A probabilistic generative model for GO enrichment analysis

Yong Lu¹, Roni Rosenfeld², Itamar Simon³, Gerard J. Nau⁴ and Ziv Bar-Joseph^{1,2,*}

¹Computer Science Department, ²Machine Learning Department, Carnegie Mellon University, 5000 Forbes Ave, Pittsburgh, PA, 15213 USA, ³Department of Molecular Biology, Hebrew University Medical School, Jerusalem, Israel 91120 and ⁴Department of Molecular Genetics and Biochemistry, University of Pittsburgh Medical School, Pittsburgh, PA 15213, USA

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ABSTRACT

The Gene Ontology (GO) is extensively used to analyze all types of high-throughput experiments. However, researchers still face several challenges when using GO and other functional annotation databases. One problem is the large number of multiple hypotheses that are being tested for each study. In addition, categories often overlap with both direct parents/descendents and other distant categories in the hierarchical structure. This makes it hard to determine if the identified significant categories represent different functional outcomes or rather a redundant view of the same biological processes. To overcome these problems we developed a generative probabilistic model which identifies a (small) subset of categories that, together, explain the selected gene set. Our model accommodates noise and errors in the selected gene set and GO. Using controlled GO data our method correctly recovered most of the selected categories, leading to dramatic improvements over current methods for GO analysis. When used with microarray expression data and ChIP-chip data from yeast and human our method was able to correctly identify both general and specific enriched categories which were overlooked by other methods.

INTRODUCTION

High-throughput experiments in molecular biology are enabling researchers to obtain large quantities of data. In many cases these datasets are in the form of lists of genes (for example, differentially expressed genes or targets of a transcription factor). However, due to the size of the resulting lists it is often hard to manually inspect them to characterize the functional outcome of the experiment. To overcome this challenge researchers have been

increasingly relying on automated analysis using curated databases of functional annotations. These include the Gene Ontology (GO) (1) and the MIPS (2) databases, among others. In these databases, genes are annotated by standardized terms (for example, GO categories) indicating their known functions or related biological processes. The popularity of this type of analysis is evident from its wide use in almost all types of high-throughput experiments, including large-scale sequencing efforts (3,4), microarrays (5,6), protein–protein interactions (7–9), protein–DNA interactions (10,11), knockouts (12) and many more.

While using curated databases to analyze highthroughput experiments has led to some success, there are many challenges facing researchers trying to use these databases. Multiple hypothesis testing is often an issue since GO contains thousand of categories which are all tested for enrichment for the same gene set (13). While this issue can be addressed by statistical correction methods, other problems remain unsolved. The categories to which genes are assigned are not independent, making it hard to determine if a set of identified significant categories represents a set of different functional outcomes or rather a redundant view of the same biological process. For example, GO categories are organized into a hierarchy with more general categories close to the root and more specific categories at the bottom. Genes annotated by a specific term are implicitly annotated to all parent terms, resulting in highly overlapping categories. Thus, if an intermediate node is determined to be significant it is often the case that many nodes below it would also be significant. In addition, many genes are annotated to multiple categories that do not share a directed path in the GO hierarchy, resulting in overlapping categories that cannot be detected using the hierarchical structure. Indeed, when using GO to compute hypergeometric P-values, which is the most common method used, researchers often recover several redundant categories as the top hits (14,15; see also Table 1 and Supplementary Tables 3–6) which both masks

^{*}To whom correspondence should be addressed. Tel: +1 412 268 8595; Fax: +1 412 268 3431; Email: zivbj@cs.cmu.edu

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Table 1. Categories for cell cycle experiments

Classic	Parent-Child	Elim	Weight	GenGO
Mitotic cell cycle DNA replication	Cell cycle Cell cycle process	Microtubule nucleation Mitotic sister chromatid cohesion	Microtubule nucleation Mitotic sister chromatid cohesion	Mitotic cell cycle DNA replication
Cell cycle	DNA metabolic process	Mitotic spindle organization and biogenesis	DNA strand elongation during DNA replication	Microtubule-based process
Cell cycle process	Microtubule-based process	DNA replication initiation	Mitotic spindle organization and biogenesis	Cell division
DNA-dependent DNA replication	DNA replication	Telomere maintenance via recombination	Telomere maintenance via recombination	Chromatin assembly or disassembly

Top five GO categories identified by different methods from the list of periodically expressed yeast genes during the mitotic cell cycle (18).

other important categories and makes it hard to determine the most relevant category.

These problems with GO have been recognized and a few methods were developed to address them. One of the first attempts was the use of 'GO Slim' (http://www. geneontology.org/GO.slims.shtml), a leaner version of GO containing a manually picked small set of categories (130 of the current \sim 24 000 categories in GO) with a small overlap between them. While useful, this method only retains the general categories and does not provide more specific ones which are often most interesting to biologists. Other attempts were proposed by a few recent papers. Grossmann et al. (14) recomputed the P-value for a specific category by taking into account the immediately more general terms (the parents). This can often lead to the removal of false positives, since some of the more specific categories are eliminated if their parent category is determined to be significant. Alexa et al. (15) proposed two algorithms to correct the P-values for a specific GO term. The first algorithm, 'Elim', tests the enrichment of each GO category in a gene set by examining the GO hierarchy in a bottom-up order. Once a GO category is determined to be significant, all genes associated with it are removed in the following analysis of its ancestral (more general) categories. The other algorithm, 'Weight', uses a similar strategy but rather than completely removing genes in significant categories it down-weights them for the remaining categories.

While these methods are more powerful, they only utilize local information in the graph structure (parent-child or bottom-up). Thus, they cannot account for longer range relationships and global dependencies such as highly overlapping categories that do not share a directed path. In addition, all the aforementioned methods return a (sometimes long) list of GO categories with their *P*-values requiring the user to select a cutoff in order to further analyze the resulting list.

Our approach is different. From a biological point of view, one of the goals of using functional databases is to identify a set of biological processes related to the specific study. Thus, it would be natural to identify the set of significant GO categories and processes that 'generated' the observed list. This leads us to use a generative model for this task. A generative model is a computational model that assumes that the observed data is sampled from (or was generated by) some distribution. The observed

data is then used to estimate the parameters of the distribution and to infer values that could not be directly observed. In this case the parameters we are interested in relate to the noise and incompleteness of the genomic data and the GO hierarchy and the missing observations are the GO categories that are related to the experimental study. Our goal is to identify a (preferably small) set of categories that together account for the set of genes observed. Since many experiments study complicated responses involving several processes, the categories can come from different locations and levels in the hierarchy. However, highly overlapping and redundant categories will not be selected since one of them is often enough to explain the subset of the genes belonging to these categories.

We applied our method, which we term GenGO (GENerative GO analysis), to analyzing the GO hierarchy for yeast and humans. We used a controlled analysis (in which subsets of categories are selected and the goal is to recover the (hidden) categories), microarray expression data and ChIP-chip data for both species. GenGO was able to drastically reduce the false positive rates, even after statistical correction. As we show, GenGO consistently outperforms both the original hypergeometric method and the methods considering only local structural dependencies, in some cases dramatically so.

MATERIALS AND METHODS

The activation graph for GO categories

We developed a generative model to identify a subset of active GO categories. A generative model is a model that assumes that the observed data is sampled from (was generated by) some distribution. That data is then used to estimate the parameters of the distribution, by providing either a point estimate or a Bayesian posterior. These estimates can then be used to infer missing observations. Unlike discriminative models (that are commonly used for classification) generative models make explicit assumptions about how the data was generated. Thus, generative models can be superior when the assumptions are at least approximately correct. In this case we could rely on knowledge regarding the possible noise sources for specifying our generative model.

When designing the method we placed special emphasis on simplicity and speed. GO analysis is often an

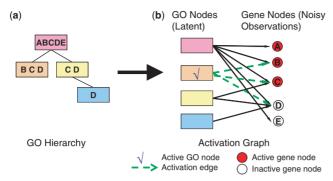


Figure 1. Construction of an activation graph. (a) A diagram showing a GO hierarchy of four categories and the five genes annotated by these categories (letters in each rectangle). Because of the 'true path' rule, each gene annotated by a category in the GO hierarchy is also annotated by all its parent categories. (b) The activation graph corresponding to this GO hierarchy when observing three of the genes (A,B,C). In this graph, we connect a gene node with a GO node if and only if the gene is annotated by that GO category. For this set of genes the active category is determined to be the orange category. Note that due to noise there is a gene that is selected even though it does not belong to the active category (A). Noise is also responsible for the fact that a gene belonging to the active category is not selected (D).

interactive process in which users change their lists, or analyze multiple lists (for example, different gene clusters or different targets of transcription factors). Thus for a method to be successful it should be computable in a reasonable time to allow interactive analysis.

To explain our method, one can think of this problem in terms of a bi-partite graph representing the relationships between GO categories and genes (Figure 1). Nodes on the left side of the graph represent GO categories and nodes on the right represent all genes annotated in that species. We connect a gene node with a GO node by an edge if and only if the gene is annotated to belong to that GO category. We denote genes that were identified in the experiment as 'ON' or active and genes that were not identified as 'OFF' or inactive. Similarly, when a biological process (corresponding to a specific GO category) is active, we represent it by setting its GO node to 'ON' and when it is inactive, we set its state to 'OFF'.

To find this set we define a probabilistic model on the activation graph (containing both gene and GO nodes). The model accounts for noise in the experimental and GO data. We develop an algorithm that identifies active GO categories by maximizing the likelihood of this model conditioned on the set of active genes. The final outcome is a small subset of active GO nodes that together explains the set of active genes. We describe the model in details in the following sections.

Probabilistic model for activation graphs

We assume a generative model for gene activation. In this model we first select a subset of GO categories and activate all genes in these categories. Next, a random process (representing noise, errors in GO assignments and partial knowledge) inactivates, with probability 1-p, genes in each of the selected categories and activates, with probability q, genes in categories that were not selected leading to the observed gene set. Given a list of active (selected)

genes and a set of active GO categories, we can define the following sets:

- (i) A_g —active gene nodes connected to at least one active GO node
- (ii) A_n —active gene nodes not connected to any active GO nodes
- (iii) *I*—inactive gene nodes
- (iv) S_{σ} —edges connecting nodes in I with active GO
- (v) S_n —edges connecting nodes in I with inactive GO nodes

Using these symbols we define the following log-likelihood function which we would like to maximize:

$$L(C | p, q, G) = |A_g| \log p + |A_n| \log q + |S_g| \log(1 - p) + |S_n| \log(1 - q) - \alpha |C|$$

where G is the set of active (selected) gene nodes (the input), C is the set of active GO nodes, and |X| represents the size of the X group $(A_{\sigma}, A_{\eta}, \text{etc.})$. This function captures our generative model. With probability P genes belonging to active categories would remain active (A_a) . With probability q genes that do not belong to any active category would be activated (A_n) . Similarly, with probability 1-pgenes in active categories will become inactive (S_{σ}) and with probability 1-q genes in inactive categories will remain inactive (S_n) . The last term in the likelihood function penalizes the size of the set of active GO categories (|C|) so that the model will prefer a smaller set of categories when explaining the selected set of genes. The hyperparameter α is a positive number controlling the penalization. See Supplementary Material for examples illustrating the differences between this likelihood function and using the classic hypergeometric method.

Note that the likelihood function formulated above discourages the identification of highly overlapping and redundant categories. For such categories it is usually enough to select one category to account for the observed genes from both categories. Selecting the second would not increase the contribution from the active genes (since these are already accounted for by the first category) and would lead to penalty for both the non active genes from the second category and the addition of another category to the active GO set (using the \alpha penalty parameter). Thus our method would select the best category that fits the data resulting in a small and unique set of GO categories for each experiment.

The above likelihood model is a function of the selected set of active GO categories (denoted by C). In the next section we present an algorithm for finding such a set that maximizes this likelihood. We also present a method for optimizing the values for the noise parameters p and q. Once the algorithm terminates we compute a P-value score for each of the selected categories using hypergeometric distribution and return an ordered list of selected categories to the user.

Optimization by greedy search

Given an input list of active genes, we would like to determine a set of active GO categories (C) that maximizes the likelihood function (1). This is an NP-hard problem as we discuss in Supplementary Methods. Thus, we use a simple and fast greedy search algorithm to look for a local maximum of the likelihood function. At each iteration, the algorithm searches for categories to add to (or remove from) to the current set of active categories in order to improve the global likelihood. If such categories exist, the one leading to the highest improvement in likelihood is added to (or removed from) to the set and the search continues. Otherwise the current set is retuned as the optimal set of active categories.

The algorithm is as follows (p and q are fixed in this part: they can either be optimized in an outer loop as we discuss below or set by the user in advance.).

Algorithm 1 (Find the best GO set for given parameters)

- (1) Initialize C_0 to be the empty set
- (2) At iteration i, we consider all possible one-step changes of the current set of active GO categories (C_i) , and compare the likelihood of the resulting sets. Let

$$t_1^i = \underset{t \in C_i}{\operatorname{arg\,max}} L(C_i \setminus \{t\}) \text{ and } t_2^i = \underset{t \in T \setminus C_i}{\operatorname{arg\,max}} L(C_i \cup \{t\}),$$

where T is the set of all GO categories. Thus among all possible reductions of C_i , $C_i^- = C_i \setminus \{t_1^i\}$ has the highest likelihood. Similarly, among all possible expansions of C_i , $C_i^+ = C_i \cup \{t_1^i\}$ has the highest likelihood.

- (3) If the likelihood of C_i^- is higher than that of both C_i^+
- and C_i , let $C_{i+1} = C_i^-$ go to Step 2. (4) If the likelihood of C_i^+ is higher than the likelihood of C_i , let $C_{i+1} = C_i^+$ go to Step 2. Otherwise go to the next step.
- (5) Return C.

It is important to note that including more GO categories will not necessarily lead to improved likelihood and thus the algorithm above does not overfit the data. The reason for this is that any category that is added must also account for all genes that are included in that category and were not selected. Adding a category for which many of its genes were not selected or if they were selected they are already explained by other selected categories will usually lead to reduction in the likelihood.

Once the algorithm terminates, we use the set of active categories as the final result. For these categories, we compute a P-value using the hypergeometric distribution and return the list, ordered by the P-value significance score, to the user. Corrected P-values can also be computed either by using the Bonferroni correction or by carrying out randomization tests (16).

Optimizing parameters

There are two parameters in our model, p and q. p is the probability that an active GO node will activate a gene belonging to that GO category and q is the probability that a gene node becomes active without being activated by any GO node. A higher p means a higher participation rate of the related genes in the biological process, and/or less uncertainty in the activation relation between a GO node and the related GO nodes. A higher q means a larger portion of the genes are allowed to be explained by background noise or errors in the current ontology. p and q can be set manually according to the estimation of noise level. Alternatively p and q can be learned from the data. See Supplementary Methods for details. The hyperparameter α can be chosen by experiments and we found it generally works well when we set $\alpha = 3$.

GO annotation data

GO files (release 2007-06) were downloaded from the GO website (ftp://ftp.geneontology.org/). GO annotations for humans and yeast were extracted from the Gene2GO database, which was downloaded from the NCBI website (ftp://ftp.ncbi.nlm.nih.gov/) on 26 June 2007. GO categories were filtered such that only those with at least 5 genes would be used. In this study, we focused on the biological process categories, but our methodology is also applicable to Cellular Component and Molecular Function categories.

Precision/recall curves

Precision/recall plots were done using the ROCR package in R (http://www.r-project.org/). Each point in the precision/recall curve corresponds to a score (or P-value) cutoff. The precision and the recall are defined as follows:

$$Precision = \frac{TP}{(TP + FP)}$$

$$Recall = \frac{TP}{(TP + FN)},$$

where TP is the number of true positives (true active categories below the cutoff), FP is the number of false positives (inactive categories below the cutoff), and FN is the number of false negatives (true active categories above the

Precision/recall curves are more informative than receiver operating characteristic (ROC) curves when working with highly skewed datasets (17). This is exactly the case when working with GO enrichment analysis in which the vast majority of categories are not expected to be enriched for any one dataset.

Comparison

For comparison with the Classic method we used the hypergeometric p-value analysis from STEM (16). We used the Parent-Child method implemented by Ontologizer (http://www.charite.de/ch/medgen/ontologizer/recomb06/ index.html), and the Weight and Elim methods implemented in the current release of topGO (R 2.5.1, topGO 1.2.1). For both Classic and Parent-Child methods, P-values are computed with Bonferroni correction, which is a commonly used method for multiple testing corrections.

In every GO analysis task we performed for a species, we used the whole set of annotated genes as the reference set. To generate the precision/recall curve for a method in a specific experiment, we followed the strategy in Grossmann et al. (14) and accumulated all P-values from 100 random gene sets.

Ranking induced genes in amino acid starvation

For each yeast gene in the amino acid starvation experiment, we looked at its second highest expression level throughout the whole time series, and ranked all genes according to this value.

GO hierarchy figures

GO hierarchy figures were generated with QuickGO (http://www.ebi.ac.uk/ego/).

RESULTS

Comparison by selecting a subset of categories

We first tested our method (GenGO) using GO data for yeast and humans. We followed the same procedures in Grossmann et al. (14) and Alexa et al. (15) for objective comparison of different GO analysis methods. For each species, 1, 2 or 5 GO categories were randomly selected as 'active', and a subset of genes associated with each active category were randomly picked (90 or 50% of genes in each of the selected categories). In addition, we randomly selected 1 or 15% of the remaining genes (from inactive categories) and combined the two sets from active and non-active categories to form the input to the GO analysis. Due to the large run time of some of the methods we were comparing to (Elim and Weight), for each experiment, 100 random sets were generated using the same parameters. Supplementary Figures 1 and 2 present results for tests carried out on a larger random set for the faster methods.

We used precision/recall curves to compare GenGO with four other methods (see Materials and methods section). These included 'Classic' (hypergeometric test) and the three other methods listed above. The results are plotted in Figure 2 (yeast) and Figure 3 (human). For all settings, the performance of GenGO dominates all other methods. When the noise level is low, the performance of GenGO is close to optimal (top rows in Figures 2 and 3). When the noise level is high, the performance drops for all methods, though GenGO is still the best. Even with high noise and multiple categories (as is the case for most real experiments) GenGO can achieve 80% precision for high recall levels (60–80%). As for the other methods, in most cases 'Weight' is the second best and 'Classic' is usually the worst, indicating that all methods previously proposed for the task indeed improve upon the standard usage of GO.

Note that while the precision usually drops as the recall increases, there could be cases where the precision actually improves even though recall is increasing. For example, in Figure 2a the 'GenGO' method correctly assigns the lowest P-values to some of the selected categories, which results in a very high precision rate at low recall rates. However, when the recall increases to 0.1, due to some non-selected categories that are (incorrectly) assigned a low P-value, the precision drops to 0.9. As the recall continues to increase, the precision increases again because the method recovers the rest of the selected categories without picking up much non-selected categories.

Analysis of noise datasets

To test the ability of GenGO to overcome the multiple hypothesis testing problem, 1, 5 and 10% of all human genes were randomly selected as a test set, and the five algorithms were run to identify significant categories. The procedure was repeated 100 times, and the percentages of sets without any significant GO categories (P-value < 0.001 with Bonferroni correction where applicable) are listed for each of the methods in Supplementary Table 1. Even after correction the Classic method, which is the most commonly used, identified significant categories in all experiments. When 10% of the genes were selected at random, all methods, except for GenGO identified significant categories in at least 50% of the experiments. In contrast, GenGO was able to determine that no such significant category exists for >98% of tested noise sets.

In addition, we used a similar procedure to test for noise sets randomly selected from different branches of the GO hierarchy. 0.1, 0.2 and 0.5% of genes from each of the Level 2 categories ('biological_process' being at Level 1) were randomly selected, and the five algorithms were run to identify significant categories. The results are presented in Supplementary Table 2. As the percentage of genes selected decreases, it becomes easier for all methods to determine that there are no significant categories. However, even with 0.2% of genes selected in this way, all methods except GenGO and Parent-Child wrongly identified significant categories in at least 77% of the experiments.

Comparison on microarray experiment for yeast

Testing GenGO using real expression data is more challenging since the 'ground truth' is unknown in most cases. Still, when the biological condition is clearly defined, it is possible to determine whether a set of GO categories provides a good summary of the experimental setup.

Cell cycle. We have initially applied GenGO to analyze the well studied cell cycle expression dataset from Spellman et al. (18). We used the 800 genes determined to be cycling during the mitotic cell cycle in budding yeast. Figure 4 plots the location in the GO hierarchy of the top five categories identified by four of the five methods (see also, Table 1 and Supplementary Figure 3). The results highlight the advantages of GenGO. For example, while both GenGO and Classic successfully identify 'mitotic cell cycle' as the most significant category, the Classic method returns highly redundant categories including 'mitotic cell cycle', 'cell cycle process', and 'cell cycle'. The Parent-Child method (14) also returns redundant categories ('cell cycle process', and 'cell cycle') though it does a better job in finding the more specific 'microtubule-based process' which is related to cytoskeleton changes during cell cycle progression (18). Both Elim and Weight fail to identify the most appropriate category for this data (cell cycle) though they do identify a number of relevant specific categories. In contrast, GenGO contains both the correct high level categories ('cell cycle' and 'cell division') as well as more specific categories ('chromatin assembly or disassembly') that play an important role in DNA replication and chromosome segregation. Note that cell division

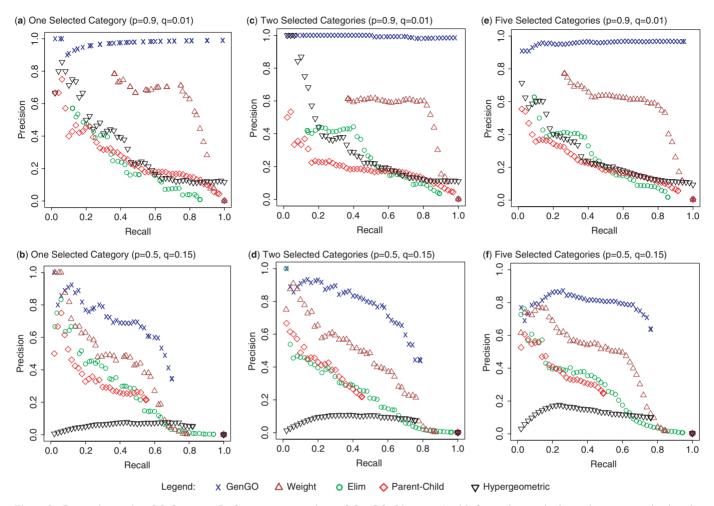


Figure 2. Comparison using GO for yeast. Performance comparison of GenGO (blue curve) with four other methods on data generated using the yeast GO database. We use p to represent the fraction of genes that are identified from an active GO category (true positive rate for a category, see Materials and methods section) and q to represent the fraction genes that are selected but do not belong to any active category. (a) Selecting one category with p = 0.9, q = 0.01; (b) Selecting one category with p = 0.5, q = 0.15; (c) and (d) Same as (a) and (b) but using two categories; (e) and (f) same with five categories. Note that even when the noise is substantial (using 50% of genes in selected categories and 15% of all other genes, bottom row) GenGO is still able to accurately recover most of the correct categories. See Supplementary Figure 1 for a more detailed figure.

here is not redundant with cell cycle. While 'cell cycle' describes the different phases of the cell cycle, their regulation, and checkpoints, 'cell division' refers to the process of separation of daughter cells following the cell cycle. See Supplementary Table 3 for additional analysis of genes associated with specific cell cycle phases.

Amino acid starvation. We repeated the above analysis using the top 500 induced genes in amino acid starvation experiments (19). Only GenGO and Weight correctly identified 'amino acid biosynthetic process' as the most signifcategory (Supplementary Table Supplementary Figures 4–8). The next significant category identified by GenGO is 'sulfur metabolic process'. It includes genes required in recycling sulfur metabolites, which are known to be highly expressed under amino acid starvation (20). In addition, an interesting finding by GenGO is 'monosaccharide catabolic process'. During amino acid starvation, besides the lack of amino acid there is a cellular need to produce energy which is carried out mainly by this process (21). Another category identified by GenGO, 'amino acid catabolic process', describes the process that generates amino acids from existing proteins, which is a known consequence of amino acid starvation. In contrast, the categories identified by Elim are too specific: three of the five categories are subcategories of 'amino acid biosynthetic process' and can be better summarized by the latter. The Classic method again identifies redundant categories: 'organic acid metabolic process', 'carboxylic acid metabolic process', and 'amino acid metabolic process'.

Analysis of human expression data

We repeated the analysis described above using human immune response experiments from Nau *et al.* (22). A total of 977 genes were identified as differentially expressed when host cells were exposed to one or more bacterial pathogens. For this set all methods have correctly identified 'immune response' in the top two categories (Table 2). However, as was the case for yeast, the Classic method returned many redundant categories.

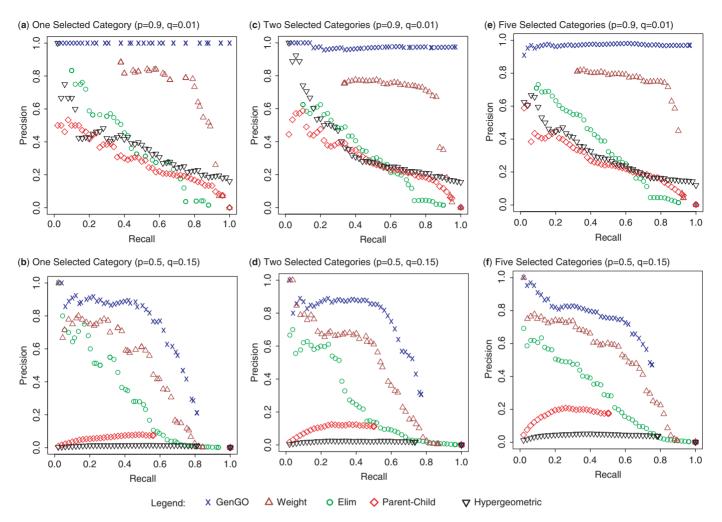


Figure 3. Comparison using GO for human data. Performance comparison of five methods on data generated using human GO database. (a-f) Same as in Figure 2 for human GO data. See Supplementary Figure 2 for a more detailed figure.

Parent-Child returned two very general categories ('biological process' and 'regulation of biology') which do not provide insight into the set of genes. Interestingly, both Elim and Weight identified 'response to virus', as one of the top five categories. Since only bacteria were used in this study this category should not have been identified. It was likely selected by these methods due to its overlap with the more general 'immune response' category. In addition to the 'immune response' and 'wound response' categories identified by GenGO it also identified 'taxis' that is clearly relevant due to the mobility need for macrophages during immune response (23). GenGO also identified 'regulation of apoptosis' that plays an important role in determining the drastically different fates for macrophages after infection (24-26). The final category identified, 'tRNA aminoacylation' is the process that joins an amino acid to its cognate tRNA, which is an important step in protein translation (27).

Application to ChIP-chip data analysis

ChIP-chip experiments (28) are used to experimentally identify the targets of transcription factors. These targets can later be used to shed light on the functional role of that factor, which can be done by using GO to determine the function of the resulting gene target set (29). We have compared the GO enrichment analysis of the different methods for the targets of transcription factors from yeast and human.

For yeast, we have looked at Swi6, a cell cycle regulator of G1 transcription (30). Supplementary Table 5 presents the results of the five methods for this factor and Supplementary Figures 9–13 present their GO enrichment hierarchies. Except for Elim and Weight, which did not return 'cell cycle' in their top five hits, the three other methods correctly selected this as the top category for Swi6. However, the hypergeometric and parent-child again returned a set of redundant categories ('cell cycle', 'cell cycle process'). In contrast, GenGO was able to balance the more detailed and the more high-level categories. Specifically it was the only one to correctly identify 'reproduction' as one of the top categories for Swi6, a role that is well documented (31).

We have also looked at the analysis of targets of E2F1, a human cell cycle regulator. Ren et al. (32) have studied the targets of E2F1 and based on their detailed analysis

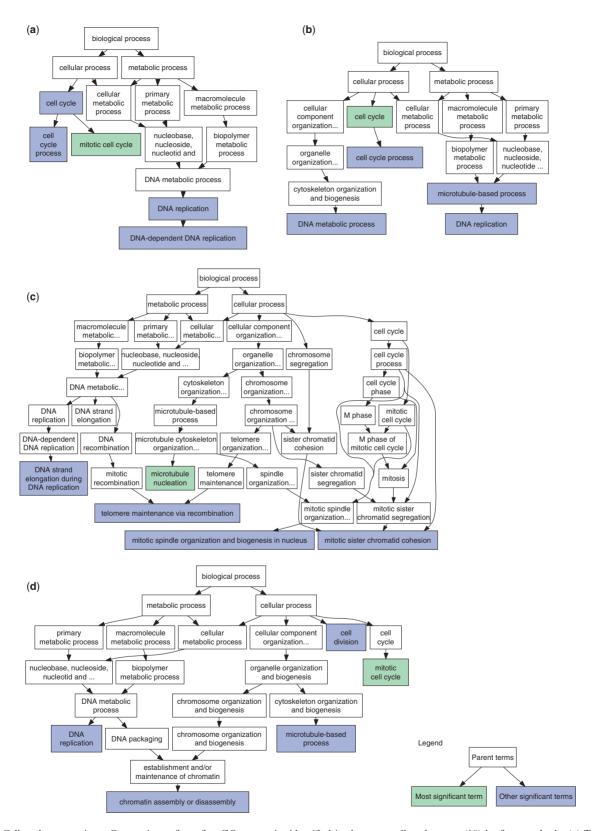


Figure 4. Cell cycle comparison. Comparison of top five GO categories identified in the yeast cell cycle genes (18) by four methods. (a) Top five GO categories identified using the Classic method (hypergeometric *P*-value) are highlighted. Green represents the most significant category identified. The five categories represent highly redundant view of only two biological processes, as highlighted by the red circles. (b) Parent_Child method (14). (c) Weight method (15) (see website for the Elim method) and (d) GenGO. See text for discussion.

Table 2. Categories for immune response

Classic	Parent-Child	Elim	Weight	GenGO
Imune response Imune system process Response to stress Response to stimulus Response to wounding	Biological process Immune system process Response to stimulus Cell proliferation Biological regulation	Immune response Inflammatory response Chemotaxis Response to virus Anti-apoptosis	Immune response Response to wounding Cell proliferation Chemotaxis Response to virus	Immune response Response to wounding Taxis Regulation of apoptosis tRNA aminoacylation

Top five GO categories identified from the list of human genes determined to be differentially expressed following exposure to bacteria (22).

determined in their title that 'E2F integrates cell cycle progression with DNA repair, replication, and G2/M checkpoints'. While all GO analysis methods correctly identified E2F1's role in controlling various aspects of the cell cycle, GenGO was only method to rank all three functions (replication, DNA repair and G2/M checkpoint) in its top five categories (See Supplementary Table 6 and Supplementary Figures 14–18).

DISCUSSION

The use of GO to analyze large datasets is rapidly becoming a standard procedure following in many high throughput experimental studies. The ability to utilize decades of prior work that have been curated into a single database allow researchers to gain initial insight regarding their experiment and can often suggest novel hypothesis for follow-up work (33,34). However, in many cases the result of this GO analysis is a long list of significant categories. This makes it hard to interpret the results and determine what the most significantly enriched functions are in the selected set of genes.

In this article, we described a generative model for identifying a small subset of categories that, combined, explain the observed set of genes. The algorithm we presented maximizes a global likelihood function to achieve this task. Our results suggest that GenGO is effective in minimizing false positives while at the same time it can accurately balance the set of categories it returns, including both high level and specific categories. GenGO was shown to work very well on both simulated data and real data from a number of different experimental techniques and species. Unlike other methods it does not require an extra step for correcting for multiple hypothesis testing resulting in categories that are both significant and unique.

We have implemented our method as a website at http:// www.sb.cs.cmu.edu/GenGO. To facilitate interactive use, the website allows the user to set default values for p and q, leading to faster analysis. Alternatively, users can let the software automatically optimize one or both of the parameters. The running time depends, of course, on the size of the input and the species. However, even when the input is rather large, the running time is very reasonable. For example, for the 800 yeast cell cycle genes mentioned above GenGO takes only 3s on a P4 2.4 GHz computer.

The current algorithm treats all GO categories in the same way regardless of their size or specificity. In future work we would like to more explicitly address this by

using different values for the penalty term α depending on the size of the selected category.

As we gain more knowledge regarding the function of genes and other transcribed elements in the cell these annotation databases will only become larger leading to further redundancies and overlaps. We thus believe that GenGO will be useful for researchers in many different areas of high-throughput biology for many years to come.

SUPPLEMENTARY DATA

Supplementary Data are available at NAR Online.

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REFERENCES

- 1. The Gene Ontology Consortium. (2000) Gene ontology: tool for the unification of biology. Nat. Genet., 25, 25-29.
- 2. Mewes, H.W., Frishman, D., Guldener, U., Mannhaupt, G., Mayer, K., Mokrejs, M., Morgenstern, B., Munsterkotter, M., Rudd, S. and Weil, B. (1999) MIPS: a database for genomes and protein sequences. Nucleic Acids Res., 27, 144-148.
- 3. The ENCODE Project Consortium. (2007) Identification and analysis of functional elements in 1% of the human genome by the ENCODE pilot project. Nature, 447, 799-816.
- 4. Kellis, M., Patterson, N., Endrizzi, M., Birren, B. and Lander, E.S. (2003) Sequencing and comparison of yeast species to identify genes and regulatory elements. Nature, 423, 241-254.
- 5. Cheung, V.G., Conlin, L.K., Weber, T.M., Arcaro, M., Jen, K.Y., Morley, M. and Spielman, R.S. (2003) Natural variation in human gene expression assessed in lymphoblastoid cells. Nat. Genet., 33, 422-425
- 6. The Toxicogenomics Research Consortium. (2005) Standardizing global gene expression analysis between laboratories and across platforms. Nat. Methods, 2, 351-356.
- 7. Bader, G.D. and Hogue, C.W.V. (2002) Analyzing yeast proteinprotein interaction data obtained from different sources. Nat. Biotechnol., 20, 991-997.
- 8. Giot, L., Bader, J.S., Brouwer, C., Chaudhuri, A., Kuang, B., Li, Y., Hao, Y.L., Ooi, C.E., Godwin, B., Vitols, E. et al. (2003) A protein interaction map of Drosophila melanogaster. Science, 302, 1727-1736.
- 9. Ewing, R.M., Chu, P., Elisma, F., Li, H., Taylor, P., Climie, S., McBroom-Cerajewski, L., Robinson, M.D., O'Connor, L., Li, M. et al. (2007) Large-scale mapping of human protein-protein interactions by mass spectrometry. Mol. Syst. Biol., 3, 89.

- Mukherjee, S., Berger, M.F., Jona, G., Wang, X.S., Muzzey, D., Snyder, M., Young, R.A. and Bulyk, M.L. (2004) Rapid analysis of the DNA-binding specificities of transcription factors with DNA microarrays. *Nat. Genet.*, 36, 1331–1339.
- Palomero, T., Lim, W.K., Odom, D.T., Sulis, M.L., Real, P.J., Margolin, A., Barnes, K.C., O'Neil, J., Neuberg, D., Weng, A.P. et al. (2006) NOTCH1 directly regulates c-MYC and activates a feed-forward-loop transcriptional network promoting leukemic cell growth. Proc. Natl Acad. Sci. USA, 103, 18261–18266.
- Deutscher, D., Meilijson, I., Kupiec, M. and Ruppin, E. (2006) Multiple knockout analysis of genetic robustness in the yeast metabolic network. *Nat. Genet.*, 38, 993–998.
- Ernst, J., Nau, G.J. and Bar-Joseph, Z. (2005) Clustering short time series gene expression data. *Bioinformatics*, 21 (Suppl 1), 1150-1168
- Grossmann, S., Bauer, S., Robinson, P.N. and Vingron, M. (2007) Improved detection of overrepresentation of gene-ontology annotations with parent-child analysis. *Bioinformatics*, 23, 3024–3031.
- Alexa, A., Rahnenfuhrer, J. and Lengauer, T. (2006) Improved scoring of functional groups from gene expression data by decorrelating GO graph structure. *Bioinformatics*, 22, 1600–1607.
- Ernst, J. and Bar-Joseph, Z. (2006) STEM: a tool for the analysis of short time series gene expression data. BMC Bioinformatics, 7, 191.
- Davis, J. and Goadrich, M. (2006) The relationship between precision-recall and ROC curves. Machine learning, *Proceedings of the twenty-third International Conference (ICML 2006)*, Pittsburgh, PA, USA pp. 233–240. ACM International Conference Proceeding series, http://dblp.uni-trier.de/rec/bibtex/conf/icml/2006.
- Spellman, P.T., Sherlock, G., Zhang, M.Q., Iyer, V.R., Anders, K., Eisen, M.B., Brown, P.O., Botstein, D. and Futcher, B. (1998) Comprehensive identification of cell cycle-regulated genes of the yeast Saccharomyces cerevisiae by microarray hybridization. Mol. Biol. Cell, 9, 3273–3297.
- 19. Gasch, A.P., Spellman, P.T., Kao, C.M., Carmel-Harel, O., Eisen, M.B., Storz, G., Botstein, D. and Brown, P.O. (2000) Genomic expression programs in the response of yeast cells to environmental changes. *Mol. Biol. Cell*, 11, 4241–4257.
- Thomas, D. and Surdin-Kerjan, Y. (1997) Metabolism of sulfur amino acids in *Saccharomyces cerevisiae*. *Microbiol. Mol. Biol. Rev*, 12, 503–532.
- Natarajan, K., Meyer, M.R., Jackson, B.M., Slade, D., Roberts, C., Hinnebusch, A.G. and Marton, M.J. (2001) Transcriptional profiling shows that Gcn4p is a master regulator of gene expression

- during amino acid starvation in yeast. Mol. Cell Biol., 21, 4347-4368
- Nau, G.J., Richmond, J.F., Schlesinger, A., Jennings, E.G., Lander, E.S. and Young, R.A. (2002) Human macrophage activation programs induced by bacterial pathogens. *Proc. Natl Acad. Sci.* USA, 99, 1503–1508.
- 23. Jones, G.E. (2000) Cellular signaling in macrophage migration and chemotaxis. *J. Leukoc. Biol.*, **68**, 593–602.
- 24. Grassme, H., Jendrossek, V. and Gulbins, E. (2001) Molecular mechanisms of bacteria induced apoptosis. *Apoptosis*, **6**, 441–445.
- Navarre, W.W. and Zychlinsky, A. (2000) Pathogen-induced apoptosis of macrophages: a common end for different pathogenic strategies. *Cell Microbiol.*, 2, 265–273.
- 26. Rojas, M., Barrera, L.F., Puzo, G. and Garcia, L.F. (1997) Differential induction of apoptosis by virulent Mycobacterium tuberculosis in resistant and susceptible murine macrophages: role of nitric oxide and mycobacterial products. *J. Immunol.*, 159, 1352–1361.
- Park,S.G., Ewalt,K.L. and Kima,S. (2005) Functional expansion of aminoacyl-tRNA synthetases and their interacting factors: new perspectives on housekeepers. *Trends Biochem. Sci.*, 30, 569–574.
- Harbison, C.T., Gordon, D.B., Lee, T.I., Rinaldi, N.J., Macisaac, K.D., Danford, T.W., Hannett, N.M., Tagne, J.B., Reynolds, D.B., Yoo, J. et al. (2004) Transcriptional regulatory code of a eukaryotic genome. *Nature*, 431, 99–104.
- 29. Bar-Joseph, Z., Gerber, G.K., Lee, T.I., Rinaldi, N.J., Yoo, J.Y., Robert, F., Gordon, D.B., Fraenkel, E., Jaakkola, T.S., Young, R.A. *et al.* (2003) Computational discovery of gene modules and regulatory networks. *Nat. Biotechnol.*, **21**, 1337–1342.
- 30. Nasmyth, K. and Dirick, L. (1991) The role of SWI4 and SWI6 in the activity of G1 cyclins in yeast. *Cell*, **66**, 995–1013.
- Leem,S.H., Chung,C.N., Sunwoo,Y. and Araki,H. (1998) Meiotic role of SWI6 in Saccharomyces cerevisiae. Nucleic Acids Res., 26, 3154–3158.
- 32. Ren,B., Cam,H., Takahashi,Y., Volkert,T., Terragni,J., Young,R.A. and Dynlacht,B.D. (2002) E2F integrates cell cycle progression with DNA repair, replication, and G2/M checkpoints. *Genes Dev.*, 16, 245–256.
- 33. Ihmels, J., Friedlander, G., Bergmann, S., Sarig, O., Ziv, Y. and Barkai, N. (2002) Revealing modular organization in the yeast transcriptional network. *Nat. Genet.*, 31, 370–377.
- 34. Eisen, M.B., Spellman, P.T., Brown, P.O. and Botstein, D. (1998) Cluster analysis and display of genome-wide expression patterns. *Proc. Natl Acad. Sci. USA*, **95**, 14863–14868.