

1 Identification of distinct subtypes of post-stroke 2 and neurotypical gait behaviors using neural 3 network analysis of kinematic time series data 4

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34 **Abstract**

35 **Background**

36 Heterogeneous types of gait impairment are common post-stroke. Studies used supervised and
37 unsupervised machine learning on discrete biomechanical features to summarize the gait cycle
38 and identify common patterns of gait behaviors. However, discrete features cannot account for
39 temporal variations that occur during gait. Here, we propose a novel machine-learning pipeline
40 to identify subgroups of gait behaviors post-stroke using kinematic time series data.

41 **Methods**

42 We analyzed ankle and knee kinematic data during treadmill walking data in 39 individuals post-
43 stroke and 28 neurotypical controls. The data were first input into a supervised dual-stage
44 Convolutional Neural Network-Temporal Convolutional Network, trained to extract temporal and
45 spatial gait features. Then, we used these features to find clusters of different gait behaviors
46 using unsupervised time series k-means. We repeated the clustering process using 10,000
47 bootstrap training data samples and a Gaussian Mixture Model to identify stable clusters
48 representative of our dataset. Finally, we assessed the kinematic differences between the
49 identified clusters using 1D statistical parametric mapping ANOVA. We then compared gait
50 spatiotemporal and clinical characteristics between clusters using one-way ANOVA.

51 **Results**

52 We obtained five clusters: two clusters of neurotypical individuals (C1 and C2) and three
53 clusters of individuals post-stroke (S1, S2, S3). C1 had kinematics that resembled the normative

54 gait pattern. Individuals in C2 had a shorter stride time than C1. Individuals in S1 had mild
55 impairment and walked with increased bilateral knee flexion during the loading response.
56 Individuals in S2 had moderate impairment, were the slowest among the clusters, took shorter
57 steps, had increased knee flexion during stance bilaterally and reduced paretic knee flexion
58 during swing. Individuals in S3 had mild impairment, asymmetric swing time, had increased
59 ankle abduction during the gait cycle and reduced dorsiflexion bilaterally during loading
60 response and stance. Every individual was assigned to a cluster with a cluster membership
61 likelihood above 93%.

62 **Conclusions**

63 Our results indicate that joint kinematics in individuals post-stroke are distinct from controls,
64 even in those individuals with mild impairment. The three subgroups post-stroke showed distinct
65 kinematic impairments during specific phases in the gait cycle, providing additional information
66 to clinicians for gait retraining interventions.

67 **Key words**

68 Stroke, gait, rehabilitation, machine learning, neural networks, clustering, kinematics

69 **Background**

70 Gait patterns differ between stroke survivors due to heterogeneity in stroke lesion type, size,
71 location, and differences in recovery ¹⁻⁷. These differences make intervention prescription
72 difficult in both research and rehabilitation interventions. Developing approaches to identify
73 intervention targets systematically can enhance the efficacy of physical therapy interventions to
74 improve walking function in stroke survivors.

75
76 The different types of gait patterns post-stroke have been identified qualitatively and
77 quantitatively in prior research studies ^{1,2,5,6,8}. Using visual assessment of paretic
78 electromyography (EMG), a seminal study ¹ identified three subgroups of abnormal muscle
79 activation during gait post-stroke based on activation onset and levels – early triceps surae
80 activation, decreased activation of paretic musculature, and paretic muscle coactivation ¹.
81 Similarly, Olney and Richards qualitatively identified different subgroups of gait impairments
82 using peak spatiotemporal, peak kinematic, and peak kinetic characteristics ⁶. A more
83 systematic quantitative approach used paretic EMGs (onset and percentages of maximum
84 voluntary contraction) and paretic peak kinematics input into a hierarchical clustering algorithm
85 to identify four clusters of gait behaviors post-stroke ²: a fast walking group with slight knee
86 flexion in mid-stance, an intermediate velocity group with increased knee flexion in mid-stance,
87 a slow group with excessive knee flexion in midstance and a slow group with knee
88 hyperextension in mid-stance ². Our recent work used spatiotemporal variables and peak
89 ground reaction forces from both the paretic and non-paretic extremity input into a k-means
90 clustering algorithm to identify four types of gait behaviors in individuals post-stroke ⁵: fast and
91 asymmetric walkers, moderate speed, and asymmetric walkers, slow walkers with frontal plane
92 impairment, and slow and symmetric walkers. While all these previous studies have provided

93 valuable information to identify different types of gait behaviors post-stroke, a caveat is that they
94 have used discrete metrics over the gait cycle ^{2,5,6,8}. These discrete gait metrics summarize
95 changes in magnitude but not in the timing of gait kinematics, kinetics, and EMGs that result in
96 gait impairment post-stroke. Thus, these previous studies cannot identify specific phases of the
97 gait cycle that could be targeted in rehabilitation interventions.

98

99 The use of machine learning methods to study gait has become common practice in research ⁹.
100 Previous studies using supervised methods aimed to accurately classify neurotypical and
101 pathological gait or detect types of activities ⁹. Most of these studies use handpicked discrete
102 summary features ⁹. However, machine learning algorithms can be leveraged to select more
103 complex and objective features using multivariate time series. Cui et al. ¹⁰ proposed a
104 framework using neural networks to handle multidimensional time series to classify neurotypical
105 and post-stroke gait and assess walking quality. While providing a walking quality score is
106 promising, it does not inform clinicians what to target systematically during rehabilitation
107 interventions. Unsupervised methods, on the other hand can be employed to identify clusters in
108 a dataset ¹¹. For example, Pulido-Valdeolivas et al ¹² used time series and combined dynamic
109 time-warping algorithms with unsupervised clustering methods to identify clusters of gait
110 behaviors in individuals with hereditary spastic paraplegia. The dynamic time warping approach
111 of the previous study can handle multivariate time series and uses a distance metric to compare
112 the similarity between signals that may differ in duration ¹³. However, a completely unsupervised
113 approach can be sensitive to outliers dependent on the choice of distance measure and leading
114 to results that are not always generalizable, thus difficult to interpret ¹¹. Therefore, using a first
115 supervised layer to accurately extract features distinct between individuals post-stroke and
116 neurotypical controls before a second unsupervised machine learning methods to identify the
117 clusters might be a more suitable approach to identify clusters of gait behaviors post-stroke.

118

119 Here, we designed a pipeline to analyze time series data that combines supervised and
120 unsupervised analyses. First, we use supervised analyses to extract features from time series
121 data that best distinguish between individuals post-stroke and neurotypical controls. Then, we
122 use unsupervised clustering using features weights of the supervised stage to identify clusters
123 of gait behaviors. We compared the performance of our proposed pipeline with an unsupervised
124 time series clustering algorithm available in R¹³. We developed and validated our approach
125 using kinematic data, as these data can be assessed in the clinic via visual gait analysis or
126 simple video gait analysis¹⁴⁻¹⁶. We implemented our pipeline in a sample of participants post-
127 stroke and age-matched controls, to determine whether less impaired individuals post-stroke
128 could be comparable to neurotypical controls. We hypothesized that we would observe distinct
129 clusters of gait behaviors in individuals post-stroke^{1,2,5}, and a cluster of control individuals and
130 individuals post-stroke with gait behaviors indistinguishable from controls⁵, indicative of full
131 recovery of gait post-stroke. Our proposed pipeline can be applied to other time series data
132 during different motor tasks and to other pathological populations to identify subtypes of
133 behaviors across different variables and populations.

134 **Methods**

135 Data for a total of $n = 67$ participants, including 39 individuals post-stroke and 28 age and sex-
136 matched controls were curated from previous studies (Table 1)^{5,17,18}. Inclusion criteria for
137 participants post-stroke were: (1) a unilateral stroke more than six months before the study, (2)
138 paresis confined to one side, (3) ability to provide informed consent and communicate with the
139 investigators, and (4) ability to walk 5 minutes on a treadmill without the assistance of another
140 individual or walking aids (e.g., a cane or walker). The use of an ankle-foot orthosis or brace
141 was permitted during data collection. Inclusion criteria for neurotypical participants were: (1)

142 being of the same age and sex as a participant post-stroke, (2) having no musculoskeletal or
143 neurologic injury that hinders walking ability, (3) ability to provide informed consent and
144 communicate with the investigators.

145 **Experimental Protocol for Data Collection**

146 We performed the following assessments in both participants post-stroke and neurotypical
147 controls: Berg Balance Scale (BBS)¹⁹, Activity-Specific Balance Confidence (ABC) test²⁰, and
148 10-meter walk test. In participants post-stroke, we performed the lower extremity motor domain
149 of the Fugl-Meyer (FM) assessment of motor impairment²¹ and the Functional Gait Assessment
150 (FGA)²².

151
152 After clinical assessments, we determined participants' self-selected speed on an instrumented
153 treadmill (Bertec, Columbus, USA) using the staircase method²³, by progressively increasing or
154 decreasing the speed in increments of 0.05 m/s until the participant felt that the speed was
155 comfortable. The treadmill speed was required to be at least 70% of their overground walking
156 speed measured via the 10-meter walk test. Post-stroke participants walked at this speed for
157 three minutes, instructed to walk as it felt natural. For neurotypical controls, participants walked
158 at their self-selected speed and the speed of a participant post-stroke matched for age and sex.
159 All clustering analyses in control participants used data collected while walking at a matched
160 speed of a stroke participant of the same age and sex to differentiate impairments due to stroke
161 from those due to walking at a slower speed.

162
163 Segmental kinematics were recorded using a full-body marker set, placing retroreflective
164 markers on bony landmarks and marker clusters over the upper arms, lower arms, thighs,
165 shanks, and heels^{24,25}. Marker data were recorded using a 10-camera Qualisys Oqus motion

166 capture system (Qualisys AB, Göteborg, Sweden) at 100 Hz. Forces were measured from force
167 plates embedded in the treadmill at a sample 1000 Hz.

168 **Data Processing**

169 Markers were labeled using Qualisys Track Manager and then exported to Visual 3D (C-Motion,
170 Kingston, Canada) to construct a full-body model. Three-dimensional marker positions were
171 filtered using a Butterworth lowpass filter with a 6 Hz cutoff frequency. We then created a body
172 model in Visual 3D with the following segments: trunk, thighs, shanks, and feet. Participants
173 post-stroke wore a safety harness over their pelvis to prevent falls¹⁸. Thus, we removed the
174 reflective markers from the pelvis, which prevented us from calculating hip and pelvis
175 kinematics. All data were exported from Visual 3D to MATLAB for further processing.

176
177 Data processing and analysis were done in MATLAB (2023b, The MathWorks Inc, Natick, USA)
178 using custom-written code. Kinematic data for the ankle in the plantar/dorsiflexion degree of
179 freedom, ankle abduction/adduction degrees of freedom, and the knee in the flexion/extension
180 degrees of freedom were extracted for the middle 50 seconds of the walking trial for both
181 extremities in all participants (Fig. 1 A). Data were segmented into strides using ground reaction
182 forces, with a threshold of 32 N^{26,27} to detect initial contact. All strides were interpolated in time
183 to 101 samples, with the first sample corresponding to 0% of the gait cycle or initial contact and
184 100% corresponding to the end of the gait cycle. We obtained the median over the gait cycle
185 across all strides to reduce the influence of outlier stepping patterns, thus obtaining a
186 representative stride for each degree of freedom in both extremities for each participant (Fig. 1
187 A). In participants post-stroke, we identified the paretic and non-paretic extremities. For data
188 collected in neurotypical adults, leg dominance was defined as the leg they would use to kick a
189 ball, which was the right leg for all participants. Control data are labeled as dominant and non-
190 dominant, and comparisons are made for the non-dominant leg vs. the paretic leg, and the

191 dominant leg vs. the non-paretic leg. 0% of the gait cycle is expressed relative to the non-
192 dominant or paretic heel strike for both limbs.

193 **Time series clustering analyses**

194 **Machine Learning Pipeline**

195 We used a deep learning method combining a Convolutional Neural Network (CNN)²⁸ and a
196 Temporal Convolutional Network (TCN)²⁹ to extract features from kinematic time series in the
197 frequency and in the time domain, respectively, to have a complete gait representation for each
198 individual. To extract the frequency-related features of the gait signals, we first applied a
199 continuous wavelet transform³⁰ to express our data in the time-frequency domain and then
200 used a CNN. In parallel, to extract the time-related features, we used a TCN on the kinematic
201 time series. Hence, CNN and TCN were first trained with labels (control/stroke) to select
202 features in a multivariate signal that can distinguish the two groups. Then, we used
203 unsupervised time series k-means clustering to identify clusters of gait behaviors using the
204 combined weights of the CNN-TCN features. The clustering pipeline was coded in Python (3.11,
205 Python Software Foundation) and is available for download³¹. In more detail, the different
206 stages of our pipeline are (Fig. 1B):

207 1) Convolutional Neural Network³²: We first pre-processed the time series data into a
208 continuous wavelet transform module that allows a two-dimensional representation of the
209 signals as time-related frequency components. We multiplied each signal by the Morlet
210 wavelet and the wavelet coefficients of the transformed signals were used as the inputs to
211 the CNN. Then, the extracted wavelet coefficients are input into a CNN designed to learn
212 spatial hierarchies of features automatically and adaptively through backpropagation. Two

213 convolution kernels were applied to obtain 32 convolutional kernels with the size of 3×3,
214 followed by a 2D max pooling layer, and 64 convolutional kernels with the size of 3×3, a 2D
215 max pooling layer, are used to extract high-level features. A flattened layer was used to
216 reorganize the feature maps into a one-dimensional array and fed into two consecutive fully
217 connected dense layers of 128 and 64 features, respectively.

218 2) Temporal Convolutional Network²⁹: Since CNN only collects waveform characteristics,
219 resulting in a lack of time series characteristics, the raw signals are fed in parallel, directly
220 into a TCN module to extract temporal features. By fusing the two networks, we can
221 effectively learn the spatial-temporal information in each gait cycle. The TCN is a residual
222 network-based CNN designed for handling time sequence data. The output of TCN is a
223 flattened layer of 64 features.

224 3) Supervised feature extraction: the outputs of CNN and TCN are concatenated into a
225 combined TCN- CNN model and fed into two consecutive fully connected layers of 101
226 features and trained with the labels control/stroke to identify the high-level spatiotemporal
227 features for neurotypical and post-stroke gait.

228 4) Unsupervised clustering: Once the full model is trained, it serves as a feature extractor for
229 every participant. The gait signals are fed again into the trained model, then the extracted
230 features are further used for time series k-means clustering.

231 To ensure that the results are representative of our dataset and not dependent on a unique
232 training and testing split, we bootstrapped the classification stroke/control from CNN-TCN, CNN
233 only and TCN only, a total of 10,000 times. At each iteration, a new random stratified 80/20
234 train/test split was performed to train the models. We also performed bootstrap analyses of the
235 R time series clustering algorithms using 10,000 iterations, with each iteration being a new
236 random seed to change the starting point of the algorithm.

237 **Number of clusters and cluster stability**

238 To determine the optimal number of clusters c , we calculated the within-clusters sum of squared
239 errors over $b = 10,000$ bootstrap iterations³³ for $c = 2$ to 10 clusters and identified the number of
240 clusters c' that did not decrease the within-clusters sum of squared errors. We then selected c
241 as the number of clusters having an average within-cluster sum of squared errors under one
242 standard error of c' ¹¹ (Fig. 1 C.1)

243 After the bootstrap iterations, we obtained a clustering matrix M (individuals x iterations) where
244 each element represents a cluster number from 1 to c . To assess the occurrences of individuals
245 classified together in the same cluster (Fig. 1 C.2), we first calculated a similarity matrix S
246 (individuals x individuals):

$$S_{i,j} = \frac{\sum_{k=1}^b \delta(M_{i,k}, M_{j,k})}{b}$$

247 Where i and j are indices to represent individuals, k is the iteration index and

$$\delta(M_{i,k}, M_{j,k}) = \begin{cases} 1, & \text{if } M_{i,k} = M_{j,k} \\ 0, & \text{if } M_{i,k} \neq M_{j,k} \end{cases}$$

248 Then to recover the c number of stable clusters, we compute the dissimilarity matrix D as
249 $D = 1 - S$, and projected it in a lower two-dimensional latent space using multidimensional
250 scaling, preserving the pairwise Euclidean distance between each element¹¹ (Fig. 1 C.3).
251 Finally, with the new latent space coordinates, we performed a clustering for c clusters using a
252 Gaussian mixture model as a sum of c Gaussian distributions with their own mixing proportions,
253 mean, and full covariance matrices¹¹. This probabilistic method is better suited to handle
254 nonspherical clusters as we obtained in the latent space (Fig. 1 C.3) and allows us to obtain
255 individual probability estimates of each participant belonging to each of the identified clusters¹¹.

256 The Gaussian mixture clustering was performed b times, each iteration corresponding to new
257 initialization parameters for the Gaussian mixture model. The final clustering model was chosen
258 to minimize the Akaike Information Criterion across the b iterations (Fig. 1 C.4) ^{11,34}.

259 **Pipeline comparison**

260 We verified if combining both frequency and time-related features improves the classification
261 into stroke/control by comparing our full CNN-TCN pipeline to the classification output of CNN
262 only and TCN only. At the supervised stage, i.e., stage 3, after the last layer, we added a size 1
263 fully connected layer using a sigmoid activation for a binary stroke/control classification. We
264 processed similarly to assess the classification of the CNN and TCN blocks alone. We used the
265 classification of each test set to build the confusion matrix of actual versus predicted labels
266 (stroke/control) and compute a standard accuracy metric of the supervised models ²⁸. We also
267 compared our method to a readily available unsupervised multivariate time series clustering
268 using a dynamic time-warping algorithm (R package *dtwclust*) ¹³ and a partitional clustering
269 performed on the dynamic time-warping barycenter averaging centroids. We used the entire set
270 for the unsupervised clustering into two groups.

271 Finally, we evaluated the goodness of fit of the five components Gaussian mixture model by
272 comparing the Akaike Information Criterion for our CNN-TCN pipeline compared to TCN only
273 and CNN only. In addition, we also verified that the supervised learning layers are not biased
274 toward classifying an individual into a control or a stroke group (Supplementary materials 1). To
275 do so, we looked at the projection of the dissimilarity matrix into the multidimensional scaling
276 space and after the 10,000 iterations when (1) we mislabeled a stroke participant that had the
277 highest Fugl-Meyer score (i.e. 34) into a control participant (total 67 individuals, 38 post-stroke
278 and 29 control), and (2) we added the high Fugl-Meyer stroke participant with a control and a
279 stroke label (total 68 individuals, 39 post-stroke and 29 control).

280 **Statistical analysis**

281 **Comparisons between individuals post-stroke and neurotypical controls**

282 We assessed for significant differences in demographics and clinical measures between
283 participants post-stroke and neurotypical controls in SPSS (29.0, IBM Corp, Armonk, USA).
284 Data were assessed for normality using the Shapiro-Wilk test. If data were normally distributed,
285 we used independent samples t-tests to compare data between groups. Otherwise, we used the
286 Wilcoxon Signed Rank test. To compare differences in the distribution of males vs. females
287 across groups, we used a Chi-Square test. For normal data, values are reported as mean \pm SD,
288 and for non-normal data, values are reported as median \pm IQR.

289 **Comparison within clusters**

290 Within each control cluster (C1 and C2), we compared the participants' self-selected speed to
291 the matched walking speed using a paired t-test.

292 Within each stroke cluster (S1, S2, S3), we used Student's t-tests to assess for asymmetries
293 within clusters between paretic/non-paretic extremities for step length, swing time, and stance
294 time. The significance level was Bonferroni corrected according to the number of tests. We also
295 computed Pearson's correlation coefficient between the treadmill walking speed and the clinical
296 assessments.

297 **Comparison between clusters**

298 We used a one-way ANOVA to compare demographics, clinical measures, and spatiotemporal
299 gait measures (dependent variables) between clusters (independent variable). If we observed
300 significant results from the ANOVA, we performed multiple comparisons with Tukey's test. We

301 clarify that these discrete metrics were not used in the machine learning pipeline to identify the
302 distinct gait clusters and were assessed post-hoc.

303 We used 1-dimensional statistical parametric mapping³⁵ one-way ANOVA with cluster identifier
304 as the independent variable to assess kinematic time series differences between clusters. Post-
305 hoc tests were done via statistical parametric mapping t-tests with Bonferroni correction for
306 multiple comparisons. We used 2-dimensional statistical parametric mapping³⁶ to compare the
307 continuous wavelet transform matrix coefficients between groups in the time-frequency domain
308 (Supplementary materials 2). These kinematics characteristics were used by the machine
309 learning pipeline to identify the distinct gait clusters.

310 **Results**

311 Participants post-stroke were 59.5 ± 10.8 years old, had a mass of 76.5 ± 15.8 kg, and were 92
312 ± 84.5 months post-stroke. 22 participants were male and 17 female. Control participants were
313 62.4 ± 14.2 years old and had a mass of 74.1 ± 16.3 kg. 12 control participants were male and
314 16 female (Table 1). As data were extracted for the middle 50 s of walking to ensure a steady
315 gait pattern, this resulted in 39.2 ± 7.2 strides for control participants at the matched speed and
316 37.9 ± 6.5 strides for individuals post-stroke. Two participants post-stroke wore an ankle brace
317 while walking.

318 **No significant differences in demographics between participants** 319 **post-stroke and neurotypical controls**

320 We observed no significant differences between participants post-stroke and neurotypical
321 controls in age, height, mass, self-selected treadmill walking speed, or matched walking speed

322 ($p > 0.050$). We did not observe differences in the study samples' proportion of males vs. females
323 ($p > 0.05$). We observed significant differences in ABC and BBS between participants post-stroke
324 and neurotypical controls (Wilcoxon Signed Rank test $p < 0.001$, Table 1).

325 [Table 1 here](#)

326 **CNN-TCN performed better than other time series clustering** 327 **algorithms**

328 The confusion matrix for the four evaluated algorithms is presented in Table 2. During the
329 supervised analyses and over 10000 iterations, our CNN-TCN pipeline predicted individuals of
330 the test set correctly 85.0 ± 14.7 % of the time for stroke participants and 87.7 ± 11.2 % for
331 control participants. The overall accuracy for the CNN-TCN model was 86.4%, slightly higher
332 than for CNN alone (86.3%) and TCN alone (84.1%) to classify individuals as stroke/control.
333 However, the Akaike Information Criterion was lower for the CNN-TCN model (-142.5)
334 compared to CNN (6.8) alone and TCN alone (-64.0), indicating a significantly better fit of the
335 five component Gaussian Mixture Model for our proposed full CNN-TCN pipeline.

336 The unsupervised clustering based on dynamic time warping package in R was better at
337 predicting control individuals (94.8 ± 0.1 %) but was close to random at predicting stroke
338 individuals (52.5 ± 0.1 %), which resulted in worse overall accuracy (73.7%). Thus, our fused
339 pipeline performed better than the individual components of the pipeline and the R package
340 during supervised analyses using two classes due to the added ground truth knowledge and the
341 combination of both temporal and spatial features.

342 **k=5 provided stable clusters**

343 When determining the optimal number of clusters, we first identified the “elbow”³³ at $k' = 7$, and
344 then selected $k = 5$ as the optimum number of clusters using the one standard error (Fig. 1
345 C.1). Thus, we computed a 5-component Gaussian mixture model from the dissimilarity matrix
346 (Fig. 1 C.2). We observed two control clusters (C1, C2) and three clusters of individuals post-
347 stroke (S1, S2, S3) (Fig. 1 C.3 and C.4). The mixing proportion, which indicates cluster
348 membership likelihood, of almost all individuals but one to be assigned to their final cluster was
349 above 99% (Fig. 1 C.3). Only one participant in S2 had a mixing proportion of 93% for S2, with a
350 mixing proportion of 7% for S1. None of the individuals post-stroke were assigned to a control
351 cluster (Fig. 1 C.4).

352 We further assessed that our pipeline did not introduce bias in the supervised stage with the
353 added knowledge of groups to extract features. The participant with a maximal Fugl-Meyer, thus
354 considered to have recovered the most motor function among our participant²¹, was always
355 projected in the stroke clusters part of the multidimensional scaling space when mislabeled to
356 control or added with a stroke and control label (Supplementary materials 1).

357 **All clusters had significantly different clinical characteristics and** 358 **kinematic patterns**

359 We compared demographics, clinical measures, and spatiotemporal characteristics using one-
360 way ANOVA between the five identified clusters (C1, C2, S1, S2, S3), except for FM and FGA
361 which was between the post-stroke clusters only (S1, S2, S3). All clinical measures were
362 significantly different between groups: FM ($p=0.003$), FGA ($p=0.02$), ABC ($p<0.001$), BBS
363 ($p<0.001$). Age ($p=0.56$) and height ($p=0.94$) were not different between clusters. The following
364 spatiotemporal characteristics were significantly different between clusters (Fig. 3): walking

365 speed ($p=0.003$), stride length ($p=0.008$), paretic/non-dominant step length ($p=0.010$), non-
366 paretic/dominant step length ($p=0.007$), stride time ($p=0.001$), paretic/non-dominant stance time
367 ($p<0.001$), non-paretic/dominant stance time ($p=0.004$). Paretic/non-dominant swing time
368 ($p=0.57$) and non-paretic/dominant swing time ($p=0.08$) were not significantly different between
369 clusters.

370 For the knee and ankle kinematics, using 1D SPM one-way ANOVA, we observed significant
371 differences between clusters in all degrees of freedom bilaterally: paretic/non-dominant ankle
372 plantar/dorsiflexion ($p<0.001$ whole gait cycle), non-paretic/dominant ankle plantar/dorsiflexion
373 ($p=0.049$ at loading response, $p=0.001$ during pre-swing and $p=0.006$ at terminal stance),
374 paretic/non-dominant ankle abduction/adduction ($p=0.03$ during loading response), non-
375 paretic/dominant ankle abduction/adduction ($p<0.001$ whole gait cycle), paretic/non-dominant
376 knee flexion/extension ($p=0.03$ during initial contact and loading response, $p<0.001$ during pre-
377 swing, and $p=0.04$ during terminal swing) and non-paretic/dominant knee flexion/extension
378 ($p=0.002$ during terminal swing, $p=0.001$ during loading response, and swing $p=0.007$ during
379 pre-swing). We describe each cluster next:

380 **Control Cluster 1 (C1):** $N=12$. Normative gait pattern (Fig. 2). Participants in C1 were $62.8 \pm$
381 13.8 years old, walked at a self-selected speed of 0.96 ± 0.28 m/s, and were significantly slower
382 when matched to participants post-stroke (0.65 ± 0.20 m/s, $p=0.010$). This cluster was
383 composed exclusively of control individuals. Their non-dominant and dominant step lengths
384 were both 0.39 ± 0.07 m, stride length was 0.78 ± 0.13 m, stride time was 1.45 ± 0.26 s, non-
385 dominant stance time was 0.99 ± 0.22 s, dominant stance time was 1.03 ± 0.26 s, non-dominant
386 swing time was 0.46 ± 0.06 s, and dominant swing time was 0.45 ± 0.06 s (Fig. 3). The
387 kinematics in this cluster are those described in the literature for non-injured, neurotypical adults
388 ³⁷⁻⁴⁰. We report all kinematic post-hoc comparisons relative to this cluster (blue line in Fig. 4 in
389 all panels).

390 **Control Cluster 2 (C2):** N=16. Control participants with short stride times. This cluster was also
391 composed exclusively of control individuals. Participants in C2 were 62.1 ± 15.6 years old,
392 walked at a self-selected speed of 0.75 ± 0.22 m/s (significantly slower than the self-selected
393 speed of C1, $p=0.03$), and a matched speed to participants post-stroke of 0.63 ± 0.18 m/s,
394 (significantly slower than their self-selected speed, $p=0.034$, but not significantly slower than the
395 imposed speed of C1). Compared to C1, they had shorter non-dominant stance time ($0.78 \pm$
396 0.13 s, $p=0.02$) and stride time (1.18 ± 0.16 s, $p=0.009$) when walking at speeds matched to
397 participants post-stroke (Fig. 3). The non-dominant step length (0.34 ± 0.08 m), dominant step
398 length (0.32 ± 0.08 m), stride length (0.66 ± 0.16 m), dominant stance time (0.82 ± 0.18 s), non-
399 dominant swing time (0.39 ± 0.06 s), and dominant swing time (0.35 ± 0.15 s) were not
400 significantly different from C1. Interestingly, we did not observe significant differences in
401 kinematics between C1 and C2 (Fig. 4). The differences between the two control clusters are
402 present in the time-frequency domain for the dominant knee flexion/extension (Supplementary
403 materials 2). In the same range of normalized frequency [0.025-0.034 cycles/sample], compared
404 to C1, the coefficients of the continuous wavelet transform matrix in C2 were lower during initial
405 swing and loading response, but higher during mid swing (Supplementary materials 2).

406 **Stroke Cluster 1 (S1):** N=17. Stroke participants with increased knee flexion at initial
407 contact/loading response bilaterally. Participants in S1 were 58.2 ± 13.8 years old and walked at
408 a speed of 0.65 ± 0.17 m/s (Fig. 3). Their FM score was 29 ± 4 , indicating mild impairment, FGA
409 was 23 ± 5 , and BBS was 54 ± 2 . ABC was 74 ± 14 , lower than C1 ($p<0.001$) and C2 ($p<0.001$)
410 (Fig. 3). Compared to C1, they had a shorter paretic stance time (0.76 ± 0.19 s, $p=0.005$), but
411 no differences were found for paretic step length (0.35 ± 0.07 m), non-paretic step length (0.35
412 ± 0.08 m), stride length (0.70 ± 0.15 m), stride time (1.24 ± 0.22 s), non-paretic stance time
413 (0.88 ± 0.21 s), paretic swing time (0.48 ± 0.30 s), non-paretic swing time (0.37 ± 0.06 s) (Fig.
414 3). No asymmetry was detected between the paretic and non-paretic extremities for step length

415 (p=0.90), swing time (p=0.14) and stance time (p=0.07). Compared to C1, we observed
416 increased paretic knee flexion at initial contact/loading response (p=0.005), and during terminal
417 swing (p=0.005) (Fig. 4). In the non-paretic extremity, we observed increased ankle abduction
418 during pre-swing (p=0.004), terminal swing (p=0.003), and terminal stance (p=0.001). Finally,
419 for the non-paretic side, we observed increased knee flexion during pre-swing (p=0.002), at
420 initial contact, and loading response (p=0.002) (Fig. 4). This cluster had a significant positive
421 correlation between walking speed and FM (r=0.77, p<0.05), walking speed and FGA (r=0.69,
422 p=0.003), but no correlation between speed and ABC or BBS (Fig. 5). One participant in S1
423 wore an ankle brace.

424 **Stroke Cluster 2 (S2):** N=12. Increased stance knee flexion bilaterally and reduced paretic
425 swing knee flexion. Participants in S2 were 64.0 ± 3.4 years old and walked at a slower speed
426 (0.40 ± 0.15 m/s, p<0.05 compared to all other clusters) (Fig. 3). The FM score was 23 ± 5
427 indicating moderate impairment. FM score was lower than S1 (p=0.004) and S3 (p=0.02). FGA
428 was 17 ± 6 , lower than S1 (p=0.019) but not S3 (p=0.06). BBS was 46 ± 7 , lower than S1
429 (p<0.001) and S3 (p=0.02). ABC was 76 ± 15 . Compared to C1, individuals post-stroke in S2
430 had a shorter paretic step length (0.26 ± 0.08 m, p=0.005), non-paretic step length (0.25 ± 0.09
431 m, p=0.004), and stride length (0.51 ± 0.17 m, p=0.004). Compared to S1, paretic step length
432 (p=0.005), non-paretic step length (p=0.004) and stride length (p=0.004) were also shorter, with
433 longer stride time (1.47 ± 0.22 s, p=0.039) and paretic stance time (0.99 ± 0.18 s, p=0.005).
434 Their non-paretic stance time was 1.12 ± 0.25 s, paretic swing time 0.48 ± 0.15 s, non-paretic
435 swing time 0.35 ± 0.12 s (Fig. 3). No asymmetry was detected between the paretic and non-
436 paretic extremities for step length (p=0.84), swing time (p=0.07) and stance time (p=0.18).
437 Compared to C1, we observed increased paretic ankle abduction during loading response and
438 stance (p<0.001), and terminal swing (p=0.003). Compared to C1, we observed increased
439 paretic knee flexion at initial contact and loading response (p=0.005), and during terminal swing

440 (p=0.004), and decreased paretic knee flexion mid-swing (p=0.004) (Fig. 4). In the non-paretic
441 extremity, we observed increased ankle abduction during the entire stance phase (p<0.001) and
442 pre-swing (p=0.005) (Fig. 4). We also observed decreased non-paretic dorsiflexion at initial
443 contact and loading response (p=0.001). Finally, we observed increased non-paretic knee
444 flexion from terminal swing to loading response (p=0.001) (Fig. 4). This cluster had a significant
445 positive correlation between walking speed and FGA (r=0.66, p=0.02) only (Fig. 5), potentially
446 indicative of balance impairment.

447 **Stroke Cluster 3 (S3):** N=10. Increased ankle abduction. Participants in S3 were 56.7 ± 11.1
448 years old and walked at a speed of 0.62 ± 0.19 m/s. The FM score was 28 ± 4 , ABC was $79 \pm$
449 12 , FGA was 23 ± 5 , BBS was 52 ± 3 (Fig. 4). Compared to C1, they had similar gait
450 spatiotemporal characteristics paretic step length was 0.33 ± 0.09 m, non-paretic step length
451 0.34 ± 0.08 m, stride length 0.67 ± 0.17 m, stride time 1.31 ± 0.22 s, paretic stance time $0.82 \pm$
452 0.18 s, non-paretic stance time 0.92 ± 0.12 s, paretic swing time 0.49 ± 0.07 s, non-paretic
453 swing time 0.38 ± 0.05 s. The peak knee flexion occurring earlier in the gait cycle caused a
454 longer swing time on the paretic side (p=0.001). Despite no significant differences in clinical
455 scores compared to S1 (Fig. 3), this cluster showed different kinematic impairments (Fig. 3).
456 Compared to C1, we observed increased paretic ankle abduction bilaterally for the entire gait
457 cycle (both p<0.001) (Fig. 4). We observed decreased paretic dorsiflexion during loading
458 response and mid-stance (p<0.001) (Fig. 4). We observed increased paretic knee flexion from
459 loading response to mid-stance (p<0.001) and during pre-swing (p<0.001) and terminal swing
460 (p=0.003), Fig. 4. In the non-paretic extremity, we observed decreased dorsiflexion during
461 loading response (p=0.001) and terminal stance (p=0.001) (Fig. 4). Finally, we observed
462 increased knee flexion during pre-swing and initial swing (p<0.001), initial contact and loading
463 response (p<0.001), and terminal stance (p=0.002) (Fig. 4). This cluster had a significant
464 positive correlation between walking speed and FGA (r=0.66, p=0.02), walking speed and BBS

465 (r=0.68, p=0.04), but no correlation between speed and FM or ABC (Fig. 5). One participant in
466 S3 wore an ankle brace.

467 Discussion

468 Gait impairment is heterogeneous, posing a challenge in the prescription of research or
469 rehabilitation interventions⁴¹. To inform rehabilitation, previous research identified subgroups of
470 gait behaviors post-stroke based on peak spatiotemporal characteristics, peak kinematics, peak
471 kinetics, or muscular activity^{1,2,5,6,8}. These discrete metrics cannot capture the simultaneous
472 temporal and spatial variation in the gait cycle seen in people post-stroke. Here, we developed a
473 pipeline using convolutional networks to identify subgroups of gait behaviors and tested it with
474 kinematic time series data of neurotypical and chronic stroke individuals. We showed that
475 providing the true labels in a supervised stage first to extract frequency and time-related gait
476 features from kinematic time series was more advantageous than fully unsupervised time series
477 clustering techniques.

478 Our pipeline identified distinct walking behaviors both in neurotypical control and post-stroke
479 participants. In neurotypical participants, the subgroups were differentiated by their self-selected
480 walking speed which was slower in C2, thus shaping their walking pattern by altering
481 spatiotemporal and kinematics characteristics⁴². In participants post-stroke, the subgroups were
482 characterized by kinematic impairments that differentially affected distinct phases of the gait
483 cycle. Contrary to our previous work that used only peak kinetics and spatiotemporal
484 characteristics⁵, our results indicate that at a joint kinematics level, post-stroke participants are
485 distinct from neurotypical controls, even when they have minimal impairment measured via
486 clinical outcomes. Our results also indicate that individuals post-stroke can show similar levels
487 of function and impairment measured using clinical outcomes while displaying vastly different

488 joint kinematics. Finally, our results also highlight movement patterns in the non-paretic
489 extremity function during gait which are often overlooked, seldom reported^{6,43,44} and that differ
490 from the typically described compensatory pattern⁴⁵. Using our pipeline, we have provided a
491 more detailed assessment of the distinct types of gait behaviors post-stroke, which affect both
492 the paretic and non-paretic extremities, and can point at intervention targets post-stroke.

493 The three post-stroke clusters obtained in our study point to different impairments and potential
494 rehabilitation interventions. S1, stroke participants with increased knee flexion at initial
495 contact/loading and terminal swing, response bilaterally showed the least amount of gait
496 impairments. The increased paretic knee flexion seen during loading response and terminal
497 swing corresponds to common knee patterns post-stroke^{6,46} and might indicate potential hip
498 extensor weakness^{43,44}. Treatment for participants in S1 might include functional step training.

499 Participants in S1 had similar clinical and spatiotemporal characteristics as '*the moderate*
500 *speed, symmetric, and short stance times*' cluster in our previous work⁵. S2, post-stroke
501 participants with increased stance knee flexion, reduced swing knee flexion, and reduced
502 dorsiflexion showed the most impaired gait pattern. Participants in this group also showed
503 increased ankle abduction in the paretic extremity, which might point to limb circumduction to
504 advance the paretic limb forward due to the observed decreased knee flexion during the swing
505 phase^{6,44,46}. This group's spatiotemporal characteristics are quasi-similar to the '*slow speed and*
506 *frontal plane force asymmetries*' group in our previous study, with only differing stance time
507 asymmetry not present in S2. Participants in this group would benefit from dorsiflexion
508 strengthening, electrical stimulation of dorsiflexors and during swing to elicit a mass flexion
509 response^{41,44}, ankle-foot orthosis^{41,44}, manual cues to guide knee flexion during swing^{41,47}, and
510 balance training⁴⁸. S3 showed no differences in speed, FM, FGA, or Berg to S1, yet it showed
511 additional gait impairments, including a flexed knee during stance bilaterally, increased non-
512 paretic knee flexion during swing, reduced dorsiflexion bilaterally, and increased ankle

513 abduction. Potential treatments for participants in S3 include strengthening of hip extensors and
514 hamstrings, gait retraining with an emphasis on improving motor control and coordination.

515 Previous studies have used speed alone ³, or identified speed as the main determinant of
516 cluster allocation ². Our findings contrast these findings, as S1 and S3 had similar average
517 speeds and clinical characteristics while showing different kinematic patterns indicating that
518 clinical scores are not granular enough to show specific gait kinematic impairments. This was
519 also confirmed by the heterogeneity of correlation between speed and clinical scores within the
520 clusters. Using time series joint kinematics, we obtained two moderate-speed clusters and one
521 slow cluster. Some of the characteristics of our clusters resembled those previously reported ².
522 For example, S1, which had slightly decreased knee extension in terminal swing, initial contact
523 and loading response but adequate dorsiflexion, resembled the Fast group reported by Mulroy ²,
524 despite the more moderate walking speed in our participants. S2 had a slow velocity with
525 excessive knee flexion in stance and inadequate dorsiflexion in swing, similar to what was
526 reported by Mulroy ² as the slow flexed group ². We supplement this information by showing
527 impaired non-paretic kinematics, particularly increasing non-paretic ankle abduction through
528 stance, and reduced non-paretic dorsiflexion during swing, and increased non-paretic knee
529 flexion in loading response in this group. We did not observe a knee hyperextension pattern as
530 in previous work ^{2,6,46}. Overall, our findings show that clinical measures such as speed or FM
531 score are not sensitive to kinematic differences, and thus our approach can provide additional
532 insights beyond what is provided by clinical measures.

533 Combining both time-frequency (CNN) and time-related features (TCN) to find subgroups of gait
534 did not improve accuracy to classify neurotypical and post-stroke gait but provided a better
535 model to identify clusters of gait behaviors post-stroke. While kinematics differences were
536 expected in the post-stroke clusters ^{2,5,6}, they were not significant in the two control clusters. By
537 adding the time-frequency domain in our pipeline, we were able to differentiate 1) between

538 neurotypical adults presenting normative gait patterns and neurotypical adults with affected
539 kinematics because of walking at a matched slower speed⁴⁹, 2) between highly functional post-
540 stroke individuals who scored high in all the clinical assessments and ‘visually normal’
541 kinematics and neurotypical controls. Our approach has the potential to complement and
542 augment the clinical observation of gait since it can use any type of time series captured in a
543 clinical setting with wearable devices⁵⁰ or phones⁵¹.

544 **Limitations**

545 The greatest limitation of our study is the lack of hip kinematics used in the definition of gait
546 clusters. The lack of these measures limits our ability to identify subtypes of hip gait impairment
547 blurring our understanding of the causes of knee and ankle impairment, which might originate
548 due to impaired hip function. The inclusion of hip kinematics might lead to detecting additional
549 clusters, and further expand the implications of our work, such that our current and future work
550 will require the inclusion of hip kinematics. Participants were allowed to use walking aids, which
551 modify ankle and knee kinematics post-stroke⁵². Given that only two participants in our study
552 wore ankle braces, this should not affect our findings significantly. The spasticity of participants
553 post-stroke was not controlled for, and no information was collected regarding botulinum toxin
554 injection to treat lower limb spasticity, which may also affect gait⁵³. Another limitation of our
555 work is the use of a median gait cycle for each participant. Initial attempts were made to use
556 non-segmented time series data collected for 30 seconds, but we ran into issues with
557 autoencoder clustering as no two participants were alike using this approach, and even the
558 supervised initial analyses using a single stroke and a single control cluster performed with an
559 accuracy below chance. A final limitation is that we only measured self-reported injuries in
560 control participants, and thus, the presence of two control clusters might be due to underlying

561 injuries or impairment in control individuals, which may not be fully accounted for in our
562 demographics.

563 **Conclusion**

564 The presented machine-learning pipeline used kinematic time series to identify five distinct
565 subgroups of gait behavior. We showed that individuals post-stroke were clearly different from
566 neurotypical individuals at a joint level, even when they had mild impairment and similar
567 spatiotemporal characteristics. Our approach has the potential to aid clinicians by augmenting
568 observation of gait. Moreover, it can be applied to any type of pathology affecting gait and any
569 type of one-dimensional data collected during gait.

570 **List of abbreviations**

- 571 **EMG**: electromyography
- 572 **BBS**: Berg Balance Scale (max 56)
- 573 **ABC**: Activities Balance Confidence score (max 100)
- 574 **FM**: Fugl-Meyer Assessment (Lower extremities, max 34)
- 575 **FGA**: Functional Gait assessment (max 30)
- 576 **CNN**: Convolutional Neural Network
- 577 **TCN**: Temporal Convolutional Network
- 578 **C1**: Control cluster 1
- 579 **C2**: Control cluster 2
- 580 **S1**: Stroke cluster 1
- 581 **S2**: Stroke cluster 2
- 582 **S3**: Stroke cluster 3

583 **Declarations**

584 **Ethics approval and consent to participate**

585 Data collection was approved by the University of Southern California Institutional Review
586 Board, with numbers HS-19-00430 and HS-18-00533, and each participant provided written
587 informed consent. The University of Southern California Institutional Review Board IRB HS-19-
588 00075 approved data curation across multiple studies. The Chapman University IRB-23-12
589 approved de-identified data transfer from USC to Chapman University and secondary data
590 analyses. All study aspects conformed to the principles described in the Declaration of Helsinki.

591 **Availability of data and materials**

592 The data and machine learning code in Python for the current study are available for download
593 in a public repository³¹. A short video (Supplementary Material 3) is also provided to illustrate
594 gait differences between the clusters³¹.

595 **Competing interests**

596 None

597 **Funding**

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600 **Author contributions**

601 AK: Conceptualization, Methodology, Software, Formal analysis, Writing – Original Draft,
602 Visualization. AM: Conceptualization, Writing – Review & Editing. NSc: Conceptualization,
603 Methodology, Writing – Review & Editing. JM: Funding acquisition, Resources, Writing – Review
604 & Editing. YW: Conceptualization, Methodology, Software, Visualization, Writing – Original
605 Draft. NSa.: Funding acquisition, Resources, Supervision, Investigation, Conceptualization,
606 Visualization, Formal analysis, Writing – Original Draft, Data Curation

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610 for this study.

611 **Table 1: Participant demographics**

	Stroke	Control
N	39	28
Sex	17F/22M	16F/12M
Age (years)	59.5 ± 10.8 [29 – 78]	62.4 ± 14.2 [24 – 81]
Mass (kg)	74.1 ± 16.3 [45 – 104]	73 ± 15.7 [46 – 110]
Height (m)	1.58 ± 0.08 [1.44 – 1.80]	1.60 ± 0.09 [1.42 – 1.74]
Treadmill Speed (m/s)	0.56 ± 0.20 [0.20 – 0.95]	SS: 0.84 ± 0.26 [0.48 – 1.43]
ABC (100 max)	74.0 ± 18.0* [38 – 98]	95.7 ± 4.7 [83.75 – 100]
BBS (56 max)	50.8 ± 5.5* [49 – 56]	54.1 ± 2.6 [49 – 56]
FM (34 max)	26.6 ± 4.83 [15 – 33]	
FGA (30 max)	21.2 ± 0.95 [6 - 30]	
Paresis	22R/17L	
Time post-stroke	92 ± 84.5 [6 – 467] months	

612 **Table 1** Descriptive statistics are presented as average ± standard deviation with the range in
613 brackets. F: Female, M: Male, SS: Self-selected, FM: lower extremity Fugl-Meyer score, ABC:
614 Activities Balance Confidence Scale, FGA: Functional Gait Assessment, BBS: Berg Balance
615 Score, L: Left, R: Right. *Significant differences between participants post-stroke and controls
616 (p<0.05)

617

CNN		Predicted	
		Stroke	Control
Actual	Stroke	85.4%	14.5%
	Control	12.9%	87.1%

TCN		Predicted	
		Stroke	Control
Actual	Stroke	83.0%	17.0%
	Control	14.8%	85.2%

CNN-TCN		Predicted	
		Stroke	Control
Actual	Stroke	85.0%	15.0%
	Control	12.3%	87.7%

dtwclust		Predicted	
		Stroke	Control
Actual	Stroke	52.5%	48.5%
	Control	5.2%	94.8%

618 **Table 2: Confusion matrix**

619

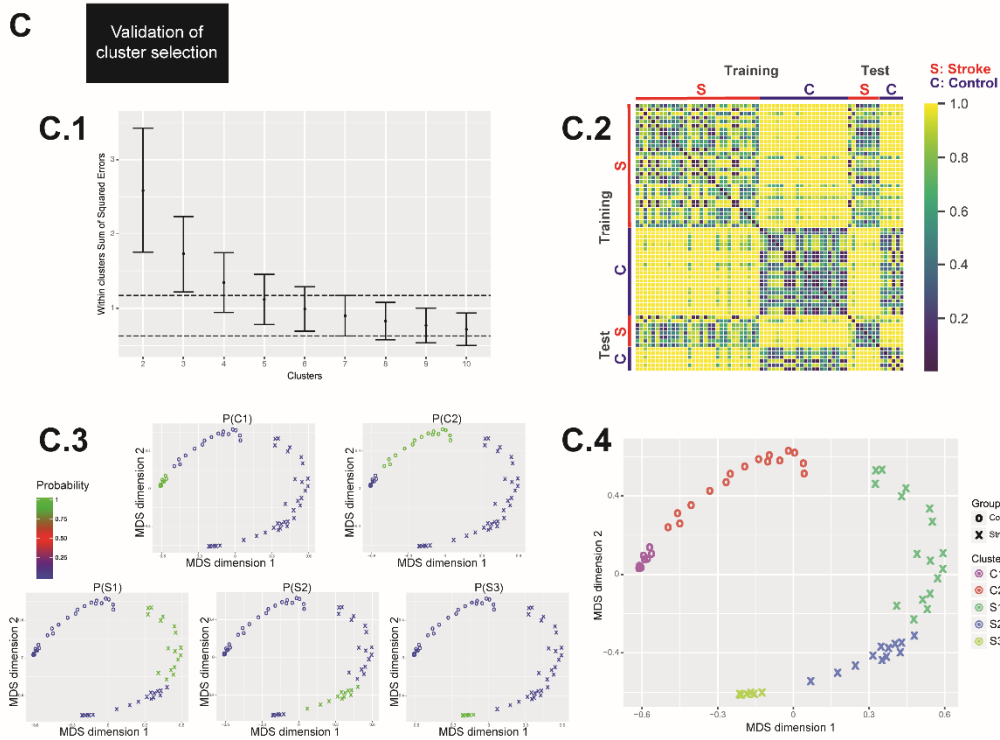
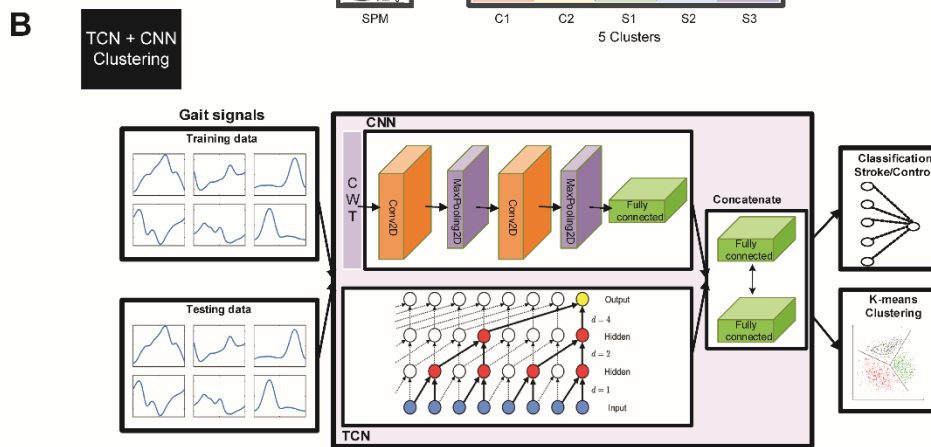
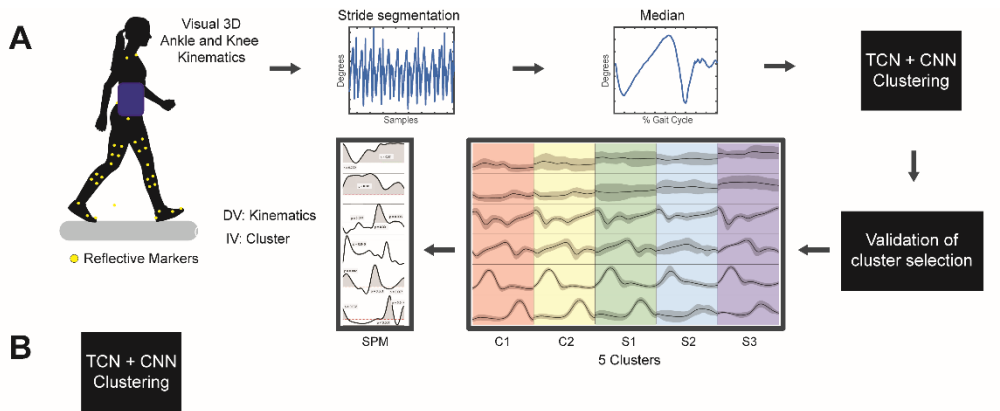
620 **Table 2:** Confusion matrix for individual blocks of Convolutional Neural Network (CNN),

621 Temporal Convolutional Network (TCN), dual-stage CNN-TCN and Dynamic Time Warping

622 clustering (dtwclust)

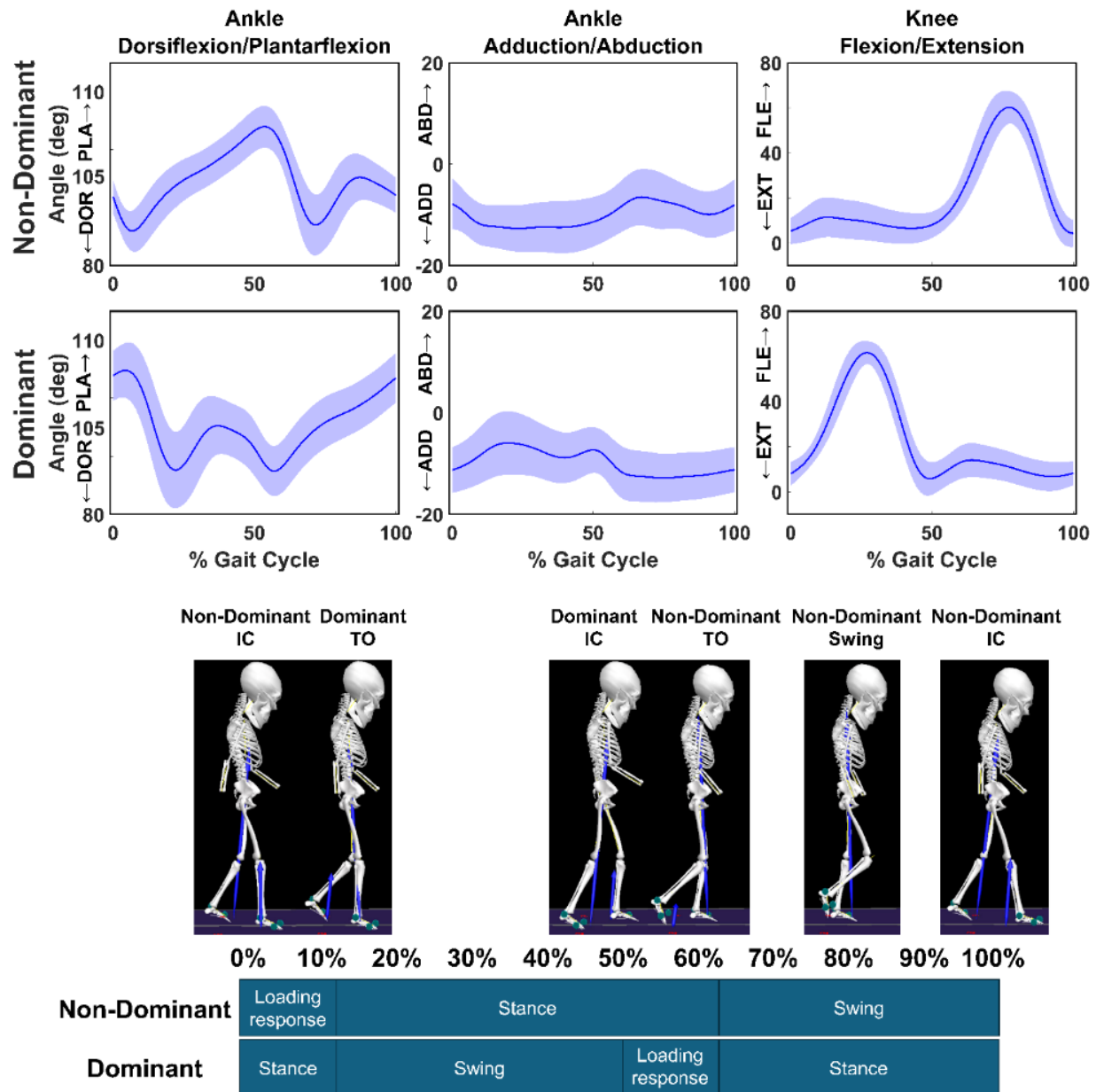
623

624 Figure 1: Study pipeline



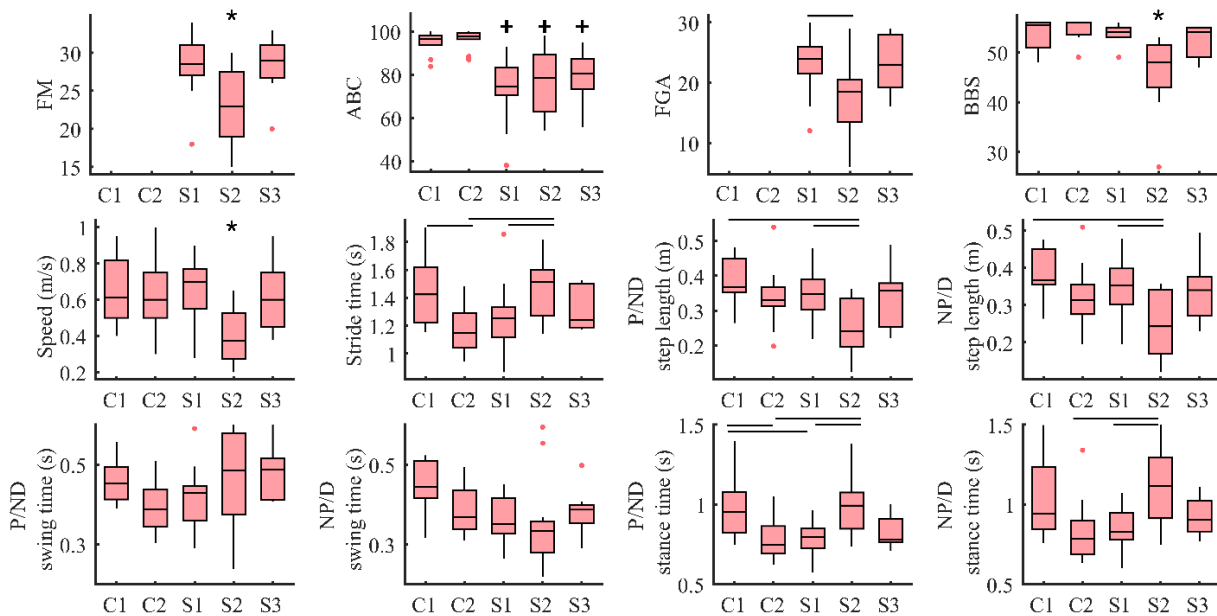
626 **Figure 1 A:** Study pipeline. We used a lower extremity marker set to derive joint-level
627 kinematics for the knee and ankle. We obtained an ensemble average of kinematics over the
628 gait cycle, and this time series data was fed into a Convolution Neural Network (CNN)-Temporal
629 Convolutional Network (TCN)⁵⁴, (Panel **B**) to obtain clusters of gait behaviors. We repeated the
630 process 10000 times to assess the cluster number and composition (Panel **C**). We then used 1-
631 D Statistical Parametric Mapping³⁵ to assess significant differences during the gait cycle
632 between clusters for each kinematic variable. **B:** Detailed machine learning pipeline. CWT:
633 Continuous Wavelet Transform. **C:** **C.1:** Optimal number of clusters using the one-standard
634 error rule. **C.2:** Matrix of dissimilarities between each of the individuals, 1 indicates never in the
635 same cluster, 0 always in the same cluster. **C.3:** Membership probability to each of the five
636 clusters for every individual, in a multidimensional scaling 2D latent space (MDS dimension 1,
637 MDS dimension 2) and a five-component Gaussian Mixture is computed.¹¹ **C.4:** A priori
638 labeling in the MDS space. O: Control; X: Post-stroke; C1 and C2 are the control groups; S1,
639 S2, and S3 are the post-stroke groups.

640 Figure 2: Normative gait cluster (C1)



641
642 **Figure 2** Gait kinematics of the normative walking cluster (C1) and corresponding gait phases
643 snapshots from Visual 3D. The cycle starts at the non-dominant initial contact (IC). TO: toe-off.

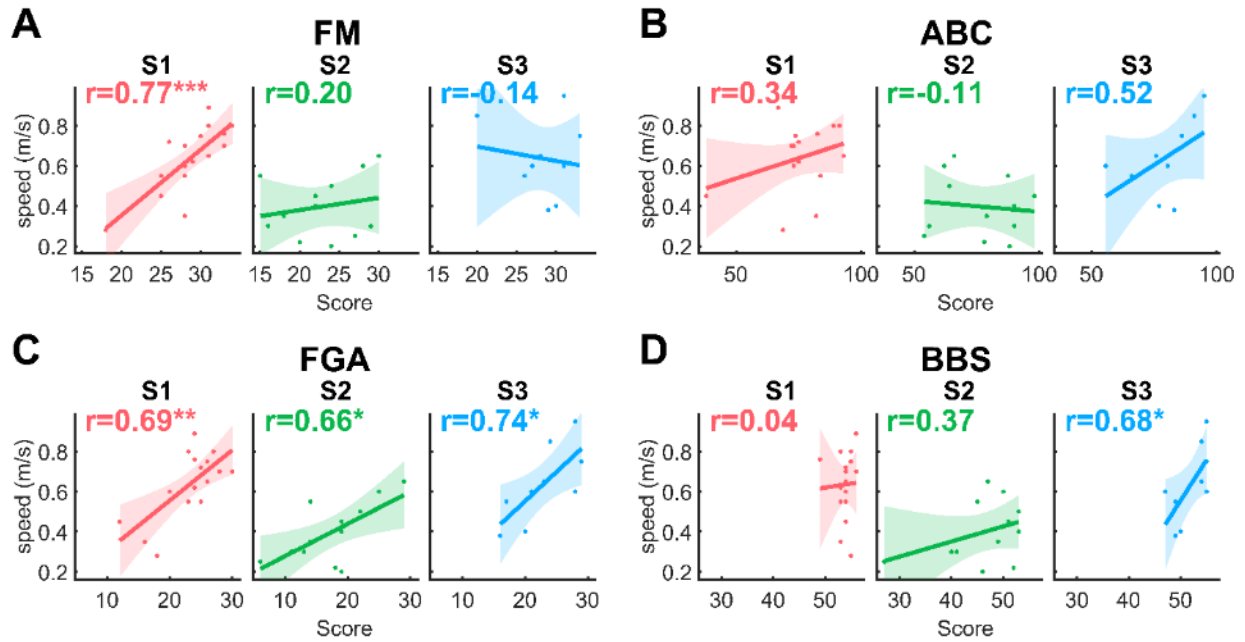
644 **Figure 3: Spatiotemporal and clinical**
645 **measures between clusters**



646
647 **Figure 3** Clinical assessments and gait spatiotemporal characteristics between the five clusters
648 (Controls: C1 and C2, Stroke: S1, S2, and S3). The non-dominant side for control individuals is
649 compared to the paretic side of post-stroke individuals, and dominant to paretic. One-way
650 ANOVA showed a difference for all parameters ($p < 0.05$), except paretic/non-dominant and non-
651 paretic/dominant swing times ($p = 0.574$ and $p = 0.078$ respectively). Tukey's test was used as
652 post-hoc. FM: Fugl-Meyer lower extremity, ABC: Activities Balance Confidence, FGA:
653 Functional Gait Assessment, BBS: Berg Balance Scale, P: Paretic, NP: Non-Paretic, D:
654 Dominant, ND: Non-Dominant. * lower than all the other clusters, + lower than C1 and C2, -
655 difference between two clusters. The significance level is set at $p < 0.05$.

657 **Figure 4** Post-hoc 1D-Statistical Parametric Mapping t-test with Bonferroni correction of joint kinematics for the median gait cycle
658 between the reference control cluster in blue (C1) and the other clusters in red (Controls: C2, Stroke: S1, S2, and S3). The non-
659 dominant side for control individuals is compared to the paretic side of post-stroke individuals, and dominant to paretic. The vertical
660 dashed lines surrounding a vertical arrow indicate endpoints of significant differences during the gait cycle.

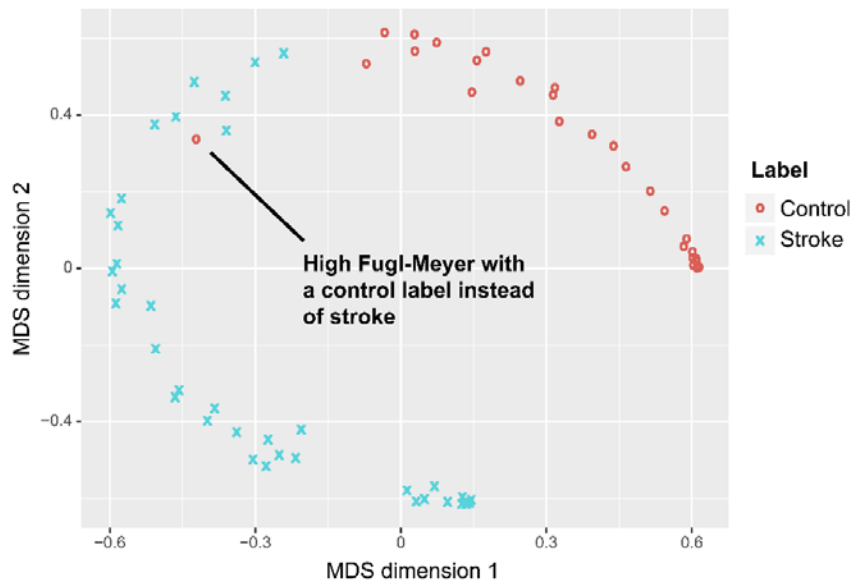
661 **Figure 5: Correlations**



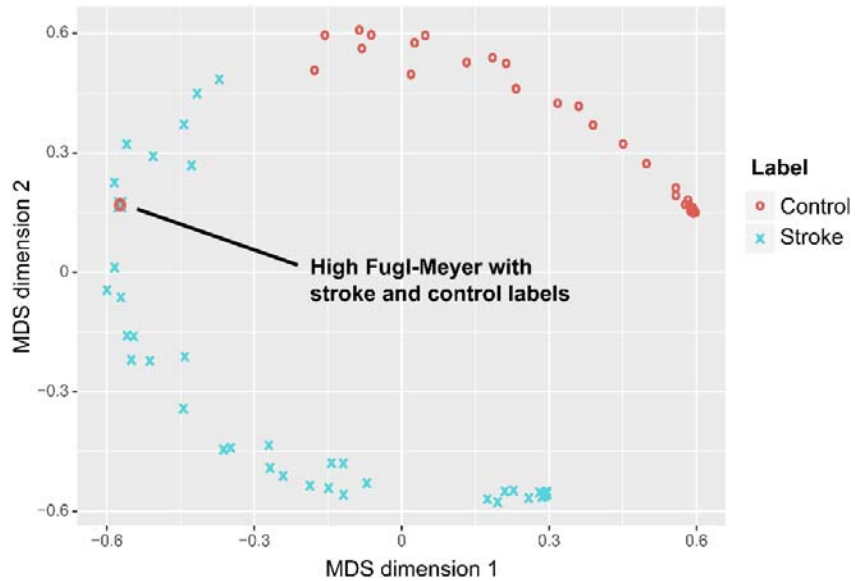
662

663 **Figure 5** Correlations between walking speed and clinical assessment scores within post-stroke
664 clusters (S1 in red, S2 in green, S3 in blue). FM: Fugl Meyer lower extremity, ABC: Activities
665 Balance Confidence, FGA: Functional Gait Assessment, BBS: Berg Balance Scale. The
666 significance level is set at $p < 0.05$. ***: $p < 0.001$, **: $p < 0.01$, *: $p < 0.05$

Mislabeling a stroke participant



Duplicating a stroke participant into a control

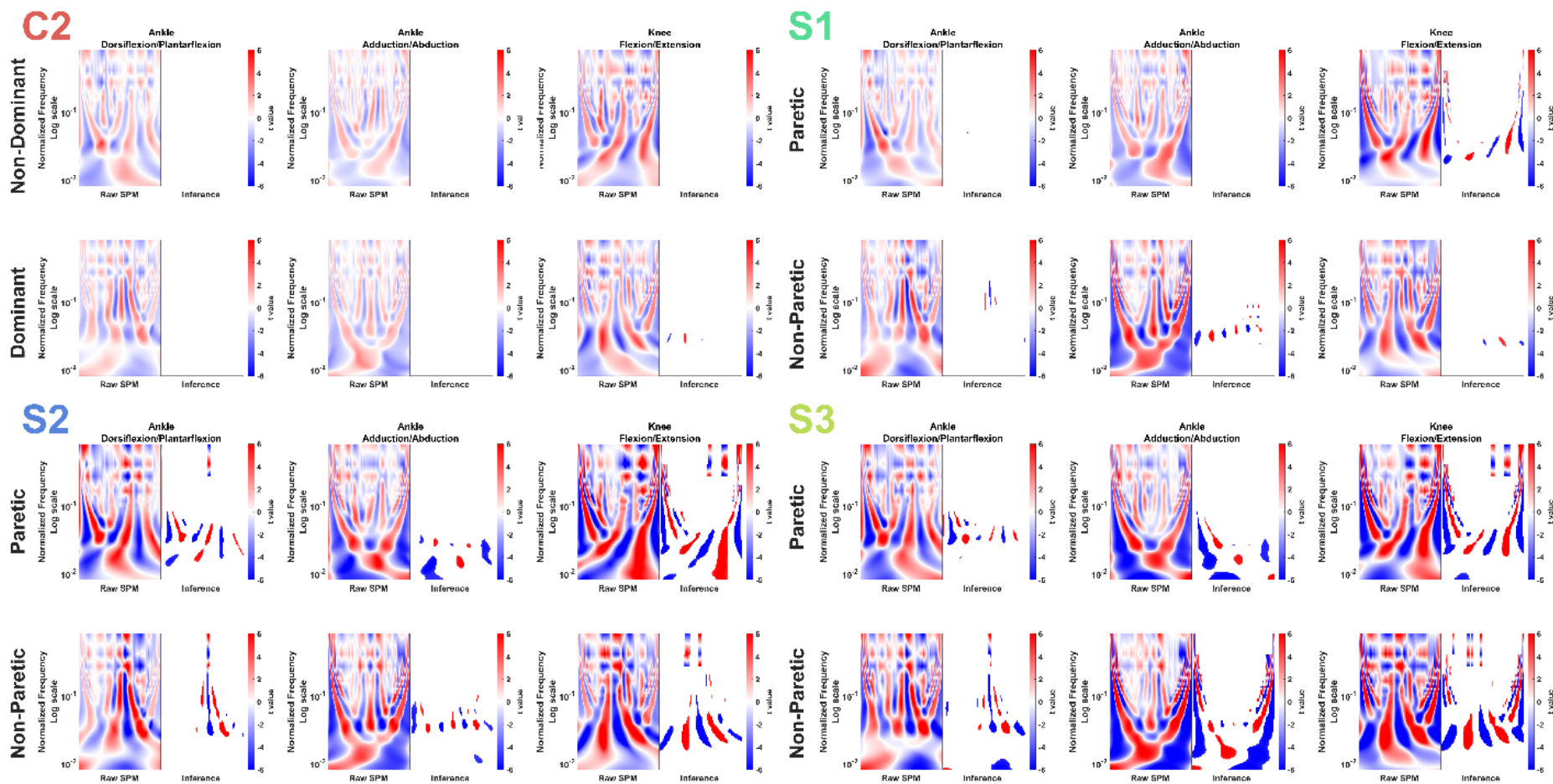


667 Supplementary materials 1

668

669 **Supplementary materials 1** Projection of each individual into the multidimensional scaling
670 latent space. When the highest Fugl-Meyer score participant is mislabeled as a control and
671 when we input this participant with a stroke and a control label, our pipeline still projects the
672 participant next to other people post-stroke.

Supplementary materials 2



676 **Supplementary materials 2** 2D-Statistical Parametric Mapping t-test of the continuous wavelet transform coefficient matrix between
677 the reference control cluster (C1) and the other clusters (Controls: C2, Stroke: S1, S2, and S3). The non-dominant side for control
678 individuals is compared to the paretic side of post-stroke individuals, and dominant to paretic. The zones displayed in each inference
679 panel indicate significant differences.

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