Harmonic oscillator model of the insulin and IGF1 receptors' allosteric binding and activation

Vladislav V Kiselyov*, Soetkin Versteyhe, Lisbeth Gauguin and Pierre De Meyts

Receptor Systems Biology Laboratory, Hagedorn Research Institute, Gentofte, Denmark

* Corresponding author. Receptor Systems Biology Laboratory, Hagedorn Research Institute, Niels Steensens Vej 6, Gentofte 2820, Denmark. Tel.: + 44 420 266; Fax: + 45 444 392 03; E-mail: vkis@novonordisk.com

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The insulin and insulin-like growth factor 1 receptors activate overlapping signalling pathways that are critical for growth, metabolism, survival and longevity. Their mechanism of ligand binding and activation displays complex allosteric properties, which no mathematical model has been able to account for. Modelling these receptors' binding and activation in terms of interactions between the molecular components is problematical due to many unknown biochemical and structural details. Moreover, substantial combinatorial complexity originating from multivalent ligand binding further complicates the problem. On the basis of the available structural and biochemical information, we develop a physically plausible model of the receptor binding and activation, which is based on the concept of a harmonic oscillator. Modelling a network of interactions among all possible receptor intermediaries arising in the context of the model (35, for the insulin receptor) accurately reproduces for the first time all the kinetic properties of the receptor, and provides unique and robust estimates of the kinetic parameters. The harmonic oscillator model may be adaptable for many other dimeric/dimerizing receptor tyrosine kinases, cytokine receptors and G-protein-coupled receptors where ligand crosslinking occurs.

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Introduction

Insulin and insulin-like growth factors (IGF) 1 and 2 have similar structures and exert their action by activating two closely related receptor tyrosine kinases-the insulin receptor and the IGF1 type I receptor (IGF1 receptor), which share largely overlapping signalling pathways (Adams et al, 2000; De Meyts and Whittaker, 2002; De Meyts, 2004; Denley et al, 2005). Despite this similarity, the two hormones produce different responses: mostly metabolic for insulin and mitogenic for IGF1 (Kim and Accili, 2002). Dysregulation of their signalling may lead to two different life-threatening diseases: type II diabetes and cancer, which are among the largest global health challenges in the world. So far, there is poor understanding of how these hormones produce such different biological effects using similar signalling networks (Kim and Accili, 2002). It has become clear that a systems biology approach is required to understand the combinatorial nature of signalling specificity (Shymko et al, 1997; Kholodenko, 2007). Insulin analogues with altered kinetic properties show

enhanced mitogenic potencies, although they bind to the same insulin receptor; they also cross-react to a variable extent with the IGF-I receptor (Shymko et al, 1997; Kurtzhals et al, 2000). Differences in kinetics of ligand binding and receptor activation by the insulin and IGF1 receptors may be one of the factors determining their specificity (Shymko et al, 1997). The two receptors' mechanism of ligand binding and activation displays complex allosteric properties (i.e. negative cooperativity and ligand dependence of the receptor dissociation rate), which no mathematical model has been able to fully account for (Jeffrey, 1982; Kohanski and Lane, 1983; Hammond et al, 1997; Wanant and Quon, 2000; Sedaghat et al, 2002). Thus, the development of a reliable mathematical model describing the two receptors' binding kinetics and activation is a critical first step in a systems biology approach to understand the function and specificity of these receptors.

The insulin and IGF1 receptors exist in the membrane as pre-formed covalent dimers of two identical moieties. Their extracellular domains comprise two leucine-rich repeat-containing large domains (L_1 and L_2) separated by a cystein-rich

(CR) domain, followed by three fibronectin type III (Fn_{1-3}) domains (Adams *et al*, 2000; De Meyts and Whittaker, 2002; De Meyts, 2004). A crystal structure of this extracellular (unliganded) insulin receptor dimer has recently been solved (McKern *et al*, 2006; Lawrence *et al*, 2007; Ward *et al*, 2007, 2008). The intracellular portion of the two receptors consists of a kinase domain flanked by regulatory regions (Hubbard and Miller, 2007).

The insulin and IGF1 receptors exhibit complex binding properties. The Scatchard plots for both receptors are concave up, indicating the presence of high- and low-affinity binding sites and/or negative cooperativity (De Meyts *et al*, 1973, 1976; De Meyts, 1994). The receptors bind only one ligand molecule with high affinity and at least another one with lower affinity. The ligand dissociation rate is dependent on its concentration (De Meyts *et al*, 1973, 1976; De Meyts, 1994). Furthermore, this dependence is bell-shaped for the insulin receptor, whereas for the IGF1 receptor, it is sigmoid (Christoffersen *et al*, 1994). When the insulin receptor is in a monomeric form, its affinity is reduced 30-fold, the Scatchard plot becomes linear and the dissociation rate of the ligand becomes independent of its concentration (De Meyts, 1994, 2004; De Meyts and Whittaker, 2002).

Insulin has two receptor-binding surfaces on the 'opposite' sides of the molecule. The first 'classical' binding surface, also involved in insulin dimerization, was defined in the early 1970s (Pullen et al, 1976; De Meyts et al, 1978), and later validated by alanine-scanning mutagenesis (Kristensen et al, 1997), whereas the second surface, also involved in insulin hexamerization, was mapped by alanine-scanning mutagenesis more recently (De Meyts, 2004; Gauguin et al, 2008). The dimerization surface interacts with a site located in the L₁ module of the insulin receptor, as well as a 12 amino-acid peptide from the insert in Fn₂, which combine to form 'site 1' (Wedekind et al, 1989; Kurose et al, 1994; Williams et al, 1995; Mynarcik et al, 1996; De Meyts and Whittaker, 2002; Kristensen et al, 2002; Huang et al, 2004), whereas the hexamerization surface interacts with a site consisting of residues located in the C-terminal portion of L2 and in the Fn₁ and Fn₂ modules (site 2) (Fabry et al, 1992; De Meyts and Whittaker, 2002; Hao et al, 2006; Benyoucef et al, 2007; Whittaker et al, 2008). Schäffer (1994) suggested that the highaffinity binding could result from insulin crosslinking site 1 of one receptor half and site 2 of the other half of the receptor dimer, thus leaving the other two sites free for interaction with the ligand. However, this model had difficulty in explaining the ligand dependence of the ligand dissociation rate. De Meyts (1994) suggested that this problem could be solved by assuming that the four sites of the receptor dimer are arranged in a symmetrical antiparallel way, a postulate that was supported by the recent structure determination of the insulin receptor extracellular domain (McKern et al, 2006). Despite its seeming simplicity, this model turned out to be notoriously difficult for a quantitative analysis and some researchers even concluded that it did not explain the ligand dependence of the dissociation rate (Hammond et al, 1997). The problem is that the qualitative crosslinking models suggested by Schäffer (1994) and De Meyts (1994) are not detailed enough from a biochemical and structural viewpoint for mathematical modelling (especially concerning the precise mechanism that

Here, we present the first mathematical model that accurately reproduces all the kinetic properties of the insulin receptor such as negative cooperativity and the bell-shaped ligand dependence of the receptor dissociation rate. On the basis of the available structural information, we develop a physically plausible model of the receptor activation, which is based on the concept of a harmonic oscillator. We justify thermodynamically that the symmetrically arranged subunits of the insulin receptor dimer experience harmonic oscillatory movements. Analysis of the behaviour of an ensemble of such harmonic oscillators in thermal equilibrium with the surrounding milieu allows to model the receptor activation in a simple way and to substantially reduce the combinatorial complexity. This model is the first one that gives a description of the insulin receptor binding and activation mechanism in terms of interactions between the molecular components and fully takes into account the combinatorial binding complexity (employing 35 insulin receptor intermediaries). Fitting of the model to experimental data provides unique and robust estimates of the kinetic parameters. With a small modification, the model can also be used for the IGF1 receptor. Furthermore, the harmonic oscillator model may be adaptable for many other dimeric or dimerizing receptor tyrosine kinases, cytokine receptors and G-protein-coupled receptors where ligand crosslinking occurs (De Meyts, 2008).

Theory and results

Our goal is to develop a physically plausible mathematical model of the insulin receptor-binding and activation mechanism in terms of interactions between the molecular components. This, however, requires the knowledge of the precise mechanism of interaction between the components involved, for which some biochemical and structural details are still missing. Thus, some assumptions are unavoidable. All of the assumptions made in this article are justified from the physicochemical point of view and are therefore physically plausible.

Binding of insulin to the inactive conformation of the insulin receptor

The structure of the insulin receptor dimer in the unliganded conformation displays a symmetrical antiparallel arrangement of the receptor's two binding sites for insulin (McKern *et al*, 2006) (see Figure 1A and C). From now on, a pair of sites 1 and 2 from the different receptor subunits will be referred to as a 'crosslink'. The structure shows that the distance between sites 1 and 2 (within the same crosslink) is rather small (see Figure 1B), indicating that if an insulin molecule binds to either of these sites, there is not enough room for binding of a second insulin molecule. Thus, it is reasonable to assume that only one insulin molecule can bind to the same crosslink (either to site 1 or 2), when the receptor dimer is in the *inactive* conformation. Mathematical modelling of insulin binding to



Figure 1 Insulin receptor structure. In all of the panels, the individual monomers of the insulin receptor dimer are coloured in green and blue, respectively, and location of the binding sites is shown approximately, as the residues involved in binding to insulin are not known precisely. (A) Crystal structure of the ecto-domain of the insulin receptor dimer (PDB code: 2DTG). Labelling of the modules is shown only for the blue-coloured monomer. (B) Half of the insulin receptor dimer is shown. The placement of insulin in the binding cavity is shown approximately. (C) A view of the insulin receptor dimer (shown in (A)) as seen from the 'top'. (D) Simplified representation of the insulin receptor dimer, in which the insulin-binding subunits are represented as rigid bodies. (E) Crosslinked (tilted) conformations of the rigid-body representation of the insulin receptor dimer. Insulin is depicted as a black dot.

the inactive conformation of the insulin receptor is straightforward and requires only four parameters: association rate constants for sites 1 and 2 (designated a_1 and a_2 , respectively) and dissociation rate constants for sites 1 and 2 (designated d_1 and d_2 , respectively). The four sites will from now on be designated as sites 1, 2, 3 and 4, where sites 3 and 4 are identical to sites 1 and 2, respectively, but from a different crosslink (see Figure 2A). Binding of insulin to the inactive conformation of the insulin receptor gives rise to nine intermediaries, designated r_0 , r_1 , r_2 , r_3 , r_4 , r_{13} , r_{14} , r_{23} and r_{24} (where indices *i* and *j* in r_i and r_{ij} designate the number of the site to which insulin is bound) (see Figure 2A).

Conformational change in the insulin receptor upon insulin binding

Currently, the precise mechanism of the insulin receptor crosslinking reaction required for mathematical modelling is not known. Therefore, we will analyse the available structural information from a physicochemical point of view to derive a plausible model.

In the absence of insulin, the insulin receptor adopts an inactive, symmetrical conformation (McKern et al, 2006) (see Figure 1A and C). Binding of insulin to both sites of a crosslink is thought to produce a conformational change in the insulin receptor, which is necessary for its activation. The crystal structure of the insulin receptor (McKern et al, 2006) is consistent with an assumption (as previously suggested by De Meyts, 1994) that this conformational change is produced by a tilt of the receptor subunits, leading to a movement of sites 1 and 2 towards each other and to a corresponding movement of sites from the second crosslink away from each other. This structural rearrangement is schematically shown in Figure 1D and E, in which the symmetrically arranged subunits of the receptor dimer are approximated by rigid bodies. Obviously, the tilted (activated) conformation has higher free energy than the symmetrical, inactive conformation (otherwise there would be a substantial receptor activation in the absence of insulin), probably due to slight distortion of bond angles and lengths. Thus, it is reasonable to assume that receptor molecules can exist in both inactive and active conformations, with equilibrium being strongly shifted towards the inactive (energetically more favourable) conformation in the absence



Figure 2 Inactive (A) and crosslinked (B, C) insulin receptor intermediaries used in the model. S1 and S2 stand for sites 1 and 2, respectively. Insulin is depicted as a black dot.

of the ligand. However, when the ligand is present, it may bind simultaneously to sites 1 and 2 of the same crosslink when the receptor molecules are in the tilted conformation and thus stabilize the active conformation.

Insulin receptor as a harmonic oscillator: a physically plausible model of the receptor conformational change

As discussed above, the tilted (active) conformation of the insulin receptor has higher free energy compared with the nontilted (inactive) conformation. It is reasonable to assume that larger tilt angles result in larger free energy values, and that the insulin receptor free energy has a local minimum at the zero tilt angle. Therefore, in a sufficiently small vicinity around the zero tilt angle, the system behaviour can be approximated by harmonic oscillations (Bloch, 1997). Let us consider the energy of the insulin receptor oscillations when the insulin receptor is in thermal equilibrium with the buffer. Then, the receptor molecules will have various energies (received from accidental collisions with the buffer molecules), and their distribution will be according to the Maxwell–Boltzmann formula (Bloch, 1997), which for a one-dimensional harmonic oscillator takes the form:

$$\frac{\mathrm{d}P}{\mathrm{d}E} = \frac{1}{kT} \,\mathrm{e}^{-E/kT} \,(\mathrm{Figure}\, 3\mathrm{A})$$

where P, E, k and T stand for probability, energy, Boltzmann constant and absolute temperature, respectively. As appears from Figure 3A, the most likely state of the receptor is that with the zero energy of oscillations (corresponding to the zero tilt angle, or an inactive conformation), with the probability

density of finding receptor molecules with higher energies decreasing exponentially as a function of energy. The Maxwell–Boltzmann distribution implies that a small fraction of receptor molecules will have sufficient energy to reach the tilt angle of the activated receptor in the absence of insulin (Figure 3A). This fraction can be easily derived from the Maxwell–Boltzmann distribution if the activation energy (designated E_{act}), corresponding to the tilt angle of the activated receptor, is known:

Fraction =
$$\int_{E_{act}}^{\infty} \frac{1}{kT} e^{-E/kT} dE$$

To estimate the fraction of the activated insulin receptor molecules in the absence of insulin, we note that the insulin receptor basal autophosphorylation rate is increased 10- to 20-fold in the presence of insulin (Flores-Riveros *et al*, 1989; Kohanski, 1993). It is reasonable to assume that the autophosphorylation rate is proportional to the fraction of the activated receptor molecules and that the basal rate is proportional to this fraction in the absence of insulin. Thus, around 5–10% of the receptor molecules are estimated to be activated in the absence of insulin. From this, the activation energy of the insulin receptor can be roughly estimated from the above equation as $5-8 \text{ kJ mol}^{-1}$. Interestingly, the conformational change of the EGF receptor also requires about $4-8 \text{ kJ mol}^{-1}$ (Ozcan *et al*, 2006), indicating that the above estimation is reasonable.

It should be pointed out that large-scale collective motions in a macromolecule are determined mostly by the macromolecule's global topology and are insensitive to structural



Figure 3 Harmonic oscillator model of the insulin receptor activation mechanism. (**A**) Plot of the Maxwell–Boltzmann distribution for a one-dimensional harmonic oscillator and reaction scheme for the spontaneous receptor activation. The 5% fraction of the activated receptor molecules (with energy of oscillations ranging from the activation energy to 'infinity') is indicated by the hatched region. (**B**) Reaction scheme for the insulin receptor activation. The forces acting to restore the inactive/ symmetrical conformation of the receptor subunits are represented by elastic springs, which can be compressed and stretched during movement of the receptor subunits. *E* stands for energy of oscillations, $E_{activation}$ —activation energy, *F*—random force vector acting on the receptor subunits, v—vector showing direction of movement of the crosslinking subunits. S1 and S2 stand for sites 1 and 2, respectively. Insulin is depicted as a black dot.

details, and that the results obtained by assuming subunits to be rigid bodies connected by elastic springs provide a good description of the allosteric dynamics (for review, see Bahar and Rader, 2005). From this perspective, the rigid body model of the symmetrical insulin receptor dimer with elastic springs attached as shown in Figure 3B (compare it with Figure 1C) is expected to provide a decent description of the insulin receptor dynamics. Indeed, such a model will be capable of the conformational changes shown in Figure 1E and the movement of its subunits will be described by harmonic oscillations. In the following, this rigid body model of the insulin receptor dimer will serve as a basis for modelling of the crosslinking reaction.

Definition of the crosslinking constant

Let us consider the behaviour of the r_0 intermediary in the absence of insulin. The harmonic oscillator model implies that in the absence of insulin there are no intermediaries with a certain stable tilt angle, although the zero tilt angle is most

likely (see Figure 3A). The tilt angle will be fluctuating (due to collisions of the solvent molecules with the receptor subunits) until an activation state is achieved, which will only be transient because the oscillation will continue its swing in the reverse direction and quickly lose its energy due to interaction with the solvent. The r_0 receptor molecules with energy of oscillations less than the energy of activation, designated $*r_0$ (and therefore in the inactive state), will reach an active state, r_0 , on average after a certain time period, τ . Then, transition from $*r_0$ to $*r_0$ can be modelled as a first-order reaction with a rate constant equal to $1/\tau$, designated from now on as the crosslinking constant, k_{cr} (see Figure 3A). As approximately 5% of receptor molecules are in the active state (see above), the transition from $*r_0$ to $*r_0$ can be modelled as a first-order reaction with a rate constant equal to $19 k_{cr}$ (Figure 3A).

Activation of the insulin receptor according to the harmonic oscillator model

Let us consider the activation of an inactive r_1 intermediary (activation of all other inactive intermediaries can be considered in a similar way). The most likely state of this intermediary (with zero energy of oscillations) is designated as $_{o}r_{1}$ and those states with energy of oscillations less than activation energy (including $_{0}r_{1}$)—as $*r_{1}$ (see Figure 3B), which represent the r_1 receptor species in an inactive state. Subunits of the $*r_1$ intermediaries will be experiencing random forces acting on them (shown by vectors *F* in Figure 3B) due to thermal motion of the solvent molecules. These forces will be varying in magnitude, direction and act for various periods of time. When these forces act synergistically for a sufficient period of time, an active state will be achieved, which (as mentioned above) will happen on average after a time period, τ , and transition to the active state, designated as r_1^+ (see Figure 3B), from the inactive can be modelled as a first-order reaction with a rate constant, k_{cr} , equal to $1/\tau$. As in the active state, the distance between insulin and site 2 is zero, the local concentration of insulin in the vicinity of site 2 becomes 'infinite', which means that the subsequent binding of insulin to site 2, and thus formation of $r_{1 \times 2}$, is 'instant' (see Figure 3B). To discriminate between ${}^*r_1^+$ and $r_{1\times 2}$, the ${}^*r_1^+$ intermediary is shown in Figure 3B with a small distance between insulin and site 2, which can also be interpreted as a snapshot of r_1^+ just before it reaches the active state. The $r_{1\times 2}$ intermediary will exist until one of the sites of the crosslink dissociates. Let us assume that it is site 2 that dissociates. This leads to the formation of r_1^- (see Figure 3B). Similar to the r_1^+ intermediary, r_1^- is shown with a small distance between site 2 and insulin, which can be interpreted as a snapshot of r_1^- just after dissociation of site 2. There is an important difference between r_1^- and r_1^+ . The two intermediaries have identical tilt angles, the same kinetic and potential energies of oscillations. But in r_1^+ the crosslinking subunits move *towards* each other (see Figure 3B, the direction of movement is indicated by vectors v), meaning that $r_{1 \times 2}$ will be formed in an instant, whereas in r_1^* the crosslinking subunits move *away* from each other (see Figure 3B), meaning that $r_{1 \times 2}$ will not be formed because as soon as r_1^- loses a small fraction of its energy due to interaction with the solvent, its energy becomes less than energy of activation, and thus by definition it becomes $*r_1$.

The crosslinking reaction leads to the formation of another six

crosslinked/activated intermediaries, designated $r_{1 \times 2}$, $r_{3 \times 4}$, $r_{1 \times 23}$, $r_{1 \times 24}$, $r_{13 \times 4}$ and $r_{23 \times 4}$ (where sign '×' in 1×2 (or

Thus, transition from ${}^*r_1^-$ to ${}_*r_1$ (see Figure 3B) can be

Reaction scheme for the insulin receptor activation

As can be seen from Figure 3B, formation of $r_{1 \times 2}$ from $*r_1$ is rate limited by the first reaction $(*r_1 \rightarrow *r_1^+)$ with a rate

constant, $k_{\rm cr}$, and dissociation of $r_{1 \times \frac{2}{*}}$ into $*r_1$ is also rate

limited by the first reaction $(r_{1 \times 2} \rightarrow *r_{1}^{-})$, which is a rate constant for dissociation of site 2 in $r_{1 \times 2}$, designated d'_{2} . As the

concentration of $*r_1$ is practically the same as that of r_1

(approximately 95% of that), the activation scheme shown in

Figure 3B can be reduced to a very simple scheme: $r_1 \rightleftharpoons r_{1 \times 2}$

(see Figure 4A), where the forward reaction has a rate constant equal to k_{cp} and the reverse— d_2' . By analogy, formation of $r_{1 \times 2}$ from r_2 is described by a similar scheme: $r_2 \rightleftharpoons r_{1 \times 2}$ (see

Figure 4A), where the rate constant of the reverse reaction

(dissociation of site 1 in $r_{1 \times 2}$) is designated as d_1' .

Binding of insulin to the crosslinked insulin

considered as almost instant.

receptor intermediaries

in the harmonic oscillator model



Figure 4 Reaction scheme for the insulin receptor binding. (A) Scheme of the crosslinking reaction. (B) Simplified scheme of the insulin receptor kinetic network. S1 and S2 stand for sites 1 and 2, respectively. Insulin is depicted as a black dot.

 3×4) means that insulin crosslinks sites 1 and 2 (or sites 3 and 4) from the inactive intermediaries $(r_1, r_2, r_3, r_4, r_{13}, r_{14}, r_{23})$ and r_{24}) (Figure 2B). Everything described so far for the insulin receptor can also be applied to the IGF1 receptor. Because of the tilt of the insulin receptor subunits in $r_{1 \times 2}$, the distance between sites 3 and 4 is increased (compared with the inactive conformation) (see Figure 1D and E), indicating that the insulin receptor may now bind two more insulin molecules (to sites 3 and 4), in contrast to inactive r_1 (which can only bind one more insulin molecule, either to site 3 or 4). Thus, we make an assumption that the insulin receptor can bind up to three insulin molecules, only when it is in the active state. As will be shown later, this assumption leads to a bell-shaped ligand dependence of the dissociation rate. Without this assumption, this dependence becomes sigmoid. Thus, for the IGF1 receptor it will be assumed that a third IGF1 molecule cannot bind to the receptor, which is reasonable because IGF1 is larger in size compared with insulin. In addition, the geometry of the binding sites in the IGF1 receptor is somewhat different from that of the insulin receptor, which could also be the reason why the third IGF1 molecule cannot bind to the receptor. Site 1 is more extensive in the IGF1 receptor complex because in addition to the 'classical' binding surface binding to L1, the C-peptide of IGF1 (absent in insulin) binds to the CR region (Keyhanfar et al, 2007). Other structural differences between site 1 of the insulin and IGF1 receptors in the L1 domain are reviewed in Lou et al (2006). Binding of the third insulin molecule to the insulin receptor leads to two more intermediaries: $r_{1 \times 234}$ and $r_{123 \times 4}$ (Figure 2C). The $r_{1 \times 2}$ intermediary will exist until one of the sites of the crosslink dissociates, leading to either r_1 (dissociation of site 2) or r_2 (dissociation of site 1), with the corresponding dissociation rate constants, d_2' for site 2, and d_1' for site 1. It is tempting to assume that $d_1'=d_1$ and $d_2'=d_2$. This is not necessarily so. For dissociation of insulin from r_1 to take place, some energy should be supplied to r_1 for breaking the binding of insulin from site 1 (the energy comes from random collisions with the solvent molecules). However, it is obvious that slightly less energy is required when the insulin receptor is in $r_{1 \times 2}$ conformation, because this conformation is 'strained' (in contrast to the 'relaxed' r_1 conformation), and the pull of the 'strained' receptor subunits contributes to breaking the binding of insulin from site 1. Thus, d_1' is expected to be larger than d_1 . Using the same reasoning, d_2' is expected to be larger than d_2 . Because the energy of the 'strained' $r_{1\times 2}$ conformation is expected to be rather small $(7.5 \text{ kJ mol}^{-1})$, one may expect that $d_1'(d_2')$ is not much larger than $d_1(d_2)$. But as it is not possible to predict precisely how much larger, two cases will be considered. In the first, it will be assumed that the increase is insignificant, or $d_1'=d_1$ and $d_2'=d_2$. In the second case, there will be no such assumption.

Effect of insulin dimerization

Insulin dimerizes in solution with a K_d value of approximately 7 μ M (Pekar and Frank, 1972). After insulin dimerization, only the hexamerization site is available for interaction of the insulin dimer with sites 2 and 4. It is not known whether the insulin dimer can bind to the receptor. However, if we make an assumption that the dimer can bind to the receptor when it is in

the active state, then simulations show that this binding is negligible. Thus, we can use our modelling results as evidence that the dimer does not bind to the receptor. However, as it is not possible to predict this result in advance, binding of the dimer is considered in the model. The insulin dimer could potentially bind only to site 2 of $r_{3 \times 4}$ and site 4 of $r_{1 \times 2}$, leading to another two intermediaries $r_{2d \times 4}$ and $r_{1 \times 24d}$ (Figure 2C).

Modelling the insulin receptor binding kinetics

Binding of insulin to the insulin receptor leads to the formation of 19 intermediaries (see Figure 2) through a network of 72 individual interactions (if one counts all possible interactions between these 19 intermediaries). The essential features of this network (with 12 intermediaries and 32 interactions) are demonstrated in Figure 4B. The complete network is shown in Supplementary Figure S3 and the corresponding differential equations in Supplementary Figure S6. It should be noted that the model does not 'allow' direct dissociation of the crosslinking insulin (binding sites 1 and 2 simultaneously) from $r_{1 \times 234}$ until one of the insulin molecule dissociates from sites 3 or 4. This is a consequence of the assumption that the third molecule can bind only when the receptor is in the active state (see above). This means that as long as the third molecule is bound, the receptor is in the active state (if not, the third molecule would be bound to the receptor in the *inactive* state, contradicting the assumption). If one of the receptor's sites binding to the crosslinking insulin dissociates, the active conformation will still be maintained (as the third insulin molecule is bound). However, as the local concentration of the crosslinking insulin in the vicinity of the dissociated site is 'infinite' (because the active state is still maintained), the crosslinking insulin is expected to 'instantly' rebind. Another reason is that the crosslinking insulin could be entrapped between the receptor subunits when the receptor is in the active state (see Figure 1B), and as long as the active state is maintained, insulin may not be able to escape from the binding cavity due to steric hindrances. However, the crosslinking insulin is 'allowed' to dissociate indirectly, for example, as follows: $r_{1 \times 234} \rightarrow r_{1 \times 23} \rightarrow r_{13} \rightarrow r_3$ (see Figure 2), leading to dissociation of the insulin molecule, which was initially crosslinking sites 1 and 2 in $r_{1 \times 234}$.

Modelling the ligand dependence of the receptor dissociation rate requires explicit consideration of the binding of two types of ligand: unlabelled ('cold') and radioactively labelled ('hot'), which leads to the formation of 77 distinct receptor intermediaries. The number of intermediaries can be reduced to 35 if the initial conditions of the used experimental set-up are imposed. Mathematical modelling of the interactions between these 35 intermediaries (employing a system of the corresponding 35 differential equations) is described in the Supplementary information.

Modelling the IGF1 receptor binding kinetics

The IGF1 receptor kinetics can be modelled in essentially the same way as described for the insulin receptor except that (1) the third IGF1 molecule (as justified before) is not 'allowed' to bind to the receptor and (2) IGF1 does not dimerize (Brzozowski *et al*, 2002).

Experimental data used for modelling

Two sets of data were used for modelling. In the first one (a competition experiment), IM9 and 293 EBN cells were incubated for 2.5 h with hot insulin and 4 h with hot IGF1, respectively, in the presence of various concentrations of the respective cold ligand. Concentration of the hot ligand was 7 pM in both cases. Thereafter, the amount of bound radioactivity was measured (Figure 5A and B). In the second set (quantification of the ligand dependence of the dissociation rate), IM9 and 293 EBN cells were pre-incubated for 2 h with 24 pM hot insulin and IGF1, respectively. Thereafter, the hot ligand was removed and cells were incubated in a 40-fold dilution for various periods of time with various concentrations of the respective cold ligand (De Meyts et al, 1973). The amount of the remaining pre-bound radioactivity was then measured (Figure 5C and D). To minimize the effect of receptor recycling on the apparent kinetics, the data were obtained at 15°C. The recycling rate at 15°C is expected to be reduced 50- to 100-fold compared with that at 37°C. The reduced rate is still too high to be totally ignored because of long incubation times (up to 4 h). Modelling receptor recycling is described in the Supplementary information.

Fitting of the insulin receptor model to the experimental data

Fitting of the insulin receptor kinetics was carried out in Mathematica 5.2 (Wolfram Research, 2005) using a genetic algorithm (Mitchell, 1996) (with random initial values of all of the parameters) in combination with gradient minimization (see Supplementary information). The fitting procedure was repeated 25 times (every time with a different set of randomly selected initial parameters) and the average values of the fitted parameters and their standard deviations are shown in Table I. As appears from Table I, the genetic algorithm converges to very similar solutions, regardless of the initial choice of parameters, which indicates that all of the used parameters can be identified uniquely. As can be seen from Figure 5A and C, there is a very good fit between the simulated and experimental data points for the competition experiment (Figure 5A) (shown also as a Scatchard plot in Figure 5A) and for the ligand dependence of the dissociation rate (Figure 5C), which reflects the fact that on average the simulated data points are within \pm 0.53 standard deviations from the experimental data points. If one does not assume that $d_1' = d_1$ and $d_2' = d_2$, then the best fit



Figure 5 Fitting of the model to the experimental data for the insulin/IGF1 binding. (**A**, **B**) Competition experiments for the insulin and IGF1 binding, respectively (shown also as Scatchard plots in the insets). (**C**, **D**) Percentages of hot insulin and IGF1, respectively, remaining after dissociation for 20 and 60 min in the presence of various concentrations of the respective cold ligand. (**E**, **F**) Simulation of the ligand dependence of the receptor dissociation for insulin and IGF1, respectively, using the estimated parameter values.

Table I Fitted parameter values for the insulin and IGF1 receptor kinetics

Parameters	Insulin kinetics	IGF1 kinetics
Apparent $K_{\rm d}$ (nM)	0.19 ± 0.005	0.12 ± 0.006
$K_{\rm cr} ({\rm s}^{-1})$	0.33 ± 0.099	0.33
Site 1 K_d (nM)	6.41 ± 0.78	9.09 ± 0.40
Site 2 K_d (nM)	399 ± 76	490 ± 460
$a_1 (s^{-1} M^{-1})$	490000 ± 26000	347000 ± 7600
d_1 (s ⁻¹)	0.0031 ± 0.00031	0.0032 ± 0.000091
$a_2 (s^{-1} M^{-1})$	27900 ± 12100	8700 ± 8200
d_2 (s ⁻¹)	0.010 ± 0.0024	0.0042 ± 0.00014
Endocytosis rate (% per h)	12.1 ± 3.2	20.6 ± 0.1
Exocytosis rate (% per h)	8.3 ± 12.1	0.2 ± 0.3

is produced when d_1' and d_2' are approximately three times greater than d_1 and d_2 , respectively. However, the fit is improved only marginally, and the values of the other parameters are not changed significantly, which means that for practical purposes the assumption that $d_1'=d_1$ and $d_2'=d_2$ is reasonable. The K_d values for the two sites are approximately 6.4 and 400 nM. As the experimentally determined $K_{\rm d}$ for site 1 is approximately 10 nM, and for site 2 in the submicromolar range (Schäffer, 1994), it is reasonable to assign the 6.4 nM K_d to site 1, and the 400 nM K_d to site 2. Crosslinking of sites 1 and 2 leads to an apparent high-affinity binding with a $0.19 \text{ nM} K_d$ (determined from the initial slope of the simulated Scatchard plot), which is in good agreement with the experimentally determined value for these cells (approximately 0.2 nM). It is obvious that simulation of insulin binding to the monomeric insulin receptor would result in approximately 34-fold (6.41/0.19) reduction of the apparent affinity (in good agreement with a 30-fold reduction observed experimentally), and the monomeric form would show no ligand dependence for the dissociation rate (also in accordance with the experiments). However, the simulated Scatchard plot of the monomeric receptor would be curvilinear (because sites 1 and 2 have different affinity), whereas the experimental one seems to be linear (De Meyts, 1994). It should be noted that site 2 consists of residues located in three insulin receptor domains (L2, Fn1 and Fn2) and disruption of the insulin receptor quaternary structure (due to reduction of the covalent S-S bonds, necessary for production of the monomeric form) is quite likely to disrupt this site.

Fitting of the IGF1 receptor model to the experimental data

Initial fitting of the IGF1 receptor kinetics in the same way as for the insulin receptor produced a good data fit, but converged to similar solutions only for the a_1 and d_1 parameters (data not shown). It should be noted that the a_2 and d_2 parameters in the insulin receptor fitting are constrained by the upturn of the curve for the ligand dependence of the receptor dissociation rate (see Figure 5C), which happens at insulin concentrations of higher than 100 nM (this corresponds to binding of the third insulin molecule at site 2 with 400 nM K_d). However, this upturn is absent in the curve for the IGF1 receptor (see Figure 5D), and as a result, the site 2 parameters are not constrained sufficiently to produce a unique determination from the binding data alone.

To estimate the site 2 parameters, we made an assumption that the crosslinking constant, $k_{\rm cr}$, of the IGF1 receptor is similar to that of the insulin receptor. The plausibility of this assumption is based on the fact that $k_{\rm cr}$ depends on the dynamics of the large-scale collective motions in the receptor, which are essentially determined by the macromolecule's global topology and are insensitive to structural details (for review, see Bahar and Rader, 2005). The structure of the IGF1 receptor dimer has not yet been determined, but the structure of the IGF1 receptor L1-CR-L2 fragment is very similar to the equivalent insulin receptor fragment (Lou et al, 2006). Taking also into account high sequence similarity between the two receptors and the fact that the hybrid insulin-IGF1 receptors bind IGF-I with high affinity, there is no doubt that the global topology of the two receptors is very similar. Thus, the assumption that the crosslinking constants of the two receptors are similar is quite reasonable.

Fitting data with the fixed k_{cr} parameter (equal to the k_{cr} for the insulin receptor) results in similar solutions regardless of the initial choice of the other parameters (see Table I) and a good data fit (see Figure 5B and D). The only parameter that is not well defined is a_2 . Compared with the insulin receptor, the IGF1 receptor appears to have 1.6 higher apparent affinity, but slower association and dissociation kinetics: a_1 is lower 1.4fold, d_1 is unchanged, a_2 appears to be lower 3.2-fold (but this result is not very reliable due to a large uncertainty in a_2) and d_2 is lower 2.4-fold. A comparison in the ligand dependence of the receptor dissociation for the insulin and IGF1 receptors, based on the estimated parameter values (see Table I), is shown in Figure 5E and F.

Discussion

In this article, we present the first mathematical model that accurately reproduces all the kinetic properties of the insulin and IGF1 receptors. In previous models of the insulin receptor binding kinetics (kinetics of the IGF1 receptor has not been modelled before) (Hammond et al, 1997; Wanant and Quon, 2000; Sedaghat et al, 2002), a two-site binding model was used to generate a curvilinear Scatchard plot resembling that of the insulin receptor, but modelling of the ligand dependence of the dissociation rate was not even attempted. Our model is different from the previous ones not only because it is capable of accurately reproducing all the kinetic properties of the insulin and IGF1 receptors but also because it is the first model that gives a physically plausible description of the two receptors' binding and activation in terms of interactions between the molecular components and takes fully into account the combinatorial complexity arising from multivalent binding to multiple receptor conformations.

The presented mathematical model builds on a structurally and thermodynamically justified assumption that the insulin receptor conformational change (required for the receptor activation) can be described by harmonic oscillations of the receptor subunits. By analysis of the behaviour of an ensemble of the insulin receptor 'harmonic oscillators' in thermal equilibrium with the surrounding milieu, we developed a physically plausible model of the receptor crosslinking (activation), which allows to model the latter in a simple



Figure 6 Scheme of the insulin receptor binding at physiological insulin concentrations.

way, using only one parameter. As description of insulin binding to two different sites requires four parameters, the harmonic oscillator model requires only five parameters. In spite of this, the model gives a very accurate description of the insulin receptor binding kinetics, and with a minor modification—of the IGF1 receptor as well.

The presented model uses a rather complex network of interactions for description of the insulin kinetics. However, now that the parameters have been determined, this network may be reduced substantially depending on the experimental set-up. Simulations show that at physiological concentrations of the two ligands (i.e. lower than 0.1 nM), the kinetic network shown in Figure 4B simplifies to a very simple scheme, shown in Figure 6, in which the major route (accounting for 77% at equilibrium) is shown by solid lines, and the supplementary (accounting for 23%)—by dashed lines. If the supplementary route is ignored, the equilibrium level of $r_{1 \times 2}$ can be calculated as follows:

$$r_{1\times 2} = \frac{r_{\rm tot}k_{\rm cr}/(k_{\rm cr}+d_2)}{1 + \frac{d_2d_1}{a_1(d_2+k_{\rm cr})}/L}$$

where *L* is the insulin concentration and r_{tot} is the total receptor level. By comparing this expression with the formula for a single site binding:

bound =
$$\frac{r_{\rm tot}}{1 + K_{\rm d}/L}$$

we obtain that the insulin receptor K_d can be calculated from the values of the individual parameters as

$$K_{\rm d} = \frac{d_1 d_2}{a_1 (d_2 + k_{\rm cr})}$$

Using the determined parameter values (see Table I), we obtain from this formula that the insulin receptor K_d can be estimated as 0.186 nM (in good agreement with experiments). The scheme shown in Figure 6 is also valid for the physiological concentrations of IGF1, and applying the above formula to the estimated IGF1 parameters (see Table I), the IGF1 receptor K_d can be estimated as 0.114 nM (also in good agreement with experiments).

Our model represents an essential first step in building a systems biology analysis of the insulin/IGF-I signalling networks to explain the combinatorial nature of their biological specificity. It has been demonstrated previously that mitogenic potencies of insulin analogues with altered kinetic properties correlate well with the analogues' dissociation rate from the receptor: the slower the dissociation, the higher the mitogenic potency (Shymko *et al*, 1997; Kurtzhals *et al*, 2000). In this study, we have shown that IGF1 dissociates from its receptor much slower than insulin

(compare dissociations shown in Figure 5C with D at physiological concentrations of the two ligands, i.e. below 0.1 nM). The apparent dissociation rates for IGF1 and insulin (in the presence of the two ligands at physiological concentrations) can be estimated from Figure 5C and D as 0.16 and $0.54 \,h^{-1}$, respectively. Thus, IGF1 also complies with the above-mentioned correlation of mitogenicity versus dissociation rate, as IGF1 dissociates slower and it is more mitogenic than insulin. This suggests that kinetic proofreading could be one of the factors determining the signalling specificity of insulin, IGF1 and the insulin analogues (at least as far as mitogenicity is concerned). In the kinetic proofreading model of signalling specificity (McKeithan, 1995; Hlavacek et al, 2001), the activated receptor must complete a cascade of reversible modifications before a cellular response can occur. If the ligand dissociates before the full set of modifications is complete, the receptor reverts to its basal unmodified state. Thus, the average lifetime of the receptor in the activated state (which is equal to the reciprocal of the ligand dissociation rate constant) determines whether or not a particular biological response occurs in a signalling cascade that is under a strict kinetic proofreading control. However, application of the kinetic proofreading concept to the insulin/IGF1 signalling appears to be problematic, because the average lifetime of the insulin and IGF1 receptors in the ligand-bound state is approximately 2 and 6 h (calculated from the rate constants estimated above), respectively, whereas all of the insulin/IGF1 receptor effectors require at most 20 min for maximum activation in brown adipocytes (Krüger et al, 2007) and 45 min in white adipocytes (Schmelzle et al, 2006), with the majority of the effectors requiring only from 1 to 5 min for the maximum activation.

However, according to the presented model, the active state is maintained continuously for a much shorter period of time than the ligand-bound state. If we consider an insulin receptor intermediary with one insulin molecule bound (which corresponds to the binding under physiological insulin concentrations), then the insulin receptor molecule is expected to shuttle between the active $r_{1 \times 2}$ state and the inactive r_1 and r_2 states (see Figure 6). On the basis of the determined rate constants (see Table I), it is easy to calculate that the insulin receptor is expected to be continuously in the active state on average for approximately 76 s, whereas the IGF1 receptor for approximately 135 s. Thus, the difference in the average lifetime of the activated states of the two receptors is approximately two-fold. This two-fold difference, as demonstrated by Hlavacek et al (2001), can result in high signalling specificity depending on the kinetic parameters of a particular signalling pathway. As the majority of the insulin/IGF1 receptor's effectors reach maximum activation with a delay of 1-5 min after stimulation with the ligand (Krüger et al, 2007), the predicted lifetimes of the active states of the two receptors are sufficiently short to have a potential effect on some of the effectors due to kinetic proofreading. Whether or not a particular effector is under control of kinetic proofreading requires a careful kinetic analysis of the signalling pathway involved, which is not the aim of this study. However, it is interesting to note that activation of the Ras-MAP kinase pathway, responsible for the control of cell growth, results in a maximum activation of the ERK1 and ERK2 kinases with a delay of approximately 5 min (Krüger et al, 2007). If we hypothesize that this pathway is under control of kinetic proofreading, and use the 5 min delay as a rough estimate of the time period necessary for activation of the two MAP kinases, then IGF1 is expected to activate this pathway more efficiently than insulin, as the average lifetime of the activated state of the IGF1 receptor is two-fold smaller than the time period required for the MAP kinase activation, whereas in the case of the insulin receptor it is four-fold smaller. The above observation provides a possible explanation for the fact that IGF1 is more mitogenic than insulin, and in general for the correlation between the mitogenicity of insulin analogues and the kinetics of their dissociation. Whether or not it is true requires further investigation.

The soluble insulin receptor has a 10-fold higher affinity than the receptor expressed in the cell membrane (Schäffer, 1994). The reason for this interesting phenomenon has until now been lacking. However, the presented model provides a natural explanation for it. As discussed before, the crosslinking constant depends on the dynamics of the receptor conformational change. As the conformational change is coupled with some movement of the receptor transmembrane subunits in the membrane, the dynamics in solution are expected to be faster due to lower viscosity of the buffer solution (used in the binding experiments) in comparison with the cell membrane. The faster dynamics are expected to result in a larger value for the crosslinking constant, and thus higher affinity. For more discussion of this topic as well as an analysis of the receptor dissociation routes leading to the ligand dependence of the receptor dissociation, see Supplementary information.

It should be pointed out that the scope of our model is far from being purely theoretical. It has in fact wide-ranging applications due to its ability to provide robust determination of experimental binding parameters. Thus, we have now evaluated the five constants that define the model for the two alternatively spliced isoforms of the insulin receptor and solved some kinetic issues that had been controversial for many years (Knudsen et al, manuscript in preparation). We have shown that the insulin receptor A isoform (lacking exon 11) has 1.5-fold higher affinity and slightly faster apparent association and dissociation kinetics compared with the insulin receptor B isoform (containing exon 11). The differences between the two isoforms appear to be entirely due to the parameters of the site 1: the a_1 and d_1 are larger three- and two-fold, respectively, in the A isoform compared with the B-isoform. We have also started a detailed evaluation of the kinetics of binding of a number of 'supermitogenic' insulin analogues to both insulin receptor isoforms, to determine which parameters correlate with enhanced mitogenicity. This is a critical issue in the molecular toxicology of insulin analogues, which are increasingly replacing regular insulin in the therapy of diabetes mellitus; enhanced mitogenicity in vitro of some analogues has been an issue of great concern (Kurtzhals et al, 2000; Hansen, 2008).

In conclusion, we present the first model that allows to explain mathematically all the kinetic properties of the insulin and IGF1 receptors. The model may be adaptable to other RTKs as well as cytokine receptors. Also, there is growing evidence that many receptors of the GPCR family (containing more than 800 members in humans) function as pre-bound dimers, and some of them have been shown to display negative cooperativity in ligand binding similar to that of the insulin receptor/ IGF1R (Springael *et al*, 2007). The present model may thus be used for modelling not only the insulin and IGF1 receptors' binding but also a large number of other receptors in which ligand crosslinking occurs.

Supplementary information

Supplementary information is available at the *Molecular Systems Biology* website (www.nature.com/msb).

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Conflict of interest

The authors declare that they have no conflict of interest.

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