

# Theoretical Study of Anisotropic Carrier Mobility for Two-Dimensional Nb<sub>2</sub>Se<sub>9</sub> Material

You Kyoung Chung, Junho Lee, Weon-Gyu Lee, Dongchul Sung, Sudong Chae, Seungbae Oh, Kyung Hwan Choi, Bum Jun Kim, Jae-Young Choi,\* and Joonsuk Huh\*

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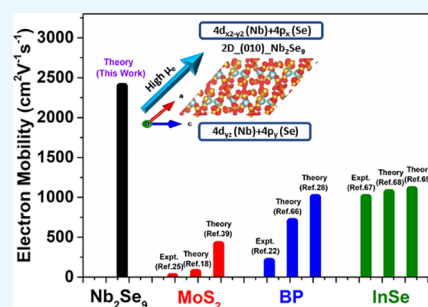
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**ABSTRACT:** Finding new materials with satisfying all the desired criteria for nanodevices is an extremely difficult work. Here, we introduce a novel Nb<sub>2</sub>Se<sub>9</sub> material as a promising candidate, capable of overcoming some physical limitations, such as a suitable band gap, high carrier mobility, and chemical stability. Unlike graphene, it has a noticeable band gap and no dangling bonds at surfaces that deteriorate transport properties, owing to its molecular chain structure. Using density functional theory (DFT) calculations with deformation potential (DP) theory, we find that the electron mobility of 2D Nb<sub>2</sub>Se<sub>9</sub> across the axis direction reaches up to  $2.56 \times 10^3 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  and is approximately 2.5–6 times higher than the mobility of other 2D materials, such as MoS<sub>2</sub>, black phosphorous, and InSe, at room temperature. Moreover, the mobility of 2D Nb<sub>2</sub>Se<sub>9</sub> is highly anisotropic ( $\mu_a/\mu_c \approx 6.5$ ). We demonstrate the potential of 2D Nb<sub>2</sub>Se<sub>9</sub> for applications in nanoscale electronic devices and, possibly, mid-infrared photodetectors.



## INTRODUCTION

Since the discovery of graphene in 2004,<sup>1</sup> successful isolation of individual atomic layers from bulk crystals using mechanical exfoliation has led to a considerable exploration of two-dimensional (2D) van der Waals (vdW) materials. The unique ballistic transport and extraordinarily high carrier mobility of graphene makes it suitable for various potential applications.<sup>2–10</sup> However, the major hurdle presented by its zero band gap motivates the exploration of other 2D vdW materials, including graphdiynes,<sup>11,12</sup> molybdenum disulfide (MoS<sub>2</sub>),<sup>13–19</sup> molybdenum diselenide (MoSe<sub>2</sub>),<sup>20</sup> tungsten disulfide (WS<sub>2</sub>),<sup>21</sup> and black phosphorous (BP),<sup>22–24</sup> as promising materials for field-effect transistors (FETs) and highly sensitive photodetectors. While these materials have shown great potential for a wide range of chemical and physical applications, some limitations, due to inherent weaknesses, still persist. For example, MoS<sub>2</sub> has a moderate band gap (1.3–1.8 eV) but exhibits one order of magnitude lower mobility than the theoretically predicted phonon-limited value ( $400 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ),<sup>25</sup> limiting its application in nanoelectronics. Phosphorene exhibits high carrier mobility ( $200\text{--}1000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ )<sup>26</sup> and has a band gap of 0.3–2.0 eV, depending on its thickness, and this widely tunable band gap is promising for near- and mid-infrared (IR) optoelectronics.<sup>27,28</sup> Despite these excellent intrinsic material qualities, its instability in ambient air presents a fundamental challenge for practical utilization.<sup>29,30</sup> Therefore, significant efforts have been devoted to exploring 2D materials that satisfy the fundamental properties (finite band gap, high mobility, good stability, and the absence of surface dangling bonds), providing compatibility with quasi-2D conducting

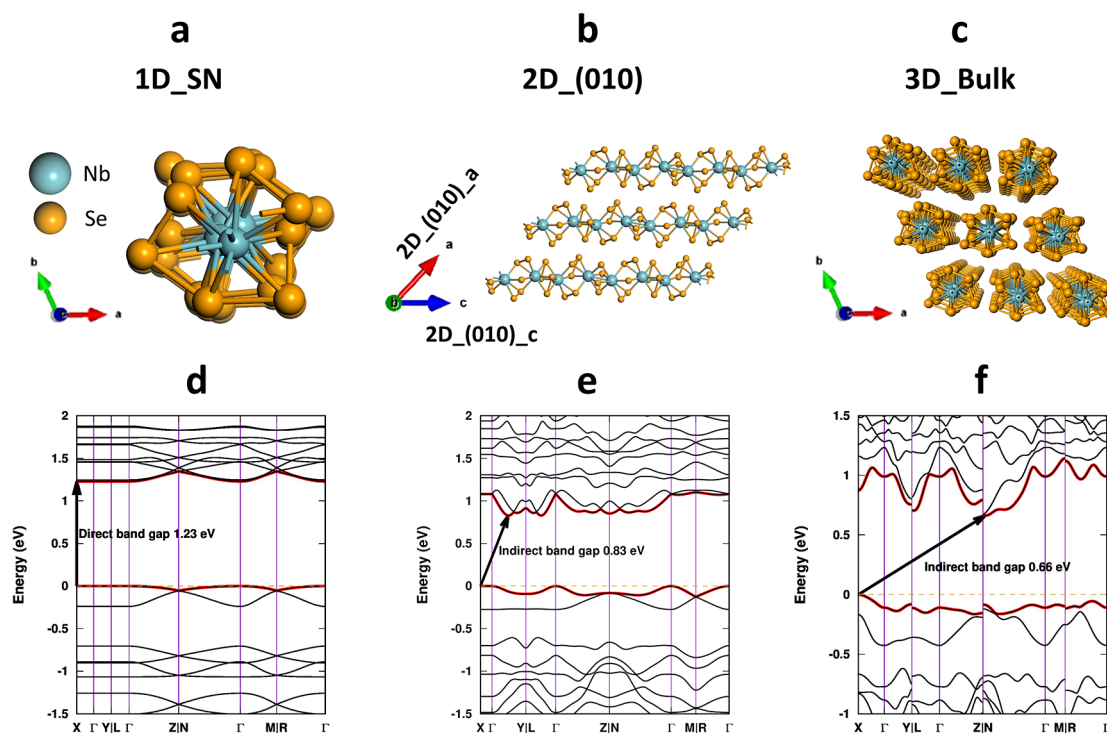
channels for future applications in nanoelectronics. Recently, a novel one-dimensional (1D) semiconducting Nb<sub>2</sub>Se<sub>9</sub> material was synthesized in bulk *via* simple vapor transport.<sup>31</sup> The as-grown, needle-like, single crystal Nb<sub>2</sub>Se<sub>9</sub> was formed by multiple single molecular chains coupled by weak vdW interactions,<sup>32,33</sup> and the experiment<sup>34,35</sup> showed that this bundle of chains could be easily separated by mechanical cleavage, as demonstrated by Novoselov *et al.*<sup>36</sup> The isolated Nb<sub>2</sub>Se<sub>9</sub> flakes exhibited a quasi-2D layered structure, eventually to the monolayer, with thicknesses controlled by the repeated peeling method. The monolayer was stable with the uniform width of less than 1 nm, even though the exfoliation and analysis processes were performed under atmospheric conditions.<sup>34</sup> Moreover, Nb<sub>2</sub>Se<sub>9</sub> nanowire was also stable in liquid exfoliation with various chemical environments such as water, PBS buffer solution, and organic solvents.<sup>35,37</sup> Therefore, it could be studied for the applications as a biomaterial<sup>38</sup> and an electrocatalyst.<sup>39</sup> With its characteristic molecular-chain structures, this Nb<sub>2</sub>Se<sub>9</sub> material has no surface dangling bonds that function as scattering centers,<sup>9</sup> adversely affecting carrier transport properties when downscaled to less than a few tens of nanometers. Moreover, our previous theoretical study showed that Nb<sub>2</sub>Se<sub>9</sub> materials, in 1D, 2D, and 3D structures,

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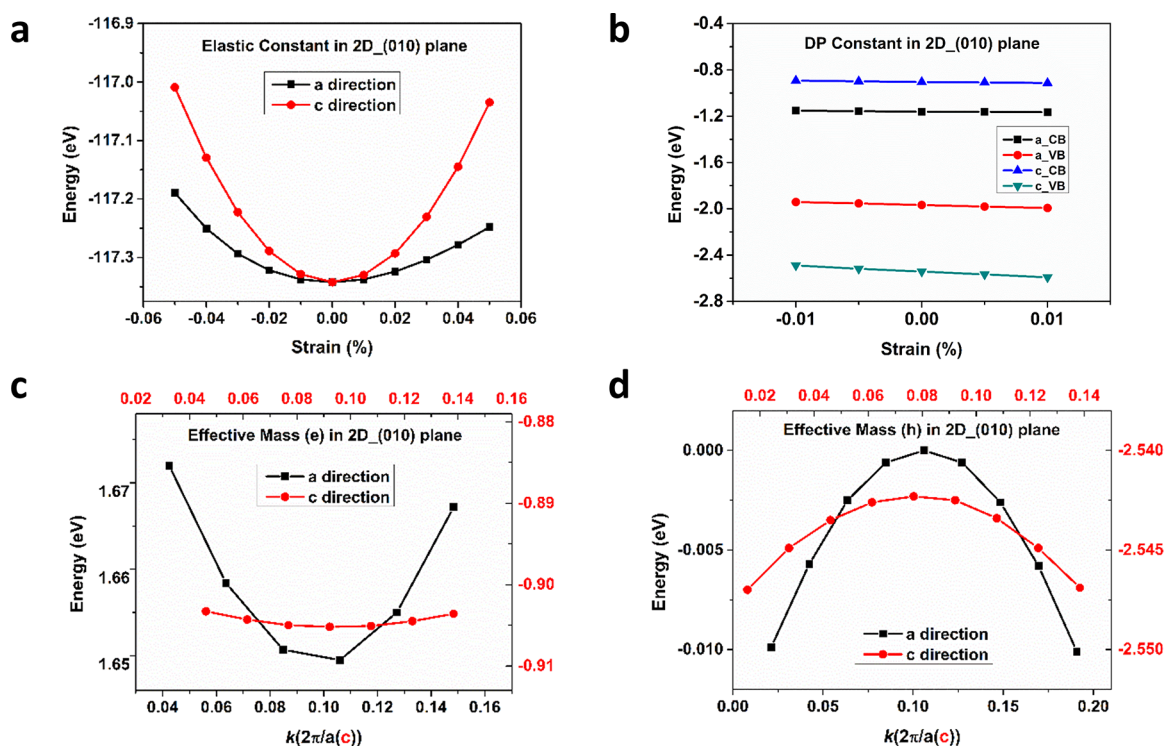
**Figure 1.** Atomic structures of the (a) 1D\_SN, (b) 2D\_(010) plane, and (c) 3D\_bulk  $\text{Nb}_2\text{Se}_9$  materials (gray and yellow spheres represent Nb and Se atoms, respectively). Electronic band structures of (d) 1D\_SN, (e) 2D\_(010) plane, and (f) 3D\_bulk  $\text{Nb}_2\text{Se}_9$  materials.

had nonzero band gaps in the range of 0.66–1.33 eV, depending on their structural dimensions, accompanied by an indirect-to-direct band gap transition from bulk crystal to single nanowire (SN) structures.<sup>40</sup> Additionally, high electron mobility is predicted, up to  $10^3 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  in 2D  $\text{Nb}_2\text{Se}_9$  materials, across the axis direction using density functional theory (DFT) calculations. Electron mobility of 2D  $\text{Nb}_2\text{Se}_9$  is highly anisotropic ( $\mu_a/\mu_c \approx 6.5$ ) and approximately 2.5–6 times higher than that of other 2D materials, such as  $\text{MoS}_2$ , BP, and InSe, at room temperature. In addition, 2D  $\text{Nb}_2\text{Se}_9$  has an appropriate band gap of 0.83 eV, important for telecommunication and solar energy harvesting applications.<sup>28</sup> These properties make  $\text{Nb}_2\text{Se}_9$  potentially useful for practical applications in transistors,<sup>41–44</sup> solar cells,<sup>23</sup> photodetectors,<sup>24</sup> and thermoelectric devices.<sup>45–47</sup> Our proposed novel  $\text{Nb}_2\text{Se}_9$  material is a promising candidate for overcoming the carrier transport deterioration commonly observed in 2D layered materials.

## ■ COMPUTATIONAL METHODS

**Numerical Methods on Mobility Anisotropy.** To understand the electronic and charge-transport properties of  $\text{Nb}_2\text{Se}_9$  with structural dimension, we calculated the intrinsic carrier mobility based on the deformation potential (DP) theory, proposed by Bardeen and Shockley<sup>48</sup> in the 1950s to describe charge transport in nonpolar semiconductors. In an inorganic semiconductor, electron coherence is close to the acoustic phonon wavelength, which is much longer than bond length. Thus, scattering of a thermal electron or hole arises mostly from the acoustic phonons. Since Tang *et al.*<sup>49</sup> calculated oligoacene mobilities using acoustic phonon scattering, the DP theory has been widely used to evaluate charge transport in 1D nanoribbons,<sup>11,12,18,19</sup> 2D materials,<sup>10,17,23,50</sup> and 3D materials such as deoxyribonucleic acid

stacks<sup>51</sup> and closely packed molecular crystals.<sup>52</sup> The DP approach can be simplified to an effective mass approximation, which we proved was valid for our system using a numerical derivation by Belezny *et al.*<sup>51,53</sup> In our theoretical calculations, the elastic modulus and effective mass were found to be anisotropic in the 2D layered structure. Thus, we investigated the essential factors of DP parameters (elastic constant, deformation constant, and effective mass), which primarily influence mobility anisotropy, by applying two different numerical equations. (Tables S1 and S2) One only includes the influence of effective mass on mobility anisotropy as presented below (eqs 2 and 3),<sup>54,55</sup> and the other embraces the anisotropic properties of all three DP parameters, using eqs 4 and 5 of the Supporting Information. This comparison exhibits no noticeable difference (less than 7%) for carrier mobilities calculated with the two different equations, so we determine that the different effective mass in each direction and deformation potential are essential factors, affecting the mobility anisotropy. In other words, the anisotropic carrier mobility of  $\text{Nb}_2\text{Se}_9$  material is determined by the complex influences of the three DP parameters, but anisotropy of the effective mass is more influential than that of the deformation potential. Therefore, we focused on the equations that apply the anisotropy of effective mass with the deformation potential fixed as an isotropic value for the 1D\_SN, 2D\_sheet, and 3D\_bulk structures on mobility anisotropy, using the equations denoted as each dimension of the structure and the carrier transport direction. For 1D\_SN, we only consider the main direction of the carrier movement as a nanowire direction, so the isotropic equation is applied to calculate the intrinsic carrier mobility. The following list of summarized equations employed for 1D\_SN (eq 1), 2D\_sheet (eqs 2 and 3), and 3D\_bulk structures (eqs 4 and 5, SI), using the DP approach to calculate the intrinsic carrier mobility:



**Figure 2.** DP parameters using the HSE06 DFT functional. (a) Total unit cell energies of the 2D\_(010) plane as a function of lattice deformation along the uniaxial direction (elastic constants can be obtained using a parabola fitting). (b) Shifts in the CBs and VBs of the 2D\_(010) plane under uniaxial strain along the *a* and *c* directions. (c, d) Energy-strain relationships for the electron and hole effective masses for 2D\_(010) along the (c) *a* and (d) *c* directions.

$$\mu_{1D\_c} = \frac{e\tau}{m^*} = \frac{e\hbar^2 C(1D\_c)}{(2\pi k_B T)^{1/2} |m_c^*|^{3/2} E_{1c}^2} \quad (1)$$

$$\mu_{2D\_a} = \frac{e\tau}{m^*} = \frac{e\hbar^3 C(2D\_a)}{k_B T |m_a^*|^{3/2} |m_c^*|^{1/2} E_{1a}^2} \quad (2)$$

$$\mu_{2D\_c} = \frac{e\tau}{m^*} = \frac{e\hbar^3 C(2D\_c)}{k_B T |m_a^*|^{1/2} |m_c^*|^{3/2} E_{1c}^2} \quad (3)$$

$$\mu_{3D\_c} = \frac{e\tau}{m^*} = \frac{2^{3/2} \pi^{1/2} e\hbar^4 C(3D\_c)}{3(k_B T)^{3/2} |m_a^*|^{1/2} |m_b^*|^{1/2} |m_c^*|^{3/2} E_{1c}^2} \quad (4)$$

where  $m^*$  is effective mass;  $\tau$  is relaxation time;  $T$  is temperature;  $E_1$  is the DP constant, which represents the strain-induced shift of the band edges; and  $C$  is the elastic modulus, attributed to simulation of lattice distortion by the strain. In anisotropic semiconductors, electrons and phonons behave differently in different directions, so the three-half exponent is applied to the directions in which an effective mass is expected to travel.

**DFT Calculations.** To obtain the intrinsic carrier mobility for 1D, 2D, and 3D Nb<sub>2</sub>Se<sub>9</sub> structures with mobility anisotropy, we conducted DFT calculations with the projector-augmented wave method,<sup>56</sup> implemented in the Vienna ab-initio simulation package (VASP).<sup>57</sup> The ionic and electronic relaxations were carried out with the Perdew–Burke–Ernzerhof (PBE) generalized gradient approximation (GGA).<sup>58</sup> We adopted Grimme’s DFT-D3 vdW corrections to include weak vdW interactions between Nb<sub>2</sub>Se<sub>9</sub> chains. A hybrid HSE06<sup>59</sup> DFT functional was used to verify more elaborate band structures, but no prominent difference was

found in mobility upon changes in structural dimensions. The energy cutoff was set to 520 eV. Gaussian smearing with Blöchl correction was used for geometry optimization, with a smearing width of 0.05 eV.

To describe the finite isolated nanowire, we placed nanowires in a triclinic unit cell with a vacuum spacing of 15 Å in the *x*- and *y*-directions to limit interwire interactions. The convergence criterion of the total energy in the self-consistent field iteration was 10<sup>−8</sup> eV, whereas the maximum force allowed on each atom was 0.01 eV/Å. In self-consistent potential and total energy calculations, the Brillouin zone was sampled by a 1 × 1 × 6 grid for 1D\_SN, 6 × 1 × 6 grid for the 2D\_(010) plane, and 6 × 6 × 6 grid for the 3D\_bulk in the  $\Gamma$ -centered automatic *k*-meshes scheme. The crystal orbital Hamiltonian population (COHP)<sup>60,61</sup> was used to analyze orbital energies and interactions between specific atoms.

## RESULTS AND DISCUSSION

**Geometry and Band Structure.** We performed DFT calculations to investigate atomic and electronic properties of Nb<sub>2</sub>Se<sub>9</sub> materials, as shown in Figure 1. The optimized geometries of the 1D\_SN, 2D\_(010) plane, and 3D\_bulk Nb<sub>2</sub>Se<sub>9</sub> materials are shown in Figure 1a–c. The unit cell of bulk Nb<sub>2</sub>Se<sub>9</sub> has 4 niobium (Nb) cations and 18 selenium (Se) anions, forming a chain structure. The inorganic bulk crystals of Nb<sub>2</sub>Se<sub>9</sub> are formed by strong bonds along the chain axis and weak interchain interactions across the chain axis. There are three distinct 2D sheets in the (010), (100), and (−101) planes, which can be formed by properly arranging 1D Nb<sub>2</sub>Se<sub>9</sub> chains, depending on the cutting planes of the bulk Nb<sub>2</sub>Se<sub>9</sub> structure.<sup>62</sup> We verified the stability of each plane by the phonon dispersion bands of the 2D-Nb<sub>2</sub>Se<sub>9</sub> structure (Figure



**Table 1. Various Parameters along the Lattice Constant (*a* or *c*) Direction for the 1D<sub>SN</sub>, 2D<sub>(010)</sub> Plane, and 3D<sub>bulk</sub> Structures of the vdW Nb<sub>2</sub>Se<sub>9</sub> Material, Calculated Using the PBE-D3 Functional (Numbers in Parenthesis Denote the Equation Number Used for Mobility Calculations)**

	<i>L</i> (Å)	carrier type	<i>C</i> <sub>1D</sub> (J/m)	<i>C</i> <sub>2D</sub> (N/m)	<i>C</i> <sub>3D</sub> (N/m <sup>2</sup> )	<i>E</i> <sub>1a</sub> (eV)	<i>E</i> <sub>1c</sub> (eV)	<i>m</i> <sub>a</sub> <sup>*</sup> ( <i>m</i> <sub>e</sub> )	<i>m</i> <sub>b</sub> <sup>*</sup> ( <i>m</i> <sub>e</sub> )	<i>m</i> <sub>c</sub> <sup>*</sup> ( <i>m</i> <sub>e</sub> )	<i>μ</i> (cm <sup>2</sup> V <sup>-1</sup> s <sup>-1</sup> )
1D <sub>c</sub> (eq 1)	13.0	e	2.61 × 10 <sup>-8</sup>				-1.19			1.22	4.19 × 10
		h	2.61 × 10 <sup>-8</sup>				-2.33			-4.49	0.25 × 10
2D <sub>a</sub> (eq 2)	8.2	e		14.8		-0.94		0.29		1.43	1.91 × 10 <sup>3</sup>
		h		14.8		-2.63		-1.35		-1.04	2.85 × 10
2D <sub>c</sub> (eq 2)	13.0	e		38.5			-1.72	0.29		1.43	3.01 × 10 <sup>2</sup>
		h		38.5			-4.97	-1.35		-1.04	2.69 × 10
3D <sub>c</sub> (eq 3)	13.2	e			9.58 × 10 <sup>10</sup>		-6.69	0.41	1.47	1.37	1.04 × 10 <sup>2</sup>
		h			9.58 × 10 <sup>10</sup>		-10.05	-1.25	-2.32	-0.43	1.19 × 10 <sup>2</sup>

**Table 2. Various Parameters along the Lattice Constant (*a* or *c*) Direction for the 1D<sub>SN</sub>, 2D<sub>(010)</sub> Plane and 3D<sub>bulk</sub> vdW Nb<sub>2</sub>Se<sub>9</sub> Materials, Calculated Using the Hybrid HSE06 Functional (Numbers in Parenthesis Denote the Equation Number Used for Mobility Calculations)**

	<i>L</i> (Å)	carrier type	<i>C</i> <sub>1D</sub> (J/m)	<i>C</i> <sub>2D</sub> (N/m)	<i>C</i> <sub>3D</sub> (N/m <sup>2</sup> )	<i>E</i> <sub>1a</sub> (eV)	<i>E</i> <sub>1c</sub> (eV)	<i>m</i> <sub>a</sub> <sup>*</sup> ( <i>m</i> <sub>e</sub> )	<i>m</i> <sub>b</sub> <sup>*</sup> ( <i>m</i> <sub>e</sub> )	<i>m</i> <sub>c</sub> <sup>*</sup> ( <i>m</i> <sub>e</sub> )	<i>μ</i> (cm <sup>2</sup> V <sup>-1</sup> s <sup>-1</sup> )
1D <sub>c</sub> (eq 1)	13.0	e	2.61 × 10 <sup>-8</sup>				1.06			1.56	5.94 × 10
		h	2.61 × 10 <sup>-8</sup>				-2.74			-6.64	0.10 × 10
2D <sub>a</sub> (eq 2)	8.2	e		14.8		-0.73		0.31		1.80	2.56 × 10 <sup>3</sup>
		h		14.8		-2.83		-1.44		-1.21	2.07 × 10
2D <sub>c</sub> (eq 2)	13.0	e		38.5			-1.30	0.31		1.80	3.60 × 10 <sup>2</sup>
		h		38.5			-5.06	-1.44		-1.21	2.03 × 10
3D <sub>c</sub> (eq .3)	13.2	e			9.58 × 10 <sup>10</sup>		-6.50	0.35	1.21	1.31	1.39 × 10 <sup>2</sup>
		h			9.58 × 10 <sup>10</sup>		-10.60	-1.16	-1.27	-0.51	1.18 × 10 <sup>2</sup>

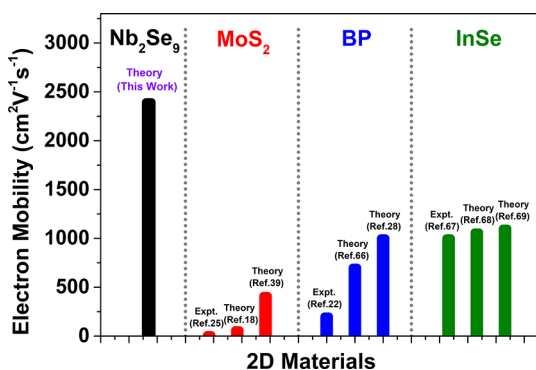
S1)<sup>62,63</sup> The (010) plane is the most stable, and the other planes have 0.21 eV higher energy than the plane (010). We chose the (010) plane for the 2D Nb<sub>2</sub>Se<sub>9</sub> sheets as the most stable structure, and the two directions (denoted as 2D<sub>(010)</sub><sub>a</sub> and 2D<sub>(010)</sub><sub>c</sub>) were considered for carrier mobility, as presented in Figure 1b. Electronic structures of the 1D<sub>SN</sub>, 2D<sub>(010)</sub> plane, and 3D<sub>bulk</sub> Nb<sub>2</sub>Se<sub>9</sub> materials are shown in Figure 1d–f, respectively. Compared to valleys of the valence band (VB) and conduction band (CB) in the 2D<sub>(010)</sub> plane and 3D<sub>bulk</sub>, those in 1D<sub>SN</sub> have broader, almost flat shapes, which reduce electron effective mass and mobility. The 2D<sub>sheets</sub> and 3D<sub>bulk</sub> Nb<sub>2</sub>Se<sub>9</sub> structures are indirect band gap semiconductors with band gaps of 0.83 and 0.66 eV, respectively. 1D<sub>SN</sub> has a 1.23 eV direct band gap at the X point, as determined by the PBE-D3 DFT functional, and the band gap of 3D<sub>bulk</sub> Nb<sub>2</sub>Se<sub>9</sub> structures is shifted to a larger band gap (1.43 eV) by the HSE06 hybrid functional (Figure S2). The indirect-to-direct band gap transition of Nb<sub>2</sub>Se<sub>9</sub> upon structural dimension renders this material suitable for FET applications.

**DP Constants.** In this study, we conducted DFT calculations based on the DP theory because we only considered the acoustic phonon scattering mechanism. The acoustic phonon wavelength is much longer than bond length in our Nb<sub>2</sub>Se<sub>9</sub> material. DP constants include the elastic constant (*C*), deformation constant (*E*<sub>1</sub>), and effective mass (*m*<sub>e</sub><sup>\*</sup>). The analytical methods used to obtain the DP constants for the 2D<sub>(010)</sub> plane of a Nb<sub>2</sub>Se<sub>9</sub> sheet are shown in Figure 2a–d. Figure 2a shows variations in total energy (*E*) with the uniaxial strain (*δ*) applied along the lattice directions (*a* and *c*) in the 2D<sub>(010)</sub> plane for a Nb<sub>2</sub>Se<sub>9</sub> sheet. The elastic modulus is defined as  $C_{2D} = [\partial^2 E / \partial \delta^2] / \Delta$ , where *E* is the total energy of the unit cell, *δ* is the uniaxial strain applied along the lattice direction, and  $\Delta = S/S_0$  describes the change in surface area at a dilation. The elastic constant *C* is obtained by parabola fitting

energy-strain curves, and the value of *C*<sub>3D</sub> in a 3D structure is obviously higher than that of *C*<sub>1D</sub> in a 1D structure. This implies that the elastic modulus is proportional to mobility. On the other hand, the elastic modulus of *C*<sub>2D</sub> in the 2D<sub>(010)</sub><sub>c</sub> direction is approximately 2.5 times greater than that of *C*<sub>2D</sub> in the 2D<sub>(010)</sub><sub>a</sub> direction. This shows the inverse relationship between elastic constant and carrier mobility, motivating us to evaluate other parameters associated with high carrier mobility. Figure 2b shows band edge shifts as a function of uniaxial strain. By dilating the lattice, we calculated the DP constant *E*<sub>1</sub> as  $dE/d\delta$ , which is equivalent to the slope of the fitting line with five points, where *E* is the energy of the CB edge for the electron and VB edge for the hole under uniaxial strain (*δ*) applied along the lattice direction. When the lattice is dilated, due to applied strain along the uniaxial direction, these energy band edges shift because of the interaction between the electrons (thermal energy) and acoustic modes (vibration).<sup>64</sup> Considering dilations in the longitudinal waves, carrier mobility is related to shifts in the CB and VB. For a Nb<sub>2</sub>Se<sub>9</sub> sheet, the VB edge energy is more deformed than the CB edge energy under strain, so hole mobility is expected to be lower than electron mobility. Figure 2c,d shows the energy-strain relationships along the lattice direction. The effective mass, *m*<sup>\*</sup>, is calculated using  $\hbar^2[\partial^2 \epsilon(k) / \partial k^2]^{-1}$ , where  $\epsilon(k)$  is the band energy at the minimum valley for the electron and maximum peak for the hole along the *k*-point. For parabolic bands, the electron will move much like a free particle with *m*<sup>\*</sup>, which results in constant effective masses. Using this parabolic approximation,<sup>65</sup> we see that the effective carrier masses are parabolic in the 2D<sub>(010)</sub> plane in each direction, allowing us to apply the DP theory in our calculations. Indicating that the effective mass is inversely proportional to band curvature, the more parabolic band shape for the 2D<sub>(010)</sub><sub>a</sub> direction is expected to have a smaller effective mass, contributing to its higher carrier mobility.

**Intrinsic Carrier Mobility.** Based on the obtained energy band spectrum using the VASP program, the acoustic-phonon-limited mobility at room temperature (300 K) was obtained with values  $E_b$ ,  $C$ , and  $m^*$ . The results are tabulated in Tables 1 and 2 for the PBE-D3 and the HSE06 DFT functionals, respectively. In our calculations, electron mobility in 1D and 2D structures is obviously higher than hole mobility, whereas electron mobility in the 3D structure is on nearly the same order of magnitude as hole mobility. Our results show that the  $\text{Nb}_2\text{Se}_9$  material exhibits high electron mobility, especially in the  $2\text{D}_{(010)}$  plane along the  $a$  direction, which is approximately 40 times higher than the 1D structure and highly anisotropic ( $\mu_a/\mu_c \approx 6.5$ ). This highly anisotropic electron mobility in the  $2\text{D}_{(010)}$   $a$  direction originates from the smaller DP constant ( $-0.94$  eV) and lower effective mass ( $0.31 m_e$ ), compared to the bigger DP constant ( $-2.63$  eV) and higher effective mass ( $0.80 m_e$ ) in the  $2\text{D}_{(010)}$   $c$  direction. In addition, the  $3\text{D}_{\text{bulk}}$  along  $a$  direction also shows the anisotropic electron mobility ( $\mu_a/\mu_c \approx 0.6$ ), using the PBE-D3 functional, as presented in Table S1. In particular, electron mobility in the  $2\text{D}_{(010)}$   $a$  plane reached  $2.56 \times 10^3 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$  (HSE06) using eq 2 and only showed a difference of less than 7% for carrier mobilities, calculated by eqs 4 and 5 of the Supporting Information. From this fact, we discover that effective mass and the deformation potential are more influential factors on mobility anisotropy in 1D, 2D, and 3D structures, even if carrier mobility, based on the DP theory, is determined by the complex interplay of three DP constants.

In Figure 3, the proposed 2D  $\text{Nb}_2\text{Se}_9$  material shows high carrier mobility compared to other 2D materials currently used



**Figure 3.** Electron mobilities of the  $\text{Nb}_2\text{Se}_9$  material compared to the most studied 2D materials.

in nanoelectronics. This graph clearly shows that the electron mobility of  $\text{Nb}_2\text{Se}_9$  in the  $2\text{D}_{(010)}$   $a$  direction is approximately six times higher than the highest mobility of  $\text{MoS}_2$  ( $10\text{--}400 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ),<sup>18,25,42</sup> 2.5 times higher than that of BP ( $200\text{--}1000 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ),<sup>22,28,66,67</sup> and 2.3 times higher than that of InSe ( $1000\text{--}1100 \text{ cm}^2 \text{ V}^{-1} \text{ s}^{-1}$ ).<sup>68–70</sup> Carrier mobility is an essential property for any semiconducting material, especially those used in FETs. Carrier density and mobility determine the controllable switching of conductance of a semiconducting channel in the operation of electronic devices.<sup>28</sup> So far, semiconductor devices have achieved improved performance,<sup>71,72</sup> reduced power consumption, and improved integration through scaling down. However, issues of carrier velocity saturation<sup>73,74</sup> and threshold voltage reduction still need to be addressed, owing to the reduction in channel length, which is a limiting factor for scaled down processes

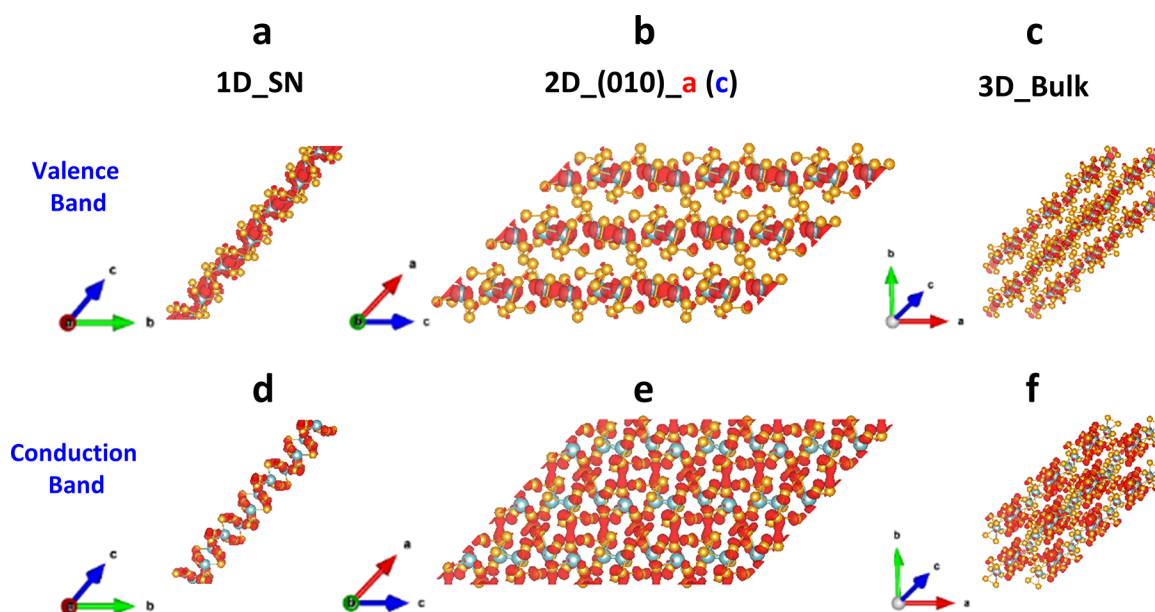
below 100 nm. Many problems have occurred, and various methods are being studied, though not in universal scaling. In the case of the proposed 2D  $\text{Nb}_2\text{Se}_9$  material, the structure is formed by 1D chains, eliminating dangling bonds at the surfaces, and providing high electron mobility. Therefore, given its characteristic properties, the proposed vdW  $\text{Nb}_2\text{Se}_9$  material is a potential alternative material, capable of solving the above-mentioned problems for nanoscale electronic devices.

**Partial Charge Density & Orbital Analysis.** The band-decomposed partial charge densities of the corresponding bands near the Fermi level of the  $\text{Nb}_2\text{Se}_9$  1D<sub>SN</sub>, 2D<sub>(010)</sub> plane, and 3D<sub>bulk</sub> structures are shown in Figure 4a–f. The iso-surface values of all charge densities are  $0.0015 e/a_0^3$  ( $a_0 = \text{Bohr radius}$ ). Charge density of the CB is much denser than that of the VB in the  $2\text{D}_{(010)}$  plane. In particular, bonding orbitals of Nb and Se atoms in CB for  $2\text{D}_{(010)}$  plane are more diffused, and the orbital overlaps are clearly delocalized compared to those of the 1D<sub>SN</sub> and 3D<sub>bulk</sub> forms, resulting in an electron mobility that is much higher than the hole mobility for the  $2\text{D}_{(010)}$  plane. The VB maximum (VBM) is located along the nanowire axis, and its charge distribution is primarily in the central region of the nanowire.

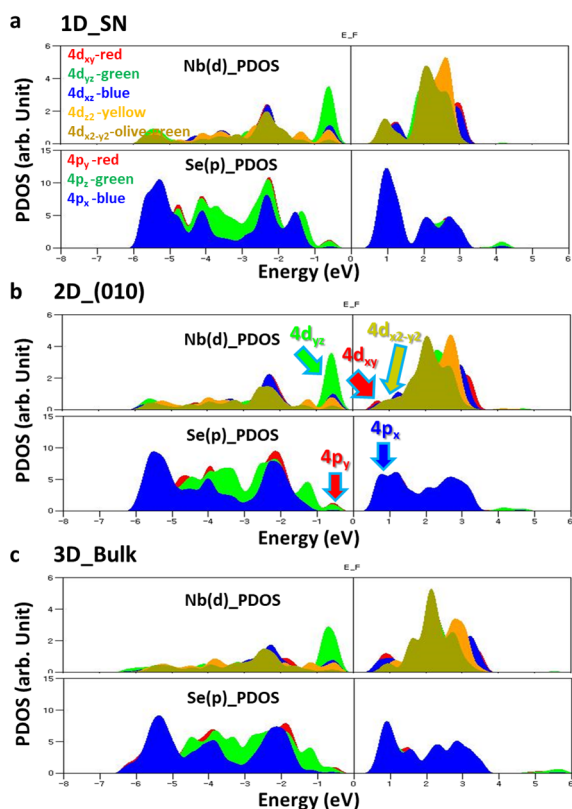
In addition, we investigated the projected density of states (PDOSs) of orbital for the 1D<sub>SN</sub>, 2D<sub>(010)</sub> plane, and 3D<sub>bulk</sub>  $\text{Nb}_2\text{Se}_9$  structures by re-extracting the atom-resolved information using the COHP curves implemented in the Local-Orbital-Basis Suite Toward Electronic-Structure Reconstruction (LOBSTER).<sup>75</sup> The orbital-PDOSs show primary charge contribution of the VB and CB. The contribution of the VB primarily originates from the  $d$  orbital of the Nb atoms; however, the  $p$  orbital of the Se atoms contributes to both the VB and CB. The dominant contributors are the Nb in-plane  $4d_{x^2-y^2}$  and out-of-plane  $4d_{xy}$  orbitals for the CB; the contribution of out-of-plane  $4d_{yz}$  orbitals is dominant for the VB of the 1D<sub>SN</sub>, 2D<sub>(010)</sub> plane, and 3D<sub>bulk</sub> structures, as shown in Figure 5a–c. Orbital contributions of Se atoms are primarily from the  $4p_x$  orbital in the CB for all structures, as presented in Figure 5a–c. In the CBM, Se  $p$  orbitals are dominant, and the  $2\text{D}_{(010)}$  plane has interchain  $\sigma$  bonds between Se  $p_x$  orbitals on one of the  $\text{Se}_5$  bridges and one of the Se octahedrons.<sup>62</sup> Therefore, the  $2\text{D}_{(010)}$  plane has a more delocalized distribution than the other structures, and the interchain interactions between the Selenium ions are strongest in the  $2\text{D}_{(010)}$  plane. The hybridization in the  $2\text{D}_{(010)}$  plane along the  $a$  direction is related to the non-covalent bonding, and it is weaker than the covalent bonding in the  $2\text{D}_{(010)}$  plane along the  $c$  direction. This weak hybridization makes the energy of VBM and CBM change smaller along  $a$  direction and induces the small deformation potential with less sensitivity to the applied strain. It enables the  $2\text{D}_{(010)}$  plane to have the high mobility along the  $a$  direction. Thus,  $\text{Nb}_2\text{Se}_9$  can be used as an appropriate material in nanoscale optoelectronic devices in the future.

## CONCLUSIONS

We proposed a 2D- $\text{Nb}_2\text{Se}_9$  material as a potential candidate for use in nanoelectronic devices. The needle-like single crystal  $\text{Nb}_2\text{Se}_9$  is composed of numerous single  $\text{Nb}_2\text{Se}_9$  chains linked by weak vdW interactions, and the chain bundles can be easily separated by mechanical cleavage. The proposed 1D, 2D, and 3D  $\text{Nb}_2\text{Se}_9$  structures are free from surface dangling bonds that hinder the transport properties of carriers when scaled down.



**Figure 4.** Side views of the band-decomposed partial charge densities of the (a, d) 1D<sub>SN</sub>, (b, e) 2D<sub>(010)</sub> plane, and (c, f) 3D<sub>bulk</sub> structures of Nb<sub>2</sub>Se<sub>9</sub> (upper panels (a–c) represent the VBs, whereas the lower panels (d–f) represent the CBs). Iso-surface values of all charge densities are 0.0015  $e/a_0^3$  ( $a_0$  = Bohr radius).



**Figure 5.** Orbital-PDOSs of the Nb<sub>4d</sub> and Se<sub>4p</sub> orbitals for the (a) 1D<sub>SN</sub>, (b) 2D<sub>(010)</sub> plane, and (c) 3D<sub>bulk</sub> Nb<sub>2</sub>Se<sub>9</sub> structures. (PDOSs of the 4d<sub>xy</sub>, 4d<sub>yz</sub>, 4d<sub>xz</sub>, 4d<sub>z<sup>2</sup></sub>, and 4d<sub>x<sup>2</sup>-y<sup>2</sup></sub> Nb orbitals are represented by red, green, blue, yellow, and olivegreen colors; contributions from the p<sub>x</sub>, p<sub>y</sub>, and p<sub>z</sub> Se orbitals are represented by blue, red, and green, respectively.)

The isolated Nb<sub>2</sub>Se<sub>9</sub> flakes exhibit a quasi-2D layered structure and are expected to be *p*-type semiconductors with a suitable band gap. Our transport study, based on the DP theory,

predicts that electron mobility in the 2D<sub>(010)</sub> plane along the *a* direction exhibits high values of  $2.40 \times 10^3$  (HSE06) and  $1.74 \times 10^3$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup> (PBE-D3), which are about 2.5–6 times higher than the highest mobilities achieved with other 2D materials, such as MoS<sub>2</sub>, BP, and InSe at room temperature. Applying the DP theory and an anisotropic numerical formula, the high electron mobility in the 2D<sub>(010)</sub><sub>*a*</sub> direction was found to originate from the smaller electron  $|E_1|$  and lower effective mass in the CB, which is induced by the weaker hybridization of non-covalent bond in the 2D<sub>(010)</sub><sub>*a*</sub> direction than that in the 2D<sub>(010)</sub><sub>*c*</sub> direction. We also show that electron mobility of the 2D monolayered Nb<sub>2</sub>Se<sub>9</sub> material is highly anisotropic ( $\mu_a/\mu_c \approx 6.5$ ), and the anisotropy of effective mass and the deformation potential are the governing factors of the mobility anisotropy. We expect the proposed dangling-bond-free vdW Nb<sub>2</sub>Se<sub>9</sub> material to be a suitable *p*-type semiconductor with high electron mobility and a nonzero band gap, with applications in optoelectronics, sensors, thermoelectric devices,<sup>76–79</sup> and, possibly, mid-infrared photodetectors.<sup>27,28</sup> However, the DP theory is based on the simplified approach so our results can give an upper limit for the mobility in Nb<sub>2</sub>Se<sub>9</sub> at room temperature. The more accurate quantitative description, including other possible scattering mechanisms,<sup>67,80–85</sup> requires a separate consideration.

## ■ ASSOCIATED CONTENT

### Supporting Information

The Supporting Information is available free of charge at <https://pubs.acs.org/doi/10.1021/acsomega.1c03728>.

Description of equations we applied for finding the primary factor that influenced the mobility anisotropy with the obtained values of various parameters for the vdW Nb<sub>2</sub>Se<sub>9</sub> material, calculated using the PBE-D3 and HSE06 functionals; phonon dispersion of 2D-Nb<sub>2</sub>Se<sub>9</sub>; band structure using HSE06 functional for 2D-Nb<sub>2</sub>Se<sub>9</sub>; PDOS for the 2D-Nb<sub>2</sub>Se<sub>9</sub> structure (PDF)



## AUTHOR INFORMATION

### Corresponding Authors

**Jae-Young Choi** – School of Advanced Materials Science and Engineering and School of Advanced Institute of Nanotechnology, Sungkyunkwan University, Suwon 16419, Republic of Korea; [orcid.org/0000-0003-1042-6171](https://orcid.org/0000-0003-1042-6171); Email: [jy.choi@skku.edu](mailto:jy.choi@skku.edu)

**Joonsuk Huh** – Department of Chemistry, School of Advanced Institute of Nanotechnology, and Institute of Quantum Biophysics, Sungkyunkwan University, Suwon 16419, Republic of Korea; [orcid.org/0000-0002-8792-5641](https://orcid.org/0000-0002-8792-5641); Email: [joonsukhuh@skku.edu](mailto:joonsukhuh@skku.edu)

### Authors

**You Kyoung Chung** – Department of Chemistry, Sungkyunkwan University, Suwon 16419, Republic of Korea

**Junho Lee** – Department of Chemistry, Sungkyunkwan University, Suwon 16419, Republic of Korea

**Weon-Gyu Lee** – Department of Chemistry, Sungkyunkwan University, Suwon 16419, Republic of Korea

**Dongchul Sung** – Department of Chemistry, Sungkyunkwan University, Suwon 16419, Republic of Korea

**Sudong Chae** – School of Advanced Materials Science and Engineering, Sungkyunkwan University, Suwon 16419, Republic of Korea

**Seungbae Oh** – School of Advanced Materials Science and Engineering, Sungkyunkwan University, Suwon 16419, Republic of Korea

**Kyung Hwan Choi** – School of Advanced Institute of Nanotechnology, Sungkyunkwan University, Suwon 16419, Republic of Korea

**Bum Jun Kim** – School of Advanced Institute of Nanotechnology, Sungkyunkwan University, Suwon 16419, Republic of Korea

Complete contact information is available at:

<https://pubs.acs.org/10.1021/acsomega.1c03728>

### Author Contributions

J.Y.C. and J.H. directed and designed the project. Y.K.C., W.G.L., J.L., and D.S. conducted the computational studies, analyzed the data, and prepared the manuscript. S.C., S.O., K.H.C., and B.J.K. carried out the experiments and analyzed the data. All the authors have commented on this paper.

### Notes

The authors declare no competing financial interest.

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## ABBREVIATIONS

2D, two dimensional; DFT, density functional theory; DP, deformation potential; vdW, van der Waals; MoS<sub>2</sub>, molybdenum disulfide; MoSe<sub>2</sub>, molybdenum diselenide; WS<sub>2</sub>, tungsten disulfide; BP, black phosphorous; FETs, field-effect transistors;

mid-IR, mid-infrared; 1D, one dimensional; SN, single nanowire; VASP, Vienna ab-initio simulation package; PBE, Perdew–Burke–Ernzerhof; GGA, generalized gradient approximation; HSE, Heyd–Scuseria–Ernzerhof; COHP, crystal orbital Hamiltonian population; VB, valence band; CB, conduction band; VBM, valence band maximum; CBM, conduction band minimum; LOBSTER, Local-Orbital-Basis Suite Toward Electronic-Structure Reconstruction

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