# Predicting the Sequence-Dependent Backbone Dynamics of Intrinsically Disordered Proteins

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# Abstract

Dynamics is a crucial link between sequence and function for intrinsically disordered proteins (IDPs). NMR spin relaxation is a powerful technique for characterizing the sequencedependent backbone dynamics of IDPs. Of particular interest is the <sup>15</sup>N transverse relaxation rate  $(R_2)$ , which reports on slower dynamics (10s of ns up to 1 µs and beyond). NMR and molecular dynamics (MD) simulations have shown that local interactions and secondary structure formation slow down backbone dynamics and raise  $R_2$ . Elevated  $R_2$  has been suggested to be indicators of propensities of membrane association, liquid-liquid phase separation, and other functional processes. Here we present a sequence-based method, SeqDYN, for predicting  $R_2$  of IDPs. The  $R_2$  value of a residue is expressed as the product of contributing factors from all residues, which attenuate with increasing sequence distance from the central residue. The mathematical model has 21 parameters, representing the correlation length (where the attenuation is at 50%) and the amplitudes of the contributing factors of the 20 types of amino acids. Training on a set of 45 IDPs reveals a correlation length of 5.6 residues, aromatic and long branched aliphatic amino acids and Arg as  $R_2$  promotors whereas Gly and short polar amino acids as  $R_2$  suppressors. The prediction accuracy of SeqDYN is competitive against that of recent MD simulations using IDP-specific force fields. For a structured protein, SeqDYN prediction represents  $R_2$  in the unfolded state. SeqDYN is available as a web server at <u>https://zhougroup-uic.github.io/SeqDYNidp/</u> for rapid  $R_2$ prediction.

Keywords: intrinsically disordered proteins; NMR spin relaxation; transverse relaxation rate; backbone dynamics;  $R_2$  prediction

# **Significance Statement**

How the sequences of intrinsically disordered proteins (IDPs) code for functions is still an enigma. Dynamics, in particular residue-specific dynamics, holds crucial clues. Enormous efforts have been spent to characterize residue-specific dynamics of IDPs, mainly through NMR spin relaxation experiments. Here we present a sequence-based method, SeqDYN, for predicting residue-specific backbone dynamics of IDPs. SeqDYN employs a mathematical model with 21 parameters and is trained on 45 IDPs. It provides not only rapid, accurate prediction but also insightful physical interpretation of sequence-dependent IDP dynamics.

# Introduction

Intrinsically disordered proteins (IDPs) or regions (IDRs) do not have the luxury of a threedimensional structure to help decipher the relationship between sequence and function. Instead, dynamics has emerged as a crucial link between sequence and function for IDPs (1). NMR spin relaxation is a uniquely powerful technique for characterizing IDP dynamics, capable of yielding residue-specific information (2). Backbone <sup>15</sup>N relaxation experiments typically yield three parameters per residue: transverse relaxation rate ( $R_2$ ), longitudinal relaxation rate ( $R_1$ ), and steady-state heteronuclear Overhauser enhancement (NOE). While all the three parameters depend on ps-ns dynamics,  $R_2$  is the one most affected by slower dynamics (10s of ns to 1 µs and beyond). An increase in either the timescale or the amplitude of slower dynamics results in higher  $R_2$ . For IDPs,  $R_2$  is also the parameter that exhibits the strongest dependence on sequence (1, 2).

 $R_2$  was noted early on as an important indicator of residual structure in the unfolded state of the structured protein lysozyme (3). This property has since been measured for many IDPs to provide insight into various biophysical processes. Just as the residual structure in the unfolded state biases the folding pathway of lysozyme (3), a nascent  $\alpha$ -helix in the free state of Sendai virus nucleoprotein C-terminal domain (Sev-NT), as indicated by highly elevated  $R_2$  (4), biases the coupled binding and folding pathway in the presence of its target phosphoprotein (5). Local secondary structure preformation also facilitates the binding of yesassociated protein (YAP) with its target transcription factor (6). Likewise a correlation has been found between  $R_2$  in the free state and the membrane binding propensity of synaptobrevin-2: residues with elevated  $R_2$  have increased propensity for membrane binding (7).  $R_2$  in the free state has also been used to uncover factors that promote liquid-liquid phase separation of IDPs. For example, a nascent  $\alpha$ -helix (shown by elevated  $R_2$ ) is important for the phase separation of TDP-43 low-complexity domain, as both the deletion of the helical region and a helix-breaking mutation (Ala to Pro) abrogates phase separation (8). Similarly, nascent  $\alpha$ -helices in the free state of cytosolic abundant heat-soluble 8 (CAHS-8), upon

raising concentration and lowering temperature stabilize to form the core of fibrous gels (9). For hnRNPA1 low-complexity domain (A1-LCD), aromatic residues giving rise to local peaks in  $R_2$  also mediate phase separation (10).

Both NMR relaxation data and molecular dynamics (MD) simulations have revealed determinants of  $R_2$  for IDPs. It has been noted that the flexible Gly has a tendency to lower  $R_2$  whereas secondary structure and contact formation tend to raise  $R_2$  (11). This conclusion agrees well with recent MD simulations (1, 12-14). These MD studies, using IDP-specific force fields, are able to predict  $R_2$  in quantitative agreement with NMR measurements, without ad hoc reweighting as done in earlier studies. According to MD, most contact clusters are formed by local sequences, within blocks of up to a dozen or so residues (1, 12, 13). Tertiary contacts can also form but are relatively rare; as such their accurate capture requires extremely extensive sampling and still poses a challenge for MD simulations. Opposite to Gly, aromatic residues have been noted as mediators of contact clusters (3, 10).

Schwalbe et al. (15) introduced a mathematical model to describe the  $R_2$  profile along the sequence for lysozyme in the unfolded state. The  $R_2$  value of a given residue was expressed as the sum of contributions from this residues and its neighbors. This model yields a mostly flat profile across the sequence, except for falloff at the termini, resulting an overall bell shape. Klein-Seetharaman et al. (3) then fit peaks above this flat profile as a sum of Gaussians. Cho et al. (16) proposed bulkiness as a qualitative indicator of backbone dynamics. Recently Sekiyama et al. (17) calculated  $R_2$  as the geometric mean of "indices of local dynamics"; the latter were parameterized by fitting to the measured  $R_2$  for a single IDP. All these models merely describe the  $R_2$  profile of a given IDP, and none of them is predictive.

Here we present a method, SeqDYN, for predicting  $R_2$  of IDPs. Using a mathematical model introduced by Li et al. (18) to predict propensities for binding nanoparticles and also adapted for predicting propensities for binding membranes (19), we express the  $R_2$  value of a residue as the product of contributing factors from all residues. The contributing factor

attenuates as the neighboring residue becomes more distant from the central residue. The model, after training on a set of 45 IDPs, has prediction accuracy that is competitive against that of the recent MD simulations using IDP-specific force fields (1, 12-14). For lysozyme, the SeqDYN prediction agrees remarkably well with  $R_2$  measured in the unfolded state.

### Results

# The data set of IDPs with $R_2$ rates

We collected  $R_2$  data for a total of 54 nonhomologous IDPs or IDRs (Table S1; Fig. S1). According to indicators from NMR properties, including low or negative NOEs, narrow dispersion in backbone amide proton chemical shifts, and small secondary chemical shifts (SCSs), most of the proteins are disordered with at most transient  $\alpha$ -helices. A few are partially folded, including Sev-NT with a well-populated (~80%) long helix (residues 478-491) (20), CREB-binding protein fourth intrinsically disordered linker (CBP-ID4) with > 50% propensities for two long helices (residues 2-25 and 101-128) (21), HOX transcription factor DFD (HOX-DFD) with a well-folded domain comprising three helices (22), and Hahellin (apo form) as a molten globule (23). In Fig. 1, we display representative conformations of five IDPs, ranging from fully disordered MAPK kinase 4 (MKK4) (24) and  $\alpha$ -synuclein (25) to Measles virus phosphoprotein N-terminal domain (Mev-P<sub>NTD</sub>) (26) with transient short helices to Sev-NT and CBP-ID4 with stable long helices. The sequences of all the IDPs are listed in Table S2.

We used 45 of the 54 IDPs to train and validate SeqDYN and reserved the remaining 9 for testing. The sequence lengths of the training set range from 39 to 406 residues, with an average of 125.3 residues. Altogether  $R_2$  data are available for 3966 residues. A large majority (35 out of 45) of the 45 IDPs have mean  $R_2$  values ( $\bar{R}_2$ , calculated among all the residues in a protein) between 2.5 and 5.5 s<sup>-1</sup> (Table S1 and Fig. 2A). This  $\bar{R}_2$  range is much lower than that of structured proteins with similar sequence lengths. The low  $\bar{R}_2$  values and

lack of dependence on sequence length (Fig. S2A) suggest that  $R_2$  of the IDPs is mostly dictated by local sequence as opposed to tertiary interaction.

The most often used temperature for acquiring the  $R_2$  data was 298 K, but low temperatures (277 to 280 K) were used in a few cases (Table S1 and Fig. S2B). Of the seven IDPs with  $\bar{R}_2 > 6.4 \text{ s}^{-1}$ , four can be attributed to low temperatures (27-30), one is due to a relatively low temperature (283 K) as well as the presence of glycerol (20% v/v) (31), and two can be explained by tertiary structure formation [a folded domain (22) or molten globule (23)]. A simple reason for higher  $R_2$  values at lower temperatures is the higher water viscosity, resulting in slowdown in molecular tumbling; a similar effect is achieved by adding glycerol. In some cases,  $R_2$  was measured at both low and room temperatures (4, 10). To a good approximation, the effect of lowering temperature is a uniform scaling of  $R_2$  across the IDP sequence. For Sev-NT, downscaling of the R<sub>2</sub> values at 278 K by a factor of 2.0 brings them into close agreement with those at 298 K (Fig. S2C), with a root-mean-square-deviation (RMSD) of 0.5 s<sup>-1</sup> among all the residues. Likewise, for A1-LCD, downscaling by a factor of 2.4 brings the  $R_2$  values at 288 K into good match with those at 298 K (Fig. S2D), with an RMSD of 0.4 s<sup>-1</sup>. Because SeqDYN is concerned with the sequence dependence of  $R_2$ , a uniform scaling has no effect on model parameter or prediction; therefore mixing the data from different temperatures is justified. The same can be said about the different magnetic fields in acquiring the  $R_2$  data (Table S1 and Fig. S2E). Increasing the magnetic field raises  $R_2$  values, and the effect is also approximated well by a uniform scaling (4, 8, 29).

One measure on the level of sequence dependence of  $R_2$  is the standard deviation,  $\sigma_{R_2}$ , calculated among the residues of an IDP. Among the training set, the  $R_2$  values of 30 IDPs have moderate sequence variations, with  $\sigma_{R_2}$  ranging from 0.5 to 1.5 s<sup>-1</sup> (Table S1); the histogram of  $\sigma_{R_2}$  calculated for the entire training set peaks around 0.75 s<sup>-1</sup> (Fig. 2A). There is a moderate correlation between  $\sigma_{R_2}$  and  $\bar{R}_2$  (Fig. 2A, inset), reflecting in part the fact that  $\sigma_{R_2}$ can be raised simply by a uniform upscaling, e.g., as a result of lowering temperature. Still, only two of the five IDPs with high  $\bar{R}_2$  attributable to lower temperature or presence of

glycerol are among the seven IDPs with high sequence variations ( $\sigma_{R_2} > 2 \text{ s}^{-1}$ ). Therefore the sequence variation of  $R_2$  as captured by  $\sigma_{R_2}$  manifests mostly the intrinsic effect of the IDP sequence, not the influence of external factors such as temperature or magnetic field strength. The mean  $\sigma_{R_2}$  value among the training set is 1.24 s<sup>-1</sup>.

One way to eliminate the influence of external factors is to scale the  $R_2$  values of each IDP by its  $\overline{R}_2$ ; we refer to the results as scaled  $R_2$ , or  $sR_2$ . We then pooled the  $sR_2$  values for all residues in the training set, and separated them according to amino-acid types. The amino acid type-specific mean  $sR_2$  values, or  $msR_2$ , are displayed in Fig. 2B. The seven amino acids with the highest  $msR_2$  are, in descending order, Trp, Arg, Tyr, Phe, Ile, His, and Leu. The presence of all the four aromatic amino acids in this "high-end" group immediately suggests  $\pi$ - $\pi$  stacking as important for raising  $R_2$ ; the presence of Arg further implicates cation- $\pi$  interactions. In the other extreme, the seven amino acids with the lowest  $msR_2$  are, in ascending order, are Gly, Cys, Val, Asp, Ser, Thr, and Asn. Gly is well-known as a flexible residue; it is also interesting that all the four amino acids with short polar sidechains are found in this "low-end" group. Pro has an excessively low  $msR_2$  [with data from only two IDPs (32, 33)], but that is due to the absence of an amide proton.

## The SeqDYN model and parameters

The null model is to assume a uniform  $R_2$  for all the residues in an IDP. The root-meansquare-error (RMSE) of the null model is equal to the standard deviation,  $\sigma_{R_2}$ , of the measured  $R_2$  values. The mean RMSE,  $\overline{\text{RMSE}}$ , of the null model, equal to 1.24 s<sup>-1</sup> for the training set, serves as the upper bound for evaluating the errors of  $R_2$  predictors. The next improvement is a one-residue predictor, where first each residue (with index *n*) assumes its amino acid-specific mean s $R_2$  (ms $R_2$ ) and then a uniform scaling factor Y is applied:

$$R_2(n) = \Upsilon \cdot \mathrm{ms}R_2(n) \tag{1}$$

This one-residue model does only minutely better than the null model, with a  $\overline{\text{RMSE}}$  of 1.22 s<sup>-1</sup>.

In SeqDYN, we account for the influence of neighboring residues. Specifically, each residue *i* contributes a factor f(i; n) to the  $R_2$  value of residue *n*. Therefore

$$R_2(n) = \Upsilon \prod_{i=1}^N f(i;n)$$
(2a)

where N is the total number of residues in the IDP. The contributing factor depends on the sequence distance s = |i - n| and the amino-acid type of residue *i*:

$$f(i;n) = 1 + \frac{q(i) - 1}{1 + bs^2}$$
(2b)

There are 21 global parameters. The first 20 are the q values, one for each of the 20 types of amino acids; the last parameter is b, appearing in the Lorentzian form of the sequencedistance dependence. We define the correlation length,  $L_{corr}$ , as the sequence distance at which the contributing factor is midway between the values at s = 0 and  $\infty$ . It is easy to verify that  $L_{corr} = b^{-1/2}$ . Note that the single-residue model can be seen as a special case of SeqDYN, with  $L_{corr}$  set to 0 and q set to ms $R_2$ .

The functional forms of Eqs (2a,b) were adapted from Li et al. (18); we also used them for predicting residue-specific membrane association propensities of IDPs (19). In these previous applications, a linear term was also present in the denominator of Eq (2b). In our initial training of SeqDYN, the coefficient of the linear term always converged to near zero. We thus eliminated the linear term. In addition to the Lorentzian form, we also tested a Gaussian form for the sequence-distance dependence and found somewhat worse performance. The more gradual attenuation of the Lorentzian form with increasing sequence distance evidently provides an overall better model for the  $R_2$  data in the entire training set. Others (16, 17, 24) have modeled  $R_2$  as the average of some parameters over a window; a window has an extremely abrupt sequence-distance dependence (1 for  $s < L_{corr}$  and 0 for  $s > L_{corr}$ ).

We parametrized the SeqDYN model represented by Eqs (2a,b) on the training set of 45 IDPs. In addition to the 21 global parameters noted above, there are also 45 local parameters, namely one uniform scaling factor (Y) per IDP. The parameter values were selected to minimize the sum of the mean-square-errors for the IDPs in the training set, calculated on  $R_2$  data for a total of 3924 residues. We excluded the 42 Pro residues in the training set because, as already noted, their  $R_2$  values are lower for chemical reasons. We will present validation and test results below, but first let us look at the parameter values.

The *q* values are displayed in Fig. 2B alongside ms $R_2$ . The seven amino acids with the highest *q* values, in descending order, are Trp, Ile, Tyr, Arg, His, Phe, and Leu. These are exactly the same amino acids in the high-end group for ms $R_2$ , though their order there is somewhat different. The seven amino acids (excluding Pro) with the lowest *q* values, in ascending order, are Gly, Asn, Ser, Asp, Val, Thr, and Cys. The composition of the low-end group is also identical to that for ms $R_2$ . The *q* values thus also suggest that  $\pi$ - $\pi$  and cation- $\pi$ interactions in local sequences may raise  $R_2$ , whereas Gly and short-polar residues may lower  $R_2$ .

Given the common amino acids at both the high and low ends for  $msR_2$  and q, it is not surprising that these two properties exhibit a strong correlation, with a coefficient of determination ( $R^2$ ; excluding Pro) at 0.92 (Fig. 3A). Also, because the high-end group contains the largest amino acids (e.g., Trp and Tyr) whereas the low-end group contains the smallest amino acids (e.g., Gly and Ser), we anticipated some correlation of  $msR_2$  and q with amino-acid size. We measure the latter property by the molecular mass (m). As shown in Fig. 3B, both  $msR_2$  and q indeed show medium correlation with m, with  $R^2 = 0.67$  (excluding Pro) and 0.61, respectively. A bulkiness parameter was proposed as an indicator of sequencedependent backbone dynamics of IDPs (16, 24). Bulkiness was defined as the sidechain volume to length ratio, and identifies amino acids with aromatic or branched aliphatic sidechains as bulky (34). We found only modest correlations between either  $msR_2$  or q and bulkiness, with  $R^2$  just below 0.4 (Fig. 3C).

The optimized value of *b* is  $3.164 \times 10^{-2}$ , corresponding to an  $L_{corr}$  of 5.6 residues. The resulting optimized  $\overline{\text{RMSE}}$  is 0.95 s<sup>-1</sup>, a clear improvement over the value 1.24 s<sup>-1</sup> of the null model. To check the sensitivity of prediction accuracy to *b*, we set *b* to values corresponding to  $L_{corr} = 0, 1, 2, ...$ , and retrained SeqDYN for *b* fixed at each value. Note that the null-model  $\overline{\text{RMSE}}$ , 1.24 s<sup>-1</sup>, sets an upper bound. This upper bound is gradually reached when  $L_{corr}$  is increased from the optimal value. In the opposite direction, when  $L_{corr}$  is decreased from the optimal value,  $\overline{\text{RMSE}}$  rises quickly, reaching 1.22 s<sup>-1</sup> at  $L_{corr} = 0$ . The latter  $\overline{\text{RMSE}}$  is the same as that of the single-residue model. Lastly we note that there is strong correlation between the uniform scaling factors and  $\overline{R}_2$  values among the 45 IDPs ( $R^2 = 0.77$ ), as to be expected. For 39 of the 45 IDPs,  $\Upsilon$  values fall in the range of 0.8 to 2.0 s<sup>-1</sup>.

As presented next, we evaluate the performance of SeqDYN by leave-one-out cross validation, where each IDP in turn was left out of the training set and the model was trained on the remaining 44 IDPs to predict  $R_2$  for the IDP that was left out. The parameters from the leave-one-out (also known as jackknife) training sessions allow us to assess potential bias of the training set. For this purpose, we compare the values of the 21 global parameters, either from the full training set or from taking the averages of the jackknife training sessions. For each of the *q* parameters, the values from these two methods differ only in the fourth digit; e.g., for Leu, they are both 1.1447 from full training and from jackknife training. The values for *b* are  $3.164 \times 10^{-2}$  from full training as stated above and  $3.163 \times 10^{-2}$  from jackknife training suggests no significant bias in the training set.

Another question of interest is whether the difference between the q parameters of two amino acids is statistically significant. To answer this question, we carried out five-fold crossvalidation training, resulting in five independent estimates for each parameter. For example, the mean  $\pm$  standard deviation of the q parameter is  $1.1405 \pm 0.0066$  for Leu and  $1.2174 \pm$ 0.0211 for Ile. A t-test shows that their difference is statistically significant (P < 0.0001). In contrast, the difference between Leu and Phe ( $q = 1.1552 \pm 0.0304$ ) is not significant.

#### Validation of SeqDYN predictions

We now present leave-one-out cross-validation results. We denote the RMSE of the  $R_2$  prediction for the left-out IDP as RMSE(-1). As expected, RMSE(-1) is higher than the RMSE obtained with the IDP kept in the training set, but the increases are generally slight. Specifically, all but eight of the IDPs have increases < 0.1 s<sup>-1</sup>; the largest increase is 0.35 s<sup>-1</sup>, for CBP-ID4. The mean RMSE(-1), or  $\overline{RMSE}(-1)$ , for the 45 IDPs is increased by 0.05 s<sup>-1</sup> over  $\overline{RMSE}$ , to 1.00 s<sup>-1</sup>. The latter value is still a distinct improvement over the mean RMSE 1.24 s<sup>-1</sup> of the null model. The histogram of RMSE(-1) for the 45 IDPs is shown in Fig. 4A. It peaks at 0.5 s<sup>-1</sup>, which is a substantial downshift from the corresponding peak at 0.75 s<sup>-1</sup> for  $\sigma_{R_2}$  (Fig. 2A). Thirty-four of the 45 IDPs have RMSE(-1) values lower than the corresponding  $\sigma_{R_2}$ .

To further illustrate the performance of SeqDYN, we present comparison of predicted and measured  $R_2$  values for five IDPs: MKK4,  $\alpha$ -synuclein, Mev-P<sub>NTD</sub>, Sev-NT, and CBP-ID4 (Fig. 4B-F). A simple common feature is the falloff of  $R_2$  at the N- and C-termini, resulting from missing upstream or downstream residues that otherwise would be coupled to the terminal residues, as first recognized by Schwalbe et al. (15). Representative conformations of the five IDPs are displayed in Fig. 1, with residues colored according to the predicted  $R_2$  values. For four of these IDPs, the RMSE(-1) values range from 0.44 to 0.76 s<sup>-1</sup> and are scattered around the peak of the histogram, while the RMSE(-1) for the fifth IDP, namely CBP-ID4, the RMSE(-1) value is 2.01 s<sup>-1</sup> and falls on the tail of the histogram (Fig. 4A). Figure 4B displays the measured and predicted  $R_2$  for MKK4. SeqDYN correctly predicts higher  $R_2$  values in the second half of the sequence than in the first half. It even correctly predicts the peak around residue Arg75. The sequence in this region is H<sub>72</sub>IERLRTH<sub>79</sub>; six of these eight residues belong to the high-end group. In contrast, the lowest  $R_2$  values occur in the sequence S<sub>7</sub>GGGGSGGGSGGSGGSG<sub>19</sub>, comprising entirely of two amino acids in the low-end group.

 $R_2$  values for  $\alpha$ -synuclein are shown in Fig. 4C. Here SeqDYN correctly predicts higher  $R_2$  near the C-terminus and a dip around Gly68. However, it misses the  $R_2$  peaks around Tyr39 and Asp121. MD simulations (1) have found that these  $R_2$  peaks can be explained by a combination of secondary structure formation ( $\beta$ -sheet around Tyr39 and polyproline II helix around Asp121) and local (between Tyr39 and Ser42) or long-range (between Asp121 and Lys96) interactions. SeqDYN cannot account for long-range interactions (e.g., between  $\beta$ -strands and between Asp121 and Lys96). Figure 4D shows that SeqDYN gives excellent  $R_2$  predictions for Mev-P<sub>NTD</sub>. It correctly predicts the high peaks around Arg17, Glu31, Leu193, and lower peaks around Arg235 and Trp285, but does underpredict the narrow peak around Tyr113.

The overall  $R_2$  profile of Sev-NT is predicted well by SeqDYN, but the peak in the long helical region (residues 478-491) is severely underestimated (green curve in Fig. 4E). A similar situation occurs for CBP-ID4, where the peak in the second long helical region (around Glu113) is underpredicted (green curve in Fig. 4F). While the measured  $R_2$  exhibits a higher peak in the second helical region than in the first helical region (around Arg16), the opposite is predicted by SeqDYN. When the  $R_2$  data were included in the training set (i.e., full training), the second peak is higher than the first one, but that is not a real prediction because the  $R_2$  data themselves were used for training the model. It merely means that the SeqDYN functions can be parameterized to produce any prescribed  $R_2$  profile along the sequence. Indeed, when the  $R_2$  data of CBP-ID4 alone were used to parameterize SeqDYN, the measured  $R_2$  profile is closely reproduced (Fig. S3). The reversal in  $R_2$  peak heights between the two helical regions is the reason for the aforementioned unusual increase in RMSE when CBP-ID4 was left out of the training set.

# **R2** boost in long helical regions

It is apparent that SeqDYN underestimates the  $R_2$  of stable long helices. Transient short helices does not seem to be a problem, since these are present, e.g., in Mev-P<sub>NTD</sub>, where

transient helix formation in the first 37 residues and between residues 189-198 (26) coincides with  $R_2$  peaks that are correctly predicted by SeqDYN. SeqDYN can treat coupling between residues within the correlation length of 5.6 residues, but a much longer helix would tumble more slowly than implied by an  $L_{corr}$  of 5.6, and thus it makes sense that SeqDYN would underestimate  $R_2$  in that case.

Our solution then is to apply a boost factor to the long helical region. To do so, we have to know whether an IDP does form long helices and if so what the constituent residues are. Secondary structure predictors tend to overpredict  $\alpha$ -helices and  $\beta$ -strands for IDPs, as they are trained on structured proteins. One way to counter that tendency is to make the criteria for  $\alpha$ -helices and  $\beta$ -strands stricter. We found that, by filtering PsiPred (http://bioinf.cs.ucl.ac.uk/psipred) (35) helix propensity scores ( $p_{HIx}$ ) with a very high cutoff of 0.99, the surviving helix predictions usually correspond well with residues identified by NMR as having high helix propensities. For example, for Mev-P<sub>NTD</sub>, PsiPred plus filtering predicts residues 14-17, 28-33, and 191-193 as helical; all of them are in regions that form transient helices according to chemical shifts (26). Likewise long helices are also correctly predicted for Sev-NT (residues 477-489) and CBP-ID4 (residues 6-17 and 105-116).

We apply a boost factor,  $B_{Hlx}$ , to helices with a threshold length of 12:

$$B_{\text{Hlx}} = 1 + \alpha p_{\text{Hlx}} \Theta(p_{\text{Hlx}} \ge 0.99; L_{\text{Hlx}} \ge 12)$$

(3)

The  $\Theta$  function is 1 if the helix propensity score is above the filtering cutoff and the helix length ( $L_{Hlx}$ ) is above the threshold, and 0 otherwise. With a boost amplitude  $\alpha$  at 0.5, the boosted SeqDYN prediction for Sev-NT reaches excellent agreement with the measured  $R_2$ (Fig. 4E, red curve). The RMSE(-1) is reduced from 0.76 s<sup>-1</sup> to 0.38 s<sup>-1</sup> upon boosting. Applying the same helix boost to CBP-ID4 also results in a modest reduction in RMSE(-1), from 2.01 to 1.90 s<sup>-1</sup> (Fig. 4F, red curve). The only other IDP for which PsiPred plus filtering predicts a long helix is the N-terminal region of lysyl-tRNA synthetase (KRS-NT). The authors who studied this protein did not report on secondary structure (36), but feeding their reported chemical shifts to the TALOS+ server

(<u>https://spin.niddk.nih.gov/bax/nmrserver/talos/</u>) (37) found only short stretches of residues that fall into the helical region of the Ramachandran map. The SeqDYN prediction for KRS-NT is already good [RMSE(-1) =  $0.83 \text{ s}^{-1}$ ]; applying a helix boost would deteriorate the RMSE(-1) to 1.16 s<sup>-1</sup>.

### **Further test on a set of nine IDPs**

We have reserved nine IDPs for testing SeqDYN (parameterized on the training set of 45 IDPs). The level of disorder in these test proteins also spans the full range, from absence of secondary structures [ChiZ N-terminal region (12), Pdx1 C-terminal region (11), and TIA-1 prion-like domain (17)] to presence of transient short helices [synaptobrevin-2 (7),  $\alpha$ -endosulfine (38), YAP (6), angiomotin-like 1 (AMOTL1) (39)] to formation of stable long helices [FtsQ (13) and CAHS-8 (9)]. For eight of the nine test IDPs, the RMSEs of SeqDYN predictions are lower than the experimental  $\sigma_{R_2}$  values, by an average of 0.62 s<sup>-1</sup>. For the nineth IDP (Pdx1), the SeqDYN RMSE is slightly higher, by 0.06 s<sup>-1</sup>, than the experimental  $\sigma_{R_2}$ .

The comparison of predicted and measured  $R_2$  profiles along the sequence is presented in Fig. 5A-I. For ChiZ, SeqDYN correctly predicts the major peak around Arg25 and the minor peak around Arg46 (Fig. 5A). The  $R_2$  profile of Pdx1 is largely featureless, except for a dip around Gly216, which is correctly predicted by SeqDYN (Fig. 5B). Correct prediction is also obtained for the higher  $R_2$  in the first half of TIA-1 prion-like domain than in the second half (Fig. 5C). SeqDYN gives an excellent prediction for synaptobrevin-2, including a linear increase up to Arg56 and the major peak around Trp89 (Fig. 5D).

The prediction is also very good for  $\alpha$ -endosulfine, including elevated  $R_2$  around Glu34, which coincides with the presence of a transient helix, and depressed  $R_2$  in the last 40 residues (Fig. 5E). The only miss is an underprediction for the peak around Lys74. SeqDYN also predicts well the overall shape of the  $R_2$  profile for YAP, including peaks around Asn70,

Leu91, Arg124, and Arg161, but severely underestimates the peak height around Asn70 (Fig. 5F).NOE signals indicate contacts between Met86, Leu91, Fhe95, and Fhe96 (6); evidently this type of local contacts is captured well by SeqDYN. The  $R_2$  elevation around Asn70 is mostly due to helix formation: residues 61-74 have helix propensities up to 40% (6). PsiPred predicts helix for residues 62-73, but only residues 65-68 survive the filtering that we impose, resulting a helix that is too short to apply a helix boost. The prediction for AMOTL1 is mostly satisfactory, including peaks around Phe200 and Arg264 and a significant dip around Gly292 (Fig. 5G). However, whereas the two peaks have approximately equal heights in the measured  $R_2$  profile, the predicted peak height around Phe200 is too low. SCSs indicate helix propensity around both  $R_2$  peaks (39). PsiPred also predicts helix in both regions, but only five and two residues, respectively, survive after filtering, which are too short for applying a helix boost.

For FtsQ, SeqDYN correctly predicts elevated  $R_2$  for the long helix [residues 46-74 (13)] but underestimates the magnitude (RMSE = 2.32 s<sup>-1</sup>; green curve in Fig. 5H). PsiPred plus filtering predicts a long helix formed by residues 47-73. Applying the helix boost substantially improves the agreement with the measured  $R_2$ , with RMSE reducing to 1.71 s<sup>-1</sup> (red curve in Fig. 5H). SeqDYN also gives a qualitatively correct  $R_2$  profile for CAHS-8, with higher  $R_2$  for the middle section (residues 95-190) (RMSE = 2.36 s<sup>-1</sup>; green curve in Fig. 5I). However, it misses the extra elevation in  $R_2$  for the first half of the middle section (residues 95-145). According to SCS, the first and second halves have helix propensities of 60% and 30%, respectively (9). PsiPred plus filtering predicts helices for residues 96-121, 124-141, 169-173, and 179-189. Only the first two helices, both in the first half of the middle section, are considered long according to our threshold. Once again, applying the helix boost leads to marked improvement in the predicted in  $R_2$ , with RMSE reducing to 1.92 s<sup>-1</sup> (red curve in Fig. 5I).

# Inputting the sequence of a structured protein predicts $R_2$ in the unfolded state

SeqDYN is trained on IDPs, what if we feed it with the sequence of a structured protein? The prediction using the sequence of hen egg white lysozyme, a well-studied single-domain protein, is displayed in Fig. 6A. It shows remarkable agreement with the  $R_2$  profile measured by Klein-Seetharaman et al. (3) in the unfolded state (denatured by 8 M urea and reduced to break disulfide bridges), including a major peak around Trp62, a second peak around Trp111, and a third peak around Trp123. Klein-Seetharaman et al. mutated Trp62 to Gly and the major peak all but disappeared. This result is also precisely predicted by SeqDYN with the mutant sequence (Fig. 6B).

# Discussion

We have developed a powerful method, SeqDYN, that predicts the backbone amide transverse relaxation rates ( $R_2$ ) of IDPs. The method is based on IDP sequences, is extremely fast, and available as a web server at <u>https://zhougroup-uic.github.io/SeqDYNidp/</u>. The excellent performance supports the notion that the ns-dynamics reported by  $R_2$  is coded by the local sequence, comprising up to 6 residues on either side of a given residue. The amino-acid types that contribute the most to coupling within a local sequence are aromatic (Trp, Tyr, Phe, and His), Arg, and long branched aliphatic (Ile and Leu), suggesting the importance of  $\pi$ - $\pi$ , cation- $\pi$ , and hydrophobic interactions in raising  $R_2$ . These interactions are interrupted by Gly and amino acids with short polar sidechains (Ser, Thr, Asn, and Asp), leading to reduced  $R_2$ . Transient short helices produce moderate elevation in  $R_2$ , whereas stable long helices result in a big boost in  $R_2$ . Tertiary contacts can also raise  $R_2$ , but appears to be infrequent in most IDPs (1).

Our method incorporates ideas from a number of previous efforts at describing  $R_2$ . The first serious effort was by Schwalbe et al. (15), who accounted for contributions from neighboring residues as additive terms, instead of multiplicative factors as in SeqDYN. Cho et al. (16) and Delaforge et al. (24) used the running average of the bulkiness parameter over a window of five to nine residues as a qualitative indicator of  $R_2$ . Here again the calculation

was based on an additive model. Sekiyama et al. (17) employed a multiplicative model, with  $R_2$  calculated as a geometric mean of "indices of local dynamics" over a five-residue window. These indices, akin to our q parameters, were trained on a single IDR (TIA-1 prion-like domain) and used to reproduce the measured  $R_2$  for the same IDR. As we have illustrated on CBP-ID4 (Fig. S3), training on a single protein merely biases the parameters to that model and has little value in predicting  $R_2$  for other proteins. In comparison, SeqDYN is trained on 45 IDPs and its predictions are robust and achieve quantitative agreement with measured  $R_2$ .

Ten of the IDPs tested here have been studied recently by MD simulations using IDPspecific force fields (1, 12-14). In Table 1 we compare the RMSEs of SeqDYN predictions with those for  $R_2$  calculations from MD simulations. For five of these IDPs: A1-LCD, A $\beta$ 40,  $\alpha$ -synuclein, tau K18, and FtsQ, RMSEs of SeqDYN and MD are remarkably similar. Four of these IDPs lack significant population of  $\alpha$ -helices or  $\beta$ -sheets, but FtsQ forms a stable long helix. For one other IDP, namely HOX-DFD, MD, by explicitly modeling its folded domain, does a much better job in predicting  $R_2$  than SeqDYN (RMSEs of 1.40 s<sup>-1</sup> vs 1.99 s<sup>-1</sup>). However, for the four remaining IDPs: p53TAD, Pup, Sev-NT, and ChiZ, SeqDYN significantly outperforms MD, with RMSEs averaging only 0.47 s<sup>-1</sup>, compared to the MD counterpart of 1.14 s<sup>-1</sup>. Overall, SeqDYN is very competitive against MD in predicting  $R_2$ , but without the significant computational cost. While MD simulations can reveal details of local interactions, as noted for  $\alpha$ -synuclein, and capture tertiary interactions if they occur, they still suffer from perennial problems of force-field imperfection and inadequate sampling. SeqDYN provides an accurate description of IDP dynamics at a "mean-field" level, but could miss idiosyncratic behaviors of specific local sequences.

Deep-learning models have become very powerful, but they usually have millions of parameters and require millions of protein sequences for training (40). In contrast, SeqDYN employs a mathematical model with dozens of parameters and requires only dozens of proteins for training. Reduced models (by collapsing amino acids into a small number of distinct types) have even been trained on < 10 IDPs to predict propensities for binding

nanoparticles (18) or membranes (19). The mathematical model-based approach may be useful in other applications where data, similar to  $R_2$ , are limited, including predictions of IDP secondary chemical shifts or residues that bind drug molecules (41) or protein targets, or even in protein design, e.g., for recognizing an antigenic site or a specific DNA site.

### Methods

# Collection of IDPs with measured $R_2$

Starting from six nonhomologous IDPs in our previous MD study (1), we obtained  $R_2$  data for eight IDPs from the Bimolecular Magnetic Resonance Data Bank (BMRB; <u>https://bmrb.io</u>); data for two other IDPs were from our collaborators (12, 13). Most of the 54 IDPs studied here were from searching the literature. Disorder was judged by dispersion in backbone amide proton chemical shifts, NOE, and SCS.  $R_2$  data that were not available from the authors or BMRB were obtained by digitizing  $R_2$  plots presented in figures of published papers, using WebPlotDigitizer (<u>https://automeris.io/WebPlotDigitizer</u>) (42) and further inspected visually.

Homology of IDPs was checked by sequence alignment using Clustal W (<u>http://www.clustal.org/clustal2</u>) (43), and presented as a clock-like tree using the "ape" package (<u>http://ape-package.ird.fr</u>) (44). IDPs that had discernible homology with the selected training set were removed. Removed IDPs included HOX-SCR and β-synuclein from our previous MD study (1), due to homology with HOX-DFD and α-synuclein, respectively.

# **Coding for SeqDYN**

The training of SeqDYN was coded in python, similar to our previous work for predicting residue-specific membrane association propensities (ReSMAP; <u>https://zhougroup-uic.github.io/ReSMAPidp/</u>) (19). The cost function was the sum of mean-squared-errors for the IDPs in the training set. We used the least\_squares function in scipy.optimize, with Trust Region Reflective as the minimization algorithm and all parameters restricted to the positive

range. For the web server (<u>https://zhougroup-uic.github.io/SeqDYNidp/</u>), we rewrote the prediction code javascript.

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IDP name	SeqDYN	MD
A1-LCD	0.60ª	0.59 <sup>d, e</sup>
Αβ40	0.38ª	0.38 <sup>d</sup>
HOX-DFD	1.99ª	$1.40^{d}$
α-synuclein	0.44ª	0.50 <sup>d</sup>
p53TAD	0.33ª	1.04 <sup>f</sup>
Pup	0.43ª	1.00 <sup>f</sup>
Sev-NT	0.38 <sup>a, b</sup>	1.10 <sup>d, g</sup>
tau K18	0.83ª	0.80 <sup>d</sup>
ChiZ	0.74 <sup>c</sup>	1.40 <sup>h</sup>
FtsQ	1.71 <sup>c, b</sup>	1.70 <sup>i</sup>

# Table 1. RMSEs (s<sup>-1</sup>) of $R_2$ predictions by SeqDYN and MD for 10 IDPs

<sup>a</sup>Based on leave-one-out training (using 44 IDPs).

<sup>b</sup>Helix boost applied.

<sup>c</sup>Based on training by the full training set (45 IDPs).

<sup>d</sup>From ref (1).

<sup>e</sup>RMSE is scaled down by a factor of 2.39, to correct for the effect of temperature (MD at 288

K; see Fig. S2C).

<sup>f</sup>From ref (14).

<sup>g</sup>RMSE is scaled down by a factor of 2.99, to correct for the effects of temperature and

magnetic field (MD at 274 K and 850 MHz; see Fig. S2B).

<sup>h</sup>Originally calculated in ref (12) with correction in ref (45).

<sup>i</sup>From ref (13).

# **FIGURE CAPTIONS**

Figure 1. Representative conformations of five IDPs. (A-E) MKK4,  $\alpha$ -synuclein, Mev-P<sub>NTD</sub>, Sev-NT, and CBP-ID4. Conformations were initially generated using TraDES (http://trades.blueprint.org) (46), selected to have radius of gyration close to predicted by a scaling function  $R_g = 2.54N^{0.522}$  (Å) (47). Conformations for residues predicted as helical by PsiPred plus filtering were replaced by ideal helix. Finally residues are colored according to a scheme ranging from green for low predicted  $R_2$  to red for high predicted  $R_2$ . Figure 2. Properties of the 45 IDPs in the training set. (A) Histograms of means and standard deviations, calculated for individual proteins. Curves are drawn to guide the eye. Inset: correlation between  $\bar{R}_2$  and  $\sigma_{R_2}$ . (B) Experimental mean scaled  $R_2$  (ms $R_2$ ) and SeqDYN qparameters, for the 20 types of amino acids. Note that Pro residues have low ms $R_2$  for the lack of backbone amide proton. Amino acids are in descending order of q.

Figure 3. SeqDYN model parameters. (A) Correlation between  $msR_2$  and q. The values are also displayed as bars in Fig. 2B. (B) Correlation of  $msR_2$  and q with amino-acid molecular mass. (C) Correlation of  $msR_2$  and q with bulkiness. (D) The optimal correlation length and deterioration of SeqDYN prediction as the correlation length is moved away from the optimal value.

Figure 4. Quality of SeqDYN predictions. (A) Histogram of RMSE(-1). Letters indicate RMSE(-1) values of the IDPs to be presented in panels (B-F). (B-F) Measured (bars) and predicted (curves)  $R_2$  profiles for MKK4,  $\alpha$ -synuclein, Mev-P<sub>NTD</sub>, Sev-NT, and CBP-ID4. In (E) and (F), green curves are SeqDYN predictions and red curves are obtained after a helix boost.

Figure 5. Measured (bars) and predicted (curves)  $R_2$  profiles for ChiZ N-terminal region, TIA1 prion-like domain, Pdx1 C-terminal region, synaptobrevin-2,  $\alpha$ -endosulfine, YAP, AMOTL1, FtsQ, and CAHS-8. In (C),  $R_2$  does not fall off at the N-terminus because the sequence is preceded by an expression tag MGSSHHHHHHHHHHHHHS. In (H) and (I), green curves are SeqDYN predictions and red curves are obtained after a helix boost.

Figure 6. Predicted  $R_2$  profiles (curves) for the lysozyme sequence and a mutant show close agreement with those measured (bars) on the proteins in the unfolded state. (A) Wild type. (B) With Trp62 to Gly mutation.





























