of DE-MRI intensities in this context as taking the ratio of DE-MRI voxel's intensity to blood pool.

To model enhancement, human raters delineated scar in training images. The blood pool was also delineated. The scar to blood pool ratio was determined for every voxel labelled as scar. This ratio could be modelled suitably with a Gaussian

distribution:

$$p(\mathbf{I}|f_p = 1) = \frac{1}{\sqrt{2\pi\sigma^2}} \exp \left[ -\frac{1}{2} \left( \frac{r - \mu}{\sigma} \right)^2 \right] \quad (6)$$

Here  $r$  is normalized intensity of labelled scar. Re-training this model allows it to adapt to images from a different source which may exhibit different scar-blood CNR levels due to its inversion times.

## 2) INTENSITY MODEL FOR NON-SCAR TISSUE

This is based on some prior knowledge about different tissue classes that could possibly interface with scar. As scar tissue normally borders with blood pool, normal myocardium and pericardial regions, a multi-modal mixture distribution is used:

$$\sum_{i=1}^n a_i \mathbf{G}_i(\mu_i, \sigma_i) \quad (7)$$

where  $\mathbf{G}_i$  is a Gaussian distribution for non-scar tissue  $i$  with mean  $\mu_i$  and variance  $\sigma_i$  for some mixture proportion  $a_i \in [0, 1]$ .

The model parameters were obtained from the image to be segmented (i.e. unseen image). However, as scar tissue is also part of myocardium, the mixture most likely to correspond to scar was identified and eliminated. This was the mixture with the highest mean. Following the elimination of the mixture  $\mathbf{G}_t$ , the weights of the remaining Gaussians of the mixture model were normalized to sum to one. The non-scar tissue model is given by:

$$p(\mathbf{I}|f_p = 0) = \sum_{i=1}^{n-t} \hat{a}_i \mathbf{G}_i(\mu_i, \sigma_i) \quad (8)$$

where  $t$  is the eliminated distribution. The parameters of the Gaussian mixture model ( $a_i, \mu_i, \sigma_i$ ) were obtained using the Expectation-Maximization (EM)-algorithm [36]. The number of tissue classes used was 4 pertaining to: blood pool, myocardium, scar and pericardial region. Starting with an initial estimate of the mean and variance for the four classes, the EM-algorithm iteratively computed the multimodal distribution parameters until convergence. This was followed by a truncation of the distribution pertaining to scar.

In summary, the algorithm extracted and incorporated knowledge both from the training dataset and the unseen image. The SC-BP contrast ratio was modelled from the training and intensity distributions of non-scar tissue were modelled from the unseen. This made the algorithm better equipped to handle contrast variations commonly encountered in DE-MRI.

## G. SMOOTHNESS CONSTRAINT

To ensure smoothness and avoid discontinuities in the final segmentation, the  $E_{\text{prior}}$  term of the MRF energy function in Eq. 3 penalised for assigning different labels to neighbouring voxels sharing similar intensity levels. The Lorentzian error

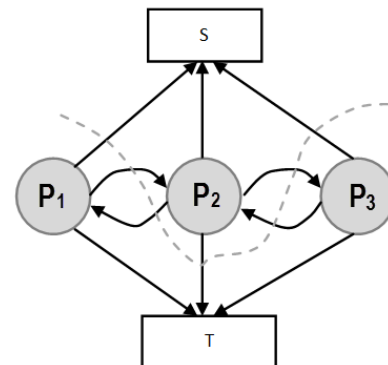
norm was employed, which is a robust metric for measuring intensity differences within a neighbourhood:

$$\varphi(p, q) = 1 + \frac{1}{2} \left( \frac{|I_p - I_q|}{\sigma} \right)^2 \quad (9)$$

The scale  $\sigma$  can be estimated from the DE-MRI image and depends on the variance of the actual scar and non-scar tissue class intensity distributions. With decreasing scale, the algorithm becomes less forgiving to small differences in intensities. Given that it is technically challenging to acquire high quality DE-MRI scans that show a clear distinction between scar and non-scar tissue, a larger value for the scale  $\sigma$  is almost always preferred. For convenience, to bound  $E_{\text{prior}}$  above and below by  $[0, 1]$  it is re-adjusted by  $1/(1 + \varphi(p, q))$ . This allows, if necessary, some adaptation of the training model to the unseen image.

## H. OPTIMIZATION

The optimization of the MRF energy function in Eq. 2 yields the desired image segmentation for scar. In [15], it was shown that it is possible to find the global optimum of functions of this type using the graph-cut method. In the graph-cut method, the MRF energy function is converted to a directional graph and the minimum  $s$ - $t$  cut gives the desired segmentation. A graph  $G = \langle V, E \rangle$  with two terminal nodes  $s$  and  $t$  representing the scar and healthy segmentation labels. The graph has a set of nodes  $V$  for every voxel in the image and  $E$  is the set of edges connecting these nodes (see Fig. 3). There are edges connecting every voxel to the two terminal nodes also known as the  $t$ -links. There are also edges connecting neighbouring nodes called the  $n$ -links. Each of these edges has a non-negative weight assigned to it. The  $t$ -link edge weights are obtained from the non-scar and scar tissue intensity priors in Eqs. 8 and 6 respectively. The  $n$ -link edge weights are obtained from Eq. 9. An  $s$ - $t$  cut on  $G$  partitions the nodes into two disjoint sets belonging to either the foreground or the background classes. Every  $s$ - $t$  cut incurs a cost and corresponds to a segmentation labelling  $\mathbf{f}$ . The total cost of an  $s$ - $t$  cut is equivalent to the sum of the edge weights the cut passes through. Fig. 3 illustrates how an  $s$ - $t$  cut in a simple



**FIGURE 3.** An illustration of an  $s$ - $t$  cut through a simple graph that represents the energy functional of an image containing only 3 voxels.

graph of an image with only 3 voxels computes a possible segmentation. Note how the  $t$ -links are assigned a value based on the affinity of the node to the particular class label. In a similar way, the  $n$ -links represent affinity for neighbouring voxels, holding nodes with similar intensities together and resisting to a cut passing through them resulting in a labelling of neighbouring voxels into two separate tissue classes.

### 1) ADAPTIVE FEEDBACK

The algorithm iteratively improved the segmentation result by incorporating new intensity information about scar. This step is shown in Fig. 2 as 'Adapting training model'. Starting from the initial training model for scar (see section II-F.1), this prior model may be sub-optimal since scar-blood CNR typically varies between DE-MRI images. It was iteratively adapted by incorporating the mean and SD of intensities in the segmentation:

$$\mu_{k+1} = \mu_k + \omega \cdot \tilde{\mu}_k; \sigma_{k+1} = \sigma_k + \omega \cdot \tilde{\sigma}_k \quad (10)$$

where  $k$  is the  $k$ -th iteration of adapting the scar training model with present parameters  $(\mu_k, \sigma_k)$  and those obtained from the new segmentation  $(\tilde{\mu}_k, \tilde{\sigma}_k)$ ;  $\omega$  is the learning rate and empirically set to 0.2. The iterative process was stopped when the difference in consecutive means was small:  $\Delta_k = (\tilde{\mu}_{k+1} - \tilde{\mu}_k) / \tilde{\mu}_k$ .

## III. EXPERIMENTS

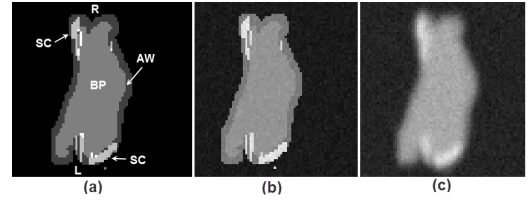
The algorithm was evaluated on both numerical phantom and real patient MRI datasets as described below.

### A. NUMERICAL PHANTOM DATA

In the rest of the paper, the true location of scar is referred to as the ground-truth for scar. The extent of scarring during ablation is non-deterministic and there is also confounding pre-ablation fibrosis. Therefore, identifying locations where ablations were made is not sufficient to be a surrogate for the ground truth for scar. Moreover, there is a high degree of inter- and intra-observer variability in manual segmentations of scar. These make evaluating algorithms more difficult and challenging. To overcome these issues, numerical phantoms were employed to extensively validate the algorithm.

### 1) PHANTOM CONSTRUCTION

The phantom was constructed in a four step process. The result of some steps is shown in Fig. 4. In the first step the LA geometry was extracted from a typical patient dataset. In the second step, a 2.5 mm wall was constructed around the LA. This represented LA wall. In a third step, regions were manually drawn within the constructed LA wall; these regions represented scar. In the final fourth step, intensities were sampled randomly from pre-determined distributions. These distributions belong to LA wall and blood-pool, and are measured and obtained from real MRI data. This ensured likeness of the phantoms to real MRI. Scar was filled with intensities from blood-pool *but* multiplied by a factor of 1.0 or above, and thus an SC-BP ratio of at-least 1.0 was

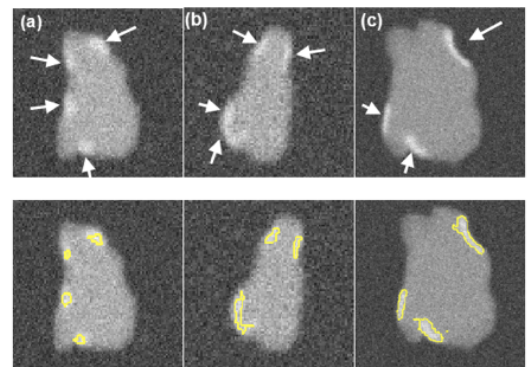


**FIGURE 4.** Images of a single-slice through a phantom taken at each stage of its construction process: (a) the phantom template with blood pool (BP) and atrial wall (AW) outlined semi-automatically using morphological dilation; scar (SC) drawn manually. (b) Assignment of intensity levels drawn randomly from pre-defined Gaussian distributions, with separate distributions for each tissue class. (c) In-plane and through-plane blurring followed by the addition of Gaussian white noise. Abbreviations: L - left side, R - right side.

maintained. This ratio emulated the selection of different inversion times for nulling the blood pool and was varied in experiments that follow. It is important to simulate partial voluming, anisotropic voxel sizes and noise in the phantoms. An anisotropic blur was applied with a kernel size of 2 mm in the through-plane direction and 1 mm in the in-plane direction. Gaussian white noise ( $\mu = 0, \sigma = 1$ ) was added to the image.

### 2) PHANTOM EXPERIMENTS

Numerical phantoms were generated by varying the SC-BP contrast ratio between 1.0 to 3.0. Some instances of these phantoms can be seen in Fig. 5. This evaluated the algorithm's performance on scar with varying contrast in relation to blood pool. The noise in the phantoms was maintained at signal-to-noise (SNR) of 9.0. This was the average SNR observed on a cohort of clinical datasets. Training ( $n = 50$ ) and testing ( $n = 50$ ) data sets were generated accordingly. To make training as realistic as possible, it was separately trained on SC-BP ratios: 1.5–1.8 and 1.8–2.1. The algorithm was compared to ground-truth using the Dice overlap coefficient [37].



**FIGURE 5.** Single slices through three different phantoms with numerically generated scars indicated by the arrows (Top row). SC-BP contrast is varied keeping SNR constant at 9.0. SC-BP: (a) 1.4, (b) 1.6 and (c) 1.8. The segmentations from the algorithm are also shown (Bottom row).

In a separate experiment, the SNR was varied from 4 to 16 along with the SC-BP contrast ratios. A single instance of the

algorithm was tested and this was trained on the SC-BP range 1.8–2.1. The Dice overlap of the segmentation with ground truth was compared.

In addition to the above experiments on scar enhancement and noise variation, the performance of the algorithm and fixed models (FWHM and  $n$ -SD) were compared on the same dataset. Five separate phantoms were used from which 200 different scarred regions were identified and their SC-BP contrast ratio noted. The accuracy with each method segmented each of the 200 regions was measured with Dice and reported.

### 3) CLINICAL DATA

A total of 15 clinical human datasets were available. In these set of experiments, segmentations from the algorithm were compared to the combined manual segmentations of three observers. In addition to this, the algorithm was also compared to fixed models: FWHM and  $n$ -SD methods. Training for the algorithm was accomplished using the leave-one-out principle, where 14/15 datasets were used for training and 1/15 used for testing. In the test scan, segmentation performance was measured both locally and globally for the image. For local comparison, performance on individual sections of scar was measured (a total of 155 regions were considered) and for a global comparison, total scar volume was measured. The pre-processing (left atrium geometry extraction and registration) was the same for each approach.

Three experienced observers manually segmented scars in each DE-MRI scan. They were combined to generate a consensus segmentation or *pseudo*-ground truth for each scan. This is necessary in order to consolidate inter-observer variabilities. Segmentations were combined using the STAPLE algorithm described in [38]. For each voxel, a probability estimate for the scar label could be computed. The STAPLE ground-truth was then be obtained by considering voxels to be scar if their probability is greater than 0.7, or 70%. This is a reasonable threshold capable of generating a strong consensus segmentation (In [38] the authors chose a lower consensus at 50%). To explore this threshold further, an experiment was performed by varying the threshold. Segmentations were available from five experienced observers on a random subset of the clinical datasets. The segmentations were combined using STAPLE and three thresholds were considered: 1)  $< 20\%$ , 2)  $\geq 20\%$  and 3)  $\geq 70\%$ . This generated different consensus segmentations with varying degrees of consensus against which the algorithm's performance was measured. Finally, to further explore whether better training of the algorithm leads to better segmentations and thus better performance, different instances of the algorithm are evaluated by incrementing the number of training set.

It is important to note that segmentations from the proposed algorithm were obtained without any user interaction necessary at any step of the algorithm. The most computationally demanding step was that of graph-cuts. On images of the resolution described above, there are typically 50 000–100 000 nodes that require processing. However, each

step of the iterative process took less than a minute. The total running time of the proposed approach is less than a minute on a 2.5 GHz PC.

## B. EVALUATION METRICS

To our experience, there is no single metric which works best for comparing segmentation overlaps. We chose two different metrics to quantify segmentation overlap.

### 1) REGIONAL OVERLAP

The Dice co-efficient of similarity is a well-known metric [37]. It is given by:

$$D = \frac{2|X \cap Y|}{|X| + |Y|} \times 100 \quad (11)$$

where  $X$  is the region in ground-truth and  $Y$  is the region in the algorithm.  $|X \cap Y|$  is total overlapping pixels and  $|X|$ ,  $|Y|$  are total number of pixels in each region. A Dice of 100 denotes perfect overlap.

### 2) SENSITIVITY AND SPECIFICITY

The proportion of true positives and true negatives in the detection process was analyzed by means of Receiver Operating Characteristic (ROC) curves where possible.

### 3) TOTAL SCAR VOLUME

Segmentations were also compared by measuring the total scar volume. This is mostly how scar is quantified and interpreted in clinical studies [39] and also serves as an important indicator for the total scar burden on the atrium.

## IV. RESULTS

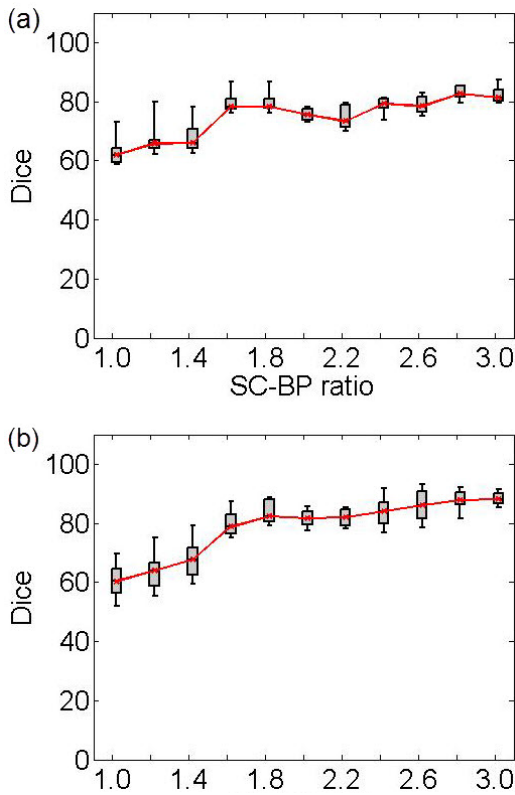
### A. NUMERICAL PHANTOMS

#### 1) SCAR CONTRAST

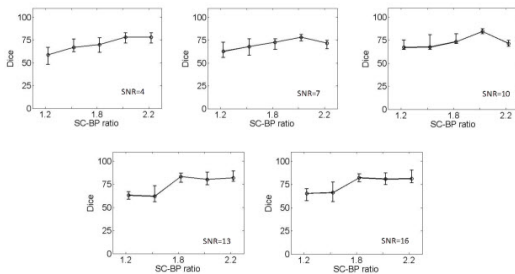
Fig. 6 show results from testing the algorithm on phantoms generated by varying the SC-BP contrast. Segmentation overlap with known true location of scar was measured using Dice. The algorithm performs well within its training range with median Dice  $\geq 80$  in both ranges:  $1.5 \leq \text{SC-BP} \leq 1.8$  [Fig. 6(a)] and  $1.8 \leq \text{SC-BP} \leq 2.2$  [Fig. 6(b)]. Outside its training area, the algorithm showed that it is able to adapt to excellent SC-BP contrast ( $\geq 2.2$ ) and good segmentations were achieved. Values of SC-BP explored in this experiment included realistic DE-MRI values but SC-BP  $\geq 3.0$  is very difficult to achieve in practice. To summarise, this experiment evaluated the algorithm across a wide dynamic SC-BP contrast range and the algorithm's approximation of ground truth was found to be good.

#### 2) NOISE VARIATION

Fig. 7 show results from testing the algorithm on phantoms generated by varying SNR. The SNR is varied between 4 and 16. The algorithm is trained on datasets generated with SC-BP ranging between  $1.8 \leq \text{SC-BP} \leq 2.1$ . Results show that SC-BP dictates over SNR for achieving good segmentations. Note segmentations are poor with SC-BP = 1.2 when



**FIGURE 6.** Performance of algorithm on numerical phantoms with increasing SC-BP contrast and SNR fixed at 9.0. Each graph is an instance of the algorithm: (a) trained on 1.5 to 1.8, and (b) trained on 1.8 to 2.1. The trend-lines show the median. Boxes in the plot indicate the 9th, 25th, 50th, 75th and 91st percentiles.

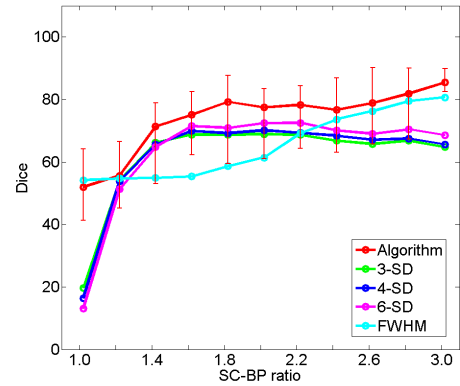


**FIGURE 7.** Performance of algorithm on numerical phantoms with varying SNR. The SNR is varied between 4 to 16. The median Dice segmentation overlap is plotted for the trend line shown.

SNR = 4 and with SNR = 16. But this is improved when  $SC-BP \geq 1.8$  demonstrating that the algorithm is robust to noise. SNR in actual DE-MRI is typically around 9.0 and the algorithm is seen to perform well in this range.

### 3) COMPARISON WITH FIXED MODELS

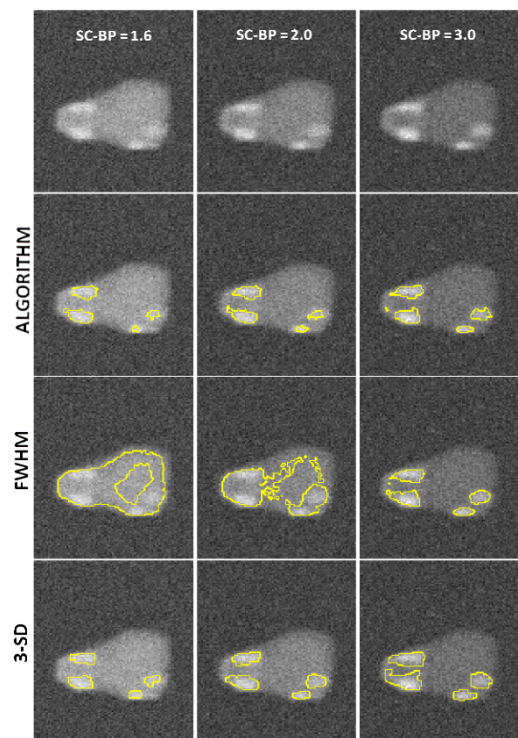
Fig. 8 show how the algorithm and fixed models performed on the same datasets. A total of 200 scarred regions were identified in five anatomically-unique phantoms. Their SC-BP contrast were computed and the overlap accuracy noted for each method. This allowed each method to be evaluated on specific SC-BP ratios and the plots in Fig. 8 show the



**FIGURE 8.** Comparing performance of algorithm with fixed models on numerical phantoms. Fixed models namely 3-SD, 4-SD, 6-SD and FWHM were evaluated. The trend-lines show the median Dice computed from 200 different scarred regions obtained from 5 separate phantoms.

segmentation accuracy trend. Fixed models 3,4,6-SD generated better segmentations than FWHM when scar contrast is between 1.2 to 2.2. However, FWHM improved substantially with higher scar contrast ( $SC-BP > 2.2$  in Fig. 8), which is when the 50 percent cut-off was more reasonable. Overall, as illustrated in Fig. 8, the algorithm maintained good accuracy when compared to fixed models in numerical phantoms.

The failure of FWHM revealed in this experiment is further illustrated in Fig. 9 (see columns 1 and 2). When the contrast in scar is not high, 50 percent of maximal signal as considered



**FIGURE 9.** Instances where 50% cut-off in FWHM is not optimal. First row: Original images of phantom with variable scar contrast. Second row: Algorithm's segmentation. Third row: Segmentation from FWHM with leaks. Fourth row: Segmentation from 3-SD.

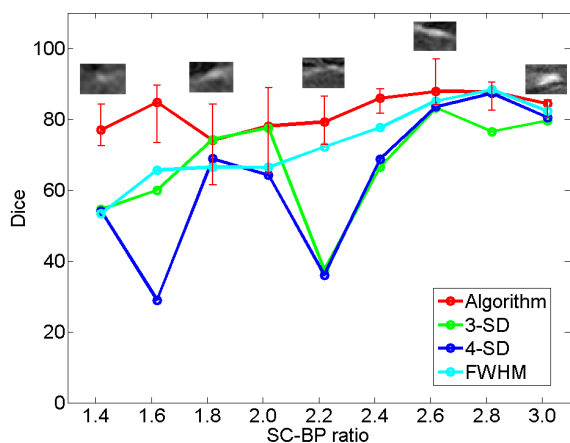


in FWHM, is not optimal and leaks in segmentation are inevitable [Fig. 9 (row 3)].

### B. CLINICAL DATA

#### 1) COMPARISON WITH FIXED MODELS USING OVERLAP METRIC

In the clinical datasets, performance of algorithm and fixed models were tested by measuring overlap with pseudo ground-truth (STAPLE) and comparing segmentation outputs in terms of scar volumes. For assessing performance based on overlap, each method was tested on individual SC-BP contrast levels: 1.0, 1.4, 1.8, 2.2, 2.6 and 3.0. This was possible by sampling 155 individual scarred regions from the clinical scans, measuring their SC-BP contrast ratio and testing how well each method segmented it. Results are given in Fig. 10.

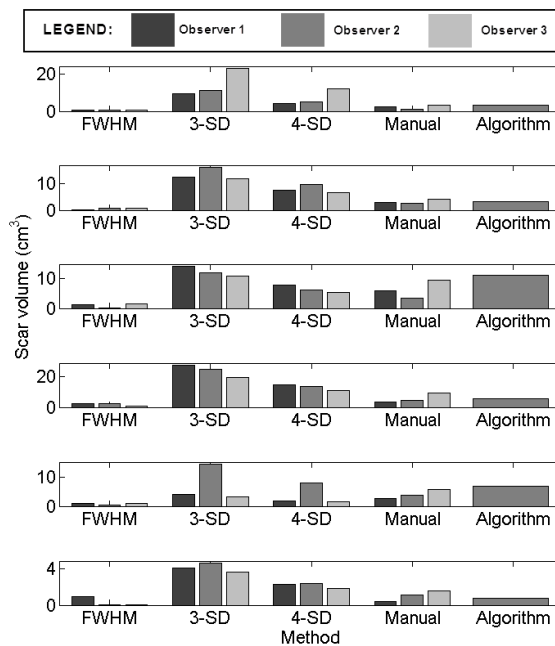


**FIGURE 10.** Comparing performance of fixed models with algorithm on patient scans. The performance over a total of 155 scarred regions are shown here. The trend-lines show the median. Five example snapshots of scar are also given to illustrate SC-BP contrast levels. Note SC-BP ratios analysed range from 1.4 to 3.0.

Fixed models perform less accurately than the algorithm when SC-BP is less than 2.5. At excellent and rarely attainable SC-BP levels ( $>> 2.5$ ), this trend changes and all models perform equally well. FWHM and the algorithm perform consistently across the entire SC-BP range used in this experiment, with 3- and 4-SD models outputting less accurate segmentations on scar at certain SC-BP contrast levels (1.6, 2.2). This is because scar is not adequately segmented by 3- or 4-SD due to non-overlapping intensities between model and actual. These results highlight that the algorithm performs consistently on actual DE-MRI and across realistic SC-BP levels. Performance of fixed models is found to be variable.

#### 2) COMPARISON WITH FIXED MODELS USING QUANTIFIED VOLUME

Assessment of performance using total scar volume reported by each method is important as this is mostly how scar is quantified and interpreted for clinical studies. Results obtained from scar volume quantified by each *run* of method is given in Fig. 11 for six clinical datasets. Each method was run three separate times with inputs (i.e. normal and



**FIGURE 11.** Assessment of inter-observer variation in fixed models, manual segmentation and algorithm. Six clinical cases are illustrated here.

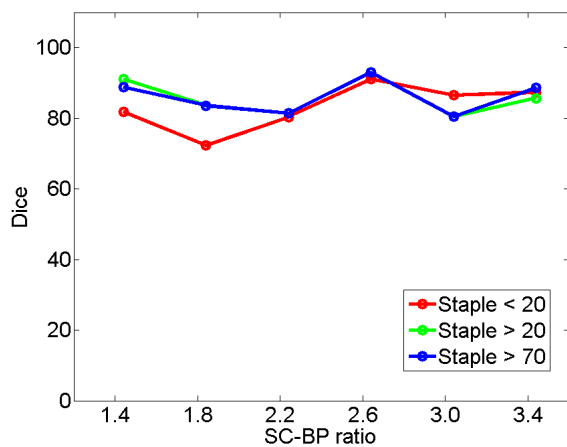
hyper-enhanced myocardium) fed from three independent observers. Volume reported by each method was compared to the volume reported by three independent experienced observers (see *Manual method* in Fig. 11). The algorithm correlated well with manual scar volumes. All three runs of the algorithm produced the same result as depicted by the single bar in Fig. 11. All other methods showed variations in the quantified volume. This variation was primarily due to observer variability in selecting normal or hyper-enhanced tissue required for fixed models. This highlights that a standardized quantification for scar using a fixed model approach (FWHM and SD) can be difficult to achieve.

#### 3) QUALITATIVE COMPARISON ON DE-MRI SCANS

Segmentation quality was assessed by overlaying region contours over the original DE-MRI slices. It was generally observed that in images with excellent SC-BP contrast, contours followed scar boundaries accurately in both algorithm and fixed models. Fixed models 3 and 6-SD were less accurate. An example is shown in Fig. 15 where segmentations similar to the consensus segmentation [Fig. 15(b)] could be obtained. Fixed models showed poor correlation when the SC-BP contrast is not sufficiently high. An example is shown in Fig. 16 where FWHM and the algorithm fared well with the algorithm providing a better approximation to the consensus segmentation. Fixed models 3 and 6-SD have gross errors in their segmentations due to a large overlap of intensities between their scar model and actual healthy tissue. Such segmentations are not usable for clinical studies and the operator would require to resort to threshold re-adjustment.

#### 4) ANALYZING ALGORITHM PERFORMANCE BY VARYING CONSENSUS LEVELS OF PSEUDO GROUND TRUTH

The algorithm's performance on a subset of clinical datasets was evaluated by varying the STAPLE threshold and thus the level or strength of the consensus segmentation. Results are plotted in Fig. 12 showing segmentation overlap on three consensus levels. There was a small difference in the algorithm's performance noted when SC-BP contrast levels were low. With higher SC-BP the performance was nearly similar. When SC-BP contrast is poor, the consensus or agreement between observers can be low. By lowering the acceptable consensus threshold (to 20%), dubious pixels are included in the ground truth where 2/10 observers would agree that it is scar. As the algorithm generally selects pixels which have close affinity to its models and priors, dubious pixels are omitted by the algorithm. There is a decrease in performance when segmentations with low consensus are presented.



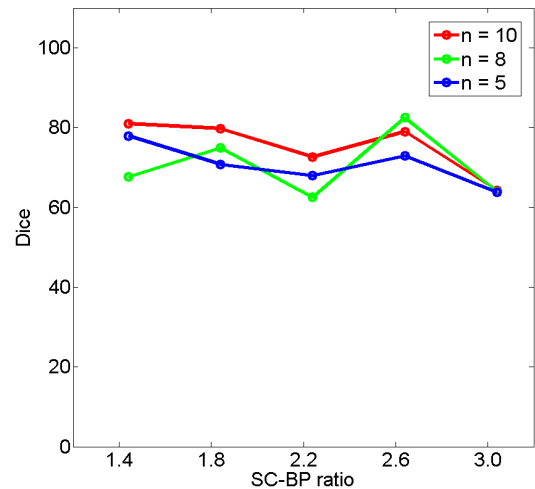
**FIGURE 12.** Performance trends of the algorithm on STAPLE consensus ground truths. Each curve represents performance on consensus segmentations, with consensus varied from 20% (weak) to 70% (strong).

#### 5) ANALYZING ALGORITHM PERFORMANCE BY VARYING STRENGTH OF THE TRAINING SET

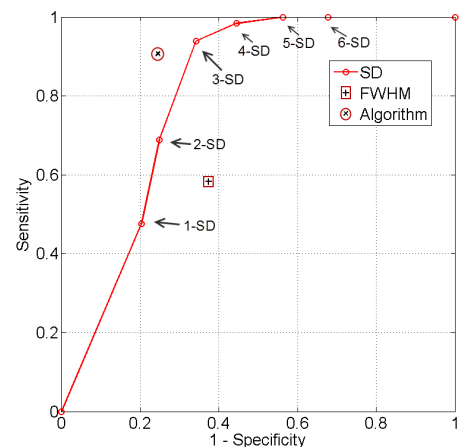
The algorithm's training set was incrementally increased and its segmentation overlap performance was noted. There was little notable difference in the performance. Results are plotted in Fig. 13. Training had an impact on performance only when the training set and test set had similar SC-BP contrast levels. If these vastly differ, initial iterations of the algorithm generate poor segmentations and these progressively become better in later iterations when the scar intensity model is continuously adapted with feedback from previous iterations (refer to 'adapting training step' in Fig. 2).

#### 6) ROC ANALYSIS

The true positive and true negatives rates were analyzed by looking at sensitivity and specificity of the algorithm and the fixed-models. A ROC curve between sensitivity and specificity was only plotted, where each point on the curve

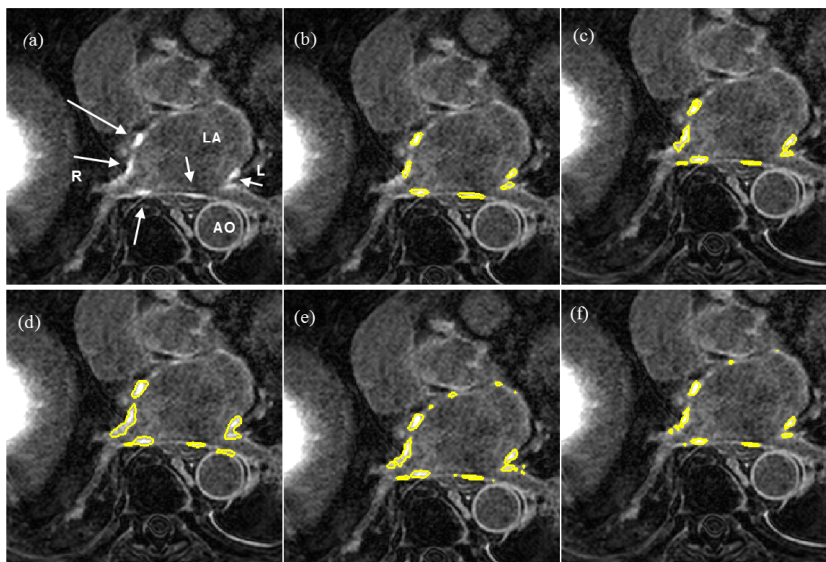


**FIGURE 13.** Performance trends of the algorithm by increasing the training set. Each curve represents an instance of the algorithm trained on  $n = 9, 7, 5$  datasets.

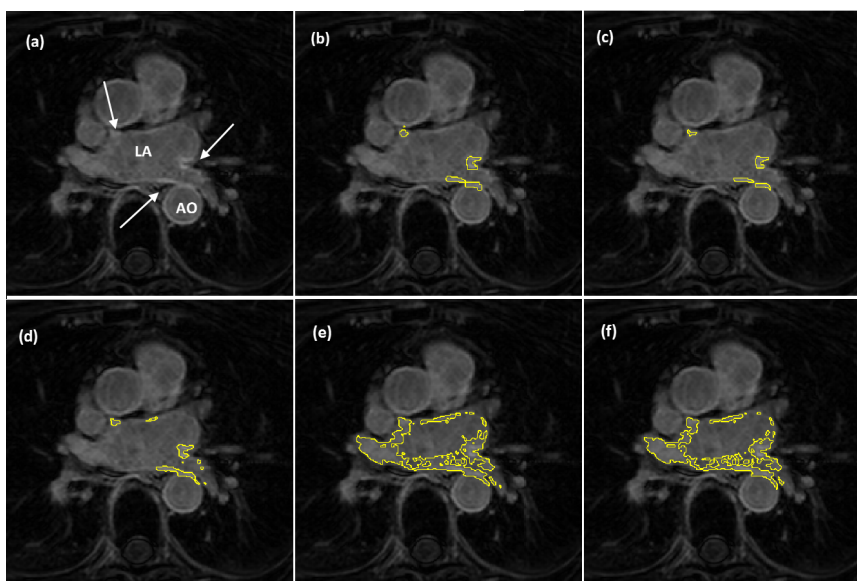


**FIGURE 14.** ROC analysis of the algorithm, FWHM and  $n$ -SD method. The ROC curve is only plotted for the  $n$ -SD method and the overall sensitivity and specificity is plotted for the parameter-less proposed algorithm and FWHM.

represented a decision threshold. The plots are given in Fig. 14 for the  $n$ -SD fixed model's ROC curve, where the decision threshold was varied between  $n = 1$  to  $n = 6$ . Since both the algorithm and FWHM do not require a decision threshold for obtaining segmentations, their overall sensitivity and specificity on all datasets was plotted. The  $n$ -SD fixed model approach has low specificity for  $n = 1, 2, 3$  and increasingly mis-labelled healthy tissues as scar. However, its higher sensitivity indicated that scar tissues are mostly labelled correctly. This reversed with  $n = 4, 5, 6$  and the trade-offs between sensitivity and specificity was seen to be optimal when  $n = 4, 5$ . Overall, the algorithm maintained both higher sensitivity and specificity than the fixed models as indicated in the ROC plot. The FWHM fell behind in this global ROC analysis and this is in-line with earlier tests on individual regions where it was shown that its 50% cut-off is too low for scar with low SC-BP, but more suitable for high SC-BP ratios.



**FIGURE 15.** Segmentations on clinical scans I: (a) original scan, (b) consensus STAPLE segmentation, (c) Algorithm, (d) FWHM, (e) 3-SD, (f) 6-SD. Arrows show enhancement. This scan has excellent SC-BP contrast and all methods except 3-SD and 6-SD demonstrate good accuracy. Abbreviations: AO - Aorta, LA - Left atrium, R - Right side, L - left side.



**FIGURE 16.** Segmentations on clinical scans II: (a) original scan, (b) consensus STAPLE segmentation, (c) Algorithm, (d) FWHM, (e) 3-SD, (f) 6-SD. Arrows show enhancement. This scan has excellent SC-BP contrast and all methods except 3-SD and 6-SD demonstrate good accuracy. Abbreviations: AO - Aorta, LA - Left atrium, R - Right side, L - left side.

## V. DISCUSSION

In this work a segmentation algorithm was investigated for fast quantification of fibrosis in DE-MRI scans. The proposed algorithm offers the following advantages: 1) Segments fibrosis without requiring a manual outline of remote or healthy myocardium. This is beneficial since remote myocardium tends to have low SNR and manual selection suffers from high observer variability. 2) The algorithm does not routinely generate false positives as was observed in existing

fixed model methods: FWHM and  $n$ -SD. 3) The algorithm is developed particularly for left atrial fibrosis segmentation and all present approaches were developed for ventricle scans. 4) Analysis of DE-MRI scans was shortened to an average of 30 seconds when compared to existing semi-automatic approaches requiring 2 minutes per scan on average.

The algorithm along with existing approaches was tested on both numerical phantoms and clinical datasets. Numerical phantoms provided with a wide dynamic range of variation

in scar contrast otherwise not possible in clinical datasets. Furthermore, in present literature, methods were validated on images using global overlap measures and not on individual regions and nor on individual SC-BP ratios. In this work, these together have allowed existing approaches to be investigated more thoroughly and results have revealed where they fail to perform. Both FWHM and SD methods can have gross errors in its segmentations when scar contrast is not high enough causing significant overlap of intensities between the scar and healthy tissue. On the clinical datasets, the variability in scar volume from FWHM and SD when operated by three different experienced operators meant no standard quantification was possible. The algorithm reported the same volume in each run and this was also consistently found to be close to the consensus segmentation of experienced observers.

The algorithm incorporates knowledge both from its training dataset and the unseen image. The SC-BP contrast ratio is modelled from the training and intensity distributions of non-scar tissue is modelled from the unseen. The SC-BP model is automatically adapted iteratively where necessary. These made the algorithm better equipped to handle contrast variations commonly encountered in DE-MRI. Built-in smoothness constraints and the graph-cuts approach allow it to consider neighbouring regions for inclusion or exclusion even when they do not fit the model. This enabled it to produce accurate scar boundaries.

The absence of ground truth for scar in DE-MRI is an important issue for segmentation methods and this has not been properly addressed in literature. One approach is to use voltage as a surrogate for scar [30]. In this work, three experienced observers manually segmented scars in each DE-MRI scan. These were then combined to generate a consensus segmentation or pseudo-ground truth for each scan using a statistical approach. This consolidated inter-observer variabilities commonly encountered in such scans. The degree of agreement of the consensus was also varied to show that a strong consensus was needed, especially when SC-BP levels were poor. A 70% threshold was overall deemed appropriate and this meant pixels with 7/10 consensus or above were included in the pseudo ground truth on which all tests were performed. Furthermore, numerical phantoms are employed in this work to evaluate the algorithm, FWHM and SD over a wider dynamic range of SC-BP contrast ratios.

The training step is also further explored in this work. A decrease in algorithm performance was noted when a small training set was used. However, there might come a point where increasing the training set would not substantially increase the accuracy of the algorithm but this is dependent on the variation of the image population. The algorithm was evaluated using the leave-one-out approach, with 14/15 of the datasets used for training and 1/15 for testing. This would always be applicable with unseen data always being left out of the training and any previous data being added to the training.

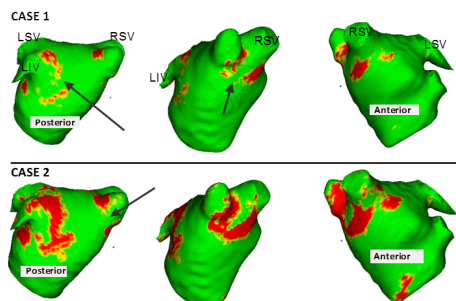
## A. CLINICAL TRANSLATION AND APPLICATION

Several recent studies [7]–[11] have highlighted the importance of quantifying LA fibrosis in DE-MRI and these include its use in deciding treatment strategy and thus selecting patients who will respond better to RFCA procedures. Quantifying using fixed models such as FWHM and SD is frequently utilised clinically due to its simplicity. In this work, both SD and FWHM were shown to have several disadvantages. The FWHM had overall equally low sensitivity and specificity than SD; it is more reliable in segmenting scar with high SC-BP than low SC-BP. The SD fixed model was overall more sensitive with a higher true positive rate than FWHM, but this comes at the expense of reduced specificity. In scar detection, a higher true positive rate and thus detecting most scar pixels is more desirable. This is because rectifying quantified volumes by manually removing mis-labelled healthy pixels is relatively simpler and less time-consuming than manually labelling and including scar pixels that are missed. The algorithm is shown to have good true positive and true negative rates in the ROC analysis, and higher than FWHM in all decision thresholds explored for SD. Moreover, standardization is impossible to achieve in fixed models such as SD with several choices of thresholds left to the operator to tweak. The clinical translation of the proposed algorithm thus becomes clear - it aims to provide a reliable and standardized method of quantifying scar.

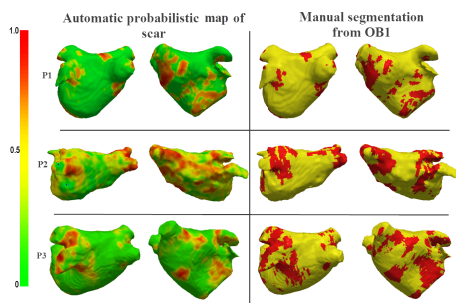
Quantification algorithms such as the one proposed, which can potentially be used in deciding treatment strategy, should be evaluated on a wide randomized spectrum of datasets from different imaging centres. To this end, the algorithm was recently evaluated in a segmentation challenge organized to compare quantification algorithms from seven different centres [33]. It was evaluated on sixty datasets obtained from three different imaging centres. A similar level of performance was achieved in these datasets. Dice segmentation overlap scores were comparable to those obtained from semi-automatic methods.

## B. OTHER APPLICATIONS

The proposed algorithm generates binary images of scar and this can be mapped and represented on the segmented LA surface model in two ways: 1) Maximum Intensity Projection (MIP) maps, and 2) Probabilistic maps. The former can be used to visualise scar on LA geometry and potential uses include predicting gaps in ablation patterns (see Fig. 17). A recent algorithm [40] also allows them to be visualized on two-dimensional flattened maps of the LA. Gaps play an important role in reconnection of re-entrant circuits in AF-cured patients. The latter can be used to obtain confidence levels on each region of scar extracted by the algorithm (i.e. a probability value between 0 and 1 of the chance of it being scar). An example of such a map can be seen in Fig. 18.



**FIGURE 17. Clinical applications I: Two clinical cases with scar quantified by the algorithm and projected on left atrial surface using MIP. Potential gaps are indicated using arrows. Gaps have important implications in re-do procedure planning.**



**FIGURE 18. Clinical applications II: Probabilistic map generated from the algorithm for three clinical cases (P1, P2, P3) shown alongside Maximum Intensity Projections (MIP) of manually outlined scar.**

### C. LIMITATIONS

One of the limitations of the study is the absence of ground truth in the clinical datasets. To overcome this consensus segmentations from three observers were generated using probabilistic methods. Furthermore, numerical phantoms were used and ground truth was readily available in these cases. A second limitation is in the Dice co-efficient used to measure overlap between segmentations. Dice can be highly sensitive to small translational errors between the test and true regions. To overcome this, clinical datasets were also evaluated by comparing segmentation volumes.

### VI. CONCLUSION

DE-MRI is becoming a preferred method for non-invasive imaging of myocardial scar. The amount of scar predicts whether a patient will respond to RFCA procedures. Thus accurately quantifying scar is important and has implications in patient selection for RFCA. Currently, SD and FWHM fixed thresholding models are frequently utilized clinically to quantify scar due to their simplicity. Present literature has only evaluated these methods using global image measures and thus their deficiencies could not be noted. In this work, there are two important contributions: 1) SD and FWHM fixed models are evaluated on individual regions of scar and thus various scar contrast ratios are examined to show they fail when some contrast levels do not suit the selected threshold in SD or 50% cut-off in FWHM. This is further confirmed and validated in numerical phantoms. 2) the proposed algorithm

has the potential to standardize quantification of scar from routine clinical scans; it requires no threshold selection and is shown to be more sensitive and specific than SD and FWHM in scar detection.

Accurate and standardized quantification will allow appropriate selection of patient candidates for RFCA. This could considerably reduce the recurrence rates, procedure risk and high financial burden associated with unsuccessful RFCA treatment. Patients not deemed appropriate for RFCA based on their scar assessment could be treated far less invasively using drug therapy. A standardized quantification of scar in DE-MRI is thus necessary.

### ACKNOWLEDGMENT

The authors would like to thank members of the Division of Biomedical Engineering and Imaging Sciences, King’s College London who assisted with this study. The views expressed are those of the author(s) and not necessarily those of the NHS, the NIHR or the Department of Health.

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