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Cyclotron resonance in the high mobility GaAs/AlGaAs 2D electron system over the microwave, mm-wave, and terahertz- bands

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The reflected microwave power from the photo-excited high mobility GaAs/AlGaAs 2D device has been measured over the wide frequency band spanning from 30 to 330 GHz simultaneously along with diagonal magnetoresistance as a function of the magnetic field. Easily distinguishable resonances in the reflected power signal are observed at the same magnetic fields as a reduced amplitude in the Shubnikov-de Haas (SdH) oscillations of the diagonal magnetoresistance. The reflection resonances with concurrent amplitude reduction in SdH oscillations are correlated with cyclotron resonance induced by microwave, mm-wave, and terahertz photoexcitation. The magnetoplasma effect was also investigated. The results suggest a finite frequency zero-magnetic-field intercept, providing an estimate for the plasma frequency. The experimentally measured plasma frequency appears to be somewhat lower than the estimated plasma frequency for these Hall bars. The results, in sum, are consistent with an effective mass ratio of $m^*/m = 0.067$, the standard value, even in these high mobility GaAs/AlGaAs devices, at very large filling factors. Preliminary findings from this article have been published as conference proceedings, see Kriisa, A., *et al.*, *J. of Phys. Conf. Ser.* 864, 012057 (2017).

Two dimensional electron systems have constituted a remarkable arena for the development of condensed matter physics over, approximately, the last forty years¹. More recently, the study of novel emergent phenomena in the photo-excited transport properties of such low-dimensional systems have been a focus of interest²⁻⁷⁶. Emergence is found in systems that are far from equilibrium. Associated phenomena are characterized by complex behaviors that arise out of a multiplicity of basic interactions, and they can exhibit remarkable collective and cooperative aspects. It turns out that a high quality two-dimensional electron system based on GaAs/AlGaAs heterostructures subjected to modest constant microwave/mm-wave/terahertz photo-excitation at low temperature, for example, develops novel steady state non-equilibrium effects. Such non-equilibrium effects can be manifested in the transport properties of the photo-excited system as temperature and radiation-frequency dependent oscillatory changes in the electrical resistance as a function of the magnetic field, and the associated photo-excited oscillatory resistance minima evolve into novel radiation-induced zero-resistance states - zero-resistance states which are characterized by an absence of Hall quantization in a two dimensional electron system^{3-31,33-43,45,46}. The observations of photo-excited zero-resistance states and associated magnetoresistance oscillations has also brought with it new interest in the microwave/mm-wave/terahertz reflection, absorption, and transmission properties of the GaAs/AlGaAs 2D electron systems (2DES) at low magnetic fields, including the remote detection of the cyclotron resonance (CR), and the correlation of CR with magnetotransport¹⁰.

It is well known that the parabolic energy bands in 2D electronic systems, at finite magnetic fields, B , are split into quantized Landau levels, separated by cyclotron energy $\hbar\omega_c = \hbar \frac{eB}{m^*}$. Here, \hbar is the reduced Planck constant, ω_c is the cyclotron frequency, m^* is the effective mass, and e is the electron charge. Photo-excitation of this system with electromagnetic radiation leads to absorption of energy, i.e., to cyclotron resonance, if the photon energy equals the cyclotron energy, $hf = \hbar\omega_c$, where f is the photon frequency⁷⁷. Classically, one obtains the picture that

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the electrons undergo circular motion perpendicular to the magnetic field, in the plane of the 2DES, as the Lorentz force causes centripetal acceleration. The angular frequency of this circular motion $\omega = 2\pi f = qB/m^*$ is independent of the radius of the circular orbit and the electron velocity. Thus, when a circularly polarized electric field at frequency f , is applied at the electron cyclotron frequency, i.e., $2\pi f = \omega_c$, with the same sense of rotation as the electron orbit, the electron accelerates under the influence of the electric field of the radiation, which increases the electron velocity, leading to energy gain and a larger orbit radius without changing the frequency of cyclotron motion, until collisions lead to energy relaxation. Here, note that circular polarization in a sense opposite to the rotation of the electrons would not allow for the resonant acceleration and absorption of energy from the electromagnetic field, i.e., cyclotron resonance. Thus, cyclotron resonance under fixed orientation circularly polarized photo-excitation is observable only for one orientation of the magnetic field, the cyclotron resonance active orientation - the orientation for which the sense of circular polarization is the same as the cyclotron rotation of electrons. Cyclotron resonance is often viewed within the context of the so-called “Kohn’s theorem,” which states that electron-electron interactions do not modify the cyclotron frequency in a system characterized by translational invariance and parabolic dispersion relation⁷⁸. However, interactions in a disordered system are thought to modify the cyclotron frequency⁷⁹.

Typically, cyclotron resonance studies are carried out with circularly polarized radiation. However, cyclotron resonance is also observable under linearly polarized photo-excitation since linearly polarized radiation can be decomposed into a sum of cyclotron resonance active- and inactive- components. Since, after such decomposition, an active component will exist for both the normal and reverse magnetic field orientation, cyclotron resonance becomes possible and observable for both directions of the magnetic field under linearly polarized photoexcitation, unlike for circularly polarized photo-excitation. From the law for conservation of energy, the total incident irradiation energy that reaches the sample should equal the sum of the energy absorbed in the sample, the energy reflected back from the sample, and the energy transmitted through the sample. Thus, at cyclotron resonance, the resonant coupling between the 2DES and the electromagnetic radiation should be registered in the absorbed, reflected, and transmitted power signals. Here we examine cyclotron resonance in the electromagnetic wave signal reflected back from a high mobility GaAs/AlGaAs 2DES. In addition to collecting the reflected power signal as a function of the magnetic field at fixed photo-excitation energies, we simultaneously measured the diagonal magnetoresistance, R_{xx} in order to examine Shubnikov-de Haas oscillations in R_{xx} for concurrent signatures of cyclotron resonance. By utilizing the knowledge that cyclotron resonance is accompanied by resonant electron heating, we here take advantage of the high sensitivity of Shubnikov de Haas (SdH) oscillations to small increases in the electron temperature to identify the signature of cyclotron resonance in the SdH lineshape^{6,17,44}. The observed cyclotron resonance in the magnetoreflexion signal is compared with the cyclotron resonance signature in the Shubnikov de Haas oscillations, and the effective mass extracted from the two methods are reported and compared. The magnetoplasma effect was also investigated by plotting f^2 vs. B^2 . The results suggested a finite frequency zero-magnetic-field intercept, providing an estimate for the plasma frequency. The results are consistent with an effective mass ratio of $m^*/m = 0.067$, the standard value, even in these high mobility GaAs/AlGaAs devices.

Results

Figure 1 shows the experimental configuration where the samples are immersed in a liquid helium cryostat within a superconducting solenoid and irradiated with linearly polarized electromagnetic waves, through a waveguide.

Figure 2 shows a selection of reflected power signals measured at different frequencies in a GaAs/AlGaAs 2DES. As linearly polarized electromagnetic waves were used in these experiments, a resonance signal, attributable to cyclotron resonance, is seen on both sides, positive and negative, of the magnetic field axis. Easily distinguishable peaks/valleys, as seen in Fig. 2, appear at each measured frequency, from 36 GHz to 330 GHz. Resonance peaks/valleys in the reflected power signal were not observed for frequencies below 36 GHz. For each irradiation frequency, the measurement was conducted two times, once by sweeping the magnetic field in one direction, then a second time by sweeping in the opposite direction. Power signals were found to be identical for both sweeping directions. As seen in Fig. 2, the shape, symmetry, and even the direction of the tip of the resonance peak (up or down) varied from frequency to frequency. However, the location of resonance peak steadily shifted to higher magnetic field values with increasing frequency. Occasionally, the resonance orientation changed direction even within the same irradiation frequency over different sides of magnetic field, as for example for $f = 267$ GHz. The changing symmetry of the lineshape with the frequency appears reminiscent of the signature of a Fano-type resonance, where interference between a continuum and a resonant scattering process brings about an asymmetric line-shape⁸⁰. Further studies are being carried out to identify the origin of the lineshape observed in this reflection signal. The physical origin of the observed resonance peaks/valleys in the reflected power signal becomes clearer when the peak/valley positions in magnetic field are plotted as a function of microwave frequency f , as shown in Fig. 3. Resonance positions at positive and at negative magnetic field are plotted separately, so as to ascertain their symmetrical location along the B -axis. As would be expected for cyclotron resonance, resonance positions in magnetic field increase approximately linearly with increasing frequency throughout the examined frequency range. The location of the resonances in reflected power is found to be same on both sides of the magnetic field, as the slopes of linear fits through the data, $dB/df = 2.44 \pm 0.02$ mT/GHz for positive side and $dB/df = -2.46 \pm 0.01$ mT/GHz for negative side of magnetic field, agree to within experimental error. A feature of interest in Fig. 2 is that the resonances are rather broad in the magnetic field scale. This suggests a relatively short single particle lifetime for the carriers⁸¹.

In 2D electron systems, additional electrodynamic effects like plasma oscillations can noticeably shift the measured resonance response with respect to the cyclotron frequency^{51,59}. To find whether resonance peaks in this experiment were influenced by electron plasma oscillations, the peak positions shown in Fig. 3 are replotted along with data measured from the second sample on a quadratic scale, i.e. f^2 vs B^2 in Fig. 4 (black circles and red triangles, respectively). Each data point shown in Fig. 4 represents an absolute average of peak positions over the

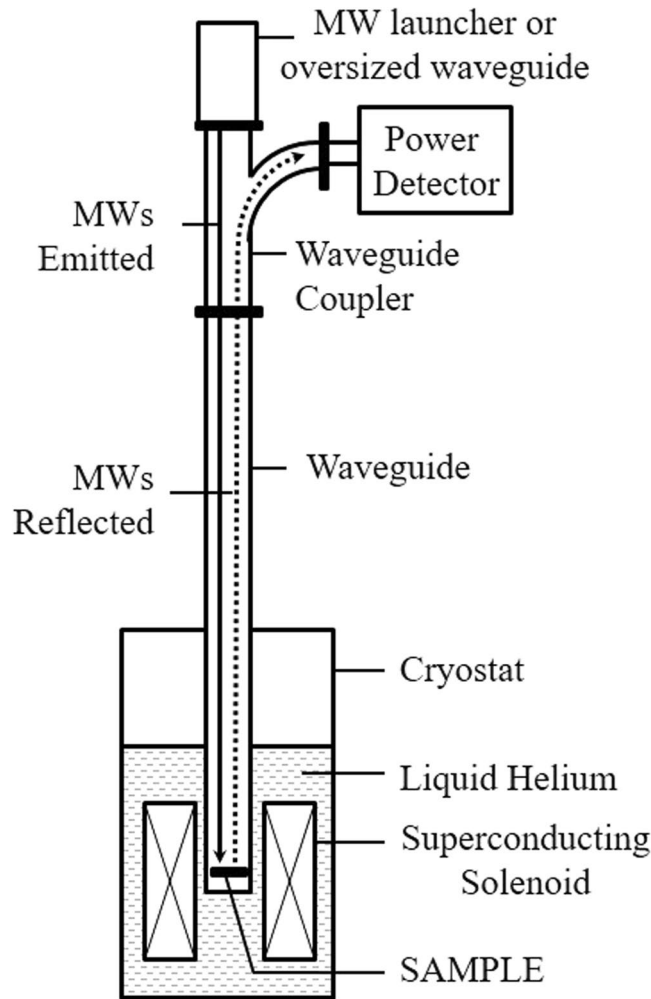


Figure 1. The experimental setup with a sample of 2D GaAs/AlGaAs submerged in the liquid helium cryostat within a superconducting solenoid. Solid line with an arrow indicates the path of the in-bound electromagnetic waves, while the dotted line heading in the opposite direction indicates the waves reflected back from the sample. Reflected waves are directed to the power detector with the waveguide coupler and read out with a power meter.

negative and the positive magnetic field sides. Hybridization of cyclotron resonance frequency, f_{CR} , and plasmon frequency, f_p , under magnetic fields perpendicular to 2DES, is described by the magnetoplasmon frequency, $f_{mp} = \sqrt{(f_{CR})^2 + (f_p)^2}$, where electrons in the plasma oscillate with frequency, $f_p = \sqrt{\frac{n_s e^2}{2\epsilon_{eff}\epsilon_0 m^*}} k$, where n_s is the electron density, e is the electron charge, ϵ_{eff} is the effective dielectric constant (for GaAs $\epsilon_{eff} = 6.9$)⁵¹, ϵ_0 is the permittivity of free space, m^* is the effective mass, and k is the plasmon wave vector. Often, the simple assumption of plasma confinement $k \approx \pi/W$ is made, where width of sample, W , is half the plasmon wavelength⁵¹. With this assumption, we find the estimate $f_p(n_s \approx 2.4 \times 10^{11} \text{ cm}^{-2}) = 57.3 \text{ GHz}$ and $f_p(n_s \approx 3.3 \times 10^{11} \text{ cm}^{-2}) = 67.2 \text{ GHz}$ for the two samples. These calculated values are much higher than the plasmon frequencies $f_p(n_s \approx 2.4 \times 10^{11} \text{ cm}^{-2}) = 23.8 \pm 14.8 \text{ GHz}$ (black) and $f_p(n_s \approx 3.3 \times 10^{11} \text{ cm}^{-2}) = 36.2 \pm 13.2 \text{ GHz}$ (black) extracted directly from the experimental data, i.e. from square root of the intercept of linear fit through the data in Fig. 4. It seems that the theoretical model used here does not adequately describe the experimental findings, as resonance peaks in the reflected power signal are observed below 57.3 GHz for both samples, all the way down to 36 GHz. We do not believe that the difference between theoretical and experimentally found values of f_p could be explained with the presence of retardation effects, as the dimensionless retardation parameter $\alpha \approx 0.29 \sqrt{n_s [10^{11} \text{ cm}^{-2}]} \times W [\text{mm}] \approx 0.2$ for our samples⁵⁹. Retardation effects start influencing magnetotransport only once retardation parameter approaches unity, i.e. when the velocity of 2D plasmons approach the velocity of light⁵⁹.

In Fig. 4, the slopes of the linear fit $d(B)^2/d(f_{MW})^2 = (e/2\pi m^*)^2$, give the effective mass $m^* = (0.0670 \pm 0.0003) m_0$ (black) and $m^* = (0.0677 \pm 0.0004) m_0$ (red), where m_0 is the free electron mass. These values for m^* agree, to within experimental error, with the most frequently quoted $m^* = 0.067 m_0$ for GaAs/AlGaAs devices. However, the observed effective mass ratio in these measurements exceeds the value extracted from the study of the radiation-induced magnetoresistance oscillations in similar materials⁵.

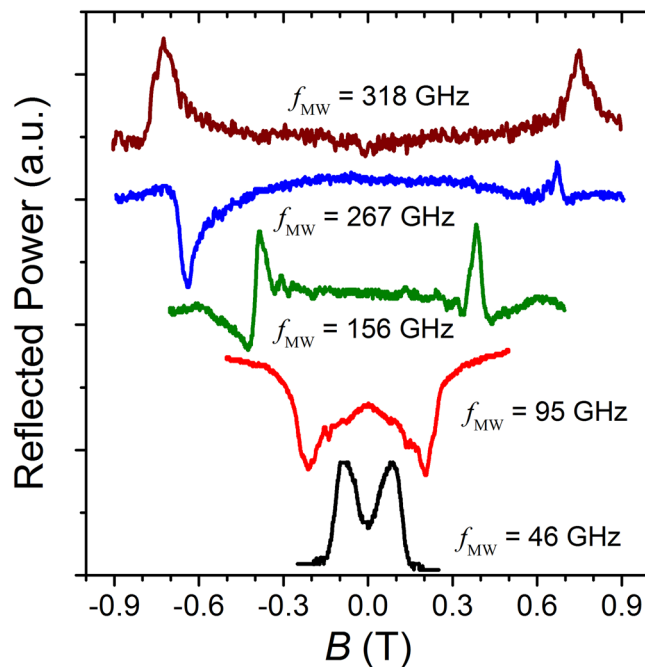


Figure 2. The reflected power signals as a function of the magnetic field measured with different mm-wave and terahertz electromagnetic wave frequencies, f , show strong resonances in the GaAs/AlGaAs 2DES heterostructures at temperature $T = 1.7$ K.

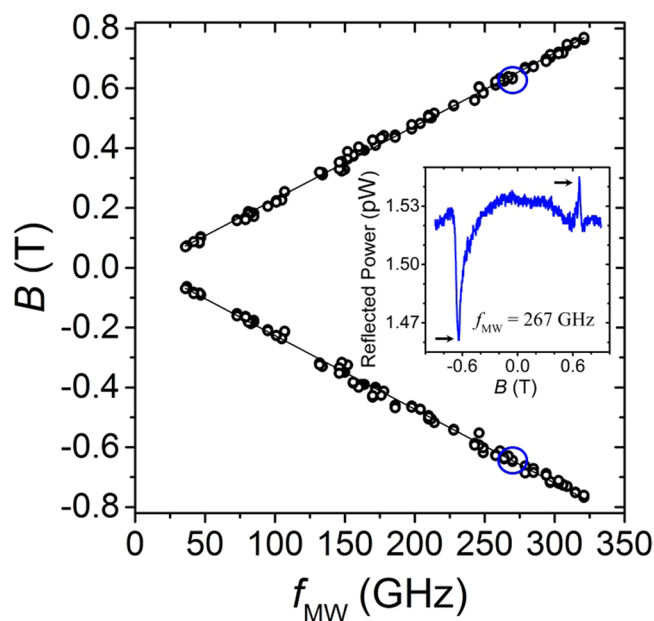


Figure 3. Reflected power resonance positions in magnetic field as a function of microwave frequency f in the GaAs/AlGaAs 2DES. Black lines are linear fits through the data points. The slope values, found from linear fits through both the positive and negative magnetic field data, agree to within experimental error. Inset: arrows point to peaks observed in reflected power measured at frequency $f = 267$ GHz and correspond to data points located inside blue circles in main graph.

In addition to measuring the reflected power signal, we concurrently measured the diagonal resistance, R_{xx} , in our samples. Figure 5 plots the normalized reflected power (right ordinate) along with R_{xx} (left ordinate) as a function of magnetic field at microwave frequency, $f = 267$ GHz. Above $|B| = 0.3$, the resistance signal shows regular SdH oscillations, with apparent reduction in oscillations between $|B| \approx 0.60$ T and $|B| \approx 0.70$ T. These disturbances in SdH oscillation amplitude were observed only under irradiation, suggesting that the location of changes in

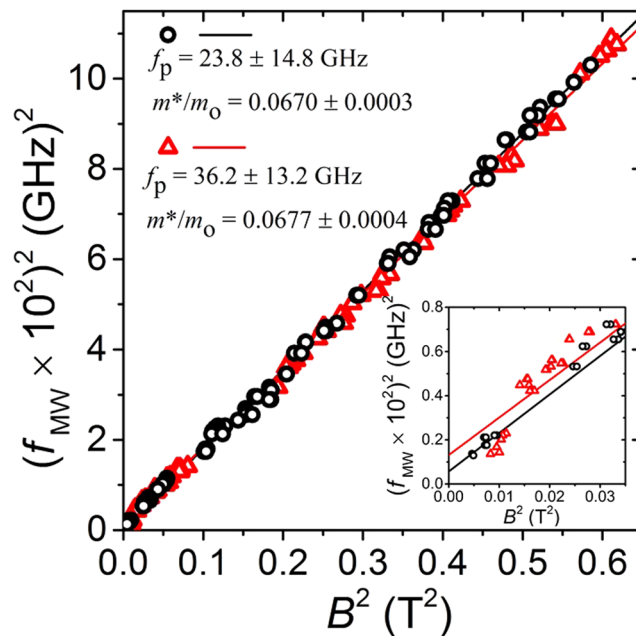


Figure 4. This figure compares the resonance peak locations in the reflected power measured in two different samples, plotted as f^2 vs B^2 . Black circles and red triangles correspond to data measured in samples with density $n_s \approx 2.4 \times 10^{11} \text{ cm}^{-2}$ (data replotted from Fig. 3) and $n_s \approx 3.3 \times 10^{11} \text{ cm}^{-2}$, respectively. Effective mass ratios, m^*/m , are found from slopes of linear fit through the data, while plasmon frequencies, f_p , are found from the square root of the intercept. Inset: close-up of main graph near the origin.

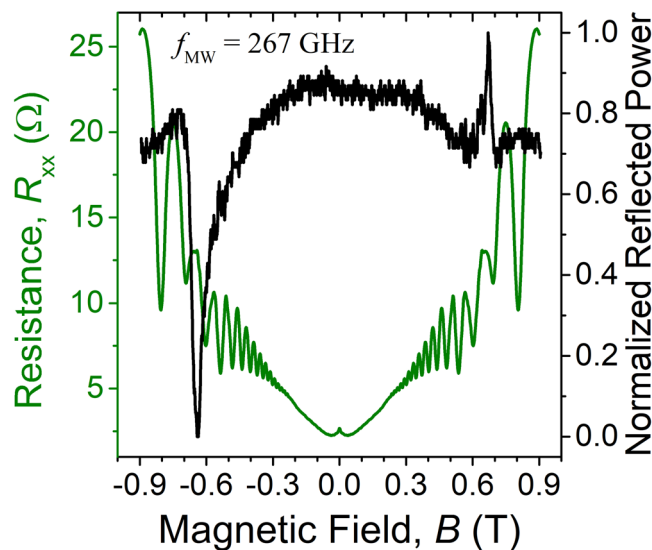


Figure 5. Reflected power (right ordinate) and the diagonal resistance, R_{xx} , (left ordinate) as a function of magnetic field, B , measured in a GaAs/AlGaAs 2DES heterostructure at temperature $T = 1.7 \text{ K}$ and frequency $f = 267 \text{ GHz}$. The coexisting resonances seen in both signals, peaks in reflected power at $|B| = 0.654 \pm 0.015 \text{ T}$, and the change to SdH oscillations between $|B| \approx 0.60 \text{ T}$ and $|B| \approx 0.70 \text{ T}$, point out the same underlying physical phenomenon: cyclotron or magnetoplasmon resonance.

oscillations point to the location of the cyclotron resonance⁶. We also notice in Fig. 5, that the disturbance in SdH oscillations coincides with the location of the resonance peaks at $|B| = 0.654 \pm 0.015 \text{ T}$ in the reflected power signal.

Locating resonant heating in SdH oscillations with high accuracy can be difficult, as they can spread over a wide span of magnetic fields. We circumvent this problem by calculating the derivative of diagonal resistance, dR_{xx}/dB , and plotting it as a function of magnetic field, as shown in Fig. 6. Drawing the upper and lower envelopes (red line) to the boundaries of dR_{xx}/dB then aids in pinpointing the strongest change to the SdH oscillations, i.e. the average magnetic field location of the upper minimum and lower maximum envelope ($|B| = 0.640 \pm 0.005 \text{ T}$

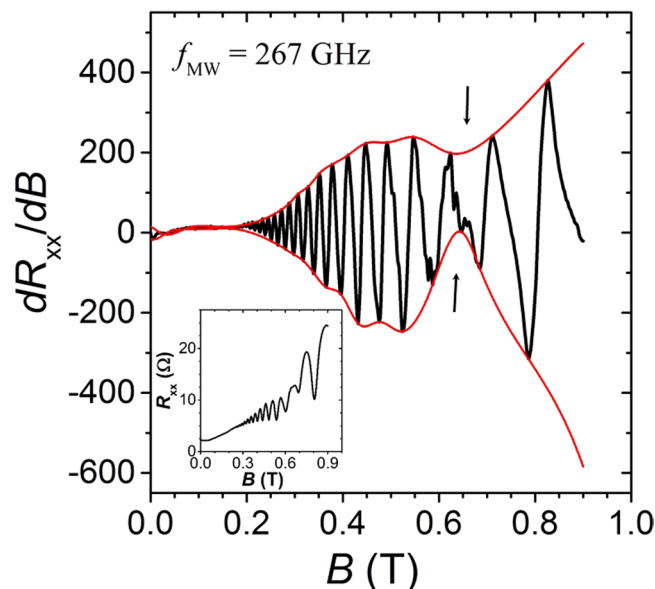


Figure 6. Derivative of diagonal resistance, dR_{xx}/dB , as a function of magnetic field B in a GaAs/AlGaAs 2DES heterostructure at temperature $T = 1.7$ K and frequency $f = 267$ GHz. Red lines show envelopes drawn to the upper and lower bounds of dR_{xx}/dB . Arrows point to the strongest change to SdH oscillations at $B = 0.640 \pm 0.005$ T, found as an average of the upper envelope minimum at 0.636 T and the lower envelope maximum at 0.643 T. Inset: resistance signal, R_{xx} , averaged over the positive and negative sides of the magnetic field, before calculating the derivative of the diagonal resistance, dR_{xx}/dB in the main graph.

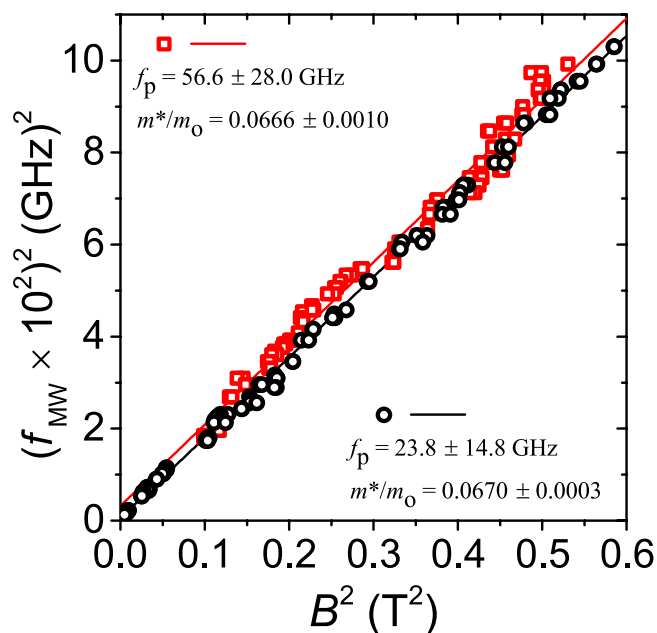


Figure 7. Comparison of resonance peak locations in reflected power (black circles, data also shown in Fig. 4) and in Shubnikov de Haas oscillations in the resistance signal (red squares), plotted on quadratic scale of f^2 vs. B^2 . Data were measured concurrently in a sample with density $n_s \approx 2.4 \times 10^{11}$ cm⁻². Effective mass ratio, m^*/m_0 , and plasmon frequency, f_p , found from the slope and intercept, respectively, are indicated within the plot.

in Fig. 6). The shallower extrema on the upper and lower envelopes, near 0.47 T in Fig. 6, are not investigated in this report.

Using the method shown in Fig. 6, we locate the resonance positions in SdH oscillations over the measured frequency range, and plot them in Fig. 7 (red squares), in a quadratic scale of f^2 vs. B^2 . Effective mass ratio, $m^*/m_0 = 0.0666 \pm 0.0010$ and plasmon frequency, $f_p = 56.6 \pm 28.0$ GHz, are found from slope and intercept of linear fit through data, respectively. These values agree with $f_p = 54.0 \pm 30.0$ GHz and $m^*/m_0 = 0.0681 \pm 0.0010$ found from resonance positions in SdH oscillations for the second sample, with $n_s \approx 3.3 \times 10^{11}$ cm⁻² (data not

shown). For comparison, the resonance positions in the reflected power, measured in the same sample, are also shown in Fig. 7 (black circles). It is clear that both signals show resonance in the same place. This implies that both phenomena, though measured via different methods, point to the same physics in the sample, i.e., cyclotron or magnetoplasmon resonance. The higher error in f_p and m^* values estimated from the data in SdH oscillations relates to the fact that SdH oscillations could not be measured below 0.3 T and to the overall higher inaccuracy in locating the resonance positions in SdH.

Discussion and Summary

At liquid helium temperatures, we have measured microwave reflection and standard diagonal magnetoresistance as a function of the magnetic field in high mobility GaAs/AlGaAs heterostructures under linearly polarized photoexcitation over the wide frequency band spanning from 30 to 330 GHz. The microwave reflection indicated a cyclotron or magnetoplasmon resonance that shifted to higher magnetic fields with increasing frequency of photo-excitation on both sides of the magnetic field axis. The diagonal magnetoresistance exhibited Shubnikov-de Haas oscillations with a reduction in the SdH amplitude in the vicinity of the cyclotron or magnetoplasmon resonance. This feature is attributed to resonant electron heating in the vicinity of the resonance and an associated reduction in the SdH amplitude. The magnetoplasma effect was further investigated by plotting f^2 vs. B^2 . The results suggested a finite frequency zero-magnetic-field intercept, providing an estimate for the plasma frequency. The experimentally measured plasma frequency was somewhat lower than the estimated plasma frequency for these Hall bars. The results, in sum, are consistent with an effective mass ratio of $m^*/m = 0.067$, the standard value, even in these high mobility GaAs/AlGaAs devices. Thus, the results show the possibility of observing the cyclotron or magnetoplasmon resonance from the reflected excitation and also in the Shubnikov-de Haas magnetoresistance oscillations in the photoexcited high mobility 2D electron specimen.

Methods

GaAs/AlGaAs heterostructures were patterned into Hall bar devices with a width $W = 200 \mu\text{m}$ by photolithography. These devices were loaded onto a waveguide sample holder and inserted into a liquid helium cryostat to place the specimen at the center of a superconducting solenoid magnet. The samples were immersed in liquid helium for all the reported measurements. Commercially available power sensors were attached to one arm of a waveguide coupler, see Fig. 1, to capture the reflected power from the specimen, for the reflection measurements as a function of the magnetic field. The reflected power was read-out by a power meter. Note that, since the reflected resonance signal was significantly weaker than the incident photo-excitation, it was necessary to remove via an offset the background reflection, to realize the necessary enhanced sensitivity to observe cyclotron or magnetoplasmon resonance in the reflected signal. Magnetotransport measurements were performed, concurrently with the reflection measurements, using low frequency lock-in techniques, in order to obtain the diagonal resistance R_{xx} vs. the magnetic field. Measurements are reported here for a pair of samples which exhibited electron density $n_s = 2.4 \times 10^{11} \text{ cm}^{-2}$ and mobility $\mu = 10 \times 10^6 \text{ cm}^2/\text{Vs}$ for the first sample and $n_s = 3.3 \times 10^{11} \text{ cm}^{-2}$ and $\mu = 6 \times 10^6 \text{ cm}^2/\text{Vs}$ for the second sample.

The linearly polarized photo-excitation was produced using a number of sources: Over the 30–50 GHz frequency band, the photoexcitation was generated using commercially available synthesizers and conveyed via semirigid coax to an electric dipole launcher atop the waveguide. A 6x multiplier mm-wave module served to provide radiation between 65–110 GHz. Above 110 GHz, a highly stable and frequency tunable microwave oscillator in the 10–20 GHz region, with a linewidth of 1 Hz and output power of 17 dBm, excited a series of voltage biased- and unbiased- frequency multipliers. The frequency multiplication stage immediately following the 10–20 GHz oscillator was a frequency-doubling Spacek amplifier. Subsequent frequency multipliers, based on a planar GaAs Schottky diode technology have individual multiplication factors of $\times 2$ or $\times 3$ and are daisy-chained to obtain the desired output frequency up to 330 GHz. At the highest frequencies, attenuation between the radiation source and specimen is estimated to be between 10 and 20 dB, caused by a number of factors including mode mismatch, Ohmic losses, and atmospheric attenuation at the highest frequencies.

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Author Contributions

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Additional Information

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