

## Fullerenes | Hot Paper |

 Synthesis and Isolation of the Titanium–Scandium Endohedral Fullerenes— $\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$ ,  $\text{Sc}_2\text{TiC}@D_{5h}\text{-C}_{80}$  and  $\text{Sc}_2\text{TiC}_2@I_h\text{-C}_{80}$ : Metal Size Tuning of the  $\text{Ti}^{\text{IV}}/\text{Ti}^{\text{III}}$  Redox PotentialsKatrin Junghans,<sup>[a]</sup> Kamran B. Ghiassi,<sup>[b]</sup> Nataliya A. Samoylova,<sup>[a]</sup> Qingming Deng,<sup>[a]</sup> Marco Rosenkranz,<sup>[a]</sup> Marilyn M. Olmstead,<sup>\*[b]</sup> Alan L. Balch,<sup>\*[b]</sup> and Alexey A. Popov<sup>\*[a]</sup>

**Abstract:** The formation of endohedral metallofullerenes (EMFs) in an electric arc is reported for the mixed-metal Sc–Ti system utilizing methane as a reactive gas. Comparison of these results with those from the Sc/CH<sub>4</sub> and Ti/CH<sub>4</sub> systems as well as syntheses without methane revealed a strong mutual influence of all key components on the product distribution. Whereas a methane atmosphere alone suppresses the formation of empty cage fullerenes, the Ti/CH<sub>4</sub> system forms mainly empty cage fullerenes. In contrast, the main fullerene products in the Sc/CH<sub>4</sub> system are Sc<sub>4</sub>C<sub>2</sub>@C<sub>80</sub> (the most abundant EMF from this synthesis), Sc<sub>3</sub>C<sub>2</sub>@C<sub>80</sub>, isomers of Sc<sub>2</sub>C<sub>2</sub>@C<sub>82</sub>, and the family Sc<sub>2</sub>C<sub>2n</sub> (2n = 74, 76, 82, 86, 90, etc.), as well as Sc<sub>3</sub>CH@C<sub>80</sub>. The Sc–Ti/CH<sub>4</sub> system produces

the mixed-metal Sc<sub>2</sub>TiC@C<sub>2n</sub> (2n = 68, 78, 80) and Sc<sub>2</sub>TiC<sub>2</sub>@C<sub>2n</sub> (2n = 80) clusterfullerene families. The molecular structures of the new, transition-metal-containing endohedral fullerenes, Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub>, Sc<sub>2</sub>TiC@D<sub>5h</sub>-C<sub>80</sub>, and Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub>, were characterized by NMR spectroscopy. The structure of Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> was also determined by single-crystal X-ray diffraction, which demonstrated the presence of a short Ti=C double bond. Both Sc<sub>2</sub>TiC- and Sc<sub>2</sub>TiC<sub>2</sub>-containing clusterfullerenes have Ti-localized LUMOs. Encapsulation of the redox-active Ti ion inside the fullerene cage enables analysis of the cluster–cage strain in the endohedral fullerenes through electrochemical measurements.

## Introduction


Creating molecules with unprecedented structural, chemical, electronic, and magnetic properties is the main motivation behind the developments in the field of endohedral fullerenes (EMFs). In this class of molecules, carbon cages of various sizes can encapsulate one, two, or three metal atoms as well as complex clusters comprising of up to seven atoms.<sup>[1]</sup> The vast majority of endohedral clusterfullerenes is based on Group III


metals, including Sc, Y, and lanthanides. In particular, Sc provides the largest variety of clusterfullerenes, such as nitrides (Sc<sub>3</sub>N@C<sub>2n</sub> (2n = 68, 70, 78–82)<sup>[2]</sup>), carbides with one or two interior carbon atoms (Sc<sub>4</sub>C@C<sub>2n</sub> (2n = 80, 82),<sup>[3]</sup> Sc<sub>2</sub>C<sub>2</sub>@C<sub>2n</sub> (2n = 72–88),<sup>[4]</sup> Sc<sub>3</sub>C<sub>2</sub>@C<sub>80</sub>,<sup>[5]</sup> Sc<sub>4</sub>C<sub>2</sub>@C<sub>80</sub><sup>[6]</sup>), carbohydrides (Sc<sub>3</sub>CH@C<sub>80</sub>,<sup>[7]</sup> Sc<sub>4</sub>C<sub>2</sub>H@C<sub>80</sub><sup>[8]</sup>), oxides (Sc<sub>2</sub>O@C<sub>2n</sub> (2n = 70–82),<sup>[9]</sup> Sc<sub>4</sub>O<sub>2</sub>@C<sub>80</sub>,<sup>[10]</sup> Sc<sub>4</sub>O<sub>3</sub>@C<sub>80</sub><sup>[11]</sup>), sulfides (Sc<sub>2</sub>S@C<sub>2n</sub> (2n = 70–82)<sup>[12]</sup>), cyanide (Sc<sub>3</sub>CN@C<sub>2n</sub> (2n = 78, 80)<sup>[13]</sup>), and even mixed carbidocyanide (Sc<sub>3</sub>C<sub>2</sub>CN@C<sub>80</sub>).<sup>[14]</sup>

Fullerenes are electro-active and form a special type of non-innocent π ligand for the metals inside. Yet, there are certain endohedral species, which can exhibit their own redox activity in the potential window of the carbon cage.<sup>[15]</sup> In this situation, the fullerene cage plays the role of an “electron-transparent” container that protects the endohedral charge states from the environment. Thus, a combination of the stable carbon cage shielding the endohedral species from the environment with the encapsulation of the redox pair (be it a particular metal or part of the cluster) presents the opportunity to change the properties of the EMF of interest. Although some Group III metal clusterfullerenes exhibit an endohedral redox activity due to the complex electronic structure of the cluster (e.g., Sc<sub>3</sub>N@I<sub>h</sub>-C<sub>80</sub> and its derivatives,<sup>[16]</sup> Sc<sub>4</sub>O<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub>,<sup>[17]</sup> or Sc<sub>3</sub>CN@I<sub>h</sub>-C<sub>80</sub><sup>[18]</sup>), encapsulation of redox-active metal ions is an appealing approach to create endohedrals with electrochemical activity. Transition metals, with their rich electrochemistry and variety of spin states, would be ideal for the formation of new endo-

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hedral species for electronically and magnetically tunable EMFs.

The number of structurally characterized EMFs that involve transition metals is quite limited. Group IV metals have been found to form EMFs in early laser ablation experiments (Ti@ $T_r$ - $C_{28}$  being most famous,<sup>[19]</sup> and its formation mechanism has been recently disclosed<sup>[20]</sup>). However, the bulk synthesis of  $M^{IV}$ -EMFs was delayed for almost a decade, until the reports on the arc-discharge synthesis and isolation of  $Ti_2C_{80}$  and three isomers of  $Ti_2C_{84}$  by Shinohara et al.<sup>[21]</sup> It was later determined that  $Ti_2C_{80}$  was actually a carbide clusterfullerene, that is,  $Ti_2C_2@D_{3h}$ - $C_{78}$ .<sup>[22]</sup> Another Ti-based clusterfullerene, namely,  $Ti_2S@D_{3h}$ - $C_{78}$ , was obtained by Echegoyen et al.<sup>[23]</sup> Note that both Ti-based EMFs utilize the  $D_{3h}$ - $C_{78}$  cage. Hafnium was also reported to yield small amounts of the EMFs  $Hf_2C_{80}$  and  $HfC_{84}$ , but their structures have not been determined yet.<sup>[24]</sup>

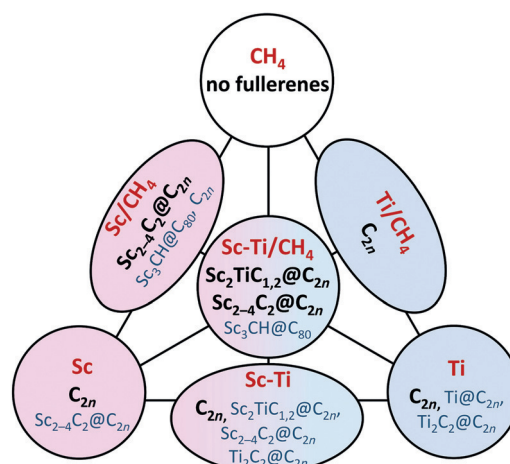
Another strategy for the encapsulation of transition metals within EMFs was first applied by Yang and coworkers. The process employed the use of Group III metals (which readily form EMFs) as “templates” to create mixed-metal clusterfullerenes. When titanium was mixed with Sc or Y, the nitride clusterfullerenes  $TiM_2N@I_h$ - $C_{80}$  ( $M = Sc, Y$ ) were obtained when a nitrogen atmosphere was involved in the arc synthesis.<sup>[25]</sup> The first successful synthesis of vanadium EMFs, that is,  $VSc_2N@I_h$ - $C_{80}$  and  $V_2ScN@I_h$ - $C_{80}$ , utilized a similar strategy.<sup>[26]</sup> It is noteworthy that vanadium-containing EMFs are not formed through laser-ablation experiments.<sup>[27]</sup> By using the reactive gas atmosphere method, we have discovered that a Ti–lanthanide system formed a special type of  $\mu_3$ -C carbido clusterfullerene featuring a Ti=C double bond,  $M_2TiC@I_h$ - $C_{80}$  ( $M = Y, Nd, Gd, Dy, Er, Lu$ ).<sup>[28]</sup> Such clusterfullerenes are formally isostructural and isoelectronic with the nitride clusterfullerenes  $M_2ScN@I_h$ - $C_{80}$  and can be synthesized with high selectivity when methane is added to the arc-discharge reactor atmosphere.

In this article, we explore the formation of endohedral metallofullerenes in the mixed-metal Sc–Ti system by using the reactive gas method with methane and study their electrochemical properties. The mutual influence of the two metals in the synthesis of clusterfullerenes is studied. Finally, electrochemical studies reveal a systematic dependence of the reduction potentials on the endohedral  $Ti^{IV}/Ti^{III}$  redox couple in a series of Ti–lanthanide carbide clusterfullerenes. This is characteristic of the size of the lanthanide, which is interpreted as a manifestation of the inherent cage/cluster strain present in many clusterfullerenes.

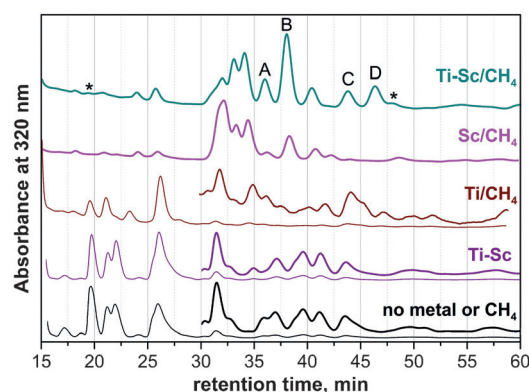
## Results and Discussion

### Synthesis of EMFs

Methane was shown to be an efficient reactive gas in the synthesis of endohedral metallofullerenes that suppressed the yield of empty cage fullerenes and produced carbide clusterfullerenes as the main fullerene products.<sup>[3,28a]</sup> To obtain a complete overview on the influence of the individual metals, a series of arc-discharge syntheses with Sc, Ti, and  $CH_4$  was performed. The results are summarized in Figure 1 and select-



**Figure 1.** Overview of the EMF syntheses conditions and resulting fullerenes (the amount of graphite and helium gas is constant for all syntheses). Initial conditions (metals and reactive gas) are printed in red, the main fullerene products in black, and the minor fullerene products in blue.



**Figure 2.** HPLC chromatograms of raw fullerene mixtures synthesized under different conditions (Buckyprep column, toluene as eluent). A–D denote the fractions with a large content of mixed  $Sc_2Ti$  carbide clusterfullerenes, asterisks mark the minor  $Sc_2Ti$  clusterfullerene fractions. The retention times of  $C_{60}$  and  $C_{70}$  are  $t_r = 9.2$  and  $14.3$  min, respectively (not shown). The other empty fullerenes elute at  $t_r = 18.9$  ( $C_{76}$ ),  $20.5$ – $21.2$  ( $C_{78}$ ),  $26.5$  min ( $C_{84}$ ).

ed high-pressure liquid chromatography (HPLC) chromatograms of the raw  $CS_2$  extracts are shown in Figure 2.

When methane was used as a reactive gas in the arc-discharge synthesis, no empty cage fullerenes were formed. However, others have reported the isolation of  $C_{64}H_4$ <sup>[29]</sup> and  $C_{70}CH_2$ <sup>[30]</sup> in somewhat different arc-discharge syntheses by using methane. In the Sc/ $CH_4$  system, the main fullerene products are carbide clusterfullerenes, including  $Sc_4C_2@C_{80}$  (the most abundant EMF, retention time  $t_r = 32$  min),  $Sc_3C_2@C_{80}$  ( $t_r = 39$  min), isomers of  $Sc_2C_2@C_{82}$  and the family  $Sc_2C_{2n}$  ( $2n = 74, 76, 82, 86, 90$ , etc.), as well as  $Sc_3CH@C_{80}$  (see also Refs. [3], [7b]). Some amounts of  $Sc_3N@C_{80}$  are also formed because of the presence of trace nitrogen in the generator. Surprisingly, a completely different behavior was observed in the Ti/ $CH_4$  system. Instead of producing Ti–carbide EMFs, we found that Ti has a suppressing influence of  $CH_4$  during the synthesis. As a result, the Ti/ $CH_4$  system produced only empty cage ful-

lerenes, but with a considerably different size and isomeric distribution (compare the HPLC curves in Figure 2, see also Figure S1 in the Supporting Information). Formation of Ti EMFs in the Ti/CH<sub>4</sub> system could not be detected even by mass spectrometry.

The mixed-metal Sc–Ti/CH<sub>4</sub> system was also examined. Figure 2 shows that in the mixed-metal system methane efficiently suppresses empty cage-fullerene formation. One of the major differences between the Sc/CH<sub>4</sub> and Sc–Ti/CH<sub>4</sub> systems is the decrease in the yield of Sc<sub>4</sub>C<sub>2</sub>@C<sub>80</sub> in the presence of Ti. Sc<sub>4</sub>C<sub>2</sub>@C<sub>80</sub> is the main EMF formed in the Sc/CH<sub>4</sub> synthesis, but it is a minor component in the Sc–Ti/CH<sub>4</sub> system. Another major difference involves the formation of a series of mixed-metal Sc<sub>2</sub>TiC<sub>x</sub> clusterfullerenes with both even and odd numbers of carbon atoms.

The main fractions containing Sc<sub>2</sub>TiC<sub>x</sub> clusterfullerenes are marked with block letters in the chromatogram in Figure 2. Fraction A contains Sc<sub>2</sub>TiC<sub>79</sub> (presumably Sc<sub>2</sub>TiC@C<sub>78</sub>) mixed with comparable amounts of Sc<sub>2</sub>C<sub>82</sub> and Sc<sub>2</sub>C<sub>2</sub>@C<sub>84</sub>. Pure Sc<sub>2</sub>TiC@C<sub>78</sub> was isolated by recycling HPLC on a Buckyprep column (Figure S2 in the Supporting Information). The most abundant EMF product in the Sc–Ti/CH<sub>4</sub> system is Sc<sub>2</sub>TiC<sub>81</sub>-I (Sc<sub>2</sub>TiC@C<sub>80</sub>-I) eluting in the fraction B (t<sub>R</sub> = 37–39 min). Unlike M<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> with lanthanides, which was a single compound in one fraction, Sc<sub>2</sub>TiC@C<sub>80</sub>-I co-elutes with Sc<sub>3</sub>C<sub>2</sub>@C<sub>80</sub> (≈ 15% of the fraction B; the corresponding peak is also seen in the chromatogram of the Sc/CH<sub>4</sub> system). Isolation of pure Sc<sub>2</sub>TiC@C<sub>80</sub>-I was accomplished with recycling HPLC on a Buckyprep-M column (see Figure S3 in the Supporting Information). In Figure 2, Fractions C and D contain pure Sc<sub>2</sub>TiC@C<sub>80</sub>-II and Sc<sub>2</sub>TiC<sub>82</sub>-I (presumably Sc<sub>2</sub>TiC<sub>2</sub>@C<sub>80</sub>-I), respectively. Mass spectrometry also provided evidence for the formation of Sc<sub>2</sub>TiC@C<sub>68</sub> and Sc<sub>2</sub>TiC<sub>2</sub>@C<sub>80</sub>-II (the corresponding fractions are marked with asterisks in Figure 2, see Figures S4 and S5 in the Supporting Information), but their low amounts and similar retention times with other EMFs made further separation impractical. To summarize, the cage-size distribution of the Sc<sub>2</sub>TiC@C<sub>2n</sub> clusterfullerenes is similar to that of Sc<sub>3</sub>N@C<sub>2n</sub> (note that Sc<sub>3</sub>N is isoelectronic to Sc<sub>2</sub>TiC). However, the retention times of the Sc<sub>2</sub>Ti carbide clusterfullerenes are generally longer. In addition, the difference in the retention times of the two isomers for Sc<sub>2</sub>TiC@C<sub>80</sub> is considerably larger than for the isomers of Sc<sub>3</sub>N@C<sub>80</sub>, a situation that facilitates separation.

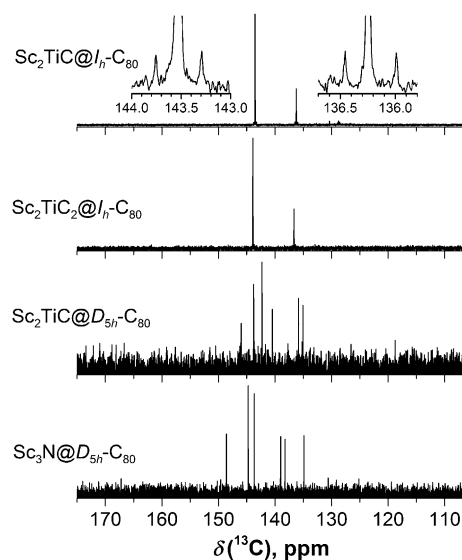
#### Molecular structure elucidation for Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> Sc<sub>2</sub>TiC@D<sub>5h</sub>-C<sub>80r</sub> and Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub>

Elucidation of the molecular structure of two isomers of Sc<sub>2</sub>TiC<sub>81</sub> and Sc<sub>2</sub>TiC<sub>82</sub> was accomplished by <sup>13</sup>C NMR spectroscopy. Sc<sub>2</sub>TiC<sub>81</sub>-I has a characteristic two-line spectrum, which unambiguously points to the freely rotating Sc<sub>2</sub>TiC cluster encapsulated within the I<sub>h</sub>(7)-C<sub>80</sub> cage. A similar spectrum with slightly different chemical shifts was observed for Sc<sub>2</sub>TiC<sub>82</sub>, which suggests that the compound can be formulated as Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>(7)-C<sub>80</sub>. Table 1 compares the <sup>13</sup>C chemical shifts of the Sc clusterfullerenes with the I<sub>h</sub>-C<sub>80</sub>-cage.

**Table 1.** <sup>13</sup>C and <sup>45</sup>Sc NMR chemical shifts (in [ppm]) of the Sc-based clusterfullerenes with an I<sub>h</sub>(7)-C<sub>80</sub> carbon cage

EMF	<sup>13</sup> C <sub>5,6,6</sub> <sup>[a]</sup>	<sup>13</sup> C <sub>6,6,6</sub> <sup>[a]</sup>	<sup>45</sup> Sc	Reference <sup>[b]</sup>
Sc <sub>2</sub> TiC@C <sub>80</sub>	143.15	135.86	277	t.w.
Sc <sub>2</sub> TiC <sub>2</sub> @C <sub>80</sub>	143.52	136.24	316	t.w.
Lu <sub>2</sub> TiC@C <sub>80</sub>	143.46	136.60	–	[28]
Lu <sub>2</sub> TiC <sub>2</sub> @C <sub>80</sub>	143.20	136.05	–	[28a]
Sc <sub>3</sub> N@C <sub>80</sub>	144.76 (144.57)	136.41 (137.24)	191 (200)	t.w. ([2b])
Sc <sub>3</sub> CH@C <sub>80</sub>	144.06	136.78	292	[7b]
Sc <sub>3</sub> C <sub>2</sub> @C <sub>80</sub>	145.6	138.9	n/a	[5c]
Sc <sub>3</sub> CN@C <sub>80</sub>	144.9	137.7	280/360	[13b]
Sc <sub>4</sub> C <sub>2</sub> @C <sub>80</sub>	143.90 (144.7)	137.14 (137.8)	373	t.w. ([6])
Sc <sub>4</sub> O <sub>2</sub> @C <sub>80</sub>	144.82	137.29	129/292	[17]

[a] “C<sub>5,6,6</sub>” and “C<sub>6,6,6</sub>” denote two types of carbon atoms in the I<sub>h</sub>-C<sub>80</sub> cage: C<sub>5,6,6</sub> (60 atoms) is on a pentagon/hexagon/hexagon junction, whereas C<sub>6,6,6</sub> (20 atoms) is on a triple hexagon junction. [b] “t.w.” stands for “this work”



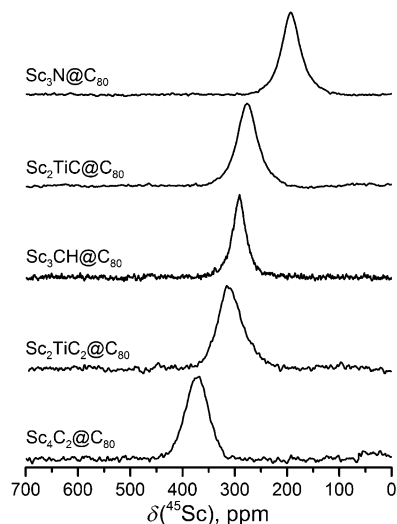
**Figure 3.** <sup>13</sup>C NMR spectra of Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub>, Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub>, Sc<sub>2</sub>TiC@D<sub>5h</sub>-C<sub>80r</sub>, and Sc<sub>3</sub>N@D<sub>5h</sub>-C<sub>80</sub>. The insets show <sup>13</sup>C satellites for <sup>13</sup>C-enriched Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> (J(C,C) = 58 Hz).

The <sup>13</sup>C NMR spectrum of Sc<sub>2</sub>TiC<sub>81</sub>-II has six lines, characteristic of the D<sub>5h</sub>(6)-C<sub>80</sub> cage, which indicates that the compound is Sc<sub>2</sub>TiC@D<sub>5h</sub>(6)-C<sub>80</sub>. A similar spectrum was observed for Sc<sub>3</sub>N@D<sub>5h</sub>(6)-C<sub>80</sub> as shown in Figure 3. The amounts of Sc<sub>2</sub>TiC<sub>69</sub>, Sc<sub>2</sub>TiC<sub>79</sub>, and Sc<sub>2</sub>TiC<sub>82</sub>-II we obtained were not sufficient for characterization by <sup>13</sup>C NMR spectroscopy. However, by analogy with the well-established structures of Sc<sub>3</sub>N@D<sub>3</sub>(6140)-C<sub>68r</sub>,<sup>[2c]</sup> Sc<sub>3</sub>N@D<sub>3h</sub>(5)-C<sub>78r</sub>,<sup>[2a]</sup> and Sc<sub>3</sub>N@D<sub>5h</sub>(6)-C<sub>80r</sub>,<sup>[31]</sup> it is likely that they are Sc<sub>2</sub>TiC@D<sub>3</sub>(6140)-C<sub>68r</sub>, Sc<sub>2</sub>TiC@D<sub>3h</sub>(5)-C<sub>78</sub> (see also the UV/Vis spectra in Figure S7 in the Supporting Information), and Sc<sub>2</sub>TiC<sub>2</sub>@D<sub>5h</sub>(6)-C<sub>80</sub>.

Attempts to observe the <sup>13</sup>C NMR signals of the internal carbon atoms for <sup>13</sup>C-enriched Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> and Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub> were not successful. <sup>13</sup>C satellites of the cage signals are clearly visible for Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> (Figure 3), which shows that the sensitivity of the measurement was sufficient for detection in cases

with similar linewidths. We propose that broadening of the resonance of the internal carbon atom inhibited the detection as was observed previously for  $\text{Sc}_2\text{C}_2@C_{3v}\text{-C}_{82}$ .<sup>[32]</sup>

The  $^{45}\text{Sc}$  NMR chemical shifts of Sc clusterfullerenes have been found to be quite characteristic and sensitive to the EMF structure as shown in Figure 4 and Table 1. The signals of

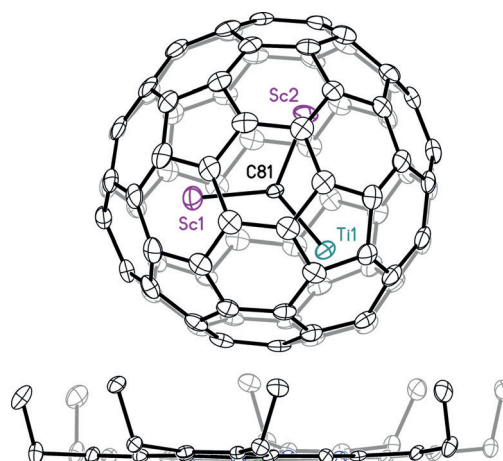


**Figure 4.**  $^{45}\text{Sc}$  NMR spectra of  $\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$ ,  $\text{Sc}_2\text{TiC}_2@I_h\text{-C}_{80}$ , and some other clusterfullerenes with the  $I_h\text{-C}_{80}$  carbon cage.

$\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$  ( $\delta = 277$  ppm) and  $\text{Sc}_2\text{TiC}_2@I_h\text{-C}_{80}$  ( $\delta = 316$  ppm) are shifted downfield versus  $\text{Sc}_3\text{N}@C_{80}$ ; the value for the former is close to the  $^{45}\text{Sc}$  chemical shift in  $\text{Sc}_3\text{CH}@C_{80}$  ( $\delta = 292$  ppm), another clusterfullerene with a single internal carbon atom. For comparison, we also measured the  $^{45}\text{Sc}$  NMR spectrum of  $\text{Sc}_4\text{C}_2@I_h\text{-C}_{80}$ , which was not reported before. The value is more positive ( $\delta = 373$  ppm) than for other clusterfullerenes with the  $I_h\text{-C}_{80}$  cage. The  $^{45}\text{Sc}$  NMR linewidth in  $\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$  is similar to that in  $\text{Sc}_3\text{N}@I_h\text{-C}_{80}$  ( $\approx 4500$  Hz and 4000 Hz, respectively), whereas in  $\text{Sc}_2\text{TiC}_2@I_h\text{-C}_{80}$ , the peak is noticeably broader (6000 Hz). The broadening may be tentatively ascribed to the internal dynamics of the cluster (such as the motion of the  $\text{C}_2$  unit).

### Single-crystal X-ray diffraction

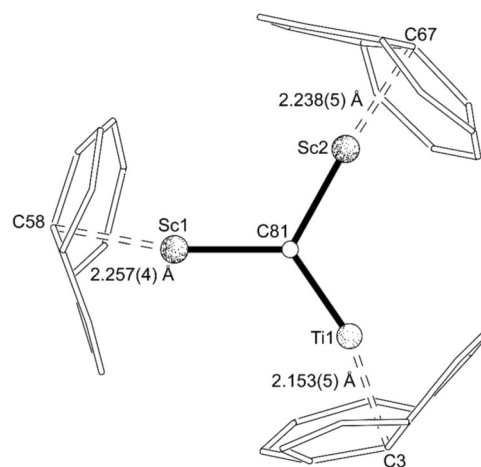
Crystals suitable for X-ray diffraction were grown by co-crystallization of  $\text{Sc}_2\text{TiC}@I_h(7)\text{-C}_{80}$  with  $[\text{Ni}(\text{OEP})]$ ; OEP is the dianion of octaethylporphyrin. The crystals of  $\text{Sc}_2\text{TiC}@I_h(7)\text{-C}_{80}\cdot\text{Ni}(\text{OEP})\cdot 2(\text{C}_7\text{H}_8)$  are isostructural to crystals of  $\text{Lu}_2\text{TiC}@I_h(7)\text{-C}_{80}\cdot\text{Ni}(\text{OEP})\cdot 2(\text{C}_7\text{H}_8)$ , which were previously characterized.<sup>[28b]</sup> The asymmetric unit contains one endohedral fullerene, one porphyrin, and two molecules of toluene. The endohedral fullerene consists of a nearly planar  $\text{Sc}_2\text{TiC}$  unit inside an  $I_h\text{-C}_{80}$  cage, with the central C81 atom adopting a  $\mu_3$  configuration (Figure 5). The deviation of the C81 atom from the least-squares plane of Ti1/Sc1/Sc2 is only 0.022(4) Å. The cage is ordered, whereas there is some disorder in the positioning of the  $\text{Sc}_2\text{TiC}$  unit. However, the major site for the  $\text{Sc}_2\text{TiC}$  unit has an



**Figure 5.** View for the structure of  $\text{Sc}_2\text{TiC}@I_h(7)\text{-C}_{80}\cdot\text{Ni}(\text{OEP})\cdot\text{toluene}$  with hydrogen atoms omitted for clarity. Only the predominant Sc and Ti positions (occupancy 0.87) are shown. Displacement parameters are shown at the 50% probability level. Selected bond lengths: Ti1–C81 1.917(4), Sc1–C81 2.102(4), and Sc2–C81, 2.104(4) Å.

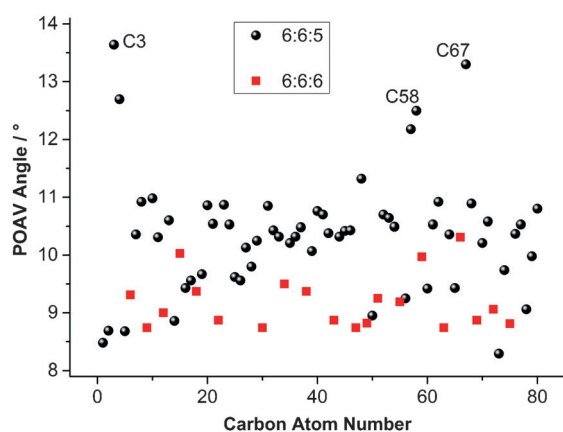
occupancy of 0.87. For this major site, the distances to the central carbide are: Ti1–C81 1.917(4), Sc1–C81 2.102(4), and Sc2–C81, 2.104(4) Å. The trimetallic carbide is tipped in such a way that the Ti is the metal atom closest to the porphyrin (Figure 5). The shortest distance between the nearest cage carbon atom and the Ni atom is 2.834(4) Å, compared to 2.871(5) Å observed in the  $\text{Lu}_2\text{TiC}$  cluster structure.

Inside the  $I_h(7)\text{-C}_{80}$  cage, the  $\text{Sc}_2\text{TiC}$  cluster is slightly shifted away from the central cage position by 0.21 Å in the direction of Ti, in keeping with the shorter contacts between Ti...C(cage) relative to Sc...C(cage). In addition, each metal is closest to a 6:6:5 junction where the carbon is highly pyramidalized at the C3 (13.6°), C58 (12.5°), and C67 (13.1°) atoms as shown in Figures 6 and 7, which show the pyramidalization of the individual carbon atoms in the cage. For comparison, the average pyramidalization angle for an  $I_h\text{-C}_{80}$  endohedral is 10.1°. A similar increase in the pyramidalization of carbon atoms near the



**Figure 6.** Depiction of the interaction of the metal ions with the closest portions of the cage.



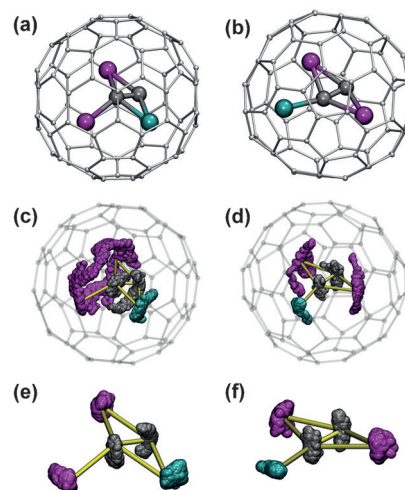


**Figure 7.** POAV angles for the various carbon atoms in  $Sc_2TiC_2@I_h-C_{80}$ . The red squares denote carbon atoms at 6:6:6 ring intersections, whereas the black circles represent carbon atoms at 6:6:5 intersections. The C3, C58, and C67 atoms are the carbon atoms closest to the metal ions.

internal metal ions has been observed for a functionalized version of  $Sc_3N@C_{80}$ .<sup>[33]</sup> Those carbon atoms showing unusually small POAV ( $\pi$ -orbital vector analysis) angles of 8.29–8.95° are one or two bonds away from the C3, C58, and C67 atoms and their flattening compensates for the high pyramidalization of the C3, C58, and C67 atoms as shown in Figure 7. In the present case, all three metals are evidently deforming the geometry at these points. In the case of  $Lu_2TiC_2@I_h-C_{80}\cdot Ni(OEP)\cdot 2(C_7H_8)$ , only the Ti atom had such a large effect (13.7°). In sum, the positioning of the  $Sc_2TiC_2$  unit within the  $I_h-C_{80}$  cage resembles, but is not identical, to that of  $Lu_2TiC_2$ . The Ti=C bond in the  $Sc_2TiC_2$  cluster is 0.043 Å longer than in the  $Lu_2TiC_2$  cluster (1.874(6) Å) but still remains in the bond length range typical for Ti=C double bonds.

### DFT calculations of the cluster geometry

In the absence of single-crystal X-ray diffraction data for  $Sc_2TiC_2@I_h-C_{80}$ , its molecular structure was studied computationally at the PBE/TZ2P level of theory. Optimization of multiple initial configurations showed that the structure of the  $Sc_2TiC_2$  cluster resembles  $Sc_3C_2$  in  $Sc_3C_2@C_{80}$ .<sup>[34,35]</sup> The  $Sc_2TiC_2$  unit adopts a bat ray structure with the three metal atoms forming a triangle whereas the  $C_2$  unit is tilted from the plane of the metal atoms. Two metal atoms have a  $\eta^2$ -coordination to the  $C_2$  unit, whereas the third atom is bonded to only one carbon atom in an acetylide fashion ( $\eta^1$ -coordination). Due to the fast rearrangement of the  $C_2$  unit, all Sc atoms in  $Sc_3C_2@C_{80}$  are dynamically equivalent. In the  $Sc_2TiC_2$  case, such configuration of the cluster can be realized in two ways: in the lowest-energy structure, Ti shares a  $\eta^2$ -coordination with the other Sc atoms, whereas the Ti of the higher-energy configuration (14.3 kJ mol<sup>-1</sup>) has a  $\eta^1$ -coordination. Both Sc atoms are  $\eta^2$ -coordinated to the acetylide (Figure 8). For each of the cluster configurations, several near-isoenergetic orientations (within a few kJ mol<sup>-1</sup>, see Figure S8 in the Supporting Information) with respect to the cage were found. We also located two different pathways between the two configurations, both with



**Figure 8.** a,b) DFT-optimized molecular structures of two low-energy configurations of the  $Sc_2TiC_2@I_h-C_{80}$  clusterfullerene with  $\eta^2$ - and  $\eta^1$ -coordination of Ti (shown in a) and b), respectively). c,d) Born–Oppenheimer molecular dynamics trajectories of the two structures (PBE/DZVP,  $T=300$  K, propagation time > 50 ps). e,f) MD trajectories of the  $Sc_2TiC_2$  cluster in both types of structures obtained after subtraction of the rotational and translational degrees of freedom of the cluster (the cage is not shown for clarity); in essence, e) and f) illustrate internal dynamics of the cluster. Color coding for all figures: magenta = Sc, cyan = Ti, and dark gray = endohedral carbon atoms. In c–f), the yellow lines show bonds in the starting configuration of the cluster (i.e., before molecular dynamics).

barriers of 80–90 kJ mol<sup>-1</sup>. Note that for the  $M_2TiC_2@I_h-C_{80}$  clusterfullerenes with larger metals (i.e., Y, Lu), the lowest-energy configuration corresponds to the structure with the  $C_2$  unit perpendicular to the plane of three metals (so that all metals are  $\eta^2$ -coordinated to the acetylide).<sup>[28a]</sup> The structure of  $Lu_2TiC_2@C_{80}$  with the  $C_2$  unit tilted from the plane was found to be 9 kJ mol<sup>-1</sup> less stable. For the  $Sc_2TiC_2@I_h-C_{80}$ , the cluster configuration with a perpendicular  $C_2$  unit is 45 kJ mol<sup>-1</sup> less stable than the conformer with the tilted arrangement. Presumably, such variations of the structure traversing from Lu to Sc are caused by the increase of the metal atom size, which forces the cluster to adopt a more compact shape.

To study the dynamic behavior of the  $Sc_2TiC_2$  cluster in  $Sc_2TiC_2@I_h-C_{80}$ , Born–Oppenheimer molecular dynamics simulations were performed at the PBE/DZVP level of theory. Two stable configurations were chosen as starting points and the structures were then equilibrated at 300 K during 5 ps. The trajectories were followed for 50 ps with a Nosé–Hoover thermostat. Figure 8 shows the trajectories that were obtained. The two-line <sup>13</sup>C NMR spectrum of  $Sc_2TiC_2@I_h-C_{80}$  indicates that the cluster rotates freely on the NMR time scale (which is usually in the nanosecond range). The accessible time frame for our MD simulations is much shorter, approximately 50 ps. Over this period of time, the cluster cannot fully establish rotational motion, but large displacements of the Sc atoms parallel to the inner surface of the cage can be seen, especially in Figure 8c. Interestingly, the mobility of the Ti atoms is clearly much lower, an observation that may point to stronger metal–cage bonding. Similar observations were found earlier in the MD studies of  $Sc_2TiN@C_{80}$ .<sup>[36]</sup> The internal dynamics of the clus-

ter are better seen when its external degrees of freedom (rotations and translations) are subtracted. Such trajectories are shown in Figures 8e and f. Both cluster configurations are found to be dynamically stable (i.e., substantial changes of the cluster geometry are not observed over 50 ps). The most dynamic part of the cluster is the acetylide fragment, which is continuously changing its tilt angle with respect to the plane of the metal atoms. Note that similar motion of the C<sub>2</sub> unit was reported in the MD studies of Sc<sub>3</sub>C<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub>.<sup>[37]</sup>

The bonding situation in Sc<sub>2</sub>TiC@C<sub>80</sub> and Sc<sub>2</sub>TiC<sub>2</sub>@C<sub>80</sub> was studied by applying Bader's quantum theory of atoms in molecules (QTAIM).<sup>[38]</sup> Table 2 lists the atomic charges *q* and the delocalization indices δ(A,B) (roughly equivalent to bond order between the atoms A and B).

EMF	R	<i>q</i>	δ(R,μ <sub>3</sub> -C)	δ(R,μ <sub>2</sub> -C)
Sc <sub>2</sub> TiC@I <sub>h</sub> -C <sub>80</sub>	Ti	+1.65	1.43	
	Sc	+1.71	0.71/0.74	
	μ <sub>3</sub> -C	-1.75		
Sc <sub>2</sub> TiC <sub>2</sub> @I <sub>h</sub> -C <sub>80</sub>	Ti	+1.59	0.55	0.66
	η <sup>2</sup> -Sc	+1.71	0.35	0.42
	η <sup>1</sup> -Sc	+1.65	0.60	0.08
	μ <sub>3</sub> -C	-1.13		1.94
	μ <sub>2</sub> -C	-0.63	1.94	
[Sc <sub>3</sub> C <sub>2</sub> @I <sub>h</sub> -C <sub>80</sub> ] <sup>-</sup>	η <sup>2</sup> -Sc	+1.62	0.43/0.39	0.44/0.48
	η <sup>1</sup> -Sc	+1.69	0.64	0.09
	μ <sub>3</sub> -C	-1.17		1.99
	μ <sub>2</sub> -C	-0.63	1.99	

The charge and bond distribution in Sc<sub>2</sub>TiC@C<sub>80</sub> closely resembles that reported for Lu<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub>.<sup>[28b]</sup> Ti and Sc have similar charges (+1.65 and +1.71, respectively), whereas the central carbon atom bears a large negative charge (-1.75) similar to that in nitride clusterfullerenes. The delocalization index δ(Ti,C) of 1.43 is roughly two times larger than the δ(Sc,C) indices, which is in accord with the Ti=C double bond.

The charges of the metal atoms in Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub> are similar to those in Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub>. The acetylide group bears a negative charge of -1.76, which is unevenly distributed between the μ<sub>3</sub>- and μ<sub>2</sub>-carbon atoms (-1.13 and -0.63, respectively). The δ(η<sup>2</sup>-Ti,C) indices are systematically larger than the δ(η<sup>2</sup>-Sc,C) values, and hence the total metal-acetylide delocalization index, δ(Ti,C<sub>2</sub>) of 1.21 is noticeably higher than the δ(Sc,C<sub>2</sub>) value, that is, 0.76. Analysis of the charges and delocalization indices shows that the acetylide unit in Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub> is similar to that of the single carbon atom in Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub>. The C-C bond index in Sc<sub>2</sub>TiC<sub>2</sub> is 1.94, thus the formal charge and bond distribution in the C<sub>2</sub> unit can be described as (C=C)<sup>4-</sup>. QTAIM analysis of the [Sc<sub>3</sub>C<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub>]<sup>-</sup> ion, which is isostructural and isoelectronic with Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub>, gives very similar values for the atomic charges and delocalization indices (Table 2).

## Electronic structure and electrochemistry

The frontier molecular orbitals of Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> and Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub> are visualized in Figure 9. The predominant localization of

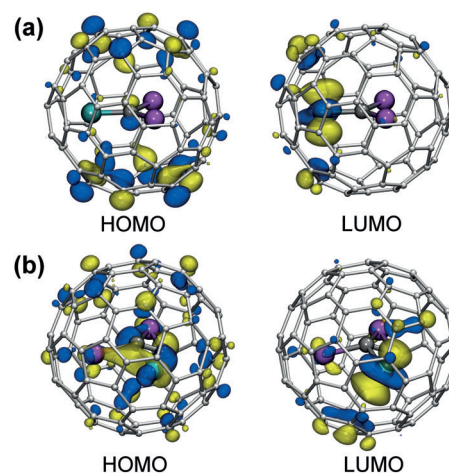
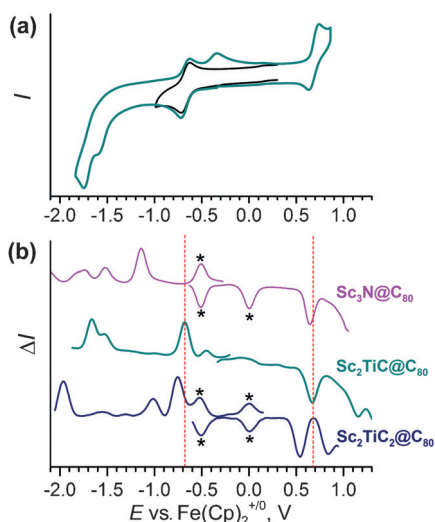


Figure 9. Frontier molecular orbitals of a) Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> and b) Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub> computed at the PBE/def2-TZVP level of theory (isovalues: ±0.038 a.u.). Magenta = Sc, cyan = Ti, and dark gray = internal carbon atoms.

the LUMO on the Ti atom is characteristic for both of these clusterfullerenes. The HOMO of Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> is localized on the carbon cage and resembles the HOMO of Sc<sub>3</sub>N@I<sub>h</sub>-C<sub>80</sub>, whereas the HOMO of Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub> is equally delocalized between the cluster and the carbon cage. Comparison to lanthanide-based clusterfullerenes shows that substitution by Sc does not affect the nature of the frontier MOs in M<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub>. For M<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub>, the difference between Sc and lanthanides is more pronounced, especially for the HOMO, which has almost no cage contribution in the lanthanide-based M<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub> clusterfullerenes.

The cyclic voltammetry study shows that the first reduction and oxidation of Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> are electrochemically reversible (Figure 10a), whereas increasing the potential window to include the second and third reduction steps also affects the reversibility of the first reduction (observe new re-oxidation peak at -0.34 V). The first reduction potentials of both Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> and Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub> (-0.67 and -0.76 V, respectively, Table 3) are substantially more positive than that of Sc<sub>3</sub>N@I<sub>h</sub>-C<sub>80</sub> (-1.14 V) and can be ascribed to the endohedral Ti<sup>IV</sup>/Ti<sup>III</sup> redox couple. The oxidation potential of Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> is virtually equal to that of the nitride clusterfullerene, which is in accord with almost identical HOMOs in both molecules. The first oxidation potential of the Sc<sub>2</sub>TiC<sub>2</sub>@I<sub>h</sub>-C<sub>80</sub> is shifted in the cathodic direction due to the cluster contribution to the HOMO, but the shift is not dramatic, which is consistent with the distribution of the HOMO between the cluster and the cage.

Comparison of the first reduction potential of Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> with that of other Ti-based clusterfullerenes reveals substantial variability of the endohedral Ti<sup>IV</sup>/Ti<sup>III</sup> redox couple (Table 3). The variation of the redox potential in the M<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> series, from -0.67 V in Sc<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> to -1.04 V in Gd<sub>2</sub>TiC@I<sub>h</sub>-C<sub>80</sub> (Table 3) is



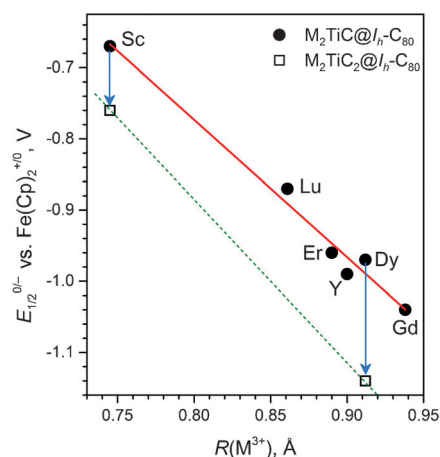
**Figure 10.** a) Cyclic voltammograms of  $\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$  and b) square-wave voltammograms of  $\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$ ,  $\text{Sc}_2\text{TiC}_2@I_h\text{-C}_{80}$ , and  $\text{Sc}_3\text{N}@I_h\text{-C}_{80}$ . Measurements are performed at room temperature in *o*-dichlorobenzene/TBAPF<sub>6</sub> (TBA = tetrabutylammonium) with a scan rate of a) 100  $\text{mV s}^{-1}$  and b) 50  $\text{mV s}^{-1}$ . In a), the black curve shows the measurement in the limited potential range covering only the first reduction, whereas the cyan curve shows the measurement in the whole accessible range of potentials. To guide the eye, vertical bars in b) mark the first reduction and oxidation potentials of  $\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$ . Asterisks in b) mark the redox processes of  $[\text{Fe}(\text{Cp}^*)_2]$  and  $[\text{Fe}(\text{Cp})_2]$  ( $\text{Cp}^* = 1,2,3,4,5$ -pentamethylcyclopentadienyl,  $\text{Cp} = \text{cyclopentadienyl}$ ) used as internal standards.

**Table 3.** Redox potentials<sup>[a]</sup> of  $\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$ ,  $\text{Sc}_2\text{TiC}_2@I_h\text{-C}_{80}$ , and selected Ti-based EMFs.

EMF	Ox-I	Red-I	Red-II	Red-III	gap <sub>EC</sub>	Reference
$\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$	0.66	-0.67	-1.51	-1.66	1.33	t.w.
$\text{Sc}_2\text{TiC}_2@I_h\text{-C}_{80}$	0.53	-0.76	-1.01	-1.96	1.26	t.w.
$\text{Gd}_2\text{TiC}@I_h\text{-C}_{80}$	0.60	-1.04	-1.72	-1.91	1.64	[28a]
$\text{Y}_2\text{TiC}@I_h\text{-C}_{80}$	0.60	-0.99	-1.67	-1.89	1.59	[28a]
$\text{Dy}_2\text{TiC}@I_h\text{-C}_{80}$	0.61	-0.97	-1.62	-1.87	1.58	[28a]
$\text{Dy}_2\text{TiC}_2@I_h\text{-C}_{80}$	0.47	-1.14	-1.58	-2.29	1.61	[28a]
$\text{TiSc}_2\text{N}@I_h\text{-C}_{80}$	0.16	-0.94	-1.58	-2.21	1.10	[36]
$\text{TiY}_2\text{N}@I_h\text{-C}_{80}$	0.00	-1.11	-1.79	-1.11	1.11	[25a]
$\text{Sc}_3\text{N}@I_h\text{-C}_{80}$	0.63	-1.15	-1.54	-1.73	1.78	t.w.
$\text{Ti}_2\text{S}@D_{3h}(5)\text{-C}_{78}$	0.23	-0.92	-1.53	-1.80	1.15	[23]

[a] Potentials are listed in Volt versus the  $[\text{Fe}(\text{Cp})_2]^{+/0}$  pair, "Ox" stands for oxidation, "Red" stands for reduction, gap<sub>EC</sub> is an electrochemical gap defined as the difference of the first reduction and oxidation potentials.

especially striking. Figure 11 shows that a linear correlation exists between the reduction potential of  $\text{M}_2\text{TiC}@I_h\text{-C}_{80}$  and the ionic radius of the metal,  $R(\text{M}^{3+})$ . Such a strong variation of the Ti-based reduction on the second metal, which is not involved in the LUMO, suggests that the energetics of the reduction is controlled by geometric factors. Earlier, we observed a similar phenomenon for the endohedral  $\text{Ce}^{\text{IV}}/\text{Ce}^{\text{III}}$  redox couple in  $\text{CeM}_2\text{N}@I_h\text{-C}_{80}$  ( $\text{M} = \text{Sc}, \text{Lu}, \text{Y}$ ) and in other Ce-containing nitride clusterfullerenes.<sup>[39]</sup> In these EMFs, the first oxidation step is usually described as an oxidation of the trivalent Ce. Because the ionic radius of  $\text{Ce}^{\text{IV}}$  is smaller than that of  $\text{Ce}^{\text{III}}$ , oxidation of  $\text{Ce}^{\text{III}}$  results in a decrease of the size of the endohedral cluster.



**Figure 11.** Correlation between the reduction potentials of  $\text{M}_2\text{TiC}@I_h\text{-C}_{80}$  (dots) and  $\text{M}_2\text{TiC}_2@I_h\text{-C}_{80}$  (squares) and the Shannon ionic radii of the metals,  $R(\text{M}^{3+})$ . The arrows denote negative shifts of the reduction potentials when going from  $\text{M}_2\text{TiC}@I_h\text{-C}_{80}$  to  $\text{M}_2\text{TiC}_2@I_h\text{-C}_{80}$ .

For a metal with a large ionic radius, such as Y, the cluster in  $\text{CeM}_2\text{N}@I_h\text{-C}_{80}$  is highly strained due to the limited room inside the cage, and the oxidation of Ce releases the strain. The variation of the oxidation potential in the  $\text{CeM}_2\text{N}@I_h\text{-C}_{80}$  series is therefore ascribed to the alteration of the strain energy of the nitride cluster. Similar arguments apply here for the  $\text{M}_2\text{TiC}@I_h\text{-C}_{80}$  family. The ionic radius of Ti is increased on going from  $\text{Ti}^{\text{IV}}$  (0.605 Å) to  $\text{Ti}^{\text{III}}$  (0.67 Å), and therefore, the size of the  $\text{M}_2\text{TiC}$  cluster is increased in the anion (we use Shannon ionic radii throughout this discussion<sup>[40]</sup>). When the size of the cluster is relatively small, as in  $\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$ , the increase of the cluster size does not result in a considerable increase of the strain energy ( $\Delta E_{\text{strain}}$  is relatively small). On the contrary, in  $\text{Gd}_2\text{TiC}@I_h\text{-C}_{80}$  the size of the cluster is rather large resulting in a non-negligible steric strain. A further increase of the cluster size upon reduction is, therefore, not thermodynamically favorable ( $\Delta E_{\text{strain}}$  is large) and requires additional energy input (e.g., more negative potential) to overcome the strain. Thus, the variation of the potential of the internal  $\text{Ti}^{\text{IV}}/\text{Ti}^{\text{III}}$  redox couple can serve as a measure of the strain energy in the  $\text{M}_2\text{TiC}@I_h\text{-C}_{80}$  clusterfullerenes. The increment of the linear correlation in Figure 11 is  $-1.93 \text{ V}\text{Å}^{-1}$ , which can be interpreted as an increase of the strain energy by 19  $\text{kJ mol}^{-1}$  with an increase of the ionic radius by 0.1 Å. Although the inner strain in EMFs is an intuitively clear concept, it is not straightforward to give a numerical estimation of the strain energy, especially within experimental studies. Implantation of redox-active transition metals that change their sizes upon reduction or oxidation into the endohedral cluster thus provides a rare opportunity to address the strain problem in EMFs experimentally. In a similar fashion, the variation of the redox potential of transition metals has been used to analyze the ligand strain in organometallic complexes of Fe, Co, or Cu.<sup>[41]</sup>

This line of argument can be used for other types of Ti-based clusterfullerenes. Thus, the reduction potentials of  $\text{Sc}_2\text{TiC}_2@I_h\text{-C}_{80}$  and  $\text{Dy}_2\text{TiC}_2@I_h\text{-C}_{80}$  are shifted negatively versus  $\text{Sc}_2\text{TiC}@I_h\text{-C}_{80}$  and  $\text{Dy}_2\text{TiC}@I_h\text{-C}_{80}$ , and the shift is larger for



$\text{Dy}_2\text{TiC}_2@C_{80}$  due to the larger ionic radius of  $\text{Dy}^{3+}$  (and hence larger  $\Delta E_{\text{strain}}$  value). In a similar fashion, in nitride clusterfullerenes  $\text{TiM}_2\text{N}@C_{80}$ , the first reduction step is also a Ti-based process, and the first reduction of  $\text{TiY}_2\text{N}@I_h-C_{80}$  is more negative than in  $\text{TiSc}_2\text{N}@I_h-C_{80}$ , because of the larger cluster size in the former. Furthermore, in  $\text{TiM}_2\text{N}@C_{80}$  the valence state of titanium is  $\text{Ti}^{\text{III}}$ , and it becomes  $\text{Ti}^{\text{II}}$  when the molecule is reduced. The ionic radius of  $\text{Ti}^{\text{II}}$  is 0.86 Å, and therefore, the increase of the metal size in the  $\text{Ti}^{\text{III}}/\text{Ti}^{\text{II}}$  couple ( $\Delta R(\text{M}^{3+/2+})=0.19$  Å) is more pronounced than in the  $\text{Ti}^{\text{IV}}/\text{Ti}^{\text{III}}$  couple ( $\Delta R(\text{M}^{4+/3+})=0.06$  Å). This observation explains why the reduction potentials of the  $\text{TiM}_2\text{N}@I_h-C_{80}$  nitride clusterfullerene are more negative than their carbide counterparts  $\text{M}_2\text{TiC}@I_h-C_{80}$ .

## Conclusion

The synthesis of the mixed Ti–Sc system in a  $\text{He}/\text{CH}_4$  atmosphere affords a series of new EMFs with mixed-metal  $\text{Sc}_2\text{TiC}$  and  $\text{Sc}_2\text{TiC}_2$  clusters. Both clusters have a formal charge of 6+ and thus, prefer the  $I_h-C_{80}$  cage as disclosed by  $^{13}\text{C}$  NMR spectroscopy. Clusterfullerenes with the  $D_{5h}-C_{80}$  cage isomer and other cage sizes (i.e.,  $\text{Sc}_2\text{TiC}@C_{68}$ ,  $\text{Sc}_2\text{TiC}@C_{78}$ ) are also formed in smaller amounts. A single-crystal X-ray diffraction study of  $\text{Sc}_2\text{TiC}@I_h-C_{80}$  suggested the presence of the Ti=C double bond.  $\text{Sc}_2\text{TiC}@I_h-C_{80}$  and  $\text{Lu}_2\text{TiC}@I_h-C_{80}$  are the only single carbide-containing EMFs that have been crystallographically characterized.<sup>[28b]</sup> They serve as potential models for the series of EMFs with odd numbers of carbon atoms such as  $\text{Y}_3\text{C}_{107}$  to  $\text{Y}_3\text{C}_{125}$  and  $\text{Lu}_3\text{C}_{107}$  to  $\text{Lu}_3\text{C}_{115}$ , which have been discovered recently.<sup>[42]</sup>

The presence of methane in the reactor atmosphere is crucial for the high selectivity of the synthesis of carbide clusterfullerenes. In particular, it dramatically reduces the yield of empty fullerenes. Interestingly, this function of  $\text{CH}_4$  is efficient in the presence of Sc (either  $\text{Sc}/\text{CH}_4$  or  $\text{Sc-Ti}/\text{CH}_4$  systems), whereas Ti blocks the reactive atmosphere effect with the predominant formation of empty fullerenes in the  $\text{Ti}/\text{CH}_4$  system. The presence of Ti also affects the distribution of Sc–carbide clusterfullerenes. The most striking effect is a dramatic decrease of the yield of  $\text{Sc}_4\text{C}_2@C_{80}$ , the most abundantly formed clusterfullerene in the  $\text{Sc}/\text{CH}_4$  system. Finally, the distribution of empty fullerenes formed in the  $\text{Ti}/\text{CH}_4$  system is noticeably different from that of standard empty fullerene synthesis. Thus, Ti is actively involved in the fullerene formation in the arc discharge even when Ti EMFs are not formed.

Electrochemical and frontier orbital studies of  $\text{Sc}_2\text{TiC}@I_h-C_{80}$  and  $\text{Sc}_2\text{TiC}_2@I_h-C_{80}$  revealed a Ti-based reduction in both types of clusterfullerenes. Reduction potentials of endohedral  $\text{Ti}^{\text{IV}}/\text{Ti}^{\text{III}}$  redox couples showed dramatic variation with the size of the endohedral clusters. In particular, the reduction potential in the  $\text{M}_2\text{TiC}@I_h-C_{80}$  series scales linearly with the ionic radius of the electrochemically inert metals. This phenomenon is explained by consideration of the inner strain in clusterfullerenes emerging when the size of the cluster is non-commensurable with that of the carbon cage. The increase of the ionic radius of Ti upon reduction increases the strain energy and pushes the reduction potentials of the EMFs with larger (and hence more strained) clusters to more negative values.

## Experimental Section

**Arc-discharge synthesis:** The arc-discharge synthesis was performed in a static 250 mbar helium atmosphere in the presence of a several mbar of methane. Graphite rods were drill-holed and packed with a mixture of Sc/graphite, Ti/graphite, or Sc–Ti/graphite powder (Sc and Ti were used as metals, the molar ratio in the mixed-metal system was 1:1);  $^{13}\text{C}$  enrichment ( $\approx 5\%$ ) was achieved by adding amorphous  $^{13}\text{C}$  powder. According to our recent study of  $\text{Sc}_3\text{CH}@C_{80}$ ,  $^{13}\text{C}$  enrichment through carbon powder gives a comparable  $^{13}\text{C}$  content for the cage and endohedral carbon atoms.<sup>[7b]</sup> Note that reducing the amount of residual nitrogen in the generator is crucial for the successful synthesis because nitride clusterfullerenes are readily formed in the presence of nitrogen.

**Spectroscopic measurements:** MALDI mass spectra were measured with a Bruker autoflex mass spectrometer by using sulfur as a matrix. NMR measurements were performed on a Bruker Avance 500 spectrometer equipped with the multiprobe head 1152Z. The measurements were performed for compounds dissolved in  $\text{CS}_2$  with  $[\text{D}_6]$ acetone placed in a coaxial tube as a lock; relaxation agents were not used in the NMR measurements. Electrochemical measurements were performed in a glovebox with a three-electrode cell (Pt wire as working and counter electrodes, Ag wire as a pseudo-reference electrode; the potentials were calibrated versus  $[\text{Fe}(\text{Cp})_2]$  and  $[\text{Fe}(\text{Cp}^*)_2]$  as internal standards).

**Crystal-structure determination of  $\text{Sc}_2\text{TiC}@I_h(7)-C_{80}\text{-Ni}(\text{OEP})\cdot 2(\text{C}_2\text{H}_6)$ :** Crystals suitable for X-ray diffraction studies were obtained by layering a toluene solution of  $[\text{Ni}(\text{OEP})]$  over a toluene solution of  $\text{Sc}_2\text{TiC}@I_h(7)-C_{80}$  in a 5 mm outside diameter glass tube approximately 18 cm in length. The crystal selected for data collection was a black plate of the dimensions  $0.005 \times 0.090 \times 0.140$  mm<sup>3</sup>. The crystal was mounted in the 100 K cold nitrogen stream provided by an Oxford Cryostream low-temperature apparatus on the goniometer head of a Bruker D8 diffractometer equipped with a Bruker Photon 100 CMOS detector. Data were collected with the use of synchrotron radiation ( $\lambda=0.7749$  Å) at the Beamline 11.3.1 at the Advanced Light Source, Lawrence Berkeley Laboratory. The structure was solved by a dual space method, (SHELXT)<sup>[43]</sup> and refined by full-matrix least-squares on  $F^2$  (SHELXL-2014).<sup>[44]</sup> The structure is a pseudo-merohedral twin with twin law  $(0 \ -1 \ 0 \ -1 \ 0 \ 0 \ 0 \ -1)$  and refined twin parameter of 0.2410(9). The  $\text{Sc}_2\text{TiC}$  cluster is disordered over three orientations. There is only one position for the central carbide carbon atom. The three clusters are comprised of  $\text{Ti1}/\text{Sc1}/\text{Sc2}$ ,  $\text{Ti2}/\text{Sc3}/\text{Sc4}$ , and  $\text{Ti3}/\text{Sc1}/\text{Sc5}$  with relative occupancies of 0.87:0.05:0.08. The atoms of the minor orientations were refined with isotropic thermal parameters. All other non-hydrogen atoms were refined with anisotropic displacement parameters. One of the two toluene molecules is disordered over two orientations with relative occupancies of 0.88:0.12. The minor component of this second toluene site was restrained to have the same geometry as the major component. CCDC 1472263 contains the supplementary crystallographic data for this paper. These data can be obtained free of charge from The Cambridge Crystallographic Data Centre.

**Crystal data:**  $\text{C}_{131}\text{H}_{60}\text{N}_4\text{NiSc}_2\text{Ti}$ ;  $M_w=1886.36$  g mol<sup>-1</sup>; triclinic;  $P\bar{1}$ ;  $a=14.6160(6)$ ,  $b=14.6376(7)$ ,  $c=20.4430(9)$  Å;  $\alpha=83.135(2)$ ,  $\beta=83.596(2)$ ,  $\gamma=60.686(2)^\circ$ ;  $V=3779.1(3)$  Å<sup>3</sup>;  $Z=2$ ;  $R_1$  [15380 reflections with  $I > 2\sigma(I)]=0.0631$ ;  $wR_2$  (all 17305 unique data)=0.1726, 1309 parameters; 15 restraints; largest diff. peak and hole 1.488 and  $-1.547$  e Å<sup>-3</sup>.

**Computational studies:** Density functional theory computations were carried out within the generalized gradient approximation (GGA) PBE<sup>[45]</sup> for the exchange-correlation term and the original



TZ2P-quality basis set as implemented in the PRIRODA package.<sup>[46]</sup> Wavefunctions for QTAIM analysis were obtained in single-point energy calculations at the PBE/def2-TZVP level with full-electron basis sets and scalar-relativistic DKH correction as implemented in the Orca suite.<sup>[47]</sup> QTAIM analysis was performed with the AIMALL code.<sup>[48]</sup> Born–Oppenheimer molecular dynamics (MD) calculations performed in the CP2K code<sup>[49]</sup> and employed the velocity Verlet algorithm with a time step of 0.5 fs and the Nosé–Hoover thermostat set at 300 K. Before a production run, the systems were first thermostated for 5 ps. MD calculations were performed with the PBE functional and employed Gaussian and plane wave GPW scheme with Goedecker–Teter–Hutter pseudopotentials and DZVP basis set.<sup>[49a,50]</sup> Molecular structures, orbitals, and MD trajectories were visualized by using the VMD package.<sup>[51]</sup>

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