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OPEN Design of defect spins in piezoelectric aluminum nitride for solid-state hybrid quantum technologies

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Spin defects in wide-band gap semiconductors are promising systems for the realization of quantum bits, or qubits, in solid-state environments. To date, defect qubits have only been realized in materials with strong covalent bonds. Here, we introduce a strain-driven scheme to rationally design defect spins in functional ionic crystals, which may operate as potential gubits. In particular, using a combination of state-of-the-art *ab-initio* calculations based on hybrid density functional and many-body perturbation theory, we predicted that the negatively charged nitrogen vacancy center in piezoelectric aluminum nitride exhibits spin-triplet ground states under realistic uni- and bi-axial strain conditions; such states may be harnessed for the realization of gubits. The strain-driven strategy adopted here can be readily extended to a wide range of point defects in other wide-band gap semiconductors, paving the way to controlling the spin properties of defects in ionic systems for potential spintronic technologies.

The idea of realizing and harnessing coherent quantum bits in scalable solid-state environments has attracted widespread attention in the past decade¹. One of the milestones in the field has been the coherent manipulation of the single nitrogen-vacancy (NV) defect spin in diamond^{2,3}, opening a new era for using atom-like point defects in crystals as solid-state qubits^{4,5}. However, inherent difficulties in growing and controlling the lattice of C diamond pose severe limitations to the use of the NV center for scalable quantum technologies, begging the question of whether analogs to this defect exist or can be engineered in other technologically mature materials⁶⁻¹⁰, for examples III-V crystals. Exploration of quantum defect spins in functional ionic crystals such as, e.g. w-AlN, would potentially lead to new opportunities in scalable quantum technologies, including the realization of strongly-coupled spin-mechanical resonator hybrid quantum systems¹¹⁻¹³. Indeed, the piezoelectric properties of w-AlN make it an ideal system for measuring and controlling the vibrational motion of the lattice^{14,15} and may offer a variety of control schemes for quantum spins^{8,13}. The strong spontaneous polarization in w-AlN combined with advanced hetero-structuring and band-gap engineering techniques could add flexibility in designing device functionalities¹⁵. Interestingly, w-AIN has recently gained significant attention as an opto-mechanical system^{16,17}, making it attractive as a new host crystal for quantum defect spins.

A key step towards building hybrid quantum systems in ionic crystals, and in particular in aluminum nitride, is the identification of localized spin-triplet states akin to the NV center in diamond⁶. Within a crystalline environment, the spin sublevels of a spin-triplet state may be split even in the absence of an external magnetic field and they can be chosen to function as a quantum bit³. For optical addressability³, the defect center should possess excited spin-triplet states, which can lead to spin-selective decays. These conditions are, however, challenging to realize in ionic crystals for several reasons. In an ionic solid, the energy of defect states derived from dangling bonds is usually close to either the conduction or the valence band edge and, in many cases it may be in strong resonance with that of the bulk band edges⁶. In the case of w-AlN, another critical constraint stems from doping: this material is naturally *n*-type, similar to several other nitrides¹⁸⁻²⁰, and attaining stable *p*-type doping is extremely challenging²¹⁻²⁵, effectively constraining the search for a defect qubit to *n*-type *w*-AlN.

Here, using first-principles calculations²⁶⁻³⁶ we proposed a strain-driven strategy to design stable spin defects in ionic crystals; in particular, we identified the strain conditions leading to the stabilization of localized

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Figure 1. Defect formation energy and spin-state of the native defects in *w*-AlN. Results obtained within PBE (**a**) and formation energy of V_N and O_N computed within PBE0 (**b**). The lowest-energy effective spin for a given charge state is also shown. The inset of (**b**) is a schematic representation of the defect-molecule model of V_N . Only the nearest neighbor Al atoms (numbered spheres) around the vacancy site and the Al sp^3 dangling bonds are shown for clarity. (**c**) Symmetry-adopted molecular orbitals and spin configurations of V_N^- under different symmetry environments. The Jahn-Teller distortions for the S = 0 and the S = 1 states are described by the *e* and $a_1 + e$ symmetrized displacements, respectively, as schematically shown next to the defect level diagrams.

spin-triplet defect states in *w*-AlN. We found that by applying moderate uni- and bi-axial strain to the host lattice in the presence of negatively charged N vacancies, we could stabilize spin-triplet states, which are well-localized within the fundamental gap of *n*-type *w*-AlN. Our calculations also predicted that these defect spins have a number of spin-conserved excited states, which could be used to optically address the spins³, thus making them strong candidates for solid-state implementations of quantum bits in piezoelectric aluminum nitride.

Results

Spin-state and stability of the native defects in w-AIN. We determined the charge state (q) of a given defect D(q) as a function of the Fermi level (E_F) by computing the defect formation energy ($E_f^{D(q)}$)³⁷:

$$E_f^{D(q)}(E_F) = E^{D(q)} - E^H - \sum n_i \mu_i + q(E_F + E_V) + E_{corr}^D(q),$$
(1)

where $E^{D(q)}$ and E^H are the total energies computed for supercells with and without a defect, respectively; μ_i (i = AI, N, O) is the chemical potential and E_F is referred to the valence band edge (E_V). The last term on the right hand side of equation (1) corrects for artificial electrostatic interactions present in calculations with finite-size supercells and we used a correction scheme developed by Freysoldt, Neugebauer, and Van de Walle^{38,39}. Figure 1(a) reports $E_f^{D(q)}$ as a function of the Fermi energy for the native defects of *w*-AlN as obtained within PBE²⁶. The slope of $E_f^{D(q)}(E_F)$ yields the charge state of the defect³⁷; a change in slope indicates a change in the charge state of the most stable defect, as a function of the energy of the Fermi level. The spin of each charge state is also indicated in the figure.

We first considered Al-vacancy (V_{Al})-related defects, including complexes with an N vacancy ($V_{Al}V_N$) and an O impurity at the N site ($V_{Al}O_N$). Paramagnetic states of cation-vacancy-related defects were previously investigated in III-nitrides, in particular GaN^{40,41}. The origin of the high-spin states of these cation-vacancy-related defects was attributed to the strong electron localization of the N 2*p* states leading to a large exchange splitting^{40,41}. Furthermore, two recent theoretical papers suggested that the paramagnetic state of cation vacancy – oxygen

impurity complexes in AlN and GaN may potentially operate as quantum bits, similar to the NV center in diamond^{42,43}. Consistent with previous calculations^{40–43}, we found that the V_{Al}-related defects possess a variety of effective electron spins as shown in Fig. 1(a). However, our calculations showed that the paramagnetic ground states associated with V_{Al}-related defects may not be suitable for quantum bit applications for several reasons: those defects with spin states higher than 1/2 are stable in *p*-doped AlN, which is extremely challenging to achieve^{20,21}; on the other hand, the defects stable in *n*-type AlN have spin zero. Additionally, the dangling bonds left by the presence of an Al vacancy have mainly N 2*p* character and their position in energy is very close to $E_V^{40,41}$. In some cases, e.g. for the V_{Al}O_N complex^{42,43}, the active occupied spin-orbital states are in strong resonance with the valence band due to the large exchange splitting. Therefore, we excluded the V_{Al}-related defects from all possible potential qubit operations. For instance, there may exist excited-state triplets, which may be suitable for quantum operations⁴⁴.

We now turn to the discussion of anion defects, i.e. V_N and O_N , from which the main conclusion of our work will be drawn. In this case, we also obtained results using a level of theory higher than PBE and, in particular, we adopted the PBE0 hybrid functional^{27,28} whose choice is extensively justified in the method section. In addition, we carried out calculations using many-body perturbation theory at the G_0W_0 level³³⁻³⁵. We first note that O_N has no effective spins in its ground state since substitutional oxygen either donates an electron to the host (q = +1) or traps an electron (q = -1), leading to a filled DX state⁴⁵⁻⁴⁷. On the other hand, we found that V_N has S = 1/2 and 3/2 ground states for q = 0 and -2, respectively, in the *n*-type region, as shown in Fig. 1(a) (PBE results) and (b) (PBE0 results)^{25,27}. These findings indicate that the S = 3/2 state of V_N^{2-} might be of potential interest as a defect qubit, but it might be difficult to realize, as highly *n*-doped *w*-AlN is difficult to obtain^{47,48}. Interestingly, the V_N^0 S = 1/2 state has been recently detected using electron paramagnetic resonance^{18,19}. Based on these results, we considered the Fermi level range in the vicinity of the stability region of V_N^0 , which might be accessible in experiments. Interestingly, we found that there is a meta-stable state of V_N^{--} with S = 1.

In Fig. 1 we show the *defect-molecule* model^{49,50} for V_N^- , with the four active Al sp^3 dangling bonds, { φ_i , i = 1 to 4}. The symmetry-adapted molecular orbitals { $a_1(1)$, $a_1(2)$, e_x , e_y]⁵¹ present in an ideal C_{3v} environment are shown in Fig. 1(c). In such an environment, the ground state configuration of V_N^- is $a_1(1)^2 a_1(2)^2$, which is a spin-singlet. Additionally, attaining the $a_1(1)^2 a_1(2)^1 e^1$ spin-triplet state is possible due to the Hund's rule coupling. Interestingly, both the S = 0 and S = 1 configurations undergo strong Jahn-Teller (JT)⁵² distortions (see Fig. 1(c)). A tight-binding model⁵³ with hopping matrix elements, $-t_{ij}$, between states φ_i and φ_j provides a simple picture, and for the S=0 configuration it is easy to show that the a'(2) state is pushed down in energy due to the hybridization with the a'(3) state, thus giving rise to an energy gain. On the other hand, the JT distortion for the S = 1 state results in a different orbital ordering as $\Delta t_{\parallel} \equiv t_{23} - t_{34} > 0$, and the a'(3) state is pushed above a'', diminishing the hybridization between a'(2) and a'' and the S = 1 state is stabilized according to the Hund's rule.

Strain-driven design of defect spins. We found that in the absence of any strain the S = 1 state is higher in energy than the S = 0 one by only 55 meV and 7 meV, at the PBE and PBE0 levels of theory, respectively. Note that 7 meV is within the range of our numerical errors, estimated to be ~20 meV/defect at most (see supplementary information). This means that the two spin states (S = 0 and S = 1) of V_N^- are approximately degenerate in energy within PBE0, although they are associated with two distinct JT-distorted structures, as shown in Fig. 1(c). These results suggest that one may engineer the relative stability of the two spin states by straining the lattice. Strain effects have been extensively explored in nitrides and strain levels up to 4% are considered realistic^{54,55}. Figure 2(a) reports the energy difference between the S = 1 and S = 0 states of V_N^- as a function of compressive uniaxial strain applied to the host AlN lattice along the $[11\overline{2}0]$ direction, and shows that the S = 1 state is significantly lower in energy than the S = 0 state. Even at a small compressive strain of -3%, the S = 1 state is lower in energy by about 0.25 eV than the S = 0 state within PBE0. This energy difference is well outside our numerical errors (see Supplementary Information) and we expect the energy difference to be representative of the free energy difference as well, since vibrational contributions to the free energy will be almost identical in the two spin configurations (see Supplementary Information). The uniaxial strain effect is twofold. The strained lattice environment is favorable for the S = 1 state as the lattice distortion is compatible with the $a_1 + e$ JT mode shown in Fig. 1(c). Furthermore the host lattice expands in the [0001] and $[1\overline{1}00]$ directions according to the Poisson's ratio effect⁵⁶, which is unfavorable for the S = 0 state because it tends to pull apart the Al₃ and Al₄ atoms, as well as the Al_1 and Al_2 atoms. Figure 2(b) reports the defect level diagram of the $V_N^- S = 1$ state under -1% uniaxial strain calculated at the G_0W_0 @PBE level, showing the occupied a'(2) and a'' levels being located almost 2 eV below the conduction band minimum (CBM). We also note that in all cases a'(2) and a'' are almost degenerate in energy. As shown in Table 1, the band gap of AlN increases by 0.18 eV within $G_0 W_0 @PBE$, as the uniaxial strain changes from zero to -3%. However, the energy location of the occupied levels a'(2) and a'' does not vary and it remains 3.9 eV above $E_V(\nu \text{ in Table 1})$, indicating that the ³A" spin-triplet state becomes more localized as the compressive uniaxial strain is increased, a beneficial effect for potential quantum information applications.

We further explored the possible stability of the $S = 1 V_N^-$ defect by considering biaxial strain. Figure 3(a) reports the energy difference between the S = 1 and S = 0 states of V_N^- as a function of biaxial strain applied in the (0001) plane, showing the stabilization of the S = 1 state above 3% strain, within the PBE0 approximation. Under 4% biaxial strain, the S = 1 state is lower in energy by 80 meV than the S = 0 state in PBE0, a result again outside the numerical errors and possible temperature effects (see Supplementary Information). We note that under the biaxial strain considered in Fig. 3(a), the lowest-energy geometry for the S = 0 state is again the $C_{1h}^{(e)}$ JT-distorted structure, with the same orbital ordering shown in Fig. 1(c). However, an increase of biaxial strain to 2% induces a structural transition in the S = 1 state of V_N^- , and the defect symmetry changes from C_{1h} to C_{3v} .





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		Defect orbitals (eV)		
Strain	Band gap (eV)	μ	ν	λ
Strain-free	5.94	0.36	3.90	0.73
Uniaxial, -1%	6.01	0.34	3.91	0.77
Uniaxial, -2%	6.11	0.47	3.93	0.83
Uniaxial, -3%	6.12	0.42	3.89	0.80
Biaxial, 3%	5.35	0.30	3.55	0.66
Biaxial, 4%	5.10	0.20	3.42	0.59

Table 1. Computed electronic properties of the $V_N^- S = 1$ state in *w*-AlN under the uniaxial and biaxial strain discussed in the main text, including the band gap within $G_0W_0@PBE$, the location of the occupied defect orbitals referred to E_V in $G_0W_0@PBE$ (μ,ν,λ shown in Figs 2(b) and 3(b)).

Moreover, the structural transition is accompanied by an a_1 -type displacement, in which Al₄ (see Fig. 1(b)) is moved out of the (0001) plane and up in the *z*-direction, for example by 0.3 Å at 3% biaxial strain. Let us consider a tight-binding model in the C_{3v} symmetry. The orbital energy of the *e*-states and the $a_1(2)$ state are t_{\parallel} and $-t_{\parallel} + \sqrt{t_{\parallel}^2 + 3t_{\perp}^2}$, respectively; here, t_{\parallel} (= $t_{23} = t_{34} = t_{24}$) and $t_{\perp}(= t_{12} = t_{13} = t_{14})$ are the in-plane and out-of-plane hopping constants, which are decreased and increased, respectively, under tensile biaxial strain. Therefore, application of such strain could reverse the orbital order between $e_{x,y}$ and $a_1(2)$ in V_N^- beyond a certain critical strain level and lead to the formation of a ${}^{3}A_2 S = 1$ spin-triplet state, according to Hund's rule. Figure 3(b) reports the G_0W_0 quasi-particle electronic structure of the S = 1 state of V_N^- under 3% biaxial strain, showing the doubly degenerate *e*-states with two spin-up electrons localized in the band gap of *w*-AlN. We found that the band gap of *w*-AlN is decreased from 5.94 eV to 5.35 and 5.10 eV under biaxial strain of 3% and 4%, respectively, within the $G_0W_0@PBE$ approximation (see Table 1). However, in both cases, the *e*-states are well-localized and located deep in the gap, 1.8 eV (3% strain) and 1.7 eV (4% strain) below the CBM, within $G_0W_0@PBE$.

Hyperfine coupling between the V_N^- **defect spin and Al nuclear spins.** Electron paramagnetic resonance (EPR)⁵⁷ is a powerful experimental technique to detect and identify paramagnetic impurities in solids. EPR measurements yield hyperfine parameters, which are mainly determined by the interaction between an impurity's electron spin and the surrounding nuclear spins, thus these measurements play a key role in the identification of point-like paramagnetic impurities in solids⁵⁷. Son and co-workers resolved the detailed hyperfine structure of an electron spin-1/2 in *w*-AlN, mostly interacting with four ²⁷Al nuclei (nuclear spin I = 5/2, 100% natural abundance), and they identified its origin to be V_N^0 with the help of *ab-initio* density functional calculations¹⁸. In Table 2, we report the computed principal values of the hyperfine tensor of V_N^0 and we compare them with



Figure 3. Control of the nitrogen vacancy spin using biaxial lattice strain. (a) Total energy difference between the S = 1 and S = 0 state of V_N^- as a function of the biaxial strain applied in the (0001) plane. The local defect geometry of the S = 0 state maintains a $C_{1h}^{(e)}$ symmetry, as shown in Fig. 1(c), while that of the S = 1 state changes from $C_{1h}^{(a1+e)}$ to $C_{3\nu}$ for biaxial strain larger than 2%. (b) The G₀W₀@PBE quasi-particle electronic structure of the S = 1 state of V_N^- under 3% biaxial strain. The number next to a defect level is the location of the state referred to E_V . Three constants, μ , ν , and λ are used to denote the positions of the occupied defect orbitals (see Table 1).

Center	Atom		A _{xx} (mT)	A _{yy} (mT)	A _{zz} (mT)	CP (mT)	
$V_N^{\ 0}$	41	This work	6.0	6.0	7.5	1.2	
		Theory ¹⁸	6.4	6.5	8.0	-1.2	
	41	This work	6.4	6.4	7.7	1.1	
	Al ₂	Theory ¹⁸	6.7	6.7	8.2	-1.1	
	A1 A1	This work	5.3	5.3	6.9	-1.2	
	$AI_3 AI_4$	Theory ¹⁸	5.9	6.0	7.5–7.6		
EI-1	Al ₁₋₄	Experiment18	~6.0	~6.0	~7.2		



the previous theoretical and experimental data. Our results are in good agreement with all the previous results, supporting the interpretation of the resolved hyperfine structure being derived from V_N^0 .

Similar to V_N^{0} in *w*-AlN, the V_N^{-1} electron spin S = 1 may also interact with the nearest four Al atoms (Al_{1.4} shown in Fig. 1). We calculated the principal values of the hyperfine tensor of V_N^{-1} (S = 1) as a function of strain and the results are reported in Fig. 4. Interestingly, the hyperfine parameters exhibit high sensitivity to the applied strain. For the uniaxial case, the hyperfine parameters (A_{xx} , A_{yy} , and A_{zz}) for Al₂ decrease by -75 MHz as the compressive uniaxial strain is increased from 0 to -3%, while those of Al_{1.34} increase. To understand this trend, we show in Fig. 4 the isotropic Fermi contact term as a function of strain along with the hyperfine parameters. We found that the Fermi contact term, which is mainly determined by the electron spin density localized at the corresponding Al site, is mostly responsible for the change of the hyperfine parameters as a function of strain. Figure 4(a-c) indicate that as a result of uniaxial strain in the $V_N^- S = 1$ state the spin density is transferred from Al₂ to the other Al atoms.

Interestingly, the hyperfine parameters as functions of biaxial strain show a more drastic change. The hyperfine parameters for Al_1 decrease by more than 250 MHz and become negative while those of the other basal Al nuclei (Al_{2-4}) significantly increase. This is due to the structural transition of the defect geometry from C_{1h} to C_{3v} beyond the 2% biaxial strain, as previously discussed. As a result of the transition, beyond 2% strain the Al_2 , Al_3 , and Al_4 nuclei become symmetrically equivalent and hence their hyperfine parameters become equal, as shown in Fig. (e,f). The negative hyperfine parameters of Al_1 are due to the negative spin density localized near the Al_1 atom, which makes the Fermi contact term negative. Before the structural transition occurs, the spin density is



Figure 4. Hyperfine parameters of the V_N^- spin. Principal values (in MHz) of the hyperfine tensors and Fermi contact terms for interaction between the V_N^- electronic spin (S = 1) with the nearest four ²⁷Al nuclei as a function of the uniaxial (**a**-**c**) and biaxial (**d**-**f**) strains. The four ²⁷Al nuclei (Al₁ to Al₄) can be seen in Fig. 1. Note that the applied uniaxial strain and the biaxial strain are compressive (negative value) along the [1120] direction and tensile (positive value) in the (0001) plane, respectively. The local defect geometry of the S = 1 state changes from $C_{1h}^{(a1+e)}$ to C_{3v} for biaxial strain larger than 2%, inducing the drastic change in the hyperfine parameters.

distributed almost equally over the four nearest Al nuclei as it is derived from the a'(2) and a'' orbitals in the C_{1h} symmetry. The structural transition to C_{3v} induces, however, a change in the orbital ordering and the spin density is derived from the e_x and e_y orbitals, which are mainly localized at the basal plane of Al_2 , Al_3 , and Al_4 , leading to increased Fermi contact terms as shown in Fig. 4 (e,f).

Spin-conserved intra-defect excitations in nitrogen vacancy spins. One of the most important properties of the NV center in diamond is the single-spin optical addressability, which relies on the presence of an excited ³E spin-triplet state and its spin-selective decay³. Similar to the diamond NV center, we found that in *w*-AlN the atomic configuration in which the negatively charged N vacancy has a S = 1 ground state also exhibits S = 1 excited states; hence these states could be obtained by a spin-conserving optical excitation from an occupied defect orbital to an empty defect orbital, as shown in Figs 2(b) and 3(b). Some of the empty defect levels are located slightly above the CBM. We note, however, that the lowest-lying empty defect-orbitals are not in resonance with the CBM; they remain localized, as shown by their dispersion-less character in our computed band structure (not shown) due to the following reasons. The lowest conduction band of *w*-AlN is a single parabolic band centered at Γ . The next available conduction states appear close the K and L points and they are located at 0.9 and 1.1 eV above the CBM, respectively, according to previous GW calculations⁵⁸, and consistent with our GW results. Furthermore we found that the CBM mainly exhibits a nitrogen *p* character, leading to a negligible hybridization with the aluminum dangling bonds created by the V_N⁻ defect.

The ZPL was obtained by carrying out calculations of total energy differences (Δ SCF calculations) within the PBE and PBE0 approximation^{59,60}. We first describe possible intra-defect spin-conserving excitation in the spin-down channel, which may be similar to the excitation scheme of the NV center in diamond⁶⁰. In the case of uniaxial strain, we promoted an electron from a'(1) to a'(2) and the resulting configuration corresponds to the optically excited ³A'' spin-triplet state. The ZPL is rather insensitive to the amount of uniaxial strain, up to 3%, and it is calculated to be ~3.2 eV within PBE. A similar excitation for V_N^- under biaxial strain, shown in Fig. 3(b), corresponds to a transition to the excited ³E spin-triplet state; for the ZPL we found 3.35 and 3.25 eV under 3% and 4% biaxial strain, respectively within PBE. We note, however, that these near ultra-violet excitations may lead to photo-ionization of V_N^- to V_N^0 considering the corresponding (0/-1) charge transition level is about 1.1 eV below the conduction band edge, as shown in Fig. 1(b). In the spin-up channel, however, the ZPLs from a'' to a'(3) under uniaxial strain, and from e to $a_1(2)$ under biaxial strain, are expected to be at much lower energies, in the near infrared range. For these cases, we used the PBE0 hybrid functional to better estimate the ZPLs⁶⁰. We find that the spin-up ZPLs are 0.83 eV and 0.89 eV for -1% uniaxial strain and 3% biaxial strain, respectively.

Discussion

We proposed a strain-driven defect design scheme to obtain point defects with localized spin-triplet ground states for implementation of spin qubits in piezoelectric aluminum nitride. We found that negatively charged nitrogen vacancies exhibit localized spin-triplet states in *n*-type aluminum nitride under realistic strain conditions. Nitrogen vacancies are naturally incorporated in aluminum nitride during crystal growth and they are known to be the main source of the intrinsic *n*-type behavior of aluminum nitride^{18–21}, thus making the nitrogen vacancy spins easily amenable to experimental investigations^{18,19}. Extra *n*-type doping control might be achievable by introducing substitutional oxygen impurities (O_N) during crystal growth²⁴. As shown in Fig. 1(a,b), O_N can donate electrons in the region where V_N^0 is stable and provide the extra charge necessary to form V_N^- .

In addition to nitrogen vacancies, V_{Al} -related defects are also commonly observed in experiments^{22,23}. Our calculations showed that such defects could in principle introduce a variety of electron spins in the host lattice, which would make it difficult to isolate a single defect spin for qubit applications. However, as shown in Fig. 1(a), the V_{Al} -related defects are magnetically passivated (i.e. S = 0) in the stability region of V_N^- , thus allowing for the V_N^- spins to be easily isolated for qubit applications.

We showed that both the S = 0 and S = 1 configurations of V_N^- undergo static Jahn-Teller (JT)⁵² distortions as shown Fig. 1(c) and the relative stability of the S = 0 and S = 1 states can be controlled by applying a uniaxial or biaxial strain to the host lattice. Regarding possible temperature effects on the relative stability under strain, dynamic Jahn-Teller effect⁵² might be an important factor to be considered in addition to the vibrational entropy effect discussed in the Supplementary Material. We also note that potential dynamic Jahn-Teller effects at elevated temperature might be strain-dependent, as we found the defect structure and its lattice environment change significantly in response to external strain perturbations. An investigation of potential dynamic Jahn-Teller effects will be the subject of future studies.

We also showed that excited spin-triplet states are present for negatively charged nitrogen vacancies and these states may play an important role in potential optical manipulations of the vacancy spins. We found that the zero phonon lines for a spin-conserving intra-defect excitation in the spin-down and spin-up channels of the V_N^- S = 1 state are in the near ultra-violet and in the near infrared range, respectively. We pointed out that the near ultra-violet excitation could lead to photo-ionization of the V_N^- defect, thus the near infrared excitation may be more suitable for potential optical manipulation of the V_N^- spin.

The excited triplet may couple to the ground state triplet non-radiatively, similar to the NV center in diamond. We note, however, that additional important issues remain to be considered in order to address the potential optical manipulation of the V_N^- spin. The optical manipulation of the NV center is based on the spin-orbit-induced spin-selective decay through dark singlet states³. For the V_N^- system studied here there are open-shell singlet states such as 1A_1 or 1E states in the C_{3v} symmetry case and ${}^1A''$ in C_{1h} , which may be close in energy to the 3A_2 triplet in C_{3v} and the ${}^3A''$ triplet in C_{1h} , respectively. These single states may play a role in the optical manipulation of the V_N^- spin. However, whether these singlet states are positioned in energy between the ground spin triplet and the excited triplet remains to be seen⁶¹, as well as whether the spin-orbit interaction between the excited triplet states is sufficiently strong to couple them. We further note that the C_{3v} symmetry of the NV center in diamond is responsible for specific selection rules for the spin-selective decay⁶². The V_N^- defect in *w*-AlN has the C_{3v} symmetry only under the biaxial strain, while it has C_{1h} symmetry under uniaxial strain; such symmetry difference may be an important factor in establishing the potential optical manipulation of the V_N^- spin.

It is worth mentioning that a number of alternative strain-driven spin manipulation and readout schemes are being actively developed in the literature^{63,64}, and the V_N^- spins proposed in our study may lead to excellent platforms for the implementation of strain-driven spin control schemes due to the strong piezoelectricity of the host lattice⁸.

Methods

Ab-initio charged defect calculations. We carried out density functional theory (DFT) calculations with semi-local (PBE²⁶) and hybrid (PBE0^{27,28}) functionals, using plane wave basis sets (with a cutoff energy of 75 Ry), norm-conserving pseudopotentials²⁹, and the Quantum Espresso code³⁰. In the case of *w*-AlN, the self-consistent Hartree-Fock mixing parameter, as derived using the method of Ref. [28], is 24%²⁸, which justifies the use of the PBE0 hybrid functional, whose mixing parameter is defined to be 25% (see below). We examined the most common native defects, which may be easily accessible in experiment (including Al^{22,23} and N vacancies^{18,19}, O impurities²⁴, and cation-anion defect complexes^{23,25}). To mimic the presence of isolated defects, we employed supercells with 480 and 96-atoms, when using the PBE and PBE0 approximations, respectively, and full geometry optimizations were performed with both functionals. We sampled the Brillouin zone by a 2 × 2 × 2 *k*-point mesh. Numerical errors in terms of supercell size, k-point sampling and the plane wave cutoff energy were examined and are summarized in the supplementary information. We considered 7 different types of defects and 6 to 7 different charge states for each of them, in addition to 2 to 3 spin multiplicities for each case. For all defect states, total energy minimizations were started from three different initial geometries (with symmetry C_{3v} and C_{1h}) and the state with the lowest energy was selected as the ground state. In total, we explored approximately 300 different defect states.

The use of PBE0 to describe AlN is appropriate, based on our recent work²⁸, as the average electronic dielectric constant of AlN is ~ 4.1^{28} and we expect the optimal amount of the Hartree-Fock mixing to be 1/4.1 = 24%, which

	Lattice parameters		Electronic properties		Dielectric constants		
	a (Å)	c/a	и	E _g (eV)	$\Delta_{\rm CF}$ (meV)	Electronic ($\epsilon_{\infty,\parallel}/\epsilon_{\infty,\perp}$)	Static ($\epsilon_{0,\parallel}/\epsilon_{0,\perp}$)
PBE	3.130	1.603	0.382	4.09	-201	4.42/4.63	8.33/9.77
PBE0	3.107	1.601	0.382	6.35	-223	4.06/4.22	7.71/8.95
Experiment	3.110 ³⁶	1.601 ³⁶	0.382 ³⁶	6.0-6.3 ³⁶	-23036	$4.13\pm 0.02^{67}/4.27\pm 0.05^{67}$	(not known)/9.18 ⁶⁸ , 8.5 (poly-crystalline) ⁶⁹

Table 3. Computed electronic and structural properties of *w*-AlN using PBE and PBE0 compared to the experimental values, including the lattice constant, the direct band gap (E_g), the crystal field splitting (Δ_{CF}) and the electronic and static dielectric constants.

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is almost identical to the 25% mixing parameter entering the definition of the PBE0 functional. The accuracy of the PBE0 functional to describe pristine AlN was checked for several properties, which are summarized in Table 3 and are all in excellent agreement with experiment. In particular, using the PBE0 functional we calculated the electronic and static dielectric constants of AlN with a combined finite E-field and Berry phase method^{65,66}. We calculated the electronic dielectric constants to be 4.06 and 4.22 for $\epsilon_{\infty,\parallel}$ and $\epsilon_{\infty,\perp}$, respectively, to be compared with experimental values of 4.13 ± 0.02 for $\epsilon_{\infty,\parallel}$ and 4.27 ± 0.05 for $\epsilon_{\infty,\perp}^{67}$. For the static dielectric constants, we calculated $\epsilon_{0,\parallel}$ and $\epsilon_{0,\perp}$ to be 7.71 and 8.95, respectively, to be compared with experimental values of 9.18 fore_{0,\perp}⁶⁸ and the result of 8.5 obtained from polycrystalline AlN⁶⁹. Note that PBE0 accurately describes the anisotropic nature of the dielectric constants of AlN. The accuracy of the PBE0 functional to describe the native defects in AlN was checked by calculating defect formation energies and charge transition levels of the N vacancy and O impurity as shown in Fig. 1(b). Recently, similar results using another hybrid functional (HSE) were reported in Ref. [25]; the authors were able to successfully explain the experimentally observed optical absorption and emission of the defects and we verified that our PBE0 results are in almost perfect agreement with those of Ref. [25].

The zero-phonon line (ZPL) was obtained by carrying out calculations of total energy differences (Δ SCF calculations) within the PBE and PBE0 approximation^{59,60}. We employed 480-atom and 288-atom supercells along with 75 Ry and 65 Ry plane-wave cutoff energies for the PBE and PBE0 calculations, respectively. By using the PBE functional, we checked the numerical error induced by reducing the supercell size from 480 atoms to 288 atoms and the plane-wave cutoff energy from 75Ry to 65Ry to be around 0.05 eV.

First-principles calculations of hyperfine tensors. We carried out calculations of hyperfine tensors between V_N spins and nuclear spins in *w*-AlN at the PBE level of theory. The calculations were performed in two steps. First, we calculated the ground-state wavefunctions for V_N using the 480-atom supercell as described in the previous section. Then, we used the gauge-including projector-augmented wave method (GIPAW) of Ref. [70] to calculate the hyperfine tensor, which is comprised of the isotropic Fermi contact term and the anisotropic dipolar coupling term. Numerical convergence in terms of the energy cutoff, the k-point sampling, and the supercell size was checked, with a numerical error in the hyperfine tensor less than 10 MHz. To verify the accuracy of the PBE functional, we calculated the hyperfine parameters of the neutral V_N spin (S = 1/2) and compared them to previous theoretical and experimental results¹⁸ as shown in Table 2. We found an excellent agreement between our and previous results. In addition, we found that adding core polarization effects^{71,72} improves the agreement between our results and experiment, thus we included core polarization effects throughout all of our calculations.

Large-scale many-body GW calculations. In order to check the robustness of our predictions, we carried out calculations of quasi-particle energies within the G_0W_0 approximation^{31,32}, using the Γ point only and 480-atom supercells with defect geometries optimized at the PBE level of theory. GW calculations were performed utilizing a spectral decomposition technique for the dielectric matrix^{33,34} and an efficient contour deformation technique for frequency integration³⁵, as implemented in the WEST code (www.west-code.org), where the evaluation of virtual electronic states is not required. Calculations carried out with the WEST code started from the results obtained with the semi-local PBE functional and perturbative corrections to the Kohn-Sham eigenvalues were obtained. The massively parallel implementation of the GW method in WEST takes advantage of separable expressions for both the Green's function (G) and the screened Coulomb interaction (W). The newly developed technique for large-scale GW calculations allowed us to explore defective AlN systems of unprecedented size, containing ~2000 electrons. For the band gap of *w*-AlN, we obtained 5.94 eV within the G_0W_0 @ PBE approximation using our 480-atom supercell with a point defect, which is in very good agreement with the previous G_0W_0 @LDA results of 5.8 eV⁵⁸ and 6.08 eV⁷³ obtained for the pristine bulk.

References

- Awschalom, D. D., Bassett, L. C., Dzurak, A. S., Hu, E. L. & Petta, J. R. Quantum spintronics: engineering and manipulating atomlike spins in semiconductors. Science 339, 1174–1179 (2013).
- Gruber, A. et al. Scanning confocal optical microscopy and magnetic resonance on single defect centers. Science 276, 2012–2014 (1997).
- 3. Jelezko, F. *et al.* Observation of coherent oscillation of a single nuclear spin and realization of a two-qubit conditional quantum gate. *Phys. Rev. Lett* **93**, 130501 (2004).
- 4. Bernien, H. et al. Heralded entanglement between solid-state qubits separated by three metres. Nature 497, 86-90 (2013).
- 5. Kucsko, G. et al. Nanometre-scale thermometry in a living cell. Nature 500, 54-58 (2013).
- 6. Weber, J. R. et al. Quantum computing with defects. Proc. Nat. Acad. Sci. 107, 8513-8518 (2010).

- Koehl, W. F., Buckley, B. B., Heremans, F. J., Calusine, G. & Awschalom, D. D. Room temperature coherent control of defect spin qubits in silicon carbide. *Nature* 479, 84–87 (2011).
- Falk, A. L. et al. Electrically and mechanically tunable electron spins in silicon carbide color centers. Phys. Rev. Lett. 112, 187601 (2014).
- 9. Widmann, M. et al. Coherent control of single spins in silicon carbide at room temperature. Nature Mater. 14, 164–168 (2015).

10. Christle, D. J. *et al.* Isolated electron spins in silicon carbide with millisecond coherence times. *Nature Mater.* **14**, 160–163 (2015). 11. Ovartchaiyapong, P., Lee, K. W., Myers, B. A. & Bleszynski Jayich, A. C. Dynamic strain-mediated coupling of a single diamond spin

- to a mechanical resonator. *Nat. Commun.* 5, 4429 (2014).
 12. Kepesidis, K. V., Bennett, S. D., Portolan, S., Lukin, M. D. & Rabl, P. Phonon cooling and lasing with nitrogen-vacancy centers in diamond. *Phys. Rev. B* 88, 064105 (2013).
- Treutlein, P., Genes, C., Hammerer, K., Poggio, M. & Rabl, P. Hybrid mechanical systems, in *Cavity Optomechanics*, ed. by Aspelmeyer, M., Kippenberg, T. J. & Marquardt, F. (Springer, Berlin 2014) p. 327.
- Piazzaa, G., Felmetsgera, V., Muralta, P., Olsson III, R. H. & Rubya, R. Piezoelectric aluminum nitride thin films for microelectromechanical systems. MRS Bulletin 37, 1051-1061 (2012).
- 15. Egawa, T. & Oda, O. III-Nitride Based Light Emitting Diodes and Applications, edited by Seong, T.-Y., Han, J., Amano, H. & Morkoc, H. (Springer, Berlin, 2013).
- 16. Xiong, C. et al. Aluminum nitride as a new material for chip-scale optomechanics and nonlinear optics. New J. Phys. 14, 095014 (2012).
- 17. Bochmann, J., Vainsencher, A., Awschalom, D. D. & Cleland, A. N. Nanomechanical coupling between microwave and optical photons. *Nature Phys.* 9, 712–716 (2013).
- 18. Son, N. T. et al. Defects at nitrogen site in electron-irradiated AlN. Appl. Phys. Lett. 98, 242116 (2011).
- 19. Soltamov, V. A. et al. EPR and ODMR defect control in AlN bulk crystals. Phys. Stat. Sol. (c) 10, 449-452 (2013).
- 20. Buckeridge, J. *et al.* Determination of the nitrogen vacancy as a shallow compensating center in GaN doped with divalent metals. *Phys. Rev. Lett.* **114**, 016405 (2015).
- Zhang, Y., Liu, W. & Niu, H. Native defect properties and *p*-type doping efficiency in group-IIA doped wurtzite AlN. *Phys. Rev. B* 77, 035201 (2008)
- 22. Sedhain, A., Du, L., Edgar, J. H., Lin, J. Y. & Jiang, H. X. The origin of 2.78 eV emission and yellow coloration in bulk AlN substrates. *Appl. Phys. Lett.* **95**, 262104 (2009).
- 23. Mäki, J.-M. et al. Identification of the V_{Al}-O_N defect complex in AlN single crystals. Phys. Rev. B 84, 081204R (2011).
- 24. Bickermann, M., Epelbaum, B. M. & Winnacker, A. Characterization of bulk AlN with low oxygen content. J. Cryst. Growth 269, 432–442 (2004).
- 25. Yan, Q., Janotti, A., Scheffler, M. & Van de Walle, C. G. Origins of optical absorption and emission lines in AlN. Appl. Phys. Lett. 105, 111104 (2014).
- 26. Perdew, J. P., Burke, K. & Ernzerhof, M. Generalized gradient approximation made simple. Phys. Rev. Lett. 77, 3865–3868 (1997).
- Adamo, C. & Barone, V. Toward reliable density functional methods without adjustable parameters: The PBE0 model. J. Chem. Phys. 110, 6158–6170 (1999).
- 28. Skone, J. H., Govoni, M. & Galli, G. Self-consistent hybrid functional for condensed systems. Phys. Rev. B 89, 195112 (2014).
- Troullier, N. & Martins, J. L., Efficient pseudopotentials for plane-wave calculations. *Phys. Rev. B* 43, 1993–2006 (1991).
 Giannozzi, P. et al. QUANTUM ESPRESSO: a modular and open-source software project for quantum simulations of materials. *J. Phys. Condens. Matter* 21, 395502 (2009)
- Hedin, L. New method for calculating the one-particle Green's function with application to the electron-gas problem. *Phys. Rev.* 139, A796–A828 (1965).
- 32. Hybertsen, M. S. & Louie, S. G. First-principles theory of quasiparticles: calculation of band gaps in semiconductors and insulators. *Phys. Rev. Lett.* 55, 1418–1421 (1985).
- Nguyen, H.-V., Pham, T. A., Rocca, D. & Galli, G. Improving accuracy and efficiency of calculations of photoemission spectra within the many-body perturbation theory. *Phys. Rev. B* 85, 081101 (2012).
- Pham, T. A., Nguyen, H.-V., Rocca, D. & Galli, G. GW calculations using the spectral decomposition of the dielectric matrix: Verification, validation and comparison of methods. *Phys. Rev. B* 87, 155148 (2013).
- 35. Govoni, M. & Galli, G. Large scale GW calculations. J. Chem. Theory Comput., 11, 2680-2696 (2015).
- 36. Rinke, P. et al. M. Consistent set of band parameters for the group-III nitrides AlN, GaN, and InN. Phys. Rev. B 77, 075202 (2008).
- 37. Freysoldt, C. et al. First-principles calculations for point defects in solids. Rev. Mod. Phys. 86, 253-305 (2014).
- Freysoldt, C., Neugebauer, J. & Van de Walle, C. G. Fully ab initio finite-size corrections for charged-defect supercell calculations. *Phys. Rev. Lett.* 102, 016402 (2009).
- 39. Komsa, H., Rantala, T. T. & Pasquarello, A. Finite-size supercell correction schemes for charged defect calculations. *Phys. Rev. B* 86, 045112 (2012).
- Gohda, Y. & Oshiyama, A. Stabilization mechanism of vacancies in group-III nitrides: exchange splitting and electron transfer. J. Phys. Soc. Jpn. 79, 083705 (2010).
- 41. Dev, P., Xue, Y. & Zhang, P. Defect-induced intrinsic magnetism in wide-gap III nitrides. *Phys. Rev. Lett.* **100**, 117204 (2008).
- 42. Tu, Y. et al. A paramagnetic neutral V_{AI}O_N center in wurtzite AlN for spin qubit application. Appl. Phys. Lett. 103, 072103 (2013).
- 43. Wang, X. et al. Spin-polarization of V_{Ga}O_N center in GaN and its application in spin qubit. Appl. Phys. Lett. 100, 192401 (2012).
- 44. Lee, S. et al. Readout and control of a single nuclear spin with a metastable electron spin ancilla. Nature Nanotech. 8, 487-492 (2013).
- 45. Park, C. H. & Chadi, D. J. Stability of deep donor and acceptor centers in GaN, AlN and BN. Phys. Rev. B 55, 12995–13001 (1997).
- 46. Van de Walle, C. G. DX-center formation in wurtzite and zinc-blende $Al_xGa_{1-x}N$. *Phys. Rev. B* 57, R2033–R2036 (1998).
- 47. Silvestri, L., Dunn, K., Prawer, S. & Ladouceur, F., Hybrid functional study of Si and O donors in wurtzite AlN. Appl. Phys. Lett. 99, 122109 (2011).
- 48. Schulz, T. et al. n-type conductivity in sublimation-grown AlN bulk crystals. Phys. Stat. Solidi (RRL) 1, 147-149 (2007).
- 49. Coulson, C. A. & Kearsley, M. J. Colour centres in irradiated diamonds. I. Proc. R. Soc. London Ser. A 241, 433-454 (1957).
- 50. Loubser, J. H. N. & van Wyk, J. P. Diamond Research (London) (Industrial Diamond Information Bureau, London, 1977), pp. 11–15.
- 51. Lenef, A. & Rand, S. C. Electronic structure of the N-V center in diamond: theory. *Phys. Rev. B* 53, 13441–13455 (1996).
- 52. Bersuker, I. B. The Jahn-Teller Effect (Cambridge University Press, Cambridge, 2006)
- 53. Harrison, W. A. Electronic Structure and the Properties of Solids (Dover Publication Inc., New York, 1989).
- 54. Yan, Q., Rinke, P., Janotti, A., Scheffler, M. & Van de Walle, C. G. Effects of strain on the band structure of group-III nitrides. *Phys. Rev. B* 90, 125118 (2014).
- 55. Jones, E. et al. Towards rapid nanoscale measurement of strain in III-nitride heterostructures. Appl. Phys. Lett. 103, 231904 (2013).
- 56. Nye, J. F. Physical Properties of Crystals: Their Representation by Tensors and Matrices (Oxford University Press Inc., New York, 1985).
- Schweiger, A. & Jeschke, G. Principles of pulse electron paramagnetic resonance (Oxford University Press Inc., New York, 2001)
 Rubio, A., Corkill, J. L., Cohen, M. L., Shirley, E. L. & Louie, S. G. Quasiparticle band structure of AlN and GaN. Phys. Rev. B 48,
- 11810–11816 (1993).
- 59. Gali, A., Fyta, M. & Kaxiras, E. Ab initio supercell calculations on nitrogen-vacancy center in diamond: electronic structure and hyperfine tensors. *Phys. Rev. B* 77, 155206 (2008).

- Gali, A., Janzén, E., Deák, P., Kresse, G. & Kaxiras, E. Theory of spin-conserving excitation of the N-V⁻ center in diamond. *Phys. Rev. Lett.* 103, 186404 (2009).
- 61. Choi, S., Jain, M. & Louie, S. G. Mechanism for optical initialization of spin in NV⁻ center in diamond. *Phys. Rev. B* 86, 041202 (2012).
- 62. Goldman, M. L. et al. State-selective intersystem crossing in nitrogen-vacancy centers. Phys. Rev. B 91, 165201 (2015).
- 63. MacQuarrie, E. R. *et al.* Coherent control of a nitrogen-vacancy center spin ensemble with a diamond mechanical resonator. *Optica* 2, 233–238 (2015).
- 64. Struck, P. R., Wang, H. & Burkard, G. Nanomechanical readout of a single spin. Phys. Rev. B 89, 045404 (2014).
- Souza, I., Íñiguez, J. & Vanderbilt, D. First-Principles Approach to Insulators in Finite Electric Fields. *Phys. Rev. Lett.* 89, 117602 (2002).
- 66. Umari, P. & Pasquarello, A. Ab initio Molecular Dynamics in a Finite Homogeneous Electric Field. *Phys. Rev. Lett.* **89**, 157602 (2002).
- 67. Shokhovets, S. *et al.* Determination of the anisotropic dielectric function for wurtzite AlN and GaN by spectroscopic ellipsometry. *J. Appl. Phys.* **94**, 307–312 (2003).
- Malengreaua, F. et al. Epitaxial growth of aluminum nitride layers on Si(111) at high temperature and for different thicknesses. J. of Mater. Res. 12, 175–188 (1997).
- 69. Akasaki, I. & Hashimoto, M. Infrared lattice vibration of vapour-grown AlN. Solid State Comm. 5, 851-853 (1967).
- 70. Pickard, C. J. & Mauri, F. All-electron magnetic response with pseudopotentials: NMR chemical shifts. *Phys. Rev. B* 63, 245101 (2001).
- Bahramy, M. S., Sluiter, M. H. F. & Kawazoe, Y. Pseudopotential hyperfine calculations through perturbative core-level polarization. Phys. Rev. B 76, 035124 (2007).
- 72. Filidou, V., Ceresoli, D., Morton, J. J. L. & Giustino, F. First-principles investigation of hyperfine interactions for nuclear spin entanglement in photoexcited fullerenes. *Phys. Rev. B* 85, 115430 (2012).
- 73. Cociorva, D., Aulbur, W. G. & Wilkins, J. W. Quasiparticle calculations of band offsets at AlN-GaN interfaces. *Solid State. Commun.* **124**, 63–66 (2002).

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Author Contributions

H.S. and G.G. designed the research. Most of the calculations were performed by H.S., with contributions from all authors. M.G. implemented the GW many-body perturbation theory in the WEST code. All authors contributed to the analysis and discussion of the data and the writing of the manuscript.

Additional Information

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