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Polytypism in superhard transition-metal triborides

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The quest of novel compounds with special structures and unusual functionalities continues to be a central challenge to modern materials science. Even though their exact structures have puzzled scientists for decades, superhard transition-metal borides (TMBs) have long been believed to exist only in simple crystal structures. Here, we report on a polytypic phenomenon in superhard WB₃ and MoB₃ with a series of energetically degenerate structures due to the random stacking of metal layers amongst the interlocking boron layers. Such polytypism can create a multiphase solid-solution compound with a large number of interfaces amongst different polytypes, and these interfaces will strongly hinder the interlayer sliding movement within each polytype, thereby further increase the hardness of this particular material. Furthermore, in contrast to the conventional knowledge that intrinsically strong chemical bonds in superhard materials should lead to high lattice thermal conductivity, the polytypic TMB₃ manifest anomalously low lattice thermal conductivity due to structural disorders and phonon folding. These findings promise to open a new avenue to searching for novel superhard materials with additional functionalities.

uperhard materials are technologically important in many applications, from reducing the wear of everyday objects to creating machining tools. The hardness of a material is usually measured by indenter techniques and is thus determined by how resistant the bonds in the material are against distortions and how dislocations are able to move in the system¹. A three-dimensional strong covalent network formed by carbon atoms makes diamond the hardest known material². To overcome the limitation of diamond to ineffectively cut ferrous metals, dense TMBs with high boron content (e.g., OsB₂, ReB₂, CrB₄, FeB₄, MnB₄)³⁻⁹ have been pursued. Implicit in such efforts is the assumption that dense TM atoms (creating high valence-electron density) prevent the structures from being squeezed while the high boron content (forming strong covalent B-B and TM-B network) withstands both elastic and plastic deformations, both of which enhance the hardness of materials. Amongst these TMBs, the highest boride of tungsten has currently become a focus of promising superhard materials because it combines ambient pressure synthesis, inexpensive raw materials with a measured superhardness (43.3-46.2 GPa under an applied load of 0.49 N)¹⁰⁻¹⁷. However, until recently, its structure has not been completely resolved. The heavy tungsten atoms hamper the accuracy to which the light boron atoms can be located by x-ray diffractions. Moreover, the versatile nature of boron atoms to form sp-, sp²-, and sp³-hybridized bonds brings about the coexistence of various phases. These technological challenges result in the structural and compositional uncertainties. Combining first-principles calculations with thermodynamics, the long assumed WB4 phase18 has recently been determined as a simple and stoichiometric WB₃ structure (called 2H)¹⁹. This conclusion has subsequently been substantiated by many theoretical and experimental studies^{20–26}. On the other hand, agreement is far from complete for WB₃. A theoretical study of WB₃ has suggested that the 2H structure is incompatible with experimental results (e.g., superhardness, normalized c/a ratio) and that the question of the crystal structure of samples must be reopened²⁷. In particular, an energetically more favorable WB₃ (called 3R) has been proposed²⁸. Hence, it is still unclear whether other phases are possible and what structural similarities may exist amongst these phases.

Since molybdenum is isoelectronic with tungsten, the crystal structure ambiguity for molybdenum borides is very much in parallel to that for tungsten borides. The highest boride of molybdenum was first reported as the MoB_4 phase²⁹ and later identified to be a triboride-based $Mo_{1-x}B_3$ structure³⁰, but it was recently proposed³¹ that



Figure 1 | **Structures of boron and metal layers.** (a) Overlap view of hexagonal boron (H) and metal layers (A) along the [001] direction. (b) Side views of boron (H) and metal layers (A, B, C) along the [110] direction. The honeycomb metal layer (A) can be derived from a close-packed metal layer by removing one third of the metal atoms (marked by the red plus sign "+"), and the B and C layers are actually identical to the A layer only shifted by translations of (2a/3, a/3) and (a/3, 2a/3), respectively. Here *a* is the lattice constant of its unit cell (shown by the black dashed lines). The small (green) and large (blue) spheres represent the boron and metal atoms, respectively.

MoB₄ should be the 2H-type MoB₃. Meanwhile, the 3R-type MoB₃ was theoretically presented³². It is therefore timely to elucidate the long-standing common mystery of this family of TMB₃ and, in particular, to provide the essential guidance in the design of superhard materials.

Results

Polytypism in TMB₃. The 2H (3R) structure adopts hexagonal (rhombohedral) symmetry with space group $P6_3/mmc$ (*R*-3*m*), in which boron and metal atoms locate at the Wyckoff 12*i* (18*f*) and 2*b*, 2*c* (6*c*) sites, respectively. As illustrated in Fig. 1, the boron atoms form planar graphitelike sheets (H). The metal atoms sit directly above the boron hexagons, skipping one column in every three, thus forming honeycomb metal layers (A). The B and C layers are actually identical to the A layer only displaced by one atom and two atoms, respectively. Accordingly, the stacking sequence AHBH (AHBHCH) well describes the 2H (3R) architecture, and both consist of identical units of substructure (AH), piled one on top of the other in different numbers and in different stacking sequences within the unit cells.

Superhard TMBs have long been believed to exist only in simple crystal structures, similar to 2H, 3R or other structure types, following the general idea in the design of superhard materials²⁻⁴. However, on the basis of the structure stacking principle mentioned above, we may reasonably infer that a very large number of polytypic structural modifications of TMB₃ can be built up using alternating metal and boron layers by systematically specifying the stacking sequence of metal layers. In these architectures, the stacking sequences of boron layers are completely the same. The differences amongst various structures, however, lie in the stacking sequences of metal layers. For the case with two metal layers in the unit cell, the only two stacking sequences (AB and AC) yield an equivalent hexagonal structure that is none other than the experimentally observed 2H form²⁵. Likewise, three metal layers comprise two orders (ABC and ACB) that produce a same rhombohedral framework. This framework is exactly the theoretically uncovered 3R structure^{28,32}. For four metal layers, the four stacking sequences (ABAC, ABCB, ACAB, and ACBC) equivalently create a previously unreported hexagonal configuration (called 4H). A complete list of previously unidentified structures (called 5H, 6H1, 6H2, 7H1, 7H2, 7H3, 8H1, 8H2, 8H3, $8H_4$, $8H_5$, and $8H_6$) comprising 5–8 metal layers in their unit cells can be constructed. In general, the TMB₃ crystals could be imagined to display one-dimensional disordered stacking of metal layers along the [001] direction. Therefore, polytypism is revealed to be the extra hidden degree of freedom in the structure design of superhard WB₃ and MoB₃ with a large number of polytypes due to the different stacking of metal layers amongst the interlocking boron layers.

Stability of TMB₃ polytypes. The thermodynamic stability of all those TMB₃ polytypes can be firmly proved for their viability from first-principles calculations (see Supplementary Information for details). Based on that, our work is able to systematically identify a set of new configurations that are energetically more favorable than the experimentally observed but metastable 2H structure. The calculated formation energies of fifteen TMB₃ polytypes are summarized in Fig. 2. In addition to the concrete values, the relative stability of different polytypes for WB₃ and MoB₃ has main features in common. The formation energy of the 2H structure is found to be the highest amongst the TMB₃ polytypes considered, though it is still negative $(-1.185 \text{ eV/f.u. for WB}_3 \text{ or }$ -1.256 eV/f.u. for MoB₃). This makes the 2H structure metastable but thermodynamically viable, which supports the experimental observation²⁵. Amongst these polytypes, the 3R type has the lowest formation energy (-1.222 eV/f.u. for WB₃ or -1.283 eV/f.u. for



Figure 2 | Formation energy versus the number of metal layers within the unit cell for (a) WB₃ and (b) MoB₃ polytypes. The formation energy, defined as $\Delta E = E(TMB_3) - E(TM) - 3E(B)$, is obtained from the first-principles calculations, referring to W and Mo in body-centered cubic phases and to B in α -B phase as their respective ground states. The red and black dashed lines indicate the lowest and highest energy values, with an energy distribution width as small as 37 meV (27 meV) per WB₃ (MoB₃) formula unit (f.u.), amongst all the calculated polytypes.



Figure 3 | Calculated bulk modulus *B*, shear modulus *G*, and Vickers hardness *H* versus the number of metal layers within the unit cell for WB₃ and MoB₃ polytypes. In (a)–(c) and (d)–(f), the same symbols denote the same WB₃ and MoB₃ polytypes, respectively.

 MoB_3) and becomes the ground state of TMB₃. Hence, the 2H and 3R structures are the extremes in formation energy governing the thermodynamic stability of these polytypes. It is interesting to note that the energy differences amongst polytypes are extremely small, and the maximum separation is as low as 0.037 eV/f.u. for WB₃ and 0.027 eV/f.u. for MoB₃. Considering the temperature effect on formation energy, such a small energy difference manifests polytypism in TMB₃ with a large class of energetically degenerate structures.

As a matter of fact, the newly identified TMB₃ structures can be envisaged as different mixtures of the 2H and 3R ones. In these layered crystals, the metal layers can be considered as being held together by the boron layers. In contrast to the classic layered materials (e.g., graphite, *h*-BN) that are characterized by weak interlayer interactions (e.g., Van der Waals), TMB₃ are dominated by strong intralayer B-B and interlayer TM-B covalent bonds^{22,28}. Stacking faults between the adjacent metal layers, say between AHB and AHC, basically do not alter the local environments of B-B and TM-B interactions and the energy difference amongst different stackings is very small. Hence, stacking faults, resulting from the intrinsic short-range behavior of strong covalent bonds, play a decisive role in the occurrence of polytypism in TMB₃.

The dynamic lattice stability of TMB₃ polytypes can also be supported through their phonon dispersion. For the 2H and 3R structures, the calculated phonon dispersion curves show no imaginary frequencies throughout the whole Brillouin zones, confirming the dynamic stability of both basic structures. Since other polytypes are viewed as different mixtures of 2H and 3R, the TMB₃ polytypes are deemed dynamically stable (see Supplementary Information for details).

Based on the published XRD patterns^{11,25} of the experimental samples, only the 2H structure can agree with them, since others polytypes cannot avoid introducing apparent additional peaks generated by tungsten layer which obviously disagrees with the experimental patterns. Although the newly identified structures are metastable with respect to the ground-state 3R phase, they are energetically more favorable than the experimentally synthesized 2H structure and are dynamically stable. Moreover, as mentioned above, the energy differences amongst various polytypes are extremely small. Considering the temperature effect, the newly identified TMB₃ polytypes should be viable. The temperature-dependent Gibbs free energies derived by Cheng *et al.*²⁵ has revealed that the 2H phase becomes more stable than the 3R phase above 659 K within the GGA method (above 678 K within the LDA method), which explains why the ground-state 3R phase has never been observed. Therefore, these results provide an extremely useful indication that the polytypic TMB₃ structures should be synthesized under appropriate conditions (e.g., at proper temperatures).

Mechanical properties of TMB₃ polytypes. We also evaluate the influence of different polytypic structures on mechanical properties of TMB₃. The obtained bulk modulus, shear modulus and Vickers hardness for fifteen TMB₃ structures are displayed in Fig. 3. The overall trends are very similar, even though mechanical properties of MoB₃ are slightly inferior to those of WB₃. Interestingly, their mechanical properties are hardly affected by the number of metal layers in their unit cells, and the differences amongst various polytypic structures are also very small. In particular, the estimated hardness values (38.0-38.9 GPa for WB₃ or 36.1–37 GPa for MoB₃) do not change much from the calculated data with the range of only 1 GPa, regardless of the polytypes stacking sequence. The results demonstrated that the intrinsic hardness of the TMB₃ polytypes mainly depends on the interaction between metal and boron layers. In these layered TMB₃ structures, the interlayer TM-B bonds are relatively weaker than the intralayer B-B bonds, although they are also strong bonds. This allows the layers to cleave readily under a large shear stress. It was verified by a theoretical study of the 2H structure that has the lowest indentation shear strength along the [110] direction under the (001) plane²⁷. Therefore, the sliding strength between layers largely limits the intrinsic hardness enhancement of the TMB₃ polytypes.

To further enhance the hardness, the relatively easy sliding of the layers under the large shear stress must be suppressed. As mentioned above, TMB_3 can form a variety of polytypic structures. Moreover, these structures have the nearly same energies. We thus propose that one can create a multiphase solid-solution compound with the coexistence of various polytypes. This particular material may include a large number of interfaces amongst different polytypic structures with different easy sliding directions, and these interfaces would strongly hinder the interlayer sliding movement of each polytype,



Figure 4 | (a) Low-frequency phonon dispersion curves along the [001] direction of the 2H and 4H polytypes for WB₃ and (b) Estimated room temperature lattice thermal conductivity along the [001] direction for WB₃ and MoB₃. In (a), the changes of Debye temperatures for acoustic modes are labeled.

accordingly allowing the possibility of an extrinsic hardness enhancement. A recent experiment¹⁵ showed that a greatly enhanced hardness was achieved when pure metals (e.g., Ta, Mn, Cr) were added to WB₃. In contrast to this traditional solid-solution of different compositional substances, the hardening way by creating a multiphase compound with various polytypes to restrict the propagation of dislocations does not change the chemical compositions of materials. Moreover, this mechanism is expected to be applicable to other systems. As a matter of fact, the ultrahigh strength (hardness) of the recently synthesized nano-twin Cu (*c*-BN) samples^{33,34} has already corroborated this. The nature of strengthening is the effective blockage of dislocation motion by numerous coherent boundaries, although the practical approaches of creating grain boundaries are different.

Thermal conductivity of TMB₃ polytypes. Such a class of special superhard materials own ultra-low thermal transport capability, completely opposite to the conventional knowledge that intrinsically strong chemical bonds in superhard materials would lead to high lattice thermal conductivity due to the inherently high bulk moduli and sound velocities. The polytypism in TMB₃ greatly influences lattice thermal conductivity κ_L along the [001] direction. As well understood, the acoustic part of phonons carries most of the heat in a material. The out-of-phase vibrations from a large number of randomly distributed atoms within the polytypism-enlarged unit cell, together with the inherently polytypism-induced interfaces, strongly scatter heat-carrying phonons. Meanwhile, as the number of metal layers in the unit cell increases, the Brillouin zone keeps "folding-in", and the Debye temperatures Θ_D and Debye frequencies ω_D of acoustic phonon modes decrease correspondingly³⁵. Figure 4(a) plots the phonon dispersions along the [001] direction for the 2H and 4H structures of WB₃. Since the Brillouin zone of 4H in this direction becomes smaller, the acoustic modes "hit" the Brillouin zone boundary much earlier than the phonons in 2H. Hence, ω_D s are greatly reduced from 4.4 THz and 3.8 THz for 2H to 2.7 THz and 2.0 THz for 4H for the longitudinal acoustic mode (LA) and transverse acoustic mode (TA), respectively. On the other hand, the sound velocities (5180 m/s and 6900 m/s) and Grüneisen parameters (1.37 and 1.74) for the TA and LA modes remain almost the same amongst the 2H, 3R, 4H and 5H polytypes. Given these parameters, the lattice thermal conductivity κ_L could be estimated via the Debye-Callaway method³⁶. The room temperature κ_L along the [001] direction with respect to the number of atoms in the unit cell is plotted in Fig. 4(b). It can be observed that κ_L decreases with increasing number of the random stacking layers, primarily due to the reduced Debye frequencies or Debye temperatures. Very low κ_L close to minimal might be achieved after several repetitions of units.

Such unusual ultra-low lattice thermal conductivity of TMB₃ is very unique and could be extremely useful in particular applications, such as one-dimensional thermal barrier with superhardness.

In summary, we show that polytypism exists in superhard WB_3 and MOB_3 with a large number of energetically degenerate structures due to the different stacking of metal layers amongst the interlocking boron layers. Although all the polytypic structures have nearly equivalently intrinsic hardness, such polytypism may create a multiphase solid-solution compound with a large number of interfaces amongst different polytypes, and these interfaces will strongly suppress the interlayer sliding movement of each polytype, accordingly allowing the possibility of an extrinsic hardness enhancement. Furthermore, the polytypic TMB₃ manifest extremely low lattice thermal conductivity due to structural disorders and phonon folding. Our findings shed light on the structure design of superhard materials and, at the same time, provide a new strategy in the search for superhard materials with additional functionalities.

Methods

Calculations on the basis of the density functional theory were carried out with the Vienna *Ab initio* Simulation Package (VASP) code³⁷ and the electron-ion interactions are described by means of projector augmented wave (PAW) with 5*d*⁴6*s*² (4*d*⁴5*s*²) and 2*s*²2*p*¹ electrons as valence for W (Mo) and B, respectively. The exchange-correlation functional within the generalized gradient approximation (GGA)³⁸ were employed. Because of the extremely small energy difference amongst different structures, a large cutoff energy of 500 eV and dense Monkhorst-Pack *k*-point meshes with a grid of 0.02 Å⁻¹ for Brillouin zone samplings were adopted to ensure the numerical convergence of formation energy differences to typically 1 meV/atom.

Having fully optimized fifteen specific polytypic structures for TMB₃, their formation energies (ΔE) at temperature T = 0 K were calculated. Bulk modulus (*B*) and shear modulus (*G*) are determined by the efficient strain energy method³⁹ while the intrinsic Vickers' hardness is estimated by Chen's model [$H = 2(k^2G)^{0.585} - 3, k = G/B$]^{40.41}. Also, the phonon dispersion curves and lattice thermal conductivities along the [001] direction for the 2H, 3R, 4H and 5H structures in WB₃ and MoB₃ were calculated. (see Supplementary Information for details).

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Author contributions

W.Q.Z. and Y.C.L. conceived the project; Y.C.L., J.Y., X.Y. and W.J.Q. performed theoretical calculations; Y.C.L., J.Y., X.Y., W.J.Q., Z.Z., J.H.Y. and W.Q.Z. analyzed results; Y.C.L., J.Y., W.Q.Z. and J.H.Y. wrote the paper. All contributed to the discussion of the results.

Additional information

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