ORIGINAL RESEARCH ARTICLE

First-principles calculation of adsorption of shale gas on CaCO3 (100) surfaces

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Abstract

Background: To demonstrate the adsorption strength of shale gas to calcium carbonate in shale matrix, the adsorption of shale gas on CaCO₃ (100) surfaces was studied using the first-principles method, which is based on the density functional theory (DFT).

Methods: The structures and electronic properties of CH_a , C_2H_6 , CO_2 and N_2 molecules were calculated by the generalized gradient approximation (GGA), for a coverage of 1 monolayer (ML). Under the same conditions, the density of states (DOS) of CaCO₃ (100) surfaces before and after the adsorption of shale gas molecules at highsymmetry adsorption sites were compared.

Results: The results showed that the adsorption energies of CH₄, C₂H₆, CO₂ and N₂ on CaCO₃ (100) surfaces were between 0.2683 eV and -0.7388 eV. When a CH $_{\rm_4}$ molecule was adsorbed at a hollow site and its 2 hydrogen atoms were parallel to the long diagonal (H3) on the CaCO₃ (100) surface, it had the most stable adsorption, and the adsorption energy was only -0.4160 eV. The change of adsorption energy of CH₄ was no more than 0.0535 eV. Compared with the DOS distribution of CH₄ before adsorption, it shifted to the left overall after adsorption. At the same time, the partial density of states (PDOS) curves of CaCO₃ (100) surfaces before and after adsorption basically overlapped.

Conclusions: This work showed that the adsorption effect of shale gas on calcium carbonate is very weak, and the adsorption is physisorption at the molecular level.

Keywords: Adsorption energy, CaCO₃ (100) surface, First-principles, Shale gas

Introduction

Shale gas, as one of the global unconventional natural gases, has received extensive attention around the world. The United States and Canada have achieved commercial exploitation of shale gas with good results. China has done a lot of work with respect to shale gas research status, reservoiring mechanisms and favorable-area evaluation, but the study of the adsorption of shale gas was only just initiated in recent years (1, 2). The development from conventional oil and gas fields to shale gas fields actually reflects the scale transition from

Accepted: March 17, 2017 **Published online:** May 29, 2017

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micron to nanometer, and macroscopic breakthroughs have become increasingly dependent on microscopic studies. Therefore, it becomes particularly important to improve our microscopic understanding by using new theories and methods (3). Moreover, the study of shale gas molecule adsorption on shale substrate surfaces helps to understand the occurrence of shale gas, to assess the gas adsorption capacity quantitatively, to explore the correlation of adsorption properties and mineral composition and to evaluate the quantity of shale gas as a natural resource.

Shale gas is generally dry and mainly consists of CH₄, C₂H₆, CO_2 , N₂ and other components, with the content of CH₄ up to more than 95% (4, 5). The adsorption of shale gas and shale has been investigated through a large number of experimental and theoretical studies (6-12). Most of the theoretical studies show that shale gas is mainly absorbed on the surface of the kerogen and clay minerals, and is almost not adsorbed at all on the surface of calcium carbonate (13-16). Ji et al (5) studied methane adsorption on clay minerals of different sources and origins by isothermal adsorption experiment. The results showed that different types of clay minerals had evidently different gas adsorption capacities. However, there is no direct evidence of very weak gas adsorption on the surface of calcium carbonate.

At the same time, the first-principles method is used to study the adsorption of gas molecules on material surface (17-26), but there are few reports about the adsorption of gas molecules on the surface of calcium carbonate. Based on density functional theory with solid-state nuclear magnetic resonance (SS-NMR) calculations, Bevilaqua et al (27) simulated the adsorption of hydrocarbon molecules on calcite surface (CaCO₃(10 $\overline{1}$ 4)), but the adsorption of shale gas was not studied. In this paper, we adopted the first-principles method based on density functional theory (DFT) to study the adsorption stability of shale gas and its components at different high-symmetry positions on CaCO₃ (100) surfaces. By analyzing the adsorption results, such as the adsorption energy of gas molecules and the structure and electronic properties of $\textsf{CaCO}_3^{\text{}}$ (100) surfaces, we uncovered the microscopic mechanisms of shale gas adsorption on CaCO₃ surfaces.

Methods

Computational methods

Based on the first-principle method of DFT (28, 29), the ground state geometries and electronic properties of CH₄, C_2H_{6} , CO₂ and N₂ molecules adsorbed on CaCO₃ (100) were calculated using the Cambridge Sequential Total Energy Package (CASTEP) module in Materials Studio. Within the generalized gradient approximation (GGA), Perdew-Burke-Ernzerhof (PBE) (30) exchange correlation functionals combined with ultrasoft pseudopotentials were used in the calculations. The value of plane wave cutoff energy was 300 eV. The K point grid (31) size was $3 \times 1 \times 1$. Self-consistent field calculations were performed with a convergence criterion of 2.0×10^{-6} eV on single atom energy. The convergence of parameters was tested for each supercell. The Broyden-Fletcher-Goldfarb-Shanno (BFGS) optimization algorithm proposed by Broyden, was used in the structure optimization (32-35).

Structural models

In this paper, the P (1×1) periodic supercell is used as the initial surface. Under the coverage of 1 monolayer (ML), the adsorption of $CH_{\frac{4}{2}}$, $C_2H_{\frac{6}{2}}$, CO₂ and N₂ on the surface was theoretically studied for each. First, an optimized CaCO₃ unit cell (Fig. 1) was cleaved for a (100) surface. Then a vacuum layer of 2-nm thickness was constructed to simulate the CaCO₃ (100) surface (Fig. 2). Finally, the CaCO₃ (100) structure was optimized. We focused on shale gas molecule adsorption on CaCO₃ (100) surfaces. Therefore, in the structural optimization computation, the position of oxygen atoms was kept on the surface layer, and the number of adsorbed of shale gas molecules was variable, whereas the atoms of the non–surface layer were immobilized. We adopted such a setting to simulate the adsorption of CaCO_3^2 on shale gas molecules in order to reduce the number of calculations and to exclude the effect of substrate thickness. The initial lattice constant of calcium carbonate was an experimental value for, $a = 0.499$ nm, $c = 1.7061$ nm (36). After optimization, the lattice constant was $a = 0.499$ nm, $c = 1.7060$ nm. The gas molecules were added on the CaCO₃ (100) surface to a height of 0.5 nm.

Fig. 1 - Structural model of an optimized CaCO₃ cell with oxygen atoms (red), calcium atoms (green) and carbon atoms (gray).

Fig. 2 - Structural model of a CaCO₃ (100) surface supercell with vacuum layer.

In the structural model of $CaCO₃$ (100) surface supercell, there were 3 possible high-symmetry adsorption sites, the top (T), the bridge (B) and the hollow (H) part, in a parallelogram consisting of 4 oxygen atoms of surface (Fig. 3). The bridges included the short-side bridge (B1) and the long-side bridge (B2).

Due to the nature of parallelogram geometry, each gas molecule had 4 types of adsorption forms in the CaCO₃ (100) surface H site. As shown in Figure 4, H1 was parallel to the short edge of the parallelogram, H2 was parallel to the short diagonal, H3 was parallel to the long diagonal and H4 was parallel to the long edge. Similarly, T-type sites were denoted

Fig. 3 - High-symmetry adsorption site on p (1×1) CaCO₃ (100) surface: top (T) , short-side bridge (B1), long-side bridge (B2) and hollow (H).

Fig. 4 - Adsorption directions of H site.

by T1, T2, T3 and T4, and B-type sites were mainly related to the situation in which the adsorption of gas molecules was parallel to the short edge or long edge, and were designated as B11, B14, B21 and B24. Therefore, taking all of the possibilities into account, each gas species of CH₄, C_2H_{ϵ} , CO_2 and N₂ had 12 adsorption modes on the CaCO₃ (100) surface.

To analyze the adsorption stability of shale gas molecules on CaCO₃ (100) surfaces, the adsorption energy of gas molecules on $\widetilde{\mathsf{CaCO}}_{_3}$ (100) surfaces was calculated. The total energy of the system before adsorption was obtained by calculating the energy of $CaCO₃$ (100) surfaces and gas molecules. Then in the same way, the total energy of the system was calculated after adsorption. The equation to calculate the adsorption energy is given by

$$
\Delta E_{\scriptscriptstyle{\text{ad}}} = E_{\scriptscriptstyle{\text{gas}+CaCO_{3}}} - (E_{\scriptscriptstyle{\text{CaCO}_{3}}} + E_{\scriptscriptstyle{\text{gas}}}) \hspace{3cm} \text{Eq. [1]}
$$

where $E_{gas+CaCO_3}$ is the total energy of the system after gas adsorption, E_{cacc3} is the energy of pure CaCO₃ without the gas molecule, $\overline{\text{and}}^2 \text{E}_{\text{gas}}$ is the energy of the isolated shale gas molecule. The value of ΔE_{ad} reflects the stability of the adsorption system. ΔE_{ad} < 0 means that the energy of the system decreases after adsorption, and the gas molecules are adsorbed. The adsorption process is exothermic. $\Delta E_{ad} > 0$ means that the energy of the system increases, and the gas molecules cannot be adsorbed (37). A smaller value of ΔE_{ad} indicates better stability of the adsorption system.

Results and discussion

Analysis of adsorption energy

Table I lists the adsorption energy of CH_{4} , C_2H_{6} , CO_2 and N_2 molecules on CaCO₃ (100) surfaces in the 12 adsorption modes. CH₄, C₂H₆ and N₂ molecules had negative ΔE_{ad} , and the lowest adsorption energy was -0.4160 eV, -0.7388 eV and -0.1567 eV, respectively. The adsorption capacity of 3 kinds of

TABLE I - Adsorption energy of CH_{4} , C_2H_{6} , CO_2 and N_2 molecules on 12 types of adsorption sites on $CaCO₃$ (100) surfaces

Adsorption energy (eV)			
CH ₄	C_1H_6	CO ₂	N,
-0.3886	-0.7087	0.1872	-0.0855
-0.3625	-0.6933	0.1463	-0.1567
-0.3676	-0.7260	0.1619	-0.1505
-0.3855	-0.7022	0.1871	-0.1032
-0.3967	-0.7382	0.1672	-0.0903
-0.3721	-0.7388	0.2044	-0.1279
-0.4034	-0.6370	0.1679	-0.0805
-0.4085	-0.6211	0.2683	-0.1243
-0.4080	-0.6214	0.1361	-0.0971
-0.4107	-0.6849	0.1521	-0.1363
-0.4160	-0.6592	0.1127	-0.1312
-0.4137	-0.6286	0.2033	-0.1195

 $T1$ = on the top site and parallel to the short edge of the parallelogram; T2 = on the top site and parallel to the short diagonal; T3 = on the top site and parallel to the long diagonal; T4 = on the top site and parallel to the long edge; B11 = on the short side bridge site and parallel to the short edge; B14 = on the short-side bridge site and parallel to the long edge; B21 = on the longside bridge site and parallel to the short edge; B24 = on the long-side bridge site and parallel to the long edge; H1 = on the hollow site and parallel to the short edge of the parallelogram; H2 = on the hollow site and parallel to the short diagonal; H3 = on the hollow site and parallel to the long diagonal; H4 = on the hollow site and parallel to the long edge.

Fig. 5 - Bar chart of adsorption energy of CH₄ at various adsorption sites on the CaCO₃ (100) surface.

gases on the surface of calcium carbonate follows the order of $C_2H_6 > CH_4 > N_2$. However, the ΔE_{ad} of CO_2 was positive, which means that CO_2 molecule cannot be adsorbed on the surface of calcium carbonate. Therefore, the adsorption of $CO₂$ is not discussed in the following.

Since the percentage of $CH₄$ is dominant in shale gas, the adsorption energy of CH₄ molecular was compared for different adsorption sites to analyze the stability of shale gas molecules adsorbed on CaCO₃ (100) surfaces, as shown in Figure 5. It can be seen that CH₄ molecules had the lowest $\Delta \mathsf{E}_{_{\mathsf{ad}}}$ at the H3 site.

From the point of view of the quantity of adsorption energy, CH₄ molecules had a minimum adsorption energy of -0.4160 eV on H3, which was the most stable adsorption structure among the 12 high-symmetry sites (Fig. 6). Therefore, it is relatively easier for CH₄ molecules to be adsorbed on H3. When adsorbed on T2, CH_4 molecules had a maximum energy of -0.3625 eV, which means that it was most difficult for T2 to adsorb CH_4 molecules. Similarly, C_2H_6 molecules had their minimum adsorption energy and most stable adsorption structure at B14, which was the position for easiest adsorption. B24 had the maximum energy and the most unstable adsorption structure. At T2, N_2 molecules had their minimum adsorption energy, and could be easily adsorbed at T2. B21 was the most difficult position to adsorb N_2 molecules. The small absolute values of adsorption energy indicate very weak adsorption of CH₄, C₂H₆ and N₂ molecules on $CaCO₃$ (100) surfaces.

In terms of the range of adsorption energies, the adsorption energy of CH $_{\textrm{\tiny{4}}}$ at different sites ranged from -0.3625 eV to -0.4160 eV, with the largest difference being only 0.0535 eV. Besides, the largest differences of the adsorption energy ranges for C_2H_6 and N_2 molecules were only 0.1177 eV and 0.0762 eV, respectively. The range of adsorption energies was very small, which indicates that the adsorption of each gas molecule at the high-symmetry sites on CaCO₃ (100) surfaces was very similar, and the gas molecules tended to move on the calcium carbonate surfaces. By comparison, it is known that the mobility of CH₄ is the strongest.

Fig. 6 - Structural model of CH₄ molecule adsorbed at H3 site on $CaCO₃$ (100) surface.

Analysis of physical structure

In Table II, we can see that after $CH₄$ molecules were adsorbed at H3 sites, the C-H bond length became 0.1097 nm, which is in good agreement with the experimentally spectroscopic data of 0.1086 ± 0.0001 nm (38). Compared with the value before adsorption, the bond length changed by 0.091%, and bond angle changed by 0.779%.

Similarly, the physical structure was analyzed for C_2H_6 and N_2 before and after adsorption. The relative changes were 1.422% and 1.400% for C=C bond length and H-C-H bond angle of C_2H_{6} , respectively. The N≡N bond length increased by 1.396% after N_2 was adsorbed. It was found that the structures of CH₄, C₂H₆ and N₂ molecules showed negligible changes, so the adsorption effect was weak on the CaCO₃ (100) surface.

Analysis of density of states

The CASTEP module can analyze the band structure, electronic density of states (DOS), optical properties, phonon dispersion relations, phonon DOS and stress before and after the optimization of the physical model. Here we mainly discuss the electronic DOS changes and their effect on adsorption. According to the analysis of the DOS changes for CH_{α} , C_2H_g , N₂ and CaCO₃ (100) surfaces before and after adsorption, the interactions between shale gas molecules and $CaCO₃$ (100) surface can be further understood.

TABLE II - Changes of bond length and bond angle of CH₄, C₂H₆ and N₂ molecules on CaCO₃ (100) surfaces after adsorption

* Situation for the most stable adsorption position.

⁺The bond lengths were C-H for CH₄, C = C for C₂H₆, N = N for N₂.

 * The bond angles were C-H for CH $_{_{4}}$ and C₂H₆, N $\stackrel{.}{=}$ N for N₂.

Fig. 7 - Density of states (DOS) of CH₄ molecules before and after adsorption at H3 site and T2 site. The black dotted line indicates the Fermi level.

In Figure 7, the DOS of CH₄ before and after adsorption at H3 and T2 is compared. The black curve represents the electronic DOS before adsorption, the red curve represents the electronic DOS after adsorption at H3, and the blue curve represents the electronic DOS after adsorption at T2. The vertical dashed line at 0 eV indicates the Fermi level. It can be seen that whether adsorbed at H3 or T2, the electron DOS curves of CH_4 molecules shifted to the left overall after adsorption. The adsorption energy decreased, and the electronic structure became more stable, which shows that the adsorption had a significant influence on the distribution of electron DOS of CH₄ molecules. Besides, the DOS curve of H3 has 2 peaks, at -12.77 eV and -5.18 eV, which move to the left about 0.3 eV compared with those of T2 at -12.47 eV and -4.88 eV. It is thus proven that the adsorption of $CH₄$ molecules on CaCO₃ (100) surface high-symmetry sites is basically from the point of view of electronic structure, and has better mobility on the surface of the calcium carbonate.

Figure 8 shows the partial density of states (PDOS) of oxygen atoms in CaCO₃ (100) surface before and after the adsorption of CH₄ molecules at H3 under the coverage of 1 ML. The contribution of *s* electronic states and *p* electronic states to the total density of states in energy regions is different. When the energy is greater than -10 eV, the *p* electronic states (red curve) play a major role in the total electron density. When the energy is less than -10 eV, the *s* electronic states (blue curve) play a major role in the total

electron density. Before adsorption, the *s* electronic states energy is mainly continuously distributed in the ranges of 0 eV to -9 eV and -17 eV to -24 eV, and there are 7 peaks in the 2 intervals. While *p* electronic states energy is mainly continuously distributed in the ranges of 2 eV to -9 eV and -17 eV to -24 eV, and there are 9 peaks in the 2 intervals. After adsorption, the PDOS of *s* electronic state of oxygen atoms basically coincides with that of the state before adsorption, as does that of the *p* Electronic State. This suggests that there is no chemical bond formed between $CH₄$ molecules and the oxygen atoms on $CaCO₃$ (100) surfaces. This indicates that the adsorption of CH_4 on calcium carbonate surfaces is mainly affected by the Van Der Waals force, and it is physical adsorption. To better illustrate this point, we compared the DOS of CaCO₃ (100) surfaces with the different shale gas molecules adsorbed, as shown in Figure 9.

Figure 9 presents the DOS of CH₄, C₂H₆ and N₂ adsorbed on a CaCO₃ (100) surface. We can see that the adsorption of different gas molecules on the CaCO₃ (100) surface has similar effects on the electronic structure of the oxygen atom on the $CaCO₃$ (100) surface. After adsorption, the 3 DOS curves almost overlap, indicating that C_2H_6 and N_2 molecules have similar adsorption effects on oxygen atoms on the CaCO₃ (100) surface to those of the CH_4 molecule, and the adsorption of the 3 kinds of gas molecules on the CaCO₃ (100) surface are physical.

Fig. 8 - Partial density of states (PDOS) and density of states (DOS) of oxygen atoms in CaCO₃ (100) surface before and after the adsorption of CH4 molecules on the H3 site. (**A**) Before adsorption and (**B**) after adsorption.

Fig. 9 - Density of states (DOS) of oxygen atoms on $CaCO₃$ (100) surface after the adsorption of CH₄, C₂H₆ and N_2 molecules at the most stable adsorption sites.

Conclusions

Using the first-principle method based on DFT, we established adsorption models for CH₄, C₂H₆, CO₂ and N₂ on CaCO₃ (100) surfaces, and calculated the corresponding adsorption energies. The adsorption abilities of CH₄, C₂H₆ and N₂ molecules on the CaCO₃ (100) surface were weak. CO₂ molecules could not be adsorbed. The adsorption abilities of the different molecules were different. The adsorption ability of hydrocarbon gas was stronger than that of nonhydrocarbon gas, and the adsorption ability of $\mathsf{C}_\mathrm{2}\mathsf{H}_\mathrm{6}$ was stronger than that of CH_4 . In addition, the adsorption energy of different gas molecules varied over the range of sites and followed the order of CH_4 < N_2 < C_2H_6 . The change of CH₄ was the smallest, indicating the best mobility of CH₄ molecules on the surface of calcium carbonate. This may be due to the fact that the methane molecule has the smallest relative molecular mass.

We also analyzed the electronic structures of the adsorption systems. After adsorption, the changes of geometric structures of the molecules were small and the electron DOS of atoms in the CaCO₃ (100) surface was basically unchanged. The findings above show that the adsorption of shale gas molecules on the surface of calcium carbonate is physical.

Acknowledgements

The authors would like to acknowledge the assistance of A.P. Li P. Chen for English correction.

Disclosures

Financial support: This work was supported by the Young Scientists Fund of the National Natural Science Foundation of China (grant no. 51204141), the Major Program of the National Natural Science Foundation of China (grant no. 51374179), the Southwest Petroleum University Foundation (grant no. 2014QHS009, 2015JXYJ-07) and the Open Research Fund of the Computational Physics Key Laboratory of Sichuan Province (grant no. JSWL2014KF03).

Conflict of interest: The authors declare they have no conflicts of interest.

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