# Research Paper <br> Sex differences in genetic and environmental influences on frailty and its relation to body mass index and education 

Jonathan K. L. Mak ${ }^{1}$, Chandra A. Reynolds ${ }^{2}$, Sara Hägg ${ }^{1}$, Xia Li ${ }^{1}$, Malin Ericsson ${ }^{1,3}$, Nancy L. Pedersen ${ }^{1}$, Juulia Jylhävä ${ }^{1}$, Ralf Kuja-Halkola ${ }^{1}$<br>${ }^{1}$ Department of Medical Epidemiology and Biostatistics, Karolinska Institutet, Stockholm, Sweden<br>${ }^{2}$ Department of Psychology, University of California, Riverside, CA 92521, USA<br>${ }^{3}$ Melbourne School of Psychological Sciences, MDHS, The University of Melbourne, Melbourne, Australia

Correspondence to: Jonathan K. L. Mak; email: jonathan.mak@ki.se
Keywords: frailty, twin, heritability, body mass index, education
Received: March 13, $2021 \quad$ Accepted: June 22, $2021 \quad$ Published: July 6, 2021
Copyright: © 2021 Mak et al. This is an open access article distributed under the terms of the Creative Commons Attribution License (CC BY 3.0), which permits unrestricted use, distribution, and reproduction in any medium, provided the original author and source are credited.


#### Abstract

Frailty is influenced by numerous genetic and environmental factors. However, sex differences in how these factors affect frailty, and the gene-environment interplay among frailty and two of its well-established risk factors, unhealthy body mass index (BMI) and low education, are less clear. In a large sample of 42,994 Swedish twins, we used structural equation models to estimate the genetic (heritability) and environmental sources of variance in frailty, defined as the frailty index (FI), separately in men and women. Genetic and individualspecific environmental factors contributed approximately equally to the FI variance. The heritability of FI was slightly, but significantly, higher in women (52\%) than in men (45\%), yet we found only weak-to-no indication of different sources of genetic variance influencing frailty across sexes. We observed a small-to-moderate genetic overlap between FI and BMI, and that the correlation between FI and education was largely explained by environmental factors common to twins in a pair. Additionally, genetic factors accounted for more of FI variation at both low and high BMI levels, with similar patterns in both sexes. In conclusion, the twin-based heritability of frailty is higher in women than in men, and different mechanisms may underlie the associations of frailty with BMI and education.


## INTRODUCTION

Frailty, as a manifestation of aging, is a state of increased vulnerability due to cumulative decline in multiple physiological systems [1]. The concept of frailty has been operationalized in two principal models: the frailty phenotype (FP) defines frailty as a clinical syndrome associated with unintentional weight loss, weak grip strength, slow walking speed, exhaustion, and low physical activity [2], whereas the Rockwood frailty index (FI) summarizes vulnerability quantitatively and defines frailty as the accumulation of deficits from a wide range of physical and psychosocial functioning [3, 4]. Regardless of the definition being used, frailty has been consistently linked to adverse outcomes such as falls,
hospitalizations, loss of independence, and mortality [5], posing a significant public health concern. Tackling frailty is also recognized as a priority by the European Union [6], calling for better understanding of the syndrome. The prevalence of frailty increases with age, with an overall estimated prevalence of $10.7 \%$ among those aged $\geq 65$ and $26.1 \%$ among those aged $\geq 85$, varying depending on which frailty scale is used [7]. Meanwhile, there is sizable variability in the frailty status at all ages [8], highlighting the necessity to gain understanding on the underpinnings of the individual differences. The sex-paradox of frailty has been widely described, in which women experience higher levels of frailty but men are more vulnerable to death at any given level of frailty, yet the mechanisms behind remain elusive [9].

In accordance with its multifactorial nature, frailty is influenced by both genetic and environmental factors, with twin-based heritability estimates of the FI ranging from 30 to $45 \%$ [10, 11]. However, these studies included female twins only, leaving sex differences in the heritability of FI unaddressed. A vast body of literature has discerned the lifestyle and environmental determinants of frailty [12-14], and showed a persisting socioeconomic gradient in frailty, with increasing socioeconomic adversity associated with higher frailty and contributing to health inequalities even in old age [15]. Two of the most significant risk factors of frailty are unhealthy body mass index (BMI) ranges, including both underweight and obesity [16-18], and low educational attainment [12, 19-21]. A recent Mendelian randomisation analysis showed that the genetic risk of higher BMI and lower educational attainment had the strongest associations with frailty among all modifiable risk factors [22]. However, few studies have elucidated the mechanisms by which these risk factors influence frailty, and whether there may be overlap in the genetic and/or environmental underpinnings of FI with BMI and education. Moreover, it is not known whether the genetic and environmental influences on the FI are altered by BMI and education levels, that is, whether there is gene-environment interaction $(\mathrm{G} \times \mathrm{E})$ such that genetic risk of frailty may be amplified or suppressed with different environmental circumstances. It is also unclear whether men and women may differ with respect to $G \times E$.

Twin studies offer a natural experiment to partition variance of traits into genetic and environmental etiologies by comparing the genetic similarities between monozygotic (MZ) and dizygotic (DZ) twins, who share $100 \%$ and $\sim 50 \%$ of their segregating alleles respectively. Large twin samples also allow robust assessment on whether the heritability of a trait differs quantitatively by sex, meaning whether it is the same genes but at different magnitudes that act upon the trait. Moreover, with the inclusion of opposite-sex twins, qualitative sex differences can be examined, informing whether the trait is influenced by different genetic factors in men and women. As the extension to classical twin models, bivariate models allow study of the sources of covariation between traits, while moderation models enable examination of $G \times E$. To date, studies on the variance components of the FI are scarce and the potential sex differences remain unaddressed. The mechanisms by which high BMI and low education influence frailty are likewise poorly known. Not only is understanding the basis of the sex differences in frailty of importance, but identifying how the risk factors affect frailty will also aid in informing preventive strategies and public health interventions.

Towards this end, we performed structural equation modelling using data from the Screening Across the Lifespan Twin study (SALT), a large sample of Swedish twins ( $n=42,994$ ), with aims to (i) provide a comprehensive estimation of the contribution of genetic and environmental factors to the variance of the FI, and identify potential quantitative and qualitative sex differences therein; (ii) explore the common genetic and environmental influences on the covariation of FI with BMI and education, two of the most prominent risk factors of frailty; and (iii) test for $G \times E$ by levels of BMI and education.

## RESULTS

## Sample characteristics

Table 1 shows the descriptive statistics of the sample, among the 42,994 twin individuals the mean age of which was 58.8 (standard deviation 10.7; range 41-99). The median FI, i.e., the proportion of endorsed frailty items out of 44 (items listed in Supplementary Table 1), was 0.108 (interquartile range $0.062-0.176$ ). Women were on average older (mean age 59.2 vs 58.4 years) and had a higher median FI ( 0.119 vs 0.097 ) than men. Mean BMI and length of education were $25.0 \mathrm{~kg} / \mathrm{m}^{2}$ and 10.5 years respectively; both were similar across sex.

## Phenotypic, intraclass and cross-twin cross-trait correlations

Age-adjusted correlations across zygosity are presented in Table 2 (unadjusted correlations in Supplementary Table 2). For FI, BMI and education, when correlating the same phenotype across twins in a pair (i.e., intraclass correlation), the MZ correlations were larger than DZ correlations and were less than 1, suggesting both genetic and individual-specific environmental influences on all three traits. We observed significantly greater intraclass correlations of FI in women than in men for same-sex twins, implying quantitative sex differences; nevertheless, intraclass correlation of FI in opposite-sex twins did not seem to be smaller than that in same-sex DZ twins, suggesting absence of qualitative sex differences.

FI had a positive phenotypic correlation with BMI ( $r=$ 0.13 ) and a negative correlation with education ( $r=-$ 0.09). The higher MZ than DZ cross-twin cross-trait correlation between FI and BMI indicated that part of their covariation could be explained by genetic influences in common. In contrast, cross-twin cross-trait correlations between FI and education were comparable for MZ and DZ twins, indicating environmental factors common to twins in a pair, rather than genetic factors, contributing to their covariance.

Table 1. Characteristics of study population by sex.

| Characteristic | Total <br> $(\boldsymbol{n}=\mathbf{4 2 , 9 9 4})$ | Men <br> $(\boldsymbol{n}=\mathbf{1 9 , 9 4 0})$ | Women <br> $(\boldsymbol{n}=\mathbf{2 3 , 0 5 4})$ |
| :--- | :---: | :---: | :---: |
| Age at interview, mean (SD) | $58.8(10.7)$ | $58.4(10.4)$ | $59.2(11.0)$ |
| FI, median (IQR) | $0.108(0.062,0.176)$ | $0.097(0.057,0.153)$ | $0.119(0.068,0.193)$ |
| BMI (kg/m²), mean (SD) | $25.0(3.5)$ | $25.5(3.1)$ | $24.5(3.8)$ |
| Education (years), mean (SD) | $10.5(3.2)$ | $10.5(3.2)$ | $10.4(3.3)$ |
| Zygosity, n (\%) |  |  |  |
| MZ | $10,785(25.1)$ | $4,788(24.0)$ | $5,997(26.0)$ |
| Twins from complete pairs | $8,516(79.0)$ | $3,640(76.0)$ | $4,876(81.3)$ |
| DZ same-sex | $16,448(38.3)$ | $7,640(38.3)$ | $8,808(38.2)$ |
| Twins from complete pairs | $11,824(71.9)$ | $5,266(68.9)$ | $6,558(74.5)$ |
| DZ opposite-sex | $15,761(36.7)$ | $7,512(37.7)$ | $8,249(35.8)$ |
| Twins from complete pairs | $11,582(73.5)$ | $5,791(77.1)$ | $5,791(70.2)$ |

Note: BMI, body mass index; DZ, dizygotic twins; FI, frailty index; IQR, interquartile range; MZ, monozygotic twins; SD, standard deviation.

Table 2. Adjusted phenotypic correlations, intraclass correlations and cross-twin cross-trait correlations for the frailty index (FI), body mass index (BMI) and education.

| Zygosity | Phenotypic correlations |  |  | Intraclass correlations |  |  | Cross-twin cross-trait correlations |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | FI and BMI | FI and Education | FI | BMI | Education | FI and BMI | FI and Education |
| Total | $0.13(0.12,0.14)$ | $-0.09(-0.10,-0.08)$ |  |  |  |  |  |
| MZ | $0.12(0.10,0.14)$ | $-0.09(-0.11,-0.07)$ | $0.51(0.49,0.53)$ | $0.68(0.67,0.70)$ | $0.65(0.64,0.67)$ | $0.10(0.08,0.12)$ | $-0.07(-0.10,-0.05)$ |
| DZ | $0.14(0.13,0.15)$ | $-0.09(-0.11,-0.07)$ | $0.18(0.17,0.20)$ | $0.23(0.22,0.25)$ | $0.42(0.40,0.43)$ | $0.06(0.05,0.07)$ | $-0.08(-0.09,-0.06)$ |
| MZ males | $0.14(0.11,0.17)$ | $-0.10(-0.13,-0.07)$ | $0.45(0.41,0.48)$ | $0.66(0.63,0.68)$ | $0.66(0.63,0.68)$ | $0.11(0.08,0.14)$ | $-0.07(-0.10,-0.04)$ |
| MZ females | $0.15(0.12,0.18)$ | $-0.09(-0.12,-0.06)$ | $0.53(0.50,0.56)$ | $0.69(0.67,0.71)$ | $0.65(0.63,0.67)$ | $0.13(0.10,0.16)$ | $-0.08(-0.11,-0.05)$ |
| DZ males | $0.12(0.09,0.14)$ | $-0.09(-0.11,-0.07)$ | $0.12(0.09,0.16)$ | $0.27(0.24,0.31)$ | $0.44(0.42,0.47)$ | $0.05(0.02,0.07)$ | $-0.07(-0.10,-0.05)$ |
| DZ females | $0.19(0.17,0.21)$ | $-0.07(-0.09,-0.05)$ | $0.24(0.20,0.27)$ | $0.31(0.28,0.34)$ | $0.46(0.43,0.48)$ | $0.10(0.08,0.13)$ | $-0.06(-0.09,-0.04)$ |
| DZ opposite-sex | $0.11(0.09,0.13)$ | $-0.10(-0.13,-0.08)$ | $0.17(0.15,0.20)$ | $0.18(0.15,0.20)$ | $0.38(0.36,0.41)$ | $0.03(0.01,0.06)$ | $-0.09(-0.11,-0.06)$ |

Note: MZ, monozygotic twins; DZ, dizygotic twins. Phenotypic correlations are the within-individual correlations between FI and BMI, and between FI and education. Intraclass correlations indicate the extent to which each trait correlates within twin pairs. Cross-twin cross-trait correlations show the extent to which FI of the first twin correlate with the other trait (i.e., BMI or education) of the second twin. $95 \%$ confidence intervals are presented in parenthes es. All correlations were adjusted for age.

## Univariate twin modelling

Univariate sex-limitation models of FI were fitted as shown in Table 3, providing estimates of the variance components in men and women: additive genetic factors (A), dominance genetic factors (D), common environmental factors (C), and unique environmental factors (E). Overall, the best-fitting model was an ADE model (i.e., a model including $\mathrm{A}, \mathrm{D}$ and E variance components) with only quantitative sex differences. Compared to the saturated model (i.e., a model that fully describes the observed data), the full ADE model did not provide a worse model fit, indicating that the model fit the data well, but both the ACE and AE models provided a poor fit to the data. Removing
quantitative sex differences (i.e., different magnitude of heritability) from the ADE quantitative sex-limitation model resulted in a reduced model fit. Meanwhile, the genetic correlation for opposite-sex twins ( $r_{\mathrm{fm}}$ ), which is used for assessing qualitative sex difference (i.e., different sources of genetic variance), was close to, and statistically non-significantly different from unity. This suggests the presence of quantitative, but not qualitative sex differences in the genetic contributions to FI. We observed largely dissimilar proportions of additive and dominance genetic influences on FI for men and women. Alternatively, we estimated the broad-sense heritability, H, of FI (i.e., proportion of variance that can be explained by the total of additive and dominance genetic factors), which was estimated to be $45 \%$ [ $95 \%$

Table 3. Model fitting results and parameter estimates from univariate sex-limitation models of the frailty index (FI).

| Model | Model fit statistics |  |  |  | Parameter estimates for men and women (95\% CI) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | AIC | $\Delta \mathrm{LL}$ | $\Delta \mathrm{df}$ | $p$ | A | D/C | H | E | $r_{\text {fm }}$ |
| Saturated | 19953 | - | - | - | - | - | - | - | - |
| ADE full sex-limitation | 19940 | 19.1 | 16 | 0.264 | $\begin{gathered} \text { M: } 7 \%(0,23) \\ \text { F: } 41 \%(28,55) \end{gathered}$ | $\begin{gathered} \text { M: } 38 \%(21,55) \\ \text { F: } 11 \%(0,25) \end{gathered}$ | $\begin{gathered} \text { M: } 44 \%(41,48) \\ \text { F: } 52 \%(50,55) \end{gathered}$ | $\begin{gathered} \text { M: } 56 \%(52,59) \\ \text { F: } 48 \%(45,50) \end{gathered}$ | 0.69 (0.41, 0.96) |
| ADE quantitative sex-limitation | 19939 | 19.7 | 17 | 0.288 | $\begin{gathered} \text { M: 0\% }(0,1) \\ \text { F: } 41 \%(28,55) \end{gathered}$ | $\begin{aligned} & \text { M: } 44 \%(41,48) \\ & \text { F: } 11 \%(0,25) \end{aligned}$ | $\begin{aligned} & \text { M: } 45 \%(41,48) \\ & \text { F: 52\% }(50,55) \end{aligned}$ | $\begin{aligned} & \text { M: 55\% }(52,59) \\ & \text { F: 48\% }(45,50) \end{aligned}$ | 1.00 (NA) |
| ADE no sex difference | 19949 | 32.1 | 18 | 0.021 | $\begin{gathered} \text { M: } 0 \%(0,2) \\ \text { F: } 44 \%(31,58) \end{gathered}$ | $\begin{gathered} \mathrm{M}: 49 \%(45,52) \\ \mathrm{F}: 4 \%(0,19) \end{gathered}$ | $\begin{gathered} \text { M: } 49 \%(47,51) \\ \text { F: } 49 \%(47,51) \end{gathered}$ | $\begin{gathered} \text { M: } 51 \%(49,53) \\ \text { F: } 51 \%(49,53) \end{gathered}$ | 1.00 (NA) |
| ACE full sex-limitation | 19961 | 40.4 | 16 | 0.001 | $\begin{aligned} & \text { M: } 41 \%(37,44) \\ & \text { F: } 51 \%(49,54) \end{aligned}$ | M: $0 \%(0,0)$ <br> F: $0 \%(0,0)$ | $\begin{gathered} \text { M: } 41 \%(37,44) \\ \text { F: } 51 \%(49,54) \end{gathered}$ | $\begin{aligned} & \text { M: } 59 \%(56,63) \\ & \text { F: } 49 \%(46,51) \end{aligned}$ | 0.76 (0.64, 0.88) |
| AE full sex-limitation | 19957 | 40.4 | 18 | 0.002 | $\begin{gathered} \text { M: } 41 \%(37,44) \\ \text { F: } 51 \%(49,54) \end{gathered}$ | $\begin{aligned} & \text { M: } 0 \% \text { (NA) } \\ & \text { F: } 0 \% \text { (NA) } \end{aligned}$ | $\begin{aligned} & \text { M: } 41 \%(37,44) \\ & \text { F: } 51 \%(49,54) \end{aligned}$ | $\begin{gathered} \text { M: } 59 \%(56,63) \\ \text { F: } 49 \%(46,51) \end{gathered}$ | 0.76 (0.64, 0.88) |

Note: AIC, Akaike's Information Criterion; LL, log-likelihood; df, degrees of freedom; p, p-values of likelihood ratio tests compared with the saturated model. Cls are Wald-type confidence intervals with lower and upper bounds of 0 and 1 respectively. A, additive genetic factors; D, dominance genetic factors; C, common environmental factors; $H$, total genetic factors/ broad-sense heritability; E , unique environmental factors; $r_{f m}$, genetic correlation between men and women, estimated using opposite-sex twins. M and F represents parameter estimates for men and women respectively. Full sexlimitation models allowed both quantitative and qualitative sex differences. In ADE quantitative sex-limitation model, $r_{f m}$ was fixed to be 1. In ADE no sex difference model, broad-sense heritability of men and women were equated, but variance difference between sex was allowed. ACE and AE sub-models are not shown as the full models fit significantly worse than the saturated model. All models were adjusted for age. Best-fitting model is shown in bold.
confidence interval (CI): 41-48\%] in men, and at a statistically significantly higher proportion of $52 \%$ ( $95 \%$ CI: $50-55 \%$ ) in women. The rest of the variation in FI was explained by unique environmental factors.

## Bivariate twin modelling

Using bivariate twin models, we assessed the overlap of genetic and environmental variance components of FI with BMI and education and allowed for sex differences. The best-fitting bivariate model for FI and BMI was an ADE model (Figure 1A; model fit statistics and parameter estimates in Supplementary Tables 3, 4). Variance of BMI was predominantly explained by genetic factors (men: $\mathrm{H}=66 \%$; women: $\mathrm{H}=69 \%$ ). We observed modest genetic correlations between FI and BMI, which were 0.19 ( $95 \%$ CI: $0.14-0.23$ ) and 0.26 ( $95 \% \mathrm{CI}: 0.22-0.29$ ) in men and women, respectively. The bivariate heritability for FI and BMI, i.e., the proportion of covariance explained by genetic factors, was $81 \%$ ( $95 \%$ CI: $65-97 \%$ ) in men and $87 \% ~(95 \%$ CI: $78-95 \%$ ) in women, indicating that a substantial part of the correlation between FI and BMI could be attributable to genetic factors in common to both traits (Figure 1C). By contrast, the best-fitting bivariate model for FI and education according to the Akaike's Information Criterion (AIC) was an ACE model (Figure 1B), although, all bivariate models between FI and education provided a worse fit than the saturated model.

A moderate proportion of the variation in education was due to common environmental factors, which was $25 \%$ ( $95 \%$ CI: $19-31 \%$ ) in men and $29 \%$ ( $95 \%$ CI: $23-34 \%$ ) in women. The C component of FI was small and nonsignificant in both sexes, however, they had perfect negative correlations with that of education ( $r_{\mathrm{C}}=-1.00$ ). Common environmental factors also accounted for considerable proportions of the phenotypic correlations between FI and education, which were $65 \%$ ( $95 \% \mathrm{CI}$ : $23-107 \%$ ) in men and $74 \%$ ( $95 \%$ CI: $22-126 \%$ ) in women (Figure 1C). There was only weak overlap of genetic factors and unique environmental factors between FI and education.

## Moderation analysis

To determine whether genetic and environmental variance components of FI change with levels of BMI and education, we constructed a series of bivariate and univariate moderation models to examine whether there is moderation on the covariance between FI and the moderator (i.e., BMI and education), in addition to the variance unique to FI. For moderation by BMI, we observed significant moderating effects on the variance unique to FI as well as on the covariance between FI and BMI; in contrast, for moderation by education, we observed only significant moderating effects on the unique variance of FI (Supplementary Tables 5, 6). Therefore, a full bivariate moderation
model and an extended univariate moderation model were fitted for moderation by BMI and education, respectively, as proposed by van der Sluis et al [23]. The H and E components of FI from the best-fitting moderation models are plotted in Figure 2 (see Supplementary Figure 1 for separate A and D components; and Supplementary Figure 2 for separate common and unique variance estimates of FI by BMI levels). Patterns of moderation were consistent in both men and women, although women had a higher absolute variance of FI than men. The total variance of FI was larger at low and high BMI levels and at fewer years of education. It appeared that genetic variance of FI increased at both ends of BMI levels, while unique environmental variance of FI was similar at all BMI values; hence, the heritability of FI was greater at low and high BMI. In contrast, both genetic and environmental variance of FI declined to a comparable extent with increased years of education; therefore, the relative proportions of genetic and environmental sources of FI variance did not seem to vary across education years.

## Sensitivity analysis

We additionally performed sensitivity analysis to examine if the skewed distribution of FI affected its heritability estimates. Variance component estimates of the square-root transformed FI were largely consistent with that of the non-transformed FI variable (Supplementary Table 7). Moreover, similar patterns of moderating effects by BMI and education on the transformed FI were observed in men, but there was less evidence of moderation by BMI in women (Supplementary Figure 3). We also fitted the univariate and bivariate models using an alternative "direct symmetric approach" that allows negative variance components [24]; all the conclusions were essentially the same as in the main analysis (Supplementary Tables 8-10).

## DISCUSSION

Using a large sample of Swedish twins, we found that the variation in frailty was attributed rather equally to


Figure 1. Parameter estimates from the best-fitting bivariate twin models. (A) ADE bivariate quantitative sex-limitation model between frailty index (FI) and body mass index (BMI), adjusted for age. Single headed-arrows represent the proportion of each traits explained by latent (circular) variance components; while double-headed arrows represent correlations between variance components. H indicates the sum of additive and dominance genetic factors; E indicates unique environmental factors; M and F are the estimates for men and women respectively. (B) ACE bivariate quantitative sex-limitation model between FI and education, adjusted for age. A indicates additive genetic factors; C indicates common environmental factors. (C) Phenotypic correlations of FI with BMI and education among men and women (with $95 \%$ confidence intervals), and the proportion of correlations explained by total genetic, common environmental and unique environmental factors. Note: Model-fitting results and parameter estimates can be found in Supplementary Tables 3, 4.
both genetic (with presence of additive and dominance effects) and individual-specific environmental influences. The twin-based heritability of FI was greater in women than in men, but there was no strong evidence of qualitative sex difference, indicating that the same genes, although at different magnitudes, are influencing FI in both sexes. There was small-to-moderate genetic overlap between FI and BMI, and a complete overlap of the environmental factors common to twins within pairs between FI and education, suggesting different mechanisms on how BMI and education influence the risk of frailty. In addition, moderation analysis showed that the total variance of FI varies with levels of BMI and years of education, so that genetic influence on frailty was greater at both low and high levels of BMI, but the heritability of FI did not seem to differ across education years.

Our finding that much of the FI variance is due to genetic factors is in line with two prior UK twin studies analyzing variance components of FI, which reported a heritability of $30-45 \%$ [ 10,11$]$. By contrast, it is higher than the SNP-based heritability of $14 \%$ estimated in a recent genome-wide association study (GWAS) [22], which may be partly due to the overestimation of
heritability in twin studies [25], or that GWAS does not include non-additive genetic effects, as observed in the current study, and it has limited power to detect rare genetic variants that normally exist in complex traits like frailty [25, 26]. Environmental factors shared by members within twin pairs, which are usually those from childhood such as family environment, have negligible influence on frailty. Instead, a substantial proportion of the variation of FI is shaped by environmental factors unique to individuals, although this component also includes measurement error. This may reflect the multidimensional nature of frailty, in which diverse physical, social, behavioral and psychological factors have been linked to the elevated risk of frailty [12-14].

To our knowledge, this is the first study that has formally examined sex differences in the heritability of frailty. We observed rather small, but significantly greater heritability in women (52\%) than in men (45\%); meanwhile, there was weak and statistically nonsignificant qualitative sex difference. A higher heritability of some psychological and neurological traits, such as depression [27], pain [28], and insomnia [29], has also been observed among women, which is

## B Moderation by education



Figure 2. Moderation analysis of frailty index (FI) by (A) body mass index (BMI) and (B) education, stratified by sex. First row shows the absolute variance of FI , while the second row shows the proportion of FI variance explained by total genetic ( H , indicating sum of additive and dominance genetic factors) and unique environmental (E) factors, with changes in BMI and education. Variance estimates of moderation by BMI were obtained from the full ADE bivariate moderation model between FI and BMI ; while variance estimates of moderation by education were obtained from the ADE extended univariate moderation model between FI and education. Quantitative sex-differences were allowed in the models to obtain estimates separately for men and women. Models were adjusted for age. Note: Model-fitting results can be found in Supplementary Tables 5, 6.
attributed at least partly to the higher prevalence of these traits in women. Similarly, women may also be more genetically susceptible to frailty, given that the genetic underpinnings of frailty have been found to be associated with neurological pathways [22]. Another possible explanation to the difference in variance components across sex may be that men tend to report health problems less accurately [30], leading to an inflation of the E component. Notably, the total variance of FI was also higher in women than in men, reflecting the fact that women tend to have higher levels of frailty across the age range. The apparent sex difference may merely be owing to the overall greater variation of FI in women, instead of disparities in variance structure across sex, as shown in other traits such as BMI [31]. Furthermore, the observed sex difference is not immense, yet statistically significant, perhaps also due to our large sample that provided enough statistical power. More research is warranted to further investigate if sex differences in genetic and environmental factors contribute to the sex-specificity of frailty.

Our second aim was to assess the overlap in genetic and environmental influences of FI with BMI and education. There was a small-to-moderate genetic correlation between FI and BMI, suggesting that frailty and BMI may in part be influenced by the same genes. This may be attributable to their shared underlying mechanisms of energy metabolism and inflammation, known to be associated with both frailty [32, 33] and BMI [34, 35]. Also, genes related to synaptic pathways, were found to be enriched in the genetic architecture of frailty [22], and likewise may affect BMI [35]. On the other hand, we found a relatively low genetic correlation between FI and education; instead, despite small and nonsignificant common environmental variance component of FI , it explains a large proportion of the correlation between FI and education, suggesting the relative importance of family environment on the educationfrailty association. Previous studies found that genes associated with educational attainment have an inverse relationship with frailty [22, 36]; our finding may therefore imply a possible mechanism that educationassociated genes are not directly influencing frailty, but indirectly through affecting individuals' socioeconomic circumstances [37]. The better family environment may then contribute to higher educational attainment and consequently prevention of frailty development, through the improved health literacy that higher education in the family brings [38, 39], as well as the health seeking behavior that is especially characteristic to women with high education [40]. It is however important to note that the common environmental factors of FI itself were small and not statistically significant and should be interpreted with caution.

Finally, we saw significant moderating effects on the genetic and unique environmental variance components of FI by both BMI and education, and the patterns were generally similar in men and women, although sensitivity analysis showed less evidence of moderation by BMI on the transformed FI in women. The overall variance of FI, as well as the relative proportion of genetic variance component were higher at both low and high BMI levels, which follows the U-shaped association between BMI and physical frailty reported in the literature [16-18]. This indicates that in individuals whose BMI falls outside a healthy range, especially those with obesity ( $\mathrm{BMI}>30$ ), the increased risk of frailty may be due to their more pronounced expression of genetic susceptibilities to frailty. On the other hand, the reduced FI variance with increased years of education is congruent to previous literature showing smaller variance of health status at higher education levels [41]. Meanwhile, the proportions of genetic and unique environmental variance components over the total variance did not seem to differ over education years, suggesting that genetic and individual-specific environmental factors may have a stable contribution to frailty, independent of education.

This study included a population-representative adult twin sample, which provided enough statistical power to examine sex differences in heritability of frailty. We also used a validated FI as the frailty measure, which was shown to predict higher risk of all-cause, cardiovascular disease, and respiratory-related mortality from midlife to old age [42]. Nevertheless, several limitations should be considered. First, given the cross-sectional nature of our data, we could not establish causal relationships among BMI, education and FI. Whether the variance components change with age should also be researched in future longitudinal studies with repeated measurements of frailty. Second, measures of frailty items, BMI, and education are all based on self-reported data, possibly causing misclassification and inaccurate reporting, especially in men [43]. Third, due to the different contribution of dominance genetic factors and common environmental factors to the variance of FI and education, all bivariate models for FI and education provided a poor fit, and we were unable to include both C and D parameters in the same statistical model with only reared-together twins in a classical twin design. Finally, there are some inherent limitations of twin modelling such as potential overestimation of heritability [25] and violation on the assumptions of equal environments (i.e., MZ and DZ twins are treated the same) and random mating in population (i.e., no assortment), although these should have minimal effects on the heritability estimates [44].

Overall, our findings demonstrate that individual differences in frailty are attributable to both genetic and individual-specific environmental factors. Sex differences are evident, in which women have a slightly higher heritability of frailty than men, yet there is limited evidence of different genetic factors influencing frailty in men and women. Furthermore, the two main risk factors of frailty, BMI outside a healthy range and low education, seem to operate through different mechanisms in frailty development, highlighting the relative importance of genes and family environment on the associations of frailty with BMI and education, respectively. These results would help in expanding our current understanding on the individual differences in frailty.

## MATERIALS AND METHODS

## Study population

Twin participants were from SALT, which is part of the population-based Swedish Twin Registry [45]. During 1998-2002, all twins born in 1958 or before were invited to attend a telephone interview with questions on common diseases, symptoms, medication use, demographics, and lifestyle factors. With a response rate of $65 \%$ for those born in 1886-1925 and $74 \%$ for those born in 1926-1958, a total of 44,919 twin individuals participated in the survey [46]. Zygosity was determined based on DNA, or questions on intra-pair similarities during childhood; the latter method was over $95 \%$ accurate when validated against DNA testing [47]. This study has been approved by the Swedish Ethical Review Authority in Stockholm. Informed consent was obtained from all participants prior to data collection.

For the present analysis, we excluded those with uncertain zygosity and those who had over $20 \%$ missing data across the 44 frailty items, leaving $n=42,994$ consisting of 31,922 paired and 11,072 single respondents, aged from 41 to 99 years. Single twin individuals were retained as they contribute to the mean, variance and within-individual covariance estimates. Twins were grouped by zygosity: $4,788 \mathrm{MZ}$ males ( 1,820 complete pairs), $5,997 \mathrm{MZ}$ females ( 2,438 complete pairs), $7,640 \mathrm{DZ}$ same-sex males (2,633 complete pairs), $8,808 \mathrm{DZ}$ same-sex females (3,279 complete pairs), and 15,761 DZ opposite-sex individuals (5,791 complete pairs).

## Measures

We constructed an FI based on Rockwood's deficit accumulation model [3], using a total of 44 selfreported frailty items selected from a wide range of
health-status related symptoms, signs, disabilities, and diseases in various biological systems (items listed in Supplementary Table 1). Each respondent's frailty items were summed up and divided by the total number of deficits measured (i.e., 44 in this study), yielding a continuous FI score ranging from 0 to 1 . For instance, an individual with five deficits would have an FI of $5 / 44$ $=0.11$. The FI in SALT has previously been validated for its ability to predict mortality [42].

Information on body mass index (BMI) and education were obtained from self-reported data. BMI was calculated as weight ( kg ) divided by height-squared $\left(\mathrm{m}^{2}\right)$. We defined education as a continuous variable of the number of years of education completed.

## Statistical analysis

## Twin design

The classical twin design allows decomposition of phenotypic variance into genetic and environmental sources, based on the fact that MZ twins are genetically identical while DZ twins share on average half of their segregating alleles. Genetic sources of variance include additive genetic variance ( A , representing the sum of allelic effects at different loci that influence the trait) and dominance genetic variance ( D , representing interactions between alleles at the same locus). In MZ twins, both A and D correlate $100 \%$; while in DZ twins, A and D are assumed to correlate $50 \%$ and $25 \%$ respectively. The sum of A and D influences is referred to as the broad-sense heritability ( H ), which is the proportion of phenotypic variance that can be explained by genetic effects. On the other hand, environmental sources of variance include common environmental factors (C) such as family environment and environments that are in common or correlated in adulthood, which correlate $100 \%$ in both MZ and DZ twins; and unique environmental factors ( E ) which are uncorrelated between twins and contribute to differences between them. The E component also contains measurement error. In addition to variance, phenotypic covariance can also be partitioned into the same sources of influence, indicating the extent to which genetic and environmental variance components overlap across two or more traits.

## Phenotypic, intraclass and cross-twin cross-trait correlations

For initial inspection of the familial similarity for MZ and DZ twin pairs, we estimated intraclass correlations for FI, BMI and education, which show how much each trait correlates within twin pairs. A higher MZ correlation than DZ correlation indicates contribution of genetics to variance in the trait. If DZ correlation is less than half of the MZ correlation, the D component is
inferred; on the contrary, the C component is implied if DZ correlation is greater than half of the MZ correlation. A MZ correlation less than 1 indicates presence of E .

Within-individual between-trait correlations, which we refer to as "phenotypic correlations", were calculated for FI with BMI and education. To explore the genetic and environmental sources of covariances, we computed cross-twin cross-trait correlations, which represent the strength of relationship between one trait of the first twin and another trait of the second twin. They can be interpreted in a similar way as intraclass correlations. For example, a larger cross-twin cross-trait correlation in MZ than DZ twins suggests that phenotypic correlation between the two traits is partially owing to common genetic influences; and if MZ crosstwin cross-trait correlation is less than the phenotypic correlation then E is present.

Phenotypic, intraclass and cross-twin cross-trait correlations across zygosity were estimated from constrained saturated models in which means, variances and phenotypic correlations were equated across twin order. Age was regressed out of the means (as linear effect for FI and linear+quadratic effect for BMI and education, after initial investigation of associations between variables), so that twin correlations are not spuriously inflated due to the same age of twins in pairs.

## Univariate twin modelling

Before model fitting, we checked and observed no violations in the assumptions of equal means and variances across twin order and zygosity. Univariate twin models were fitted to estimate variance components of FI, after adjusting for age. Since C and D are confounded in classical twin modelling, either an ACE or ADE model can be fitted at a time. Sex differences were allowed in the models to examine whether genetic influence on FI differs across sex quantitatively (i.e., different magnitude of heritability in men and women) and qualitatively (i.e., different genetic sources in men and women). Quantitative sex differences were modelled by allowing variance components to differ among men and women. Qualitative sex differences were estimated by multiplying a genetic correlation term $\left(r_{\mathrm{fm}}\right)$ to the expected genetic covariance of opposite-sex twin pairs, where a value of 1 would imply maximum genetic correlation (see Supplementary Methods for details). ACE or ADE sex-limitation models were then compared with their reduced models. We examined quantitative sex difference by constraining the broadsense heritability to be equal in men and women (but allowing total variance to differ across sex) and tested if there was a significant reduction in model fit.

Qualitative sex difference was assessed by testing whether $r_{\mathrm{fm}}$ was significantly less than 1 . AE models were fitted to determine if the C and D parameters can be excluded from ACE and ADE models.

## Bivariate twin modelling

During assumption testing, all means and variances could be equated across twin order and zygosity, except that equating means of education across zygosity led to a significant decrease in model fit, so they were estimated separately in subsequent bivariate models. A "correlated factor model" [48] was applied to estimate the etiological correlations between genetic ( $r_{\mathrm{A}}$ and $r_{\mathrm{D}}$ ) and environmental ( $r_{\mathrm{C}}$ and $r_{\mathrm{E}}$ ) variance components of FI with BMI and education, apart from estimating variance components of each variables. We define the correlation between $A+D$ in trait $X$ and $A+D$ in trait $Y$ as the broad-sense genetic correlation, $r_{\mathrm{H}}$. Correlation of $\pm 1$ indicates complete overlap, while 0 indicates no overlap. Bivariate heritability was also calculated, which is referred to as the proportion of phenotypic correlation explained by genetic covariation. Since estimates of A and D components are highly dependent, as shown by non-significant A and D estimates, we estimated the broad-sense heritability and interpreted in ADE models to indicate the total genetic effects. Only same-sex twins were included in the bivariate quantitative sex-limitation models, and variance components and etiological correlations were estimated separately by sex, after adjusting for age.

## Moderation analysis

In previous univariate and bivariate models, we assumed that variance components of FI were constant across the population (i.e., no gene-environment interaction). We relaxed this assumption and examined whether the genetic and environmental influences on FI are moderated by different levels of BMI and education. Moderation may occur on the variance that is unique to FI ; for example, changes in genetic variance components of FI with years of education would suggest differential genetic sensitivity of FI to education levels. Furthermore, moderation may exist on the covariance between FI and the moderator, for example, the genetic correlation between FI and BMI may vary with different levels of BMI. To investigate these possible moderating effects, we adopted the full bivariate moderation models developed by Purcell [49], and the extended univariate moderation models proposed by van der Sluis et al [23] (Supplementary Figures 4, 5). By the bivariate moderation models, we first assessed if there were significant moderating effects on the covariance of FI with BMI and education on top of the variance unique to FI. In case of no statistically significant moderation on the covariance between FI and the moderator, the extended univariate moderation models were employed instead. All moderating effects were examined separately
by sex in quantitative sex-limitation models using samesex twins and controlled for age. Absolute genetic and environmental variance components of FI, as well as their proportions to the total variance, were plotted over BMI and education.

## Sensitivity analysis

Since the FI variable is positively skewed (Supplementary Figure 6), we followed previous work and applied a square-root transformation to obtain an approximately normally-distributed FI [10, 11]. Univariate twin modelling and moderation analysis of the transformed FI were then performed to check for robustness of our results. We additionally compared our results of univariate and bivariate twin modelling with models fitted using the "direct symmetric approach" proposed by Verhulst et al. [24], which allows variance estimates to be negative and potentially reduces Type I error rates.

For all fitted models, we used the full information maximum-likelihood modelling in the R package OpenMx (version 2.17.3) for estimation of parameters that best fit the observed data. Changes in goodness of fit of models (distributed as $\chi^{2}$ ) were assessed by likelihood ratio tests, where significant values indicate worse fit of observed data. Akaike information criterion (AIC; a lower value is better) was used to select the most parsimonious and best-fitting models.

## AUTHOR CONTRIBUTIONS

C.A.R., S.H., J.J., and R.K.-H. contributed to the study design and statistical analysis plan. J.K.L.M., X.L., and R.K.-H. performed statistical analyses. N.L.P. is the leader of the SALT study and responsible for cohort recruitment, data collection, and funding. J.K.L.M., M.E., J.J., and R.K.-H. wrote the manuscript. All authors contributed to the interpretation of the results, and read and approved the final manuscript.

## ACKNOWLEDGMENTS

We acknowledge the Swedish Twin Registry for access to data. The Swedish Twin Registry is managed by Karolinska Institutet and receives funding through the Swedish Research Council under the grant number 2017-00641. This study was accomplished within the context of the Swedish National Graduate School for Competitive Science on Ageing and Health (SWEAH) funded by the Swedish Research Council.

## CONFLICTS OF INTEREST

The authors declare that they have no conflicts of interest.

## FUNDING

This work was supported by the Swedish Research Council (2018-02077, 2019-01272), the Loo and Hans Osterman Foundation, FORTE (the Swedish Research Council for Health, Working Life, and Welfare), the Strategic Research Program in Epidemiology at Karolinska Institutet and the Karolinska Institutet Foundations.

## REFERENCES

1. Clegg A, Young J, lliffe S, Rikkert MO, Rockwood K. Frailty in elderly people. Lancet. 2013; 381:752-62. https://doi.org/10.1016/S0140-6736(12)62167-9 PMID:23395245
2. Fried LP, Tangen CM, Walston J, Newman AB, Hirsch C, Gottdiener J, Seeman T, Tracy R, Kop WJ, Burke G, McBurnie MA, and Cardiovascular Health Study Collaborative Research Group. Frailty in older adults: evidence for a phenotype. J Gerontol A Biol Sci Med Sci. 2001; 56:M146-56. https://doi.org/10.1093/gerona/56.3.m146 PMID:11253156
3. Searle SD, Mitnitski A, Gahbauer EA, Gill TM, Rockwood K. A standard procedure for creating a frailty index. BMC Geriatr. 2008; 8:24.
https://doi.org/10.1186/1471-2318-8-24
PMID:18826625
4. Rockwood K, Mitnitski A. Frailty in relation to the accumulation of deficits. J Gerontol A Biol Sci Med Sci. 2007; 62:722-27.
https://doi.org/10.1093/gerona/62.7.722 PMID:17634318
5. Vermeiren S, Vella-Azzopardi R, Beckwée D, Habbig AK, Scafoglieri A, Jansen B, Bautmans I, and Gerontopole Brussels Study group. Frailty and the Prediction of Negative Health Outcomes: A Meta-Analysis. J Am Med Dir Assoc. 2016; 17:1163.e1-17.
https://doi.org/10.1016/i.jamda.2016.09.010 PMID:27886869
6. Cano A, Dargent G, Carriazo A, López-Samaniego L, Apostolo J, Campos E, Holland C, Varela-Nieto I, Luz Sánchez-Sánchez M, Illario M, laccarino G, Roller RE, Goossens E, et al. Tackling frailty and functional decline: Background of the action group A3 of the European innovation partnership for active and healthy ageing. Maturitas. 2018; 115:69-73.
https://doi.org/10.1016/i.maturitas.2018.06.009 PMID:30049350
7. Collard RM, Boter H, Schoevers RA, Oude Voshaar RC. Prevalence of frailty in community-dwelling older
persons: a systematic review. J Am Geriatr Soc. 2012; 60:1487-92.
https://doi.org/10.1111/j.1532-5415.2012.04054.x PMID:22881367
8. Rockwood K, Song X, Mitnitski A. Changes in relative fitness and frailty across the adult lifespan: evidence from the Canadian National Population Health Survey. CMAJ. 2011; 183:E487-94.
https://doi.org/10.1503/cmaj. 101271 PMID:21540166
9. Gordon EH, Peel NM, Samanta M, Theou O, Howlett SE, Hubbard RE. Sex differences in frailty: A systematic review and meta-analysis. Exp Gerontol. 2017; 89:30-40.
https://doi.org/10.1016/j.exger.2016.12.021 PMID:28043934
10. Young AC, Glaser K, Spector TD, Steves CJ. The Identification of Hereditary and Environmental Determinants of Frailty in a Cohort of UK Twins. Twin Res Hum Genet. 2016; 19:600-09.
https://doi.org/10.1017/thg.2016.72 PMID:27719687
11. Livshits G, Ni Lochlainn M, Malkin I, Bowyer R, Verdi S, Steves CJ, Williams FM. Shared genetic influence on frailty and chronic widespread pain: a study from TwinsUK. Age Ageing. 2018; 47:119-25.
https://doi.org/10.1093/ageing/afx122 PMID:28985290
12. Chamberlain AM, St Sauver JL, Jacobson DJ, Manemann SM, Fan C, Roger VL, Yawn BP, Finney Rutten L. Social and behavioural factors associated with frailty trajectories in a population-based cohort of older adults. BMJ Open. 2016; 6:e011410.
https://doi.org/10.1136/bmjopen-2016-011410 PMID:27235302
13. Feng Z, Lugtenberg M, Franse C, Fang X, Hu S, Jin C, Raat H. Risk factors and protective factors associated with incident or increase of frailty among communitydwelling older adults: A systematic review of longitudinal studies. PLoS One. 2017; 12:e0178383. https://doi.org/10.1371/journal.pone. 0178383 PMID:28617837
14. Raymond E, Reynolds CA, Dahl Aslan AK, Finkel D, Ericsson M, Hägg S, Pedersen NL, Jylhävä J. Drivers of Frailty from Adulthood into Old Age: Results from a 27Year Longitudinal Population-Based Study in Sweden. J Gerontol A Biol Sci Med Sci. 2020; 75:1943-50.
https://doi.org/10.1093/gerona/glaa106 PMID: $\underline{32348465}$
15. Brunner EJ, Shipley MJ, Ahmadi-Abhari S, Valencia Hernandez C, Abell JG, Singh-Manoux A, Kawachi I, Kivimaki M. Midlife contributors to socioeconomic differences in frailty during later life: a prospective cohort study. Lancet Public Health. 2018; 3:e313-22.
https://doi.org/10.1016/S2468-2667(18)30079-3 PMID:29908857
16. Hubbard RE, Lang IA, Llewellyn DJ, Rockwood K. Frailty, body mass index, and abdominal obesity in older people. J Gerontol A Biol Sci Med Sci. 2010; 65:377-81. https://doi.org/10.1093/gerona/glp186 PMID:19942592
17. Rietman ML, van der A DL, van Oostrom SH, Picavet $H S$, Dollé ME, van Steeg $H$, Verschuren WM, Spijkerman AM. The Association between BMI and Different Frailty Domains: A U-Shaped Curve? J Nutr Health Aging. 2018; 22:8-15. https://doi.org/10.1007/s12603-016-0854-3 PMID:29300416
18. Watanabe D, Yoshida T, Watanabe Y, Yamada Y, Kimura M, Kyoto-Kameoka Study Gr. A U-Shaped Relationship Between the Prevalence of Frailty and Body Mass Index in Community-Dwelling Japanese Older Adults: The Kyoto-Kameoka Study. J Clin Med. 2020; 9:1367.
https://doi.org/10.3390/icm9051367 PMID:32384756
19. Szanton SL, Seplaki CL, Thorpe RJ Jr, Allen JK, Fried LP. Socioeconomic status is associated with frailty: the Women's Health and Aging Studies. J Epidemiol Community Health. 2010; 64:63-67. https://doi.org/10.1136/jech.2008.078428 PMID:19692719
20. Etman A, Burdorf A, Van der Cammen TJ, Mackenbach JP, Van Lenthe FJ. Socio-demographic determinants of worsening in frailty among community-dwelling older people in 11 European countries. J Epidemiol Community Health. 2012; 66:1116-21.
https://doi.org/10.1136/jech-2011-200027
PMID:22544921
21. Hoogendijk EO, van Hout HP, Heymans MW, van der Horst HE, Frijters DH, Broese van Groenou MI, Deeg DJ, Huisman M. Explaining the association between educational level and frailty in older adults: results from a 13-year longitudinal study in the Netherlands. Ann Epidemiol. 2014; 24:538-44.e2. https://doi.org/10.1016/i.annepidem.2014.05.002 PMID:24935466
22. Atkins JL, Jylhava J, Pedersen N, Magnusson P, Lu Y, Wang Y, Hagg S, Melzer D, Williams D, Pilling LC. A Genome-Wide Association Study of the Frailty Index Highlights Synaptic Pathways in Aging. medRxiv. 2019. https://doi.org/10.1101/19007559
23. van der Sluis S, Posthuma D, Dolan CV. A note on false positives and power in $G \times E$ modelling of twin data. Behav Genet. 2012; 42:170-86. https://doi.org/10.1007/s10519-011-9480-3 PMID:21748401
24. Verhulst B, Prom-Wormley E, Keller M, Medland S, Neale MC. Type I Error Rates and Parameter Bias in Multivariate Behavioral Genetic Models. Behav Genet. 2019; 49:99-111.
https://doi.org/10.1007/s10519-018-9942-y PMID:30569348
25. Young Al. Solving the missing heritability problem. PLoS Genet. 2019; 15:e1008222.
https://doi.org/10.1371/journal.pgen. 1008222 PMID:31233496
26. Wainschtein P, Jain D, Zheng Z, Cupples LA, Shadyab AH, McKnight B, Shoemaker BM, Mitchell BD, Psaty BM, Kooperberg C, Liu CT, et al. Recovery of trait heritability from whole genome sequence data. bioRxiv. 2021.
https://doi.org/10.1101/588020
27. Chen J, Yu J. Sex Differences in Genetic and Environmental Influences on Adolescent Depressive Symptoms: A Meta-Analytic Review. Depress Res Treat. 2015; 2015:476238. https://doi.org/10.1155/2015/476238 PMID:26649194
28. Hartvigsen J, Nielsen J, Kyvik KO, Fejer R, Vach W, lachine I, Leboeuf-Yde C. Heritability of spinal pain and consequences of spinal pain: a comprehensive genetic epidemiologic analysis using a population-based sample of 15,328 twins ages 20-71 years. Arthritis Rheum. 2009; 61:1343-51.
https://doi.org/10.1002/art. 24607 PMID:19790135
29. Lind MJ, Aggen SH, Kirkpatrick RM, Kendler KS, Amstadter AB. A Longitudinal Twin Study of Insomnia Symptoms in Adults. Sleep. 2015; 38:1423-30.
https://doi.org/10.5665/sleep. 4982
PMID:26132482
30. Gordon EH, Hubbard RE. Do sex differences in chronic disease underpin the sex-frailty paradox? Mech Ageing Dev. 2019; 179:44-50.
https://doi.org/10.1016/i.mad.2019.02.004 PMID: $\underline{\underline{0825457}}$
31. Schousboe K, Willemsen G, Kyvik KO, Mortensen J, Boomsma DI, Cornes BK, Davis CJ, Fagnani C, Hjelmborg J, Kaprio J, De Lange M, Luciano M, Martin NG, et al. Sex differences in heritability of BMI: a comparative study of results from twin studies in eight countries. Twin Res. 2003; 6:409-21.
https://doi.org/10.1375/136905203770326411 PMID:14624725
32. Mekli K, Marshall A, Nazroo J, Vanhoutte B, Pendleton N . Genetic variant of Interleukin-18 gene is associated with the Frailty Index in the English Longitudinal Study of Ageing. Age Ageing. 2015; 44:938-42.
https://doi.org/10.1093/ageing/afv122
PMID:26396182
33. Inglés M, Mas-Bargues C, Gimeno-Mallench L, CruzGuerrero R, García-García FJ, Gambini J, Borrás C, Rodríguez-Mañas L, Viña J. Relation Between Genetic Factors and Frailty in Older Adults. J Am Med Dir Assoc. 2019; 20:1451-57.
https://doi.org/10.1016/i.jamda.2019.03.011 PMID:31078485
34. Akiyama M, Okada Y, Kanai M, Takahashi A, Momozawa Y, Ikeda M, Iwata N, Ikegawa S, Hirata M, Matsuda K, Iwasaki M, Yamaji T, Sawada N, et al. Genome-wide association study identifies 112 new loci for body mass index in the Japanese population. Nat Genet. 2017; 49:1458-67. https://doi.org/10.1038/ng. 3951 PMID:28892062
35. Locke AE, Kahali B, Berndt SI, Justice AE, Pers TH, Day FR, Powell C, Vedantam S, Buchkovich ML, Yang J, Croteau-Chonka DC, Esko T, Fall T, et al. Genetic studies of body mass index yield new insights for obesity biology. Nature. 2015; 518:197-206.
https://doi.org/10.1038/nature14177
PMID: 25673413
36. Huibregtse BM, Newell-Stamper BL, Domingue BW, Boardman JD. Genes Related to Education Predict Frailty Among Older Adults in the United States. J Gerontol B Psychol Sci Soc Sci. 2021; 76:173-83. https://doi.org/10.1093/geronb/gbz092 PMID:31362310
37. Belsky DW, Domingue BW, Wedow R, Arseneault L, Boardman JD, Caspi A, Conley D, Fletcher JM, Freese J, Herd P, Moffitt TE, Poulton R, Sicinski K, et al. Genetic analysis of social-class mobility in five longitudinal studies. Proc Natl Acad Sci USA. 2018; 115:E7275-84. https://doi.org/10.1073/pnas. 1801238115 PMID:29987013
38. van der Heide I, Wang J, Droomers M, Spreeuwenberg P, Rademakers J, Uiters E. The relationship between health, education, and health literacy: results from the Dutch Adult Literacy and Life Skills Survey. J Health Commun. 2013 (Suppl 1); 18:172-84. https://doi.org/10.1080/10810730.2013.825668 PMID:24093354
39. Lastrucci V, Lorini C, Caini S, Bonaccorsi G, and Florence Health Literacy Research Group. Health literacy as a mediator of the relationship between socioeconomic status and health: A cross-sectional study in a population-based sample in Florence. PLoS One. 2019; 14:e0227007.
https://doi.org/10.1371/journal.pone. 0227007 PMID:31869381
40. Mackian S. A Review of Health Seeking Behaviour: Problems and Prospects. Heal Syst Dev Program.

Manchester; 2003.
http://r4d.dfid.gov.uk/pdf/outputs/healthsysdev kp/0
5-03 health seeking behaviour.pdf
41. Johnson W, Kyvik KO, Mortensen EL, Skytthe A, Batty GD, Deary IJ. Education reduces the effects of genetic susceptibilities to poor physical health. Int J Epidemiol. 2010; 39:406-14.
https://doi.org/10.1093/ije/dyp314 PMID:19861402
42. Li X, Ploner A, Karlsson IK, Liu X, Magnusson PK, Pedersen NL, Hägg S, Jylhävä J. The frailty index is a predictor of cause-specific mortality independent of familial effects from midlife onwards: a large cohort study. BMC Med. 2019; 17:94.
https://doi.org/10.1186/s12916-019-1331-8 PMID:31088449
43. Theou O, O'Connell MD, King-Kallimanis BL, O'Halloran AM, Rockwood K, Kenny RA. Measuring frailty using self-report and test-based health measures. Age Ageing. 2015; 44:471-77.
https://doi.org/10.1093/ageing/afv010 PMID: 25687601
44. Barnes JC, Wright JP, Boutwell BB, Schwartz JA, Connolly EJ, Nedelec JL, Beaver KM. Demonstrating the validity of twin research in criminology. Criminology. 2014; 52:588-626.
https://doi.org/10.1111/1745-9125.12049
45. Zagai U, Lichtenstein P, Pedersen NL, Magnusson PK. The Swedish Twin Registry: Content and Management as a Research Infrastructure. Twin Res Hum Genet. 2019; 22:672-80.
https://doi.org/10.1017/thg.2019.99
PMID:31747977
46. Lichtenstein P, Sullivan PF, Cnattingius S, Gatz M, Johansson S, Carlström E, Björk C, Svartengren M, Wolk A, Klareskog L, de Faire U, Schalling M, Palmgren J, Pedersen NL. The Swedish Twin Registry in the third millennium: an update. Twin Res Hum Genet. 2006; 9:875-82.
https://doi.org/10.1375/183242706779462444 PMID:17254424
47. Lichtenstein P, De Faire U, Floderus B, Svartengren M, Svedberg P, Pedersen NL. The Swedish Twin Registry: a unique resource for clinical, epidemiological and genetic studies. J Intern Med. 2002; 252:184-205. https://doi.org/10.1046/i.1365-2796.2002.01032.x PMID: 12270000
48. Neale MC, Maes HHM. Methodology for Genetic Studies of Twins and Families. Dordrecht: Kluwer Academic Publishers; 2004.
http://ibgwww.colorado.edu/workshop2004/cdrom/H TML/book2004a.pdf
49. Purcell S. Variance components models for geneenvironment interaction in twin analysis. Twin Res. 2002; 5:554-71.
https://doi.org/10.1375/136905202762342026
PMID:12573187

## SUPPLEMENTARY MATERIALS

## Supplementary Figures



Supplementary Figure 1. Variance components of frailty index (FI) by (A) body mass index (BMI) and (B) education from moderation analysis, stratified by sex. First row shows the absolute variance of FI, while the second row shows the proportion of FI variance explained by additive genetic (A), dominance genetic (D) and unique environmental (E) factors, with changes in BMI and education. Variance estimates of moderation by BMI were obtained from the full ADE bivariate moderation model between FI and BMI ; while the variance estimates of moderation by education were obtained from the ADE extended univariate moderation model between FI and education. Quantitative sexdifferences were allowed in the models to obtain estimates separately for men and women. Models were adjusted for age.


Supplementary Figure 2. Common and unique variance components of frailty index (FI) by body mass index (BMI) from moderation analysis, stratified by sex. First row shows the absolute variance of FI , while the second row shows the proportion of FI variance explained by additive genetic (A), dominance genetic (D) and unique environmental (E) factors, with changes in BMI levels. Variance estimates were obtained from the full ADE bivariate moderation model between FI and BMI . Quantitative sex-differences were allowed in the models to obtain estimates separately for men and women. Models were adjusted for age.


Supplementary Figure 3. Variance components of square-root transformed frailty index [sqrt(FI)] by (A) body mass index (BMI) and (B) education from moderation analysis, stratified by sex. First row shows the absolute variance of sqrt(FI), while the second row shows the proportion of sqrt(FI) variance explained by additive genetic (A), dominance genetic (D) and unique environmental (E) factors, with changes in BMI and education. Variance estimates of moderation by BMI were obtained from the full ADE bivariate moderation model between sqrt(FI) and BMI; while variance estimates of moderation by education were obtained from the ADE extended univariate moderation model between sqrt(FI) and education. Quantitative sex-differences were allowed in the models to obtain estimates separately for men and women. Models were adjusted for age.


Supplementary Figure 4. Full bivariate moderation model between frailty index (FI) and body mass index (BMI) (for one twin). A, additive genetic factors; D, dominance genetic factors; E, unique environmental factors. AC, DC and EC indicate genetic and environmental influences common to FI and BMI ; while $\mathrm{AU}, \mathrm{DU}$ and EU indicate genetic and environmental influences unique to FI . Total variance of FI by BMI is the sum of common and unique variance estimates; for example, the total additive genetic variance components of FI by BMI can be calculated as: $(\mathrm{ac}+\beta \mathrm{ac} \mathrm{BMI}) 2+(\mathrm{au}+\beta a \mathrm{BMI}) 2$.


Supplementary Figure 5. Extended univariate moderation model between frailty index (FI) and education (for one twin). A, additive genetic factors; D , dominance genetic factors; E , unique environmental factors. Mean of FI is adjusted for the moderator (i.e. education) of both the individual and his/her co-twin.


Supplementary Figure 6. Distribution of frailty index (FI) among men and women ( $\mathrm{n}=42,994$ ). Left panel shows the distribution of the untransformed FI, while right panel shows the distribution of the square-root transformed FI. Red color indicates men, while green color indicates women.

## Supplementary Tables

## Supplementary Table 1. List of the 44 frailty items and the scoring used for construction of frailty index (FI).

| No. | Frailty item | Scoring |
| :---: | :---: | :---: |
| 1 | General health status | $\begin{gathered} \text { Excellent }=0 ; \text { Good=0.25; Average= }=0.5 ; \text { Not so } \\ \text { good }=0.75 ; \text { Bad=1 } \end{gathered}$ |
| 2 | Health status prevents from doing things normally would like to do | Not at all $=0$; To some extent $=0.5$; <br> A great deal=1 |
| 3 | Serious infections per year (other than respiratory) | $0-1$ time $=0 ; 2-5$ times $=0.5 ; \geq 5$ times $=1$ |
| 4 | Buzzing in ears | No=0; One ear/ both ears=1 |
| 5 | Angina pectoris | No=0; Yes=1 |
| 6 | Heart attack | No=0; Yes=1 |
| 7 | Heart failure | No=0; Yes=1 |
| 8 | High blood pressure | No=0; Yes=1 |
| 9 | Lipid disorder (e.g. high cholesterol, high triglycerides) | No=0; Yes=1 |
| 10 | Vascular spasm in legs (intermittent claudication) | No=0; Yes=1 |
| 11 | Clot in leg (venous thrombosis) | No=0; Yes=1 |
| 12 | Cerebral hemorrhage or clot in brain (stroke) | No=0; Yes=1 |
| 13 | TIA attacks (temporary weakness, paralysis or reduction of sensibility) | No=0; Yes=1 |
| 14 | Irregular cardiac rhythm/ atrial fibrillation | No=0; Yes=1 |
| 15 | Chronic lung disease (incl. chronic bronchitis, emphysema) | No=0; Yes=1 |
| 16 | Dizziness | No=0; Yes=1 |
| 17 | Rheumatoid arthritis | No=0; Yes=1 |
| 18 | Knee joint problem | No=0; Yes=1 |
| 19 | Sciatica | No=0; Yes=1 |
| 20 | Osteoporosis | No=0; Yes=1 |
| 21 | Hip joint problem | No=0; Yes=1 |
| 22 | Back pain | No=0; Yes=1 |
| 23 | Neck pain | No=0; Yes=1 |
| 24 | Diabetes (incl. old age diabetes; excl. pregnancy diabetes) | No=0; Yes=1 |
| 25 | Goiter | No=0; Yes=1 |
| 26 | Glandular diseases (excl. goiter) | No=0; Yes=1 |
| 27 | Gall bladder problem | No=0; Yes=1 |
| 28 | Liver disease (e.g. cirrhosis) | No=0; Yes=1 |
| 29 | Gout | No=0; Yes=1 |
| 30 | Kidney disease | No=0; Yes=1 |
| 31 | Stomach or intestine problems | No=0; Yes=1 |
| 32 | Recurring urinary tract problems | No=0; Yes=1 |
| 33 | Cancer, tumor disease or leukemia | No=0; Yes=1 |
| 34 | Migraine | No=0; Yes=1 |
| 35 | Asthma | No=0; Yes=1 |
| 36 | Allergy | No=0; Yes=1 |
| 37 | Recurrent periods of coughing | No=0; Yes=1 |
| 38 | Feeling depressed during the past week | Never/ almost never=0; Seldom=0.5; Often/ always/ almost always $=1$ |
| 39 | Feeling happy during the past week | Never/ almost never=0; Seldom=0.5; Often/ always/ almost always $=1$ |
| 40 | Feeling lonely during the past week | Never/ almost never=0; Seldom=0.5; Often/ always/ almost always $=1$ |
| 41 | Physical handicap | No=0; Yes=1 |
| 42 | Crohn's disease or ulcerative colitis | No=0; Yes=1 |
| 43 | Vision | Good=0; Reduced=0.5; Highly reduced/ blind=1 |
| 44 | Hearing | Good=0; Reduced=0.5; Highly reduced=1 |

Supplementary Table 2. Unadjusted phenotypic correlations, intraclass correlations and cross-twin cross-trait correlations for frailty index (FI), body mass index (BMI) and education.

| Zygosity | Phenotypic correlations |  |  | Intraclass correlations |  |  | Cross-twin cross-trait correlations |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | FI and BMI | FI and Education | FI | BMI | Education | FI and BMI | FI and Education |
| Total | $0.13(0.12,0.14)$ | $-0.17(-0.18,-0.16)$ |  |  |  |  |  |
| MZ | $0.12(0.09,0.14)$ | $-0.17(-0.19,-0.15)$ | $0.53(0.51,0.56)$ | $0.69(0.67,0.70)$ | $0.71(0.69,0.72)$ | $0.09(0.07,0.12)$ | $-0.16(-0.18,-0.13)$ |
| DZ | $0.14(0.13,0.15)$ | $-0.17(-0.18,-0.16)$ | $0.23(0.21,0.25)$ | $0.24(0.22,0.26)$ | $0.50(0.49,0.52)$ | $0.07(0.06,0.08)$ | $-0.16(-0.17,-0.15)$ |
| MZ males | $0.11(0.08,0.14)$ | $-0.17(-0.20,-0.14)$ | $0.47(0.43,0.51)$ | $0.66(0.63,0.68)$ | $0.69(0.67,0.72)$ | $0.09(0.05,0.12)$ | $-0.14(-0.17,-0.10)$ |
| MZ females | $0.16(0.13,0.19)$ | $-0.18(-0.21,-0.15)$ | $0.55(0.52,0.58)$ | $0.69(0.67,0.71)$ | $0.72(0.70,0.74)$ | $0.14(0.11,0.17)$ | $-0.17(-0.20,-0.14)$ |
| DZ males | $0.10(0.07,0.12)$ | $-0.17(-0.19,-0.15)$ | $0.19(0.15,0.23)$ | $0.27(0.24,0.31)$ | $0.50(0.47,0.53)$ | $0.03(0.00,0.06)$ | $-0.15(-0.18,-0.13)$ |
| DZ females | $0.20(0.18,0.22)$ | $-0.17(-0.19,-0.15)$ | $0.28(0.25,0.31)$ | $0.32(0.29,0.35)$ | $0.57(0.55,0.59)$ | $0.12(0.09,0.14)$ | $-0.16(-0.19,-0.14)$ |
| DZ opposite-sex | $0.10(0.08,0.13)$ | $-0.17(-0.19,-0.15)$ | $0.21(0.18,0.23)$ | $0.18(0.16,0.21)$ | $0.47(0.45,0.49)$ | $0.03(0.00,0.06)$ | $-0.14(-0.17,-0.12)$ |

Note: MZ, monozygotic twins; DZ, dizygotic twins. Phenotypic correlations are the within-individual correlations between FI and BMI, and between FI and education. Intraclass correlations indicate the extent to which each trait correlates within twin pairs. Cross-twin cross-trait correlations show the extent to which FI of the first twin correlate with the other trait (i.e. BMI or education) of the second twin. 95\% confidence intervals are presented in parentheses.

Supplementary Table 3. Model fitting results from bivariate models of frailty index (FI) with body mass index (BMI) and education.

| Model | -2LL | df | AIC | $\Delta \mathbf{L L}$ | $\Delta \mathrm{df}$ | $p$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bivariate FI and BMI |  |  |  |  |  |  |
| Saturated | 203422.9 | 53568 | 96287 | - | - | - |
| ACE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 203503.7 | 53602 | 96300 | 80.8 | 34 | $1.12 \times 10^{-5}$ |
| No sex difference | 203548.6 | 53609 | 96331 | 125.6 | 41 | $1.60 \times 10^{-10}$ |
| ADE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 203459.9 | 53602 | 96256 | 36.9 | 34 | 0.335 |
| No sex difference | 203485.9 | 53605 | 96276 | 63.0 | 37 | $4.90 \times 10^{-3}$ |
| AE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 203503.7 | 53608 | 96288 | 80.8 | 40 | $1.43 \times 10^{-4}$ |
| No sex difference | 203548.6 | 53612 | 96325 | 125.6 | 44 | $8.73 \times 10^{-10}$ |
| Bivariate FI and education |  |  |  |  |  |  |
| Saturated | 198109.0 | 54150 | 89809 | - | - | - |
| ACE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 198175.0 | 54182 | 89811 | 65.9 | 32 | $3.84 \times 10^{-4}$ |
| No sex difference | 198208.4 | 54189 | 89830 | 99.4 | 39 | $3.53 \times 10^{-7}$ |
| ADE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 198300.4 | 54182 | 89936 | 191.4 | 32 | $1.29 \times 10^{-24}$ |
| No sex difference | 198315.7 | 54185 | 89946 | 206.7 | 35 | $3.18 \times 10^{-26}$ |
| AE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 198328.3 | 54188 | 89952 | 219.3 | 38 | $2.39 \times 10^{-27}$ |
| No sex difference | 198360.8 | 54192 | 89977 | 251.8 | 42 | $1.02 \times 10^{-31}$ |

Note: AIC, Akaike's Information Criterion; LL, log-likelihood; df, degrees of freedom; p, p-values of likelihood ratio tests compared with the saturated models. Opposite-sex twins were excluded in the bivariate analyses. All bivariate models between FI and education had significant worse model fit than the saturated model, since an ADE model fits better for FI while an ACE model fits better for education. During assumption testing, equating means of education across zygosity resulted in a significantly worse fit of data compared to the saturated model; therefore, means of education were estimated separately across zygosity in bivariate models between FI and education. All models were adjusted for age (as linear effect for FI , and linear+quadratic effect for BMI and education). Best-fitting models are shown in bold, and the parameter estimates of these models are presented in Supplementary Table 4.

Supplementary Table 4. Parameter estimates ( $95 \% \mathrm{CI}$ ) from the best-fitting bivariate models.

| Model | Variance components |  |  |  | Genetic and environmental correlations |  |  |  | Bivariate heritability |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | D/C | H | E | $r_{\text {A }}$ | $r_{\mathrm{D}} / r_{\mathrm{C}}$ | $r_{\text {H }}$ | $r_{\text {E }}$ | Bivariate A | Bivariate D/C | Bivariate H | Bivariate E |
| ADE bivariate model between FI and BMI |  |  |  |  |  |  |  |  |  |  |  |  |
| FI | $\begin{aligned} & \text { M: 6\% } \\ & (0,22) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 38 \% \\ & (21,54) \end{aligned}$ | $\begin{aligned} & \text { M: 44\% } \\ & (40,48) \end{aligned}$ | $\begin{aligned} & \text { F: } 56 \% \\ & (52,60) \end{aligned}$ |  |  |  |  |  |  |  |  |
| BMI | $\begin{aligned} & \text { F: } 42 \% \\ & (28,55) \end{aligned}$ | $\begin{aligned} & \text { F: } 11 \% \\ & (0,25) \end{aligned}$ | $\begin{aligned} & \text { F: } 53 \% \\ & (50,55) \end{aligned}$ | $\begin{aligned} & \text { F: } 47 \% \\ & (45,50) \end{aligned}$ |  |  |  |  |  |  |  |  |
|  | $\begin{aligned} & \mathrm{M}: 41 \% \\ & (27,55) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 25 \% \\ & (10,39) \end{aligned}$ | $\begin{aligned} & \text { M: 66\% } \\ & (64,68) \end{aligned}$ | $\begin{aligned} & \text { M: 34\% } \\ & (32,36) \end{aligned}$ | $\begin{gathered} \text { M: } 0.61 \\ (-0.25,1.46) \end{gathered}$ | $\begin{gathered} \text { M: } 0.01 \\ (-0.33,0.36) \end{gathered}$ | $\begin{gathered} \text { M: } 0.19 \\ (0.14,0.23) \end{gathered}$ | $\begin{gathered} \text { M: } 0.05 \\ (0.01,0.10) \end{gathered}$ | $\begin{aligned} & \mathrm{M}: 78 \% \\ & (-3,159) \end{aligned}$ | $\begin{gathered} \text { M: 3\% } \\ (-82,88) \end{gathered}$ | $\begin{aligned} & \text { M: 81\% } \\ & (65,97) \end{aligned}$ | $\begin{gathered} \text { M: } 19 \% \\ (3,35) \end{gathered}$ |
|  | $\begin{aligned} & \text { F: } 56 \% \\ & (42,69) \end{aligned}$ | $\begin{aligned} & \text { F: } 13 \% \\ & (0,27) \end{aligned}$ | $\begin{aligned} & \text { F: } 69 \% \\ & (67,71) \end{aligned}$ | $\begin{aligned} & \text { F: } 31 \% \\ & (29,33) \end{aligned}$ | $\begin{gathered} \text { F: } 0.48 \\ (0.29,0.67) \end{gathered}$ | $\begin{gathered} \text { F: }-0.64 \\ (-1.70,0.42) \end{gathered}$ | $\begin{gathered} \text { F: } 0.26 \\ (0.22,0.29) \end{gathered}$ | $\begin{gathered} \text { F: } 0.06 \\ (0.02,0.10) \end{gathered}$ | $\begin{aligned} & \text { F: } 130 \% \\ & (79,181) \end{aligned}$ | $\begin{aligned} & \text { F: }-43 \% \\ & (-96,10) \end{aligned}$ | $\begin{aligned} & \text { F: } 87 \% \\ & (78,95) \end{aligned}$ | $\begin{aligned} & \text { F: } 13 \% \\ & (5,22) \end{aligned}$ |

ACE bivariate model between FI and education

| FI | $\begin{aligned} & \mathrm{M}: 39 \% \\ & (35,43) \end{aligned}$ | $\begin{gathered} \text { M: } 1 \% \\ (0,3) \end{gathered}$ | $\begin{aligned} & \mathrm{M}: 39 \% \\ & (35,43) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 60 \% \\ & (56,63) \end{aligned}$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { F: } 51 \% \\ & (48,54) \end{aligned}$ | $\begin{gathered} \text { F: } 1 \% \\ (0,3) \end{gathered}$ | $\begin{aligned} & \text { F: } 51 \% \\ & (48,54) \end{aligned}$ | $\begin{aligned} & \text { F: 48\% } \\ & (46,51) \end{aligned}$ |  |  |  |  |  |  |  |  |
| Education | $\begin{aligned} & \mathrm{M}: 41 \% \\ & (34,48) \end{aligned}$ | $\begin{aligned} & \text { M: 25\% } \\ & (19,31) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 41 \% \\ & (34,48) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 35 \% \\ & (32,37) \end{aligned}$ | $\begin{gathered} \mathrm{M}:-0.02 \\ (-0.15,0.11) \end{gathered}$ | $\begin{gathered} \mathrm{M}:-1.00 \\ (-1.00,-1.00) \end{gathered}$ | $\begin{gathered} \mathrm{M}:-0.02 \\ (-0.15,0.11) \end{gathered}$ | $\begin{gathered} \text { M: -0.06 } \\ (-0.10,-0.01) \end{gathered}$ | $\begin{gathered} \text { M: } 8 \% \\ (-46,61) \end{gathered}$ | $\begin{aligned} & \text { M: 65\% } \\ & (23,107) \end{aligned}$ | $\begin{gathered} \text { M: } 8 \% \\ (-46,61) \end{gathered}$ | $\begin{gathered} \mathrm{M}: 28 \% \\ (6,49) \end{gathered}$ |
|  | $\begin{aligned} & \text { F: } 35 \% \\ & (29,42) \end{aligned}$ | $\begin{aligned} & \text { F: } 29 \% \\ & (23,34) \end{aligned}$ | $\begin{aligned} & \text { F: } 35 \% \\ & (29,42) \end{aligned}$ | $\begin{aligned} & \text { F: } 36 \% \\ & (34,38) \end{aligned}$ | $\begin{gathered} \text { F: }-0.04 \\ (-0.15,0.07) \end{gathered}$ | $\begin{gathered} \text { F: }-1.00 \\ (-1.00,-1.00) \end{gathered}$ | $\begin{gathered} \text { F: }-0.04 \\ (-0.15,0.07) \end{gathered}$ | $\begin{gathered} \text { F: }-0.01 \\ (-0.05,0.03) \end{gathered}$ | $\begin{aligned} & \text { F: } 22 \% \\ & (-40,84) \end{aligned}$ | $\begin{gathered} \text { F: } 74 \% \\ (22,126) \end{gathered}$ | $\begin{gathered} \text { F: } 22 \% \\ (-40,84) \end{gathered}$ | $\begin{gathered} \text { F: } 4 \% \\ (-17,25) \end{gathered}$ |

Note: BMI, body mass index; FI, frailty index; CI, Wald-type confidence interval; A, additive genetic factors; D, dominance genetic factors; $H$, total genetic factors/ broad-sense heritability; $C$, common environmental factors; $E$, unique environmental factors; $r$, correlation between variance components. $M$ and $F$ represents parameter estimates for men and women respectively. Bivariate heritability is the proportion of phenotypic correlation explained by genetic and environmental factors.

Supplementary Table 5. Model fitting results from moderation models of frailty index (FI) by body mass index (BMI).

| Model | -2LL | df | AIC | Comp | $\Delta \mathbf{L L}$ | $\Delta \mathrm{df}$ | $p$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ACE bivariate |  |  |  |  |  |  |  |
| 1. Full moderation | 146418.0 | 38963 | 68492 | - | - | - | - |
| ADE bivariate |  |  |  |  |  |  |  |
| 2. Full moderation | 146354.9 | 38963 | 68429 | - | - | - | - |
| 3. Drop all covariance moderation | 146453.0 | 38969 | 68515 | 2 | 98.1 | 6 | $6.29 \times 10^{-19}$ |
| 4. Drop all moderation | 146653.5 | 38975 | 68704 | 2 | 298.7 | 12 | $9.01 \times 10^{-57}$ |
| AE bivariate |  |  |  |  |  |  |  |
| 5. Full moderation | 146489.1 | 38973 | 68543 | 2 | 134.2 | 10 | $6.34 \times 10^{-24}$ |
| 6. Drop all covariance moderation | 146615.8 | 38977 | 68662 | 5 | 126.7 | 4 | $1.96 \times 10^{-26}$ |
| 7. Drop all moderation | 146697.7 | 38981 | 68736 | 5 | 208.6 | 8 | $9.73 \times 10^{-41}$ |

Note: AIC, Akaike's Information Criterion; Comp, model of comparison; df, degrees of freedom; LL, Log-likelihood; $p$, $p$-values of likelihood ratio tests compared with the models of comparison. Opposite-sex twins were excluded in the models. Quantitative sex differences were allowed to obtain separate estimates for men and women. All models were adjusted for age (as linear effect for FI , and linear+quadratic effect for BMI ). Best-fitting model is shown in bold.

Supplementary Table 6. Model fitting results from moderation models of frailty index (FI) by education.

| Models | -2LL | df | AIC | Comp | $\Delta$ LL | $\Delta$ df | $p$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ACE bivariate |  |  |  |  |  |  |  |
| 1. Full moderation | 145282.4 | 40231 | 64820 | - | - | - | - |
| 2. Drop all covariance moderation | 145289.7 | 40237 | 64816 | 1 | 7.3 | 6 | 0.297 |
| 3. Drop all moderation | 145537.7 | 40243 | 65052 | 1 | 255.3 | 12 | $1.09 \times 10^{-47}$ |
| ADE bivariate |  |  |  |  |  |  |  |
| 4. Full moderation | 145418.6 | 40231 | 64957 | - | - | - | - |
| 5. Drop all covariance moderation | 145423.2 | 40237 | 64949 | 4 | 4.6 | 6 | 0.592 |
| 6. Drop all moderation | 145665.6 | 40243 | 40243 | 4 | 247.0 | 12 | $5.71 \times 10^{-46}$ |
| AE bivariate |  |  |  |  |  |  |  |
| 7. Full moderation | 145450.9 | 40241 | 64969 | 1 | 168.4 | 10 | $5.92 \times 10^{-31}$ |
| 8. Drop all covariance moderation | 145454.7 | 40245 | 64965 | 7 | 3.8 | 4 | 0.432 |
| 9. Drop all moderation | 145694.2 | 40249 | 65196 | 7 | 243.3 | 8 | $4.42 \times 10^{-48}$ |
| ACE extended univariate |  |  |  |  |  |  |  |
| 10. Full moderation | 47816.3 | 20109 | 7598 | - | - | - | - |
| 11. Drop all moderation | 48064.9 | 20115 | 7835 | 10 | 248.6 | 6 | $8.24 \times 10^{-51}$ |
| ADE extended univariate |  |  |  |  |  |  |  |
| 12. Full moderation | 47793.4 | 20109 | 7575 | - | - | - | - |
| 13. Drop all moderation | 48039.4 | 20115 | 7809 | 12 | 246.0 | 6 | $2.90 \times 10^{-50}$ |
| AE extended univariate |  |  |  |  |  |  |  |
| 14. Full moderation | 47823.0 | 20113 | 7597 | 12 | 29.6 | - | - |
| 15. Drop all moderation | 48064.9 | 20117 | 7831 | 14 | 241.9 | 4 | $3.69 \times 10^{-51}$ |

Note: AIC, Akaike's Information Criterion; Comp, model of comparison; df, degrees of freedom; LL, log-likelihood; p, p-values of likelihood ratio tests compared with the models of comparison. Opposite-sex twins were excluded in the models. Quantitative sex differences were allowed to obtain separate estimates for men and women. Bivariate models were adjusted for age (as linear effect for FI, and linear+quadratic effect for education); extended univariate models were adjusted for age, as well as education for both the individual and the co-twin. Best-fitting model is shown in bold. Due to the non-significant moderation on the covariance between FI and education in the bivariate models, the more parsimonious ADE extended univariate model was used.

Supplementary Table 7. Model fitting results and parameter estimates from univariate sex-limitation models of the square-root transformed frailty index [sqrt(FI)].

| Model | Model fit statistics |  |  |  | Parameter estimates for men and women (95\% CI) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | AIC | $\Delta \mathbf{L L}$ | $\Delta \mathrm{df}$ | $p$ | A | D/C | H | E | $r_{\text {fm }}$ |
| Saturated | -146609 | - | - | - | - | - | - | - | - |
| ADE full sex-limitation | -146620 | 20.6 | 16 | 0.196 | $\begin{gathered} \text { M: } 7 \%(0,23) \\ \text { F: } 40 \%(27,53) \end{gathered}$ | $\begin{gathered} \text { M: } 34 \%(17,50) \\ \text { F: } 10 \%(0,24) \end{gathered}$ | $\begin{aligned} & \text { M: } 41 \%(38,45) \\ & \text { F: } 50 \%(47,53) \end{aligned}$ | $\begin{gathered} \text { M: } 59 \%(55,62) \\ \text { F: } 50 \%(47,53) \end{gathered}$ | 0.68 (0.49, 0.93$)$ |
| ADE quantitative sex-limitation | -146621 | 21.4 | 17 | 0.208 | $\begin{gathered} \text { M: } 0 \%(0,1) \\ \text { F: } 40 \%(26,53) \end{gathered}$ | $\begin{gathered} \text { M: 41\% }(\mathbf{3 8}, \mathbf{4 5 )} \\ \mathrm{F}: 10 \%(0,24) \end{gathered}$ | $\begin{aligned} & \text { M: } 42 \%(38,45) \\ & \text { F: 50\% }(47,53) \end{aligned}$ | $\begin{aligned} & \text { M: } \mathbf{5 8 \%}(\mathbf{5 5}, \mathbf{6 2}) \\ & \text { F: 50\% }(\mathbf{4 7}, 53) \end{aligned}$ | 1.00 (NA) |
| ADE no sex difference | -146609 | 35.2 | 18 | 0.009 | $\begin{gathered} \text { M: } 0 \%(0,3) \\ \text { F: } 43 \%(29,57) \end{gathered}$ | $\begin{gathered} \text { M: } 46 \%(41,50) \\ \text { F: } 3 \%(0,17) \end{gathered}$ | $\begin{aligned} & \text { M: } 46 \%(44,48) \\ & \text { F: } 46 \%(44,48) \end{aligned}$ | $\begin{gathered} \text { M: } 54 \%(52,56) \\ \text { F: } 54 \%(52,56) \end{gathered}$ | 1.00 (NA) |
| ACE full sex-limitation | -146602 | 38.7 | 16 | 0.001 | $\begin{gathered} \text { M: } 38 \%(34,41) \\ \text { F: } 49 \%(46,52) \end{gathered}$ | $\begin{aligned} & \text { M: } 0 \%(0,0) \\ & \text { F: } 0 \%(0,0) \end{aligned}$ | $\begin{aligned} & \text { M: } 38 \%(34,41) \\ & \text { F: } 49 \%(46,52) \end{aligned}$ | $\begin{gathered} \text { M: } 62 \%(59,66) \\ \text { F: } 51 \%(48,54) \end{gathered}$ | 0.77 (0.65, 0.90) |
| AE full sex-limitation | -146606 | 38.7 | 18 | 0.003 | $\begin{gathered} \text { M: } 38 \%(34,41) \\ \text { F: } 49 \%(46,52) \end{gathered}$ | $\begin{aligned} & \text { M: } 0 \% \text { (NA) } \\ & \text { F: } 0 \% \text { (NA) } \end{aligned}$ | $\begin{aligned} & \text { M: } 38 \%(34,41) \\ & \text { F: } 49 \%(46,52) \end{aligned}$ | $\begin{aligned} & \text { M: } 62 \%(59,66) \\ & \text { F: } 51 \%(48,54) \end{aligned}$ | 0.77 (0.65, 0.90) |

Note: AIC, Akaike's Information Criterion; LL, log-likelihood; df, degrees of freedom; $p, p$-values of likelihood ratio tests compared with the saturated model. Cls are Wald-type confidence intervals with lower and upper bounds of 0 and 1 . A, additive genetic factors; D, dominance genetic factors; C, common environmental factors; H, total genetic factors/ broadsense heritability; E , unique environmental factors; $r_{\mathrm{fm}}$, genetic correlation between men and women, estimated using opposite-sex twins. M and F represents parameter estimates for men and women respectively. Full sex-limitation models allowed both quantitative and qualitative sex differences. In ADE quantitative sex-limitation model, $r_{f m}$ was fixed to be 1. In ADE no sex difference model, broad-sense heritability of men and women were equated, but variance difference between sex was allowed. ACE and AE sub-models are not shown as the full models fit significantly worse than the saturated model. All models were adjusted for age. Best-fitting model is shown in bold.

Supplementary Table 8. Model fitting results and parameter estimates from univariate sex-limitation models of the frailty index (FI) using "direct symmetric approach.

| Model | Model fit statistics |  |  |  | Parameter estimates for men and women (95\% CI) |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | AIC | $\Delta \mathrm{LL}$ | $\Delta \mathrm{df}$ | $p$ | A | D/C | H | E | $r_{\text {fm }}$ |
| Saturated | 19953 | - | - | - | - | - | - | - | - |
| ADE full sexlimitation | 19940 | 19.1 | 16 | 0.264 | $\begin{aligned} & \text { M: } 7 \%(-10,23) \\ & \text { F: } 41 \%(28,55) \end{aligned}$ | $\begin{gathered} \text { M: } 38 \%(20,55) \\ \text { F: } 11 \%(-3,25) \end{gathered}$ | $\begin{gathered} \text { M: } 44 \%(41,48) \\ \text { F: } 52 \%(50,55) \end{gathered}$ | $\begin{aligned} & \text { M: } 56 \%(52,59) \\ & \text { F: } 48 \%(45,50) \end{aligned}$ | 0.69 (0.41, 0.96) |
| ADE quantitative sex-limitation | 19939 | 19.7 | 17 | 0.288 | $\begin{gathered} \text { M: } 0 \%(0,1) \\ \text { F: } 41 \%(28,55) \end{gathered}$ | $\begin{aligned} & \text { M: 44\% }(41,48) \\ & \text { F: } 11 \%(-3,25) \end{aligned}$ | $\begin{aligned} & \text { M: 45\% }(41,48) \\ & \text { F: 52\% }(50,55) \end{aligned}$ | $\begin{aligned} & \text { M: 55\% }(52,59) \\ & \text { F: 48\% }(\mathbf{4 5}, 50) \end{aligned}$ | 1.00 (NA) |
| ADE no sex difference | 19949 | 32.1 | 18 | 0.021 | $\begin{gathered} \mathrm{M}: 0 \%(-1,2) \\ \mathrm{F}: 44 \%(31,58) \end{gathered}$ | $\begin{gathered} \mathrm{M}: 49 \%(45,52) \\ \mathrm{F}: 4 \%(-10,19) \end{gathered}$ | $\begin{aligned} & \text { M: } 49 \%(47,51) \\ & \text { F: } 49 \%(47,51) \end{aligned}$ | $\begin{aligned} & \text { M: } 51 \%(49,53) \\ & \text { F: } 51 \%(49,53) \end{aligned}$ | 1.00 (NA) |
| ACE full sexlimitation* | 19940 | 19.1 | 16 | 0.264 | $\begin{aligned} & \text { M: } 63 \%(53,74) \\ & \text { F: } 58 \%(49,66) \end{aligned}$ | $\begin{gathered} \text { M: }-19 \%(-27,-10) \\ \text { F: }-5 \%(-13,2) \end{gathered}$ | $\begin{aligned} & \text { M: } 63 \%(53,74) \\ & \text { F: } 51 \%(49,54) \end{aligned}$ | $\begin{aligned} & \text { M: } 56 \%(52,59) \\ & \text { F: } 48 \%(45,50) \end{aligned}$ | $0.24(-0.03,0.51)$ |
| AE full sex-limitation | 19957 | 40.4 | 18 | 0.002 | $\begin{aligned} & \text { M: } 41 \%(37,44) \\ & \text { F: } 51 \%(49,54) \end{aligned}$ | $\begin{aligned} & \text { M: } 0 \% \text { (NA) } \\ & \text { F: } 0 \% \text { (NA) } \end{aligned}$ | $\begin{aligned} & \text { M: } 41 \%(37,44) \\ & \text { F: } 51 \%(49,54) \end{aligned}$ | $\begin{aligned} & \text { M: } 59 \%(56,63) \\ & \text { F: } 49 \%(46,51) \end{aligned}$ | 0.76 (0.64, 0.88) |

Note: AIC, Akaike’s Information Criterion; LL, log-likelihood; df, degrees of freedom; p, p-values of likelihood ratio tests compared with the saturated model. Cls are Wald-type confidence intervals. Variance component estimates are allowed to be negative in the "direct symmetric approach" (Verhulst et al. 2019). A, additive genetic factors; D, dominance genetic factors; C, common environmental factors; H , total genetic factors/ broad-sense heritability; E , unique environmental factors; $r_{\mathrm{fm}}$, genetic correlation between men and women, estimated using opposite-sex twins. M and F represents parameter estimates for men and women respectively. Full sex-limitation models allowed both quantitative and qualitative sex differences. In ADE quantitative sex-limitation model, $r_{\mathrm{f}}$ was fixed to be 1. In ADE no sex difference model, broad-sense heritability of men and women were equated, but variance difference between sex was allowed. All models were adjusted for age. Best-fitting model is shown in bold.

* An ACE quantitative sex-limitation model cannot be fitted due to an issue with the expected opposite sex twin covariance of $\mathrm{V}\left(\mathrm{VCm}{ }^{*} \mathrm{VCf}\right)$ (using notation from Verhulst et al.) when one common environmental component was negative, a problem identified in Verhulst et al. (2019).
Supplementary Table 9. Model fitting results from bivariate models of frailty index (FI) with body mass index
(BMI) and education using "direct symmetric approach.

| Model | -2LL | df | AIC | $\Delta \mathrm{LL}$ | $\Delta \mathrm{df}$ | $p$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Bivariate FI and BMI |  |  |  |  |  |  |
| Saturated | 203422.9 | 53568 | 96287 | - | - | - |
| ACE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 203459.9 | 53602 | 96256 | 36.9 | 34 | 0.335 |
| No sex difference | 203510.4 | 53609 | 96292 | 87.5 | 41 | $3.26 \times 10^{-5}$ |
| ADE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 203459.9 | 53602 | 96256 | 36.9 | 34 | 0.335 |
| No sex difference | 203485.1 | 53605 | 96276 | 62.1 | 37 | $5.96 \times 10^{-3}$ |
| AE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 203503.7 | 53608 | 96288 | 80.8 | 40 | $1.43 \times 10^{-4}$ |
| No sex difference | 203548.6 | 53612 | 96325 | 125.6 | 44 | $8.72 \times 10^{-10}$ |
| Bivariate FI and education |  |  |  |  |  |  |
| Saturated | 198109.0 | 54150 | 89809 | - | - | - |
| ACE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 198147.1 | 54182 | 89783 | 38.1 | 32 | 0.213 |
| No sex difference | 198186.2 | 54189 | 89808 | 77.2 | 39 | $2.60 \times 10^{-4}$ |
| ADE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 198147.1 | 54182 | 89783 | 38.1 | 32 | 0.213 |
| No sex difference | 198162.6 | 54185 | 89793 | 53.6 | 35 | 0.023 |
| AE bivariate |  |  |  |  |  |  |
| Quantitative sex-limitation | 198328.3 | 54188 | 89952 | 219.3 | 38 | $2.39 \times 10^{-27}$ |
| No sex difference | 198360.8 | 54192 | 89977 | 251.8 | 42 | $1.02 \times 10^{-31}$ |

Note: AIC, Akaike's Information Criterion; LL, log-likelihood; df, degrees of freedom; p, p-values of likelihood ratio tests compared with the saturated models. Variance component estimates are allowed to be negative in the "direct symmetric approach" (Verhulst et al. 2019). Opposite-sex twins were excluded in the bivariate analyses. During assumption testing, equating means of education across zygosity resulted in a significantly worse fit of data compared to the saturated model; therefore, means of education were estimated separately across zygosity in bivariate models between Fl and education. All models were adjusted for age (as linear effect for FI , and linear+quadratic effect for BMI and education). Best-fitting models are shown in bold, and the parameter estimates of these models are presented in Supplementary Table 10.

Supplementary Table 10. Parameter estimates ( $95 \% \mathrm{Cl}$ ) from the best-fitting bivariate models using "direct symmetric approach".

| Model | Variance components |  |  |  | Genetic and environmental correlations |  |  |  | Bivariate heritability |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | D/C | H | E | $r_{\text {A }}$ | $r_{\mathrm{D}} / r_{\mathrm{C}}$ | $r_{\text {H }}$ | $r_{\text {E }}$ | Bivariate A | Bivariate D/C | Bivariate <br> H | Bivariate <br> E |
| ACE bivariate model between FI and BMI $\dagger$ |  |  |  |  |  |  |  |  |  |  |  |  |
| FI | $\begin{aligned} & \mathrm{M}: 63 \% \\ & (52,73) \end{aligned}$ | $\begin{aligned} & \mathrm{M}:-19 \% \\ & (-27,-10) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 63 \% \\ & (52,73) \end{aligned}$ | $\begin{aligned} & \text { F: } 56 \% \\ & (52,60) \end{aligned}$ |  |  |  |  |  |  |  |  |
| BMI | $\begin{aligned} & \text { F: } 58 \% \\ & (50,67) \end{aligned}$ | $\begin{aligned} & \text { F: }-5 \% \\ & (-13,2) \end{aligned}$ | $\begin{aligned} & \text { F: } 58 \% \\ & (50,67) \end{aligned}$ | $\begin{aligned} & \text { F: } 47 \% \\ & (45,50) \end{aligned}$ |  |  |  |  |  |  |  |  |
|  | $\begin{aligned} & \mathrm{M}: 78 \% \\ & (70,86) \end{aligned}$ | $\begin{gathered} \mathrm{M}:-12 \% \\ (-19,-5) \end{gathered}$ | $\begin{aligned} & \text { M: 78\% } \\ & (70,86) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 34 \% \\ & (34,36) \end{aligned}$ | $\begin{gathered} \text { M: } 0.15 \\ (0.05,0.24) \end{gathered}$ | M: N/A* | $\begin{gathered} \text { M: } 0.15 \\ (0.05,0.24) \end{gathered}$ | $\begin{gathered} \text { M: } 0.05 \\ (0.01,0.10) \end{gathered}$ | $\begin{aligned} & \text { M: } 82 \% \\ & (30,135) \end{aligned}$ | $\begin{aligned} & \mathrm{M}:-1 \% \\ & (-46,43) \end{aligned}$ | $\begin{aligned} & \text { M: } 82 \% \\ & (30,135) \end{aligned}$ | $\begin{gathered} \mathrm{M}: 19 \% \\ (3,35) \end{gathered}$ |
|  | $\begin{aligned} & \text { F: 75\% } \\ & (68,82) \end{aligned}$ | $\begin{aligned} & \mathrm{F}:-7 \% \\ & (-13,0) \end{aligned}$ | $\begin{aligned} & \text { F: 75\% } \\ & (68,82) \end{aligned}$ | $\begin{aligned} & \text { F: 31\% } \\ & (29,33) \end{aligned}$ | $\begin{gathered} \text { F: } 0.18 \\ (0.09,0.26) \end{gathered}$ | F: N/A* | $\begin{gathered} \text { F: } 0.18 \\ (0.09,0.26) \end{gathered}$ | $\begin{gathered} \text { F: } 0.06 \\ (0.02,0.10) \end{gathered}$ | $\begin{aligned} & \text { F: 65\% } \\ & (34,97) \end{aligned}$ | $\begin{aligned} & \text { F: } 22 \% \\ & (-6,49) \end{aligned}$ | $\begin{aligned} & \text { F: } 65 \% \\ & (34,97) \end{aligned}$ | $\begin{gathered} \text { F: } 13 \% \\ (5,22) \end{gathered}$ |

ADE bivariate model between FI and BMI $\dagger$

| FI | M: $6 \%$ | M: $38 \%$ | M: $44 \%$ | F: $56 \%$ |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $(-10,22)$ | $(21,55)$ | $(40,48)$ | $(52,60)$ |  |  |  |  |  |  |  |
|  | F: $42 \%$ | F: $11 \%$ | F: $53 \%$ | F: $47 \%$ |  |  |  |  |  |  |  |
|  | $(28,55)$ | $(-3,25)$ | $(50,55)$ | $(45,50)$ |  |  |  |  |  |  |  |
|  | BMI | M: $41 \%$ | M: $25 \%$ | M: $66 \%$ | M: $34 \%$ | M: 0.61 | M: 0.01 | M: 0.19 | M: 0.05 | M: $78 \%$ | M: $3 \%$ |
|  | $(28,55)$ | $(11,39)$ | $(64,68)$ | $(32,36)$ | $(-0.34,1.56)$ | $(-0.36,0.38)$ | $(0.14,0.23)$ | $(0.01,0.10)$ | $(-8,165)$ | $(-88,94)$ | $(65,97)$ |
|  | F: $56 \%$ | F: $13 \%$ | F: $69 \%$ | F: $31 \%$ | F: 0.48 | F: -0.64 | F: 0.26 | F: 0.06 | F: $130 \%$ | F: $-43 \%$ | F: $87 \%$ |
|  | $(44,67)$ | $(2,25)$ | $(67,71)$ | $(29,33)$ | $(0.28,0.68)$ | $(-1.71,0.43)$ | $(0.22,0.29)$ | $(0.02,0.10)$ | $(76,184)$ | $(-99,13)$ | $(78,95)$ |
|  |  | $(5,22)$ |  |  |  |  |  |  |  |  |  |

ACE bivariate model between FI and education *

| FI | $\begin{aligned} & \mathrm{M}: 63 \% \\ & (52,73) \end{aligned}$ | $\begin{aligned} & \mathrm{M}:-19 \% \\ & (-27,-10) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 63 \% \\ & (52,73) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 56 \% \\ & (52,59) \end{aligned}$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { F: } 58 \% \\ & (49,66) \end{aligned}$ | $\begin{aligned} & \mathrm{F}:-5 \% \\ & (-12,2) \end{aligned}$ | $\begin{aligned} & \text { F: } 58 \% \\ & (49,66) \end{aligned}$ | $\begin{aligned} & \text { F: } 47 \% \\ & (45,50) \end{aligned}$ |  |  |  |  |  |  |  |  |
| Education | $\begin{aligned} & \text { M: 41\% } \\ & (34,48) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 24 \% \\ & (18,30) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 41 \% \\ & (34,48) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 35 \% \\ & (32,37) \end{aligned}$ | $\begin{gathered} \text { M: } 0.05 \\ (-0.08,0.17) \end{gathered}$ | M: N/A* | $\begin{gathered} \text { M: } 0.05 \\ (-0.08,0.17) \end{gathered}$ | $\begin{gathered} \mathrm{M}:-0.07 \\ (-0.11,0.02) \end{gathered}$ | $\begin{aligned} & \mathrm{M}:-24 \% \\ & (-91,43) \end{aligned}$ | $\begin{aligned} & \text { M: 92\% } \\ & (36,148) \end{aligned}$ | $\begin{aligned} & \mathrm{M}:-24 \% \\ & (-91,43) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 32 \% \\ & (11,53) \end{aligned}$ |
|  | $\begin{aligned} & \text { F: } 36 \% \\ & (29,42) \end{aligned}$ | $\begin{aligned} & \text { F: } 28 \% \\ & (23,34) \end{aligned}$ | $\begin{aligned} & \text { F: 36\% } \\ & (29,42) \end{aligned}$ | $\begin{aligned} & \text { F: 36\% } \\ & (34,38) \end{aligned}$ | $\begin{gathered} \text { F: }-0.02 \\ (-0.13,0.10) \end{gathered}$ | F: N/A* | $\begin{gathered} \text { F: }-0.02 \\ (-0.13,0.10) \end{gathered}$ | $\begin{gathered} \text { F: }-0.01 \\ (-0.05,0.03) \end{gathered}$ | $\begin{aligned} & \text { F: } 11 \% \\ & (-58,79) \end{aligned}$ | $\begin{gathered} \text { F: } 84 \% \\ (26,142) \end{gathered}$ | $\begin{aligned} & \text { F: } 11 \% \\ & (-58,79) \end{aligned}$ | $\begin{gathered} \text { F: 5\% } \\ (-16,27) \end{gathered}$ |

ADE bivariate model between FI and education $\ddagger$

| FI | $\begin{gathered} \text { M: } 6 \% \\ (-10,22) \end{gathered}$ | $\begin{aligned} & \mathrm{M}: 38 \% \\ & (20,55) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 44 \% \\ & (41,48) \end{aligned}$ | $\begin{aligned} & \text { M: 56\% } \\ & (52,59) \end{aligned}$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { F: } 42 \% \\ & (29,56) \end{aligned}$ | $\begin{aligned} & \text { F: } 10 \% \\ & (-4,24) \end{aligned}$ | $\begin{aligned} & \text { F: } 53 \% \\ & (50,55) \end{aligned}$ | $\begin{aligned} & \mathrm{F}: 47 \% \\ & (45,50) \end{aligned}$ |  |  |  |  |  |  |  |  |
| Education | $\begin{aligned} & \text { M: } 114 \% \\ & (102,125) \end{aligned}$ | $\begin{aligned} & \text { M: -48\% } \\ & (-61,-36) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 65 \% \\ & (63,68) \end{aligned}$ | $\begin{aligned} & \text { M: 35\% } \\ & (32,37) \end{aligned}$ | $\begin{gathered} \text { M: -0.89 } \\ (-2.02,0.24) \end{gathered}$ | M: N/A* | $\begin{gathered} \text { M: -0.12 } \\ (-0.17,-0.07) \end{gathered}$ | $\begin{gathered} \text { M: -0.07 } \\ (-0.11,-0.02) \end{gathered}$ | $\begin{aligned} & \text { M: 252\% } \\ & (146,358) \end{aligned}$ | $\begin{aligned} & \mathrm{M}:-184 \% \\ & (-297,-72) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 68 \% \\ & (47,89) \end{aligned}$ | $\begin{aligned} & \mathrm{M}: 32 \% \\ & (11,53) \end{aligned}$ |
|  | $\begin{aligned} & \text { F: } 121 \% \\ & (111,131) \end{aligned}$ | $\begin{aligned} & \text { F: }-57 \% \\ & (-67,-46) \\ & \hline \end{aligned}$ | $\begin{aligned} & \text { F: 64\% } \\ & (62,66) \end{aligned}$ | $\begin{aligned} & \text { F: } 36 \% \\ & (34,38) \end{aligned}$ | $\begin{gathered} \text { F: }-0.28 \\ (-0.41,-0.15) \\ \hline \end{gathered}$ | F: N/A* | $\begin{gathered} \text { F: }-0.12 \\ (-0.16,-0.09) \end{gathered}$ | $\begin{gathered} \text { F: }-0.01 \\ (-0.05,0.03) \\ \hline \end{gathered}$ | $\begin{aligned} & \text { F: } 262 \% \\ & (152,372) \\ & \hline \end{aligned}$ | $\begin{gathered} \text { F: -168\% } \\ (-283,-52) \end{gathered}$ | $\begin{gathered} \text { F: 95\% } \\ (73,116) \\ \hline \end{gathered}$ | $\begin{gathered} \text { F: } 5 \% \\ (-16,27) \\ \hline \end{gathered}$ |

Note: BMI, body mass index; FI, frailty index; CI, Wald-type confidence interval; A, additive genetic factors; D, dominance genetic factors; $H$, total genetic factors/ broad-sense heritability; $C$, common environmental factors; $E$, unique environmental factors; $r$, correlation between variance components. $M$ and $F$ represents parameter estimates for men and women respectively. Bivariate heritability is the proportion of phenotypic correlation explained by genetic and environmental factors. Variance component estimates are allowed to be negative in the "direct symmetric approach" (Verhulst et al. 2019).

* Correlation between C or D components were not defined when the variance components are negative.
$\dagger$ The same conclusion can be drawn from either the ACE and ADE bivariate models between FI and BMI , in which there is a modest genetic correlation ( $r_{\mathrm{H}}$ ) between FI and BMI , and their phenotypic correlation is mostly explained by genetic factors (bivariate H).
$\ddagger$ Although both ACE and ADE bivariate models have the same model fit when allowing for negative variances, the ACE bivariate model is more in line with the observed cross-twin cross-trait correlations (MZ twins: -0.07 ; DZ twins: -0.08 , shown in Table 2) that the phenotypic correlation between Fl and education is largely explained by common environmental factors (bivariate $\mathrm{C}=92 \%$ in men and $84 \%$ in women, slightly more than $65 \%$ and $74 \%$ using the standard approach). In contrast, the solution in the ADE bivariate model yielded a highly negative and non-sensical D component, and it causes all the common environmental influences on the covariance going to genetic factors - a result not in line with the standard interpretations of the observed cross-twin cross-trait correlations.


## Supplementary Methods

## INTRODUCTION

In this appendix we outline an approach to estimating the genetic correlation between males and females for a phenotype which has genetic contributions both from additive and dominance deviations to its variance. 1 . Using the biometric model in a simplified two-allelic locus with equal allele frequencies, we will derive the resulting correlation between genetic contributions in males and females with different additive and dominance deviation contributions genotypic
expression. 2. We then show that the resulting correlation depends on allele frequencies. 3. Finally, we suggest an intuitive solution for estimation of the genetic correlation between males and females, and compare its performance with other possible solutions in a series of simulations.

As outlined below, our suggested model for the covariance between twins in opposite sexed DZ pairs is

$$
\begin{align*}
& \operatorname{Cov}\left(\left[\begin{array}{l}
Y_{1} \\
Y_{2}
\end{array}\right]\right)_{o s D Z} \\
& =\left[\begin{array}{cc}
\sigma_{A f}^{2}+\sigma_{D f}^{2}+\sigma_{E f}^{2} & r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}+0.25 \sigma_{A f} \sigma_{D m}+0.25 \sigma_{D f} \sigma_{A m}\right) \\
r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}+0.25 \sigma_{A f} \sigma_{D m}+0.25 \sigma_{D f} \sigma_{A m}\right) & \sigma_{A m}^{2}+\sigma_{D m}^{2}+\sigma_{E m}^{2}
\end{array}\right. \tag{1}
\end{align*}
$$

where $\sigma_{X}^{2}$ represent contributions to variance and covariance from source $X . X$ are $A$, additive genetic contributions, $D$, dominant genetic contributions, and $E$, individually unique contributions. The sub-indexes are also complemented with $f$ and $m$ to indicate female and male sources. Below we show that this model, although not uniformly unbiased, has some features which makes it suitable for situations where additive and dominance contributions to variance of the phenotype exists in both sexes (possibly in different proportions).

## Derivation of correlation due to genetics from biometric model

Following the set-up of the biometric model in Neale and Maes [1] we define one autosomal locus having allele $A$ and $a$ at equal $1 / 2$ frequencies in a population. We define the genotypic effect on $Y$ to be $-d$ for allele combination $a a, h$ for allele combination $A a$, and $d$ for allele combination $A A$ (see Supplementary Figure 7). Note that the definition of genotypic effect is somewhat arbitrary, see e.g. Neale and Maes [1].


Supplementary Figure 7. Graphical representation of the genotypic effect. (Adapted from Neale and Maes [1]).

Here $h$ indicates the deviation from additivity; we assume $h$ to be bounded between $-d$ and $d$ to keep a biologically feasible interpretation of additivity $v s$ dominance/recessiveness. The $1 / 2$ frequencies means that a random individual has a $1 / 4$ probability of having
allele combination $a a$, a $1 / 2$ probability of having $A a$, and a $1 / 4$ probability of having $A A$. The mean genotypic contribution can be written as (using the law of total expectation).

$$
\begin{equation*}
\mu_{Y}=E(Y)=E(Y \mid a a) \operatorname{Pr}(a a)+E(Y \mid A a) \operatorname{Pr}(A a)+E(Y \mid A A) \operatorname{Pr}(A A)=-d \cdot \frac{1}{4}+h \cdot \frac{1}{2}+d \cdot \frac{1}{4}=\frac{1}{2} h . \tag{2}
\end{equation*}
$$

The variance can be calculated as

$$
\begin{align*}
\operatorname{Var}(Y)=E((Y & \left.-E(Y))^{2}\right)=E\left(Y^{2}\right)-E(Y)^{2} \\
& =E\left(Y^{2} \mid a a\right) \operatorname{Pr}(a a)+E\left(Y^{2} \mid A a\right) \operatorname{Pr}(A a)+E\left(Y^{2} \mid A A\right) \operatorname{Pr}(A A)-\left(\frac{1}{2} h\right)^{2}  \tag{3}\\
& =(-d)^{2} \cdot \frac{1}{4}+h^{2} \cdot \frac{1}{2}+d^{2} \cdot \frac{1}{4}-\frac{1}{4} h^{2}=\frac{1}{2} d^{2}+\frac{1}{4} h^{2} .
\end{align*}
$$

Now, let the same locus contribute to two phenotypes, $Y_{1}$ and $Y_{2}$ (e.g., same phenotype in males and females), possibly with different additivity and dominance deviation. Define the genotypic effects to be $\left\{-d_{1}, h_{1}\right.$, $\left.d_{1}\right\}$ and $\left\{-d_{2}, h_{2}, d_{2}\right\}$ for $Y_{1}$ and $Y_{2}$, respectively. Using
the frequencies of allele combination in full siblings (or DZ twins), following Neale and Maes [1], we can create a table indicating the contributions to the covariance from each combination of allele in the two siblings (Supplementary Table 11).

Supplementary Table 11. Contributions to covariance, and expected frequency, between two DZ twins.

| Sibling 1 <br> alleles | Sibling 2 <br> alleles | Genotypic effect <br> minus mean, <br> sibling 1 | Genotypic effect <br> minus mean, <br> sibling 2 | Contribution to covariance | Frequency |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $A A$ | $A A$ | $d_{1}-\frac{1}{2} h_{1}$ | $d_{2}-\frac{1}{2} h_{2}$ | $d_{1} d_{2}-\frac{1}{2} d_{1} h_{2}-\frac{1}{2} h_{1} d_{2}+\frac{1}{4} h_{1} h_{2}$ | $\frac{9}{64}$ |
| $A A$ | $A a$ | $d_{1}-\frac{1}{2} h_{1}$ | $\frac{1}{2} h_{2}$ | $\frac{1}{2} d_{1} h_{2}-\frac{1}{4} h_{1} h_{2}$ | $\frac{6}{64}$ |
| $A A$ | $a a$ | $d_{1}-\frac{1}{2} h_{1}$ | $-d_{2}-\frac{1}{2} h_{2}$ | $-d_{1} d_{2}-\frac{1}{2} d_{1} h_{2}+\frac{1}{2} h_{1} d_{2}+\frac{1}{4} h_{1} h_{2}$ | $\frac{1}{64}$ |
| $A a$ | $A A$ | $\frac{1}{2} h_{1}$ | $d_{2}-\frac{1}{2} h_{2}$ | $\frac{1}{2} h_{1} d_{2}-\frac{1}{4} h_{1} h_{2}$ | $\frac{6}{64}$ |
| $A a$ | $A a$ | $\frac{1}{2} h_{1}$ | $\frac{1}{2} h_{2}$ | $\frac{1}{4} h_{1} h_{2}$ | $\frac{20}{64}$ |
| $A a$ | $a a$ | $\frac{1}{2} h_{1}$ | $-d_{2}-\frac{1}{2} h_{2}$ | $-\frac{1}{2} h_{1} d_{2}-\frac{1}{4} h_{1} h_{2}$ | $\frac{6}{64}$ |
| $a a$ | $A A$ | $-d_{1}-\frac{1}{2} h_{1}$ | $d_{2}-\frac{1}{2} h_{2}$ | $-d_{1} d_{2}+\frac{1}{2} d_{1} h_{2}-\frac{1}{2} h_{1} d_{2}+\frac{1}{4} h_{1} h_{2}$ | $\frac{1}{64}$ |
| $a a$ | $A a$ | $-d_{1}-\frac{1}{2} h_{1}$ | $\frac{1}{2} h_{2}$ | $-\frac{1}{2} d_{1} h_{2}-\frac{1}{4} h_{1} h_{2}$ | $\frac{6}{64}$ |
| $a a$ | $a a$ | $-d_{1}-\frac{1}{2} h_{1}$ | $-d_{2}-\frac{1}{2} h_{2}$ | $d_{1} d_{2}+\frac{1}{2} d_{1} h_{2}+\frac{1}{2} h_{1} d_{2}+\frac{1}{4} h_{1} h_{2}$ | $\frac{9}{64}$ |

We can thus calculate the contribution to covariance from this locus between phenotypes and between DZ twins as

$$
\begin{align*}
& \operatorname{Cov}\left(Y_{1}, Y_{2}\right)=\sum E\left(\left(Y_{1}-\mu_{Y_{1}}\right)\left(Y_{2}-\mu_{Y_{2}}\right)\right) \\
& =\sum E\left(\left(Y_{1}-\mu_{Y_{1}}\right)\left(Y_{2}-\mu_{Y_{2}}\right) \mid \text { allelic combination }\right) \operatorname{Pr}(\text { allelic combination })= \\
& =\frac{9}{64}\left(d_{1} d_{2}-\frac{1}{2} d_{1} h_{2}-\frac{1}{2} h_{1} d_{2}+\frac{1}{4} h_{1} h_{2}\right)+\frac{6}{64}\left(\frac{1}{2} d_{1} h_{2}-\frac{1}{4} h_{1} h_{2}\right) \\
& +\frac{1}{64}\left(-d_{1} d_{2}-\frac{1}{2} d_{1} h_{2}+\frac{1}{2} h_{1} d_{2}+\frac{1}{4} h_{1} h_{2}\right)+\frac{6}{64}\left(\frac{1}{2} h_{1} d_{2}-\frac{1}{4} h_{1} h_{2}\right)+\frac{20}{64}\left(\frac{1}{4} h_{1} h_{2}\right) \\
& +\frac{6}{64}\left(-\frac{1}{2} h_{1} d_{2}-\frac{1}{4} h_{1} h_{2}\right)+\frac{1}{64}\left(-d_{1} d_{2}+\frac{1}{2} d_{1} h_{2}-\frac{1}{2} h_{1} d_{2}+\frac{1}{4} h_{1} h_{2}\right) \\
& +\frac{6}{64}\left(-\frac{1}{2} d_{1} h_{2}-\frac{1}{4} h_{1} h_{2}\right)+\frac{9}{64}\left(d_{1} d_{2}+\frac{1}{2} d_{1} h_{2}+\frac{1}{2} h_{1} d_{2}+\frac{1}{4} h_{1} h_{2}\right) \\
& =\frac{1}{64}(9-1-1+9) d_{1} d_{2}+\frac{1}{64}\left(-\frac{9}{2}+\frac{6}{2}-\frac{1}{2}+\frac{1}{2}-\frac{6}{2}+\frac{9}{2}\right) d_{1} h_{2} \\
& +\frac{1}{64}\left(-\frac{9}{2}+\frac{1}{2}+\frac{6}{2}-\frac{6}{2}-\frac{1}{2}+\frac{9}{2}\right) h_{1} d_{2}+\frac{1}{64}\left(\frac{9}{4}-\frac{6}{4}+\frac{1}{4}-\frac{6}{4}+\frac{20}{4}-\frac{6}{4}+\frac{1}{4}-\frac{6}{4}+\frac{9}{4}\right) h_{1} h_{2} \\
& =\frac{1}{64} \cdot 16 \cdot d_{1} d_{2}+0 \cdot d_{1} h_{2}+0 \cdot h_{1} d_{2}+\frac{1}{64} \cdot \frac{16}{4} \cdot h_{1} h_{2}=\frac{1}{4} d_{1} d_{2}+\frac{1}{16} h_{1} h_{2} \tag{4}
\end{align*}
$$

And thus, the expected correlation in this locus is

$$
\begin{equation*}
\operatorname{Cor}\left(Y_{1}, Y_{2}\right)=\frac{\operatorname{Cov}\left(Y_{1}, Y_{2}\right)}{\sqrt{\operatorname{Var}\left(Y_{1}\right)} \sqrt{\operatorname{Var}\left(Y_{2}\right)}}=\frac{\frac{1}{4} d_{1} d_{2}+\frac{1}{16} h_{1} h_{2}}{\sqrt{\frac{1}{2} d_{1}^{2}+\frac{1}{4} h_{1}^{2}} \sqrt{\frac{1}{2} d_{2}^{2}+\frac{1}{4} h_{2}^{2}}} \tag{5}
\end{equation*}
$$

We may investigate how the correlation will depend on dominance deviations by varying the $h$ 's between + and - the $d$ 's. In Supplementary Figure 8 we have plotted expected correlations over varying degrees of
dominance deviations in the two genotypic effect for the different phenotypes, the $d$ 's have value 1 . An assumption is that $d_{1}$ and $d_{2}$ have same sign, thus the correlation is positive.


Supplementary Figure 8. Contour plot of deviations from additivity, when $h$ 's are at $\pm 1$ there is maximal dominance deviation.

From the derivation and plot we may notice several things: 1. When one genotypic effect is at maximum dominance, and the other at perfect additivity, the correlation is $\frac{1}{\sqrt{6}} \approx 0.4082$. 2. When both genotypic effects have maximum deviation, in the same $\pm$ direction, the correlation is $\frac{5}{12} \approx 0.4167$. 3. When both genotypic effects are purely additive the correlation is 0.5 . 4. When the genotypic effects are at maximum deviation, but in opposite $\pm$ direction, the correlation is 0.25 .

Thus, the contribution to correlation between two phenotypes in different DZ twins depends on the amount and direction (i.e., dominance or recessiveness) of dominance deviation.

## The correlation depends on the allele frequencies

If we want to expand on previous simplified equal allele frequency and allow any allele frequency, we quickly generate a complex expression. Therefore, we set up a simulation with a larger number of alleles and a large number of DZ twins, where we vary the dominance deviations, to assess the impact of varying allele frequencies.

We simulated 100,000 DZ pairs and 100 assumed contributing loci under different scenarios. In all
scenarios we assumed that the sign and maximal genotypic effect were the same for both phenotypes. Additional assumptions were non-assortative mating (i.e., parents were treated as two random individuals in the population), no association between minor allele frequency (MAF) and genotypic effect, no interactions between loci, and no interactions with any 'environmental' (i.e., non-genetic) variable. The genotypic effects were drawn randomly from a standard normal distribution. Each scenario is based on different MAF;

1. $\mathrm{MAF}=0.5$ for all loci.
2. MAF drawn from a uniform distribution between 0 and 0.5.
3. MAF drawn from a uniform distribution between 0 and 0.1.
4. MAF drawn from a random distribution between 0 and 0.5 with an 'L'-shape (a situation with MAF pushed towards 0 but still covering the full range).

The MAF distribution in point 4 is presented in Supplementary Figure 9, and was found through

$$
\begin{equation*}
M A F=\frac{e^{U^{2}}-1}{2\left(e^{0.25}-1\right)}, \text { where } U \sim \operatorname{Uniform}(0, .5) \tag{6}
\end{equation*}
$$



## Supplementary Figure 9. A specific scenario for minor allele frequency distribution.

From the each of the four simulations with different MAF distributions we produce three separate series of estimates over varying dominance deviation: scenario A, varying degree of dominance deviation in one phenotype, and fixed additive genotypic effect in other phenotype, scenario $B$, varying degree of dominance deviation in one phenotype, and maximal dominance deviation genotypic effect in other, and Scenario C, varying dominance deviation vs maximal recessive
deviance. Note that dominance in the minor allele corresponds to recessiveness in the major allele, and vice versa. These simulations serve to investigate the impact of MAF on correlation due to genetic effects between DZ twins (and full siblings) in the scenario where genotypic expression with regard to dominance deviations differ between the twins, results are presented in Supplementary Figure 10.


Supplementary Figure 10. Simulated correlation (y-axis) due to genetics with different MAF, and where one phenotype's genotypic effect varies in dominance deviation (the $h$ as proportion of $d$; $x$-axis) while the other's is fixed as purely additive or with maximal dominance or recessive deviation. Negative values indicate that the minor allele is recessive, positive that it is dominant.

We observe allelic frequency affect in all simulated correlations except where both individual's genotypic expression is completely additive (where the correlation between individuals is 0.5 for all MAF distributions). Further, we can see that scenario $A$ has a higher correlation than scenario B and C, except for when the dominance deviation goes towards its extremes, greater/lesser than approximately $\pm 0.8$. This is most clearly seen for Scenario B, where the minor allele is recessive.

In reality, we would not have any way of knowing the MAF distributions for contributing loci, nor would we know the dominance deviations (which would vary between loci).

## Suggested intuitive solution

We suggest that estimation of genetic correlation based on twin data based on an intuitive solution. We have observed that correlating a phenotype with varying dominance deviation between twins will produce a resulting correlation which lies between pure additivity
(i.e., correlation $=0.5$ ) and maximal dominance deviation for either the major or minor allele (varying resulting correlation depending on MAF) - except for when the dominance deviations are nearing its maxima or minima. Hence, if the classic twin model correctly captures the additive genetic effects $(A)$ and dominance deviations ( $D$ ) for each trait separately, we can suggest an intuitive modeling approach to estimate the genetic correlation between the two which relies on placing the resulting correlation in between that of $A$ and $D$ alone.

## Expected genetic correlation

To be able to assess the performance of an estimating procedure of the genetic correlation we need to know the genetic correlation if both phenotypes were expressed in one individual. Since the solution when allele frequencies are unequal quickly become unruly, we simulate this is a similar fashion as in Section 2 above, using the same 'L'-shaped MAF. We simulated using 100,000 individuals per each combination of values from -1 to 1 by steps of 0.1 - in Supplementary Figure 11 the result is presented.


Supplementary Figure 11. Simulation for estimating genetic correlation. The contour plot shows resulting genetic correlation under different amounts of dominance deviation (positive) and recessive deviations (negative) for the minor allele.

We can observe that produced correlations deviate from 1 as the dominance deviations (or recessive ditto) moves away from 0 differently in the two phenotype's genotypic effects. The genetic correlation becomes lowest when one phenotype has more dominance deviation for the minor allele and the other has more recessive deviations. We can also see that it matters which of the major or minor allele is more dominant, where the minor allele being dominant is less problematic.

## Suggested estimating procedure

Per the classic twin model - with $A$, without $D$ and $C$ (the 'shared environment' contribution), but with $E$, the individually unique contributions to variance not shared
between individuals (often referred to as an $A E$-model) - we may model the covariance between opposite sexed DZ twins (osDZ) as (see e.g. Neale and Maes [1]; here sub-index ending with $f$ indicated the female twin and sub-index ending with $m$ indicated the male twin):

$$
\operatorname{Cov}\left(\left[\begin{array}{l}
Y_{1}  \tag{7}\\
Y_{2}
\end{array}\right]\right)_{o s D Z}=\left[\begin{array}{cc}
\sigma_{A f}^{2}+\sigma_{E f}^{2} & r_{f m} 0.5 \sigma_{A f} \sigma_{A m} \\
r_{f m} 0.5 \sigma_{A f} \sigma_{A m} & \sigma_{A m}^{2}+\sigma_{E m}^{2}
\end{array}\right]
$$

The model fitting would estimate the $r_{f n}$ as the genetic correlation between males and females, appropriately bounded between -1 and 1 . A direct translation into situation where the model is an $A D E$ model is

$$
\operatorname{Cov}\left(\left[\begin{array}{l}
Y_{1}  \tag{8}\\
Y_{2}
\end{array}\right]\right)_{o s D Z}=\left[\begin{array}{cc}
\sigma_{A f}^{2}+\sigma_{D f}^{2}+\sigma_{E f}^{2} & r_{f m} 0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m} \\
r_{f m} 0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m} & \sigma_{A m}^{2}+\sigma_{D m}^{2}+\sigma_{E m}^{2}
\end{array}\right]
$$

However, in this setup the estimated genetic correlation is not allowing $D$ to contribute to estimation of $r_{f m}$. A natural expansion with the inclusion of $D$ is

$$
\operatorname{Cov}\left(\left[\begin{array}{l}
Y_{1}  \tag{9}\\
Y_{2}
\end{array}\right]\right)_{o s D Z}=\left[\begin{array}{cc}
\sigma_{A f}^{2}+\sigma_{D f}^{2}+\sigma_{E f}^{2} & r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}\right) \\
r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}\right) & \sigma_{A m}^{2}+\sigma_{D m}^{2}+\sigma_{E m}^{2}
\end{array}\right]
$$

The assumption implicitly encoded here is that the same subset of loci having dominance deviations in one sex's genotypic expression also has dominance deviation expression in the other sex, while additive effects in one sex does not correlate with dominance deviations in the other sex. As shown above, if we deviate from this assumption, we will have different resulting correlations due to genetic effects. As an extreme example, from a twin modelling view-point, suppose the female trait has an estimated $0 A$ contribution according to the model
and some $D$ contribution, while the male has only $A$ contribution and no $D$; the result would be that there's no way the model could ascribe any correlation between sexes to genetics (and the modelled $r_{f m}$ would take on any value between -1 and 1 with equal likelihood). This is obviously not appropriate, since the same locus could contribute in a pure additive way for one sex's phenotype and a dominant way for the other sex's phenotype. We therefore suggest that the correlation can be modelled as (note, same equation as in Introduction)

$$
\operatorname{Cov}\left(\left[\begin{array}{l}
Y_{1} \\
Y_{2}
\end{array}\right]\right)_{o s D Z}=
$$

$$
\left[\begin{array}{cc}
\sigma_{A f}^{2}+\sigma_{D f}^{2}+\sigma_{E f}^{2} & r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}+0.25 \sigma_{A f} \sigma_{D m}+0.25 \sigma_{D f} \sigma_{A m}\right)  \tag{1}\\
r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}+0.25 \sigma_{A f} \sigma_{D m}+0.25 \sigma_{D f} \sigma_{A m}\right) & \sigma_{A m}^{2}+\sigma_{D m}^{2}+\sigma_{E m}^{2}
\end{array}\right]
$$

This suggestion is based on the observed simulated correlations behavior towards the extremes of the dominance deviation (Supplementary Figure 10), where correlation due to genetics between DZ twins seem to be most affected by differences in dominance deviations. Not allowing genetics to contribute to the correlation across individuals $A$ and $D$ sources, may cause bias; and, towards the extremes, the correlation between additive and dominant/recessive genetic effects resemble that of dominance-to-dominance correlation behavior (although, not an exact correspondence between the two). As such, we expect the performance of the estimating procedure to be most suitable for scenarios where the $A$ and $D$ contributions to phenotypic variance differ considerable between males and females.

To investigate the performance of this suggested modelling approach we performed a series of simulations. For each simulation we used the above approach of simulating parental alleles and drawing offspring alleles, and then we created same sexed MZ and DZ twin pairs in addition to the opposite sexed DZ pairs. We assumed 7000 pairs for each sex-zygosity
combination. Additionally, we estimated the resulting genetic correlation, to be able to compare the produced correlation with. We added an individually unique variation (the $E$ ), drawn from a random normal distribution with the same variance as the simulated genetic variance separately by sex, and used the classic twin methodology with sex-limitation models to the data. We fitted the models using equations (1) (our suggestion), (9), (8), and (7), to provide an overall picture of the performance of different approaches. We a. investigated the full range of dominance deviations (all combinations of the $h$ 's between -1 and 1 by 0.25 steps), b. investigated the situation where one phenotype is additive and the other has dominance deviations (the $h_{1}$ in -1.0 to -0.8 and 0.8 to 1.0 in 0.05 steps, the $h_{2}$ fixed at 0 ), and c. did a more thorough investigation on the extreme values (the $h_{1}$ in -1.0 to -0.8 and $h_{2}$ in 1.0 to 0.8 in 0.05 steps) - for each combination the simulation was run 10 times. In the simulation we used the same 'L'-shaped MAF as above. In Supplementary Figures $12 \mathrm{a}, 12 \mathrm{~b}$, and 12 c the results of these three sets of simulations are shown. We plot the difference between estimated $r_{f m}$ and calculated true $r_{G}$ as an estimate of bias in the separate estimating approaches.

A





B









Supplementary Figure 12. Performance of different estimation procedures in a simulation. A locally smoothed polynomial regression line is fitted to each scenario (using 'loess' function in $R$ ). (A) Full range of dominance deviations. (B) Dominance deviations versus additive. (C) Dominance deviations towards extreme.

We summarize the behavior of the four different estimating approaches in Supplementary Table 12. We observe the following features of the four different estimating approaches:

1. Neither estimating approach has as good performance throughout the dominance deviation range.
2. Our suggested estimating approach has best performance in the most extreme scenarios.
3. Our suggested estimating approach has a negative bias for most scenarios, and only slightly positive
bias when dominance deviations are towards the very extremes.
4. All standard estimating approach (i.e., the three simulated estimating approach except our suggestion) generally has a upwards bias, towards 1.0.
5. The modelling approach of the $A E$-model perform better than other estimating approach, except for the very extremes, with regard to bias (low mean squared error) but precision may be overestimated, i.e. too low standard errors (with relatively lower coverage probability compared with standard approaches).

Supplementary Table 12. Performance over different scenarios for the investigated estimating procedures.

|  | a. Full range of dominance deviations | b. Dominance deviations versus additive | c. Dominance deviations towards extreme |
| :---: | :---: | :---: | :---: |
| Mean squared error |  |  |  |
| $r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}+0.25 \sigma_{A f} \sigma_{D m}+0.25 \sigma_{D f} \sigma_{A m}\right)$ | 0.029 | 0.015 | 0.003 |
| $r_{f m} 0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}$ | 0.016 | 0.020 | 0.038 |
| $r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}\right)$ | 0.020 | 0.021 | 0.063 |
| $r_{f m} 0.5 \sigma_{A f} \sigma_{A m}$ from $A E$-model | 0.007 | 0.002 | 0.021 |
| Mean error |  |  |  |
| $r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}+0.25 \sigma_{A f} \sigma_{D m}+0.25 \sigma_{D f} \sigma_{A m}\right)$ | -0.126 | -0.103 | 0.024 |
| $r_{f m} 0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}$ | 0.074 | 0.100 | 0.178 |
| $r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}\right)$ | 0.086 | 0.105 | 0.242 |
| $r_{f m} 0.5 \sigma_{A f} \sigma_{A m}$ from $A E$-model | -0.001 | 0.001 | 0.134 |
| Proportion negative bias |  |  |  |
| $r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}+0.25 \sigma_{A f} \sigma_{D m}+0.25 \sigma_{D f} \sigma_{A m}\right)$ | 0.872 | 0.935 | 0.318 |
| $r_{f m} 0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}$ | 0.234 | 0.112 | 0.008 |
| $r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}\right)$ | 0.229 | 0.096 | 0.000 |
| $r_{f m} 0.5 \sigma_{A f} \sigma_{A m}$ from $A E$-model | 0.499 | 0.463 | 0.000 |
| Coverage probability |  |  |  |
| $r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}+0.25 \sigma_{A f} \sigma_{D m}+0.25 \sigma_{D f} \sigma_{A m}\right)$ | 0.602 | 0.721 | 0.895 |
| $r_{f m} 0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}$ | 0.862 | 0.895 | 0.448 |
| $r_{f m}\left(0.5 \sigma_{A f} \sigma_{A m}+0.25 \sigma_{D f} \sigma_{D m}\right)$ | 0.755 | 0.841 | 0.054 |
| $r_{f m} 0.5 \sigma_{A f} \sigma_{A m}$ from $A E$-model | 0.768 | 0.965 | 0.192 |

## CONCLUSIONS

In a scenario with diverging dominance and additive contributions to phenotypic variance in males and females using the classic twin model, the standard estimating approaches has the feature that they overestimate the genetic correlation between males and females (which we here call $r_{f m}$ ). Thus, even if there is a genetic correlation lower than 1.0 the estimating approaches will have a lower likelihood of detecting it since they are biased upwards. In contrast, using our suggested approach will produce an estimate which, if it is biased at all, will be biased downwards. Therefore, if a model fitted with our estimating approach produces a
$r_{f m}$ which is not statistically significant, it is likely a true null finding. Additionally, if fitting an $A E$-model is not appropriate (e.g., due to poor model fit), our suggested estimating approach has a lower mean squared error than standard estimating approach in extreme scenarios (with a larger proportion of negative bias).

## REFERENCE

1. Neale M, Maes HH. Methodology for genetic studies of twins and families. Secondary Methodology for genetic studies of twins and families. http://ibgwww.colorado.edu/workshop2006/cdrom/H TML/book2004a.pdf
